



भारतीय प्रौद्योगिकी संस्थान गुवाहाटी
INDIAN INSTITUTE OF TECHNOLOGY GUWAHATI

MA 374: Financial Engineering Lab Lab 02

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Question 1.

Data given to determine the initial price of a European call and a European put option in the binomial model are:

$$S(0) = 100, K = 100, T = 1, M = 100, r = 8\%, \sigma = 20\%$$

Also given 2 sets of u and d:

a) Set 1 : $u = e^{\sigma\sqrt{\Delta t}}, d = e^{-\sigma\sqrt{\Delta t}}$

b) Set 2 : $u = e^{\sigma\sqrt{\Delta t} + \left(r - \frac{1}{2}\sigma^2\right)\Delta t}, d = e^{-\sigma\sqrt{\Delta t} + \left(r - \frac{1}{2}\sigma^2\right)\Delta t}$

Using them:

```
The Call price for set 1 is: 12.085380013710122
The Put price for set 1 is: 4.397014652374142
The Call price for set 2 is: 12.12304707401244
The Put price for set 2 is: 4.434681712676475
```

The **sensitivity analysis** of option price variance with **S(0)**, **K**, **M**, **r**, σ has been done by plotting 2-D and 3-D plots .

Question 2.

The path-dependent derivative used for this question is the **Asian Option**.

The payoff for the Asian Call Option = $(S_{avg \ over \ path} - K)^+$

The payoff for the Asian Put Option = $(K - S_{avg \ over \ path})^+$

Here K is the strike price.

The data taken for this question is:

$$S(0) = 100, K = 100, T = 1, M = 10, r = 8\%, \sigma = 20\%$$

We have taken the value of **M as 10**. For an Asian option, we have to take all possible paths, which in our case will be 2^M . So taking a value of $M = 100$, would be computationally infeasible. The initial option price (for call and put) can be found using,

$$H(0) = \frac{1}{e^{rT}} \sum_{\text{over all paths}} p^{\text{ups}} (1-p)^{M-\text{ups}} f(S_{avg})$$

Here **ups** represents the **number of ups** in the path, **f** denotes the **payoff for the Asian option**, and S_{avg} denotes the **average stock price over the path**, which is computed as:

$$S_{avg} = \frac{\sum_{i=0}^{i=M} S\left(\frac{T * i}{M}\right)}{M + 1}$$

Using these formulae, we get:

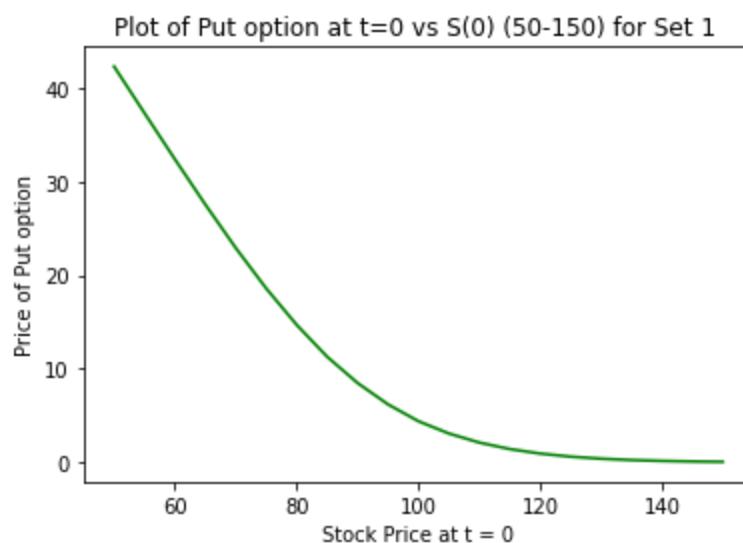
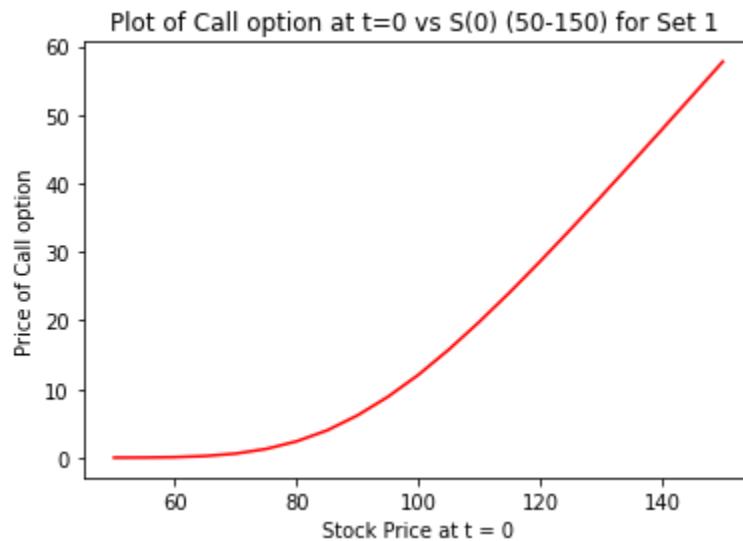
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The Asian Call price for set 1 is: 6.476003047446573
The Asian Put price for set 1 is: 2.6779455899442306
The Asian Call price for set 2 is: 6.490029377643389
The Asian Put price for set 2 is: 2.691971920141049
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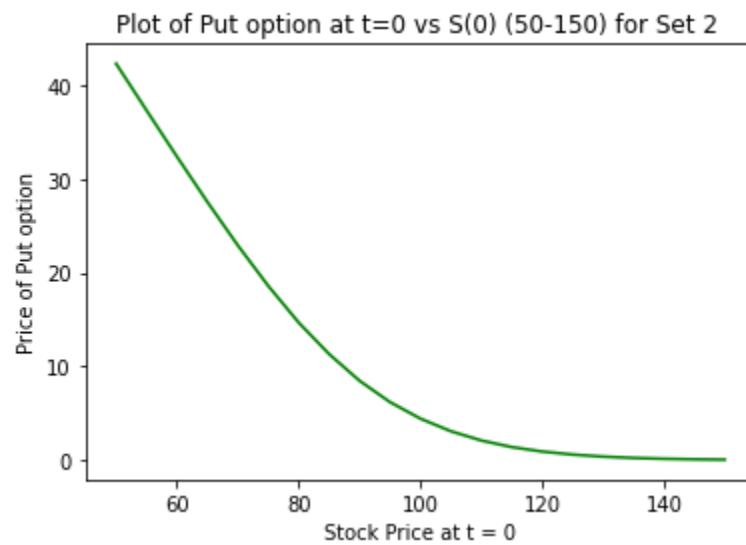
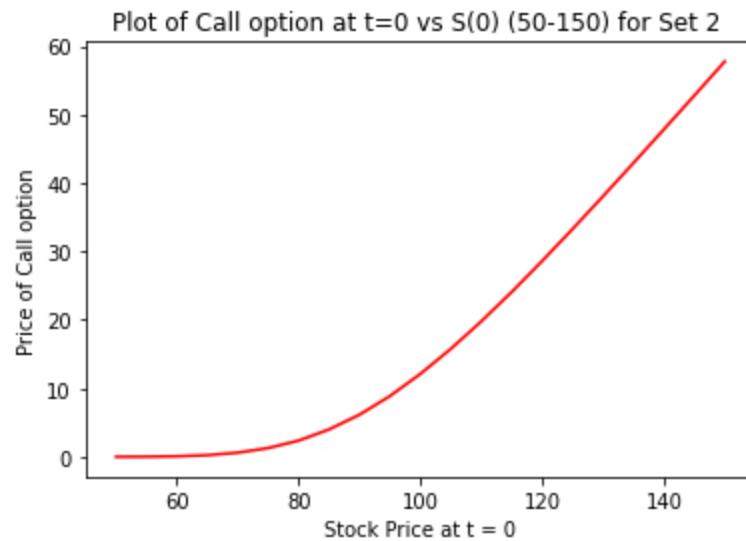
The **sensitivity analysis** of option price variance with $S(0)$, K , M , r , σ has been done by plotting 2-D and 3-D plots.

