Morphological predictability - HS: 1.2

GAMMs

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2022-10-07

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Chapter 1

Setup

1.1 Load libraries, helpers, and data

Load everything we need for the analyses.

```r
# Load libraries and helpers
source(here::here("scripts", "00_libraries.R"))
source(here::here("scripts", "01_helpers.R"))
source(here::here("scripts", "04_load_data.R"))
```

1.2 Practice model

First, we'll fit a model to the data of one participant to check and make sure everything is working ok.

```r
# Take subset of 1 participant
mon01 <- stress_50 %>%
  filter(id == "mon01",
    time_zero > -10, time_zero < 20)

# Set model formula
formula <- bf(
  target_count | trials(50) ~ 1 + stress +
    s(time_zero, bs = "cr", k = 3) +
    s(time_zero, by = stress, bs = "cr", k = 3)
)

# Get priors
get_prior(
```

```
  formula = formula,
  family = binomial(link = "logit"),
  data = mon01
) %>%
  as_tibble() %>%
  select(prior, class, coef) %>%
  knitr::kable(format = "pandoc")
```

prior	class	coef
	b	
	b	stime_zero_1
	b	stime_zero:stressOxytone_1
	b	stime_zero:stressParoxytone_1
	b	stressParoxytone
student_t(3, 0, 2.5)	Intercept	
student_t(3, 0, 2.5)	sds	
	sds	s(time_zero, bs = "cr", k = 3)
	sds	s(time_zero, by = stress, bs = "cr", k = 3)

```
# Set priors
log_spline_priors <- c(
  prior(normal(0, 3), class = Intercept),
  prior(normal(0, 10), class = b),
  prior(student_t(3, 0, 1), class = sds)
)

# Fit test mod
test_mod <- brm(
  formula = formula,
  family = binomial(link = "logit"),
  prior = log_spline_priors,
  iter = 2000, warmup = 1000, cores = 4,
  backend = "cmdstanr",
  control = list(adapt_delta = 0.99, max_treedepth = 15),
  data = mon01,
  file = here("models", "gamms", "test_mod")
)
```

1.3 Test plots of time course and marginal predicted estimates

We can use the posterior to take a look at the model fit.

```
# Plot time course
test_mod %>%
  emmeans(spec = ~ 1 + time_zero + stress,
    at = list(time_zero = seq(-5.5, 11.5, 1)),
    epred = T) %>%
  gather_emmeans_draws() %>%
  ggplot(., aes(x = time_zero, y = .value / 50, color = stress)) +
    geom_hline(yintercept = 0.5, lty = 3) +
    stat_lineribbon(size = 0.5) +
    scale_color_brewer(name = NULL, palette = "Dark2",
      labels = c("Paroxytone\n(CANta)", "Oxytone\n(canTO)")) +
    scale_fill_brewer(name = NULL, palette = "Greys",
      labels = c("95%", "80%", "50%")) +
    labs(y = "P(Target fixation)", x = "Time course") +
    coord_cartesian(xlim = c(-5.4, 11.4), ylim = c(-0.01, 1.02),
      expand = F) +
    clean_guide(position = c(0.8, 0.22),
      title = "Estimated prediction intervals")
```
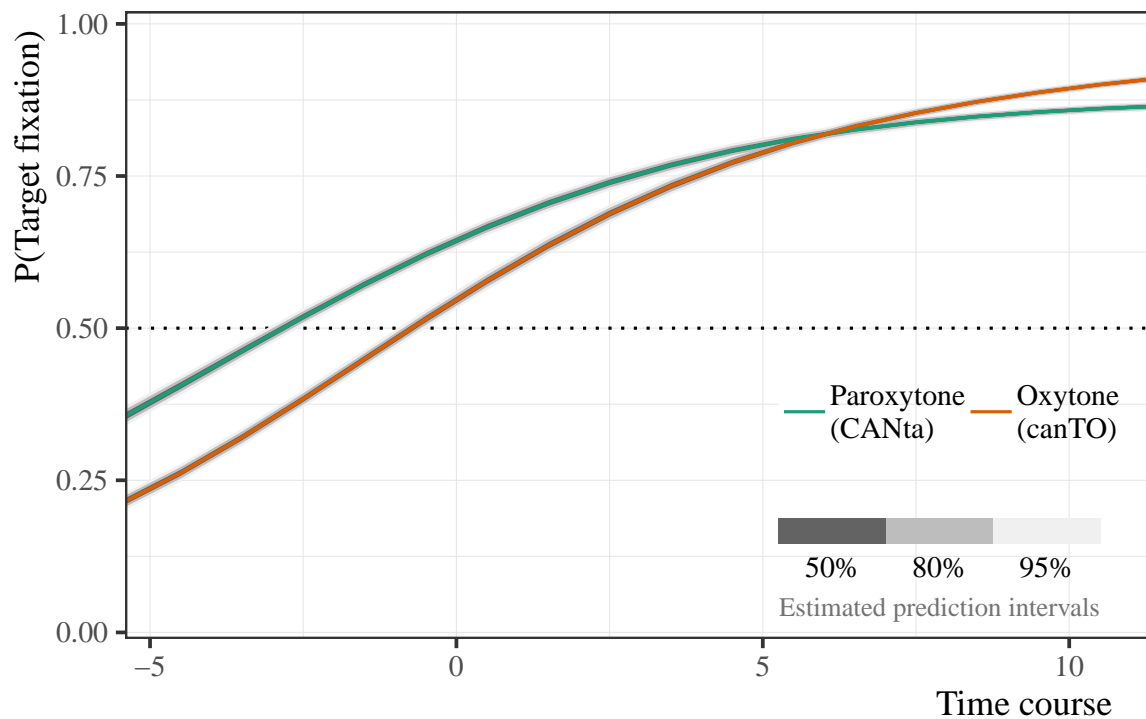

Figure 1.1: Target fixation as a function of stress for 1 participant.

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```r
# Test at time 0
test_mod %>%
  emmeans(
  spec = ~ 1 + time_zero + stress,
  at = list(time_zero = 0),
  epred = TRUE
  ) %>%
  gather_emmeans_draws() %>%
  mutate(prop = .value / 50) %>%
  ggplot(., aes(x = prop, y = stress)) +
    geom_rect(data = tibble(xmin = 0.49, xmax = 0.51),
      inherit.aes = F, fill = "lightblue", color = "white", alpha = 0.2,
      aes(xmin = xmin, xmax = xmax, ymin = -Inf, ymax = Inf)) +
    geom_vline(xintercept = 0.5, lty = 3, size = 0.5) +
    stat_dotsinterval(quantiles = 100) +
    geom_text(aes(label = label), hjust = 0,
      data = tibble(stress = 0.5, prop = 0.51,
        label = "200ms after 1st syllable offset")) +
    labs(y = NULL, x = "P(Target fixation)") +
    coord_cartesian(xlim = c(0.48, 0.68))
```
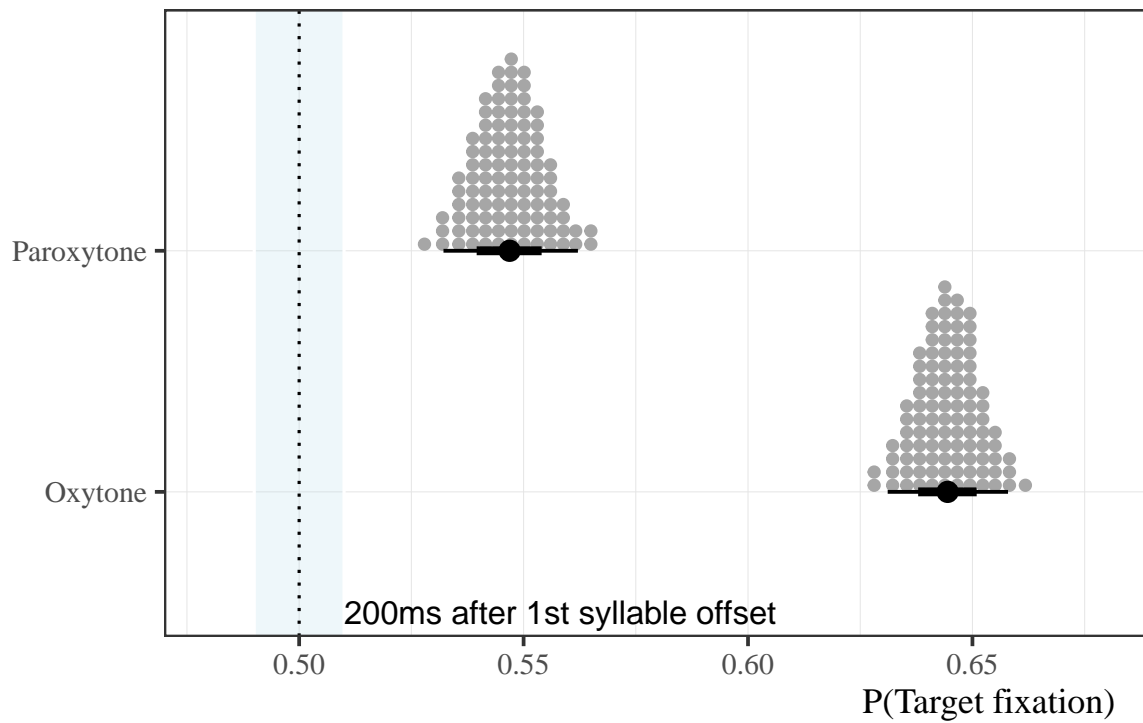
Figure 1.2: Proportion of target fixations 200ms after offset of 1st syllable. Data from one participant.

Chapter 2

Omnibus stress model

2.0.1 Logistic GAMM

Now we set up the data set for the main model. Main concerns are (1) getting the factors ready for smoothing terms and (2) subsetting the time course to reduce computational load.

