Formal Hydrogen Transfer Reactions and the Effects of Non-Redox Active Metal Cations

by

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Abstract

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Preface stuff

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List of Symbols and Abbreviations

BDE bond dissociation enthalpy

BEP Bell-Evans-Polanyi
BnO' benzyloxyl radical
CHD cyclohexadiene
CumO' cumyloxyl radical

 $\begin{array}{ll} \text{DFT} & \text{density-functional theory} \\ \text{DNA} & \text{deoxyribonucleic acid} \\ \text{DMA} & N, N\text{-dimethylacetamide} \\ \text{DMF} & N, N\text{-dimethylformamide} \end{array}$

 E_a activation energy

 $\begin{array}{ll} {\rm FHT} & {\rm formal\ hydrogen\ transfer} \\ {\mathcal H} & {\rm Hamiltonian\ operator} \\ {\rm HAT} & {\rm hydrogen\ atom\ transfer} \end{array}$

HB hydrogen bond HF Hartree-Fock

HOMO highest occupied molecular orbital

kcal mol^{-1} kilocalories per mole K_x equilibrium constant

 k_x rate constant

KSEs kinetic solvent effects

LFER linear free energy relationship

LFP laser flash photolysis
M molar concentration
MO molecular orbital
MDA malondaldehyde

NCI non-covalent interaction

PCET proton coupled electron transfer PMP 1,2,2,6,6-pentamethylpiperadine

PES potential energy surface

List of Symbols and Abbreviations

RNA ribonucleic acid

ROS reactive oxygen species

s seconds

SOMO singly occupied molecular orbital SPLET sequential proton loss electron transfer

 $\begin{array}{lll} {\rm STO} & {\rm Slater-type\ orbital} \\ {\rm TEA} & {\rm triethylamine} \\ {\rm THF} & {\rm tetrahydrofuran} \\ {\rm TS} & {\rm transition\ state} \\ {\it Z} & {\rm atomic\ number} \end{array}$

 ΔG Gibbs free energy of reaction

 ΔG^{\ddagger} Gibbs free energy barrier of reaction

 ΔH enthalpy of reaction

 ΔH^{\ddagger} enthalpic reaction barrier of reaction

 ΔS entropic change of reaction

 ∇^2 Laplacian operator

 σ_X Hammett substituent parameter

 ρ sensitivity constant, or electron density

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This is the place to thank professional colleagues and people who have given you the most help during the course of your graduate work.

Dedication

The dedication is usually quite short, and is a personal rather than an academic recognition. The *Dedication* does not have to be titled, but it must appear in the table of contents. If you want to skip the chapter title but still enter it into the Table of Contents, use this command \chapter[Dedication]{}.

Chapter 1

Introduction

Radicals are chemical species which tend to be highly reactive due to the presence of one or more unpaired electrons. Living systems depend on radical processes as part of normal metabolism but biomaterials such as proteins, are susceptible to radical induced damage. Radical induced oxidation of biomaterials has been implicated in a number of degenerative disease states, including cancer, Alzheimer's Disease, Parkinson's Disease, and multiple sclerosis. ^{2–6}

In biological systems, radicals are derived from both endogenous sources, such as transition metal-ion redox processes involved in respiration and other in vivo processes, as well as exogenous sources, for instance, solar radiation and air pollutants. A significant portion of ROSs originate from reactions of O_2 with the redox-active metals copper and iron, such as those reactions involved in Fenton chemistry. Navgen-centred radicals, known as reactive oxygen species (ROSs) in biology, are particularly important due to the nature of the aerobic respiration. The radicals of primary concern are the highly reactive hydroxyl radical (HO $^{\bullet}$), alkoxyl radicals (RO $^{\bullet}$), superoxide (HOO $^{\bullet}$ /O $_2^{\bullet}$ -), and peroxyl radicals (ROO $^{\bullet}$). Damage occurs when an ROS initiates a radical chain reaction through hydrogen atom transfer (HAT), electron transfer, or addition reactions, leading to rapid propagation. HAT is the most relevant reaction and is the focus of my work.

This work is primarily concerned with models for proteins. The oxidation of protein by ROSs occurs through a radical chain mechanism which has been studied in detail.^{8,9} As there are 20 common amino acid side chains, as well as a common peptide backbone in proteins, there are a large number of possible reactions. Proteins are the most abundant biomaterial in most biological systems, ¹⁰ thus understanding their degradation is essential to understaning degenerative disease. Some of the reactions involved in protein oxidation are shown in Scheme 1.1.

Scheme 1.1: Common reaction involved in the radical-meditated oxidation of proteins. The reactions are as follows: initiation of radical chain through abstraction by $\bf a$) the hydroxyl radical $\bf b$) α -carbon radical, $\bf c$) radical addition of molecular oxygen, $\bf d$) HAT with an incoming peroxyl radical, $\bf e$) additional reaction with an incoming peroxyl radical producing water and oxygen, $\bf f$) formation of hydroxyl-amide by HAT with an incoming peroxyl radical, $\bf g$) possible cross-linking mechanism of two carbon-centred radicals, $\bf h$) possible fragmentation pathways of an oxygen-centred radical intermediate. Figure adapted from Reference 8.

Initial abstraction (Reaction a) often occurs at the α -carbon position (R₂CH), forming a carbon-centred radical (R₂C $^{\bullet}$) which is partially delocalised in the π -system of the amide group. Many studies have indicated that the stability of R₂C $^{\bullet}$ is determined by stereo-electronic considerations

related to the planarity of the amide group. For example, steric bulk of the side chains, as well as local protein structure (helix, sheet, etc.) can constrain radical geometries. Therefore, the most captodatively stable α -carbon radical occurs at glycine residues in antiparallel β -sheets. ¹¹ The side-chains are also susceptible to oxidation. Those side-chains containing sulphur, ¹² as well as tyrosine (which has a fairly weak phenolic O-H bond of about 89 kcal mol⁻¹), ¹³ are particularly susceptible to oxidation.

Propagation occurs through various processes, including the abstraction of another H atom by the newly formed R_2C^{\bullet} (Reaction b), or radical-mediated oxidation, ¹⁴ leading to the formation of an oxidised carbon centre (R_2COH). The course of propagation through radical-mediated protein oxidation is determined by the availability of either singlet oxygen ($^{1}O_2$), or superoxide (O_2^{\bullet}) (or the protonated form, peroxyl radical ($^{\bullet}OOH$)). Those reactions which occur in the presence of O_2 and $^{\bullet}OOH$ are shown in Reactions **c-f**. The radical chain reaction can be terminated through several mechanisms, including protein-protein cross-linking (Reaction **g**), protein fragmentation (Reaction **h**), or through reactions with antioxidants. The sum total of all these processes leads to the accumulation of oxidised proteins which is associated with many degenerative diseases. ¹⁵

1.1 Studying HAT reactions

Formal HAT reactions are a fundamental radical chemical transformation which has been studied for over a century. ^{16,17} At the macroscopic level, HAT reactions which involve oxygen-centred radicals and non-radical organic substrates are reasonably well characterised: the effects of bulk solvent are well understood. ¹⁸ However, the roles of substrate-radical and substrate-radical-medium interactions at the microscopic (molecular) level continue to be relatively poorly understood. In my work, I shall make use of quantum chemistry in order to study formal HAT at the molecular level. In doing so, I hope to contribute to a better understanding of the fundamental properties which govern these reactions, and thus develop insights into the many important processes in which HAT takes place.

The potential energy surface (PES) for any chemical reaction is a complex hypersurface that depends on many variables. Typically this problem can be simplified by examining only the relevant geometry changes. Often the two most important coordinates can be isolated, giving a 3-dimensional potential energy surface. Furthermore, in chemistry we simplify this problem to 2-dimensions, such that the so-called intrinsic reaction coordinate,

or the lowest energy cross section of a higher dimension PES. This yields a reaction coordinate diagram, as is illustrated below in Figure 1.1.

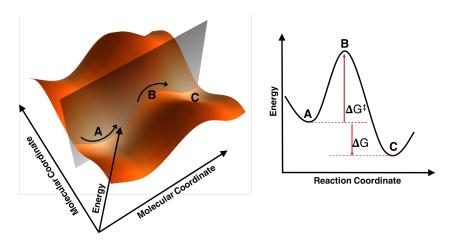


Figure 1.1: Three-dimensional potential energy surface and corresponding reaction coordinate diagram. Stationary states A, B, and C, correspond to the pre-reaction, transition state, and post-reaction complexes, respectively.

In a typical reaction coordinate diagram, the reactants begin to interact and form a pre-reaction complex (A). Given sufficient energy, the reaction will proceed over the top of the energy barrier through a transition state (TS) complex (B). After the chemical transformation is completed, a post-reaction complex (C) is formed until the products are able to separate.

In quantum chemistry, we are generally concerned with the thermodynamic and kinetic properties of a reaction. This is achieved through the investigation of stationary states (reactants, pre-reaction complex, TS complex, post-reaction complex, and products) along the reaction coordinate. Thermodynamic analysis of a reaction requires the understanding of the stability of the products relative to the reactants, measured by change in Gibbs free energy ΔG , while kinetic analysis requires the understanding of the stability of the TS complex relative to the reactants measured by the Gibbs free energy barrier ΔG^{\ddagger} .

To fully understand HAT reactions, one must analyse the factors which influence the thermodynamics and kinetics of these reactions. Thermodynamically this is relatively simple; relative bond strengths generally dictate the stability of products relative to reactants for HAT reactions. Typically, a reaction will be exergonic if the bond being formed is stronger than the bond being broken. Entropic changes (ΔS) in HAT reactions are in all

but the most unusual cases, negligible ($\Delta S \approx 0$).¹⁹ Kinetic analysis can be considerably more complicated, as there are numerous factors which can stabilise or destabilise the reactants or TS complex. I have investigated several fundamental concepts associated with HAT reactions.

Recent work from our group, in collaboration with colleagues at University of Rome Tor Vergata, has focused on the importance of substrate-radical interactions. Specifically, it has been shown that the three-dimensional structures of oxygen-centred radicals, as well as the organic substrates, impacts the nature of the interactions involved in HAT reaction pathways. ²⁰ In our work, we utilise primarily the BnO and CumO and CumO and cals, which serve as a convenient proxy to biological oxygen-centred radicals. Reaction involving BnO and CumO can be easily monitored using highly resolved laser flash photolysis (LFP) techniques. A combination of theoretical and experimental techniques have been used to examine reactions involving BnO and CumO with a variety of organic substrates. A detailed discussion of these results shall be reserved for following chapters, however, a great deal of insight has been gained into the role of structure in both the radicals and substrates, and resulting intermolecular interactions.

Non-covalent interactions (NCIs; eg. van der Waals interactions, hydrogen bonding, etc.) play a central role in all chemistry. Oxygen-centred radicals can hydrogen bond with substrates as both acceptors and donors. ²¹ These hydrogen bonding interactions, in addition to the other non-covalent interactions between the radical and substrate lead to the formation of a pre-reaction complex. NCIs are also known to be important in the stabilisation of TS complexes in HAT reactions. ^{22,23} Although the effects of NCI stabilisation are difficult to quantify, the concept of TS complex stabilisation is being recognised in applications such as enzymatic ²⁴ and synthetic catalysis. ²⁵

In Chapter 3, I shall consider non-covalent binding in the pre-reaction complex with respect to the well known, but phenomenological Arrhenius equation. Arrhenius parameters for the systems of interest in this work were previously tabulated, ²² and consist of thermoneutral or nearly thermoneutral reactions involving the creation and destruction of oxygen-centred radicals. These reactions are related to the phenol-phenoxyl self-exchange reaction in that a relatively strong pre-reaction complex is expected. As of yet, there is no framework which relates the non-covalently bound pre-reaction complex to kinetic results. We ask the simple question: does there exists a direct correlation between the Arrhenius pre-factor and the non-covalent binding energy?

Bond strengths are measured by bond dissociation enthalpies (BDEs),

and are central to the understanding of reactivity with respect to thermodynamics. In addition to this, there exists a tremendous amount of literature in which BDEs are linked to chemical reactivity, especially for HAT reactions. $^{16,26-29}$ There exists a linear free energy relationship (LFER), the Bell-Evans-Polanyi (BEP) Principle, 30,31 which states that the difference in activation energy (E_a) for two related reactions, is proportional to the differences in reaction enthalpy (ΔH):

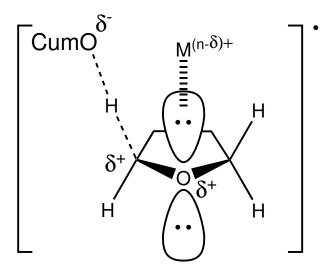
$$E_a = E_0 + \alpha \Delta H \tag{1.1}$$

where E_0 is the activation energy of a reference reaction, and α , a constant which characterises the position of the TS along the reaction coordinate. This relationship can be more generally used to compare larger families of reactions, although the applicability of this relationship is not well described.

In Chapter 4 I probe the applicability of the BEP principle, with the aim to determine how generally the BEP principle can be applied. This is achieved by relating highly-accurate, theoretically determined C-H bond strengths of species which undergo abstraction at these positions to the experimentally determined HAT rate constants. HAT reaction rate constants depend on many factors, however, by using measured rate constants from specific conditions (LFP with CumO at 298K), the difference in reactivity depend mainly on the differences in chemical properties of the systems of interest. Therefore, we hypothesise that there should exist two BEP relationships for abstraction of C-H bonds: one in which the incipient radical is delocalised into a π -system (benzylic/allylic) and the remaining alkyl radicals which are largely localised.

Finally, recent experimental results show that non-redox active metal cations, which are found ubiquitously in biological systems, have an inhibitory effect on HAT reactions involving oxygen-centred radicals and substrates which undergo abstraction from sites adjacent to heteroatoms (e.g. amines, amides, and ethers). Under various stoichiometric ratios, these metal cations have effects ranging from full inhibition to partial deactivation of HAT reactivity. $^{32-34}$ This effect has been attributed partially to the effects of hyperconjugative overlap. Take for example tetrahydrofuran (THF), shown in Scheme 1.2. Normally, there exists C-H bond weakening hyperconjugative overlap of electron density from one of the oxygen lone-pairs and the adjacent C-H σ^* anti-bonding orbitals. The interaction of a metal cation with the oxygen lone-pairs removes electron density from this interaction, thus increasing the C-H bond strength. As a results, the reactivity of this bond is decreased, as observed from the experimentally measured 3.2-fold

decrease in the rate constant for HAT with CumO $^{\bullet}$ in acetonitrile from 6.65 $\times 10^7 \text{ M}^{-1}\text{s}^{-1}$ to 7.0 $\times 10^7 \text{ M}^{-1}\text{s}^{-1}$ in the presence of 1.0 M Mg(ClO₄)₂.³²



Scheme 1.2: Hyperconjugative overlap in tetrahydrofuran and the effect of non-redox active metal cations. The metal cation accepts electron density from the heteroatom lone pair, reducing overlap with the C-H σ^* antibonding orbital and increasing the C-H bond strength.

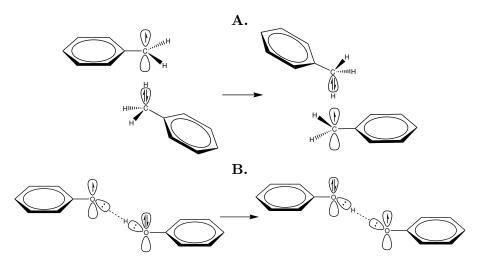
The nature of the interactions between non-redox active metal cations and organic substrates is poorly understood. The primary goal of this thesis is to understand the fundamental physico-chemical properties which lead to the experimentally observed trends in reactivity. This problem is explored in Chapter 5. The experimentally observed effects have led us to hypothesise that the presence of non-redox active metal cations has a chemoprotective effect against the radical induced oxidation of biomaterials such as proteins.