Question 1 Plots -

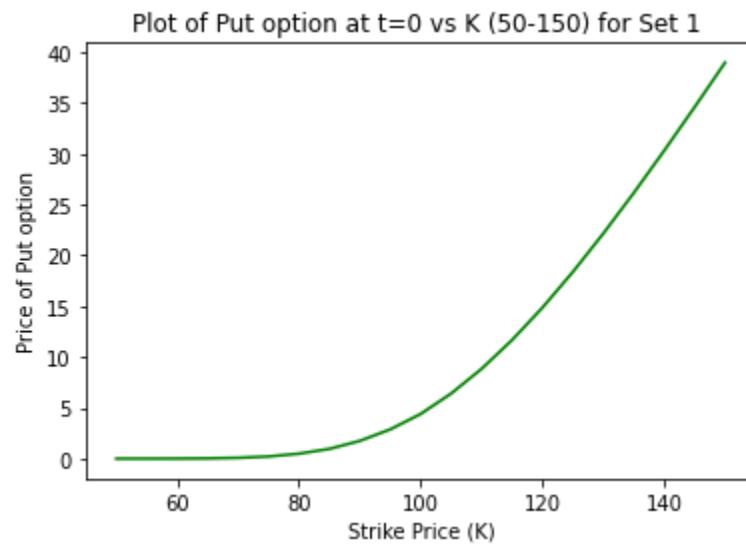
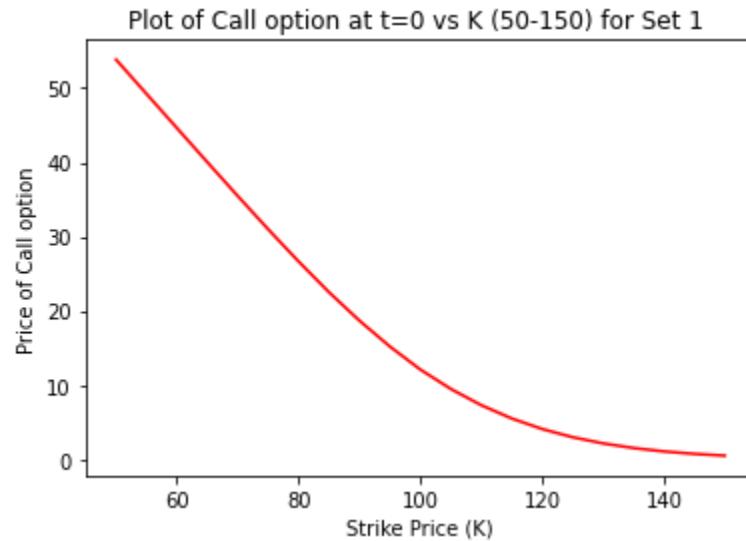
2D Plots (1 param at a time)

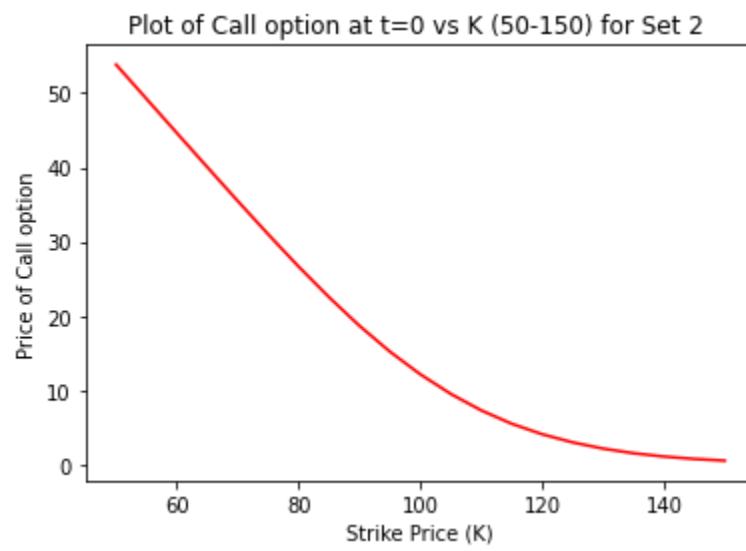
- Using Cos-Rubeinstein formula, it is evident that the Call Option price has positive dependence on $S(0)$, and then using Put-Call Parity shows that the Put Option price has negative dependence on $S(0)$.



