

Tram Le

Homework 3:

1. $n = 1000$, $p = .1$

- a) Expected value: $E[X] = n * p = 1000 * .1 = 100$
- b) Variance value: $Var[X] = n * p * (1 - p) = 1000 * .1 * (1 - .1) = 90$
Standard deviation: $Sd(X) = \sqrt{Var(X)} = \sqrt{90} = 9.49$
- c) Probability at most 100 patients: $P(X \leq 100)$
 $pbinom(100, n, p) = pbinom(100, 1000, .1) = .53$
- d) Normal approximate:
 $P(X \leq 100): pnorm(100, mean, sd, lower.tail = TRUE) = 0.5$ (Because Z value is less than or equal to 0 in Z table)

2. $N = 12 + 8 = 20$; $n(\text{size numbers of trials}) = 5$; $x(\text{number of success}) = 5$,

- a) Probability success on single trial of red balls: $p = 12/20 = 0.6$.
 $P(X=5): dbinom(x, n, p) = 0.07776$
- b) Expected value: $E[X] = n * p = 5 * .6 = 3$
- c) Standard deviation: $sd(X) = \sqrt{np(1-p)} = 1.1$

3. mean = 100; sd = 15. Standard normal distribution: $P(Z \leq (x - \text{mean})/sd)$ or $P(Z \geq (x - \text{mean})/sd)$

- a) $IQ < 120$: $pnorm(120, mean, sd, lower.tail = TRUE) = 0.908$
- b) $110 < IQ < 130$: $pnorm(130, mean, sd, lower.tail = TRUE) - pnorm(110, mean, sd, lower.tail = FALSE) = 0.724$
- c) $IQ > 140$: $pnorm(140, mean = 100, sd = 15, lower.tail = FALSE) = 0.0038$

4. $k = 5$; $p = .6$

- a) $n = 100,000$
Cal the sum of random geometric values: $sum(rgeom(5, .6))$

```
for(i in 1:n){  
  if (sum(rgeom(5, .6)) < 8)  
    countSum = countSum + 1  
}  
print(countSum)  
>> 94423
```
- b) Ratio of the number of sum < 8 / total number of trial n
 $ratio = countSum / n = 94423 / 100000 = .94423$
- c) Negative binomial distribution with $r = 5$; $p = .6$
 $P(X \leq 7): pnbinom(7, r, p) = .94269$
- d) Negative binomial distribution is approximately equal to the sum of geometric distribution

5.

- a) Population size 1000000

Using `rep()` to generate a population of “Graduate” and “Not Graduate” of 32% and 68% of total population 1000000 then put in a vector.

$g = \text{rep}(c(\text{"Graduate"}, \text{"Not Graduate"}), \text{times} = c(320000, 680000))$

- b) $n = 1000$

Using `sample()` to generate random sample of 1000 out of total population then count the `sample(g, n)`

- c) Count sample success of “Graduate” then find the estimate for proportion of “Graduate”

$\text{count} = \text{sum}(s == \text{"Graduate"})$

$p = \text{count}/n$

- d) 99% \Leftrightarrow 2.58; z value = .99506

Apply formula:

$ma = \text{qnorm}(.99506) * \text{sqrt}(p * (1-p)/n)$

Cal lower and upper of confidence interval:

$low = p - ma$

$high = p + ma$

- e) `install.packages("epitools")`

`library("epitools")`

- f) Cal 99% confidence interval using `binom.approx()`

$\text{binom.approx}(p, n, \text{conf.level} = 0.99)$