## 1. linear algebra:

linear algebra deals with linear systems. Their transformation and their applications

every LT & LS can be expressed in terms of matrices

me he of yours h = he ob colors

If in +n > Amen is ractargular matrix 98 m=n => Amxn is 39 matrix

Colomn Vector A - [aij]

raw vector: A= [aij] = XH

of 
$$\alpha_{ij} = 0$$
 for  $i \neq j$ 

$$S = \begin{pmatrix} 2 & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{pmatrix}$$

I roduct of two matric:

Note: 1) AB & BA (Not committation) 2) A(BC) = (AB) C (Associative)

I) the no of xes orequired to compute (A-B)mag = mpg

2) the no. of +" " " (A.B) = m(r.)2

let Prize, Pary, Ray be 3 matrices find the minimum no of x" required to compute POR?

4x3x4 + 4x4x1

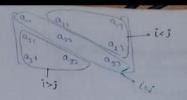
we know that p(QR) = (PP)R

consider : P(GR)

PAXX (QR) = NO OF XM = 4x 2x1 = 8

Consider: (PG) R

Pare Para -7 No ob X" = 4x2x4=32 he of Xu = xxxxx =



lower triangular matrix :

if listo for ces

upper triangular matrix .

Diagonal matrix :

Scaller matrice :-

Here the environ so of undiplication required Food POR = 16

The maximum of no of multiplication required : 42

. The minimum and of addition prequired in finding for

Transpose of matrix :

$$A = \begin{bmatrix} 1 & -1 & 2 \\ 2 & 1 & 3 \\ 2 & 2 & 3 \end{bmatrix} \qquad \Rightarrow \qquad A = \begin{bmatrix} 0 & 2 & 1 \\ -1 & 2 & 3 \\ 2 & 2 & 3 \end{bmatrix}$$

Properties . (AT) = A

$$(A+B)^T = A^T + C^T$$

Symmetric matrics:-

$$A = [a_{1i}]_{n \times n}$$
 is syn matrix  
iff  $[A^T = A]$  (or)  $[(a_{1i}) = a_{1i}]$ 

Properties - let AB are sym matrics ie AT = A; BT = B

Then 
$$\bigcirc$$
 AT is symmatrix

(3) A. A. A. A. A. B. C. Symm

(3) AB + BA C. Symm.

(4) AB + BA C. Symm.

(5) AB + BA C. Symm.

(6) AB + BA C. Symm.

(7) AB + BA C. Symmetric

(8) AB + BA C. Symmetric

(9) AB + BA

(10) AB + BA

(11) AB + BA

(12) AB + BA

(13) AB + BA

(14) AB + BA

(15) AB + BB

(16) AB + BB

(17) AB + AB

(18) AB + BB

(

Properties: let A, B are skew sym matric 
$$[-c, A^T = -A]$$
 (or)  $\begin{bmatrix} a_{ij} = -a_{ji} \\ a_{il} = 0 \end{bmatrix}$ 

Then An is symptometric if he add

(a) An is skew symptoms if he add

(b) An is skew symptoms if he add

(1) AIR+LB IS skew - 20 (1) AB+BA ISSMU. Matrice

Note - every square matrix can be expressed as

$$\begin{aligned} P_{n\times n} &= \frac{1}{2} \left[ R + R^T \right] &+ \frac{1}{2} \left[ R - R^T \right] \\ &+ \frac{1}{2} \left[ R - R^T \right] \\ &+ \frac{1}{2} \left[ R + R \right] \end{aligned}$$

$$= \frac{1}{2} \left[ \left[ R + R^T \right] + \left[ R - R^T \right] \right]$$

$$= \frac{1}{2} \left[ \left[ R + R^T \right] + \left[ R - R^T \right] \right]$$

AB is show symmetric if 
$$AB + BB - null models$$
 $(A^n)^T = (A^T)^n = (-1A)^n = (-1)^n A^n$ 
 $(A^n)^T = B^T A^T = B A = -AB = a BA - BB = a$ 
 $AB - BA = a Show symmetric matrices.$ 

Trace  $(A_{nul}) = a_{11} + a_{22} + \cdots - a_{mn}$ 

complex matrices:

 $A = \begin{bmatrix} a_{12} \\ a_{13} \end{bmatrix}_{m \times n}$ 
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(a) 
$$T = A$$

(b)  $T = A$ 

(c)  $T = A$ 

(d)  $T = A$ 

(e)  $T = A$ 

(e)  $T = A$ 

(e)  $T = A$ 

(f)  $T = A$ 

(f)

A = [ais] nxn is Hm it A = AT

It A is him as then "In" is show him and orthogonal matrix:

Then 
$$A = I = A^{T} \cdot A$$
  
Then  $A = I = A^{T} \cdot A$   
(in)  $A^{-1} = A^{T}$ 

$$M = \begin{pmatrix} 35 & 45 \\ 2 & 95 \end{pmatrix} \qquad L(m^2 = m^2) \text{ then } \propto 1^2$$

$$M^{-1} = M^{T} \implies M M^{T} = I$$

$$\begin{bmatrix} 3_{\frac{1}{3}} & 4_{\frac{1}{3}} \\ x & 3_{\frac{1}{3}} \end{bmatrix} \begin{bmatrix} 3_{\frac{1}{3}} & x \\ 9_{\frac{1}{3}} & 9_{\frac{1}{3}} \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

$$\frac{3}{5}x + \frac{4}{5}x \frac{9}{5} = 0$$

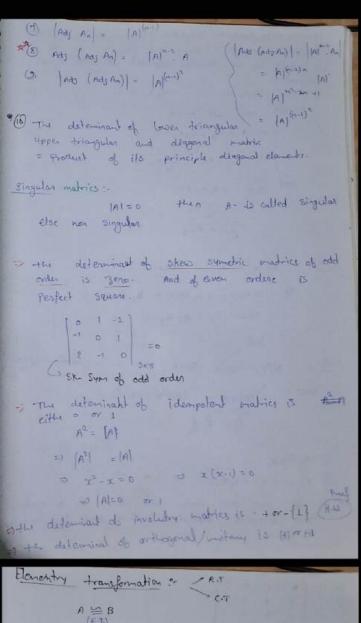
$$\Rightarrow \boxed{x = -\frac{6}{3}}$$

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Unit any matrix :
     A.A. I = A.A
       Then is is unitrary
     (or) A' = A"
Edempotent matrix:
         96 A2 - A
Properties: let A,B are idempotent matrix
     ie. A^2 = A B^2 = B then
   1 A+B is idenpotent if and only if AB+BA
     (A+B)2 = A2+B2 + A + + BA
         = (A+B)
    (1) AB is idempotent if and only if AB AB=
   (3) A" = A B" = B
 Note: @ 96 AB=P. ABA=A +hen A=A, B=B
  (1) 96 AB: A & BA: B . Hem A2=A . B2=B
  \{A^2 - A \cdot A = A \cdot (BA) = (AB)A - BA = A \}
Q:00 xy = y & yx = x then x2+y2 = x+y
         x5+45= x+4
          2 +4n = 2+4
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go AB are of same sizer and AB=B 1 DB=A then (Ant = ? a) 2, (V+B) a) 22 (V+B) given ABOB I BAON & ATOM (A+B) = A2 + B2 + AB + BA = A4B + A + B = 2 [A+B] - O [A+B) = 2[A+B] = 2[2(A+B)] = 2 [A+B] [A+B] = 2 [A+B] - 2º [2 [A+P]] = 23 [A+B] X14 by (A+B) on bs  $(B+B)^5 = 2^3 (A+B)^2$ (A+B)5 = 23 (2 (A+B)) Involutory matrix: 96 A° = I then A is involutely making A ..... where is a competition 9-19 :- A= { 1 0 0 } where the works determinant of matrix .

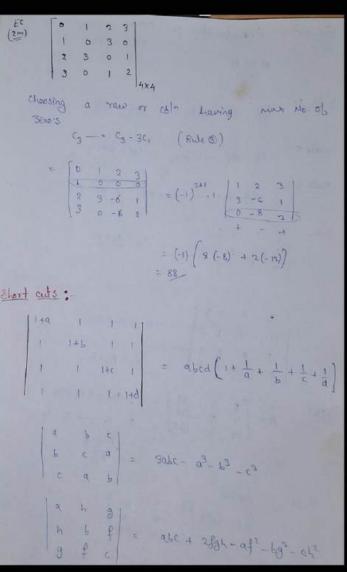
Definition:

Definition:  $|A_{n\times n}| = \sum_{j=1}^{n} \{-1\}^{j+1} \text{ arg } 9 \text{ sig}$ where  $S_{ij} = \text{ minor } a_{ij}$  and element  $a_{ij}$ is  $|a_{1i} - a_{12} - a_{23}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{1i} - a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1}$   $|a_{2i} - a_{2i}| = (-1)^{i+1}a_{1i} S_{n-1} + (-1)^{i+2}a_{1i} S_{n-1} + (-1)^{i+3}a_{1i} S_{n-1} + (-1)^{i+3}a_{1$ 



