Stratified Randomized Experiments

`sreg` `v.1.0.0` `CRAN` `Coming Soon!` `R-CMD-check` `passing` `codecov` `86%`

The `sreg` package for `R`, offers a toolkit for estimating average treatment effects (ATEs) in stratified randomized experiments. The package is designed to accommodate scenarios with multiple treatments and cluster-level treatment assignments, and accomodates optimal linear covariate adjustment based on baseline observable characteristics. The package computes estimators and standard errors based on Bugni, Canay, Shaikh (2018); Bugni, Canay, Shaikh, Tabord-Meehan (2023); and Jiang, Linton, Tang, Zhang (2023).

Dependencies: `dplyr`, `tidyr`, `extraDistr`, `rlang`

Suggests: `haven`, `knitr`, `rmarkdown`, `testthat (>= 3.0.0)`

R version required: `>= 2.10`

[Latest Build (v.1.0.0)](#)

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Supplementary files

- PDF version of the manual: [Download PDF](#)

- Sketch of the derivation of the ATE variance estimator under cluster-level treatment assignment: [Download PDF](#)

- Expressions for the multiple treatment case (with and without clusters): [Download PDF](#)

Installation

The latest version can be installed using `devtools`. The official `CRAN` release will be available soon.

```r
library(devtools)
install_github("jutrifonov/sreg")
```

```
Downloading GitHub repo jutrifonov/sreg@HEAD
  R CMD build
  checking for file '/private/var/folders/mp/06gjwr8j56zdp5j2vgdkd4z40000gq/T/RtmpZh7j1Y/remotesfbf7659
  preparing 'sreg':
  checking DESCRIPTION meta-information
  checking for LF line-endings in source and make files and shell scripts
  checking for empty or unneeded directories
  building 'sreg_0.5.8.tar.gz'

* installing *source* package 'sreg' ...
** using staged installation
** R
** data
*** moving datasets to lazyload DB
** byte-compile and prepare package for lazy loading
** help
```

```
*** installing help indices
** building package indices
** testing if installed package can be loaded from temporary location
** testing if installed package can be loaded from final location
** testing if installed package keeps a record of temporary installation path
* DONE (sreg)

library(sreg)

#>    ____   ____  _____ ____           Stratified Randomized
#> / ___||  _ \| ____/ ___|        Experiments
#> \___ \| |_) |  _|| |  _
#>  ___) |  _ <| |__| |_| |
#> |____/|_| _____| version 1.0.0

#> Type 'citation("sreg")' for citing this R package in publications.
```

The function `sreg()`

Estimates the ATE(s) and the corresponding standard error(s) for a (collection of) treatment(s) relative to a control.

Syntax

```
sreg(Y, S = NULL, D, G.id = NULL, Ng = NULL, X = NULL, HC1 = TRUE)
```

Arguments

- **Y -** a numeric `vector/matrix/data.frame/tibble` of the observed outcomes;
- **S -** a numeric `vector/matrix/data.frame/tibble` of strata indicators $0, 1, 2, ...$; if `NULL` then the estimation is performed assuming no stratification;
- **D -** a numeric `vector/matrix/data.frame/tibble` of treatments indexed by $0, 1, 2, ...$, where `D = 0` denotes the control;
- **G.id -** a numeric `vector/matrix/data.frame/tibble` of cluster indicators; if `NULL` then estimation is performed assuming treatment is assigned at the individual level;
- **Ng -** a numeric `vector/matrix/data.frame/tibble` of cluster sizes; if `NULL` then `Ng` is assumed to be equal to the number of available observations in every cluster;
- **X -** a `matrix/data.frame/tibble` with columns representing the covariate values for every observation; if `NULL` then the estimator without linear adjustments is applied [^*];
- **HC1 -** a `TRUE/FALSE` logical argument indicating whether the small sample correction should be applied to the variance estimator. [^*]: *Note: sreg cannot use individual-level covariates for covariate adjustment in cluster-randomized experiments. Any individual-level covariates will be aggregated to their cluster-level averages.*

Data Structure

Here we provide an example of a data frame that can be used with `sreg`.