1.2 Mechanistic details of hydrogen transfer reactions

For a simple HAT reaction, there exists several possible mechanisms by which this transformation can occur. The two most common concerted mechanisms are direct HATⁱ and proton-coupled electron transfer (PCET). At the basic level, direct HAT involves the transfer of an electron and proton through the same set of acceptor/donor orbitals, while PCET involves

the transfer of an electron and proton through different sets of orbitals. In practise, this distinction is poorly described and this topic is still in active discussion in the literature. $^{23,29,35-43}$ Primarily, the distinction between the two processes is unclear because the two processes cannot be entirely separated physically. 23

The quintessential example when comparing direct HAT to PCET is the self-exchange reactions of benzyl/toluene and phenoxyl/phenol shown in Scheme 1.3, as described by Mayer et al. 36



Scheme 1.3: Self-exchange reactions of the **A.** benzyl/toluene couple through direct HAT **B.** phenoxyl/phenol couple through PCET.

In this work, the transition state structures, obtained through theoretical studies, were reported. The proposed structures have C_{2h} and C_2 symmetry for Scheme 1.3 A and B, respectively, oriented so that the aromatic rings are trans relative to one another. In this geometry, the benzyl/toluene pair undergoes direct HAT, with the $2p-\pi$ orbital of the benzylic carbon radical oriented at the benzylic hydrogen on toluene and little delocalisation of the radical into the π -system. Additionally, the singly occupied molecular orbital (SOMO) is of σ -symmetry. The calculated enthalpic barrier (ΔH^{\ddagger}) is 17.7 kcal mol⁻¹. For the phenoxyl/phenol pair, a fairly strongly hydrogen bonded pre-reaction complex is first formed (-8.1 kcal mol⁻¹, relative to reactants). The TS structure is such that the phenoxyl radical occupies

ⁱNot to be confused with the net reaction of formal hydrogen atom transfer. The abbreviation HAT will be used interchangeably, although the distinction should be clear from context.

a 2p orbital, and is allowed to overlap with the 2p lone pair of the phenol moiety and the aromatic π systems. This demonstrates that the SOMO is of π -symmetry and highly delocalised, and that HAT occurs through a PCET mechanism. The reaction has a barrier height $\Delta H^{\ddagger} = 5.0$ kcal mol⁻¹ relative to the hydrogen bonded complex, so that the barrier is 3.1 kcal mol⁻¹ below the separated reactants.

The work by Mayer et al. ³⁶ suggests that hydrogen bonding is a necessary, but not sufficient condition for PCET to occur. This then implies that PCET is not possible between molecules which do not possess hydrogen bonding moieties, such as carbon atoms. Work by other authors has shown this to be untrue. ^{23,44} In particular, DiLabio and Johnson ²³ demonstrated that this neglected the important contributions of $\pi - \pi$ interactions and lone pair- π interactions. Additional calculations revealed there exists a TS structure for the benzyl/toluene couple which is 3.7 kcal mol⁻¹ lower in energy than previously reported. This structure has C_2 symmetry with the aromatic rings oriented 34° relative to one another, allowing for optimal $\pi - \pi$ overlap. Analysis of the TS HOMO and SOMO show a net partial bonding interaction between the two π -systems, thus opening up an electronic channel for PCET to occur. They also suggest that the phenol-phenoxyl couple likely prefers a π -stacked TS structure, and compare this to a structural analogue, a naturally occurring tyrosyl-tyrosine couple. Additional work by Muñoz-Rugeles et al. 43 confirmed the existence of a π -stacked TS structure for the phenol-phenoxyl couple. They used an approach which utilises natural population analysis along the intrinsic reaction coordinate, and demonstrated that both the benzyl/toluene couple and phenoxyl-phenol couple favour a π -stacked TS structure and undergo HAT through a PCET mechanism. Interestingly, they also showed that reaction barrier heights for the PCET mechanism are systematically lower than those for direct HAT.

As there is not an obvious way to explore the differences in mechanism experimentally, computational examination of formal HAT reactions enables analysis of the mechanism of these reactions. A general distinction between a direct HAT mechanism and PCET mechanism can be achieved. In doing so, important insight is gained from understanding the electronic behaviour of these reactions. The investigation the physico-chemical nature of HAT reactions shall continute to be the central theme of this thesis.

1.3 Detail to add to chapters

Note, I have yet to rewrite these snippets of writing. The aim is to isolate detail to be incorporated later.

1.3.1 A-factors

(I have incorporated most of the details already from previous drafts. I am in the process of drafting this chapter at the moment.)

Stereo-Electronic interactions

The effects of steric bulk also play an important role in HAT, and have been studied extensively by our colleagues in Rome, as well as by others. $^{45-52}$ Although a C-H bond may be weaker than others on a given substrate, if it is not accessible due to steric constraints, abstraction will not occur at this site. Otherwise, additional steric bulk can lead to significant reductions in reactivity, through destabilisation of the TS complex. For example, in reactions of tertiary acetamides with CumO $^{\bullet}$, 52 where abstraction occurs mainly from C-H bonds α to the nitrogen atom, a two fold decrease in normalised rate constant is observed in going from N, N-dimethylacetamide to N, N-diisobutylacetamide ($k_H = 2.0 \times 10^5$ and 7.8×10^4 M $^{-1}$ s $^{-1}$, respectively).

1.3.2 BDEs

Bond strengths and the Bell-Evans-Polanyi Principle

Often, BDEs are used in linear free energy relationships (LFERs) to relate chemical reactivity to bond strength. One such example ²⁸ is the application of BDEs to the Hammett equation, ⁵³ which can be used to study substituent effects from thermodynamic (Equation 1.2) or kinetic analysis (Equation 1.3).

$$\log \frac{K_X}{K_H} = \rho \sigma_X \tag{1.2}$$

$$\log \frac{k_X}{k_H} = \rho \sigma_X \tag{1.3}$$

In the above equations, K is an equilibrium constant and k is a rate constant for either a reference reaction with a hydrogen substituent H or a given substituent X. The substituent parameters σ_X , have been measured

for various different reference reactions, although the original parameters were measured for the acidity of benzoic acid. ⁵⁴ Plots of $\log(K_X/K_H)$ or $\log(k_X/k_H)$ against σ_x have been used to determine ρ , the sensitivity constant. Originally ρ was used to determine whether a reaction was more sensitive ($\rho > 1$), less sensitive ($\rho < 1$), or equally sensitive to substituents than benzoic acid, with negative charges being produced. If ρ is negative then positive charge is said to be formed as a result of substituents.

In the context of BDEs, Pratt et al. ²⁸ examined a series of substituents (Y) on toluenes, anilines, and phenols (4-YC₆H₄-ZX), and showed that the Z-X BDEs can be correlated to the electrophilic substituent constants, $\sigma_p^+(Y)$. This was surprising because it demonstrated that homolytic properties correlated with properties derived from the heterolytic S_N1 solvolyses of para-substituted cumyl chlorides. ⁵⁵ Specifically, this showed that since $\sigma_p^+(Y)$ describes the relative ability of Y to stabilise a positive charge, the ability to stabilise strong electron withdrawing (EW) moieties can be well described in general by these parameters. This means that BDEs for toluenes and anilines are well correlated to $\sigma_p^+(Y)$, since O and NH can be described like positive charges (strong EW groups). Toluenes, which have resulting radicals (CH₂) which are neither electron withdrawing nor donating, are poorly correlated with $\sigma_p^+(Y)$.

Another interesting LFER, which is utilised in Chapter 4, is the Bell-Evans-Polanyi (BEP) Principle, 30,31 which states that the difference in activation energy (E_a) for two related reactions (within the same family), is proportional to the differences in reaction enthalpy (ΔH) :

$$E_a = E_0 + \alpha \Delta H \tag{1.4}$$

This relationship has been more generally used to compare larger families of reactions. The remaining terms in Equation 1.4 are E_0 , the activation energy of a reference reaction, and α is a constant which characterises the position of the TS along the reaction coordinate. This can be rationalised by considering a series of reactions with similar energy profiles: if the reaction becomes more exothermic, the barrier height will decrease (the opposite is also true for endothermic reactions), as illustrated in Figure 1.2.

If the BEP relationship holds for a series of related HAT reactions, then BDEs should correlate with the activation energy, where increased bond strengths would represent a destabilisation in the TS complex. In practice, plots of BDEs against the logarithm of rate constant are used. An interesting example of this is the work of Pratt et al. ⁵⁶, in which the free radical

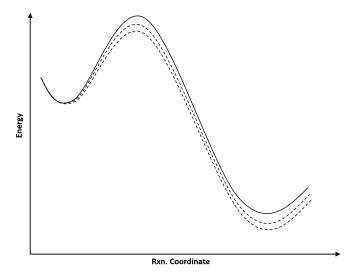


Figure 1.2: Energy profiles for a series of related exothermic reactions illustrating the Bell-Evans-Polanyi Principle.

oxidation of unsaturated lipids is examined. They achieve this through the correlation of theoretically determined C-H and C-OO $^{\bullet}$ bond strengths with experimentally measured HAT rate constants and O₂ addition rate constants, respectively. BEP plots (BDE vs. $\log k$) for a large range of polyunsaturated fatty acid models show good correlation for both the C-H bonds and C-OO $^{\bullet}$ bonds examined. This demonstrates that BDEs have a direct impact on the reaction barrier height, giving validation to the BEP Principle.

Although chemists often consider the importance of BDE in thermodynamic analysis, bond strengths are an important consideration in kinetic analysis as well. As such, the altering of bond strengths can be an important factor in related HAT reactions. The generallity of application of the BEP Principle is discussed in Chapter 4.

1.3.3 Metal Cation effects

1.3.4 The effects of metal cations on HAT reactions

Solvent interactions in HAT reactions can be described as Lewis acid/base interactions. In biological systems, the most common solvent is water, which can act as both a Lewis acid and base, due to its self-ionising equilibrium. Other important Lewis acids in biology are the non-redox active alkali and

alkaline earth metal cations that are present ubiquitously throughout biological systems. Metal ions such as sodium, magnesium, potassium, and calcium are essential to biological function. ⁵⁷ (Include something about number of ions per protein and/or biological concentrations)

Given the Lewis acid/base nature of these non-redox active metals, we were driven to explore the effects upon HAT reactions. Experimental investigation of these effects has been underway by the Bietti group in Rome. The effects of non-redox active metal cations on HAT from C-H bonds of cyclohexadiene (CHD), tetrahydrofuran (THF), and tertiary alkylamines to CumO were examined. This work is summarized in Table 1.1. Additional experiments examining the same reactions of N, N-dimethylacetamide (DMA) and N, N-dimethylformamide (DMF), as well as for various other acetylamides have been performed, and provides the experimental background for this thesis.

Table 1.1: Summary of experimental rate constants of HAT with CumO'for cyclohexadiene (CHD), tetrahyrofuran (THF), triethylamine (TEA), and 1,2,2,6,6-pentamethylpiperidine (PMP), including the effect of non-redox active metal cations. Rate constants were determined by LFP in 25 °C MeCN. *Rate constants are approximate as the effects of even small additions of metal cations cause rate outside the range of laser flash photolysis experiments.

Substrate	Conditions	$k_H({\rm M}^{-1}{\rm s}^{-1})$
CHD		$(6.65 \pm 0.02) \times 10^7$
	$LiClO_4$ 1.0 M	$(7.49 \pm 0.04) \times 10^7$
	$Mg(ClO_4)_2$ 1.0 M	$(7.0 \pm 0.1) \times 10^7$
THF		$(5.7 \pm 0.1) \times 10^6$
	$LiClO_4$ 1.0 M	$(2.87 \pm 0.04) \times 10^6$
	LiOTf 1.0 M	$(2.8 \pm 0.2) \times 10^6$
	$\mathrm{Mg}(\mathrm{ClO_4})_2~1.0~\mathrm{M}$	$(1.8\pm\ 0.1)\ \times 10^6$
TEA		$(2.0 \pm 0.1) \times 10^8$
	$LiClO_4$ 1.0 M	$(9.37 \pm 0.01) \times 10^7$
	$Mg(ClO_4)_2 0.005 M$	$< 1 \times 10^{6*}$
PMP		$(1.70 \pm 0.02) \times 10^8$
	$LiClO_4$ 1.0 M	$(9.0 \pm 0.3) \times 10^7$
	$Mg(ClO_4)_2 \ 0.005 \ M$	$< 1 \times 10^{6*}$

In general, metal cation interactions lead to deactivation of C-H bonds and experimental rate constants decrease as a result. An explaination for this is the same as for KSEs, where Lewis acid binding causes a decrease in α -C-H bond σ^* population, thus increasing the effective C-H bond strength and decreasing k_H . For cyclohexadiene, a marginal increase in k_H was observed with additions of 1.0 M LiClO₄ and Mg(ClO₄)₂, which was explained on the basis of interactions of the metals with CumO*. This demonstrates that metal cations have a limited ability to influence HAT reactions of CumO'with alkene based substrates. For THF, k_H is 2.0 and 3.2 times lower with the addition of 1.0 M LiClO₄ and Mg(ClO₄)₂, respectively. Li- ClO_4 has a roughly 2-fold decreasing effect on k_H for alkylamines, whereas $Mg(ClO_4)_2$ has a significantly greater effect, decreasing k_H by more than two orders of magnitude, an effect that has been attributed to the compact charge density of Mg²⁺. As a whole, these results suggest that metal ions interact more strongly with substrates than CumO', thus C-H bond deactivation is observed due to Lewis acid/base effect. The Lewis acidity of the metal appears to have an important role, since $Mg(ClO_4)_2 > LiClO_4$ in regards to Lewis acidity and effect on k_H . The Lewis basicity of the substrate is also clearly important. Alkylamines undergo a larger decrease in k_H , relative to THF, as they are stronger Lewis bases. Computational studies have validated these results, demonstrating that binding of Mg(ClO₄)₂ leads to a 5.1 kcal mol $^{-1}$ decrease in the $\alpha\text{-C-H}$ BDE in TEA and that k_H decreases by > 4 orders of magnitude.⁵⁹

Simple amides such as DMF and DMA are often used as simple peptide models. 60 As such the deactivation of C-H bonds in amides, as indicated by the observed decreases in k_H , leads to the central hypothesis of this thesis: non-redox active metals cations can serve as chemoprotective agents for biomolecules. Experimental evidence for this is demonstrated in Figure 1.3. For LiClO₄ added to DMF and DMA, total inhibition of HAT occurs up to 2 and 1 molar equivalents, respectively. Inhibition of HAT occurs for 2 and 4 molar equivalents, respectively, followed by total non-inhibition. A much weaker effect is observed with NaClO₄, while a similar strong deactivating effect is observed for Ca(ClO₄)₂. The addition of Mg(ClO₄)₂ gives weak deactivation for the first two molar equivalents of both DMF and DMA, with strong activation for an additional two equivalents. This unusual behaviour is as of yet, unexplained. Additional discussion of experimental results shall be reserved for Chapter 5.

