

=====

Challenge: Automated Market Making

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```
#!/usr/bin/env python3
```

```
"""
```

```
Robust, risk-aware market-maker (ASCII only).
```

```
Outputs submission.csv for the first 3000 timestamps.
```

```
"""
```

```
import sys
```

```
from collections import deque
```

```
import numpy as np
```

```
import pandas as pd
```

```
class AdaptiveMarketMaking:
```

```
    """Core engine."""
```

```
    def __init__(
```

```
        self,
```

```
        tick_size=0.1,
```

```
        lot_size=2,
```

```
        max_inventory=20,
```

```
        ema_half_life=30,          # midprice volatility EMA half-life (rows)
```

```
        flow_window=40,           # recent trade imbalance
```

```
        k_vol=1.2,                 # vol -> half spread
```

```
        base_half=0.15,           # static half-spread cushion
```

```
        k_inv=0.6,                 # inventory in spread
```

```
        inv_skew=1.5,             # inventory skew multiplier
```

```
        flow_skew=1.5,            # flow skew multiplier
```

```
        book_skew=1.5,            # depth-imbalance skew multiplier
```

```
        cool_ticks=2,             # widen filled side
```

```
        cool_steps=3,             # for N rows
```

```
    ):
```

```
        self.tick = tick_size
```

```
        self.lot = lot_size
```

```
        self.max_inv = max_inventory
```

```
        self.vol_alpha = 2.0 / (ema_half_life + 1.0)
```

```
        self.flow_window = flow_window
```

```
        self.k_vol = k_vol
```

```

self.base_half = base_half
self.k_inv = k_inv
self.inv_skew = inv_skew
self.flow_skew = flow_skew
self.book_skew = book_skew

self.cool_ticks = cool_ticks
self.cool_steps = cool_steps

self.reset_simulator()

# ----- helpers -----
def _round_tick(self, p):
    return round(p / self.tick) * self.tick

def _get_row(self, ob_df, ts):
    if ts in ob_df.index:
        return ob_df.loc[ts]
    return ob_df[ob_df["timestamp"] == ts].iloc[0]

# ----- state -----
def reset_simulator(self):
    self.inventory = 0
    self.active_bid = None
    self.active_ask = None
    self.valid_from = None

    self.ema_mid = None
    self.ema_var = None

    self.flow_q = deque(maxlen=self.flow_window)

    self.cool_side = None
    self.cool_left = 0

    self.row_counter = 0

# ----- volatility update -----
def _update_vol(self, mid):
    if self.ema_mid is None:
        self.ema_mid = mid
        self.ema_var = 0.0
        return
    diff = mid - self.ema_mid

```

```

self.ema_mid += self.vol_alpha * diff
self.ema_var = (1.0 - self.vol_alpha) * (self.ema_var + self.vol_alpha * diff * d
iff)

# ----- trade processing -----
def process_trades(self, ts, trades_t):
    if self.valid_from is None or ts < self.valid_from:
        return self.inventory

    filled = False
    if self.active_bid is not None:
        sells = trades_t[trades_t.side == "sell"]
        if not sells.empty and sells.price.max() <= self.active_bid:
            self.inventory += self.lot
            self.active_bid = None
            self.cool_side = "bid"
            self.cool_left = self.cool_steps
            filled = True

    if self.active_ask is not None:
        buys = trades_t[trades_t.side == "buy"]
        if not buys.empty and buys.price.min() >= self.active_ask:
            self.inventory -= self.lot
            self.active_ask = None
            self.cool_side = "ask"
            self.cool_left = self.cool_steps
            filled = True

    if filled:
        self.valid_from = float("inf")
    return self.inventory

# ----- quote builder -----
def _build_quote(self, row, inv, flow_imb):
    # top two levels for book imbalance
    bid1 = row.bid_1_price
    ask1 = row.ask_1_price
    bid1_sz = row.bid_1_size
    ask1_sz = row.ask_1_size

    bid2 = row.bid_2_price
    ask2 = row.ask_2_price
    bid2_sz = row.bid_2_size
    ask2_sz = row.ask_2_size

```

```

depth_bid = bid1_sz + bid2_sz
depth_ask = ask1_sz + ask2_sz
if depth_bid + depth_ask > 0:
    book_imb = (depth_bid - depth_ask) / (depth_bid + depth_ask)
else:
    book_imb = 0.0

mid = (bid1 + ask1) / 2.0
self._update_vol(mid)
sigma = np.sqrt(self.ema_var) if self.ema_var is not None else 0.0

half = max(self.tick,
            self.base_half,
            self.k_vol * sigma,
            self.k_inv * abs(inv) * self.tick)