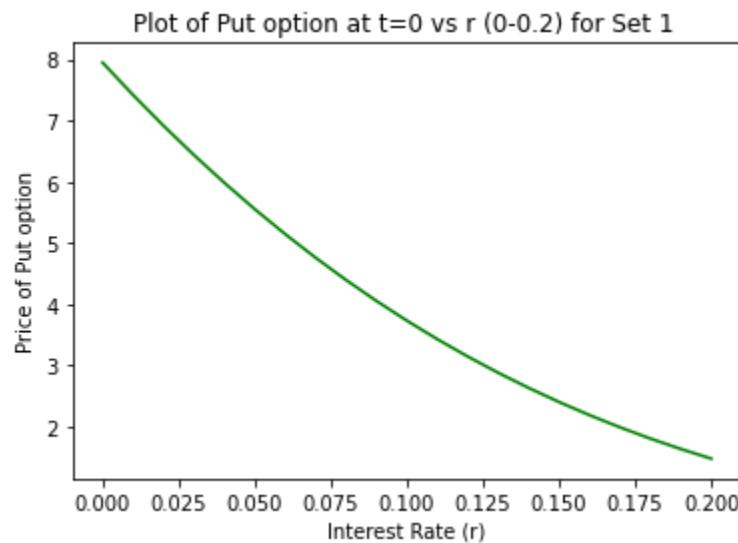
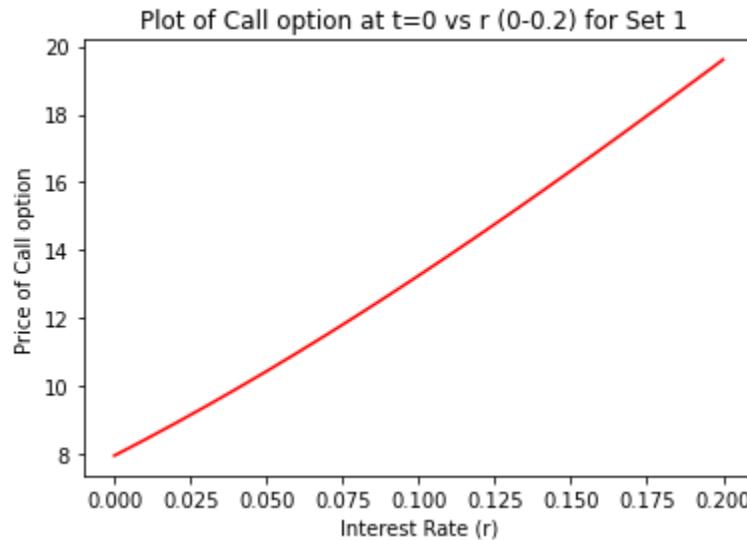


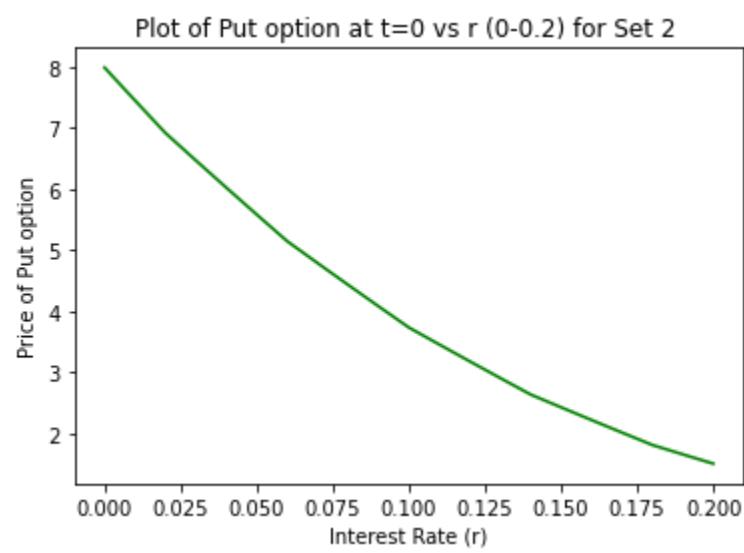
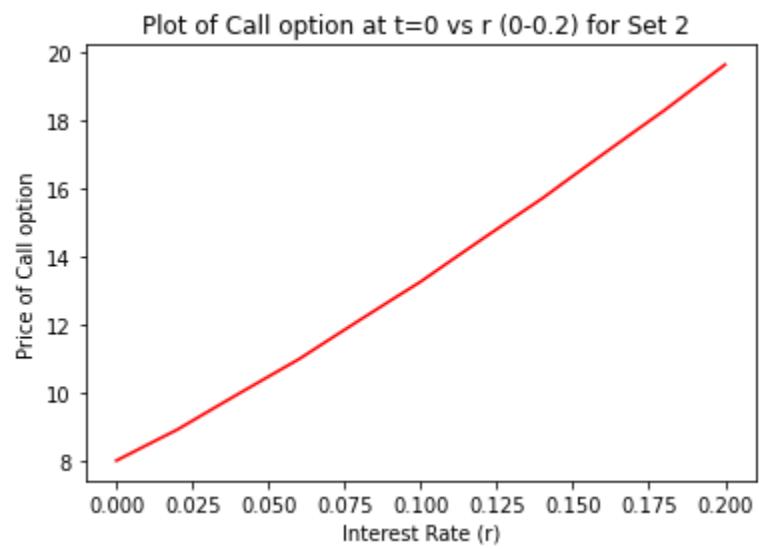
- Using Cos-Rubeinstein formula, it is evident that the Call Option price has negative dependence on K, and then using Put-Call Parity shows that the Put Option price has positive dependence on K.