1.3.5 Undecided

The species involved in HAT reactions are often neutral radicals, thus the influence of charge transfer in the TS complex can have important implications. Consider the TS of a generic HAT reaction in Scheme 1.4, there are

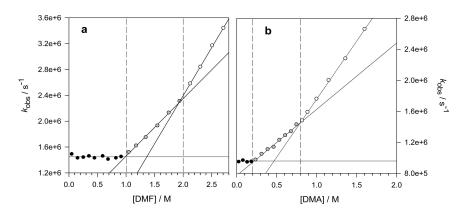


Figure 1.3: Plots of observed rate constants against concentation of substrate for HAT reactions with cumyloxyl radical: **a** Substrate = DMF, measured by LFP at 25°C in solutions of MeCN containing 1.0 M dicumyl peroxide and 0.5 M LiClO₄. Complete inhibition of HAT is observed at 0–1.0 M, while linear regression for the 1.0–2.0 M regions gives $k_{H1} = 8.91 \times 10^5$ M⁻¹s⁻¹, and $k_{H2} = 1.49$ ⁶ M⁻¹s⁻¹ in the 2.0–2.7 M region. **b** Substrate = DMA, measured by LFP at 25 °C in solutions of MeCN containing 1.0 M dicumyl peroxide and 0.2 M LiClO₄. Complete inhibition of HAT is observed at 0–0.2 M, while linear regression in the 0.2–0.8 M region gives k_{H1} =8.54 ×10⁵ M⁻¹s⁻¹ and $k_{H2} = 1.49 \times 10^6$ M⁻¹s⁻¹ in the 0.8–1.6 M region. Figure taken from Reference 58.

four obvious resonance forms. For a series of related reactions, E_a would be expected to decrease as the contribution of dipolar ion resonance forms increases. ⁶¹ oxygen-centred radicals are electrophilic in nature, thus the importance of the third resonance structure becomes important. HAT is favoured from C-H bonds which are electron rich, or nucleophilic. ²⁰

Scheme 1.4: A generic HAT transition state structures and possible resonance forms.

An example of this effect is from the work of our colleagues in Rome, 49,50 in which rate constants (k_H , normalised for the number of abstractable hydrogens) for cyclohexane and acetone to the cumyloxyl radical (CumO*) were

measured and compared to theoretically determined C-H BDEs. Cyclohexane has a C-H BDE = 99.5 kcal mol $^{-1}$ and $k_H=9.2\times10^4~\mathrm{M}^{-1}\mathrm{s}^{-1}$, while acetone has C-H BDE of 96.0 kcal mol $^{-1}$ and $k_H=<2\times10^3~\mathrm{M}^{-1}\mathrm{s}^{-1}$. As a result of polar effects, although cyclohexane has a greater bond strength, it is at least an order of magnitude more reactive in HAT than acetone.

Chapter 2

Theory

2.1 The quantum mechanical approach

The fundamental properties governing all of chemistry are dictated by the quantum mechanical wave functions, Ψ . Therefore, in quantum chemistry we seek solutions to the non-relativistic time-independent Schrödinger equation

$$\mathscr{H}|\Psi\rangle = E|\Psi\rangle \tag{2.1}$$

where \mathscr{H} is the Hamiltonian operator for a system of nuclei and electrons, and Ψ is the wave function, defined as the set of eigenvectors with energy eigenvalues E. ⁶² For a system with N electrons and M nuclei, the full Hamiltonian in atomic units is

$$\mathcal{H} = -\sum_{i=1}^{N} \frac{1}{2} \nabla_{i}^{2} - \sum_{A=1}^{M} \frac{1}{2M_{A}} \nabla_{A}^{2} - \sum_{i=1}^{M} \sum_{A=1}^{M} \frac{Z_{A}}{r_{iA}} + \sum_{i=1}^{N} \sum_{j>i}^{N} \frac{1}{r_{ij}} + \sum_{A=1}^{M} \sum_{B>A}^{M} \frac{Z_{A}Z_{B}}{R_{AB}}$$

$$(2.2)$$

In this equation, Z_A is the atomic number of nucleus A with a mass M_A divided by the mass of an electron. The Laplacian operators ∇_i^2 and ∇_A^2 represent differentiation with respect to the coordinates of the *ith* electron and Ath nucleus. The first and second terms are the kinetic energies of the electrons and nuclei, respectively. The third term represents the Coulomb attraction between electrons and nuclei with distance r_{iA} . The fourth and fifth terms represent repulsion between two electrons with distance r_{ij} , and between two nuclei with distance R_{AB} , respectively.

Nuclei move slowly relative to electrons, due to their much greater mass. This is the central pillar of the Born-Oppenheimer approximation that is nearly always applied in molecular electronic structure calculations. The application of this approximation allows for the simplification of Equation 2.2: using a separation of electronic an nuclear variables, the second term

for nuclear kinetic energy is solved separately. Also, the last term of nuclear repulsion is constant, and thus is generally ignored. This leaves us with the electronic Hamiltonian

$$\mathcal{H}_{elec} = -\sum_{i=1}^{N} \frac{1}{2} \nabla_i^2 - \sum_{i=1}^{M} \sum_{A=1}^{M} \frac{Z_A}{r_{iA}} + \sum_{i=1}^{N} \sum_{j>i}^{N} \frac{1}{r_{ij}}$$
(2.3)

Unfortunately, it is only possible to exactly solve the Schrödinger equation for the full electronic Hamiltonian \mathcal{H}_{elec} in the simplest of cases: when there is only one electron (H, H₂⁺, He⁺, Li²⁺, etc). Note that since we will always work within the Born-Oppenheimer approximation, the subscript *elec* is usually dropped. In order to proceed to systems with multiple electrons, we must make further approximations.

2.1.1 Spin and Spatial Orbitals

We will refer to the wave function of a single particle as an orbital. Naturally then, as we will deal with electrons in molecules, we shall refer to their wave functions as molecular orbitals (MOs). To fully describe electrons we must consider a spatial and spin component to the overall wave function. A spatial orbital $\psi_i(\mathbf{r})$, is a function of the position vector \mathbf{r} , and describes the distribution of an electron in all space. It is usually assumed that spatial MOs form an orthonormal set such that

$$\langle \psi_i(\mathbf{r})|\psi_j(\mathbf{r})\rangle = \int d\mathbf{r}\psi_i^*(\mathbf{r})\psi_j(\mathbf{r}) = \delta_{ij}$$
 (2.4)

where the left-hand side is standard Dirac *bra-ket* notation representing the same integral in the middle. The right-hand side of Equation 2.4 is the standard Kronecker delta.

The spin of an electron is represented by two orthonormal functions $\alpha(\omega)$ and $\beta(\omega)$, or spin up and spin down. If a wave function describes both the spatial distribution and spin of an electron it is a spin orbital, $\chi_i(\mathbf{r})$, where \mathbf{x} represents both the spatial distribution and spin coordination of an electron $(\mathbf{x} = {\mathbf{r}, \omega})$. Since $\psi_i(\mathbf{r})$ and $\alpha(\omega)/\beta(\omega)$ are orthonormal, so too is $\chi_i(\mathbf{x})$

$$\langle \chi_i(\mathbf{x}) | \chi_j(\mathbf{x}) \rangle = \delta_{ij}$$
 (2.5)

2.1.2 The Hartree product

The first steps towards describing an N electron wave function come from the work in the late 1920s by Hartree. The early $Hartree\ method$ took an

approach in which the wave function of N non-interacting electrons (Ψ^{HP}) is described by the product of N spin orbitals, known as a *Hartree product*:

$$\Psi^{HP}(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N) = \chi_i(\mathbf{x}_1)\chi_i(\mathbf{x}_2)\dots\chi_k(\mathbf{x}_N)$$
 (2.6)

In such a system the Hamiltonian has the form of a sum of N independent operators

$$\mathcal{H} = \sum_{i=1}^{N} \hat{h}(i) \tag{2.7}$$

where $\hat{h}(i)$ is

$$\hat{h}(i) = -\frac{1}{2}\nabla_i^2 + V(\mathbf{r}_i)$$
(2.8)

such that the first term describes an electron's kinetic, and the second term describes potential felt by a single electron. If we consider the case which ignores electron-electron repulsion, then case V describes only the nuclear-electron attraction. Alternatively, Hartree may have included electron-electron repulsion in some average way.

Solutions to the Schrödinger equation for this system of non-interacting electrons are facile to obtain as each h(i) depends only on the variables of $\chi_i(\mathbf{x}_i)$, so that

$$\mathscr{H}\left|\Psi^{HP}\right\rangle = E\left|\Psi^{HP}\right\rangle \tag{2.9}$$

gives an eigenvalue energy solution E that is the sum of N spin orbital energies ε_i

$$E = \varepsilon_1 + \varepsilon_2 + \dots + \varepsilon_N \tag{2.10}$$

While this theory does allow one to calculate energies for an N electron system, it has a basic deficiency: the antisymmetry principle of wave functions is not obeyed. The antisymmetry principle states that the electronic wave function must change sign (be antisymmetric) with respect to the exchange of spacial and spin coordinate of any two electrons. Hartree accounted for this by nominally applying the Pauli exclusion principle, however, this description is still incomplete in the sense that it does not describe the statistical nature of quantum particles.

2.1.3 Slater determinants

In order to satisfy the antisymmetry principle, a linear combination of Hartree products can be taken. Although the method was first utilised independently by Heisenberg 63 and Dirac, 64 this method is called a *Slater determinant* after Slater. 65 For an N electron system, a Slater determinant is written as

$$\Psi(\mathbf{x_1}, \dots, \mathbf{x_N}) = \frac{1}{\sqrt{N!}} \begin{vmatrix} \chi_i(\mathbf{x_1}) & \chi_j(\mathbf{x_1}) & \dots & \chi_k(\mathbf{x_1}) \\ \chi_i(\mathbf{x_2}) & \chi_j(\mathbf{x_2}) & \dots & \chi_k(\mathbf{x_2}) \\ \vdots & \vdots & \ddots & \vdots \\ \chi_i(\mathbf{x_N}) & \chi_j(\mathbf{x_N}) & \dots & \chi_k(\mathbf{x_N}) \end{vmatrix}$$
(2.11)

where $1/\sqrt(N!)$ is a normalisation factor. This simple mathematical trick ensures antisymmetry since the interchange of two electrons requires the exchange of two rows in the determinant, which changes the sign. Normally the short-hand form, which implicitly includes the normalisation factor and assumes the ordering of electrons is $\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N$, is written as only the diagonal elements of the determinant:

$$\Psi(\mathbf{x}_1, \mathbf{x}_2, \dots, \mathbf{x}_N) = |\chi_i \chi_j \dots \chi_k\rangle \tag{2.12}$$

Slater determinants are completely dependent on the spin orbitals from which it is formed, to within a sign. Therefore, Slater determinants also form an orthonormal set. Additionally, the introduction of antisymmetry into the Hartree product incorporates so-called *exchange correlation*. This means that the motion of two electrons with parallel spin are correlated. However, since the motion of electrons with opposite spin are not correlated, a single determinant wave function is said to be uncorrelated.

2.1.4 The Hartree-Fock approximation

Now that we have a method for describing many-electron wave functions, we can consider the computation of molecular properties. The cornerstone of quantum chemistry is the Hartree-Fock method (HF), otherwise known as the self-consistent field method. The main principle of the HF method is to approximate electron-electron interactions with an average potential. We begin with a single Slater determinant for an N electron system in the ground state:

$$|\Psi_0\rangle = |\chi_1\chi_2\dots\chi_N\rangle \tag{2.13}$$

By applying the variational method to the Schrödinger equation, we hope to find the lowest possible ground state energy, E_0 . One applies the variational principle by choosing a trial wave function (ϕ) dependent on some number of parameters. These parameters are optimised so that that expectation value of the energy is minimised:

$$E_0 \le \langle \phi | \mathcal{H} | \phi \rangle \tag{2.14}$$

The trial wave function minimises E_0 only when $\phi = \Psi_0$, the ground state wave function.

Within the Hartree-Fock approximation, we approximate the full electronic Hamiltonian \mathcal{H} with a related operator \hat{H}_0 :

$$\hat{H}_0 = \sum_{i=1}^{N} \hat{f}(i) \tag{2.15}$$

where $\hat{f}(i)$ is the Fock operator of the i-th electron, defined as

$$\hat{f}(i) = -\frac{1}{2}\nabla_i^2 + \sum_{A=1}^M \frac{Z_A}{r_{iA}} + v^{HF}(i)$$
(2.16)

The first two terms are familiarly the non-interacting one electron Hamiltonian, $\hat{h}(i)$. The third term, $v^{HF}(i)$, is the average potential experienced by each electron in the presence of other electrons.

With these approximations, the quantum problem is now reduced to solving the eigenvalue Hartree-Fock equation of the form

$$\hat{f}(i)\chi(\mathbf{x}_i) = \epsilon_i \chi(\mathbf{x}_i) \tag{2.17}$$

Solving Equation 2.17 directly is computationally very challenging, as there are infinite possible solutions. However in 1951, Roothaan 66 demonstrated that the problem can be simplified by expanding each spin orbital into a linear combination of a known finite number K basis functions:

$$\chi_i = \sum_{\mu=1}^{K} C_{\mu,i} \phi_{\mu} \tag{2.18}$$

where $C_{\mu,i}$ is a weighting coefficient and ϕ_{μ} is a basis function. As K approaches ∞ , the set $\{\phi_{\mu}\}$ becomes more complete and the energy approaches the so-called Hartree-Fock limit, or the exact energy in the Hartree-Fock approximation. One is, however, always limited to a finite number of basis functions, leaving deficiencies in the desired wave function Ψ_0 .

The expansion of spin orbitals into a basis allows Equation 2.17 to be written in terms of the *Roothaan matrix equation*

$$\mathbf{FC} = \mathbf{SC}\varepsilon \tag{2.19}$$

where $\mathbf{F} = \sum_{l,m} \langle \chi_l | \hat{f}(i) | \chi_m \rangle$ is the Fock matrix, $\mathbf{S} = \sum_{l,m} = \langle \chi_l | \chi_m \rangle$ is the orbital overlap matrix. \mathbf{C} is the orbital coefficient matrix, and ε is the diagonal matrix of orbital energies ε_i , which are generally the desire solutions. By performing a transformation of basis to an orthonormal basis, the overlap matrix \mathbf{S} becomes the identity matrix $\mathbb{1}$, and simplifies the problem. Thus, utilising 2.19 reduces the problem to the of diagonalisation \mathbf{F} . Unfortunately, this must be done iteratively, as \mathbf{F} depends on its own solution, hence the name self-consistent field method.

2.1.5 Basis sets

Choosing optimal basis functions can help significantly in terms of determining the ground state wave function Ψ_0 . Quantum chemists rely on the choice of basis sets, defined as the vector space in which an ab initio problem is defined. Basis sets usually refer to the set of one particle functions, which are used to form MOs in a linear combination of atomic orbitals (LCAO-MO) like approach. For a system with N electrons, the LCAO-MO approach gives N/2 occupied orbitals in the ground state. The remaining basis functions in a set are combined to give virtual (unoccupied) orbitals.

Early basis sets were composed of *Slater-type orbitals* (STOs), due to their resemblance to the atom orbitals (AOs) of the hydrogen atom. These are functions of the form

$$\phi_i^{STO}(\zeta, n, a, b, c, x, y, z) = Nr^{n-1}e^{-\zeta r}x^a y^b z^c$$
 (2.20)

where N is a normalisation constant, ζ is a constant related to the effective nuclear charge of the nucleus, r is the distance of the electron from the atomic nucleus, n is a natural number that plays the role of the principle quantum number, and x, y, and z are cartesian coordinates. The angular component $x^ay^bz^c$ describes the shape of the function, such that if a+b+c=0 ϕ_i^{STO} is of s-type; if a+b+c=1, ϕ_i^{GTO} is of p-type, and so forth. Although STOs approximate the long and short range behaviour of atomic orbitals correctly, performing integration with these functions is computationally very demanding, due primarily to the complexity of the integrals involved describing in electron-electron interactions.

$$\phi_i^{GTO}(\alpha, a, b, c, x, y, z) = Ne^{-\alpha r^2} x^a y^b z^c$$
(2.21)

where N is a normalisation constant, α is the orbital exponent coefficient, x, y, and z are cartesian coordinates, r is the radius ($r^2 = x^2 + y^2 + z^2$), and the angular portion is described the same as in an STO. It takes a linear combination of several GTOs to represent the same function as an STO. These linear combinations of GTOS are known as *contracted GTOs* (CGTO) with n GTOs combined as

$$\phi_i^{CTGO}(\alpha, a, b, c, x, y, z) = N \sum_{i=1}^n c_i e^{-\alpha r^2} x^a y^b z^c$$
 (2.22)

where c_i is referred to as the contraction coefficient which describes the weighting of each GTO. Although it requires more GTOs than STOs to accurately describe the atomic orbitals, the integrals can be computed 4-5 times faster, and thus calculations involving GTOs are much more efficient. ⁶⁷

Basis set nomenclature

Standard basis sets are composed of basis functions which represent atomic orbitals and that each basis function is a CGTO composed of several GTOs. A minimal basis set is one in which each AO is represented by a single basis function. To more accurately represent AOs, more basis functions should be used, although basis set size needs to be balanced with computational cost. Larger basis sets are referred to by their cardinal number, the number of basis functions which represent each AO. When two basis functions are used to represent each AO, this is called a double-zeta basis set. If three basis functions represent each AO, this is called a triple-zeta basis set. Generalised, a basis set is N-zeta in size when N basis functions are used per AO.