Y	S	D	G.id	Ng	x_1	x_2
-0.57773576	2	0	1	10	1.5597899	0.03023334
1.69495638	2	0	1	10	1.5597899	0.03023334
2.02033740	4	2	2	30	0.8747419	-0.77090031
1.22020493	4	2	2	30	0.8747419	-0.77090031
1.64466086	4	2	2	30	0.8747419	-0.77090031
-0.32365109	4	2	2	30	0.8747419	-0.77090031

```
|  2.21008191  | 4 | 2 |  2  | 30 |  0.8747419 | -0.77090031  |
| -2.25064316  | 4 | 2 |  2  | 30 |  0.8747419 | -0.77090031  |
|  0.37962312  | 4 | 2 |  2  | 30 |  0.8747419 | -0.77090031  |
```

Summary

`sreg` prints a *"Stata-style"* table containing the ATE estimates, corresponding standard errors, t-statistics, p-values, 95% asymptotic confidence intervals, and significance indicators for different levels α. The example of the printed output is provided below.

```
Saturated Model Estimation Results under CAR with clusters and linear adjustments
Observations: 30000
Clusters: 1000
Number of treatments: 2
Number of strata: 4
Covariates used in linear adjustments: x_1, x_2
---
Coefficients:
      Tau    As.se   T-stat P-value CI.left(95%) CI.right(95%) Significance
1 0.01614 0.04513  0.35753 0.72069     -0.07232        0.1046
2 0.78642 0.04642 16.94263 0.00000      0.69545        0.8774          ***
---
Signif. codes:  0 `***` 0.001 `**` 0.01 `*` 0.05 `.` 0.1 ` ` 1
```

Return Value

The function returns an object of class `sreg` that is a list containing the following elements:

- `tau.hat` - a $1 \times |\mathcal{A}|$ vector of ATE estimates, where $|\mathcal{A}|$ represents the number of treatments;

- `se.rob` - a $1 \times |\mathcal{A}|$ vector of standard errors estimates, where $|\mathcal{A}|$ represents the number of treatments;

- `t.stat` - a $1 \times |\mathcal{A}|$ vector of t-statistics, where $|\mathcal{A}|$ represents the number of treatments;

- `p.value` - a $1 \times |\mathcal{A}|$ vector of corresponding p-values, where $|\mathcal{A}|$ represents the number of treatments;

- `CI.left` - a $1 \times |\mathcal{A}|$ vector of the left bounds of the 95% as. confidence interval;

- `CI.right` - a $1 \times |\mathcal{A}|$ vector of the right bounds of the 95% as. confidence interval;

- `data` - an original data of the form `data.frame(Y, S, D, G.id, Ng, X)`;

- `lin.adj` - a `data.frame` representing the covariates that were used in implementing linear adjustments.

Empirical Example

Here, we provide the empirical application example using the data from (Chong et al., 2016), who studied the effect of iron deficiency anemia on school-age children's educational attainment and cognitive ability in Peru. The example replicates the empirical illustration from (Bugni et al., 2019). For replication purposes, the data is included in the package and can be accessed by running `data("AEJapp")`. This example can be accessed directly in R via `help(sreg)`.

```
library(sreg, dplyr, haven)
```

The description of the dataset can be accessed using `help()`:

```
help(AEJapp)
```

We can upload the `AEJapp` dataset to the R session via `data()`:

```
data("AEJapp")
data <- AEJapp
```

It is pretty straightforward to prepare the data to fit the package syntax using `dplyr`:

```
Y <- data$gradesq34
D <- data$treatment
S <- data$class_level
data.clean <- data.frame(Y, D, S)
data.clean <- data.clean %>%
  mutate(D = ifelse(D == 3, 0, D))
Y <- data.clean$Y
D <- data.clean$D
S <- data.clean$S
head(data.clean)
      Y D S
1 11.2 1 1
2 12.4 0 3
3 11.9 0 5
4 13.1 0 1
5 13.4 2 2
6 10.7 0 1
```

We can take a look at the frequency table of `D` and `S`:

```
table(D = data.clean$D, S = data.clean$S)
    S
D    1  2  3  4  5
  0 15 19 16 12 10
  1 16 19 15 10 10
  2 17 20 15 11 10
```

Now, it is straightforward to replicate the results from (Bugni et al, 2019) using `sreg`:

```
result <- sreg::sreg(Y = Y, S = S, D = D)
print(result)

Saturated Model Estimation Results under CAR
Observations: 215
Number of treatments: 2
Number of strata: 5
---
Coefficients:
       Tau    As.se   T-stat P-value CI.left(95%) CI.right(95%) Significance
1 -0.05113 0.20645 -0.24766 0.80440     -0.45577       0.35351
2  0.40903 0.20651  1.98065 0.04763      0.00427       0.81379            *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

Besides that, `sreg` allows adding linear adjustments (covariates) to the estimation procedure:

```
pills <- data$pills_taken
age <- data$age_months
data.clean <- data.frame(Y, D, S, pills, age)
data.clean <- data.clean %>%
  mutate(D = ifelse(D == 3, 0, D))
Y <- data.clean$Y
D <- data.clean$D
S <- data.clean$S
X <- data.frame("pills" = data.clean$pills, "age" = data.clean$age)
result <- sreg::sreg(Y, S, D, G.id = NULL, X = X)
```

```
print(result)
Saturated Model Estimation Results under CAR
Observations: 215
Number of treatments: 2
Number of strata: 5
Covariates used in linear adjustments: pills, age
---
Coefficients:
       Tau    As.se   T-stat P-value CI.left(95%) CI.right(95%) Significance
1 -0.02862 0.17964 -0.15929 0.87344     -0.38071       0.32348
2  0.34609 0.18362  1.88477 0.05946     -0.01381       0.70598            .
---
Signif. codes:  0 `***` 0.001 `**` 0.01 `*` 0.05 `.` 0.1 ` ` 1
```

The function `sreg.rgen()`

Generates the observed outcomes, treatment assignments, strata indicators, cluster indicators, cluster sizes, and covariates for estimating the treatment effect following the stratified block randomization design under covariate-adaptive randomization (CAR).

Syntax

```
sreg.rgen(n, Nmax = 50, n.strata,
          tau.vec = c(0), gamma.vec = c(0.4, 0.2, 1),
          cluster = TRUE, is.cov = TRUE)
```

Arguments

- **n -** a total number of observations in a sample;
- **Nmax -** a maximum size of generated clusters (maximum number of observations in a cluster);
- **n.strata -** an `integer` specifying the number of strata;
- **tau.vec -** a numeric $1 \times |\mathcal{A}|$ `vector` of treatment effects, where $|\mathcal{A}|$ represents the number of treatments;
- **gamma.vec -** a numeric 1×3 `vector` of parameters corresponding to covariates;
- **cluster -** a TRUE/FALSE argument indicating whether the dgp should use a cluster-level treatment assignment or individual-level;
- **is.cov -** a TRUE/FALSE argument indicating whether the dgp should include covariates or not.

Return Value

- **Y -** a numeric $n \times 1$ `vector` of the observed outcomes;
- **S -** a numeric $n \times 1$ `vector` of strata indicators;
- **D -** a numeric $n \times 1$ `vector` of treatments indexed by $0, 1, 2, \dots$, where `D = 0` denotes the control;
- **G.id -** a numeric $n \times 1$ `vector` of cluster indicators;
- **Ng -** a numeric `vector/matrix/data.frame` of cluster sizes; if NULL then Ng is assumed to be equal to the number of available observations in every cluster;
- **X -** a `data.frame` with columns representing the covariate values for every observation.

Example

```
library(sreg)
data <- sreg.rgen(n = 1000, tau.vec = c(0), n.strata = 4, cluster = TRUE)
> head(data)
          Y S D     x_1       x_2
1 1.717293 1 0 4.772092 2.4138491
```

```
2 2.553695 2 0 5.413440 2.0551019
3 2.237556 3 2 6.611161 0.9300293
4 1.825809 3 1 2.735503 1.7839981
5 5.536280 2 2 2.469239 2.0495611
6 1.628753 2 0 4.887561 2.1327071
```

References

Bugni, F. A., Canay, I. A., and Shaikh, A. M. (2018). Inference Under Covariate-Adaptive Randomization. *Journal of the American Statistical Association*, 113(524), 1784–1796, doi:10.1080/01621459.2017.1375934.

Bugni, F., Canay, I., Shaikh, A., and Tabord-Meehan, M. (2024+). Inference for Cluster Randomized Experiments with Non-ignorable Cluster Sizes. *Forthcoming in the Journal of Political Economy: Microeconomics*, doi:10.48550/arXiv.2204.08356.

Jiang, L., Linton, O. B., Tang, H., and Zhang, Y. (2023+). Improving Estimation Efficiency via Regression-Adjustment in Covariate-Adaptive Randomizations with Imperfect Compliance. *Forthcoming in Review of Economics and Statistics*, doi:10.48550/arXiv.2204.08356.