## CS2040S: Data Structures and Algorithms Recitation 5

## Goals:

- Recognize tree-related problems
- Learn how tree search can efficiently support various user-defined operations
- $\bullet$  Appreciate the data-summarization ability granted by augmenting data structures

## Problem 1. (Heights and Grades)

Suppose you are given a set of students with heights and grades as follows:

| Name                 | Height (cm) | Grade (GPA) |
|----------------------|-------------|-------------|
| Charles              | 176         | 4.2         |
| $\operatorname{Bob}$ | 162         | 4.5         |
| Mary                 | 180         | 3.6         |
| John                 | 155         | 4.1         |
| Wick                 | 186         | 5.0         |
| Alice                | 170         | 3.9         |

Your goal is to implement an Abstract Data Type (ADT) to efficiently answer the question: "What is the average grade of all students taller than \_\_\_\_\_?". For instance, the average grade of all students taller than John is (4.2 + 4.5 + 3.6 + 5.0 + 3.9)/5 = 4.24.

More specifically, the ADT specifications are as follows:

| Operation                   | Behaviour   |
|-----------------------------|---|
| insert(name, height, grade) | Inserts student into the dataset.                     |
| findAverageGrade(name)      | Returns the average grade among all the students that |
| TindaverageGrade(name)      | are taller than the given student.                    |

**Problem 1.a.** How do you capture the information of each student? What should the data type for each of their attributes be?

**Problem 1.b.** How do you design a Data Structure (DS) that serves as an efficient implementation of the given ADT? You may assume that name and height are unique.

**Problem 1.c.** What if height is now not unique? What issue(s) will arise from this? How might you modify your solution in the previous part to resolve the issue(s)?

## Problem 2. (A Game of Cards)

Suppose you have a deck of n cards and they are spread out in front of you on the table from left to right with each card indexed from i to n. Each card can either be facing up or down. We are tasked to implement an ADT for a magic trick with the following specification:

| Operation                 | Behaviour   |  |
|---------------------------|---|--|
| query(i)                  | Return whether card at index i is facing up or down.                        |  |
| <pre>turnOver(i, j)</pre> | Turn over all cards in the subsequence specified by the index range [i, j]. |  |

**Problem 2.a.** Given n cards already laid out on the table, how do you design a DS that implements such an ADT? Can you achieve turn0ver in  $O(\log n)$  time regardless of the length of subsequence to be turned over? What a magic trick indeed to be able to achieve that!