

Lecture #22

Cache Part I: Direct Mapped Cache





Questions?

Ask at

https://sets.netlify.app/module/676ca3a07d7f5ffc1741dc65

OR

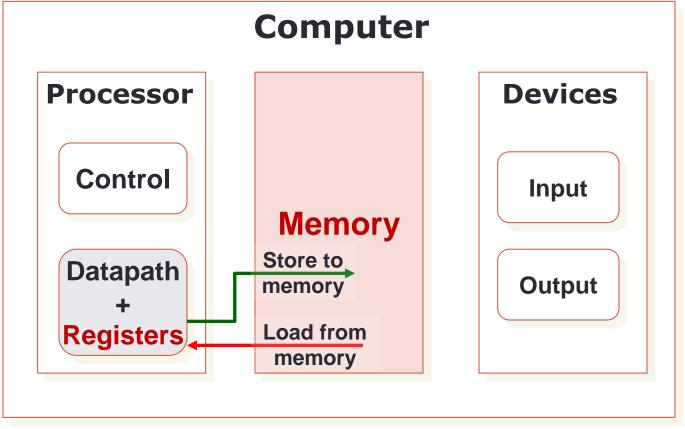
Scan and ask your questions here! (May be obscured in some slides)



Lecture #22: Cache I: Direct Mapped Cache

- 1. Introduction
- 2. Cache
 - 2.1 Locality
 - 2.2 Memory Access Time
- 3. Memory to Cache Mapping
- 4. Direct Mapping
- 5. Reading Data (Memory Load)
- 6. Types of Cache Misses
- 7. Writing Data (Memory Store)
- 8. Write Policy

1. Data Transfer: The Big Picture



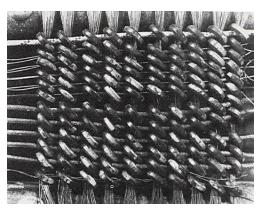
Registers are in the datapath of the processor. If operands are in memory we have to **load** them to processor (registers), operate on them, and **store** them back to memory.



1. Memory Technology: 1950s



1948: Maurice Wilkes examining EDSAC's delay line memory tubes 16-tubes each storing 32 17-bit words







Maurice Wilkes: 2005

1952: IBM 2361 16KB magnetic core memory



1. Memory Technology Today: **DRAM**

DDR SDRAM

- Double Data Rate
 - Synchronous Dynamic RAM



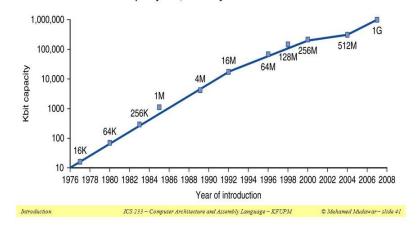
- Delivers memory on the positive and negative edge of a clock (double rate)
- Generations:
 - DDR (MemClkFreq x 2(double rate) x 8 words)
 - DDR2 (MemClkFreq x 2(multiplier) x 2 x 8 words)
 - DDR3 (MemClkFreq x 4(multiplier) x 2 x 8 words)
 - DDR4 (released in 2014)
 - DDR5 (in Q3 2021)



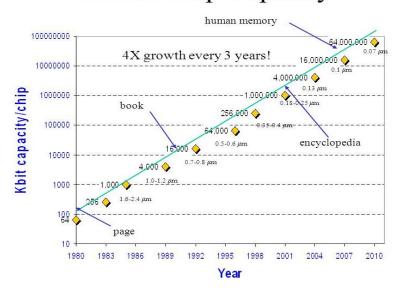
1. DRAM Capacity Growth

Growth of Capacity per DRAM Chip

DRAM capacity quadrupled almost every 3 years
 60% increase per year, for 20 years



DRAM Chip Capacity



Unprecedented growth in density, but we still have a problem

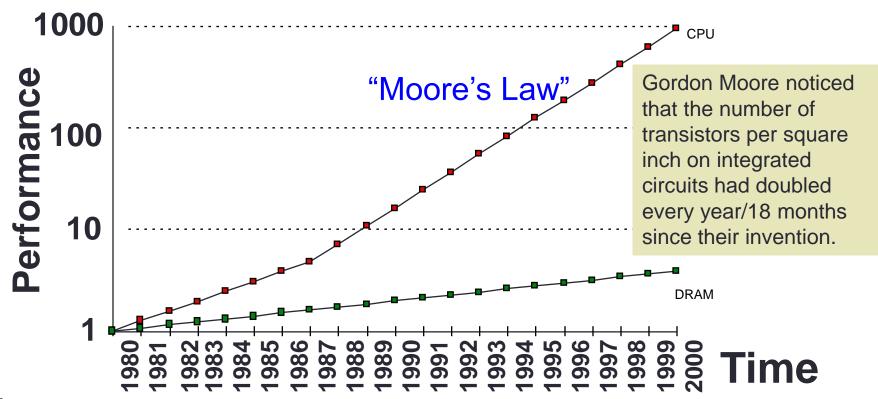


1. Processor-DRAM Performance Gap

Memory Wall:

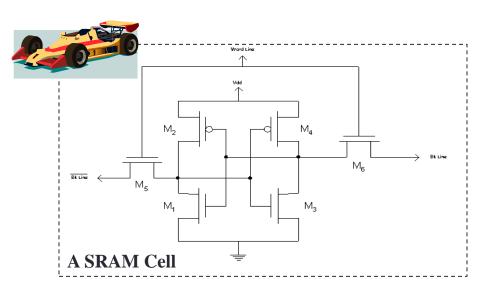
1GHz Processor → 1 ns per clock cycle

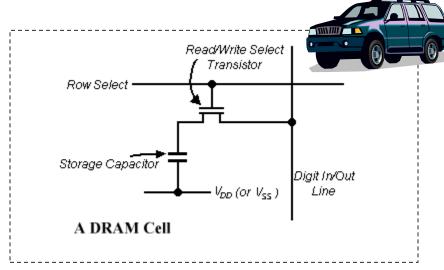
50ns for DRAM access → 50 processor clock cycles per memory access!





