

Yield gap analysis using boundary lines

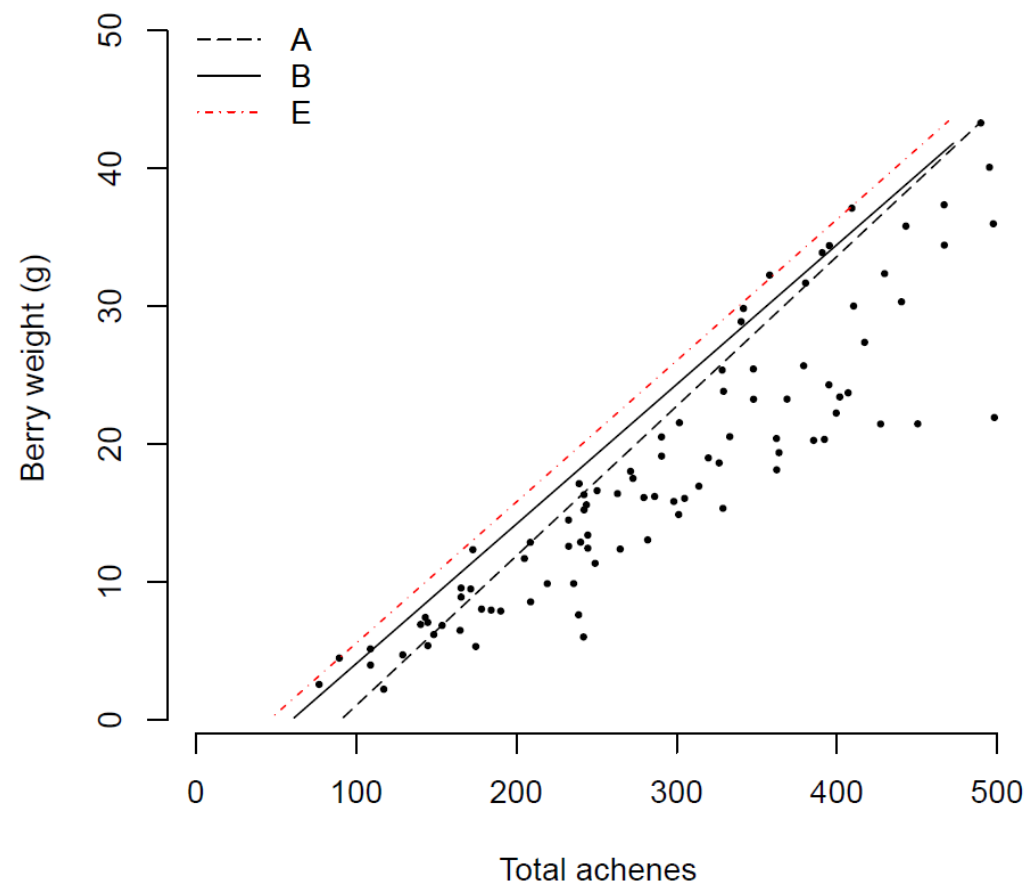
Chawezi Miti

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Background

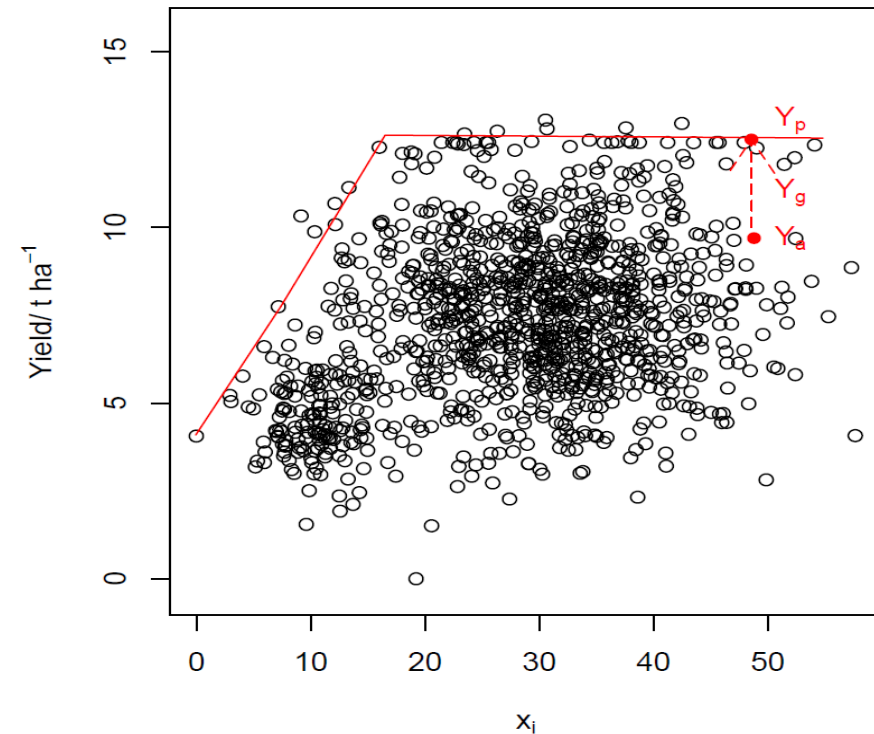
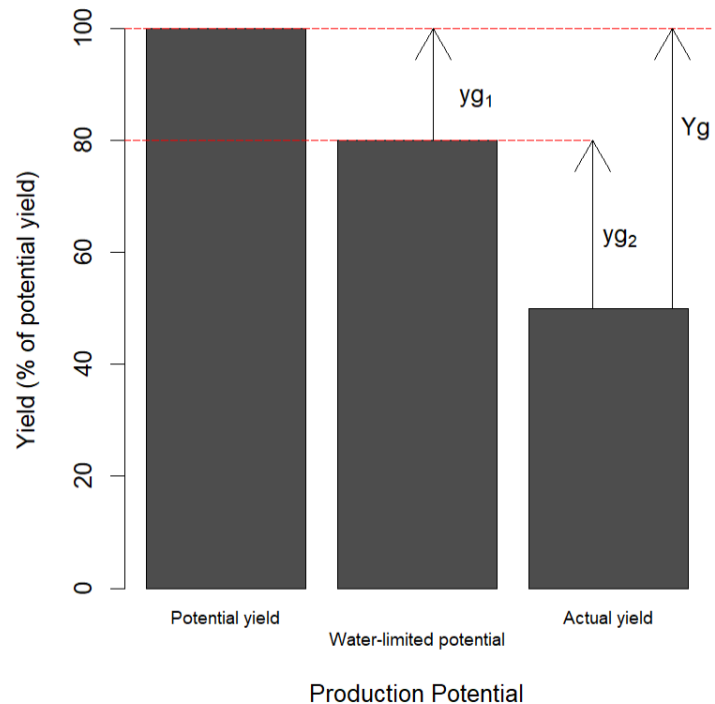
- Biological response (e.g. yield) is affected by many factors in nature
- If the relationship of one factor and response is plotted in uncontrolled environments, a **complex distribution** is observed.
- Webb (1972) proposed a **boundary line model** for such data
- The upper bounds are taken as the **most efficient response** when other factors are optimal



Source: Webb (1972)

Background

- ❑ The BL is taken as the maximum yield as function of factor x_i for that particular system
- ❑ Points below BL have a yield gap
- ❑ Used to *yield gap analysis* evaluate the *importance of production factors* on farm systems





Methods of implementing boundary line analysis

- Several methods are available in literature including *heuristic* or *statistical* methods