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Rule 1: 36 Ri - Rs => |A| = -|B|
Rub 2:- 36 Rt -- KRE -> |B| = K|A|
Rule 3:- $46 R_0 \longrightarrow R_0 + KR_1 \Rightarrow |B| = |R|
            -1 1 1 "R3 = R3 + R3
                 3 4 R3=R14R
       A = 7 8 105
                       45
                             1 R2 -> R2+R3
             13 2 195
                                2. c1 - c1-c3
      (B)=?
  Rule (8) Applied
           |\beta| = |A| = \begin{bmatrix} 8 & 4 & 45 \\ 9 & 8 & 105 \\ 13 & 2 & 195 \end{bmatrix}
               [A = 15 ] 4 3] C. = 5
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A set of vectors (Rows and colons) or To are said to be linearly dependent if the linear
     \alpha_1 x_1 + \alpha_2 x_2 + \cdots + \alpha_n x_n = 0
   for all not all a = a
        a, x, + a, x, + a, x, = 0
    (\infty) \alpha_1 x_1 + a_2 x_2 = 0
             7, = -9, 23
               X .: K . 6X
 ex: Sin x, Gsx, tanx
      96 a, sinx, + a, cox + b, tanx =0
           Then a, = 0,=03=0
  Ex sin2x, Gos2x, GO2X
    WKT (052x = 1652x-15143x
              易一男子
  1 Ri - KR;
 ( Ri = A, Ri + Az RK
Note: 36 any two rows we colors or a making
     are linearly deponded then and the determ
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1 6 62 = (a-6)(6-c) (c-a)  $\begin{vmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 1 & 1 & 2 & 1 \\ 1 & 1 & 2 & 1 \end{vmatrix} = 1 \cdot \left[ 1 + \frac{1}{1} + \frac{1}{1} + \frac{1}{1} + \frac{1}{1} \right] = 5$  $\begin{vmatrix} 1 & 2 & 3 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{vmatrix} = 3(1)(2)(3) - 1^{2} \cdot 2^{8} - 3^{3} =$ a=1, b=2, c=3, 1=-1, 9=2, f=1 1 -1 21 -1 2 1 2 1 3 = 5 + 2x(2) -1 -4 +3 90 for a + 6 76 96 | a a2 a3+1 | 6 62 63+1 = 0 them abe=? c c2 c3+1  $\begin{vmatrix} a & a^2 & a^3 \\ b & b^2 & b^3 \\ c & c^2 & c^3 \end{vmatrix} + \begin{vmatrix} a & a^3 & 1 \\ b & b^2 & 1 \\ c & c^2 & 1 \end{vmatrix} = 0$  $= abc \begin{vmatrix} 1 & a & a^{2} \\ 1 & 5 & 5^{2} \\ 1 & c & c^{2} \end{vmatrix} + \begin{vmatrix} 1 & a & a^{2} \\ 1 & 5 & 5^{2} \\ 1 & c & c^{2} \end{vmatrix} = 0$ = (abs +1) (a-b) (b-t) (c-a) = 0 : a + + + + = abc + + 0 . So abl = -1

(R) 
$$\begin{bmatrix} 2 & 1 & 1 & 2 \\ -1 & -1 & 1 & 1 \\ 1 & 0 & 2 & 3 \\ 0 & -1 & 3 & 4 \end{bmatrix}$$

= R<sub>1</sub> + R<sub>2</sub> = R<sub>3</sub>

R<sub>3</sub> + R<sub>3</sub> = R<sub>4</sub>

A minor  $\begin{vmatrix} 2 & 1 \\ -1 & -1 \end{vmatrix} \neq 0 \Rightarrow R_1, R_2 \text{ are Ind}$ 

= R(A) = r<sub>10</sub> = 0 \( \text{Ind your } \left| \text{col}^{10} = 2 \)

9\$ find rank % \[ 6 0 4 4 \\
-2 14 8 18 \\
14 -14 0 -10 \] & response  $\begin{bmatrix} 6 & 0 \\ -2 & 14 \end{bmatrix}$  = 84 \$ 0 => R<sub>1</sub>, R<sub>2</sub> are : F(A) = no ob Ind +000 / Coln =2

$$A = \begin{bmatrix} 2 & 3 & -1 & -1 \\ 1 & -1 & -2 & -4 \\ 3 & 1 & 9 & -2 \\ 4 & 3 & 0 & -7 \end{bmatrix} \qquad ? R_1 + R_2 + R_3 = R_4$$

Note (either find the Relation of either row or colony ext both are colomn and now analysis is time wasting) because

A number 
$$\begin{vmatrix} 2 & 3 & -1 \\ 1 & -1 & -2 \\ 3 & 1 & 3 \end{vmatrix} = 2(-1) - 3(9) - 1(3)$$

" R. R. Rs are ind (m) highest ordere of non

Rank of matrix: The no of linearly independent trows and column in a matrix is called mank The highest order of none gene minor is called Rank. let Agya 96 | ABX3 +0 Thenga = order 96 | A3x3 = 0 => 9(N) < order They if I alleast one non zero minor of order 2x2 Then 5(A) = 2 Else 9(A)=1/ find rank & 1 2 3 1 -1 0 2 1 3 " R,+R2 = R3 & minor  $\frac{4}{3}$   $\frac{1}{1}$   $\frac{2}{1}$  =  $-1-2\neq 0$ 

=> R., R2 are ind rows => P(A)= no ob Ind crows/cdn

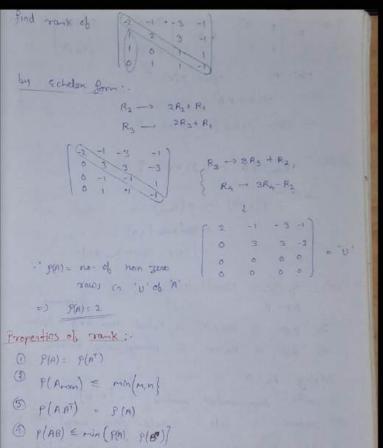
(independent)

Then 
$$T = 0$$

Soln: given  $P(A_{3N3}) = 2 \times \text{orden}$ 
 $\Rightarrow |A_{3N3}| = 0$ 
 $\Rightarrow |A_{3N3}| =$ 