1. Faster Memory Technology: SRAM





SRAM

6 transistors per memory cell

→ Low density

Fast access latency of 0.5 - 5 ns More costly

Uses flip-flops

DRAM

1 transistor per memory cell

→ High density

Slow access latency of 50-70ns

Less costly

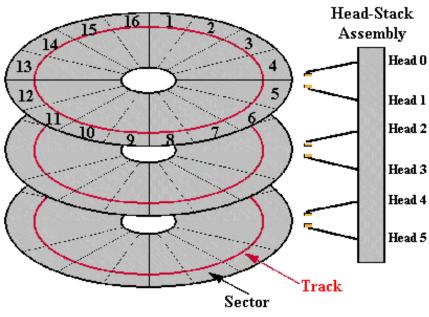
Used in main memory



1. Slow Memory Technology: Magnetic Disk







Typical high-end hard disk:

Average Latency: 4 - 10 ms

Capacity: 500-2000GB



1. Quality vs Quantity

Processor

Control

Datapath Registers

Memory (DRAM)

Devices

Input

Output

(Harddisk)







	Capacity	Latency	Cost/GB
Register	100s Bytes	20 ps	\$\$\$\$
SRAM	100s KB	0.5-5 ns	\$\$\$
DRAM	100s MB	50-70 ns	\$
Hard Disk	100s GB	5-20 ms	Cents
Ideal	1 GB	1 ns	Cheap



1. Best of Both Worlds

- What we want:
 - A BIG and FAST memory
 - Memory system should perform like 1GB of SRAM (1ns access time) but cost like 1GB of slow memory

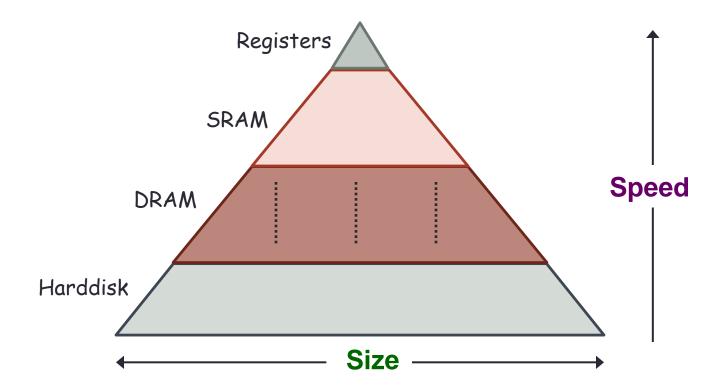
Key concept:

Use a hierarchy of memory technologies:

- Small but fast memory near CPU
- Large but slow memory farther away from CPU



1. Memory Hierarchy





2. Cache: The Library Analogy





Imagine you are forced to put back a book to its bookshelf before taking another book......



2. Solution: Book on the Desk!



What if you are allowed to take the books that are **likely to be needed soon** with you and place them nearby on the desk?

2. Cache: The Basic Idea

- Keep the frequently and recently used data in smaller but faster memory
- Refer to bigger and slower memory:
 - Only when you cannot find data/instruction in the faster memory
- Why does it work?

Principle of Locality

Program accesses only a small portion of the memory address space within a small time interval



2.1 Cache: Types of Locality

Temporal locality

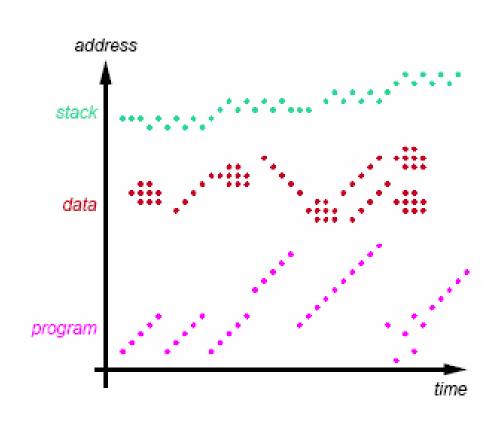
 If an item is referenced, it will tend to be referenced again soon

Spatial locality

 If an item is referenced, nearby items will tend to be referenced soon

Different locality for

- Instructions
- Data

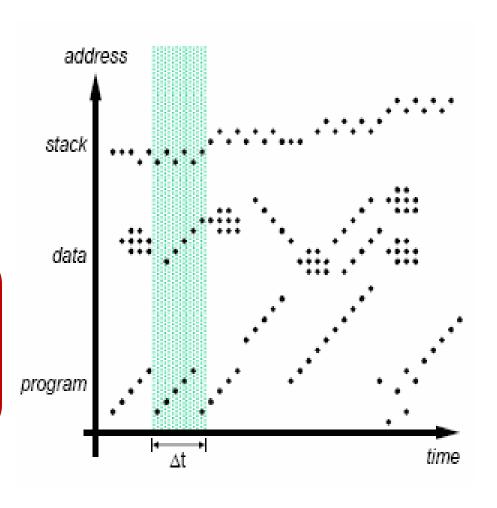




2.1 Working Set: Definition

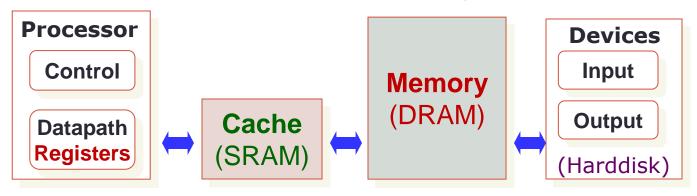
- Set of locations accessed during ∆t
- Different phases of execution may use different working sets