1. Heuristic methods

- ☐ Visual assessment
- ☐ BOLIDES algorithm
- ☐ Binning
- ☐ Quantile regression

*Heuristic methods
involve subjective
discussions*

2. Statistical methods

- ☐ Censored bivariate model

*Statistical methods
follow strict statistical
principles*



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2. Statistical methods

- ☐ **Censored bivariate normal model**

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Yield gap analysis using binning methodology



Yield gap analysis using binning methodology

Yield gap analysis using boundary lines involves three steps

1. Selection of boundary points
2. Model fitting
3. Decomposition of identified yield gaps



Yield gap analysis using binning approach

Yield gap analysis using boundary lines involves three steps



1. Selection of boundary points

2. Model fitting

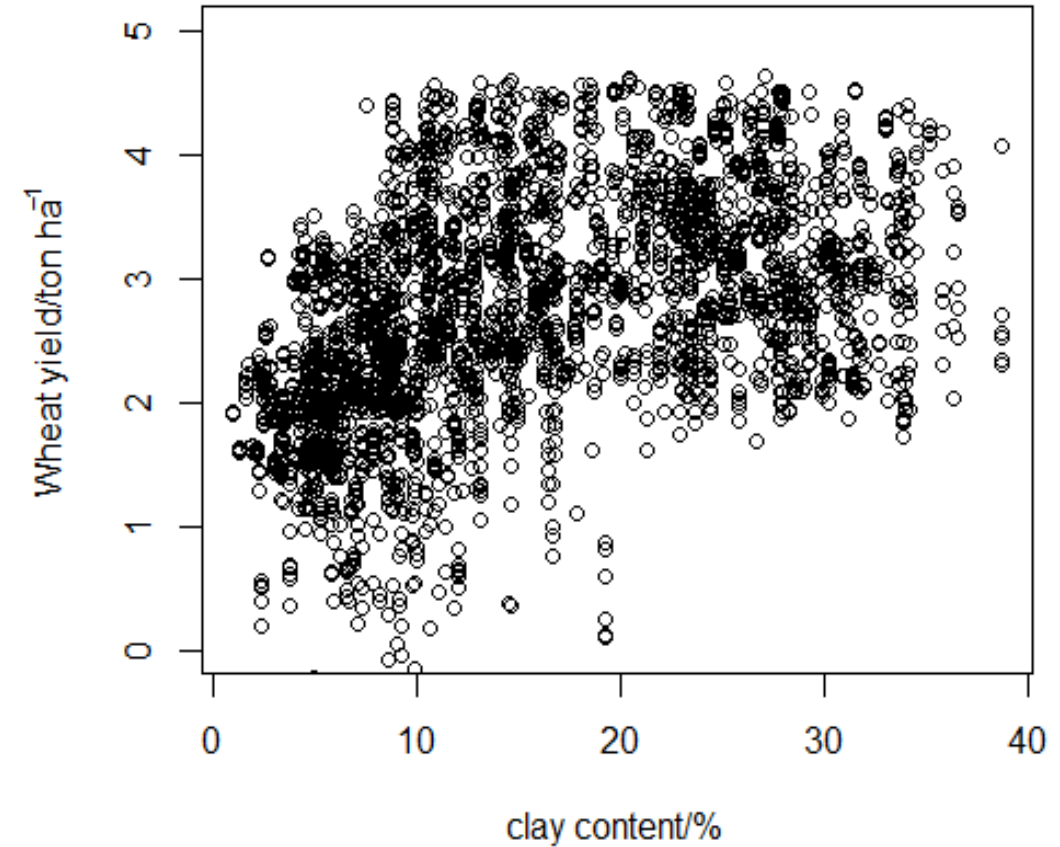
3. Decomposition of identified yield gaps



