

Tram Le

Homework 3:

1. Put all information in vector

- The point estimate $p = \text{\#rotten oranges} / \text{\#total oranges} = 0.1142$
- Expected count based on a $\text{Bin}(10, 0.1142)$. Using binomial probability distribution function to find E: $\text{dbinom}(c(0:10), 10, p)$
- Add all expected value less than 5

Number Rotten	0	1	2	3	4	5 and more
Observed count	334	369	191	63	22	21
Expected count	297.4	383.4	222.4	76.5	17.3	3.0

- Put new value on both counts into vector then Compute χ^2 statistic :
 - $\chi^2 = \sum (\text{Observed Count} - \text{Expected Count})^2 / \text{Expected Count} = 121.14$
- At $\alpha = .05$ compute p-value
 - The degree of freedom is $6 - 1 - 1 = 4$

$$P\text{-value} = P(\chi^2 > 121.14) = 0.0000... < 0.05 \text{ the } \alpha$$

At χ^2 alpha level is 9.49 is way smaller than 121.14 or we could say the P-value is very small than significant level. So we reject H_0 and conclude that there is evidence that rotten oranges do not follow distribution of $\text{Bin}(10, p)$

2. Put all information in matrix with 3 row and 3 column

a. H_0 : Number of years of college a person has completed is independent of location residence

H_a : Number of years of college a person had completed is dependent of location

- Extract data to see Observed matrix

```
[,1] [,2] [,3]
[1,]  15  12   8
[2,]   8  15   9
[3,]   6   8   7
```

- Extract data to see Expected matrix

```
[,1]      [,2]      [,3]
[1,] 11.534091 13.920455  9.545455
[2,] 10.545455 12.727273  8.727273
[3,]  6.920455  8.352273  5.727273
```

- d. Using `chisq.test()` function on both count to see χ^2 statistic

$$\chi^2 = 3.006$$

- e. With `chisq.test()` we can see the $df = 4$ at $\alpha = .05$, then compute χ^2_{α} using `qchisq()`

$$\chi^2_{\alpha} = 9.49$$

- f. P-value ($\chi^2 > 3.006$) = $1 - \text{pchisq}(3.006, df = 4) = 0.56$

- g. Inconclusion, since $p\text{-value} > 0.05$, we fail to reject H_0 and conclude that there is insufficient evidence to support number of years of college a person has completed is related to their location

3.

- On height sample t-test, 95% confidence interval: [67.97, 68.02]. Since $p\text{-value} < 2.2e-16$ is less than significant level < 0.05 , we reject H_0 which means height is not equal to 0

On weight sample t-test, 99% confidence interval: [126.89, 127.27], Since $p\text{-value} < 2.2e-16$ is less than significant level < 0.05 , we reject H_0 which means height is not equal to 0