Our aim is to capture the working set and keep it in the memory closest to CPU





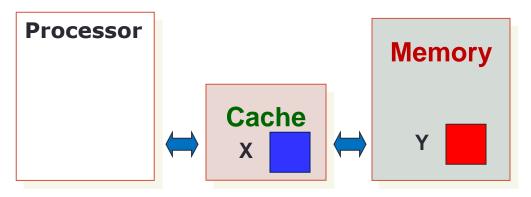
2.2 Two Aspects of Memory Access



- How to make SLOW main memory appear faster?
 - Cache a small but fast SRAM near CPU
 - Hardware managed: Transparent to programmer
- How to make SMALL main memory appear bigger than it is?
 - Virtual memory
 - OS managed: Transparent to programmer
 - Not in the scope of this module (covered in CS2106)



2.2 Memory Access Time: Terminology



- Hit: Data is in cache (e.g., X)
 - Hit rate: Fraction of memory accesses that hit
 - Hit time: Time to access cache
- Miss: Data is not in cache (e.g., Y)
 - Miss rate = 1 Hit rate
 - Miss penalty: Time to replace cache block + hit time
- Hit time < Miss penalty</p>



2.2 Memory Access Time: Formula

Average Access Time

= Hit rate x Hit Time + (1-Hit rate) x Miss penalty

Example:

Suppose our on-chip SRAM (cache) has 0.8 ns access time, but the fastest DRAM (main memory) we can get has an access time of 10ns. How high a hit rate do we need to sustain an average access time of 1ns?

> Let h be the desired hit rate. $1 = 0.8h + (1 - h) \times (10 + 0.8)$ = 0.8h + 10.8 - 10.8h $10h = 9.8 \rightarrow h = 0.98$ Hence we need a hit rate of **98%**.



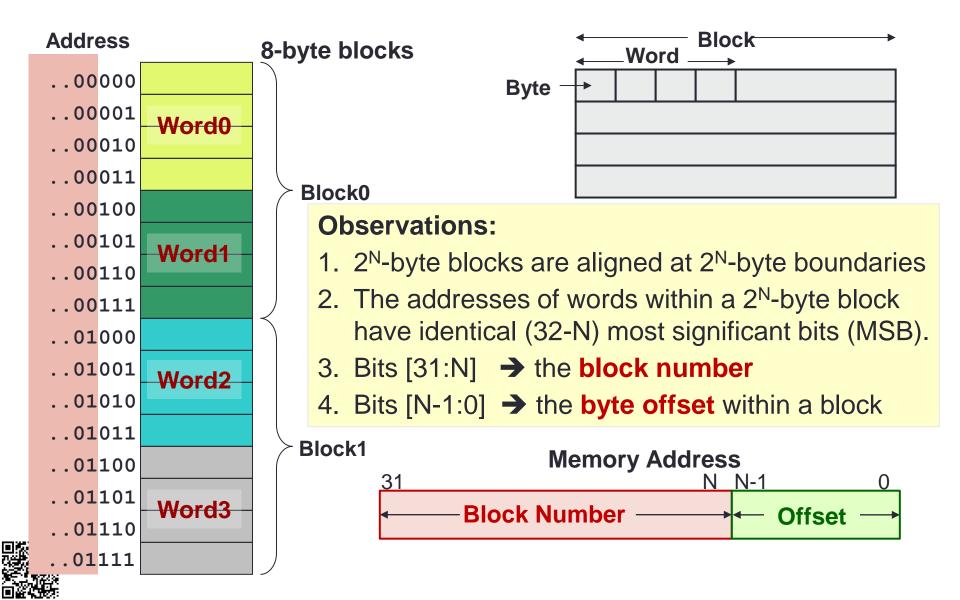
3. Memory to Cache Mapping (1/2)

- Cache Block/Line:
 - Unit of transfer between memory and cache
- Block size is typically one or more words
 - e.g.: 16-byte block

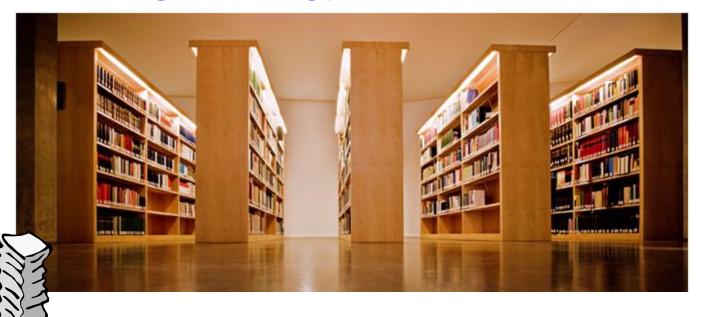
 4-word block
 - 32-byte block ≅ 8-word block
- Why is the block size bigger than word size?

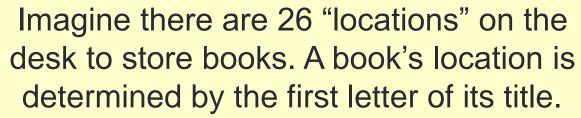


3. Memory to Cache Mapping (2/2)



4. Direct Mapping Analogy

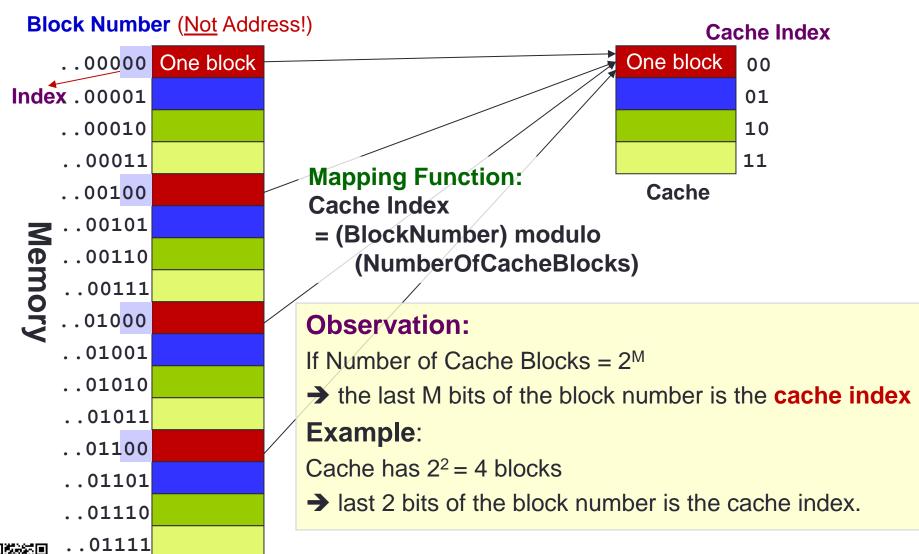




→ Each book has exactly one location.