```
# Set model formula
formula_log_gamm_stress <- bf(
  target_count | trials(50) ~ 1 + group * stress +
    s(time_zero, bs = "cr") +
    s(time_zero, by = stress, bs = "cr") +
    #s(time_zero, id, bs = "fs", m = 1, k = 3) +
    #s(time_zero, target, bs = "fs", m = 1, k = 3)
    (1 | id)
)

# Take a look at the default priors
get_prior(
  formula = formula_log_gamm_stress,
  family = binomial(link = "logit"),
  data = stress_50_gamm
) %>%
  as_tibble() %>%
  select(prior, class, coef) %>%
  knitr::kable(format = "pandoc")
```

prior	class	coef
	b	
	b	groupHL
	b	groupHL:stressOxytone

prior	class	coef
	b	groupL2
	b	groupL2:stressOxytone
	b	stime_zero_1
	b	stime_zero:stressOxytone_1
	b	stressOxytone
student_t(3, 0, 2.5)	Intercept	
student_t(3, 0, 2.5)	sd	
	sd	
	sd	Intercept
student_t(3, 0, 2.5)	sds	
	sds	s(time_zero, bs = "cr")
	sds	s(time_zero, by = stress, bs = "cr")

```r
# Set priors
stress_log_gamm_priors <- c(
  prior(normal(0, 3), class = Intercept),
  prior(normal(0, 3), class = b),
  prior(student_t(3, 0, 5.9), class = sds),
  prior(cauchy(0, 2), class = sd)
)

# Fit model
gamm_log_group_stress <- brm(
  formula = formula_log_gamm_stress,
  family =  binomial(link = "logit"),
  prior = stress_log_gamm_priors,
  iter = 11000, warmup = 1000, cores = 4, threads = threading(2), thin = 10,
  backend = "cmdstanr",
  control = list(adapt_delta = 0.9999, max_treedepth = 15),
  data = stress_50_gamm,
  file = here("models", "gamms", "gamm_log_group_stress")
)
```

Chapter 3

Bilingual model

Now we will fit a separate model to the bilingual groups' data. This model includes standardized proficiency and use scores.

```r
# Set up data frame
bi_50_gamm <- stress_50 %>%
  filter(group != "Monolingual",
    time_zero > -4, time_zero < 10) %>%
  mutate(id = as.factor(id),
    target = as.factor(target),
    stress = as.ordered(stress),
    stress = fct_relevel(stress, "Paroxytone"),
    group = fct_relevel(group, "HL"))

# Set contrasts for stress
contrasts(bi_50_gamm$stress) <- "contr.treatment"

# Set model formula
formula_gamm_bi <- bf(
  target_count | trials(50) ~ 1 + group * stress +
    prof_z + use_z +
    s(time_zero, bs = "cr", k = 3) +
    s(time_zero, by = stress, bs = "cr", k = 3) +
    #s(time_zero, id, bs = "fs", m = 1, k = 3) +
    #s(time_zero, target, bs = "fs", m = 1, k = 3)
    (1 | id),
  family = binomial(link = "logit")
)

# Get model default priors
```

```r
get_prior(
  formula = formula_gamm_bi,
  data = bi_50_gamm
) %>%
  as_tibble() %>%
  select(prior, class, coef) %>%
  knitr::kable(format = "pandoc")
```

prior	class	coef
	b	
	b	groupL2
	b	groupL2:stressOxytone
	b	prof_z
	b	stime_zero_1
	b	stime_zero:stressOxytone_1
	b	stressOxytone
	b	use_z
student_t(3, 0, 2.5)	Intercept	
student_t(3, 0, 2.5)	sd	
	sd	
	sd	Intercept
student_t(3, 0, 2.5)	sds	
	sds	s(time_zero, bs = "cr", k = 3)
	sds	s(time_zero, by = stress, bs = "cr", k = 3)

Prior predictive checks for bilingual model.

```r
# Set priors
bi_gamm_priors <- c(
  prior(normal(0, 1.5), class = Intercept),
  prior(normal(0, 3), class = b),
  prior(normal(0, 2), class = sds),
  prior(cauchy(0, 2), class = sd)
)

# Fit model to test priors
gamm_log_bi_stress_prior_fit <- brm(
  formula = formula_gamm_bi,
  family = binomial(link = "logit"),
  prior = bi_gamm_priors,
  iter = 2000, warmup = 1000, cores = 4,
  sample_prior = "only",
  backend = "cmdstanr",
```

```
    control = list(adapt_delta = 0.9999, max_treedepth = 15),
    data = bi_50_gamm,
    file = here("models", "gamms", "gamm_log_bi_stress_prior_fit")
)

# Prior predictive checks
bi_50_gamm %>%
    expand(time_zero = seq(-4, 10, length.out = 50), group, stress,
        id = "ahs01", prof_z = 0, use_z = 0) %>%
    add_epred_draws(gamm_log_bi_stress_prior_fit, ndraws = 100) %>%
    ggplot() +
        aes(x = time_zero, y = .epred/50) +
        facet_grid(stress ~ group) +
        geom_line(aes(group = .draw), alpha = 0.2, size = 0.2, color = "darkred") +
        labs(y = "P(Target fixation)", x = "Time course")
```
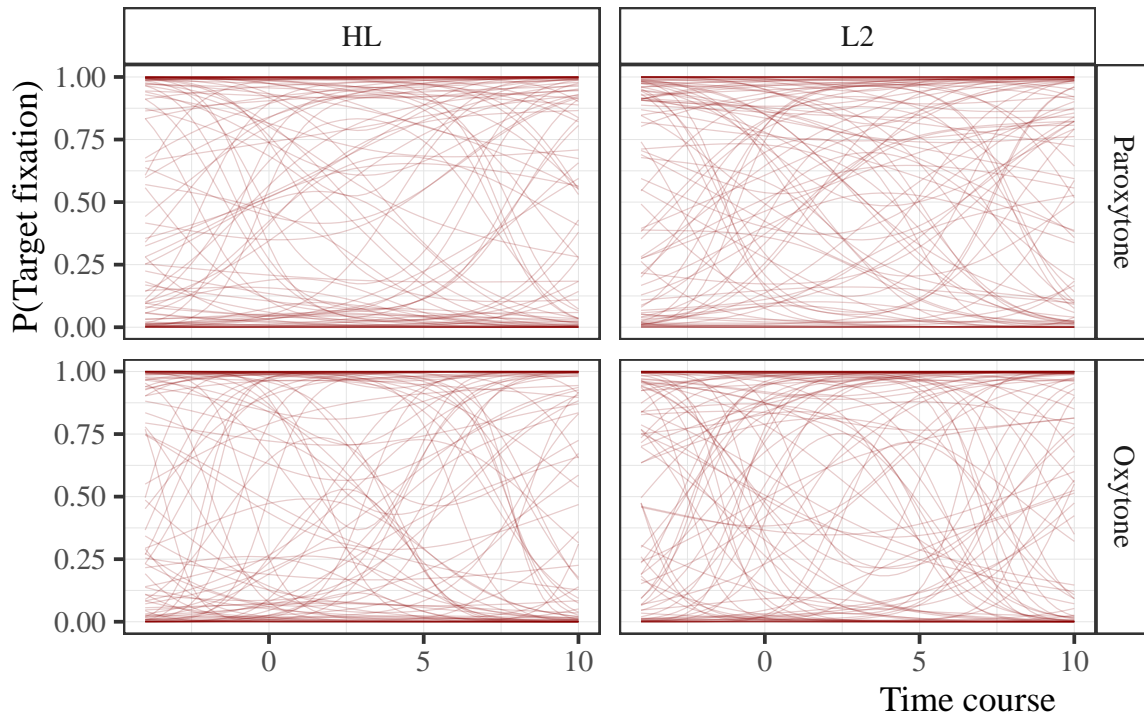

Figure 3.1: Prior predictive checks for bilingual model.

