

#### Lecture #16

# Quine-McCluskey





# Questions?

Ask at

https://sets.netlify.app/module/676ca3a07d7f5ffc1741dc65

#### OR

Scan and ask your questions here! (May be obscured in some slides)



# Lecture #16: Quine-McCluskey

This topic is only for your own reading only.

- A tabulation method similar in concept to K-map
- Applicable for functions with any number of variables
  - K-maps are useful for functions with at most 5 or 6 variables
- Tedious on paper, but can be automated (programmed)
- Non-examinable
  - But knowing it may enhance your understanding of K-maps

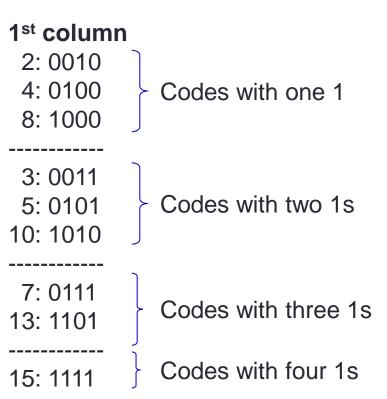


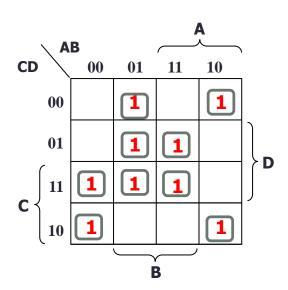
#### Pls and EPls

- To find the simplest SOP expression from a K-map, you need to obtain:
  - Minimum number of literals per product term; and
  - Minimum number of product terms.
- Achieved through K-map using
  - Biggest groupings of minterms (prime implicants) where possible; and
  - No redundant groupings (look for essential prime implicants)



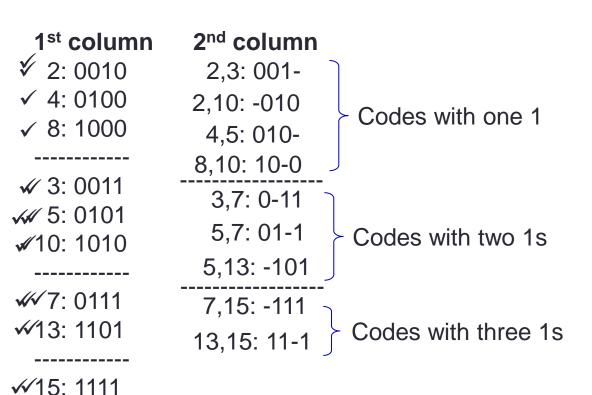
Step 1: List out all minterms in groups with same number of 1s in their binary codes.

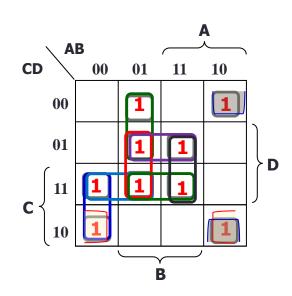






Step 2: Combine codes that differ by 1 bit into bigger group, write the combined code in next column.







Step 3: Repeat step 2 – Combine codes that differ by 1 bit into bigger group, write the combined code in next column.

#### 1<sup>st</sup> column

√ 2: 0010

√ 4: 0100

√ 8: 1000

√ 3: 0011

√ 5: 0101

**√**10: 1010

√ 7: 0111

**√**13: 1101

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**√**15: 1111

#### 2<sup>nd</sup> column

2,3: 001-2,10: -010

4,5: 010-

8,10: 10-0

3,7: 0-11

√ 5,7: 01-1

√ 5,13: -101

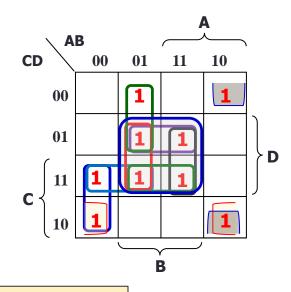
**√** 7,15: -111

**√**13,15: 11-1

#### 3<sup>rd</sup> column

5,7,13,15: -1-1

<del>5,7,13,15: -1-1</del>



We have completed

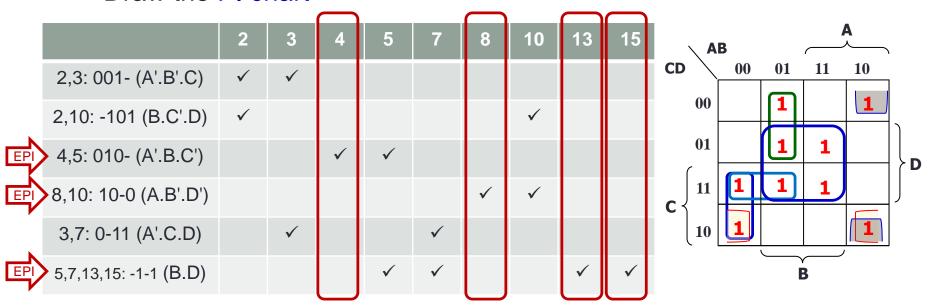
Phase 1: Identifying all the

Prime Implicants (PIs)!



#### Phase 2: Identify the Essential Prime Implicants (EPIs)

Draw the PI chart



Where are the EPIs? Look for columns containing a single tick.