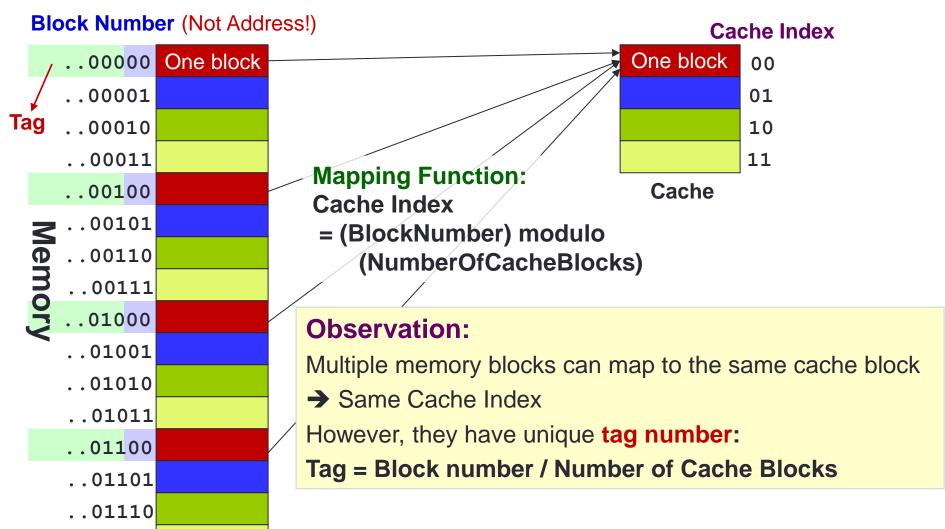


4. Direct Mapped Cache: Cache Index



..01111

4. Direct Mapped Cache: Cache Tag



4. Direct Mapped Cache: Mapping

Memory Address



Cache Block size = 2^N bytes

Memory Address



Cache Block size = 2^N bytes

Number of cache blocks = 2^{M}

Offset = N bits

Index = M bits

Tag = 32 - (N + M) bits



4. Direct Mapped Cache: Cache Structure

Cache

Valid Tag Data Index

00
01
10
11

Along with a data block (line), cache also contains the following administrative information (overheads):

- 1. Tag of the memory block
- 2. Valid bit indicating whether the cache line contains valid data

When is there a cache hit?

```
( Valid[index] = TRUE ) AND
( Tag[ index ] = Tag[ memory address ] )
```



4. Cache Mapping: Example

Memory 4GB

1 Block = 16 bytes

Cache
16KB

1 Block
= 16 bytes

Memory Address



Offset, N = 4 bits

Block Number = 32 - 4 = 28 **bits**

Check: Number of Blocks = 2^{28}



Number of Cache Blocks

 $= 16KB / 16bytes = 1024 = 2^{10}$

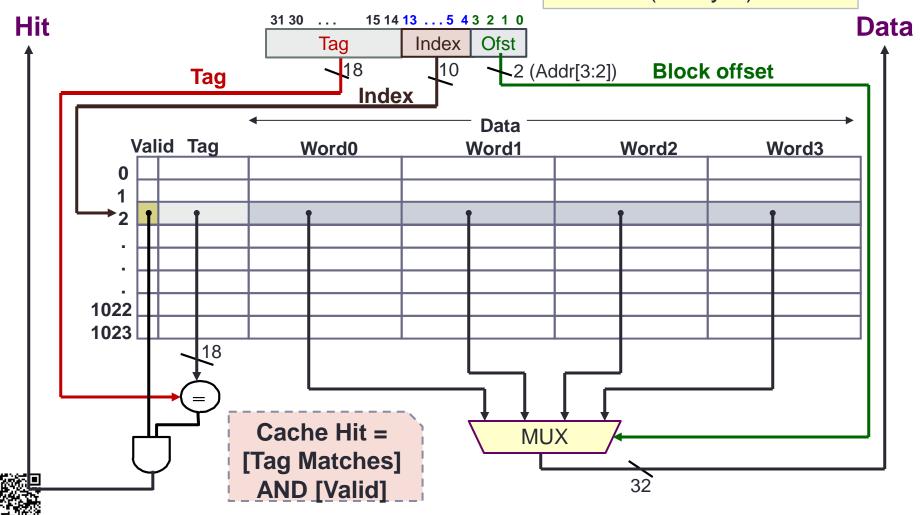
Cache Index, M = 10bits

Cache Tag = 32 - 10 - 4 = 18 bits



4. Cache Circuitry: Example

16-KB cache:4-word (16-byte) blocks



5. Reading Data: Setup

- Given a direct mapped 16KB cache:
 - 16-byte blocks x 1024 cache blocks
- Trace the following memory accesses:

Tag	Index	Offset
31 14	13 4	3 0
000000000000000000000000000000000000000	0000000001	0100
000000000000000000000000000000000000000	000000001	1100
000000000000000000000000000000000000000	000000011	0100
000000000000000000000000000000000000000	000000001	1000
000000000000000000000000000000000000000	000000001	0000



5. Reading Data: Initial State

- Intially cache is empty
 - → All *valid* bits are zeroes (false)

			•	Data				
			Word0	Word1	Word2	Word3		
Index '	Valid	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15		
0	0							
1	0							
2	0							
3	0							
4	0							
5	0							
1022	0							
1023	0							
	\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \							



Tag Index Offset

Load from

0000000000000000 000000001 0100

Step 1. Check Cache Block at index 1

			√ Word0	Data Word1	Word2	Word3	
Index V	/alid	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15	
0	0						
(1)	0						
2	0						
3	0						
4	0						
5	0						
1022	0						
1023	0						