A *split-valence* basis set is one in which a single basis function is used to represent each core AO, while more basis functions are used to represent the valence AOs. Constructing basis sets in this way can help reduce the computational cost while still accurately representing the electrons which are most important to chemistry.

Additional basis functions are often added to basis sets in order to correctly describe molecular properties. *Polarisation functions* are basis functions which are one or more angular momentum channels greater than the natural electronic configuration of an atom. For example, a single *p*-type

basis function can be added to the minimal basis of a hydrogen atom. Polarisation functions are essential to accurately describe chemical bonding, as the presence of other atoms distorts the spherical symmetry of a single atom's AOs. ⁶⁸ Diffuse functions are basis functions which extend further into space, typically by the inclusion of a very shallow Gaussian function (small ζ exponent). Diffuse functions are necessary to accurately describe anions, very electronegative atoms, and large systems in which NCIs are important.

Commonly used basis sets

A large number of basis sets currently exist in the literature.⁶⁹ While not all basis sets are created equally, we shall briefly describe four of the most commonly used basis sets used in quantum chemistry. (I have only included the first citation for the basis sets. Maybe include more.)

Pople-style basis sets

Perhaps the most utilised basis sets in chemistry are those arising from the group of Pople. 70 These basis sets were defined by fitting to HF wave functions. The earliest of these basis sets are the minimal STO-NG basis sets, where N describes the number of GTOs that go into each contraction.

The practise of using minimal basis sets has diminished significantly as technology has advanced, thus these basis sets are largely considered out of date. It is more common to utilise the split-valence basis sets, denoted as n-ijG or n-ijkG for double and triple zeta split-valence basis sets, respectively. In this system of notation, n represents the number of GTOs that comprise the core AOs, and i, j, k describe the number of GTOs for contractions in the valence AOs. Polarisation functions are denoted either with asterisks or with the specific shell and number of functions which are being added. Diffuse functions are denoted with either a single or double "+", indicating diffuse s and p-type functions for non-hydrogen atoms, and the addition of diffuse s-type functions for hydrogen, respectively. For example, the 6-31+G(d,p) \equiv 6-31+G** double-zeta basis set is one which has: 6 GTOs per core AO, 3 GTOs for the first valence set of AOs, and 1 GTO for the second, along with s and p diffuse functions of the heavy atoms, a single d polarisation function of heavy atoms, and a single p polarisation function of hydrogen atoms.

Correlation consistent basis sets

Post-Hartree-Fock methods (vide infra) are commonly used in quantum

chemistry. In 1989, Dunning⁷¹ identified that the use of basis sets optimised for HF were inappropriate for post-HF methods. The basis sets that came from Dunning and co-workers, which are referred to as "correlation consistent" basis sets are commonly used in, but not limited to, state of the art wave function calculations. These basis sets are said to be correlation consistent as they treat electron correlation (*vide infra*) in a manner which systematically approached the complete basis set limit. Correlation consistent basis sets are denoted as "cc-pVNZ", where N=D,T,Q,5,6,... is the cardinal number of the basis set. These are large sets containing polarisation functions by default and can be additionally augmented with diffuse functions, denoted by "aug." A commonly used basis set is aug-cc-pVTZ, which is a triple-zeta basis set with implicit polarisation functions and specified diffuse functions on all atoms.

Polarisation consistent basis sets

The polarisation consistent basis sets have been developed by Jensen and coworkers. The polarisation consistent basis sets have been developed to systematically complete basis set limit in density-functional theory calculations through the use of higher order polarisation functions. The notation adopted is "pc-X", where X is the cardinal number of the basis set minus one (i.e. X = N-1). Polarisation functions are included by default in these basis sets, and additional diffuse functions can be specified with the same "aug" notation as the correlation consistent basis sets.

Ahlrich basis sets

The last basis sets we will mention are those developed by Ahlrich and coworkers. 73,74 These are the "Def2" basis sets, named as such because they are the second generation of default basis set in the Turbomole quantum chemistry package. 75 Additionally, these basis sets have been developed so that consistent errors are obtained for nearly every element on the periodic table: a unique trait among modern basis sets. The nomenclature for these basis sets is fairly straightforward where either SV is used for split valence, or NZ is used for cardinal number. Addition of polarisation and diffuse functions is specified with a P and D, respectively. For example, Def2-SVP is the basis set of split-valence double-zeta quality with polarisation functions; Def2-TZVP is the triple-zeta basis set with polarisation and diffuse functions.

2.1.6 Post-Hartree-Fock methods

The HF method gives an approximation to the ground state wave function of a molecule for a reasonable computational cost (scaling with N^4 number of basis function). There is however, a lack of the complete description of dynamical electron correlation, ⁷⁶ and thus significant deviations from experimental results can be observed. Dynamical electron correlation is a measure of how much one electron's movement is affected by the presence of other electrons. As described previously, the HF method includes correlation through the average electron field potential term, however this field is in general, not static, thus correlation must be treated directly in order to obtain accurate results. The majority of methods take the HF wave function Ψ_0 as the starting point. Normally, the total energy is obtained by inclusion of an energy term for correlation E_{corr} , which can be defined as

$$E_{corr} = \Xi_{exact} - E_0 \tag{2.23}$$

 $E_{c}orr$ is the difference between the full non-relativistic energy from the Schrödinger equation, Ξ_{exact} , and a reference ground state energy E_{0} , usually the HF energy.

We shall briefly describe two important methods for accounting for electron correlation and obtaining E_{corr} : Møller-Plesset perturbation theory, and the related configuration interaction and coupled cluster theories.

Møller-Plesset perturbation theory

Møller-Plesset (MP) perturbation theory is a special case of Rayleigh-Schödinger perturbation theory in which the Hamiltonian for a system can be approximated by

$$\hat{H} = \hat{H}_0 + \lambda \hat{V} \tag{2.24}$$

where \hat{H}_0 is an unperturbed Hamiltonian, \hat{V} is a small perturbation, and λ is an arbitrary parameter which controls the size of the perturbation. The perturbed wave function and energy are expressed as a power series in λ :

$$\Psi = \lim_{m \to \infty} \sum_{i=0}^{m} \lambda^i \Psi^{(i)}$$
 (2.25)

$$E = \lim_{m \to \infty} \sum_{i=0}^{m} \lambda^i E^{(i)}$$
 (2.26)

The MP method applies perturbations to HF by defining a *shifted* Fock operator \hat{H}_0 and *correlation potential* \hat{V} as

$$\hat{H}_0 = \hat{F} + \langle \phi_0 | (\hat{H} - \hat{F}) | \phi_0 \rangle$$
 (2.27)

$$\hat{V} = \hat{H} - \hat{H}_0 \tag{2.28}$$

where ϕ_0 is the ground state Slater determinant of the Fock operator.

Within this formulation, the zeroth-order energy is the expectation of \hat{H} , which gives the HF energy. The first-order energy is

$$E_{MP1} = \langle \phi_0 | \hat{V} | \phi_0 \rangle = 0 \tag{2.29}$$

by Brillouin's Theorem of singly excited determinants. Thus, the first useful correction occurs at the second order of perturbation, which is known as MP2. Additional orders of perturbation are referred to as MP3, MP4, etc. The MP2 method has been popular in quantum chemistry because it scales with N^5 number of basis functions and is a significant improvement on the treatment of electron correlation compared to HF. One may expect higher order of perturbation theory to more accurately describe a system. Practically however, the expansions used in MPN theory do not converge smoothly to a limit with higher order of perturbation.⁷⁷ As a result, for molecular properties calculated with MP3 or higher are not guaranteed to give more accurate results than MP2.

Configuration interaction and coupled cluster theory

The solutions to the HF method give a single determinant wave function which only describes the ground state electronic configuration. Configuration interaction (CI) is a post-HF method which describes a linear combination of Slater determinants to more accurately represent a system's wave function. The additional Slater determinants represent excited electronic configurations and can be singly excited (S), doubly excited (D), and so forth. This is represented as follows:

$$|\Psi\rangle = (1 + \sum_{j=1}^{N} C_j) |\phi_0\rangle$$
 (2.30)

where C_j are operators which describes the j-th excitations of electrons. If all possible excitations are included in the CI equation, this is referred to as

full CI (FCI). Extending FCI to an infinite basis set gives the exact solution to the Schrödinger equation.

Coupled cluster (CC) theory 78 is a similar approach to CI, but uses the so-called $exponential\ ansatz$

$$|\Psi\rangle = e^{\hat{T}} |\phi_0\rangle \tag{2.31}$$

where \hat{T} is the cluster operator, defined by *n*-electron excitation operators \hat{T}_n :

$$\hat{T} = \hat{T}_1 + \hat{T}_2 + \hat{T}_3 + \dots \tag{2.32}$$

Within the exponential ansatz, $e^{\hat{T}}$ is usually truncated and expanded in a Taylor series. For example, truncation at the \hat{T}_2 excitation operator gives

$$|\Psi\rangle = e^{\hat{T}_1 + \hat{T}_2} |\phi_0\rangle$$

$$= (1 + \hat{T}_1 + \hat{T}_2 + \frac{1}{2!}\hat{T}_1^2 + \hat{T}_1\hat{T}_2 + \frac{1}{2!}\hat{T}_2^2 + \dots) |\phi_0\rangle$$
(2.33)

Considering both CI and CC with single and double excitation (CISD and CCSD), the wave functions will include similar excitations, however inclusion of cross terms $(\hat{T}_1\hat{T}_2)$ in CCSD implicitly includes higher excitation levels. Additionally, the use of the exponential operator makes the CC formulation size consistent, which is the largest short coming of the CI method. Size consistency refers to the additivity of energies for an ensemble of molecules. That is, for a pair of molecules A and B, their energies must follow the relation

$$E_{AB}(r \to \infty) = E_A + E_B \tag{2.34}$$

Size consistency is a necessary requirement of a theoretical treatment to treat systems of molecules accurately. It is for this reason that CC has superseded CI as the dominant highly correlated method in quantum chemistry.

The inclusion of higher order excitations becomes decreasingly important with degree of excitation; however, the inclusion of triples is often found to be necessary for the accurate description of electron correlation (i.e. CCSDT). The computation of triples is prohibitively expensive in all but the simplest of systems, thus approximations based on perturbation theory are often used in substitution. The most commonly used perturbative triples method is CCSD(T), where the parenthesis indicate the use of perturbative arguments.

Note also that traditionally, the use of CCSD(T) implies excitation of only the valence electrons, unless otherwise stated.

CCSD(T) is commonly referred to as the *gold standard* in quantum chemistry and is often used to obtain benchmark quality results for thermochemistry and NCIs.⁷⁹ However, CCSD(T) scales with N^7 number of basis functions, and is thus significantly more computationally expensive than HF or MP2, restricting its application to small systems of molecules.

2.1.7 The complete basis set limit

Complete basis set extrapolation

In accordance with the variational principle, the energy obtained by a particular method will always be greater than or equal to the exact energy. The exact energy can only be achieved with an infinite basis set, a value known as the *complete basis set* (CBS) limit. ⁸⁰ Since this is computationally infeasible, specific tricks have been developed to approximate the CBS limit. Specifically, molecular properties calculated using the HF and post-HF methods have been shown to asymptotically approach the CBS limit in a smooth manner when appropriate basis sets are used. Therefore, to obtain results estimating a molecular property at the CBS limit $(Y(\infty))$, properties can be fit to three-parameter ^{81,82} or two-parameter functions: ^{83,84}

$$Y(x) = Y(\infty) + Ae^{-x/B}$$
(2.35)

$$Y(x) = Y(\infty) + A/x^3 \tag{2.36}$$

where the molecular property as a function of basis set cardinal number Y(x) is fit using parameters A and B. Typically calculations of this nature are performed using the correlation consistent basis sets (cc-pVNZ), however there is evidence that the polarisation consistent basis sets (pc-X) more rapidly approach the CBS limit for some molecular properties. ⁸⁵ The true gold standard in quantum chemistry is referred to as CCSD(T)/CBS, which typically means CCSD(T) with complete basis set extrapolation with aug-cc-pVNZ basis sets, where N=D, T, Q, or 5. Although extrapolation is useful for approximating highly accurate results, there is an inherent amount of uncertainty associated with the final fitted results, which may be unclear from the nomenclature.

Explicit correlation methods

A new technique which is gaining popularity among post-HF methods is the inclusion of so called *explicit correlation*. ^{86,87} The introduction of additional functions dependent on inter-electronic distance coordinates allows for explicit correlation of electrons. ⁸⁸ As a result, the dynamical correlation of electrons is treated more accurately with reduced basis sets, therefore accurate results can be achieved at a reduced computational cost. Basis set extrapolation can also be performed on explicitly correlated results: this is quickly become the standard approach. ⁸⁹

2.1.8 Composite quantum chemistry methods

In order to calculate thermochemical and kinetic properties that are within a sub-kcal mol⁻¹ range of experiment, multistep ab initio procedures which are referred to as *composite methods* have been developed. ⁹⁰ These procedures work by including important energy terms which contribute to molecular properties. Generally, composite methods make use of a combination of low correlation methods with large basis sets and high correlation methods with small basis sets, as is illustrated in Figure 2.1. Some of the relevant energy terms include: core-valence, relativistic, spin-orbital, Born-Oppenheimer, and zero-point vibrational energy corrections. There exist many composite methods, each of which makes use of a variety of quantum mechanical (QM) methods and different basis set extrapolation techniques in order to best approximate energy terms which are relevant, with the ultimate goal of achieving the exact energy of a system. In our work, we have made use of several composite methods including: the G4 and G4(MP2) methods, 91,92 CBS-QB3 and CBS-APNO methods, 93-95 and the W1BD method. 96 A description of these methods will be provided in Chapter 4.

2.1.9 Density-functional theory

Density-functional theory (DFT) is the most popular quantum chemical method applied to date. It relies on the two Hohenberg-Kohn theorems, the first of which states that there exists a unique electron density ρ that defines the properties of a many-electron system. The second theorem defines an energy functional of the electron density and demonstrates that the correct ground state electron density minimises the energy functional through the variational theorem. ^{97,98} These theorems alone do not provide the solutions to the Schrödinger equation.

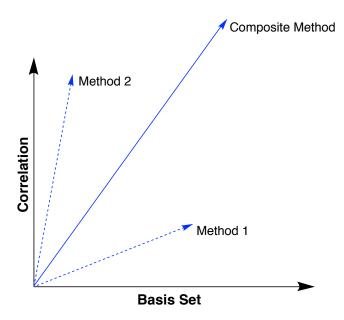


Figure 2.1: Schematic representation of a quantum mechanical composite method. The exact energy can only be achieved at the limits of an infinite basis set and complete correlation. Using a combination of Method 1 (low correlation/large basis set) and Method 2 (high correlation/small basis set), the Composite method approaches the exact energy.