Yield gap analysis using binning approach

1. Selection of boundary points

- This follows a two step process
 1. Dataset is divided into bins (group) of equal intervals based on the factor of interest
 2. In each group, boundary point is selected corresponding to the *maximum value* or *95 percentile* of each group



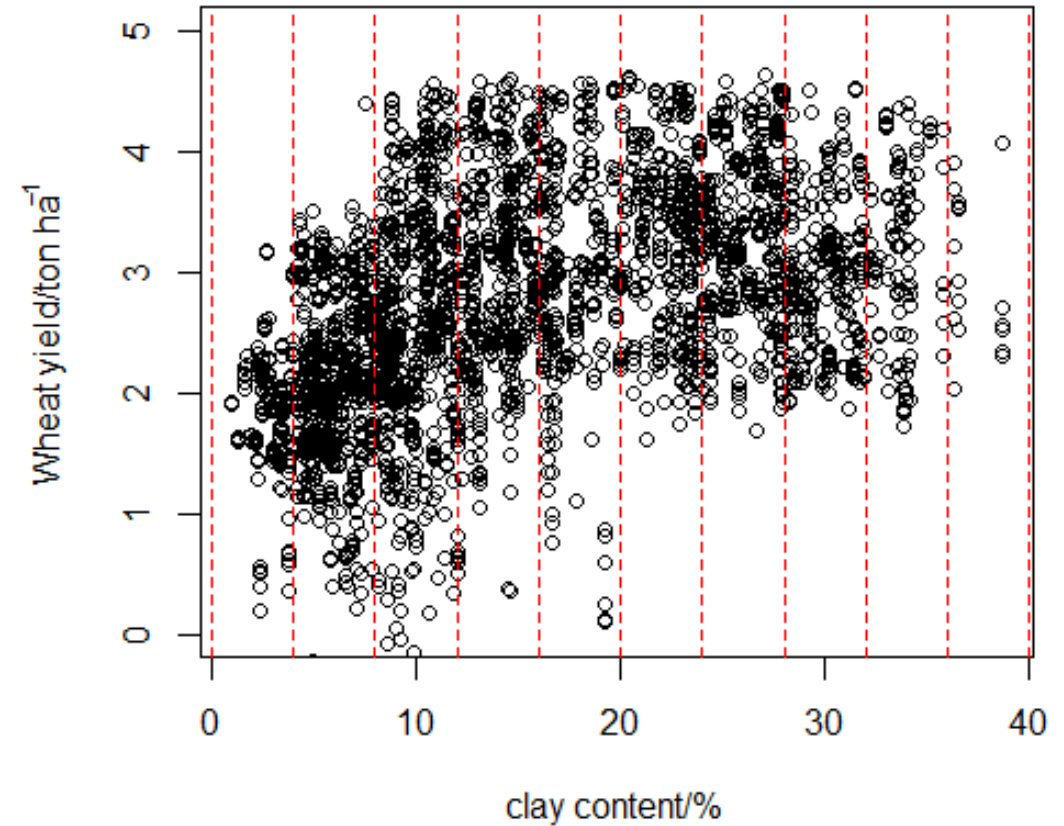
Yield gap analysis using binning approach

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- This follows a two step process