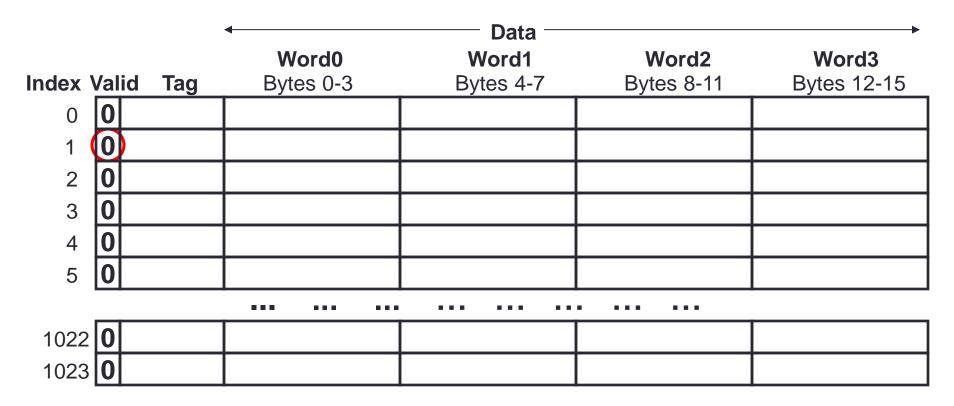


Tag Index Offset

Load from

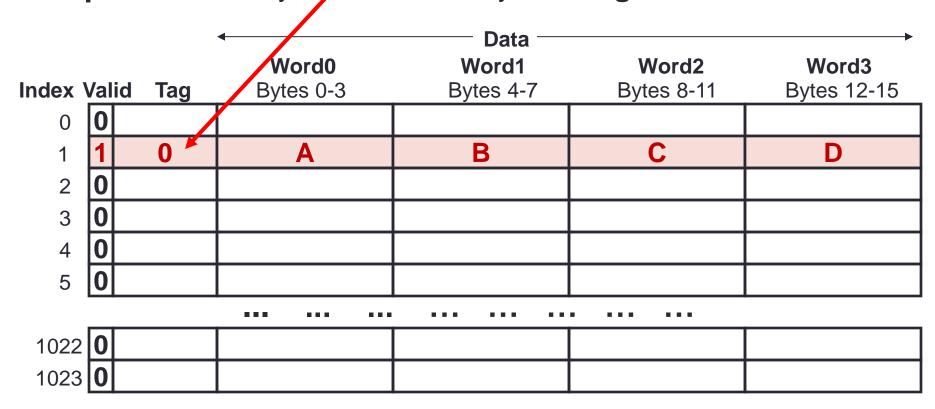
0000000000000000 000000001 0100

Step 2. Data in block 1 is invalid [Cold/Compulsory Miss]





Step 3. Load 16 bytes from memory; Set Tag and Valid bit





Step 4. Return **Word1** (byte offset = 4) to Register

			∀ Word0	Data Word1	Word2	→ Word3	
Index	Valid	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15	
0	0						
1	1	0	Α	В	С	D	
2	0						
3	0						
4	0						
5	0						
1022	0						
1023	0						



Tag

Index

Offset

Load from

000000001

1100

Step 1. Check Cache Block at index 1

Index \	/alid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0	0					
1	1	0	Α	В	С	D
2	0					
3	0					
4	0					
5	0					
1022	0					
1023	0					



Tag Index Offset

Load from

00000000000000000 000000001 1100

Step 2. [Cache Block is Valid] AND [Tags match] → Cache hit!

	▼ Word0	Data Word1	Word2	Word3
Index Valid Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15
0 0				
1 1 0	Α	В	С	D
2 0				
3 0				
4 0				
5 0				
1022 0				
1023 0				



Tag Index Offset

Load from

Step 3. Return **Word3** (byte offset = 12) to Register [Spatial Locality]

Index \	/alid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0		Tag	Dytes 6 5	Dytes + 1	Dytes o 11	Dytes 12 10
1	1	0	Α	В	С	D
2	0					
3	0					
4	0					
5	0					
1022	0					
1023	0					



Tag Index Offset

Load from

0000000000000000 000000011 0100

Step 1. Check Cache Block at index 3

			•	Data		•
			Word0	Word1	Word2	Word3
Index	<u>Valid</u>	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15
0	0					
1	1	0	Α	В	С	D
2	0					
3	0					
4	0					
5	0					
1022	0					
1023	0					



Tag

Index

Offset

Load from

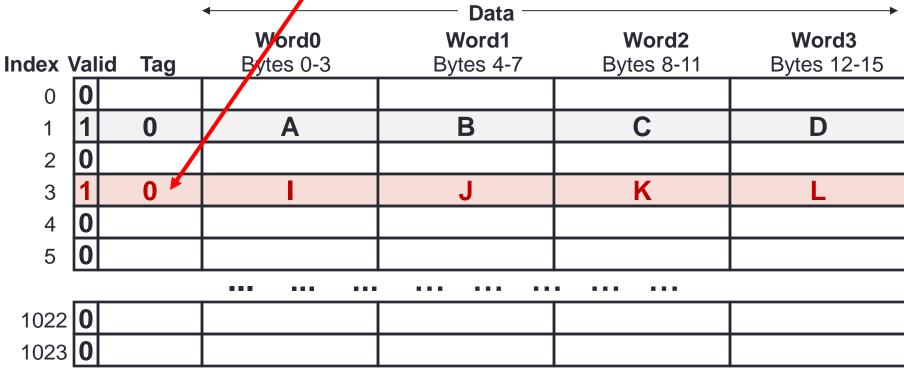
000000011

0100

Step 2. Data in block 3 is invalid [Cold/Compulsory Miss]

Index '	Valid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0	0		j	,	,	
1	1	0	Α	В	С	D
2	0					
3	0					
4	0					
5	0					
1022	0					
1023	0					_