It wasn't until the formulation of Kohn-Sham DFT 99 that the theory began gaining ground as a useful quantum theory. Kohn-Sham DFT scales formally with N^3 number of electrons 76 which is better than HF by a factor of N. In addition, DFT is a complete theory like FCI; however, there is no straightforward way to determine the correct functionals of the electron density as the exact form of the functionals is unknown. Nonetheless, the drive for the development of the correct density-functional has been one of the main endeavours in quantum chemistry in the last two decades.

The framework behind conventional DFT is built into the description of the full energy functional E:

$$E[\rho] = T_{ni}[\rho] + V_{ne}[\rho] + V_{ee}[\rho] + \Delta T[\rho] + \Delta V_{ee}[\rho]$$
 (2.37)

where T_{ni} is the kinetic energy of non-interacting electrons, V_{ne} is the potential of nuclear-electron interactions, and V_{ee} is the classical electron-electron repulsion. The last two terms are collectively referred to as the exchange-correlation (XC) functionals, where ΔT is the dynamical correlation term,

and ΔV_{ee} is the non-classical correction to electron-electron repulsion. All the functionals, except the XC functionals have an exact form. It is therefore the XC functionals in which there is currently empiricism.

The ultimate goal in describing XC functionals is to find the "correct" XF functional which gives the exact energy of a system from the electron denisty. At this point, this must be done using approximations, for which there are several degrees of complexity. These approaches follow a hierarchical scheme, commonly referred to as the "Jacob's ladder" of DFT. ¹⁰⁰ The first rung represents the simplest approximation which is known as local-density approximations (LDAs), which approximate the exchange-correlation density at a given point by the electron density at that same point. The form of these functionals is:

$$E_{XC}^{LDA} = \int \rho(\mathbf{r}) \varepsilon_{XC}(\rho(\mathbf{r})) dr \qquad (2.38)$$

where $\varepsilon_{XC}(\rho(\mathbf{r}))$ is the exchange-correlation energy per particle (energy density) of a uniform electron gas of density $\rho(\mathbf{r})$. This approximation is overly simple and applies only when the electron density if constant at all points, and are thus not generally applied in chemical problems. Nonetheless, LDA based approaches are commonly employed in solid state physics.

The second rung on the ladder corresponds to generalised-gradient approximation (GGA) based functionals, which are still amongst some of the most popular density-functionals. GGAs depend on both the electron density and the gradient of the electron density at a point:

$$E_{XC}^{GGA} = \int \rho(\mathbf{r}) \varepsilon_{XC}^{GGA}(\rho(\mathbf{r}), \nabla \rho(\mathbf{r})) dr$$
 (2.39)

where, $\varepsilon(\rho(\mathbf{r}), \nabla \rho(\mathbf{r})) dr$ is the energy density associated with a given GGA. GGA functionals provide a substantial improvement over LDAs, and most are constructed so that they correct the LDA energy:

$$\varepsilon_{XC}^{GGA}(\rho(\mathbf{r}), \nabla \rho(\mathbf{r})) = \varepsilon_{XC}^{LDA}(\rho(\mathbf{r})) dr + \Delta \varepsilon_{XC} \left(\frac{\nabla \rho(\mathbf{r})}{\rho^{4/3}(\mathbf{r})} \right)$$
(2.40)

A step above GGAs on the third rung of the ladder are meta-GGAs, which depend on the electron density, as well as the first derivative of electron density at a point, and the kinetic-energy density, $\tau(\mathbf{r})$, defined as:

$$\tau(\mathbf{r}) = \sum_{i}^{occupied} \frac{1}{2} |\nabla \chi_i(\mathbf{r})|^2$$
 (2.41)

where $\chi_i(\mathbf{r})$ are the self-consistently determined Kohn-Sham orbitals. Meta-GGAs improve upon the accuracy of GGAs at a comparable cost.⁷⁶

The XC functionals described up to this point (LDAs, GGAs, meta-GGAs) depend only on the electron density and derivatives of the electron density. The fourth and fifth rungs of the ladder improve upon the prior functionals by inclusion of terms dependent on additional properties. While this approach improves upon the accuracy of these functionals, it comes with an increase in computational cost. On the fourth rung sit functionals which depend to some percentage on the HF exact exchange. When the ratio of HF exchange is fixed, these functionals are termed hybrid functionals. Alternatively, functionals are said to be range-separated corrected if a different amount of exact-exchange to describe long and short-range behaviours. In the cases of hybrid and range-separated functionals, the added computational cost comes from the calculation of the HF exact exchange.

Alternatively, one can describe the fourth rung functionals as the depending upon the properties of the occupied molecular orbitals. The fifth rung then, is said to depend on the properties of unoccupied molecular orbitals. These functionals are typically referred to as double-hybrids, and incorporated correlation energy from a post-HF method, typically MP2. ¹⁰¹ Double-hybrid DFT methods are once again more accurate than the lower rung methods, however, calculating the MP2 correlation energy is considerably more computationally demanding than traditional DFT approaches. Therefore, double-hybrid DFT methods have not gained popularity in the literature.

There are many published XC functionals. Fortunately, there is a fairly standard system of nomenclature, such that density functionals are described as exchange functional-correlation functional. The most commonly used density functional is the B3-LYP, which uses the 3-parameter hybrid exchange functional of Becke, ¹⁰² and the correlation functional of Lee, Yang, and Parr. ¹⁰³ There are also standalone functionals which have built in exchange and correlation functionals. A common example of these are the Minnesota family of functionals from the Truhlar group. ^{104,105}

Aside from the problem of choosing density-functionals, solving DFT is computationally very similar to the HF method. Within Kohn-Sham (KS) DFT, we define a fictitious system of non-interacting electrons with the same electron density as the real system. This is achieved by the use of a Hamiltonian in which there is an effective local potential, $V_s(\mathbf{r})$:

$$\hat{H}_s = -\frac{1}{2} \sum_{i}^{N} \nabla_i^2 |\sum_{i}^{N} V_S(\mathbf{r}_i)$$
 (2.42)

The ground state wave function of this non-interacting Hamiltonian is represented by a single Slater determinant with spin orbitals (χ) , completely analogous to the HF problem. These spin orbitals, referred to as Kohn-Sham orbitals are determined by

$$\hat{h}_i^{KS} \chi_i = \varepsilon_i \chi_i \tag{2.43}$$

where the one-electron Kohn-Sham operator \hat{h}^{KS} is defined as

$$\hat{h}_i^{KS} = -\frac{1}{2}\nabla^2 + V_s(\mathbf{r}) \tag{2.44}$$

It is crucial to realise that this procedure does not give us the exact energy of a system, but rather is used to determine an electron density which represents our real system. The connection between this fictitious system comes from the chose of the effective potential such that the density of our real system is a result of summing over the squared moduli of the KS orbitals:

$$\rho(\mathbf{r}) = \sum_{i} |\chi_i|^2 \tag{2.45}$$

Once again in analogy to HF theory, on applies the variational principle to minimise the total energy functional in Equation 2.37 with respect to χ . The effective potential which variationally minimises the energy is given by 106

$$V_{s}(\mathbf{r}) = \frac{\delta J[\rho]}{\rho(\mathbf{r})} + \frac{\delta E_{XC}[\rho]}{\delta \rho(\mathbf{r})} + \sum_{A}^{M} \frac{Z_{A}}{r_{iA}}$$

$$= \int \frac{\rho(\mathbf{r}_{2})}{r_{12}} + V_{XC} + \sum_{A}^{M} \frac{Z_{A}}{r_{iA}}$$
(2.46)

where the first term describes the Coulombic potential between two electrons, the last term is the potential between the electron and each nucleus. The middle term is once again the unknown XC potential. The electron density obtained from the fictitious system of non-interacting particles is finally used in Equation 2.37 to find the total energy of the system. Since

 $V_s(\mathbf{r})$ depends on the electron density, these equation must be solvent iteratively, as with HF theory. Note however, that if the exact form of $E_{XC}[\rho]$ was known, this method would give the exact ground state electron density of the system, and thus the exact energy.

Challenges for density-functional theory methods

Pure DFT has low computational cost and potentially good accuracy, hence its popularity as a quantum chemical treatment. However, there are several problems which common DFT methods experience that lead to erroneous results in many cases. 107 It is well established that traditional DFT methods completely fail at describing non-covalent interactions. 108 This shortcoming leads to poor descriptions of chemistry beyond equilibrium geometries, including transition states. Fortunately, there are several methods which can correct for this problem, commonly through the addition an energy correction term E_{disp} to the DFT energy E_{DFT} , as

$$E_{tot} = E_{DFT} + E_{disp} (2.47)$$

It is common to employ the empirical D3 pair-wise correction of Grimme, ¹⁰⁹ paired with of the Becke-Johnson damping functions, ¹¹⁰ denoted as D3(BJ). This correction works by calculating the dispersion interactions between all pairs of atoms A and B separated by distance R_{AB} , with the following equation:

$$E_{disp} - \sum_{A>B} \frac{C_6^{AB}}{R_{AB}^6} f_6(R_{AB}) + s_8 \frac{C_8^{AB}}{R_{AB}^8} f_8(R_{AB})$$
 (2.48)

where C_6 and C_8 are dispersion coefficients, s_8 is an empirically determined scaling parameter, and f_n are the damping functions which limit the range of dispersion correction, avoiding near singularities at small R_{AB} . Another approach to correcting for dispersion is to add parameters directly to the functional, as is the case in the Minnesota functionals. ^{104,104} Both of these empirical corrections have the benefit of adding negligible computational time, but must be parametrised for each DFT method with which they are employed.

Another striking issue with DFT is the unphysical ability of an electron to interact with itself, termed *self-interaction error*. This is most obvious in what is known as *delocalisation error*, which is a result of many-electrons interacting with themselves, or many-electron self-interaction error. In HF theory, self-interaction error is exactly cancelled, thus DFT methods which

have a high portion of HF exchange in their formulation are able to account for this issue. Consider for a moment a one electron system: there should be exactly zero electron correlation. In terms of the energy functionals shown in Equation 2.37, the electronic repulsion term $V_{ee}[\rho]$ should cancel exactly with the XC term $(V_{ee}[\rho] = -E_{XC}[\rho])$. Unfortunately, all pure DFT methods fail to reproduce this expected behaviour. An obvious manifestation of delocalisation error is the incorrect treatment of charge-transfer in intramolecular interactions, 111,112 as well as in transition state complexes. Even for the simplest HAT reaction $H_2 + H^{\bullet} \longrightarrow H^{\bullet} + H_2$, the calculated barrier height is underestimated by 8–9 kcal mol⁻¹ using a GGA functional. Charge-transfer occurs when a fraction of an electron is transferred between molecular entities. Specifically, charge-transfer is mistreated at longer ranges, thus either high percentage exact exchange hybrid functionals, or range-separated functionals are suggested for systems in which charge-transfer may occur.

As is the case for most experimental methods, identifying the correct theoretical methods requires the careful consideration of the problem at hand. Choosing a DFT based method requires calibration, however, once a method has been tested and is known to provide reasonably accurate results, DFT methods have the ability to help understand chemical problem with relatively low computational costs.

2.2 Applying theory to chemical problems

2.2.1 Geometry optimisation

All QM methods depend parametrically on the geometry of a molecular system. That is the electronic energy of a system depends on the positions of the nuclei. While the wave functions can describe any arbitrary geometry, we are typically only interested in certain geometries of a molecule. These geometries of interest are normally stationary states along a the potential energy surface (PES) of a system, that is, points where the gradient of energy with respect to nuclear coordinates is zero. Therefore, we perform geometry optimisation calculations to determine these points.

Molecular systems have complex PESs. For a non-linear molecule, the nuclear PES has 3N-6 dimensions, where N is the number of nuclei present. 114 In geometry optimisation, we seek the local minima (reactants, products, or intermediates) and local maxima (TS complexes). Consider only local minima for a moment. Often complex molecules have more than one possible conformation, and each conformation represents a different local minimum

along the PES. It is therefore important to ensure the correct conformation, typically the lowest energy structure (global minimum), is used when approaching chemical problems.

In order to efficiently perform geometry optimisation, numerical analysis techniques are employed. All geometry optimisation methods follow the same general framework. 115 First, energy and necessary derivatives are computed from an initial geometry. Second, the geometry is modified to step towards the nearest stationary state. And last, some test is performed to determine if the new geometry is near enough to the stationary state along the PES. The most efficient method to do this is the *Newton method*, in which the energy is expanded in a Taylor series (truncated at the second order point) about the current point, \mathbf{x}_0 :

$$E(\mathbf{x}) = E_0 + \mathbf{g}_0 \Delta \mathbf{x} + \frac{1}{2} \Delta \mathbf{x} \mathbf{H}_0 \Delta \mathbf{x}$$
 (2.49)

where E_0 , \mathbf{g}_0 , and \mathbf{H}_0 are the energy, gradient (Jacobian), and second derivative (Hessian) at point \mathbf{x}_0 , and $\Delta \mathbf{x} = x_i - x_0$. The aim of the Newton method is to minimise the gradient of the Taylor expansion, $\mathbf{g}(\mathbf{x})$, such that

$$\mathbf{g}(\mathbf{x}) = \mathbf{g}_0 + \mathbf{H}_0 \Delta \mathbf{x} \tag{2.50}$$

Solving for $\Delta \mathbf{x}$ gives the so-called Newton step that leads to minimisation:

$$\Delta \mathbf{x} = -\mathbf{H}_0^{-1} \mathbf{g}_0 \tag{2.51}$$

The analytic computation of the Hessian is very expensive, especially for large systems. Therefore, to simply the problem at the beginning of geometry optimisation, the Hessian matrix is approximated and updated at each step in the optimisation, using clever algorithms. ¹¹⁵ This is called the *quasi-Newton method*, and is the default optimisation routine in the Gaussian ¹¹⁶ quantum chemistry package, as well as many other quantum chemistry packages.

Some additional caution must be taken in optimising molecular structures. Normal algorithms which optimise structures stop when the gradient of energy is sufficiently close to zero; however, often PES can be flat or very shallow in regions and structures that are not fully optimised can be obtained. To avoid this, geometries are always subject to molecular vibration analysis.

2.2.2 Molecular vibrations

The computation of molecular vibrations can be performed simply given a set of molecular coordinates. 117 Assuming a non-linear molecule, we start with 3N-6 internal coordinates which are non-coupled (orthogonal). We then apply the *harmonic approximation*, in which we assume each normal mode follows Hooke's Law

$$F = kx (2.52)$$

where F is the force, k is the force constant, and x is the displacement along one normal mode's coordinates. This approximation assumes the PES along the normal mode is parabolic, which in general is not true, but is a good approximation near the minima. Deviations from this approximation are known as anharmonicity. In practise, however, at normal temperatures ($\sim 298 \mathrm{K}$) the harmonic approximation is sufficient to describe molecular vibrations as displacements are assumed to be small.

Typically to obtain molecular frequencies, one computes the mass-weighted Hessian matrix elements F_{ij}

$$F_{ij} = \frac{1}{\sqrt{m_i m_j}} mathb f H_i j \tag{2.53}$$

where the partial derivatives of internal coordinates x_i of the potential energy U are taken for 3N atoms with mass m. One then seeks to diagonalise this $3N \times 3N$ matrix to obtain eigenvalues λ_i , which describe the force constant of each normal mode. The harmonic frequencies ν_i are then obtained by

$$\nu_i = \frac{\sqrt{\lambda_i}}{2\pi} \tag{2.54}$$

and the lowest 6 modes are then discarded to account for 3N-6 normal modes. These lowest energy modes generally correspond the internal rotations, and thus must be discarded to correctly obtain thermochemical corrections.