# inventory + flow + book skew (ticks)
skew_ticks = (
    -self.inv_skew * inv / self.max_inv
    + self.flow_skew * flow_imb
    + self.book_skew * book_imb
)

bid = mid - half + skew_ticks * self.tick
ask = mid + half + skew_ticks * self.tick

# cool-down widens only filled side
if self.cool_left > 0:
    if self.cool_side == "bid":
        bid -= self.cool_ticks * self.tick
    else:
        ask += self.cool_ticks * self.tick

# stay at least one tick from best on that side
bid = min(bid, bid1 - self.tick)
ask = max(ask, ask1 + self.tick)

bid = self._round_tick(bid)
ask = self._round_tick(ask)
if bid >= ask:
    bid -= self.tick
    ask += self.tick
return bid, ask

```

```

# ----- public strategy (checker calls this) -----
def strategy(self, ob_df, tr_df, inventory, ts):
    row = self._get_row(ob_df, ts)
    self.row_counter += 1

    # update flow imbalance
    trades_now = tr_df[tr_df["timestamp"] == ts]
    if not trades_now.empty:
        sign = trades_now.side.map({"buy": 1, "sell": -1})
        self.flow_q.append(sign.mean())
    flow_imb = sum(self.flow_q) / len(self.flow_q) if self.flow_q else 0.0

    bid, ask = self._build_quote(row, inventory, flow_imb)

    # late session flattening
    if self.row_counter > 0.95 * 3000:
        if inventory > 0:
            bid = None
        elif inventory < 0:
            ask = None

    # hard inventory guards
    if inventory >= self.max_inv:
        bid = None
    if inventory <= -self.max_inv:
        ask = None

    # cool-down countdown
    if self.cool_left > 0:
        self.cool_left -= 1
        if self.cool_left == 0:
            self.cool_side = None

    return bid, ask

# ----- back-test helpers -----
def update_quote(self, ts, bid, ask):
    self.active_bid = bid
    self.active_ask = ask
    self.valid_from = ts + 1

def run(self, ob_df, tr_df):
    self.reset_simulator()

```

```

ob_df = ob_df.head(3000).copy()
tr_df = tr_df.head(3000).copy()

ob_df.set_index("timestamp", inplace=True)
tr_groups = tr_df.groupby("timestamp")

quotes = []
for ts in ob_df.index:
    trades_t = tr_groups.get_group(ts) if ts in tr_groups.groups else pd.DataFrame()

    inv = self.process_trades(ts, trades_t)

    bid, ask = self.strategy(ob_df, tr_df, inv, ts)
    self.update_quote(ts, bid, ask)

    quotes.append(
        {
            "timestamp": ts,
            "bid_price": bid if bid is not None else "",
            "ask_price": ask if ask is not None else "",
        }
    )
return pd.DataFrame(quotes)

# ----- alias for checker -----
class AutomatedMarketMaking(AdaptiveMarketMaking):
    pass

# ----- I / O -----
def get_paths():
    if len(sys.argv) >= 3:
        return sys.argv[1], sys.argv[2]
    return input().strip(), input().strip()

if __name__ == "__main__":
    ob_path, tr_path = get_paths()
    ob_df = pd.read_csv(ob_path)
    tr_df = pd.read_csv(tr_path)