Load from

5. Reading Data: Load #3-4

 Tag
 Index
 Offset

 0000000000000000000
 0000000011
 0100

Step 4. Return **Word1** (byte offset = 4) to Register

		◆	Data		———
		Word0	Word1	Word2	Word3
Index Val	id Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15
0 0					
1 1	0	Α	В	С	D
2 0					
3 1	0	I	J	K	L
4 0					
5 0					
1022 0					
1023 0					



Tag

Index

Offset

Load from

00000000000000010

000000001

1000

Step 1. Check Cache Block at index 1

Index \	Valid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0	0		,	,	,	
1	1	0	Α	В	С	D
2	0					
3	1	0		J	K	L
4	0					
5	0					
1022	0					
1023	0					

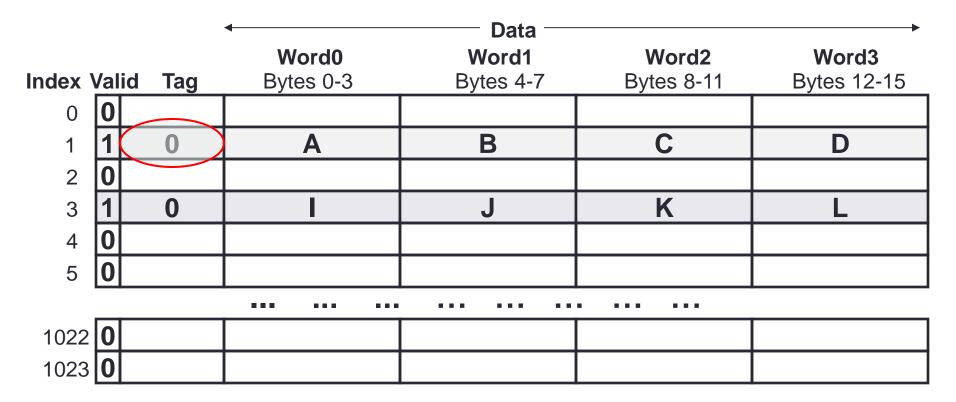


Tag Index Offset

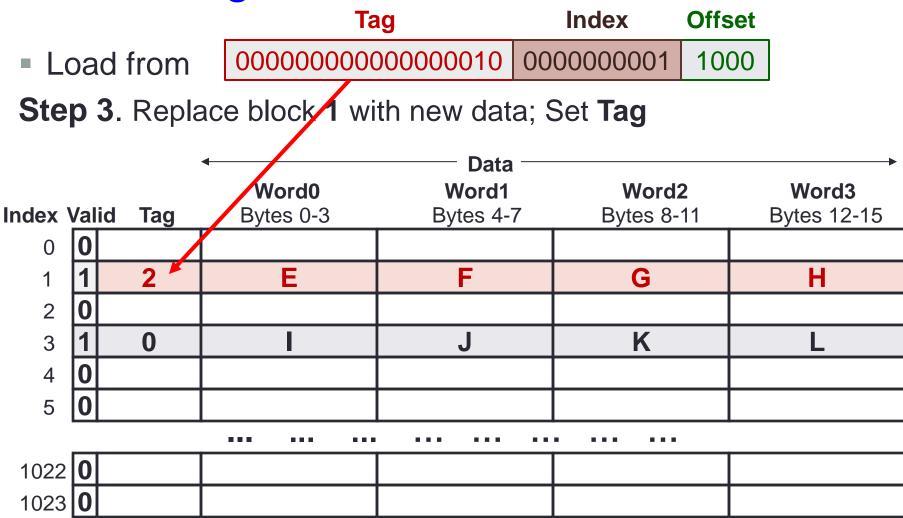
Load from

0000000000000001 000000001 1000

Step 2. Cache block is Valid but Tags mismatch [Cold miss]









Tag Index Offset

Load from

0000000000000001 000000001 1000

Step 4. Return **Word2** (byte offset = 8) to Register

			▼ Word0	Data Word1	Word2	→ Word3
Index	<u>Valid</u>	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15
0	0					
1	1	2	E	F	G	Н
2	0					
3	1	0	I	J	K	L
4	0					
5	0					
1022	0					
1023	0					



Tag

Index

Offset

Load from

000000001

0000

Step 1. Check Cache Block at index 1

Inday \		Toa	Word0	Word1	Word2	Word3
Index \	Vallu	Tag	Bytes 0-3	Bytes 4-7	Bytes 8-11	Bytes 12-15
0	0					
1	1	2	E	F	G	Н
2	0					
3	1	0	I	J	K	L
4	0					
5	0					
		-				
1022	0					
1023	0					



Tag Index Offset

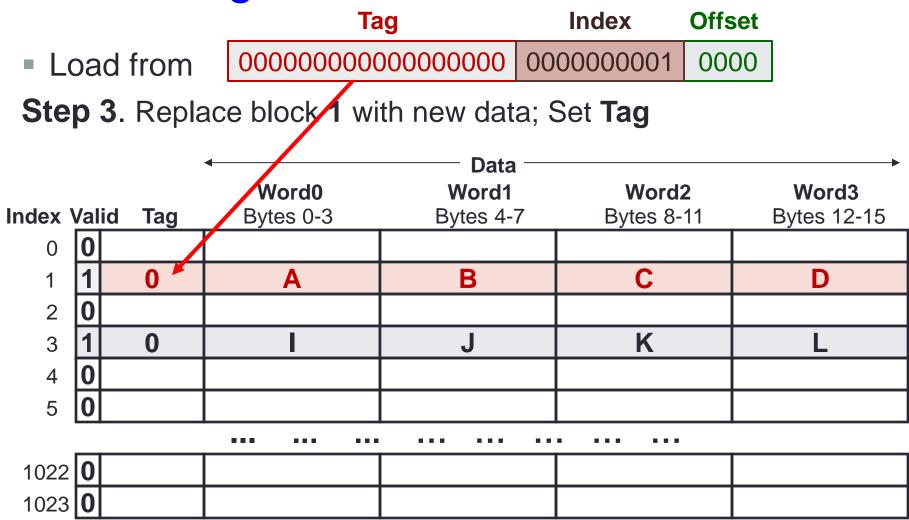
Load from

00000000000000000 000000001 0000

Step 2. Cache block is Valid but Tags mismatch [Cold miss]