From these frequencies, the zero-point vibrational energy (ZPE, E_{ZPE}) is calculated:

$$E_{ZPE} = \sum_{i=1}^{3N-6} \frac{h\nu_i}{2} \tag{2.55}$$

The ZPE is an important quantum correction to the classical potential, giving the electronic potential energy

$$U = E_{elec} + E_{ZPE} \tag{2.56}$$

where E_{elec} is the QM electronic energy.

If a normal mode describes a non-minimum along the PES, the energy gradient will be negative (imaginary) instead of positive. Only energy maxima or saddle-points (TS structures) should have a single imaginary mode. Therefore, if a non-TS molecular structure calculation yields one or more imaginary modes, the geometry optimisation has yielded a structure which is not at minimum on the PES. In this situation additional steps must be taken to find a corrected structure.

2.2.3 Thermochemistry

Up until this point we have been viewing molecules from a microscopic perspective; however, this is not useful for describing properties of bulk systems. Fortunately, fundamental statistical thermodynamics can be used to approximately describe a system in bulk. 118,119 We approximate our system as an ensemble of non-interacting particles: the ideal gas. Within statistical thermodynamics, the fundamental starting point is the partition function Q, 120 from which all thermodynamic properties can be calculated. For our ensemble, the molecular partition function is

$$Q = \sum_{I} e^{\varepsilon_j/k_B T} \tag{2.57}$$

where a Boltzmann distribution of j energy states ε is taken at temperature T, and k_B is the Boltzmann constant. All calculations herein are defined under conditions of temperature T=298.15 K and pressure P=1 atm.

Normally, the molecular partition function is decomposed into contributions from translational, vibrational, rotational, and electronic motion:

$$Q = q_{trans}q_{vib}q_{rot}q_{elec} (2.58)$$

The equation describing the translational partition function q_{trans} is

$$q_{trans} = \left(\frac{2\pi m k_B T}{h^2}\right)^{3/2} \frac{k_B T}{P} \tag{2.59}$$

where m is the mass of the molecule, h is Planck's constants.

The vibrational partition function q_{vib} depends on the contributions of each of K vibrational modes. Only the 3N-6 (or 3N-5 for linear molecules) real vibrational modes of a molecule are considered, and imaginary frequencies are ignored. Therefore, for molecules which posses an imaginary frequency this thermodynamic analysis is invalid. TS complexes do posses a single imaginary frequency which is ignored, as it is assumed to not contribute to the overall vibrational partition function as no formal bond is said to be formed between acceptor-donor system. (I'm not 100% sure about this) Each vibrational mode has a characteristic vibrational electronic temperature, $\Theta_{\nu,K} = h\nu/k_B$, and the partition function is

$$q_{vib} = \prod_{K} \frac{e^{-\Theta_{\nu,K}/2T}}{1 - e^{-\Theta_{\nu,K}/T}}$$
 (2.60)

The rotational partition function depends on the geometry of a system. For a single molecule $q_{rot}=1$. For a linear molecule, the rotational partition function is

$$q_{rot} = \frac{1}{\sigma_r} \left(\frac{T}{\Theta_r} \right) \tag{2.61}$$

where σ_r is the symmetry number for rotation which depends on the molecular symmetry, and $\Theta_r = h^2/8\pi^2 I k_B$. I is the moment of inertia. Finally, for a non-linear polyatomic molecule, the rotational partition function is

$$q_{rot} = \frac{\sqrt{\pi}}{\sigma_r} \left(\frac{T^{3/2}}{\sqrt{\Theta_{r,x}\Theta_{r,y}\Theta_{r,z}}} \right)$$
 (2.62)

where $\Theta_{r,x}$, $\Theta_{r,y}$, and $\Theta_{r,z}$ describe contributions of the moment of inertia in each of the x, y, and z-planes.

Finally, we make an important assumption that electronic contributions are assumed to exist in only the ground state, as excited states are generally safely assumed to be much larger than k_BT in energy. The full electronic partition function is

$$q_{elec} = \sum_{i=0} \omega_i e^{-\epsilon_i/k_B T} \tag{2.63}$$

where ω is the degeneracy of an energy level with energy ϵ . Applying our assumption, and by setting the ground state energy $\epsilon_0 = 0$, our problem simplifies dramatically, such that $q_{elec} = \omega_0$, which is simply the spin multiplicity of the molecule.

We now have all the information needed to calculate the thermodynamic quantities we are interested in. In chemistry we are concerned with the Gibbs free energy G, which is defined by the entropy S and enthalpy H as

$$G = H - TS \tag{2.64}$$

From each of the partition functions, the entropy of a system with N moles, $S_{tot} = S_{trans} + S_{vib} + S_{rot} + S_{elec}$, is calculated using the relation

$$S = Nk_B + Nk_B \ln\left(\frac{Q}{N}\right) + Nk_B T \left(\frac{\partial \ln Q}{\partial T}\right)_V$$
 (2.65)

Similarly, the internal energy of a system, $E_{int,tot} = E_{int,trans} + E_{int,vib} + E_{int,rot} + E_{int,elec}$, is given by the relation

$$E_{int} = Nk_B T^2 \left(\frac{\partial \ln Q}{\partial T}\right)_V \tag{2.66}$$

Finally, the enthalpy is obtained from

$$H_{tot} = E_{int.tot} + k_B T (2.67)$$

Using very simple statistical thermodynamic arguments, the properties of a bulk system are easily computed. It is important to emphasise that these results are for particles in the gas phase, thus additional steps must be taken if one desires to compare results to experiments performed in solvent.

2.2.4 Modelling solvent

It is in principle possible to include solvent molecules explicitly in QM calculations: this is in practise, extremely cost prohibitive. In order to approximate the important contributions of solvation, so-called *implicit continuum solvent models* are generally employed. ^{76,121} Mathematically, one describes this as

$$\hat{H}^{tot}(\mathbf{r}_m) = \hat{H}^{mol}(\mathbf{r}_m) + \hat{V}^{mol+sol}(\mathbf{r}_m)$$
(2.68)

where a perturbation $\hat{V}^{mol+sol}$ dependent only on the coordinates of the solute (\mathbf{r}_m ; thus implicit) is applied to the Hamiltonian of the solute. The perturbation term is composed of interaction operators which contribute to the net free energy:

$$G_{solv} = G_{cavity} + G_{electrostatic} + G_{dispersion} + G_{repulsion} + G_{solv \ kinetic}$$
 (2.69)

where the total solvation free energy G_{solv} contains terms from: the formation of a solvation cavity G_{cavity} , the electrostatic interactions between solvent and solute $G_{electrostatic}$, the dispersion interactions between solvent and solute $G_{dispersion}$, the QM exchange repulsion between solvent and solute $G_{repulsion}$, and the movement of solvent molecules $G_{solv\ kinetic}$.

A widely used model for solvation comes from the Truhlar group, and is known as SMD. 122 The main parameter in implicit solvent models is the solvent dielectric constant (ε) with contributions from surface tension and the solvent-solute interface. SMD also includes terms which depend on the electron density of the solute. While many other implicit solvent models require the use of the same QM method as they were parametrised, 123 SMD is a universal model which was parametrised using several QM methods. Therefore, it does not require the use of a specific QM method and can be applied broadly in both single point energy and geometry optimisation calculations.

2.2.5 Rate constants and transition state theory

In the discussion of chemical kinetics, the rate (r) of a bimolecular reaction

$$a A + b B \Longrightarrow c C + d D$$
 (2.70)

is determined by the rate law, which can generally be described as

$$r = \frac{d\mathbf{C}}{dt} = \frac{d\mathbf{D}}{dt} = k[A]^a [B]^b \tag{2.71}$$

where k is the rate constant, t is time, A, B, C, and D are chemical species with stoichiometric coefficients a, b, c, and d, and k is the rate constant. Computational chemistry is in general, not useful for determining rate laws: this must be done experimentally. Where computational studies can be useful, is in determining reaction mechanisms, and how the reaction barrier height can be altered. In doing so, we focus entirely on k.

Most chemists are intimately familiar with the phenomenological $Arrhenius\ equation$

$$k_{Arr} = Ae^{-E_a/RT} (2.72)$$

where A is a constant, R is the gas constant, and E_a is the *activation* energy, which is an experimental measure of the reaction barrier height. This equation dates back to the 1880s, when Arrhenius noticed that the

reactions depended more heavily on temperature than was intuitive, and thus introduced the A constant, known often as the Arrhenius pre-factor. ¹²⁴ The Arrhenius pre-factor is an empirical measure of how factors other than kinetic energy affect the rate constant. From the perspective of theory, Equation 2.72 has little meaning as the parameters are empirical. Thus, to study rate constants theoretically we must turn to transition state theory.

Transition state theory

The study of transition state theory (TST) originates in the 1930s, and was developed primarily by Eyring. ^{124,125} In TST we focus on the TS complex, which is defined as a transient species which exists at the top of the energy barrier of a reaction. If we consider the same reaction in Equation 2.70, and set all the coefficients to 1, then TST states the reaction proceeds in two steps, the first of which includes a quasi-equilibrium between the reactants and TS complex

$$A + B \rightleftharpoons AB^{\ddagger} \rightleftharpoons C + D$$
 (2.73)

with an equilibrium constant (K_c^{\ddagger}) expression

$$K_c^{\dagger} = \frac{[AB^{\dagger}]/c^0}{[A]/c^0[B]/c^0}$$
 (2.74)

where c^0 is the standard-state concentration (normally taken to be 1 M).

In TST, we define the TS complex to exist throughout a small region of width δ above the reaction barrier (Figure 2.2). From the second step of the reaction in Equation 2.73, we can define a reaction rate dependent on the concentration [AB[‡]] and v_c , a factor which defines the frequency with which the complexes proceed over the barrier:

$$r = v_c[AB^{\ddagger}] \tag{2.75}$$

From Equations 2.70 and 2.73, we now have two equivalent expressions for the reaction rate, which allows us to derive the following

$$r = k[A][B] = v_c[AB^{\ddagger}]$$
(2.76)

and solving Equation 2.74 for $[AB^{\ddagger}]$ results in

$$r = v_c \frac{[\mathbf{A}][\mathbf{B}]K_c^{\ddagger}}{c^0} \tag{2.77}$$

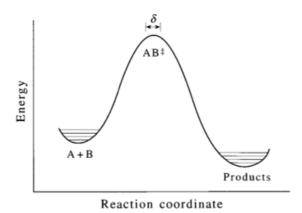


Figure 2.2: A reaction coordinate diagram for the reaction of Equation 2.73. The TS complex is defined to exist in the small region δ above the reaction barrier. Figure taken from Reference 124.

or

$$k = \frac{v_c K_c^{\ddagger}}{c^0} \tag{2.78}$$

We must now invoke the statistical thermodynamics to make sense of Equation 2.78. We can rewrite the equilibrium expression K_c^{\ddagger} in terms of partition functions of each molecular species:

$$K_c^{\ddagger} = \frac{[AB^{\ddagger}]/c^0}{[A]/c^0[B]/c^0} = \frac{(q^{\ddagger}/V)c^0}{(q_A/V)(q_b/V)}$$
 (2.79)

where V is the volume, and q_A , q_B , and q^{\ddagger} are the partition functions of A, B, and AB^{\ddagger} , respectively.

Since we have defined the reaction to be occurring with one degree of freedom, the translational partition function q_{trans} can be defined as

$$q_{trans} = \frac{\sqrt{2\pi m^{\ddagger} k_B T}}{h} \delta \tag{2.80}$$

where m^{\ddagger} is the mass of the TS complex. The partion function of the TS complex can be written as the product $q^{\ddagger} = q_{trans}q_{int}^{\ddagger}$, where the second term accounts for all remaining degrees of freedom of the TS complex. We can use this and rewrite Equations 2.79 and 2.78 as

$$K_c^{\dagger} = \frac{\sqrt{2\pi m^{\dagger} k_B T}}{h} \delta \frac{(q_{int}^{\dagger}/V)c^0}{(q_A/V)(q_b/V)}$$
(2.81)

and

$$k = v_c \frac{\sqrt{2\pi m^{\ddagger} k_B T}}{hc^0} \delta \frac{(q_{int}^{\ddagger}/V)c^0}{(q_A/V)(q_b/V)}$$
 (2.82)

We are now left with the two terms v_c and δ which are ill-defined. However, the product of these two terms is the average speed at which the TS complex crosses the barrier, $\langle u_{TS} \rangle = v_c \delta$. A Maxwell-Boltzmann distribution is used to calculate the value of $\langle u_{TS} \rangle$:

$$\langle u_{TS} \rangle = \left(\frac{m^{\ddagger}}{2\pi k_B T}\right)^{1/2} \int_0^\infty u e^{-m^{\ddagger} u^2 / 2k_B T} du = \left(\frac{m^{\ddagger}}{2\pi k_B T m^{\ddagger}}\right)^{1/2}$$
 (2.83)

Substituting Equation 2.83 into Equation 2.82 for $v_c\delta$ yields

$$k = \frac{\sqrt{k_B T}}{hc^0} \frac{(q_{int}^{\dagger}/V)c^0}{(q_A/V)(q_b/V)} = \frac{k_B T}{hc^0} K_c^{\dagger}$$
 (2.84)

Now, define the standard Gibbs free energy of activation $(\Delta^{\ddagger}G^{0})$ to be the change in Gibbs free energy in going from reactants to TS. The thermodynamical expression is

$$\Delta^{\ddagger} G^0 = -RT \ln K_c^{\ddagger} \tag{2.85}$$

which can be substituted into Equation 2.84

$$k = \frac{k_B T}{hc^0} e^{-\Delta^{\ddagger} G^0/RT} \tag{2.86}$$

The standard Gibbs free energy of activation can be expressed in terms of enthalpy and entropy as

$$\Delta^{\ddagger} G^0 = \Delta^{\ddagger} H^0 - T \Delta^{\ddagger} S^0 \tag{2.87}$$

which, upon substitution gives the equation

$$k = \frac{k_B T}{hc^0} e^{-\Delta^{\ddagger} S^0/R} e^{-\Delta^{\ddagger} H^0/RT}$$
 (2.88)

At this point, we can draw a direct comparison to the Arrhenius equation (Equation 2.72) by expressing E_a in terms of $\Delta^{\ddagger}H^0$ and A in terms of $\Delta^{\ddagger}S^0$.

We must differentiate the natural logarithm of Equation 2.84, as well as Equation 2.72 (assuming that A is independent of temperature):

$$\frac{d\ln k}{dT} = \frac{1}{T} + \frac{d\ln K_c^{\ddagger}}{dT} \tag{2.89}$$

$$\frac{d\ln k_{Arr}}{dT} = \frac{E_a}{RT^2} \tag{2.90}$$

Next, we use the fact that $d \ln K_c/dT = \Delta U^0/RT^2$ for an ideal gas, then Equation 2.89 becomes

$$\frac{d\ln k}{dT} = \frac{1}{T} + \frac{\Delta^{\ddagger}U^0}{RT^2} \tag{2.91}$$

Additionally, $\Delta^{\ddagger}H^0 = \Delta^{\ddagger}U^0 + RT\Delta^{\ddagger}n$ ($\Delta^{\ddagger}n = 1$), as so Equation 2.91 can be rewritten as

$$\frac{d\ln k}{dT} = \frac{\Delta^{\ddagger} H^0 + 2RT}{RT^2} \tag{2.92}$$

Therefore, by comparison of Equation 2.92 and 2.90, we get

$$E_a = \Delta^{\ddagger} H^0 + 2RT \tag{2.93}$$

which then converts Equation 2.88 into the form

$$k = \frac{e^2 k_B T}{h c^0} e^{\Delta^{\ddagger} S^0 / R} e^{-E_a / RT}$$
 (2.94)

Therefore, a statistical thermodynamical picture of the Arrhenius equation arises from TST, and the Arrhenius pre-factor A can be expressed as

$$A = \frac{e^2 k_B T}{hc^0} e^{\Delta^{\ddagger} S^0/R}$$
 (2.95)

In practise, we use the form of Equation 2.86 to compute the rate constant of a reaction, which we shall denote as k_{TST} . The conventional TST makes an assumption that the reaction coordinate is static along the lowest energy pathway. This can be corrected by the use of variational transition state theory. ¹²⁶ We shall not consider variational TST in this work, as with careful application, conventional TST does a remarkably good job at accounting for the magnitude and temperature dependence of a wide range of reactions. ¹²⁵ Additionally, if one makes corrections for QM tunnelling, conventional TST can easily give a more complete description of the rate constant.