```r
# Fit actual model
gamm_log_bi_stress <- brm(
  formula = formula_gamm_bi,
  family = binomial(link = "logit"),
  prior = bi_gamm_priors,
  iter = 11000, warmup = 1000, cores = 4, threads = threading(2), thin = 10,
  backend = "cmdstanr",
  control = list(adapt_delta = 0.9999, max_treedepth = 15),
  data = bi_50_gamm,
  file = here("models", "gamms", "gamm_log_bi_stress")
)
```

Chapter 4

Plots

4.1 All data

```r
# Full model
gamm_log_group_stress_draws <- gamm_log_group_stress %>%
  emmeans(spec = ~ time_zero + stress + group, epred = T,
    at = list(time_zero = seq(-4.8, 12.8, 0.25)),
    ra_formula = NULL) %>%
  gather_emmeans_draws()

gamm_log_group_stress_plot <- gamm_log_group_stress_draws %>%
  ggplot() +
    aes(x = time_zero, y = .value / 50, color = group) +
    facet_grid(. ~ stress) +
    geom_hline(yintercept = 0.5, lty = 3, size = 0.5) +
    geom_vline(xintercept = 0 + 4, lty = 3, size = 0.5) +
    stat_lineribbon(show.legend = F) +
    stat_summary(fun = median, geom = "line") +
    scale_fill_brewer(palette = "Greys") +
    scale_color_manual(name = NULL, values = my_colors) +
    coord_cartesian(xlim = c(-4.8, 12.8), ylim = c(0.28, 1.02),
      expand = F) +
    scale_x_continuous(breaks = seq(-4, 12, 4), labels = seq(-200, 600, 200)) +
    labs(y = "P(Target fixation)", x = "Time course") +
    theme(legend.position = c(0.12, 0.86),
          legend.text = element_text(size = 10))
gamm_log_group_stress_plot
```
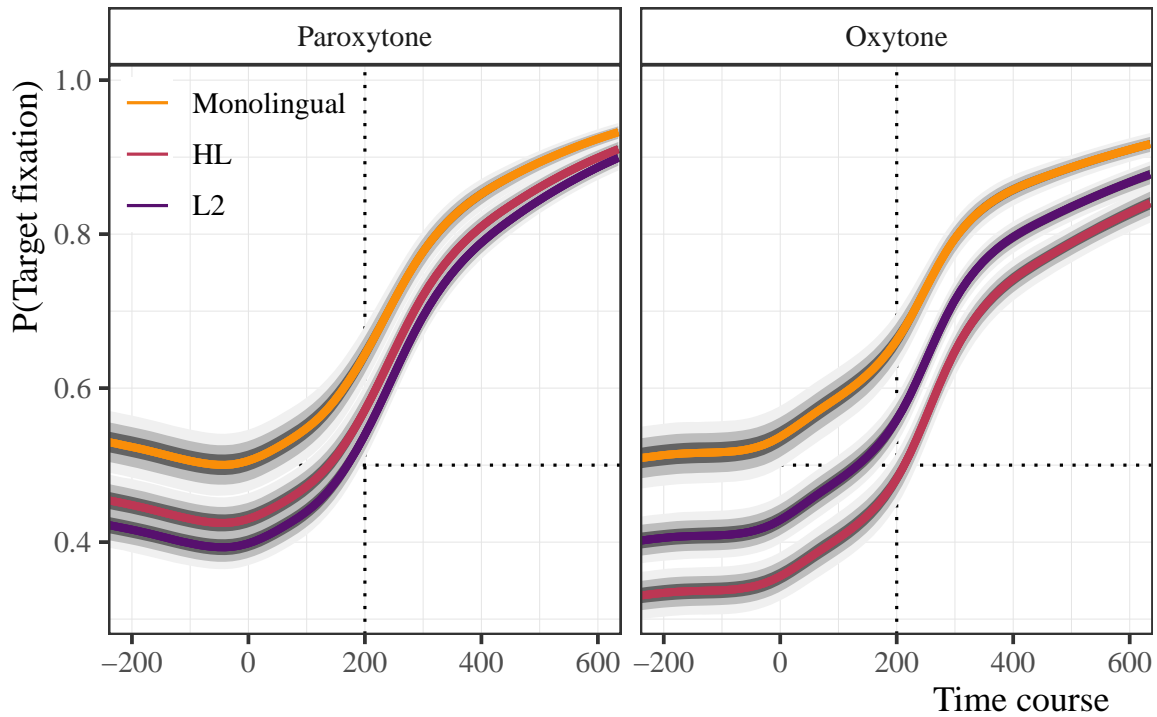
Figure 4.1: Probability of fixating on target as a function of stress for all three groups. The time course is centered around the target syllable offset (point 0). Vertical lines represent 200ms after target syllable offset. Lines represent group trajectories plus 95%, 80%, and 50% credible intervals.

```r
# Calculate difference smooths
gamm_log_group_stress_draws_diffs <- gamm_log_group_stress_draws %>%
  pivot_wider(names_from = group, values_from = .value) %>%
  mutate(`Monolingual - HL` = Monolingual - HL,
    `Monolingual - L2` = Monolingual - L2,
    `HL - L2` = HL - L2) %>%
  pivot_longer(cols = `Monolingual - HL`:`HL - L2`, names_to = "comp",
    values_to = "val")

# Plot smooths
gamm_log_group_stress_draws_diffs %>%
  mutate(comp = fct_relevel(comp, "Monolingual - HL", "Monolingual - L2")) %>%
  ggplot() +
    facet_grid(comp ~ stress) +
    aes(x = time_zero, y = val / 50) +
    geom_hline(yintercept = 0, lty = 3, size = 0.5) +
```

```r
geom_vline(xintercept = 0 + 4, lty = 3, size = 0.5) +
stat_lineribbon(color = "#11111100", show.legend = F,
  .width = c(0.1, 0.35, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95)) +
scale_color_viridis_d(aesthetics = "fill", option = "C") +
coord_cartesian(xlim = c(-4.8, 12.8), ylim = c(-0.15, 0.3),
  expand = F) +
scale_x_continuous(breaks = seq(-4, 12, 4), labels = seq(-200, 600, 200)) +
labs(y = "Difference smooths", x = "Time course")
```
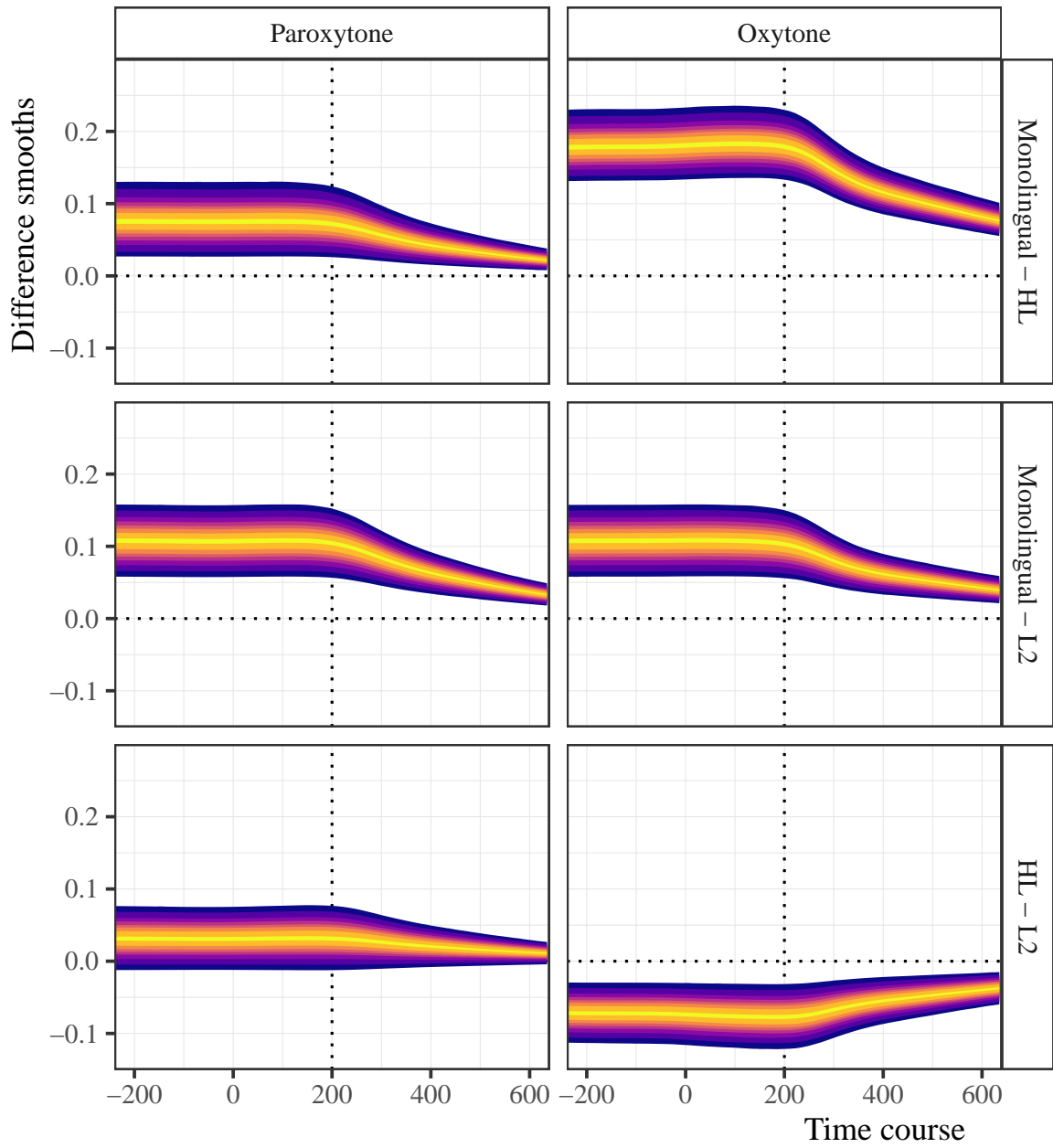
Figure 4.2: Pairwise difference smooths for paroxytone and oxytone items. From dark to light, colors represent 95%, 80%, 70%, 60%, 50%, 35% and 10% credible intervals.