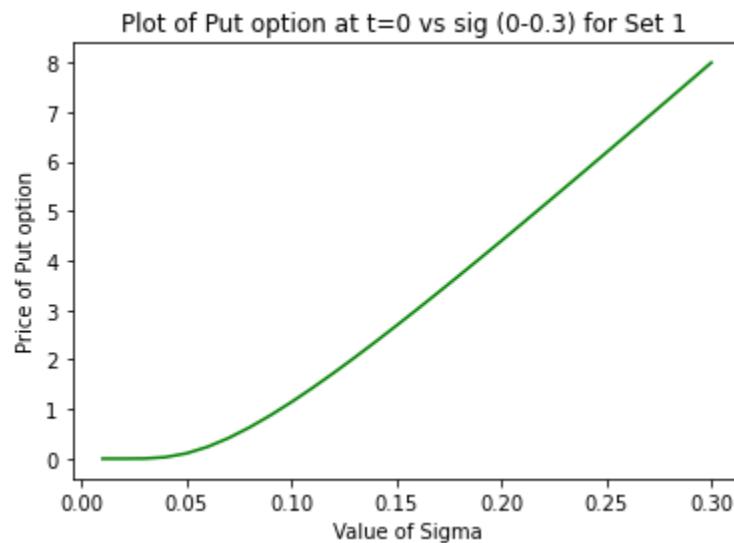
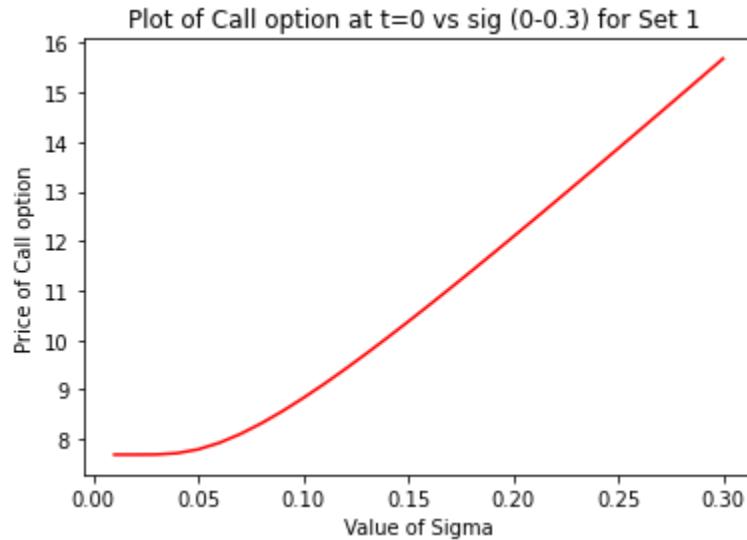