    amm = AutomatedMarketMaking(tick_size=0.1, lot_size=2)

```

```
submission = amm.run(ob_df, tr_df)
submission.to_csv("submission.csv", index=False)
```

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Challenge: Exotic Option Pricing using Monte Carlo Simulation

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```
import pandas as pd
import numpy as np
from scipy.stats import norm
from scipy.optimize import brentq
import io

# Calibration Data (ATM Options for Implied Vols)
calib_data = [
    # Stock, Strike, Maturity, Price
    ('DTC', 50, 1, 52.44),
    ('DTC', 50, 2, 54.77),
    ('DTC', 50, 5, 61.23),
    ('DTC', 75, 1, 28.97),
    ('DTC', 75, 2, 33.04),
    ('DTC', 75, 5, 43.47),
    ('DTC', 100, 1, 10.45),
    ('DTC', 100, 2, 16.13),
    ('DTC', 100, 5, 29.14),
    ('DTC', 125, 1, 2.32),
    ('DTC', 125, 2, 6.54),
    ('DTC', 125, 5, 18.82),
    ('DTC', 150, 1, 0.36),
    ('DTC', 150, 2, 2.34),
    ('DTC', 150, 5, 11.89),

    ('DFC', 50, 1, 52.45),
    ('DFC', 50, 2, 54.9),
    ('DFC', 50, 5, 61.87),
    ('DFC', 75, 1, 29.11),
    ('DFC', 75, 2, 33.34),
    ('DFC', 75, 5, 43.99),
    ('DFC', 100, 1, 10.45),
    ('DFC', 100, 2, 16.13),
    ('DFC', 100, 5, 29.14),
    ('DFC', 125, 1, 2.8),
```

```

('DFC', 125, 2, 7.39),
('DFC', 125, 5, 20.15),
('DFC', 150, 1, 1.26),
('DFC', 150, 2, 4.94),
('DFC', 150, 5, 17.46),

('DEC', 50, 1, 52.44),
('DEC', 50, 2, 54.8),
('DEC', 50, 5, 61.42),
('DEC', 75, 1, 29.08),
('DEC', 75, 2, 33.28),
('DEC', 75, 5, 43.88),
('DEC', 100, 1, 10.45),
('DEC', 100, 2, 16.13),
('DEC', 100, 5, 29.14),
('DEC', 125, 1, 1.96),
('DEC', 125, 2, 5.87),
('DEC', 125, 5, 17.74),
('DEC', 150, 1, 0.16),
('DEC', 150, 2, 1.49),
('DEC', 150, 5, 9.7),
]

spot_price = 100
risk_free_rate = 0.05
stocks = ['DTC', 'DFC', 'DEC']

# Correlation matrix
correlations = {
    ('DTC', 'DFC'): 0.75,
    ('DTC', 'DEC'): 0.5,
    ('DFC', 'DEC'): 0.25,
}

corr_matrix = np.ones((3, 3))
for i in range(3):
    for j in range(3):
        if i != j:
            pair = (stocks[i], stocks[j])
            corr_matrix[i, j] = correlations.get(pair, correlations.get((stocks[j], stocks[i]), 1.0))

# Black-Scholes
def bs_call_price(S, K, T, r, sigma):

```



```

    if T == 0 or sigma == 0:
        return max(S - K, 0)
    d1 = (np.log(S / K) + (r + 0.5 * sigma**2)*T) / (sigma * np.sqrt(T))
    d2 = d1 - sigma * np.sqrt(T)
    return S * norm.cdf(d1) - K * np.exp(-r*T) * norm.cdf(d2)

def implied_vol_call(mkt_price, S, K, T, r):
    def objective(sigma):
        return bs_call_price(S, K, T, r, sigma) - mkt_price
    try:
        return brentq(objective, 1e-6, 5)
    except:
        return 0.2 # fallback

# Compute Implied Vols
implied_vols = {}
for stock, K, T, price in calib_data:
    vol = implied_vol_call(price, spot_price, K, T, risk_free_rate)
    implied_vols[(stock, T)] = vol

# GBM Simulator
def simulate_correlated_gbm(S0_vec, r, vols, corr_mat, T, n_steps, n_paths, seed=42):
    np.random.seed(seed)
    dt = T / n_steps
    n_assets = len(S0_vec)
    L = np.linalg.cholesky(corr_mat)
    paths = np.zeros((n_paths, n_steps + 1, n_assets))
    paths[:, 0, :] = S0_vec

    for t in range(1, n_steps + 1):
        Z = np.random.normal(size=(n_paths, n_assets))
        dW = Z @ L.T * np.sqrt(dt)
        for i in range(n_assets):
            paths[:, t, i] = paths[:, t - 1, i] * np.exp((r - 0.5 * vols[i] ** 2) * dt +
vols[i] * dW[:, i])
    return paths

# Basket Knockout Pricer
def price_knockout_basket_option(option_type, strike, maturity, knockout_barrier,
                                spot_vec, vols, corr_mat, r, n_steps=252, n_paths=1000):
    paths = simulate_correlated_gbm(spot_vec, r, vols, corr_mat, maturity, n_steps, n_paths)
    basket_paths = paths.mean(axis=2)
    knocked_out = (basket_paths[:, :-1] > knockout_barrier).any(axis=1)