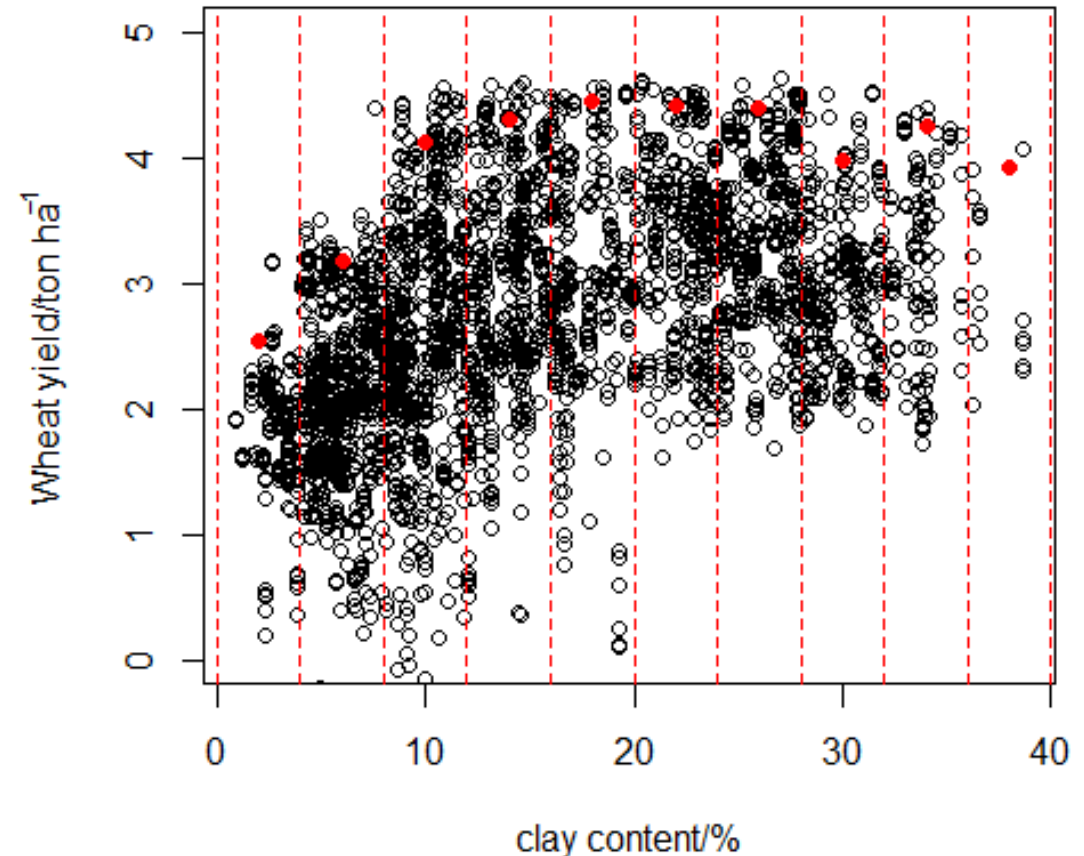
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Yield gap analysis using binning approach

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2. Model fitting

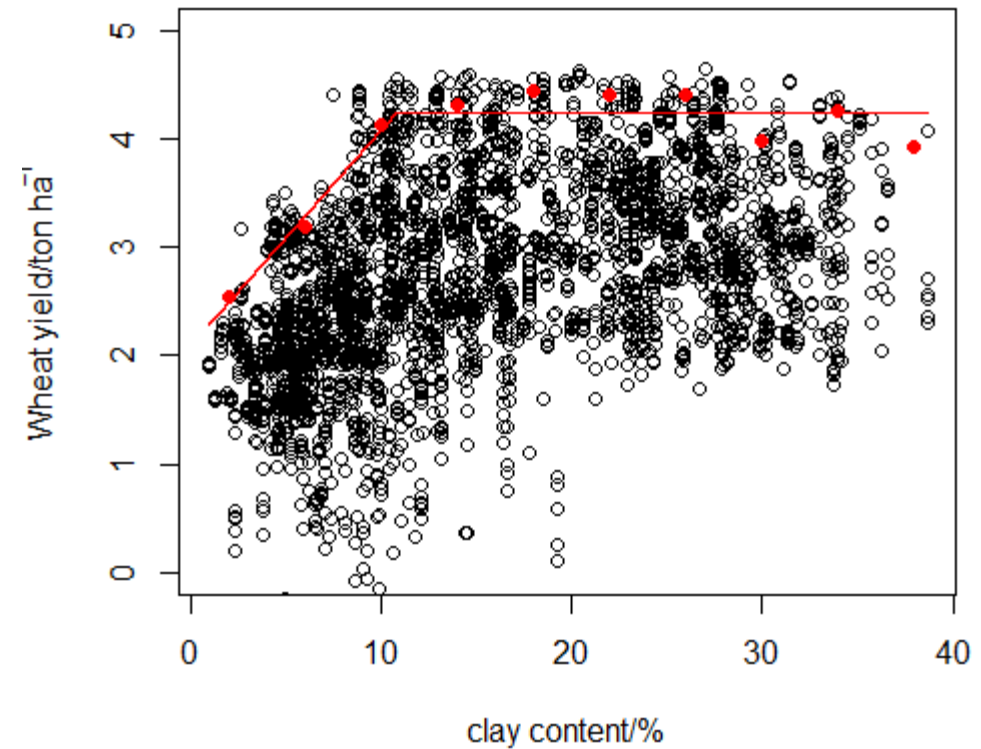
3. Decomposition of identified yield gaps