Index Valid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0 0		j	j	j	
1 1	2	E	F	G	Н
2 0					
3 1	0		J	K	L
4 0					
5 0					
1022 0					
1023 0					







 Tag
 Index
 Offset

 000000000000000000
 0000000001
 0000

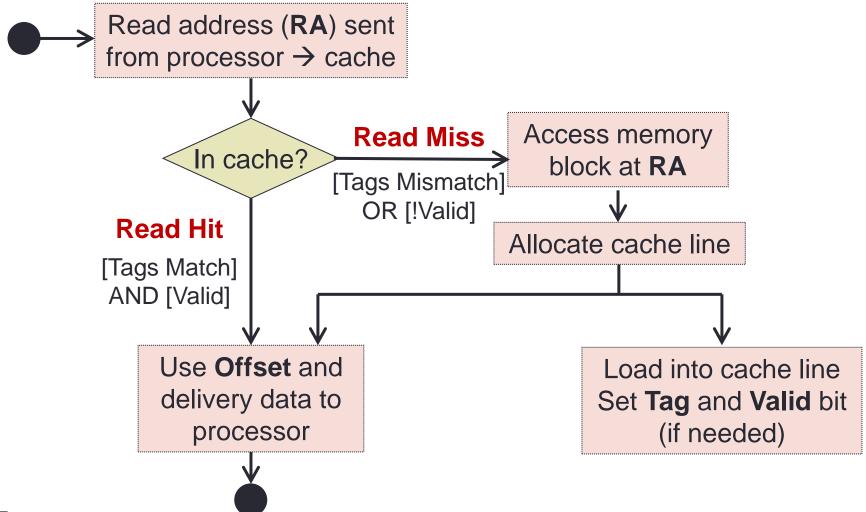
Load from

Step 4. Return **Word0** (byte offset = 0) to Register

Index '	Valid	Tag	Word0 Bytes 0-3	Data Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15
0	0					
1	1	0	A	В	С	D
2	0					
3	1	0		J	K	L
4	0					
5	0					
1022	0					
1023	0					



5. Reading Data: Summary





6. Types of Cache Misses

Compulsory misses

- On the first access to a block; the block must be brought into the cache
- Also called cold start misses or first reference misses

Conflict misses

- Occur in the case of direct mapped cache or set associative cache, when several blocks are mapped to the same block/set
- Also called collision misses or interference misses

Capacity misses

 Occur when blocks are discarded from cache as cache cannot contain all blocks needed



Exercise #1: Setup Information

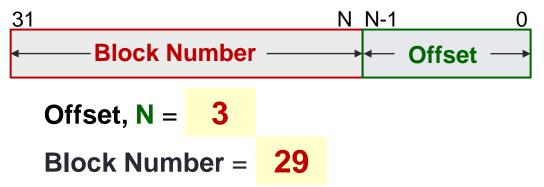
Memory 4GB

1 Block = 8 bytes

Cache 32Bytes

1 Block = 8 bytes

Memory Address





Number of Cache Blocks = 4

Cache Index, M = 2

Cache Tag = 27



Exercise #2: Tracing Memory Accesses

- Using the given setup in exercise #1, trace the following memory loads:
 - Load from addresses:

4, 0, 8, 12, 36, 0, 4

- Note that "A", "B".... "J" represent word-size data
 - Assume 1 word = 4 bytes

Memory Content

Addr	Data
0	A
4	В
8	С
12	D
	•••
32	-
36	J
	•••



56

Exercise #2: Load #1

Addresses: 4,0,8,12,36,0,4

Addr.	Data
0	Α
4	В
8	С
12	D
32	I
36	J

Tag

Index Offset

Address 4 =

00

Index	Valid	Tag	Word0	Word1
0	0 1	0	Α	В
1	0			
2	0			
3	0			

Miss Hit

Addresses: 4,(0) 8, 12, 36, 0, 4

Addr.	Data
0	Α
4	В
8	С
12	D
32	I
36	J

Tag

Index Offset

Address 0 =

00

Index	Valid	Tag	Word0	Word1
0	1	0	A	В
1	0			
2	0			
3	0			

Miss Hit Miss

Addresses: 4, 0,(8) 12, 36, 0, 4

Addr.	Data
0	Α
4	В
8	С
12	D
32	I
36	J

Tag

Index Offset

Index	Valid	Tag	Word0	Word1
0	1	0	A	В
1	0 1	0	(U)	D
2	0			
3	0			



Miss Hit Miss Hit

Addresses: 4, 0, 8, (12), 36, 0, 4

Addr. Data 0 Α 4 B 8 C 12 D 32 36 J

Tag

Index Offset

Index	Valid	Tag	Word0	Word1
0	1	0	Α	В
1	1	0	С	D
2	0			
3	0			



Miss Hit Miss Hit

Addresses: 4, 0, 8, 12, 36, 0, 4

Addr. Data 0 Α 4 B 8 C 12 D 32 36 J

Tag

Index Offset

Index	Valid	Tag	Word0	Word1
0	1	Ø ₁	×Ι	B (J)
1	1	0	С	D
2	0			
3	0			



Data

Α

B

C

D

J

Addr.

0

4

8

12

32

36

Exercise #2: Load #6

Miss Hit Miss Hit Miss Miss

Addresses: 4, 0, 8, 12, 36, 0,

Tag

Index Offset

Address 0 =

00

Index	Valid	Tag	Word0	Word1
0	1	810	XXA	BYB
1	1	0	С	D
2	0			
3	0			



Data

Α

B

C

D

J

Addr.