Quantum mechanical tunnelling

Atoms are quantum mechanical particles, and are thus subject to the strange probabilistic behaviours observed at the microscopic level. QM tunnelling refers to the ability of particles to penetrate the reaction barrier, rather than surmounting it classically (Figure 2.3). While all reactions are subject to QM tunnelling, we will show that due to the low mass of the hydrogen atom, QM tunnelling can play a significant role in HAT reactions.

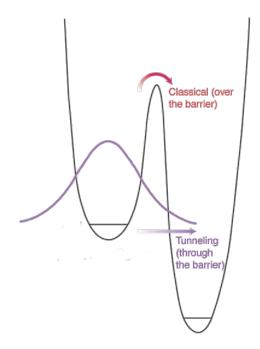


Figure 2.3: Quantum mechanical tunnelling occurs when a particle penetrates a reaction barrier, rather than surmounting it. Figure adapted from Reference 1

In order to determine the effects of scattering, one must find transmission coefficients (κ) by solving the Schrödinger equation. ⁶² This is done by approximating the reaction barrier with an analytical potential, thus simplifying the problem mathematically. The earliest model potentials were introduced by Bell, who used a parabolic function to approximate the reaction barrier. ¹²⁷ To obtain κ , and thus the observed rate constant (k_{obs}), the following equations were used:

$$k_{obs} = \kappa A e^{-E_a/RT} \tag{2.96}$$

$$\kappa = \frac{e^{\alpha}}{\beta - \alpha} \left(\beta e^{-\alpha} - \alpha e^{-\beta} \right) \tag{2.97}$$

$$\alpha = E_a/RT \tag{2.98}$$

$$\beta = \frac{2a\pi^2 (2mE_a)^{1/2}}{h} \tag{2.99}$$

where the Arrhenius equation was used to estimate the rate constant, m is the mass of the tunnelling particle, and 2a is the width of the barrier. Since the equation is dependent on the mass of the particle, tunnelling occurs more often when lighter particles are involved. As a consequence, tunnelling is more common in HAT reactions than other atom transfer reactions. Also, the height and width of the barrier are important factors in determining the contributions to tunnelling: reactions with small barriers have low tunnelling contributions; narrow barriers result in higher tunnelling contributions.

The Bell model is a poor representation of an actual reaction barrier. One which is a much better approximation is the $Eckart\ potential$. The form of this potential is

$$V = -\frac{Ay}{1-y} - \frac{By}{1-y^2} \tag{2.100}$$

$$y = -e^{2\pi x/L} \tag{2.101}$$

where x is the variable along the reaction coordinate and L is called the characteristic length. If A=0 the potential becomes a symmetric function, further simplifying the problem; however, most reactions do not have a symmetric potential. A, B and L are related to the change in barrier height in the forward and reverse direction, ΔV_1 and ΔV_2 , respectively:

$$A = \Delta V_1 - \Delta V_2 \tag{2.102}$$

$$B = ((\Delta V_1)^{1/2} + (\Delta V_2)^{1/2})^2$$
(2.103)

$$\frac{L}{2\pi} = \left(-\frac{2}{F^*}\right)^{1/2} \left[\frac{1}{(\Delta V_1)^{1/2}} + \frac{1}{(\Delta V_2)^{1/2}}\right]^{-1}$$
 (2.104)

where $F^* = d^2V/dx^2$ evaluated at the maximum of the potential. In this formulation, V is a placeholder energy. Note that if a reaction is endoergic, tunnelling does not occur. Alternatively, one says tunnelling only occurs in exoergic or energy-neutral reactions.

The solutions to the Schrödinger equation for the Eckart potential are analytical, thus that transmission coefficient κ can easily be computed using

standard numerical techniques. These tunnelling corrections will be applied, where applicable as $\,$

$$k_{calc} = \kappa k_{TST} = \kappa \frac{k_B T}{hc^0} e^{-\Delta^{\ddagger} G^0}$$
 (2.105)

Chapter 3

The Relationship Between Arrhenius Pre-factors with Non-Covalent Binding

DiLabio and Ingold²² previously investigated the formal HAT reaction of the iminoxyl/oxime self-exchange reaction. In this paper, they compiled a table of parameters from the phenomenological Arrhenius equation for a series of interesting reactions, which appear here in Table 3.1.^{129–136} These are self-exchange reactions, of oxygen-centred π -radicalsⁱⁱ and other thermoneutral (or nearly thermoneutral) reactions involving the destruction and formation of oxygen-centred π -radicals, reactions 3.1 and 3.2, respectively:

$$\pi - RO' + ROH \longrightarrow ROH + \pi - RO'$$
 $\Delta H = 0$ (3.1)

$$\pi - R'O' + ROH \longrightarrow R'OH + \pi - RO'$$
 $\Delta H \approx 0$ (3.2)

Although it is well known that reactions of this nature involve remarkably low activation energies $(E_a),^{137-140}$ they also have unusually low Arrhenius pre-exponential factors (A), or as we shall refer to them, A-factors. As a result, these reactions are generally slower than expected, evidence for which is summarised in Table 3.1. The measured A-factors range from $10^{3.5}\text{--}10^{8.3}\,\mathrm{M}^{-1}\mathrm{s}^{-1}$, while normal HAT reactions are typically $10^{8.5\pm0.5}\,\mathrm{M}^{-1}\mathrm{s}^{-1}$. This is likely due to steric shielding around the oxygen atoms, resulting in a large entropic barrier. 22 Additionally, it was noted that the degree of steric shielding on the oxygen atom appears to play an important role in the order of the A-factor; systems with greater bulk have lower A-factors while non-shielded systems have larger A-factors.

 $^{^{}ii}\pi$ -radicals are those in which the SOMO is orthogonal to the plane of the molecular framework, i.e. of π -symmetry. Note that free alkoxyl radicals cannot be distinguished as either σ or π -radicals, as the SOMO is free to rotate with respect to the rest of the molecular framework. Therefore, only the geometry of the radical-molecule complex can determine the symmetry of the SOMO.

Table 3.1: Table of experimental results which needs revision

ID	RO'/R'O'	ROH	ΔH (kcal mol ⁻¹)	$\log_{\mathrm{M}^{-1}\mathrm{s}^{-1}}^{A})$	E_a (kcal mol ⁻¹)	$\begin{pmatrix} k \\ (M^{-1}s^{-1}) \end{pmatrix}$
1^{129}	t-Bu t-Bu	* t-Bu OH	0.0	3.7	1.2	3.3×10^{2}
2^{130}	o=	N—OH	-2.0	3.8	3.8	10
3^{129}	N	NOH	0.0	5.1	3.5	3.3×10^{2}
$4^{131,132}$	r-Bu PBu	• rBu—OF	4.2	5.5	4.8	93
5^{133}	<i>t</i> -BuOO•	t-Bu OH	-7.0	4.2	0.5	7×10^3
6^{129}	Ph ₂ NO•	Ph ₂ NOH	0.0	>7	-	>107
7^{134}	o•	OH	-2.2	8.3	2.3	4×10^{6}
8^{135}	t-BuOO⁴	ОН	0.3	7.2	5.2	3×10^3
9^{135}	t-BuOO⁴	OH	-1.9	6.4	2.6	3×10^4
10^{136}	t-BuOO⁴	OOH	1.4	6.0	4.5	7×10^2

Upon first inspection, all of the reactions in Table 3.1 appear to be fairly similar in nature. In all cases the breaking and formation of O-H bonds are the most thermodynamically favourable and should be comparable in strength, therefore, differences should not contribute significantly to reaction barriers in a Bell-Evans-Polanyi principle fashion. Hence, the large degree of variance in their rate constants (k) is somewhat surprising. For the closely related self-exchange reaction between phenol and phenoxyl, 36 a strong molecule-radical pre-reaction complex is formed, ca. 10 kcal mol⁻¹ below the separated reactants. It is therefore expected that most, if not all, of the systems in Table 3.1 should exhibit a similar molecule-radical

complex, although the strength of the interaction will vary because of steric repulsion.

Steric-electronic effects are known to play an important role in HAT, and have been studied extensively by our colleagues in Rome, as well as by others. $^{45-52}$ Although the abstraction of a specific bond may be more thermodynamically favourable than others on a given substrate, if it is not accessible due to steric constraints, abstraction will not occur at this site. Otherwise, additional steric bulk can lead to significant reductions in reactivity, through destabilisation of the TS complex. For example, in reactions of tertiary acetamides with CumO $^{\bullet}$, 52 where abstraction occurs mainly from C-H bonds α to the nitrogen atom, a two-fold decrease in the normalised rate constant is observed in going from N, N-dimethylacetamide to N, N-diisobutylacetamide ($k_H = 2.0 \times 10^5$ and 7.8×10^4 M $^{-1}$ s $^{-1}$, respectively).

Currently, there is no literature which describes the relationship between the pre-reaction complex and the kinetics of a reaction. Using the reactions and data in Table 3.1, we ask the question: Do A-factors have a correlation with non-covalent binding energies of the pre-reaction complex? This is a reasonable question as non-covalent binding and steric hinderance represent a loss of degrees of freedom and therefore entropy, iii which ultimately determines the A-factor magnitude. If the answer to the question is yes, then non-covalent binding can be used as a diagnostic for the "looseness" or "tightness" of a TS complex and provide an important link between theory and experiment.

3.1 Results and discussion

The theoretically determined electronic binding energies calculated for the lowest energy pre-reaction complex of each system are listed in Table 3.2, along with images of the three-dimensional structures. The plot of the logarithm of A-factor against binding energy is shown in Figure 3.1. The overall correlation is quite poor $(R^2=0.33)$, however, the majority of the data is grouped about a single line with good correlation $(R^2=0.95)$. Interestingly, the intercept of the fitted line which corresponds to zero binding energy is 8.63, which is in line with the observed A-factor in "normal" HAT reactions $(10^{8.5\pm0.5}~{\rm M}^{-1}{\rm s}^{-1})$. ¹⁴¹ This suggests that the observed correlation is valid, that is NCIs may have an impact on A-factors. I shall demonstrate that the data which do not correlate are reasonable outliers. Precisely, different

ⁱⁱⁱRecall from Equation 2.95 that the A-factor can be related to TST and that the primary variable is entropy $(\Delta^{\ddagger}S^0)$.

regimes of sterics result in different processes leading to the TS complex, and thus deviations from the observed relationship between A-factor and binding energy are observed.

(This table might go better in an appendix)

Table 3.2: Table of theoretical results which needs revision

ID	Structure	Binding Energy (kcal mol^{-1})
1		-10.82
2		-14.79
3		-10.12

Table 3.2: Table of theoretical results which needs revision

ID	Structure	Binding Energy (kcal mol^{-1})
4		-10.04
5		-6.75
6		-14.84

Table 3.2: Table of theoretical results which needs revision

ID	Structure	Binding Energy (kcal mol^{-1})
7		-8.56
8		-5.50

Table 3.2: Table of theoretical results which needs revision

ID	Structure	Binding Energy (kcal mol^{-1})
9		-5.56
10		-7.99

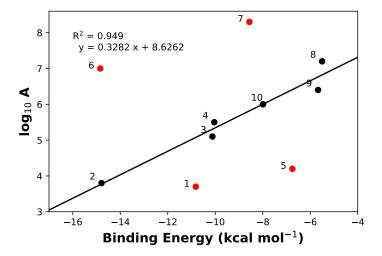


Figure 3.1: Plot of logarithm of A-factor against binding energy. Black points only were included in the line fitting (slope = 0.3282 kcal mol⁻¹, intercept = 8.6262 kcal mol⁻¹, and $R^2 = 0.949$). Red points indicate outliers, *vide infra*. The inclusion of points 1, 5, and 7 result in an R^2 =0.334. Point 6 is always omitted as the experimental A-factor is approximate.

In order to illustrate this, consider the fundamental properties of the HAT reaction involved here. Again we consider the two important concerted reaction mechanisms which can occur; direct HAT and PCET. Specifically, we must consider the geometric constraints in which these reactions occur. For direct HAT to occur, the SOMO of the radical must overlap with the O-H σ^* anti-bonding orbital. Often this requires the rotation of the hydroxyl group out of the plane, the barrier to which can be as much as 3.1 kcal mol⁻¹ on the basis of the rotational barrier in phenol. ¹⁴² In PCET, there are two possibilities: the SOMO of the radical must be able to overlap with the corresponding oxygen p-orbital, as seen in the work of Mayer et al. ³⁶; or a lone pair- π or π - π overlap must occur, as seen in the work of DiLabio and Johnson ²³. Although from the pre-reaction complex one can only make an educated guess as to the TS complex, by applying these basic principles, it is possible to rationalise the trend observed in Figure 3.1.

We shall begin by examining the points which fall on the expected line, complexes 2-4 and 8-10, all of which require small conformational changes to proceed through formal HAT reactions. Complexes 2 and 3 are very similar in structure, both are hydroxylamine-nitroxyl couples with similar

degrees of steric bulk adjacent to the reacting centres. Both the t-butyl and methyl groups prevent the alignment of the NO-H-ON frameworks in a PCET manner. Additionally both pre-reaction complexes must undergo the rotation of the hydroxyl group for direct HAT. In the most stable stacked conformation, complex 4 cannot undergo PCET as the steric clash of the para-position t-butyl groups prevent π - π overlap. In order to react via HAT, the hydroxyl group must rotate out of the plane. Alternatively, an open conformation for complex 4 is possible, which lies ca. 2 kcal mol⁻¹ higher in energy than the stacked complex, a result which is also consistent with the observed trendline. From the open conformation, PCET is still not possible due to the steric bulk of the ortho-position t-butyl groups of the radical, thus this reaction likely proceeds through direct HAT.

Complexes 8 and 9 are similar systems, in which t-BuOO reacts with unhindered phenolic substrates. As seen by the structures in Table 3.2, the bound complexes are somewhat dissimilar. The hydroxyl group of complex 8 is rotated out of the plane 24°, while this is not true for complex 9. It is likely that the larger aromatic system of 2-naphtol results in a larger OH rotational barrier, and thus the most favourable conformation is entirely in the plane. Complex 8 was previously studied by DiLabio and Johnson ²³, where it was demonstrated that a partial bonding interaction exists between the peroxyl lone-pair and phenolic π -system, giving a PCET mechanism. Although the pre-reaction complexes are somewhat dissimilar, the conformational changes necessary to reach the PCET TS complex reported in reference 23 are likely not dramatically different in terms of energetic barriers. Any small differences that are observed result in noise in the observed trend.

Complex 10 is unique in that it is the only reaction between a peroxide and a peroxyl radical. The self-exchange reaction between HOO $^{\bullet}$ and HOOH can be considered the simplest reference for the reaction of α -tetralin peroxide with t-butylperoxyl. To the best of my knowledge, the mechanism of the hydroperoxyl-hydrogen peroxide couple has not been characterised previously in the literature, although the TS structure has been previously reported. Using this structure, calculations reveal a lone pair-lone pair interaction leading to partial bonding in the TS, i.e. a PCET mechanism. Details of this can be found in Appendix X. For complex 10 to achieve the same lone pair-lone pair interaction, the two species must rotate by approximately 30° relative to one another. This is somewhat unfavourable due to steric clash.