P(A) = no ob non sero rows in 'v' ob'A'

.. Deft of Rank



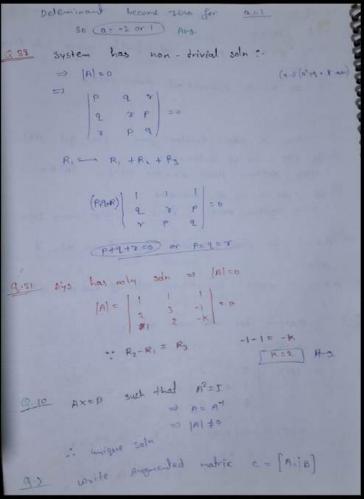
(1) P (Diagonal matrix) = no do non zero principle diagonal

(5) P(In) = n

(6) p(on) = 0

```
Pote: DAX = p
                              solu stand only
   14 1A1 $ 0
  @ 96 AX = B posses int infinitly many solution
    A-O
  (3) By AX=B inconsistant the IRI=0
 Edving Ax = 0
 (1) reduce 'A' into Echelen form we get P(A)
 @ H P(A) = no. of unknowns
    Then system posses (unique soln) 1A1 = 0
 (8 96 D(A) < no. of distinctions
    Then system passes (Al-o) only many solu
⇒ Ax=0 is posses trivial soln if and only if
                      Zero soln
    IAI + 0
          posses how trivial soln if and only if Mech
  A \times = 0
Q.7: System has ody many solar.
     -> |A| =0
      = 1A1 = | 9 1 1 |
                10 1 =0
         a(a^2-1) + (1-a) + R_1 - R_1 + R_2 + R_3
                           =0 = (4+2)
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Pr+25
                                      x2+52
         P(A) = N
                 Then 9(0)=?
       Solve .. B = AAT
        \Rightarrow P(B)= P(AAT) = P(A) = N
   9.50 :-
           X_{n_{XI}} \neq 0 , \mathfrak{P}(x_X^T) = ?
             f(x \times T) = f(x_{n_0})
                     = El mun {1,4}
                      ≤ 1 = 1 ? * *nx ≠0}
  System of linear equation:
        AX=B
     To B #0 => Ax=B is called Non-Ming Bystem
     96 peo = Ax=0 is Homogeneous system
     Solving Ax = B
    1 write Augumented matrix (=[A:B]
   (3) suduce 'c' into echelon from we get 1(0), P(4)
    (1) 36 F(A) < 9(C). Then system is Inconsisted 19/10
    (5) Al phi = p(c) = no of unknown
        Then the system posses unique sola
    (6) If of = o(1) < no. of lunknowns Then system
      poses only mass many solus, so [191=0]
            peleminant become sens for
        So (a = -2 or 1) Avy.
2 88
        system has non-drivial soln :-
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reduce c into Echelon form R2-R, , R3-R, [1 1 1 6] 8 for no 30h => 9(n) < >(c) he of non your rows in A < no ob no zero row in c for A-6=0 1 M= 20 \$0 7(A)= 2 < 9(c)=3 for to 6, who is system is incomsistant (5) why many soln P(A) = P(C) = No ob autonom P(A) = P(L) < 3 96 2 = 6, 4 = 20 = 9(N) = 9(N) = 2 x he @ wige soln: y(n) = y(c) = no of mb=3 for 246 so no. of men you rows in 1 = 3 = no ob non-seno was in y = no of sunk

Hence for 2 + 6, system posses mique sola (b) {(1,-1,0), (1,0,-1)} is a linear and selected but it is not a basis (c) 'x' is not a subspace of R3 There chiften keylow  $x = \left\{ (x_1, x_1, x_3) \in (\mathbb{R}^3) \mid x_1 + x_1 + x_3 = 0 \right\}$ let x, = k1 . x3 = k2 x1 = -x2 - x3 - $\infty_i = -K_1 - K_2$  $\begin{pmatrix} X_1 \\ X_2 \\ X_3 \end{pmatrix} = \begin{pmatrix} -K_1 - K_2 \\ K_1 \\ K_2 \end{pmatrix} = \begin{pmatrix} K_1 \begin{pmatrix} -1 \\ 1 \end{pmatrix} + \begin{pmatrix} K_2 \begin{pmatrix} -1 \\ 0 \end{pmatrix} \\ 0 \end{pmatrix}$ - for different values of k. , kz . X is is generated  $x_1 + x_2 + \alpha_3 = 0$  , therefore set of { (-1,1,0) , (-1,0,1) } spails x - Since (-1, 1,0) T and (-1,0,1) are linearly independent miner is non zero? - Hence set  $do \{(-1,+1,0)^T, (-1,0,1)^T\}$  forms a basis of dimension a there for hullity = 2 hullity = dim of space of salt ob Ax = B = no of rankn - p(A) = 3-1 = 2

 $P = \begin{bmatrix} -10 \\ -1 \end{bmatrix}$   $Q = \begin{bmatrix} -2 \\ -5 \end{bmatrix}$   $R = \begin{bmatrix} 2 \\ -7 \\ 12 \end{bmatrix}$ Of an orthogonal set ob vectors having spain spain spain that contain  $P_1$ ,  $P_2$ ,  $P_3$ ,  $P_4$ 

write c= [A:B] c = [12-3 q] system is consistant => p(n) = p(c) > row dependency in c' & A' must be some " 3R1+R2 = R3 on " = 3R1+R2 = R3 once : 3a+b=c F(pr) Put - By actulon form \* Eullity : millity = the dimension of the space of the in the Bosis of the space of the soln to Ax=B=(no. ob coloms - Rank ob A)= (no. ob Unknowns - Rank of A) A Nullite no of Coloms - Rank (PM) Dimension = nullity = n-r go consider set ob colomb vectors defined by X= {x, x, x, x, e R3 } such that x, +x+== 

(a)  $\begin{bmatrix} -6 \\ -8 \\ 3 \end{bmatrix}$ (b)  $\begin{bmatrix} -4 \\ 2 \\ 7 \end{bmatrix}$ (c)  $\begin{bmatrix} -3 \\ 2 \\ -2 \end{bmatrix}$ (d) none.

(e)  $\begin{bmatrix} -3 \\ 2 \\ -1 \end{bmatrix}$ (f)  $\begin{bmatrix} -3 \\ 2 \\ -2 \end{bmatrix}$ (g) The following vector is linearly dependent up on solt to Privious prob.

(a)  $\begin{bmatrix} -3 \\ 2 \\ 2 \end{bmatrix}$ (b)  $\begin{bmatrix} -1 \\ -7 \\ 30 \end{bmatrix}$ (c)  $\begin{bmatrix} -1 \\ 3 \end{bmatrix}$ (d) none.

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(a)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (b)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (c)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (d) none.

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(a)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (b)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (c)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (d) none.

(a)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (b)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (c)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (d)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (e)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (f)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (f)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (g)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (h)  $\begin{bmatrix} -2 \\ 3 \end{bmatrix}$ (h)