Yield gap analysis using binning approach

2. Model fitting

Considerations

1. Selection of model form
 - Agronomically plausible
2. Fitting model to boundary points
 - Least squares
 - Low root mean square error for the boundary points



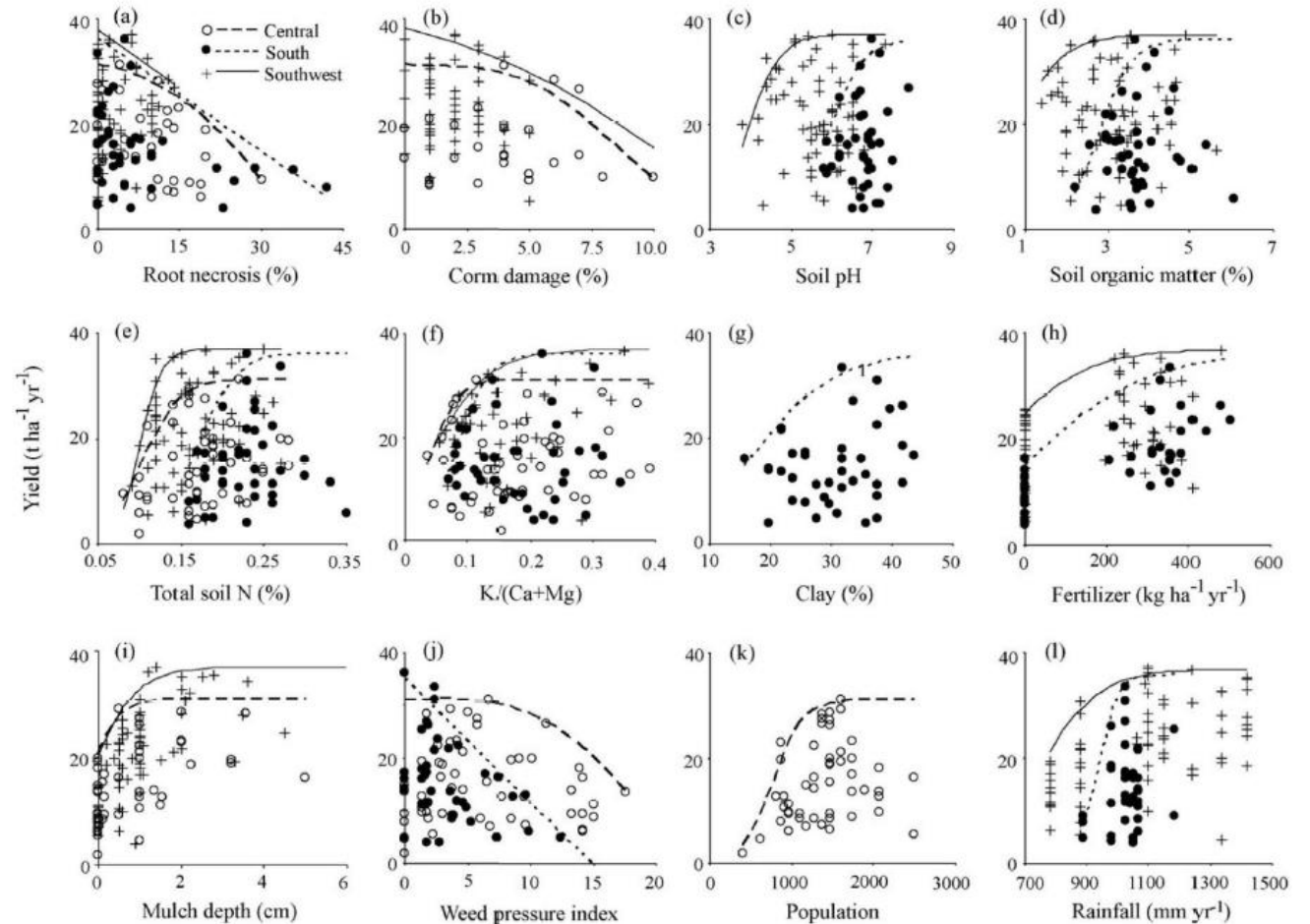


Yield gap analysis using binning approach

2. Model fitting

Fit boundary lines to all variables

- *Bio-physical factors*
- *Management factors*





Yield gap analysis using binning approach

Yield gap analysis using boundary lines involves three steps

1. Selection of boundary points
