

HW #2
CSc 137, Harvey
Total (16 pts)

1.6 What is the biggest positive FP number (in Decimal) that can be represented in 16-bit format using 1-bit sign, 4-bit biased exponent, and 11-bit fraction, where bias offset is 7? (4 pts)

$$\rightarrow 0111\ 0111\ 1111\ 1111$$

$$= \underbrace{0}_{\text{sign}} \underbrace{1111\ 0}_{\text{exp}} \underbrace{1111\ 1111\ 1111}_{\text{mantissa}}$$

step 2: $\text{exp bit} = 14 + \text{offset}$

$$= 14 - 7$$

$$= 7$$

step 3: mantissa $\rightarrow 1.\underbrace{11111111111}_{11 \text{ bits}} \times 2^7$

step 4:

$$= 1111111.1111$$

$$= 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 + 2^{-1} + 2^{-2} + 2^{-3}$$

$$= 128 + 64 + 32 + 16 + 8 + 4 + 2 + 1 + \frac{1}{2} + \frac{1}{4} + \frac{1}{8}$$

$$= 255.875$$

1.8 Do the following assuming 16-bit FP numbers with 4-bit bias exponent, bias offset = 7, and 11-bit fraction: (4 pts)

- a) What real number does an FP number with sign=0, bias exponent=1 and fraction=0 represent? (Answer in 4 decimal places)

$$\text{exponent} = \text{biased_exponent} - \text{bias}$$

$$\text{biased_exponent} = \text{exponent} + \text{bias}$$

$$\text{exponent} = 1 - 7$$

$$= -6$$

④ fraction = 0

⑤ Combine

$$1.0 \times 2^{-6}$$

$$= (0.000001)_2$$

$$= 2^{-6}$$

$$= 0.015625$$

$$= 0.0156$$

2.4 Proof Demorgan's Theorem $\overline{x+y} = \bar{x}\bar{y}$ by creating truth tables for $f = \overline{x+y}$ and $g = \bar{x}\bar{y}$. Are the two truth tables identical? (4 pts)

x	y	\bar{x}	\bar{y}	$x+y$	$\overline{x+y}$	$\bar{x}\bar{y}$
0	0	1	1	0	1	1
1	0	0	1	1	0	0
0	1	1	0	1	0	0
1	1	0	0	1	0	0

f
g

2.5 (4 pts) Draw the circuit schematic for $f = x\bar{y} + yz$ and then convert the schematic to NAND gates using the steps illustrated in the textbook.