```r
gamm_log_group_stress_dat <- gamm_log_group_stress %>%
  emmeans(spec = ~ time_zero + stress + group,
    at = list(time_zero = 4),
    ra_formula = NULL) %>%
  gather_emmeans_draws() %>%
  mutate(prop = plogis(.value))

gamm_log_group_stress_dat %>%
  ggplot() +
    aes(x = prop, y = group, fill = stat(x > 0.51)) +
    facet_grid(. ~ stress) +
    geom_rect(data = tibble(x = c(0.49, 0.51), y = NULL),
      aes(xmin = min(x), xmax = max(x), ymin = -Inf, ymax = Inf),
      fill = "lightblue", alpha = 0.2, inherit.aes = FALSE) +
    geom_vline(xintercept = 0.5, lty = 3, size = 0.5) +
    stat_slab(alpha = 0.7, color = "white", show.legend = F) +
    stat_pointinterval(pch = 21, point_fill = "white", show.legend = F) +
    scale_fill_manual(name = NULL, values = my_colors[2:3], labels = NULL) +
    scale_color_manual(name = NULL, values = my_colors[2:3], labels = NULL) +
    coord_cartesian(xlim = c(NA, NA)) +
    labs(y = NULL, x = "P(Target fixation)")
```
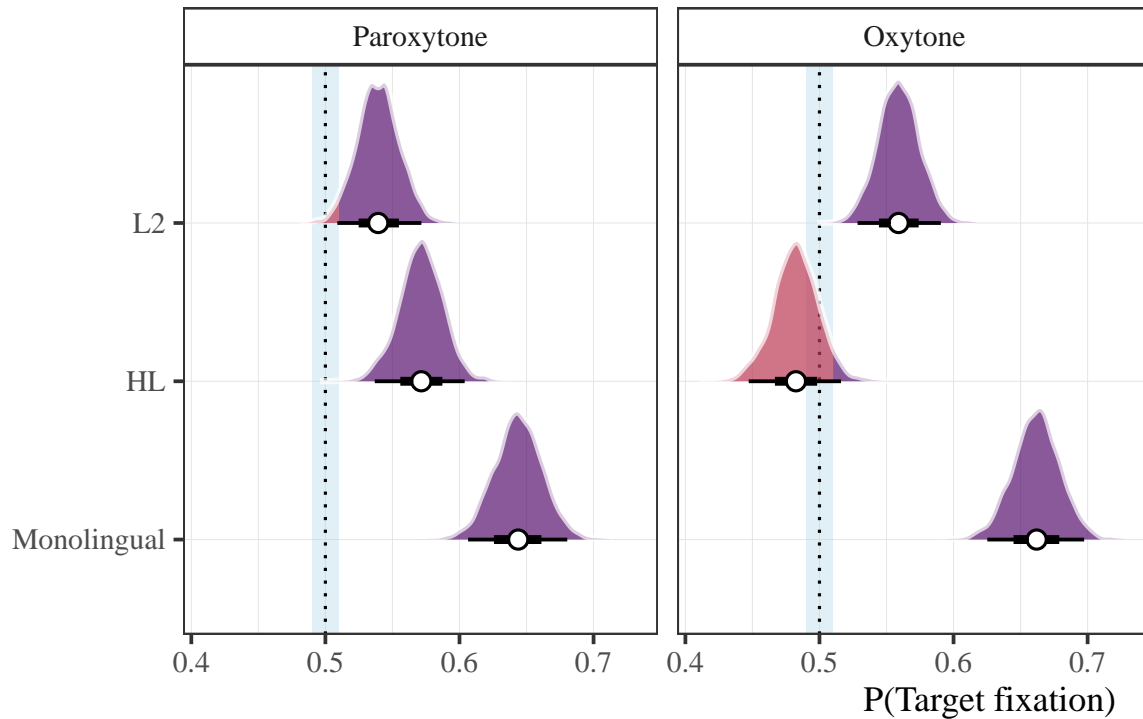
Figure 4.3: Proportion of target fixations 200ms after the offset of 1st syllable for monolinguals, heritage learners, and L2 learners in paroxytone (*CANto*) and oxytone (*canTO*) conditions. The vertical dotted line marks chance (50%) surrounded by a ±1% region of practical equivalence (ROPE). Density mass of the posterior distribution that falls within the ROPE is discolored (pinkish).

```
# Get marginal slope when time_zero = 4 as an estimate of rate of
# fixation on targets
# This can be used in a plot (if necessary) by estimating the y value
# at the desired x (time_zero == 4, for example) and then calculating
# the intercept using `find_intercept` (see example below)

# Get posterior estimates of marginal slopes
marginal_slopes_p1 <- gamm_log_group_stress %>%
  emtrends(
    spec = ~ time_zero + stress + group,
    var = "time_zero",
    at = list(time_zero = 4),
    delta.var = 0.001,
    epred = T) %>%
  gather_emmeans_draws() %>%
```

```
ungroup() %>%
mutate(group = str_replace_all(group, "Monolingual", "Mono"),
       group = fct_relevel(group, "L2", "HL")) %>%
ggplot() +
  aes(x = .value / 50, y = group, fill = group) +
  facet_grid(. ~ stress) +
  stat_slab(alpha = 0.7, color = "white", show.legend = F) +
  stat_pointinterval(pch = 21, point_fill = "white", show.legend = F) +
  scale_fill_manual(name = NULL, values = my_colors, labels = NULL) +
  coord_cartesian(xlim = c(NA, NA)) +
  labs(y = NULL, x = "Marginal slope estimate")
marginal_slopes_p1
```
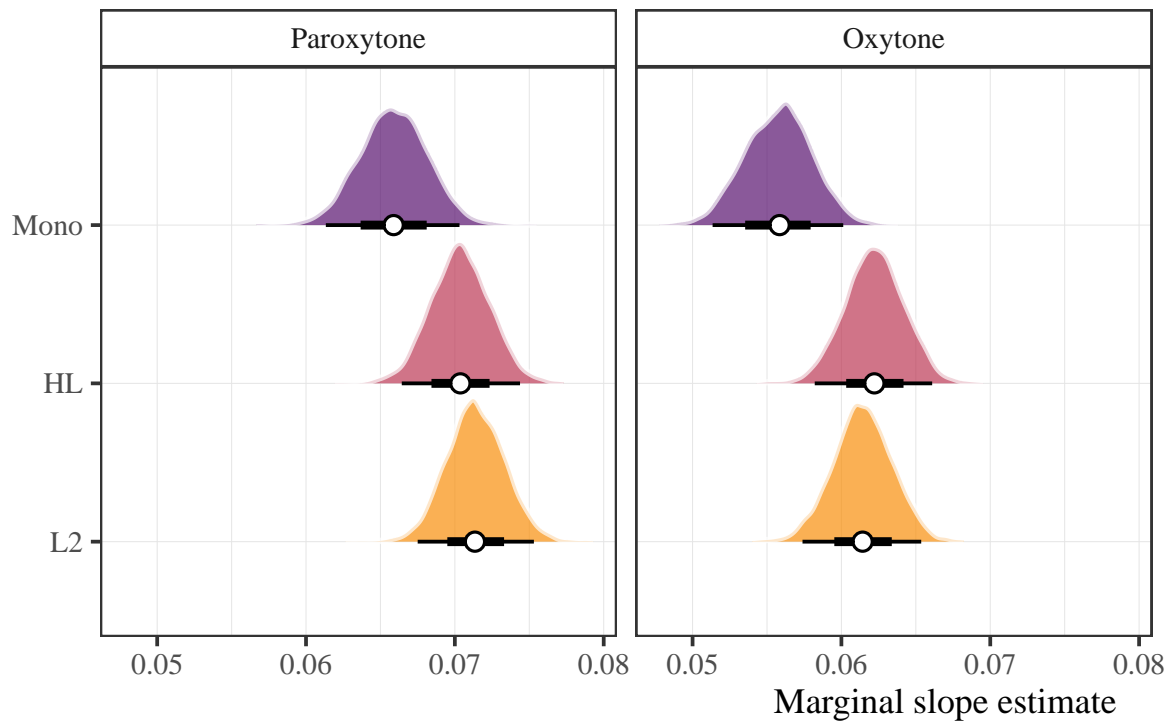

Figure 4.4: Marginal slope estimates 200ms after the offset of 1st syllable for monolinguals, heritage learners, and L2 learners in paroxytone ($CANto$) and oxytone ($canTO$) conditions.