2. Model fitting



3. Decomposition of identified yield gaps

Yield gap analysis using binning approach

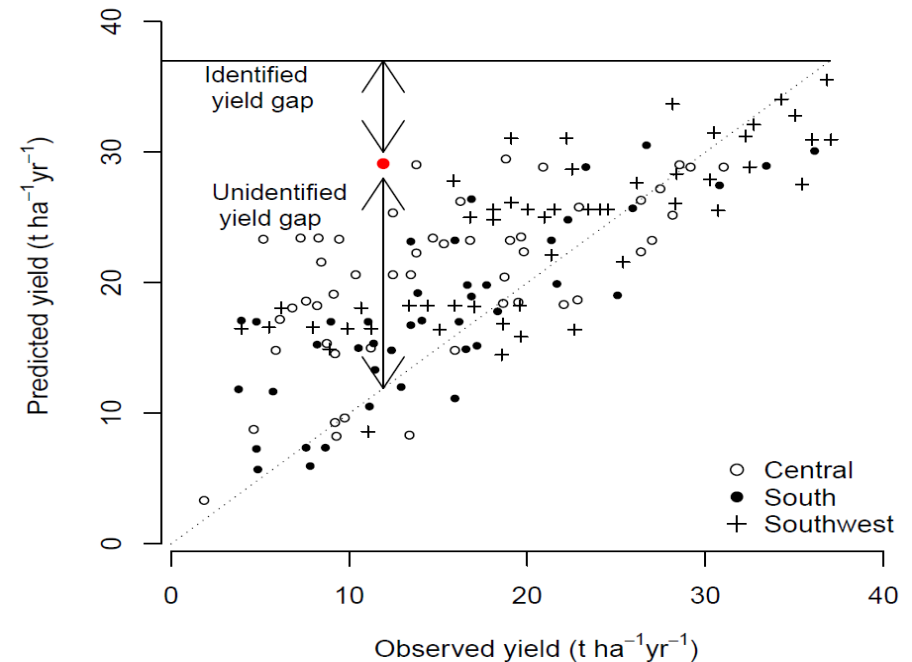
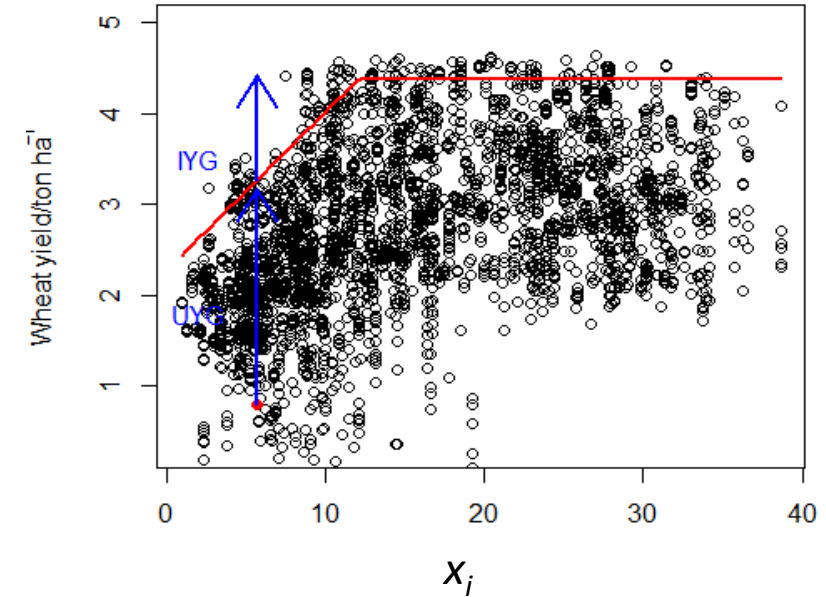
3. Decomposition of identified yield gaps

- Based on the principle of van Liebig's law of minimum

$$y_{pred} = \min(x_1, x_2, x_3, x_4)$$

Decomposition of yield gap

- *Unexplained* = predicted yield – actual yield
- *Identified* = maximum yield – predicted yield

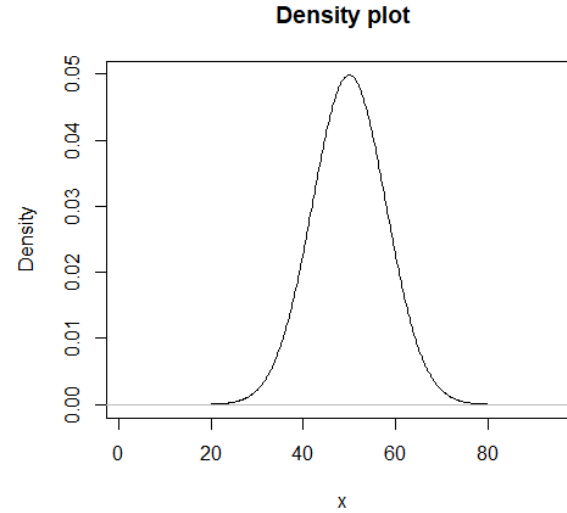
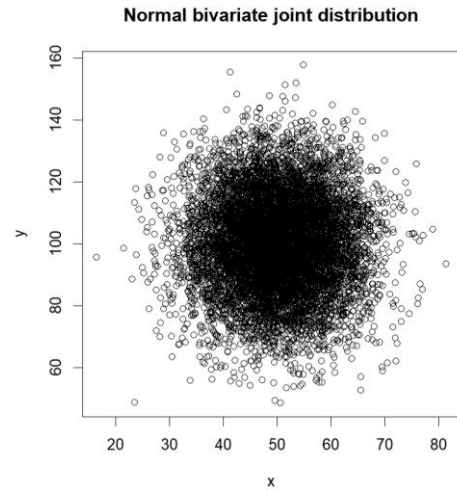