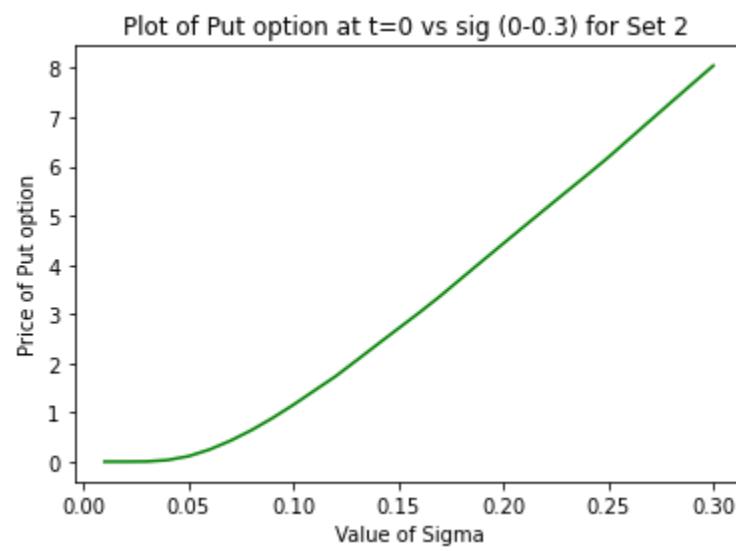
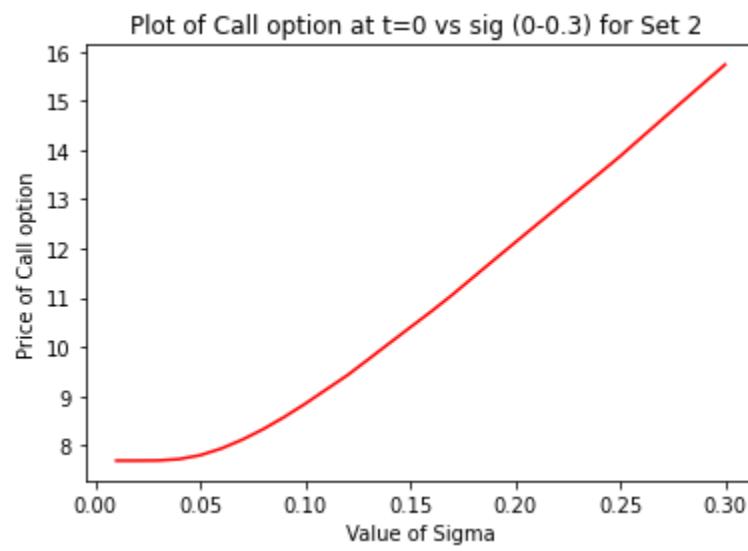
- Using Cos-Rubeinstein formula, it is evident that the Call Option price has positive dependence on r , and then using Put-Call Parity shows that the Put Option price has negative dependence on r .



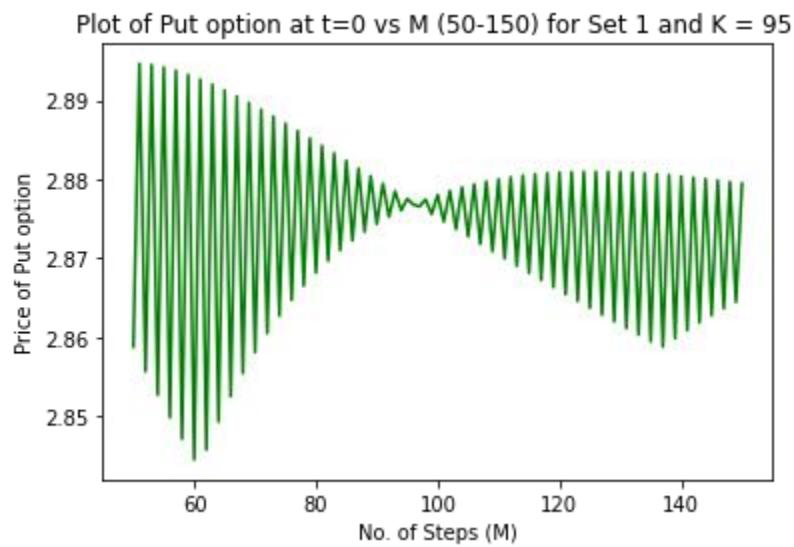
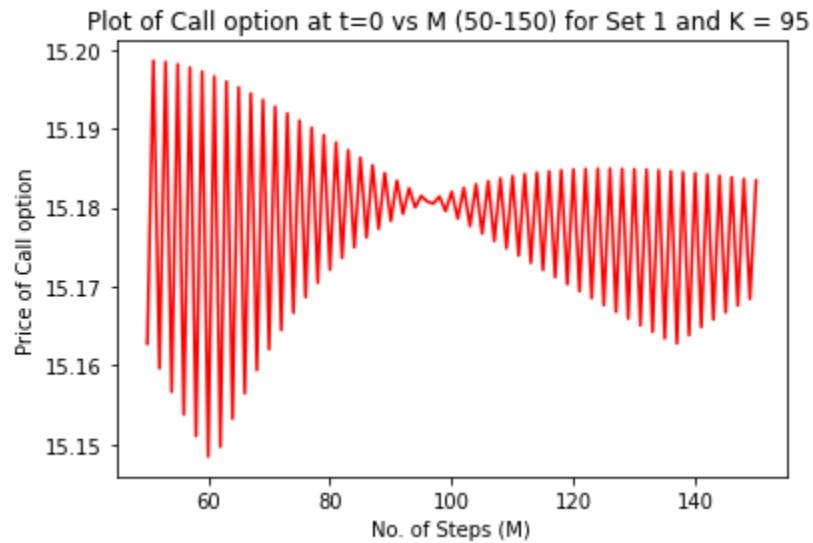


