THE SAGE ENGINE

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1. Sage

Sage is a mathematical software system providing an open source alternative to Magma, Maple, Mathematica, and Matlab. It is available from http://www.sagemath.org/ as a free download. The program provides all of the standard features expected from such a system: arbitrary precision arithmetic, symbolic integration and differentiation, two-dimensional plotting of functions, matrix algebra, and much more.

Download sage from this web site. Move the resulting "Sage" program to /Applications. The application will have a strange name, something like Sage-5.10..64bit-10.8.

The Sage command line program is inside this wrapper, and our engine folder is going to have to use that binary. If we keep the current name, the engine file will be tied to one particular version of Sage. To fix this, change the name to just "Sage". This clever step, which simplifies several steps below, is due to Daniel Grambihler.

Sage TeX is a piece of the Sage download. It is basically a LaTeX style file, which allows users to embed and process Sage code from within TeX files. The last three pages of this document show this style file in action. The source code on page three is followed by LaTeX output on pages four and five.

2. How SageTeX Works

In the source file, the initial line

tells TeXShop to process the file using the sage engine; this engine first calls pdflatex, then calls sage, and finally calls pdflatex again. The remaining lines in the preamble are standard LaTeX commands, except the required line

\usepackage{sagetex}

In the remaining source, sage commands are entered within lines of the form

These line cause sage to process commands and output LaTeX source fragments, which become part of the LaTeX document.

Notice in particular that sage can plot standard functions. Sage can also compute integrals symbolically; for example, look carefully at the command which processes $\int \frac{x^2+x+1}{(x-1)^3(x^2+x+2)}$. This command contains standard LaTeX code to display the integral, but then Sage integrates and returns a typeset copy of the result.

3. Setting Up the Engine

This folder contains an engine file named "sage.engine". Move this file to the active portion of \sim /Library/TeXShop/Engines. Dan Drake, who is responsible for SageTeX, wrote this engine.

The "Sage" program contains a style file named "sagetex.sty" and a number of support files. This style file is supposed to be copied to your TeX distribution. The file depends on other features of sage, so whenever you upgrade sage, you also need to upgrade sagetex.sty in your TeX distribution. It is easy to forget to do this. So rather than copying the style file, we just create a symbolic link from it's location in TeX Live to its location in Sage.

Run Terminal in /Applications/Utilities. Type the following

cd /usr/local/texlive/texmf-local/tex/latex

Then type the following on a single line. Terminal may make a linefeed when the line grows too long and that is fine, but do not for instance make a linefeed after the top "sage" and before the bottom "/data".

sudo ln -s /Applications/Sage.app/Contents/Resources/sage
/data/texmf/tex/generic/sagetex/sagetex.sty sagetex.sty

Finally issue the command

sudo mktexlsr

4. Final Remarks

Although spaces are permitted in LaTeX source file names, Sage does not like spaces in file names. So LaTeX source file names which call SageTeX should not contain spaces. This problem is fixed in beta releases of SageTeX not yet in the sage distribution.

A Sage tutorial is available at the Sage page http://www.sagemath.org/help.html. It is definitely recommended. Extensive additional documentation is available at the same web page.

```
% !TEX TS-program = sage
```

% The following lines are standard LaTeX preamble statements.

\documentclass[11pt, oneside]{amsart}

\usepackage{geometry}

\geometry{letterpaper}

\usepackage[parfill]{parskip}

\usepackage{graphicx}

\usepackage{amssymb}

\usepackage{epstopdf}

\title{Brief Article}

\author{The Author}

% Only one command is required to use Sage within the LaTeX source:

\usepackage{sagetex}

\begin{document}

\maketitle

\section{Introduction}

This is an example of using Sage within a \TeX\ document. We can compute extended values like

We can plot functions like $x \sin x$:

 $\square{1} \sum_{x \in S} \int \int (x * \sin(30 * x), -1, 1)$

We can integrate:

 $\pi ((x^2 + x + 1) \operatorname{((x - 1)^3 (x^2 + x + 2)}}), dx$ \$\\$= \sage{\integrate((x^2 + x + 1) / ((x - 1)^3 * (x^2 + x + 2)))}\$\$

\newpage

We can perform matrix calculations:

\$\$\sage{matrix([[1, 2, 3], [4, 5, 6], [7, 8, 9]])^3}\$\$

 $AB= \quad AB= \Lambda([[1, 2], [3, 4]]) \quad AB= \Lambda([[5, 6], [6, 8]]) = \quad AB= \Lambda([[1, 2], [3, 4]]) * Matrix([[5, 6], [6, 8]])$

Plots are fun; here is a second one showing \$x \ln x\$. The ``width" command in the source is sent to the include graphics command in LaTeX rather than to Sage.

 $\square{ \square | \squa$

Sage understands mathematical constants and writes them symbolically unless it is told to produce a numerical approximation. The term \$e \pi\$ below is not in the LaTeX source; instead it is the result of a Sage calculation, as is the numerical value on the other side of the equal sign.

The product of e and $\phi = \frac{n * e}{n * e} = \frac{N(pi * e)}{.}$

\end{document}

BRIEF ARTICLE

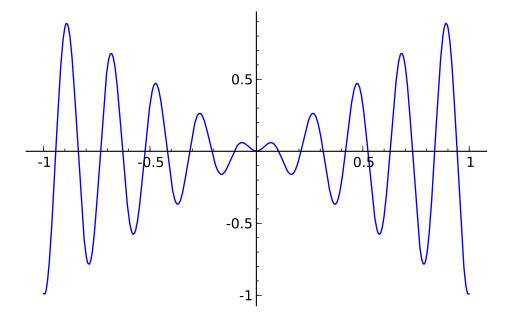
THE AUTHOR

1. Introduction

This is an example of using Sage within a TEX document. We can compute extended values like

$$32^{31} = 45671926166590716193865151022383844364247891968$$

We can plot functions like $x \sin x$:



We can integrate:

$$\int \frac{x^2 + x + 1}{(x - 1)^3 (x^2 + x + 2)} dx$$

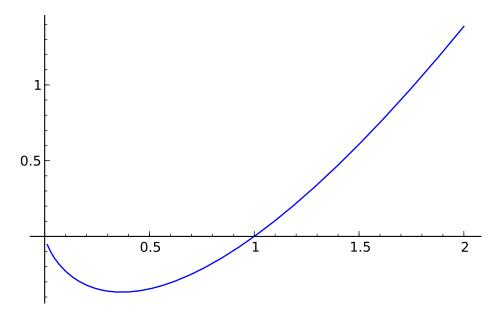
$$= -\frac{9}{448} \sqrt{7} \arctan\left(\frac{1}{7} (2x + 1)\sqrt{7}\right) - \frac{3}{16} \frac{(x + 1)}{(x^2 - 2x + 1)} - \frac{5}{64} \log(x - 1) + \frac{5}{128} \log(x^2 + x + 2)$$

We can perform matrix calculations:

$$\begin{pmatrix} 468 & 576 & 684 \\ 1062 & 1305 & 1548 \\ 1656 & 2034 & 2412 \end{pmatrix}$$

$$AB = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \begin{pmatrix} 5 & 6 \\ 6 & 8 \end{pmatrix} = \begin{pmatrix} 17 & 22 \\ 39 & 50 \end{pmatrix}$$

Plots are fun; here is a second one showing $x \ln x$. The "width" command in the source is sent to the include graphics command in LaTeX rather than to Sage.



Sage understands mathematical constants and writes them symbolically unless it is told to produce a numerical approximation. The term $e\pi$ below is not in the LaTeX source; instead it is the result of a Sage calculation, as is the numerical value on the other side of the equal sign.

The product of e and π is $\pi e = 8.53973422267357$.