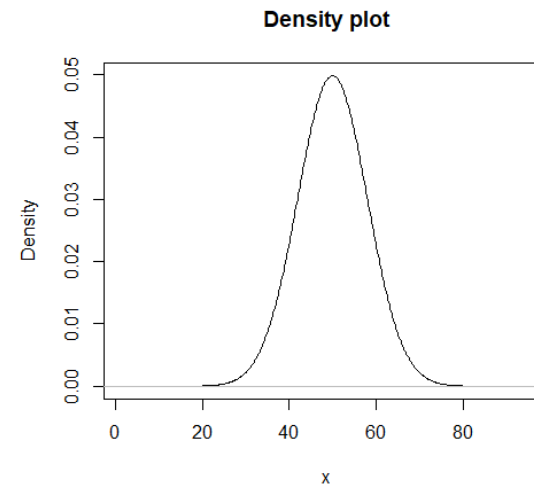
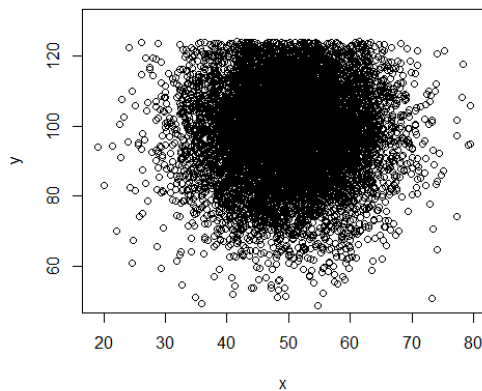
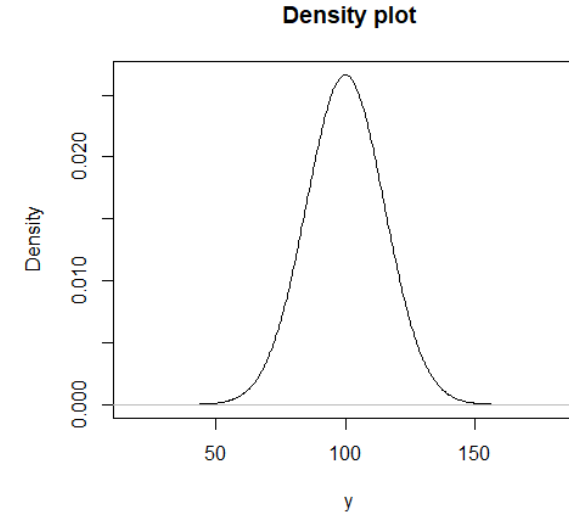
Statistical approach

Statistical approach

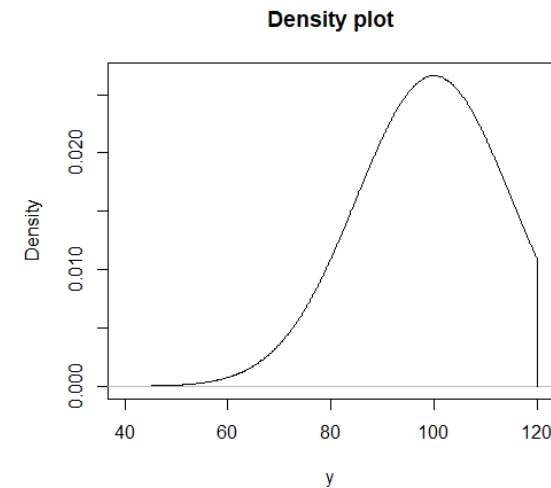
- Based on the censored bivariate normal distribution