(Add HOOH-OOH TS details to appendix)

All the the complexes which follow the observed trend must undergo an

additional process with a barrier that is likely about 3 kcal mol⁻¹ (on the basis of the phenolic rotational barrier) to reach the TS complex. This is illustrated in Figure 3.2.

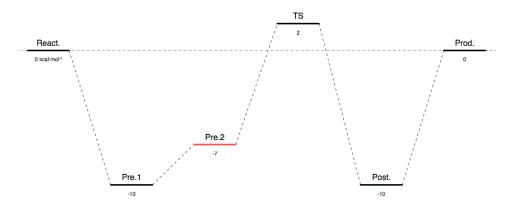


Figure 3.2: Reaction coordinate illustrating a conformational change to a second pre-reaction complex prior to transition state. All energies are arbitrarily estimated based on the phenol-phenoxyl self-exchange reaction. React. = reactants, Pre.1 = lowest energy pre-reaction complex, Pre.2 = postulated higher energy pre-reaction complex, TS = transition state, Post. = post-reaction complex, Prod. = products.

Consider next the points which sit above the trendline, complexes 6 and 7. The A-factor for complex 6 is approximate and thus does not get factored into the line fitting. In both cases, the non-covalently bound complexes are in a slipped-parallel π -stacked conformation. Complex 7 in particular is very similar to the phenol-phenoxyl couple, except with 2-naphthol instead of phenol. Therefore, it is possible to infer that both of these reactions take place through a PCET mechanism. Specifically, these pre-reaction complexes do not require an additional conformational change to approach the TS complexes, as illustrated in Figure 3.3.

Finally, consider the points which fall below the trendline, complexes 1 and 5. In both cases, a high degree of steric repulsion likely does not allow for a PCET mechanism. Complex 1 is the reaction with the most steric shielding surrounding the reaction centres, with four ortho-position t-butyl groups in total. As a result, the most stable pre-reaction complex does not have a hydrogen bond, which is unique among the ten reaction couples studied here. A higher energy (0.6 kcal mol^{-1}) pre-reaction complex 1 does exist, and possesses an open conformation hydrogen bond. This higher energy conformer is likely that which leads to HAT through a direct mechanism.

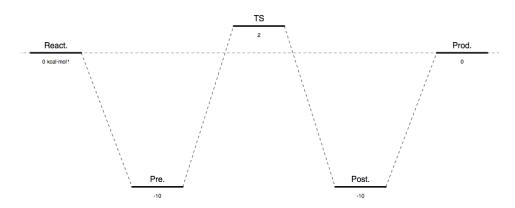


Figure 3.3: Reaction coordinate illustrating no conformational change before moving to the transition state. All energies are arbitrarily estimated based on the phenol-phenoxyl self-exchange reaction. React. = reactants, Pre. = lowest energy pre-reaction complex, TS = transition state, Post. = post-reaction complex, Prod. = products.

The geometry is such that the hydrogen group must rotate and the t-butyl groups must approach one another to approach the TS complex. This higher energy complex is still inconsistent with the trendline.

Complex 5 possesses an unusual hydrogen bond. Normally hydrogen bonds are nearly linear so that there is both a dipole-dipole interaction and an orbital interaction such that the lone pair of the acceptor donates electron density into the OH σ^* anti-bonding orbital. In the case of complex 5, the hydrogen bond is nearly perpendicular, resulting in only an orbital interaction. This is due to the steric repulsion between the t-butyl groups of t-butylperoxyl and 2,4,6-tri-t-butylphenol. Comparing this structure to the TS of complex 8 as published in reference 23 which takes place through PCET, it is apparent that complex cannot conform to the correct geometry for PCET to occur. (More detail needed) In order for this reaction to proceed, an open conformation complex must form so that a direct HAT mechanism can take place.

For complexes 1 and 5 which fall below the trendline, the lowest energy pre-reaction complex does not correspond to one which will lead to HAT. Therefore, one can describe an additional higher energy pre-reaction complex which leads to HAT, similar to the trend observed, but likely much

^{iv}The hydrogen bonding nature of this interaction has been verified using the NCIplot software. ^{145,146} These results can be found in Appendix X. (Add this to an appendix)



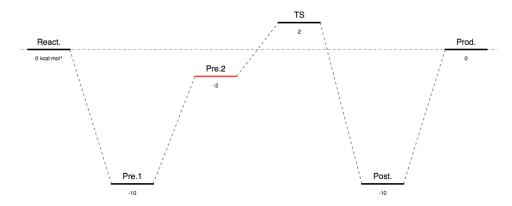


Figure 3.4: Reaction coordinate illustrating a conformational change to a second high energy pre-reaction complex prior to transition state. All energies are arbitrarily estimated based on the phenol-phenoxyl self-exchange reaction. React. = reactants, Pre.1 = lowest energy pre-reaction complex, Pre.2 = postulated higher energy pre-reaction complex, TS = transition state, Post. = post-reaction complex, Prod. = products.

3.2 Summary

In this investigation, I report the lowest energy pre-reaction complexes for a series of thermoneutral or nearly thermoneutral HAT reactions. I have plotted the theoretically determined electronic binding energies against the logarithm of the experimentally determined A-factors. These results demonstrate that the A-factor is correlated to some extent with the binding energy, given that the reactions proceed through energetically similar pathways. The results herein can be sorted into three bins: 1) Complexes which require small conformational changes to approach the TS structure. This appears to be the most likely case for formal HAT reactions. 2) Complexes which are optimally aligned to approach the TS structure. 3) Complexes which require a large conformational change to approach the TS structure.

These results suggest that different regimes of steric interactions lead to different chemical processes in seemingly similar reactions. As a results, non-covalent binding can be used as a metric for kinetics parameters, however, they cannot tell the whole story. One must first determine the relationship between the pre-reaction and TS complexes.

Additional work is necessary to extend these results. In particular, a larger sample of data points should be used. Regardless, the results herein represent a novel attempt to link theory and experiment. Given that obtaining the full PES for large molecules is computationally impractical, these results serve as a seed for developing a fundamental understanding of complex formal HAT reactions.

3.3 Computational methods and details

Density-functional theory (DFT) calculations were carried out using the Gaussian-09 software package. ¹¹⁶ Care was taken to obtain minimum energy structures through detailed conformational analysis. For this, I utilised the BLYP density-functional ^{103,147} paired with the empirical D3 dispersion correction ¹⁰⁹ with the recommended Becke-Johnson damping functions, ¹¹⁰ as well as our groups' own basis set incompletion potentials (BSIPs),*(update citation) and the minimal MINIs basis sets. ¹⁴⁸ The use of minimal basis sets corrected for basis set incompleteness allows DFT-based methods (as opposed to semi-empirical or force-field based approaches) to be used to efficiently perform a large number of calculations. Minimum energy geometries of the monomers (substrates and radicals) were first obtained by manual manipulation of the necessary dihedral bond angles, followed by geometry optimisation and vibrational analysis.

The lowest energy radicals and substrates were combined to generate the appropriate pre-reaction complexes. These pre-reaction complexes were subject to conformational analysis using the same BLYP-D3(BJ)-BSIP/MINIs method. Geometries were initially manipulated by hand. It became apparent that manual manipulation resulted in an unsatisfactory exploration of the conformational space. To solve this, all the necessary dihedral angles were scanned systematically using a combination of scripts. 149 All manipulated geometries were subject to optimisation. For each complex, the top 5-10 complex geometries were subject to further optimisation using a higher level of theory (BLYP-D3(BJ)/pc-1) to obtain the final minimum energy pre-reaction complex structures. Due to the free rotation of t-butyl and methyl groups, some of the optimised pre-reaction complex structures contain small imaginary frequencies, and thus do not represent proper stationary states. Several measures were taken to resolve this, however, no resolution was obtained. Regardless, the complexes adequately represent the pre-reaction complex and differences in "true" binding energies should be negligible.

To obtain accurate pre-reaction complex binding energies, the substrates and complexes were subject to single-point energy calculations using the LC- ω PBE long-range corrected density functional ^{150,151} with D3(BJ) dispersion corrections and pc-2 basis sets with truncated f-type functions (pc-2-spd). ¹⁵² This method was selected on the recommendation of work by Johnson et al. ¹⁵², which demonstrated that this is an efficient method for the calculation of NCIs with a reasonable degree of accuracy.

Chapter 4

Interrogation of the Bell-Evans-Polanyi Principle: Investigation of the Bond Dissociation Enthalpies correlated with Hydrogen Atom Transfer Rate Constants

Experimental BDEs from Bordwell 153 cycle are possible unreliable in the case where PCET occurs 154

H-A
$$\rightleftharpoons$$
 H⁺ + A⁻ pK_{HA} (1)
A⁻ \rightleftharpoons e⁻ + A⁺ E_{os}(A⁻) (2)
Increase/Reduce Image Size (3)
H-A \rightleftharpoons H⁺ + A⁺ BDE (4)
ΔBDE = 1.37ΔpK_{HA} + 23.06ΔE_{os}(A⁻) (5)

- 4.1 Background
- 4.2 Methods

Chapter 5

Do non-redox active metal cations have the potentials to behave as chemo-protective agents? The Effects on Metal Cations on HAT Reaction Barrier Heights

5.1 Benchmarking Density Functional Theory for the Binding of Alkali and Alkaline Earth Metals

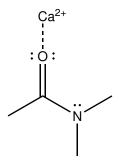
5.1.1 Background

In order to study the central hypothesis propsed in this work, we must carefully select a computational method. In particular, we wish to use density-functional theory (DFT), which is known to be prone to various problems such as self-interaction error, ¹⁵⁵ delocalization error, ¹¹² and the inability to treat non-covalent interactions. ^{108,156} The latter of these can be corrected by the selection of a method capable correcting the non-covalent corrections such as a pair-wise dispersion model (\-citeD3), or atom centered potentials developed by our group (\-citeDCPS). Other errors can be ignored through the careful selection of a DFT method.

We are interested in selecting a method which can accurately treat the interactions between alkali and alkaline earth metal cations, and organic substrates and radicals. To this end, there exists little literature, with one notable paper ¹⁵⁷ which examines the binding of calcium cations to organic substrates. In this paper, Suárez et al. ¹⁵⁷ provide accurate energetic, electronic, and structural results for the binding of calcium to organic neutral and charged species, as well as assess the performance of four different DFT methods. They also analyze the nature of ligand-metal bonding interactions using a symmetry-adapted perturbation theory approach (SAPT) (EXPAND ON THIS)

Due to our interest in alkali and alkaline earth metal cations in FHT, we determined it necessary to prepare benchmark quality data for binding to organic substrates and radicals.

(Calcium prefers to bind to O, with binding to S or N is rare ¹⁵⁸) In N,N-dimethylacetamide for example, calcium binds preferentially to the lone pairs of the carbonyl oxygen over the nitrogen lone pair. This is shown in Scheme 5.1.



Scheme 5.1: Binding of the calcium cation (Ca^{2+}) to the oxygen lone pairs of N,N-dimethylacetamide.

5.1.2 Methods

Conformers were generated using Hyperchem with the AM1 semi-empirical molecular orbital (MO) method (\-citehyperchem) followed by optimization calulations of 5-10 lowest energy structures using at the ((currently unpublished)) BLYP-D3/pc1 level of theory, including our own groups basis set incomplete potential (BSIPs).((CITATIONS))

On the basis of the work by Otero-de-la-Roza et al. 112 , which showed that in systems which are halogen bonded, erroneous charge transfer can be significant, and given the charge on the metal cations, the LC- ω PBE density functional with D3 dispersion correction and moderate 6-31+G(2d,2p) ((CI-TATIONS for DFT and D3)) basis sets were applied to determine the most strongly bound complexes of substrates and metal cations. Global minima monomers and complexes were optimized with the LC- ω PBE-D3 method

near the basis set limit (6-311+G(3df,3pd). Highly correlated wavefunction results were obtained at the CCSD(T) level of theory with extrapolation to the complete basis set limit.(CITATION) Calculations were performed using the Gaussian 09 package, ¹¹⁶ and wavefunction calculations were performed using the TURBOMOLE ⁷⁵ package.

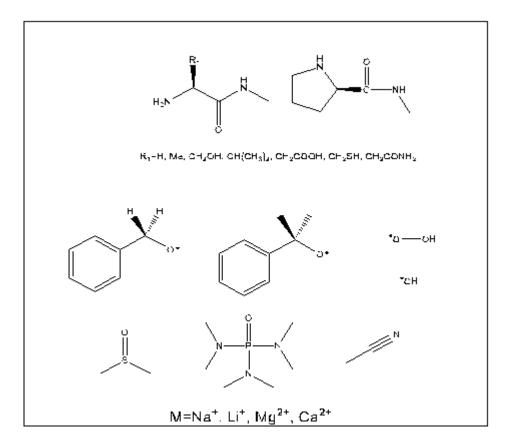
5.1.3 Benchmark systems

The purpose of this work is to provide high-level binding energies for organic substrates which are of interest directly for this project, but also which may be useful for future work. The substrates proposed were to be relevant to simple biological models such as dipeptide like molecules and the hydroxyl and hydroperoxyl radical. We also wanted to incorporate substrates with are important to the physical organic experiments that are performed to probe these systems, thus solvents such as acetonitrile and dimethylsulfoxide and the benzyloxyl and cumyloxyl radicals were also included. This set is shown in Scheme 5.2(FIND CDX).

Benchmark quality binding energies are generally calculated using the "gold standard" approach, CCSD(T)/CBS, where correlation consistent basis sets((CITATION)) (cc-pVXZ, X=T,Q,5) developed by Dunning and coworkers are used for complete basis set extrapolation. These basis sets have limited availability for the metals of interest. Specifically, basis sets for K are note available, and only non-augmented basis sets for Li, Na, Mg, and Ca. It is necessary to include core correlation of the n-1 shell in alkali and alkaline earth metals, thus it is advantageous to use core valence basis sets such as cc-pCVXZ. These basis sets are even more limitted, thus we opted for the augmented version of the polarization consistent basis sets of Jensen and co-workers (aug-pc-N, N=2,3,4). (CITATIONS FOR GOLD STANDARD AND BASIS SETS, NEED THEORY SECTION ON DIFFERENT BASIS SETS)

While performing CCSD(T)/CBS calculations, we notices that the metal cations (and neutral metal atoms), did not converge smoothly to the complete basis set limit. Given this, and the limitted computational resources, we decided to re-evaluate the size scope of the benchmark set being used. In order to facilitate future DFT work and probe the issue of basis set convergence of alkali and alkaline earth metals, a benchmark set of small substrates was proposed. This new set is shown in Scheme 5.3. The new, small benchmark set was selected to include important functional groups and radicals for biological systems and the most common solvent used in physical organic experiments, acetonitrile.

5.1. Benchmarking Density Functional Theory for the Binding of Alkali and Alkaline Earth Metals



Scheme 5.2: Initial proposed benchmark set of molecules and cations. Note this set consistes of all combinations of substrates and metal cation, thus there are 60 complexes in the set.

- 5.1.4 Metal cation basis set convergence
- 5.1.5 High level results and evaluation of various density-functional theory methods

$$h \to 0$$
 $h \to 0$ $h \to$

Scheme 5.3: Revised benchmark set of small substrates and cations. Note this set consistes of all combinations of substrates and metal cation, thus there are 35 complexes in the set.

Chapter 6

Conclusion

Here comes the conclusion.

Chapter 6. Conclusion

Your conclusion can go on for several pages.

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Appendix