```
lines <- bind_rows(
  gamm_log_group_stress %>%
    emmeans(specs = ~ time_zero + stress + group,
```

```
        at = list(time_zero = 4),
        epred = T) %>%
      gather_emmeans_draws() %>%
      mutate(.value = .value / 50) %>%
      #median_hdi() %>%
      transmute(stress, group, .draw, .value, term = "y"),

    gamm_log_group_stress %>%
      emtrends(spec = ~ time_zero + stress + group,
        var = "time_zero",
        at = list(time_zero = 4),
        delta.var = 0.001,
        epred = T) %>%
      gather_emmeans_draws() %>%
      mutate(.value = .value / 50) %>%
      #median_hdi() %>%
      transmute(stress, group, .draw, .value, term = "slope")) %>%
  pivot_wider(names_from = term, values_from = .value) %>%
  mutate(x = 4, intercept = find_intercept(x1 = 4, y1 = y, slope = slope))

marginal_slopes_p1b <- gamm_log_group_stress %>%
  emtrends(
    spec = ~ time_zero + stress + group,
    var = "time_zero",
    at = list(time_zero = 4),
    delta.var = 0.001,
    epred = T) %>%
  gather_emmeans_draws() %>%
  ggplot() +
    aes(y = .value / 50, x = group, fill = group) +
    facet_grid(. ~ stress) +
    stat_slab(alpha = 0.7, color = "white", show.legend = F) +
    stat_pointinterval(pch = 21, point_fill = "white", show.legend = F) +
    scale_fill_manual(name = NULL, values = my_colors, labels = NULL) +
    coord_cartesian(ylim = c(NA, NA)) +
    labs(x = NULL, y = "Marginal slope estimate")

marginal_slopes_p2 <- gamm_log_group_stress_plot +
  geom_abline(data = sample_n(lines, 200), alpha = 0.03, size = 0.25,
    aes(intercept = intercept, slope = slope, color = group)) +
    theme(strip.text.x = element_blank())

marginal_slopes_p1b / marginal_slopes_p2
```
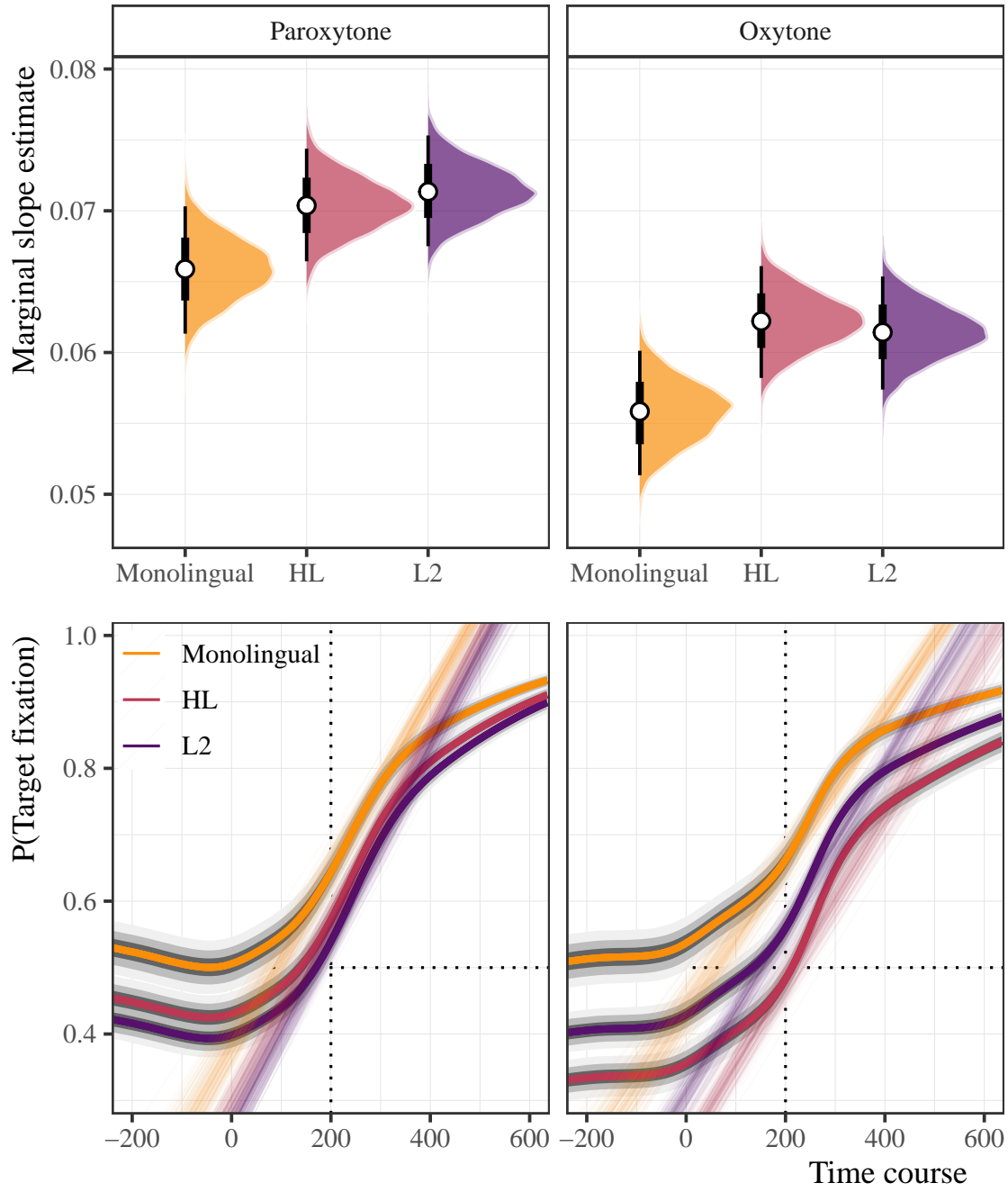
Figure 4.5: Marginal slope estimates 200ms after the offset of 1st syllable for monolinguals, heritage learners, and L2 learners in paroxytone (*CANto*) and oxytone (*canTO*) conditions.

4.2 Bilingual model

```r
gamm_log_bi_stress_draws <- gamm_log_bi_stress %>%
  emmeans(
    spec = ~ time_zero + stress + group + use_z + prof_z,
    epred = T,
    at = list(
      time_zero = seq(-4.8, 12.8, 0.25),
      prof_z = 0, use_z = 0
      ),
    ra_formula = NULL) %>%
  gather_emmeans_draws()

gamm_bi_p1 <- gamm_log_bi_stress_draws %>%
  ggplot() +
    aes(x = time_zero, y = .value / 50, color = stress) +
    facet_grid(. ~ group) +
    geom_hline(yintercept = 0.5, lty = 3, size = 0.5) +
    geom_vline(xintercept = 0 + 4, lty = 3, size = 0.5) +
    stat_lineribbon(show.legend = F) +
    stat_summary(fun = mean, geom = "line") +
    scale_fill_brewer(palette = "Greys") +
    scale_color_brewer(name = NULL, palette = "Dark2",
      labels = c("Paroxytone\n(CANta)", "Oxytone\n(canTO)")) +
    coord_cartesian(xlim = c(-4.8, 12.8), ylim = c(0.28, 1.02),
      expand = F) +
    scale_x_continuous(breaks = seq(-4, 12, 4)) +
    labs(y = "P(Target fixation)", x = NULL) +
    theme(legend.position = c(0.12, 0.86),
          legend.key.size = unit(1.7, 'lines'),
          legend.text = element_text(size = 10),
        axis.text.x = element_blank(), axis.ticks.x = element_blank())

# Calculate difference smooths
gamm_log_bi_stress_draws_diffs <- gamm_log_bi_stress_draws %>%
  pivot_wider(names_from = stress, values_from = .value) %>%
  mutate(diff = Paroxytone - Oxytone)

# Plot smooths
gamm_bi_p2 <- gamm_log_bi_stress_draws_diffs %>%
  ggplot() +
    aes(x = time_zero, y = diff / 50) +
    facet_grid(. ~ group) +
    geom_hline(yintercept = 0, lty = 3, size = 0.5) +
    geom_vline(xintercept = 0 + 4, lty = 3, size = 0.5) +
```

```
    stat_lineribbon(color = "#11111100", show.legend = F,
      .width = c(0.1, 0.35, 0.5, 0.6, 0.7, 0.8, 0.9, 0.95)) +
    scale_color_viridis_d(aesthetics = "fill", option = "C") +
    coord_cartesian(xlim = c(-4.8, 12.8), expand = F) +
    scale_x_continuous(breaks = seq(-4, 12, 4), labels = seq(-200, 600, 200)) +
    labs(y = "Difference smooths\nParoxytone - Oxytone", x = "Time course") +
    theme(strip.background = element_blank(), strip.text = element_blank())