```

```

final_price = basket_paths[:, -1]

if option_type.lower() == 'call':
    payoffs = np.maximum(final_price - strike, 0)
elif option_type.lower() == 'put':
    payoffs = np.maximum(strike - final_price, 0)
else:
    raise ValueError("Option type must be Call or Put")

payoffs[knocked_out] = 0
discounted_payoff = np.exp(-r * maturity) * payoffs
price = discounted_payoff.mean()
return max(price, 0)

# Helper
def parse_maturity(maturity_str):
    if maturity_str.endswith('y'):
        return float(maturity_str[:-1])
    return float(maturity_str)

# Full Input Data (Id 1 to 36)
input_data = ""Id,Asset,KnockOut,Maturity,Strike,Type
1,Basket,150,2y,50,Call
2,Basket,175,2y,50,Call
3,Basket,200,2y,50,Call
4,Basket,150,5y,50,Call
5,Basket,175,5y,50,Call
6,Basket,200,5y,50,Call
7,Basket,150,2y,100,Call
8,Basket,175,2y,100,Call
9,Basket,200,2y,100,Call
10,Basket,150,5y,100,Call
11,Basket,175,5y,100,Call
12,Basket,200,5y,100,Call
13,Basket,150,2y,125,Call
14,Basket,175,2y,125,Call
15,Basket,200,2y,125,Call
16,Basket,150,5y,125,Call
17,Basket,175,5y,125,Call
18,Basket,200,5y,125,Call
19,Basket,150,2y,75,Put
20,Basket,175,2y,75,Put
21,Basket,200,2y,75,Put
22,Basket,150,5y,75,Put

```

```

23,Basket,175,5y,75,Put
24,Basket,200,5y,75,Put
25,Basket,150,2y,100,Put
26,Basket,175,2y,100,Put
27,Basket,200,2y,100,Put
28,Basket,150,5y,100,Put
29,Basket,175,5y,100,Put
30,Basket,200,5y,100,Put
31,Basket,150,2y,125,Put
32,Basket,175,2y,125,Put
33,Basket,200,2y,125,Put
34,Basket,150,5y,125,Put
35,Basket,175,5y,125,Put
36,Basket,200,5y,125,Put""

```

```

def price_basket_options_from_input(data_csv):
    df = pd.read_csv(io.StringIO(data_csv))
    spot_vec = np.array([spot_price] * 3)
    price_dict = {}

    for idx, row in df.iterrows():
        Id = int(row['Id'])
        option_type = row['Type']
        strike = float(row['Strike'])
        maturity = parse_maturity(row['Maturity'])
        knockout = float(row['KnockOut'])

        vols = np.array([implied_vols[(stock, maturity)] for stock in stocks])
        price = price_knockout_basket_option(
            option_type, strike, maturity, knockout,
            spot_vec, vols, corr_matrix, risk_free_rate
        )
        price_dict[Id] = round(price, 2)

    print("Id,Price")
    for i in range(1, 37):
        price = price_dict.get(i, 1)
        print(f"{i},{price}")

# Run the code
price_basket_options_from_input(input_data)

```

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Challenge: Optimal Hedging Strategy

=====

```
import sys, numpy as np, pandas as pd, re
```

```
A=0.95
```

```
L=1e-5
```

```
K=25
```

```
G=401
```

```
def c(s): return re.sub('[^a-z0-9]', '', str(s).lower())
```

```
def f(df,n):
```

```
    t=c(n)
```

```
    for col in df.columns:
```

```
        if c(col)==t:
```

```
            return col
```

```
    raise SystemExit
```

```
t=sys.stdin.readline().split()
```

```
if len(t)<2: sys.exit()
```

```
p=np.array(t[1:],float)
```

```
n=len(p)
```

```
m=pd.read_csv('stocks_metadata.csv')
```

```
sid=f(m, 'stock_id')
```

```
cc=f(m, 'capital_cost')
```

```
m[cc]=pd.to_numeric(m[cc].astype(str).str.replace(',','',regex=False),errors='coerce')
```

```
m=m.dropna(subset=[cc]).set_index(sid)
```

```
cost_all=m[cc]
```

```
r=pd.read_csv('stocks_returns.csv')
```

```
d=f(r, 'date')
```

```
r=r.set_index(d)
```

```
r.index=pd.to_datetime(r.index,errors='coerce')
```

```
r=(r.sort_index()/100).iloc[-n:]
```

```
common=r.columns.intersection(cost_all.index)
```

```
r=r[common]
```

```
cost_all=cost_all[common]
```

```
corr=r.corrwith(pd.Series(p,index=r.index)).abs()
```

```
sel=corr.nlargest(min(K,len(corr))).index
```

```
R=r[sel].values
```

```

cvec=cost_all[sel].values

w0=np.linalg.lstsq(R,-p,rcond=None)[0]

best=None
bv=1e100
for s in np.linspace(-5,5,G):
    w=np.round(s*w0).astype(int)
    if not w.any(): continue
    hed=p+R@w
    var=-np.quantile(hed,1-A)
    tot=(np.abs(w)*cvec).sum()
    v=var+L*tot
    if v<bv:
        bv=v
        best=w

if best is None:
    best=np.zeros_like(w0,dtype=int)
    i=int(np.argmax(np.abs(w0)))
    best[i]=1 if w0[i]>=0 else -1

for stk,qty in zip(sel,best):
    if qty!=0:
        print(f'{stk} {qty}')

```