```
ts a basis or not?
                                                           Find Eigen Vector Ado.
   " Spans (5) = R3
      9, x, + a, x, + a, x, = R
             1 -2
         " R3 - 2R,
        : S' to not having mad and set of vector of R
      of call he bests
 Eigen values & Eigen value vactor
  let Anxa
    for any scalar 1. 3 x +0
  such that Ax = Ax
  Then I is Eigen value of Ann 1 x to is called
  Eigen vator corresponding to an Eigen value
  find Eigen values .
            Ax = Ax
       Ax - AIX = 0
     (A-AI) X=0 - Homog Soln
    Should posses han sow soln
   - A-XX = 0 - changelenistic segundian of A
    Adj (adj Ag) = |p| = A = |A| = n = p) n
  xly (1) to the given characteristic eet
   => - 1 - 1 + 214 4 45 = 0
       .. court torm = (A) = 45
Properties of eigen values .
(1) 1, + 12 + 12+ -- + 2n = an + ag2 + -- + an
    A. Az . Az . - . An = [A]
(3) IAI=0 if and only if attendations one of the eigen
    IAI to iff non of the eigenvalue is zeno
 ( The no of non sens eigen values = P(A) of madrice
    A and AT have the same to eigen value
@ The eigen values of any triangular matrix and
   diagonal matrix are its principle diagonal elements
(D) the eigenvalues of Real symmetrice / Hemition matrix
    are real no.
(8) the eigen values of stow synetric / show transition are
           or purly imaginary
(3) the eigen value of orthogonal / anitary are unit
               111=1
                          . A= 1, -1, -1, 1
    let the 1 be the eigen value of Annual
    (i) A" or is the eigen value of A"
```

Kd is the eigen value of

(m) 1+K

(5 - 11- - 8+KI

S= { (2,1,-2) (-2,-1,2) (4,2,-4) } of Ro

```
Sub X in (A-11) X = 0
     Solving equations : we get x = 0
offeneral characteristic equation of Anni-
     | Am AI | = (-1)" A" + (-1)" + ac(A) A" - -
   Constant term in characteristic ple polynomial of Americal
      36 A. Iz. As one Eigen values of AxxAs
      Then |Am - 11 = (-1)3(A)3 + (-0)2 (1,+2,+2) 22 + (-1)(1,3+2)34
                                        + 1, 1, 1, = 0
 (9.55 Constant term of chan polyl n. 11-0
                             : R2 28,
        f(0= +" + c, ++" + -- + c, + +c.
     convert into standard from X14 by (-1)"
       f(t) = (-1)" +" + (-1)" < , + +" + - - + (-1)" c
        .: const term of fill - (1) co = |A|
  8-1 16 2+2-212-45 =0 is a characteristic equation of
     coephicient natrice Aska in homogeneous system
       Ax =0. Then ady (add As)= 0
   (4) 450 (B) -4502
                    (A) 45 I
        # a. I + a. A + a. A2 + - + a. A"
Note: The eigen vector x corresponding to an eigen value of is some for the matrices the Mr. KA.
       A+KI and polynomial in A
Q. 26 let it be eigen value of 1
      [.c. (Ax = Ax) - 0
      x14 by 'A' on b.s
           A^2 x = A(Ax)
         In'x = Anx 1
     x The eigen vector's for the matrixes A and A" is
       same therefore the eigen vector's for A3 is same
 (11) let I be the eight value of non singular
      matrix A. | Alto them
     (i) I is the eigen value of A"
     (ii) IAI is the eigen value of (Adj A)
Note. The eigen vector & ob A, A', Adj A is same
     (Ax = Ax |- 0
     x14 by AT on bs. adja x - x x
       Tx = 1(A'x) (adi A)x = 1A1 x
     A" x = 1x 1 1
```

weget characteristic contin