gamm_bi_p1 / gamm_bi_p2
```
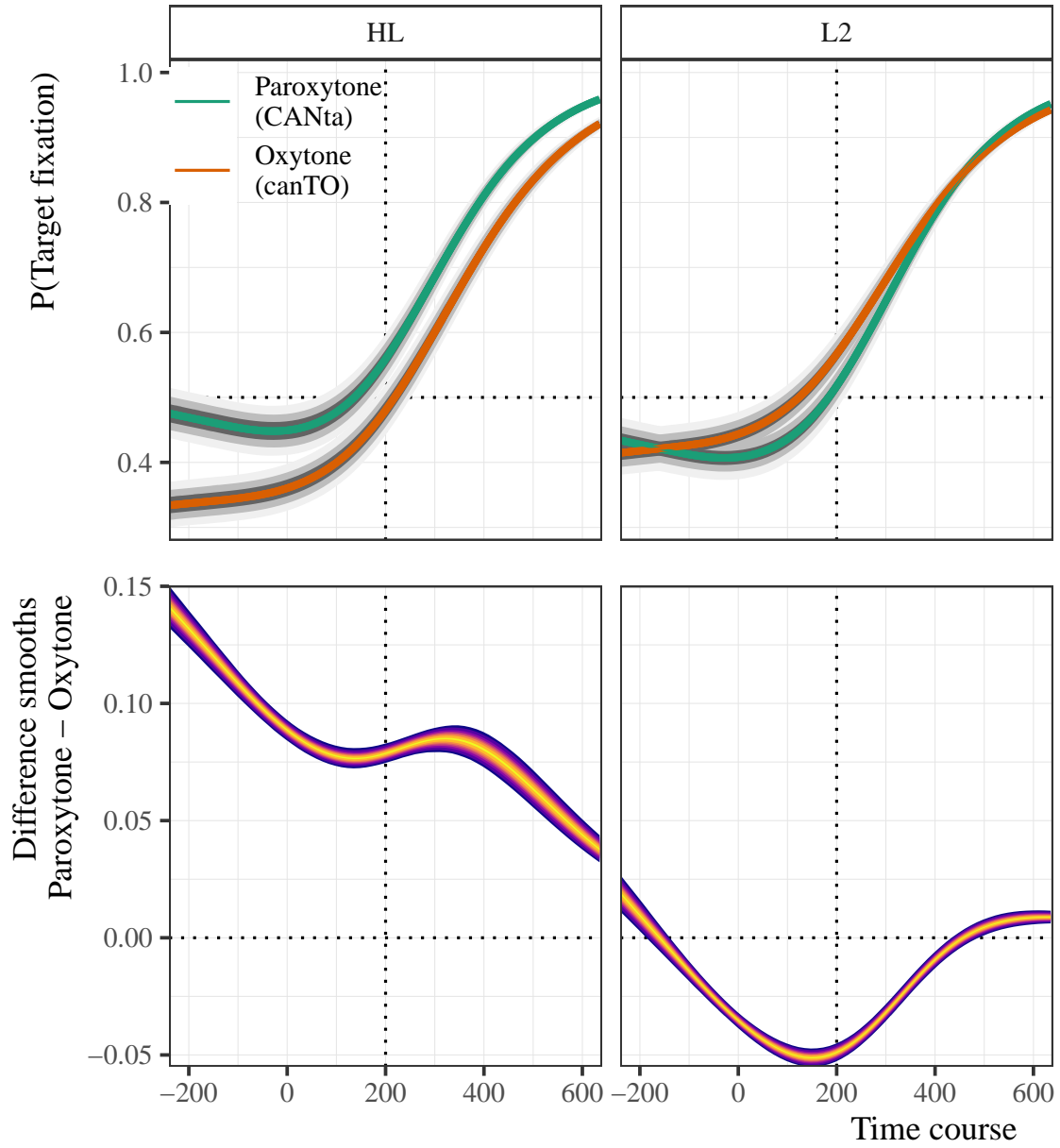
Figure 4.6: Probability of fixating on target as a function of stress for the bilingual groups. The time course is centered around the target syllable offset (point 0). Vertical lines represent 200ms after target syllable offset. Lines represent paroxytone ('CANta', green) and oxytone ('canTO', orange) conditions plus 95%, 80%, and 50% credible intervals. Pairwise difference smooths for paroxytone and oxytone items. From dark to light, colors represent 95%, 80%, 70%, 60%, 50%, 35% and 10% credible intervals.

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Chapter 5

Tables

5.1 Group model

```r
group_gamm_tib_prep <- bind_rows(
  summary(gamm_log_group_stress)[["fixed"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Population"),
  summary(gamm_log_group_stress)[["random"]][["id"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Grouping"),
  summary(gamm_log_group_stress)[["splines"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Smooths")
) %>%
  mutate(across(-c("Effect", "Term"), specify_decimal, k = 2)) %>%
  mutate(Term = case_when(
      Term == "groupHL" ~ "HL",
      Term == "groupL2" ~ "L2",
      Term == "stressOxytone" ~ "Oxytone",
      Term == "groupHL:stressOxytone" ~ "HL:Oxytone",
      Term == "groupL2:stressOxytone" ~ "L2:Oxytone",
      Term == "stime_zero_1" ~ "Time",
      Term == "stime_zero:stressOxytone_1" ~ "Time:Oxytone",
      Term == "sds(stime_zero_1)" ~ "sds(Time)",
      Term == "sds(stime_zerostressOxytone_1)" ~ "sds(Time:Oxytone)",
      TRUE ~ Term))

group_gamm_tib <- group_gamm_tib_prep %>%
  transmute(Effect, Term, Estimate,
```

```
    HDI = glue::glue("[{`l-95% CI`}, {`u-95% CI`}]"),
    Rhat, `Bulk ESS` = Bulk_ESS, `Tail ESS` = Tail_ESS) %>%
  mutate(
    Estimate = str_replace_all(Estimate, "-", "\U2212"),
    HDI = str_replace_all(HDI, "-", "\U2212")
  ) %>%
  write_csv(here("tables", "tab_group_gamm_mod.csv"))

group_gamm_tib %>%
  knitr::kable(format = "pandoc",
    align = c("l", "l", "r", "r", "r", "r", "r"),
    caption = "Group GAMM summary.")
```

Table 5.1: Group GAMM summary.

Effect	Term	Estimate	HDI	Rhat	Bulk ESS	Tail ESS
Population	Intercept	0.60	[0.44, 0.76]	1.00	797.53	1436.65
Population	HL	-0.30	$[-0.53, -0.11]$	1.01	744.97	1223.82
Population	L2	-0.43	$[-0.64, -0.23]$	1.00	708.42	761.10
Population	Oxytone	0.06	[0.05, 0.08]	1.00	3429.99	3735.29
Population	HL:Oxytone	-0.44	$[-0.46, -0.42]$	1.00	3469.26	3630.77
Population	L2:Oxytone	0.00	$[-0.02, 0.02]$	1.00	3114.31	3926.50
Population	Time	-0.26	$[-0.26, -0.26]$	1.00	3581.16	3934.31
Population	Time:Oxytone	-0.01	$[-0.01, -0.01]$	1.00	3865.39	3348.79
Grouping	sd(Intercept)	0.45	[0.40, 0.51]	1.00	1088.45	1923.43
Smooths	sds(Time)	0.03	[0.02, 0.06]	1.00	1620.98	2149.99
Smooths	sds(Time:Oxytone)	0.02	[0.01, 0.04]	1.00	2522.74	3383.84

```
# Get posterior and cleanup colnames and term names
group_gamm_tab_dat <- as_draws_df(gamm_log_group_stress) %>%
  select(starts_with(c("b_", "bs_", "sd_", "sds_"))) %>%
  pivot_longer(cols = everything()) %>%
  mutate(type = case_when(
      startsWith(name, "b_") ~ "Parametric\nPopulation",
      startsWith(name, "bs_") ~ "Non-parametric\nPopulation",
      startsWith(name, "sd_") ~ "Grouping",
      startsWith(name, "sds_") ~ "Smooth"),
    type = fct_relevel(type, "Parametric\nPopulation",
      "Non-parametric\nPopulation", "Grouping")) %>%
  mutate(name = case_when(
      name == "b_Intercept" ~ "Intercept",
      name == "b_groupHL" ~ "HL",
      name == "b_groupL2" ~ "L2",
```
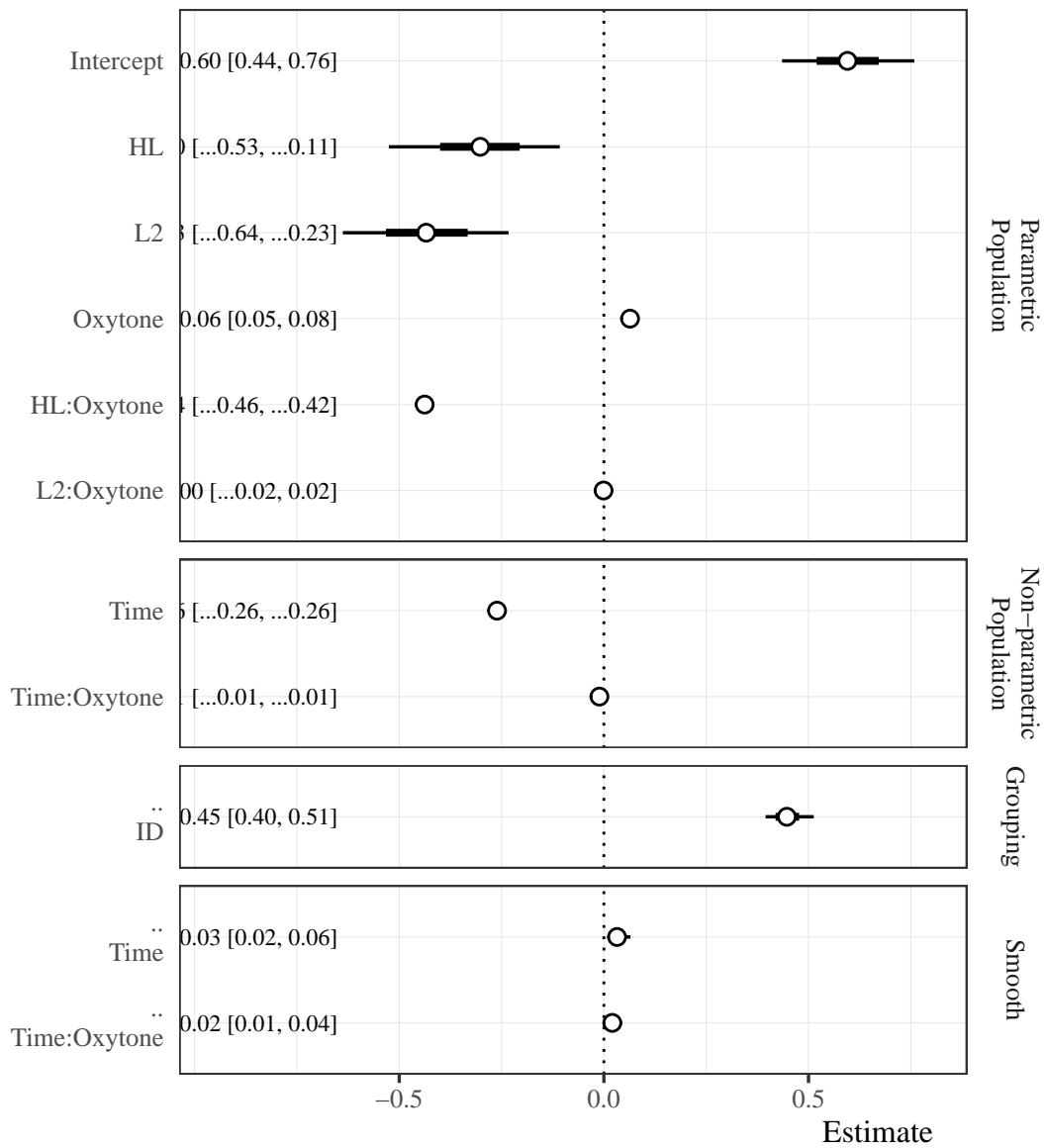
```r
        name == "b_stressOxytone" ~ "Oxytone",
        name == "b_groupHL:stressOxytone" ~ "HL:Oxytone",
        name == "b_groupL2:stressOxytone" ~ "L2:Oxytone",
        name == "bs_stime_zero_1" ~ "Time",
        name == "bs_stime_zero:stressOxytone_1" ~ "Time:Oxytone",
        name == "sd_id__Intercept" ~ " \nID",
        name == "sds_stime_zero_1" ~ " \nTime",
        name == "sds_stime_zerostressOxytone_1" ~ " \nTime:Oxytone",
    )
  ) %>%
  mutate(name = fct_relevel(name, " \nTime:Oxytone", " \nTime", " \nID",
    "Time:Oxytone", "Time", "L2:Oxytone", "HL:Oxytone", "Oxytone", "L2", "HL",
    "Intercept"))