0

4

8

12

32

36

Exercise #2: Load #7

Miss Hit Miss Hit Miss Miss Hit

Addresses: 4, 0, 8, 12, 36, 0, 4

Tag

Index Offset

Address 4 =

Index	Valid	Tag	Word0	Word1
0	1	810	XXA	B/B)
1	1	0	С	D
2	0			
3	0			



7. Writing Data: Store #1-1

Tag Index Offset

Store X to 0000000000000000 000000001 1000

Step 1. Check Cache Block 1

			◆ Data →					
Index	Valid	Tag	Word0 Bytes 0-3	Word1 Bytes 4-7	Word2 Bytes 8-11	Word3 Bytes 12-15		
macx		rag	Dytes 0 0	Dytes + 1	Dytes 6 11	Dyte3 12 10		
0	0							
1	1	0	Α	В	С	D		
2	0							
3	1	0		J	K	L		
4	0							
5	0							
1022	0							
1023	0							

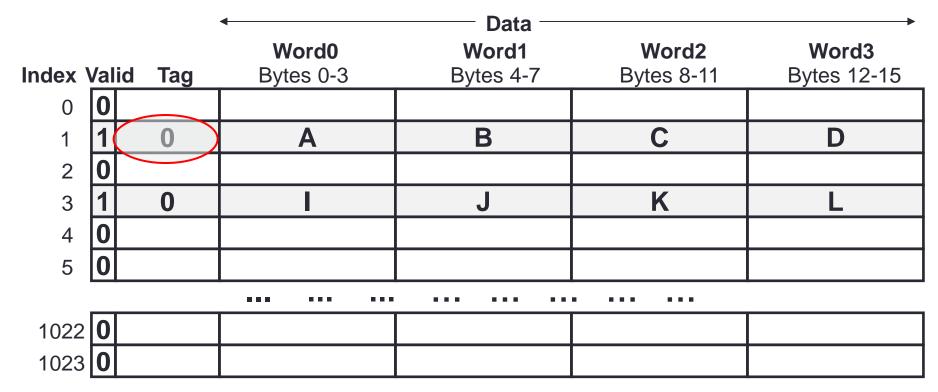


7. Writing Data: Store #1-2

Tag Index Offset

Store X to 0000000000000000 000000001 1000

Step 2. [Cache Block is Valid] AND [Tags match] → Cache hit!





7. Writing Data: Store #1-3

Step 2. Replace Word2 (offset = 8) with **X**

Index Valid Tag			◆ Data —		See any problem here?		
		Tag	Word0 Bytes 0-3			Word3 Bytes 12-15	
0	0						
1	1	0	Α	В	X	D	
2	0						
3	1	0	I	J	K	L	
4	0						
5	0						
1022	0						
1023	0						

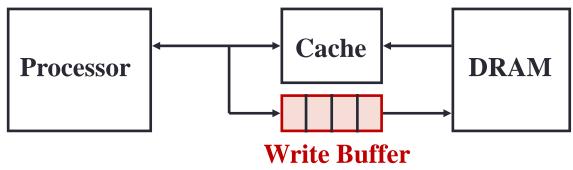


8. Changing Cache Content: Write Policy

- Cache and main memory are inconsistent
 - Modified data only in cache, not in memory!
- Solution 1: Write-through cache
 - Write data both to cache and to main memory
- Solution 2: Write-back cache
 - Only write to cache
 - Write to main memory only when cache block is replaced (evicted)



8. Write-Through Cache



Problem:

Write will operate at the speed of main memory!

Solution:

- Put a write buffer between cache and main memory
 - Processor: writes data to cache + write buffer
 - Memory controller: write contents of the buffer to memory



8. Write-Back Cache

Problem:

Quite wasteful if we write back every evicted cache blocks

Solution:

- Add an additional bit (Dirty bit) to each cache block
- Write operation will change dirty bit to 1
 - Only cache block is updated, no write to memory
- When a cache block is replaced:
 - Only write back to memory if dirty bit is 1

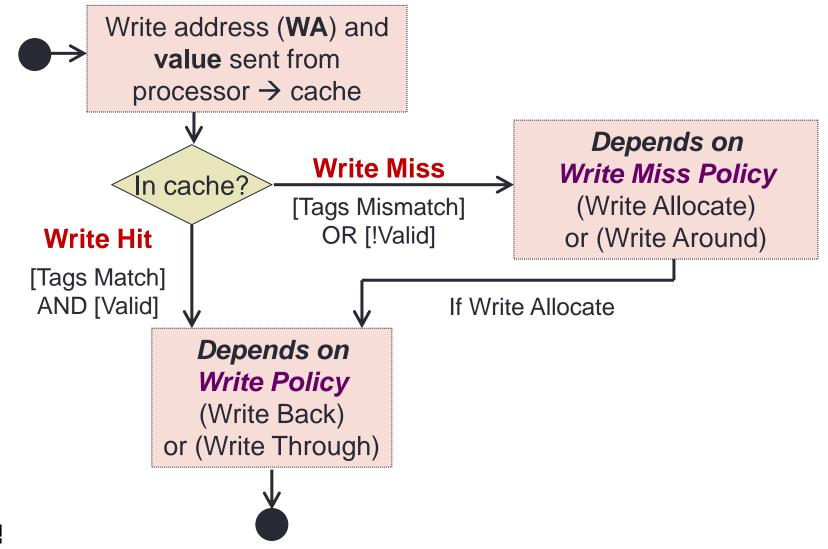


8. Handling Cache Misses

- On a Read Miss:
 - Data loaded into cache and then load from there to register
- Write Miss option 1: Write allocate
 - Load the complete block into cache
 - Change only the required word in cache
 - Write to main memory depends on write policy
- Write Miss option 2: Write around
 - Do not load the block to cache
 - Write directly to main memory only



8. Writing Data: Summary





Summary

 Memory hierarchy gives the illusion of a fast and big memory

- Hardware-managed cache is an integral component of today's processors
- Next lecture: How to improve cache performance



Reading

- Large and Fast: Exploiting Memory Hierarchy
 - Chapter 7 sections 7.1 7.2 (3rd edition)
 - Chapter 5 sections 5.1 5.2 (4th edition)





End of File