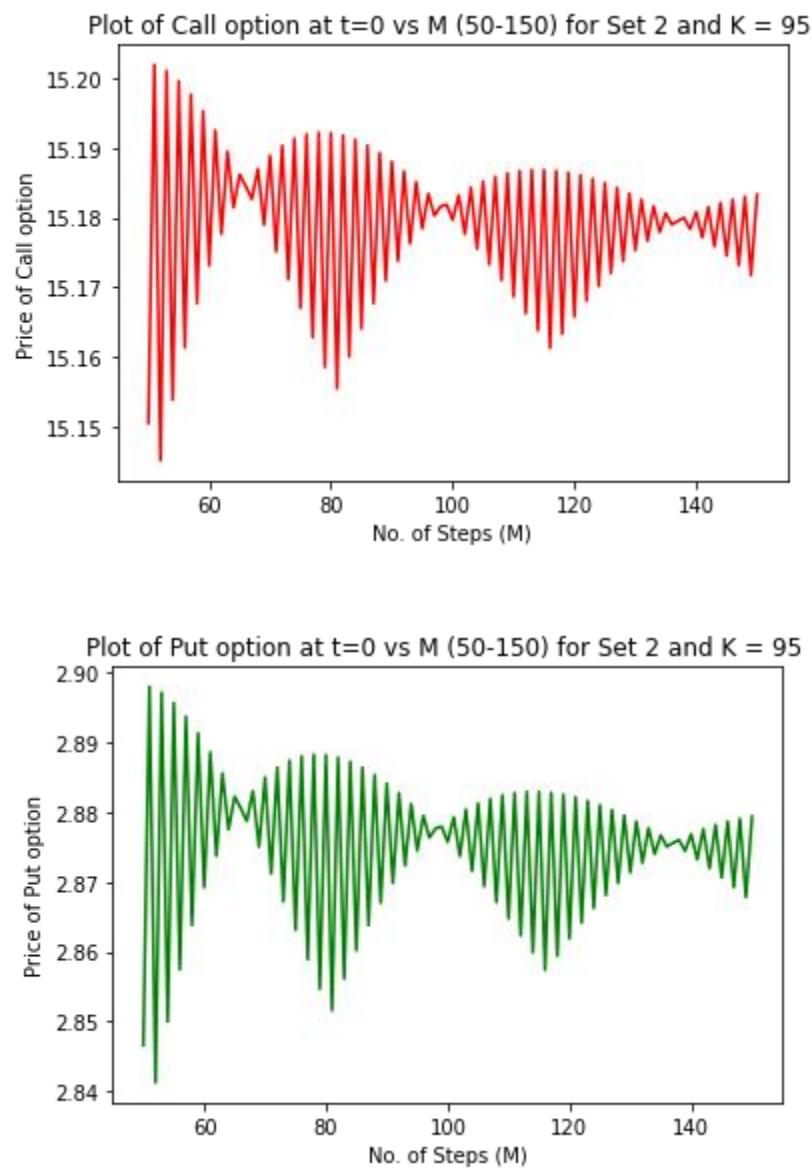
- Call Option price and Put Option has positive dependence on sigma