# Summarize posterior for printing estimates in plot
group_gamm_summary <- group_by(group_gamm_tab_dat, name, type) %>%
  mean_qi(value, .width = 0.95) %>%
  mutate_if(is.numeric, specify_decimal, k = 2) %>%
  mutate(label = glue::glue("{value} [{.lower}, {.upper}]"),
         label = str_replace_all(label, "-", "\U2212"))

# Forest plot
group_gamm_tab_dat %>%
  ggplot(., aes(x = value, y = name)) +
    facet_grid(type ~ ., scales = "free", space = "free") +
    geom_vline(xintercept = 0, lty = 3) +
    stat_pointinterval(point_fill = "white",  pch = 21, show.legend = F) +
    geom_text(data = group_gamm_summary,
      hjust = 1, family = "Times", size = 3.25,
      aes(group = type, label = label, x = -0.65)) +
    coord_cartesian(xlim = c(-0.95, 0.8)) +
    scale_x_continuous(breaks = c(-0.5, 0, 0.5, 1)) +
    labs(y = NULL, x = "Estimate") +
    theme(plot.margin = unit(x = c(0, 0, 0, 0), units = "mm"),
      strip.placement = "outside", strip.background = element_blank(),
      axis.text.y = element_text(hjust = 1), axis.ticks.y = element_blank())
```

Parametric Population

Intercept	0.60 [0.44, 0.76]
HL	0 [...0.53, ...0.11]
L2	8 [...0.64, ...0.23]
Oxytone	0.06 [0.05, 0.08]
HL:Oxytone	4 [...0.46, ...0.42]
L2:Oxytone	00 [...0.02, 0.02]

Non-parametric Population

Time	5 [...0.26, ...0.26]
Time:Oxytone	[...0.01, ...0.01]

Grouping

ID	0.45 [0.40, 0.51]

Smooth

Time	0.03 [0.02, 0.06]
Time:Oxytone	0.02 [0.01, 0.04]

```r
group_prediction_tib <- gamm_log_group_stress_dat %>%
  group_by(stress, group) %>%
  summarize(.groups = "drop",
    hdi = mean_qi(prop),
    rope = rope(prop, range = c(0, 0.51)),
    PD = pd(prop, null = 0.5)[1]) %>%
  transmute(Group = group, Stress = stress, Estimate = hdi$y,
```

```
   lower = hdi$ymin, upper = hdi$ymax, ROPE = rope$ROPE_Percentage, PD) %>%
 mutate_if(is.numeric, specify_decimal, k = 2) %>%
 transmute(Group, Stress, Estimate,
   HDI = glue::glue("[{lower}, {upper}]"), ROPE, PD,
   parameter = glue::glue("{Group}_{Stress}")) %>%
 arrange(Group) %>%
 write_csv(here("tables", "tab_group_prediction.csv"))

group_prediction_tib %>%
 select(-parameter) %>%
 knitr::kable(format = "pandoc",
   align = c("l", "l", "r", "r", "r", "r"),
   caption = "Group prediction summary.")
```

Table 5.2: Group prediction summary.

Group	Stress	Estimate	HDI	ROPE	PD
Monolingual	Paroxytone	0.64	[0.61, 0.68]	0.00	1.00
Monolingual	Oxytone	0.66	[0.63, 0.70]	0.00	1.00
HL	Paroxytone	0.57	[0.54, 0.60]	0.00	1.00
HL	Oxytone	0.48	[0.45, 0.52]	0.97	0.85
L2	Paroxytone	0.54	[0.51, 0.57]	0.01	1.00
L2	Oxytone	0.56	[0.53, 0.59]	0.00	1.00

```
group_marginal_slopes_post <- lines %>%
 ungroup() %>%
 select(stress, group, slope) %>%
 group_by(stress, group) %>%
 mutate(draw = seq_along(group)) %>%
 pivot_wider(names_from = "group", values_from = "slope") %>%
 transmute(stress,
   mono_hl = Monolingual - HL, mono_l2 = Monolingual - L2, hl_l2 = HL - L2) %>%
 pivot_longer(cols = -stress, names_to = "comp", values_to = "diff") %>%
 mutate(comp = str_replace_all(comp, "_", " - "),
        comp = str_to_upper(comp),
        comp = str_replace_all(comp, "MONO", "Mono"))

marginal_slopes_p2 <- group_marginal_slopes_post %>%
 ggplot() +
   aes(x = diff, y = comp, fill = stat(abs(x) >= 0.001)) +
   facet_grid(. ~ stress) +
   geom_rect(data = tibble(x = c(-0.001, 0.001), y = NULL),
     aes(xmin = min(x), xmax = max(x), ymin = -Inf, ymax = Inf),
```

```
      fill = "lightblue", alpha = 0.2, inherit.aes = FALSE) +
    geom_vline(xintercept = 0, lty = 3, size = 0.5) +
    stat_slab(alpha = 0.7, color = "white", show.legend = F) +
    stat_pointinterval(pch = 21, point_fill = "white", show.legend = F) +
    scale_fill_manual(name = NULL, values = my_colors[2:3], labels = NULL) +
    scale_color_manual(name = NULL, values = my_colors[2:3], labels = NULL) +
    coord_cartesian(xlim = c(-0.011, NA)) +
    labs(y = NULL, x = "Difference estimate")

marginal_slopes_p1 / marginal_slopes_p2
```
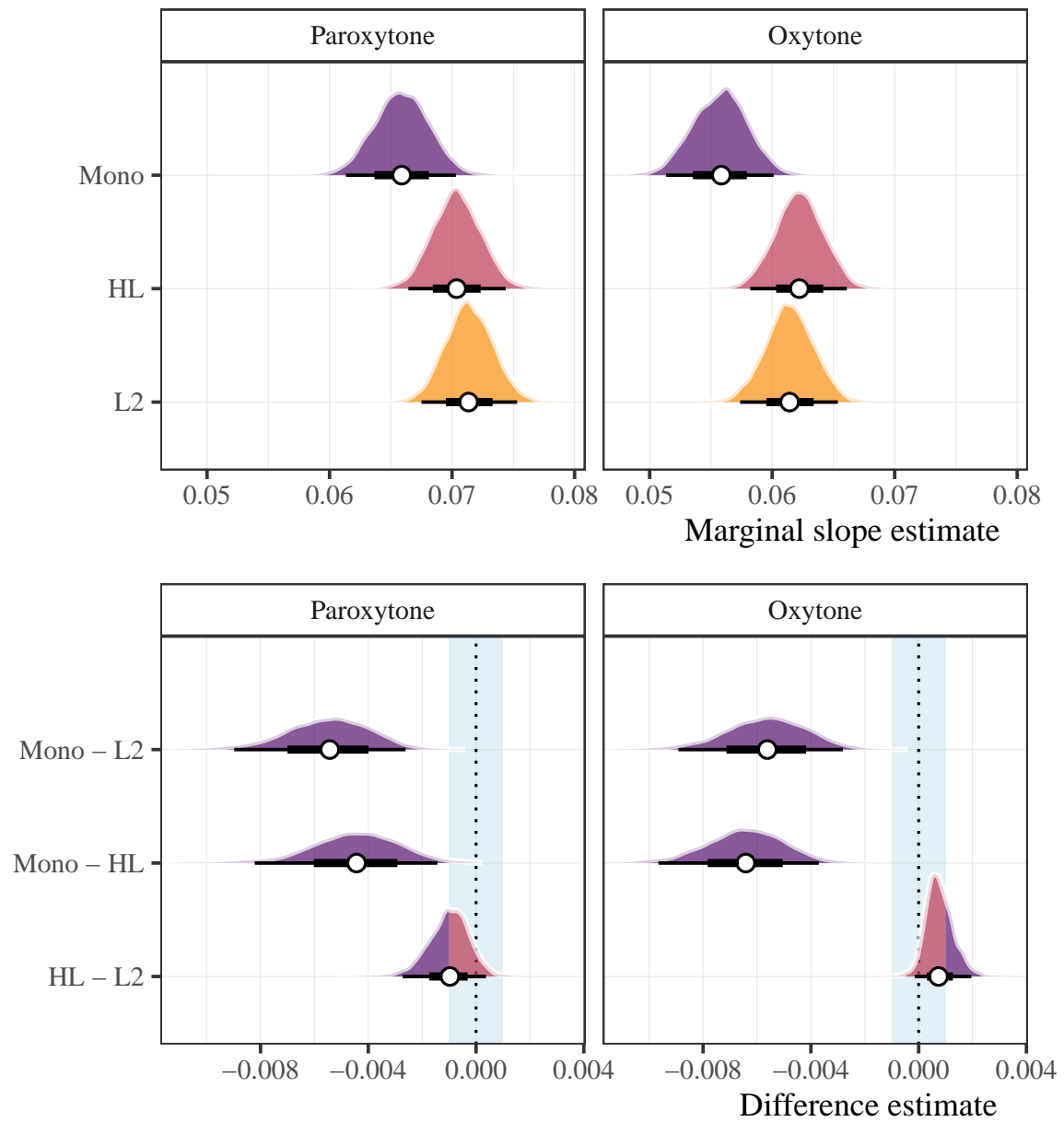
```
group_marginal_slopes_tib <- group_marginal_slopes_post %>%
  group_by(stress, comp) %>%
  summarize(.groups = "drop",
```