```
And the eigen values of Ar (Hemition matrix) are
(9.17 The secon matrix is the inverse of first
                                                                    Real o hence of and R statement are true.
   matrix there for eigen value are 1, to this is
                                                               3.32: eigen value are real the matrix is a
( The eigen values of involutory matrix are (+ or - 1)
                                                                      Hemition matrix then were AT as = as
            it be sigen value n'
                                                                    a_{2i} = \overline{a}_{12} \sqrt{x} = 5 + -i
         A2=1 [ ]= ±1 ]
(8) the eigenvalues of idempoded matrix are 0,1
                                                               JIL WKT
                                                                       \lambda_1 + \lambda_1 + \lambda_3 = \alpha_0 + \alpha_{21} + \alpha_{33} =
           A^2 = A
                                                                   A A, A2 A3 = [A] = | a 1 0
        let ibe liger value of h.
        AA = An
                                        (A=0,1)
                    A (A-1) = 0
        A2 - A = 0
                                                                               = 4 (q2-1) -1(a) = q3-2q
                                                                     (A) A, A, A3 = a3 + (A)
 9-89 · P = P
                                                                    (B) A, A2 · A3 = 0. 9. 29 = 0 ≠(A)
        13 = 1
        13-1=0 1(1-1)=0 1(1+1)(1-1)=0
                                                                         A1 . A2 . A3 = ax -29 x 20 = -493 # 1A1
                                                                   LOD
                                                                         1, 12-13 = ax(a+5e)x(a-12)= a2-10-101
        CA=0,1,-1
     The determinent of skew syndyic matrices of odd order is seno there for 1=0
 (P-20 - Ans 0
                                                             G.E (AT= A=
                                                                      1, +1, +13 = tra(A) = 3 (Au 1)
                                                                       A. 12 A3 = 1A1 = 0
and Pal
                                                                 Since the rank of this matrix =1 and track=3
   = p-1 = 0
                                                                       there must be only one non sens eigen value =
  = 10 to 10 to = 20 to , 20 to
                                                                 = trackA) = 3 there for 1 = 0,0,3
 a er: Since Ar ari = real & ari = ari
                                                                     (m) /A-AI =
       ( there fore) M is Hammitian matrix
         and 'im' is skew Hemitton
   R. = R, + R, + R3
                                                                      let 2 4 2 are the
                                1 1 1
                                                                    WHT A_1 + A_2 = Tx(A) = 2+k > 0
                                                                                         >) K>-2
      A= 3,0.
                                                                                         => KE (-2, 40)
   and de s
      1, + 12+23 = +r(A)
                                                                          A1 . A2 = 1A1 = 2K-1 >0
       3+0+2 = 3
                                                                                      =) ドンガ
                                                                                        KE (4.00)
          [18=0]
                                                                    Since both condition to be satisfied
        WRT - \lambda_1 + \lambda_2 + \lambda_3 - - \lambda_n = \alpha_{ij} + \alpha_{k2} + - - + \alpha_{nn}
                                                                                KE (-2,00) N (12,00)
             =\frac{1}{1\cdot 2}+\frac{1}{2\cdot 3}+\frac{1}{3\cdot 4}+\cdots+\frac{1}{n(n+1)}
                                                                                 Ke (12,00) KE K>12
               1 - \frac{1}{3} + \frac{1}{2} - \frac{1}{3} + \frac{1}{3} - \frac{1}{4} + - \frac{1}{2} - \frac{1}{12} - \frac{1}{12}
                                                               $4.