×



×



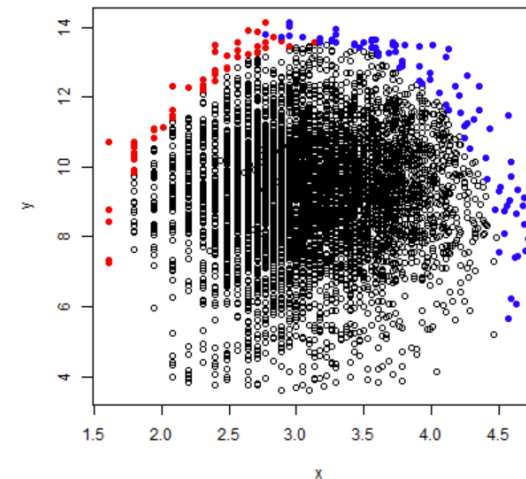
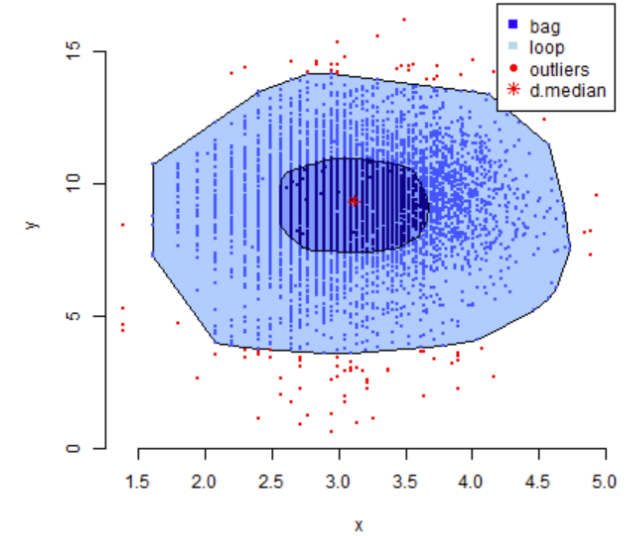
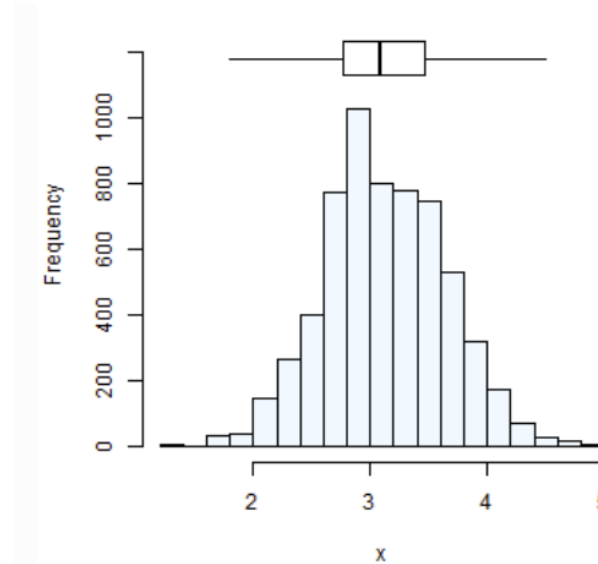
Log-likelihood

Statistical approach

Process of fitting boundary line

1. Check the distribution of variables
2. Check for outliers
3. Check for evidence of boundary
4. Fit the model (*maximum likelihood*)

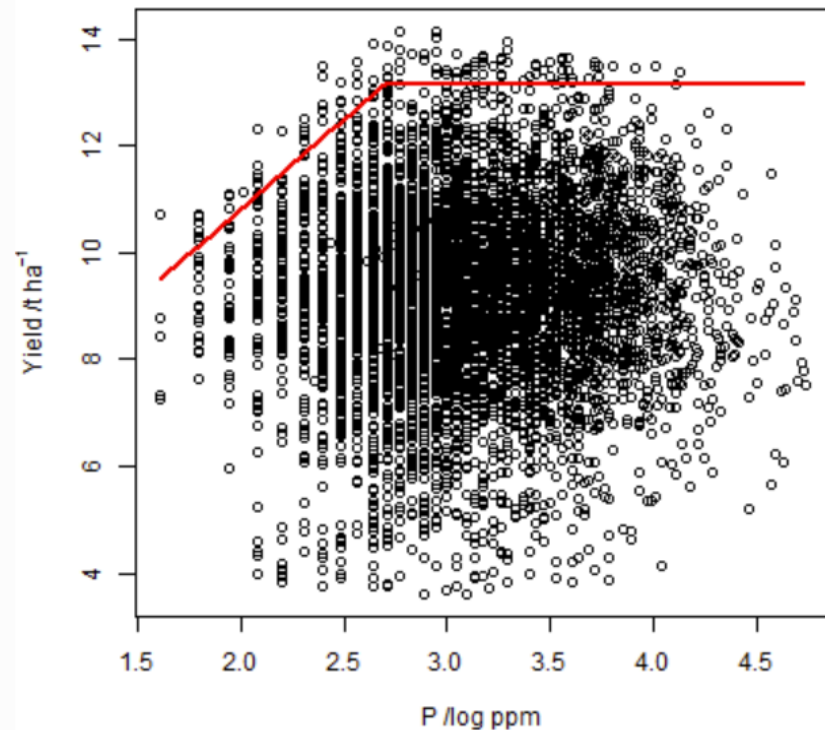
- ☐ Select model form to describe relation (*agronomically plausible*)
- ☐ Initial starting values
 - ☐ Parameters of bivariate normal distribution
 - ☐ Parameters of censor (BL)



Index	Section	value
sd	Rise	1.045711
sd	Fall	1.115379
Mean sd	Rise	1.180385
Mean sd	Fall	1.271274
p_value	Rise	0.018000
p_value	Fall	0.017000

Statistical approach

```
cbvn(vals,theta,sigh,model = "lp", xlab=expression("P /log ppm"), ylab=expression("Yield /t ha"^{-1}))
```



```
model1
## $estimates
##           Estimate Standard error
## beta0 13.17142480    0.134120445
## beta1  4.09776732    1.002709032
## beta2  3.36047473    0.457647238
## mux    3.12596783    0.006451127
## muy    9.29811648    0.022643136
## sdx    0.50053427    0.004561592
## sdy    1.61780277    0.017865349
## rcorr  0.03053177    0.014139952
##
## $AIC
##
## constant max 32431.55
## mvn          32429.55
## BL           32397.87
```



Thankyou