```
    hdi = mean_qi(diff),
    rope = rope(diff, range = c(-0.001, 0.001)),
    PD = pd(diff, null = 0)[1]) %>%
  transmute(Stress = stress, Comparison = comp, Estimate = hdi$y,
    lower = hdi$ymin, upper = hdi$ymax, ROPE = rope$ROPE_Percentage, PD) %>%
  mutate_if(is.numeric, specify_decimal, k = 3) %>%
  transmute(Stress, Comparison, Estimate,
    HDI = glue::glue("[{lower}, {upper}]"), ROPE, PD,
    parameter = glue::glue("{Stress}_{Comparison}")) %>%
  arrange(Stress) %>%
  write_csv(here("tables", "tab_group_marginal_slopes.csv"))

group_marginal_slopes_tib %>%
  select(-parameter) %>%
  knitr::kable(format = "pandoc",
    align = c("l", "l", "r", "r", "r", "r"),
    caption = "Group marginal slopes pairwise comparisons summary.")
```

Table 5.3: Group marginal slopes pairwise comparisons summary.

Stress	Comparison	Estimate	HDI	ROPE	PD
Paroxytone	HL - L2	-0.001	[-0.003, 0.000]	0.514	0.922
Paroxytone	Mono - HL	-0.004	[-0.008, -0.001]	0.000	0.999
Paroxytone	Mono - L2	-0.006	[-0.009, -0.003]	0.000	1.000
Oxytone	HL - L2	0.001	[0.000, 0.002]	0.697	0.957
Oxytone	Mono - HL	-0.006	[-0.010, -0.004]	0.000	1.000
Oxytone	Mono - L2	-0.006	[-0.009, -0.003]	0.000	1.000

5.2   Bilingual model

```
bi_gamm_tib_prep <- bind_rows(
  summary(gamm_log_bi_stress)[["fixed"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Population"),
  summary(gamm_log_bi_stress)[["random"]][["id"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Grouping"),
  summary(gamm_log_bi_stress)[["splines"]] %>%
    as_tibble(rownames = "Term") %>%
    mutate(Effect = "Smooths")
) %>%
  mutate(across(-c("Effect", "Term"), specify_decimal, k = 2)) %>%
```

```
  mutate(Term = case_when(
      Term == "groupL2" ~ "L2",
      Term == "stressOxytone" ~ "Oxytone",
      Term == "prof_z" ~ "Proficiency",
      Term == "use_z" ~ "Use",
      Term == "groupL2:stressOxytone" ~ "L2:Oxytone",
      Term == "stime_zero_1" ~ "Time",
      Term == "stime_zero:stressOxytone_1" ~ "Time:Oxytone",
      Term == "sds(stime_zero_1)" ~ "sds(Time)",
      Term == "sds(stime_zerostressOxytone_1)" ~ "sds(Time:Oxytone)",
      TRUE ~ Term))

bi_gamm_tib <- bi_gamm_tib_prep %>%
  transmute(Effect, Term, Estimate,
    HDI = glue::glue("[{`l-95% CI`}, {`u-95% CI`}]"),
    Rhat, `Bulk ESS` = Bulk_ESS, `Tail ESS` = Tail_ESS) %>%
  mutate(
    Estimate = str_replace_all(Estimate, "-", "\U2212"),
    HDI = str_replace_all(HDI, "-", "\U2212")
  ) %>%
  write_csv(here("tables", "tab_bi_gamm_mod.csv"))

bi_gamm_tib %>%
  knitr::kable(format = "pandoc",
    align = c("l", "l", "r", "r", "r", "r", "r"),
    caption = "Bilingual GAMM summary.")
```

Table 5.4: Bilingual GAMM summary.

Effect	Term	Estimate	HDI	Rhat	Bulk ESS	Tail ESS
Population	Intercept	0.38	[0.22, 0.53]	1.01	565.11	1104.64
Population	L2	-0.17	[-0.37, 0.04]	1.02	439.52	928.86
Population	Oxytone	-0.39	[-0.41, -0.38]	1.00	3169.14	3706.47
Population	Proficiency	0.04	[-0.06, 0.14]	1.01	668.20	1129.77
Population	Use	0.02	[-0.09, 0.12]	1.00	686.17	1083.40
Population	L2:Oxytone	0.51	[0.50, 0.53]	1.00	3124.51	3462.27
Population	Time	1.49	[1.48, 1.51]	1.00	3101.44	3522.33
Population	Time:Oxytone	0.00	[-0.02, 0.02]	1.00	2909.08	3457.55
Grouping	sd(Intercept)	0.49	[0.42, 0.58]	1.00	904.53	1272.59
Smooths	sds(Time)	1.39	[0.34, 3.86]	1.00	2319.02	2697.02
Smooths	sds(Time:Oxytone)	0.88	[0.10, 3.27]	1.00	1838.93	1948.50

```r
# Get posterior and cleanup colnames and term names
bi_gamm_tab_dat <- as_draws_df(gamm_log_bi_stress) %>%
  select(starts_with(c("b_", "bs_", "sd_", "sds_"))) %>%
  pivot_longer(cols = everything()) %>%
  mutate(type = case_when(
      startsWith(name, "b_") ~ "Parametric\nPopulation",
      startsWith(name, "bs_") ~ "Non-parametric\nPopulation",
      startsWith(name, "sd_") ~ "Grouping",
      startsWith(name, "sds_") ~ "Smooth"),
    type = fct_relevel(type, "Parametric\nPopulation",
      "Non-parametric\nPopulation", "Grouping")) %>%
  mutate(name = case_when(
      name == "b_Intercept" ~ "Intercept",
      name == "b_groupL2" ~ "L2",
      name == "b_stressOxytone" ~ "Oxytone",
      name == "b_prof_z" ~ "Proficiency",
      name == "b_use_z" ~ "Use",
      name == "b_groupL2:stressOxytone" ~ "L2:Oxytone",
      name == "bs_stime_zero_1" ~ "Time",
      name == "bs_stime_zero:stressOxytone_1" ~ "Time:Oxytone",
      name == "sd_id__Intercept" ~ " \nID",
      name == "sds_stime_zero_1" ~ " \nTime",
      name == "sds_stime_zerostressOxytone_1" ~ " \nTime:Oxytone",
    )
  ) %>%
  mutate(name = fct_relevel(name, " \nTime:Oxytone", " \nTime", " \nID",
    "Time:Oxytone", "Time", "L2:Oxytone", "Use", "Proficiency", "Oxytone",
    "L2", "Intercept"))

# Summarize posterior for printing estimates in plot
bi_gamm_summary <- group_by(bi_gamm_tab_dat, name, type) %>%
  mean_qi(value, .width = 0.95) %>%
  mutate_if(is.numeric, specify_decimal, k = 2) %>%
  mutate(label = glue::glue("{value} [{.lower}, {.upper}]"),
         label = str_replace_all(label, "-", "\U2212"))

# Forest plot
bi_gamm_tab_dat %>%
  ggplot(., aes(x = value, y = name)) +
    facet_grid(type ~ ., scales = "free", space = "free") +
    geom_vline(xintercept = 0, lty = 3) +
    stat_pointinterval(point_fill = "white",  pch = 21, show.legend = F) +
    geom_text(data = bi_gamm_summary,
      hjust = 1, family = "Times", size = 3.25,
      aes(group = type, label = label, x = -0.62)) +
```

```
coord_cartesian(xlim = c(-1.5, 4)) +
scale_x_continuous(breaks = c(-1, 0, 1, 2, 3, 4)) +
labs(y = NULL, x = "Estimate") +
theme(plot.margin = unit(x = c(0, 0, 0, 0), units = "mm"),
  strip.placement = "outside", strip.background = element_blank(),
  axis.text.y = element_text(hjust = 1), axis.ticks.y = element_blank())
```