                                                                       A 100 +1 = ?
                                                                                            AA = 1,-1,0
            = 1- 1
                                                                     let B= Alon +I
                                                                     Eigen value of B = 1100+1
Q.15 WKT lower triangular matrix
                                                                    $ 1 × =1 => - +1. -11 == 1 100 +1 = 2
              \lambda_1 \cdot \lambda_2 \cdot \lambda_3 - \dots \cdot \lambda_n = |A| \cdots (A = L)
                                                                    36 m=1 => -= (-1)00+1=2
                    = 1L1
                                                                                 - (0)(00+1=1
              = a, , a, a, -- a,
                                                                    Hence |B| = |A+I| = Productor ob evigen values of
                               = 1 \cdot \frac{1}{2} \cdot \frac{1}{3} \cdot \frac{1}{4} \cdot - - \frac{1}{n} = \frac{1}{n}
                                                                                            = 0.x 2 x 1 = 4
        Crisen (A-I) = 0 = (A-11)
           => [A, = 1]
                                                             Q:12 96 B = A-A. An = +3, 2,4
    WKT A, + 1 + 1 = 13
                                                                     find ( 18) ( Tr (A+B)=?
             ( de+ d3 = 12) - (1)
                                                                   The eigen values of is = 1/4 - 1/4
          A. da da = 32
  Sec 080, Thing = 31 0
                                       1. A2 + A2 + 12 = 12+8+42
                                                                  36 A3 > = (8)°-(3) = 6
             13=4)
```

181 = product of eigenvalues of . 18 = 6x2x2 = 24 (1) Tr (A+B) = Tr(A)+Tr(B)= (3+2-1) + (6+2+2) = 4+16=14 02.57 A=1 2 5 3 7 10 do 4 0000 112=2 These sust be decreas |A| = 100 + (A) = 14. 10-61=7 1,+2,+2,+2,+2+ += += (A) 16+2+9+24= 7+9+ B given 1+2+13+24=14 6+2+5+0=14 [9+b=9] A di- 12 /3- du= 1A1=100 / b=2 10 ab = 100 [ ab = 10] . 1a.b| = |5-2) = 3 Note: Do not apply elementry Transformation to find the eigen values A X = 3 X 2 1 1 1 0 0 0 1 0 0 0 1 verify each option in Ax " (B = x=[i] is satisfying Ax= 9x : x = [] to eigen vector corresponding to Imax = 3/ 134 WKT AX = AX AX = IX verifying with each option in Ax=1x .. (6) =  $x = x - \frac{4}{2}$  so diffes Ax = 1xin x = x [ ] is an eigen vector  $221 \leftarrow A_1 = 1 \Rightarrow x_1 \leftarrow \begin{bmatrix} 1 \\ -1 \end{bmatrix} \Rightarrow Ax_1 = A_1x_1$  $\begin{bmatrix} 1 & 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$  $\lambda_2 = \lambda_1 \Rightarrow \lambda_2 = \lambda_2 \times \lambda_2 = \lambda_2 \times \lambda_2$ =) [ ] [ 1 = 4. [ 2 ] - (5)

= (-1) - (-1) = 2

1- = 1 de

The no ob linearly independent Anxn = geometric multiplicity of Anxn = the dimension of the eigen space of Ann = No. of district eign values. A= (2) A= 2,2 Geometric xlicity of A: no ob distinct eigen values - Algebraic multiplicity of eigenvalue 2 : 12 times. the next linearly independent eigen vectors A 6 1 -> 1 = 3,3 Solve :-M= 2 . A. A. 3. T=(A) = 6 . A, + A2 } 1 = 3.4 . no. of Ind Eigen water vectors = no ob dotinct 'x'  $A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 2 & 1 \\ 0 & 0 & 1 \end{bmatrix} \Leftrightarrow \lambda_1 = 1$ ( +race(A)= 4 = 2,+22 \ |A| = 3 = 1, 12 remaining eigen values it given by : (c) = A = [3 2] Exactly satisfies both () ( 0)

Hence  $A = \begin{bmatrix} 3 & 2 \\ 1 & 2 \end{bmatrix}$  exactly satisfies both () &

Hence  $A = \begin{bmatrix} 3 & 2 \\ 1 & 2 \end{bmatrix}$ .

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 2 & 1 & 0 & 0 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

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\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 0 & 0 & 3 & 0 \end{pmatrix} \]

A=\[
\begin{pmatrix} 2 & 2 & 0 & 6 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2 & 1 & 0 & 0 \\ 2

Inner Product:  $x = [x_1, x_2, x_3]^{\top}$ ,  $y = [y_1, y_1, y_3]^{\top}$   $(x,y) = x^{\top}y = [x_1, x_2, x_3] \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} = x_1y_1 + x_2y_2 + 5y_3$   $(2) 4f_1(x,y) = 0 \Rightarrow x \neq y$ 