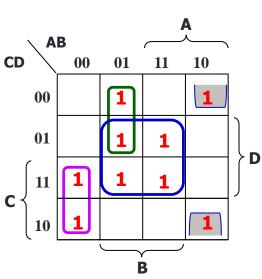
EPIs are: A'.B.C', A.B'.D', and B.D

But we are not done yet. There are still minterms not covered by the EPIs!

#### Phase 2: After identifying the EPIs

Draw the reduced PI chart if there are minterms not covered





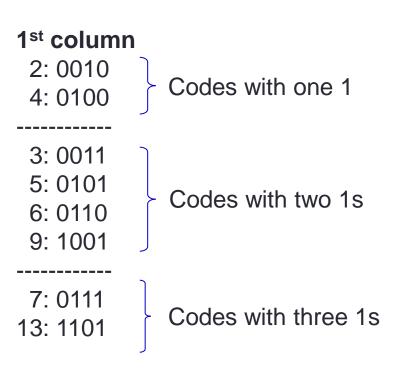
- 1. Find out what are the minterms covered by the EPIs.
- Remove the EPIs and minterms they cover from the chart → reduced PI chart.

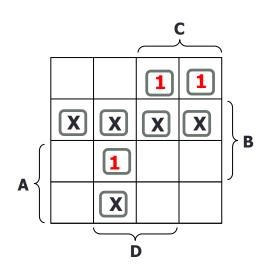
Answer: B.D + A'.B.C' + A.B'.D' + A'.B'.C





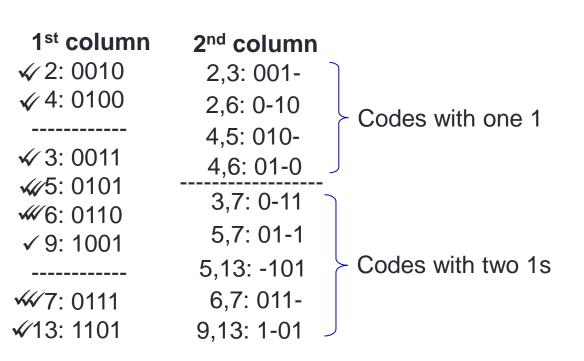
Step 1: List out all minterms in groups with same number of 1s in their binary codes.

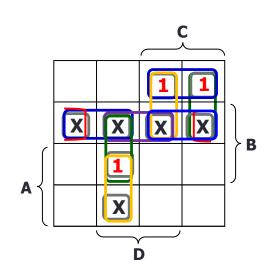






Step 2: Combine codes that differ by 1 bit into bigger group, write the combined code in next column.

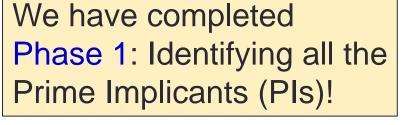






Repeat step 2 – Combine codes that differ by 1 bit Step 3: into bigger group, write the combined code in next column.

#### 1<sup>st</sup> column 2<sup>nd</sup> column 3<sup>rd</sup> column **4**/2: 0010 **√** 2,3: 001-2,3,6,7: 0-1-**√** 4: 0100 **√** 2,6: 0-10 <del>2,6,3,7: 0-1</del> **√** 4,5: 010-4,5,6,7: 01--**4**/3: 0011 **√** 4,6: 01-0 Α 4657·01 **44/5**: 0101 X √ 3,7: 0-11 **446**: 0110 √ 5,7: 01-1 Not a PI because it √ 9: 1001 5,13: -101 contains all don't cares. **%** 6,7: 011-





**√√**7: 0111

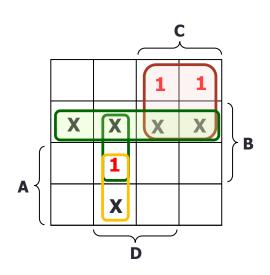
**4**13: 1101

9,13: 1-01

#### Phase 2: Identify the Essential Prime Implicants (EPIs)

Draw the PI chart

		2	3	13	4	5	6	7	9
	2,3,6,7: 0-1- (A'.C)	✓	✓				✓	✓	
	5,13: -101 (B.C'.D)			✓		✓			
	9,13: 1-01 (A.C'.D)			✓					✓



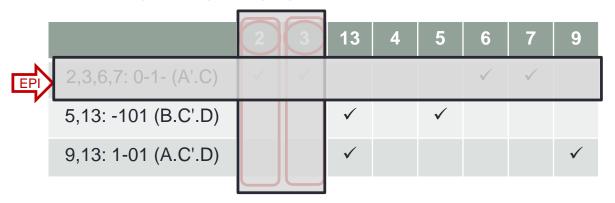
Where are the EPIs? Look for columns containing a single tick.

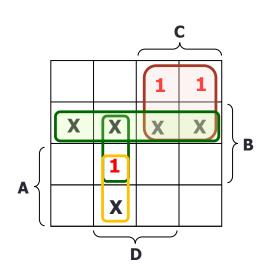
EPI: A'.C'

But we are not done yet. There are still minterms not covered by the EPIs!

#### Phase 2: Identify the Essential Prime Implicants (EPIs)

Draw the PI chart





#### Where are the EPIs? A'.C'

- 1. Find out what are the minterms covered by the EPIs.
- 2. Remove the EPIs and minterms they cover from the chart → reduced PI chart.
- 3. Find the minimum number of remaining PIs to cover the remaining minterms. Either B.C'.D or A.C'.D



Answer: A'.C' + B.C'.D or A'.C' + A.C'.D

# **End of File**