(a) 36 (x, y) =0 2 ||x|| = ||y|| = 1 Then xy one orthogon vectors.

Normalized vector of  $x = \frac{1}{\|x\|} = \int (x, x) = \int x^{T} x = \int x^{2} + x^{2} + x^{2} + x^{3}$ Normalized vector of  $x = \frac{x}{\|x\|} = \int \frac{1}{x_{1}^{2} + x_{2}^{2} + x_{3}^{2}} \left(\frac{x_{1}}{x_{2}}\right)$ 

Property De- The eigen vector of Real Symmetric matrix are orthogonal to each other [inner product of each paire is zero]  $X = [x, x_1, x_3]^T$   $y = [y, y_1, y_3]^T$  on the order or 3x3 corresponding to two distinct eigen values then x, y, + x24, + x372 =0 " X y are the eiger vectors of Real symmetric matrix . the inner product of x y = x y = xy +x\_1x+x\_2x=0 -1/2 0 1/2 1 x= 0 to an Eigen vector Then another Ergen vectorable -(a)  $\begin{bmatrix} 2 \\ 6 \\ 3 \end{bmatrix}$  (b)  $\begin{bmatrix} 1 \\ -1 \\ 6 \end{bmatrix}$  (c)  $\begin{bmatrix} 2 \\ 1 \\ 6 \end{bmatrix}$  (d)  $\begin{bmatrix} +1 \\ -2 \\ -3 \end{bmatrix}$ A - is symetric matrix was eigen we vectors are orthogonal do each other. Choosing an orthogonal vector to the given vector from the options we get  $x_0 = \begin{bmatrix} -1 \\ 0 \end{bmatrix}$ Cayley hemilton theom: - every square matrix satisfy its characteristic equation - we can suplace I by A in the characteristic equation of A. A-AI =0 A is replaced by n' | A-AT | =0 0 =0 Ex-18 A = -5 -3 A3-9 a) 124 + 121 b) 194 + 301 solm Pind the characteristic equation of Axxx | Aax - AI | = (-1) 2 x2 + (-1) (-5) x + 6 = 0 +xa(n) |n| = 1 + 5x + 6 =0 => x = -2,73 by C- H theorem (or.) d = -2, -3 suplace 'y' by 'h' (a) A3 = 15A + 12I A2+5A+6I=0 12 = 127 + 15 A2 = -5A -6 I A=-2 -> -8 #-90+12 xly by 'A' on bs. (B) - A3 = 19 A + 301 A3 = -5A2-6A 13 = 191 + 30 A3 = - 5 [-5A-61] - GA A=-2 => -8=-8L A3 = 194 4 361 A: -2 = -27 = -27 (3) It ligen values of Asx3 are 1,1,3 Then characteristic equation of matrix - A ? 3 A-1 Gadja Characteristic equation of Asxa [ Agxg - IA] = (-1)3 x3 + (-1)2 [1+1+3]x2 + (-1) [1+1+3+1+3]x + (1.1+3)=0 = -13 + 522 - 72+3=0 characteristic equation of (-A): replace it by -1 in above equation we got = -(1)3 + 5(-1)2 -7(-1)+2=0

Property (De- The eigen vector ob Real Stranetric of each paire is zero]  $X = \{x, x_1, x_3\}^T$   $y = \{y, y_1, y_3\}^T$  are the order 30 3x3 corresponding to two obtainet order 3x 3x3 corresponding to two or eigen values them x, y, + x2 y2 + x3 y3 =0 " X y are the eigen vectors of Real symmetric matrix ! the inner product of x, y = xT y = x,4,+x,4,+x,4,=0  $A = \begin{bmatrix} 3/2 & 0 & -1/2 \\ 0 & 1 & 0 \\ -1/2 & 0 & 1/2 \end{bmatrix}$  is an eigen vector b. Then another Eigen vectorofA=2 A - is symptoic matrix whos eigen to vectors as orthogonal to each either choosing an orthogonal vector to the given vector from the options we get  $x_0 = \begin{bmatrix} -1 \\ -1 \end{bmatrix}$ Cayley hemilton theorn: - every square matrix satisfy its characteristic equation -> we can replace I by A in the characteristic equation of A. A is replaced by A | A-AI = 5 A- AI =0 + A- AI) = 2 + 52 + 72 + 71 + 8 = 0 8tand form: adj A = IAI = replace i by IAI = = A MD replace 'i' by 'ax to @ we get (an-AI) = Teplace is by it in to we get | A-1 - AI) = Q -> Inverse of matrix:  $A^{-1} = \frac{AdJ A}{|A|}$  ,  $|A| \neq 0$ The A = ( to d) Then  $A^{-1} = \frac{1}{ad-bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}$ Qo find inverse ob  $A = \begin{bmatrix} 1+2i & 2 \\ 1 & 1-2i \end{bmatrix}$  $A^{-1} = \frac{1}{(1^2 + 1^2)^2 - 2} \begin{bmatrix} 1 - 2 & -2 \\ -1 & 1 + 2i \end{bmatrix}$  $A^{-1} = \frac{1}{3} \left[ \begin{array}{c} n \\ \end{array} \right]$ 

adjoint 
$$A = (cofector neatrix)^T$$

$$= [(-1)^{c+3} 8_{t3}]^T$$

$$A = [a_{ij}]_{3x3} , a_{ij} = i^2 - j^2 + ij$$

$$A^{-1} = 0$$

$$A = [a_{ij}]_{3x3} = \begin{bmatrix} 0 & -3 & -2 \\ 3 & 0 & -5 \\ 8 & 5 & 0 \end{bmatrix}$$

$$a_{11} = i^2 - i^2 = 0$$

$$a_{12} = i^2 - 2^2 = 43$$

$$a_{13} = i^2 - 3^2 = -8$$

$$a_{13} = 4 - 3 = -5$$

$$A^{-1} B^{-1}, c^{-1}, D^{-1}, E^{-1} \text{ exists}$$
Given that  $A = B, c, D, E \text{ are non singular}$ 

$$A^{-1}, B^{-1}, c^{-1}, D^{-1}, E^{-1} \text{ exists}$$
Given  $DABEC = I$ 

$$B^{-1} = 0$$

$$A = (a_{1j})_{3x3} , a_{1j} = i^2 - 2^3 + ij$$

$$a_{1j} = i^2 - 2^3 - 2^3$$

$$a_{1j} = i^2 - 2^3$$

$$a_{1j} =$$

Pre Xly by E and post xy by A on b.s.

B' = ECDA Ans.

E-1 3 A-1 = CD