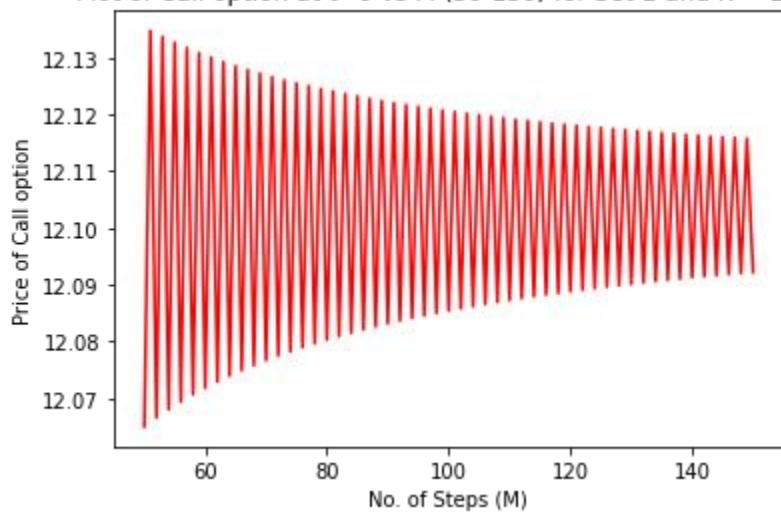


- Call Option price and Put Option price fluctuates as M ranges

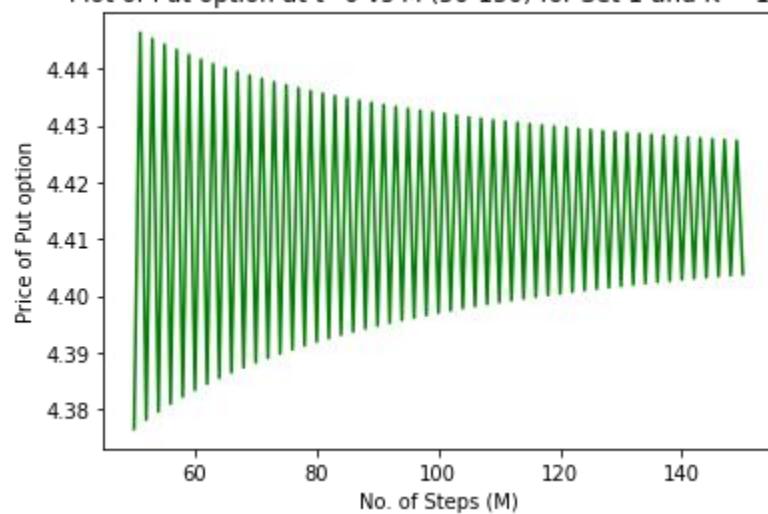


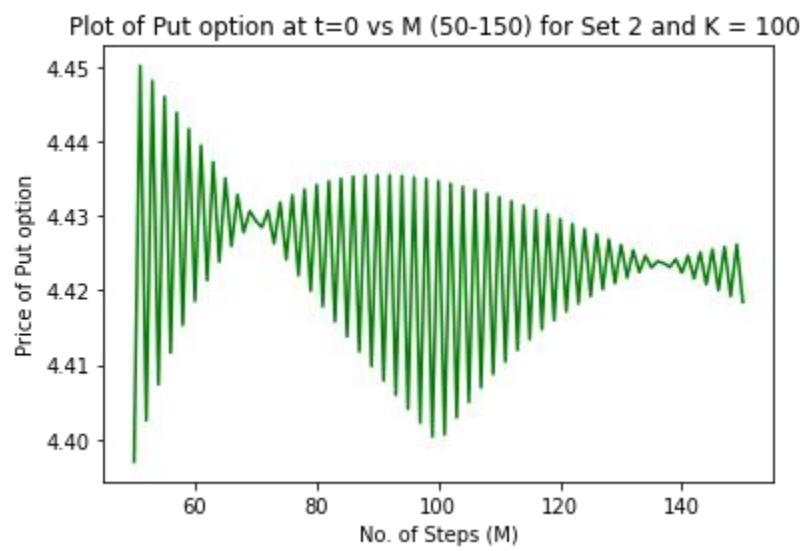
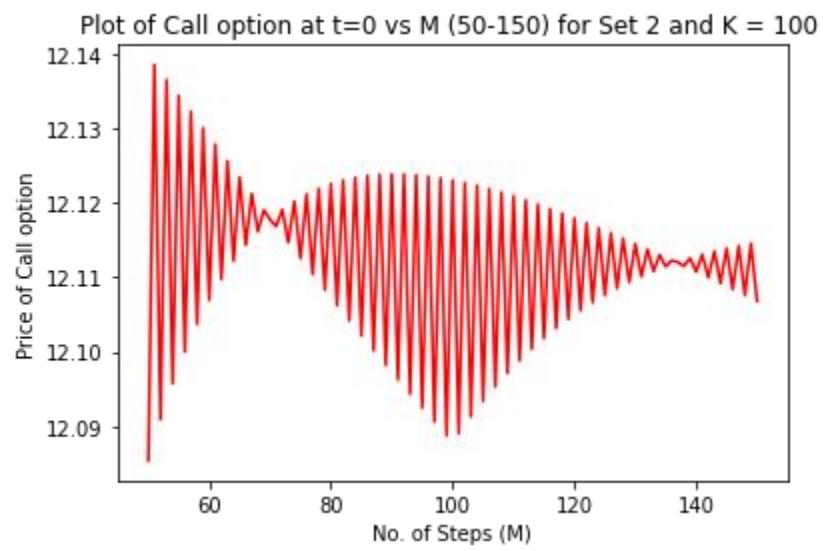


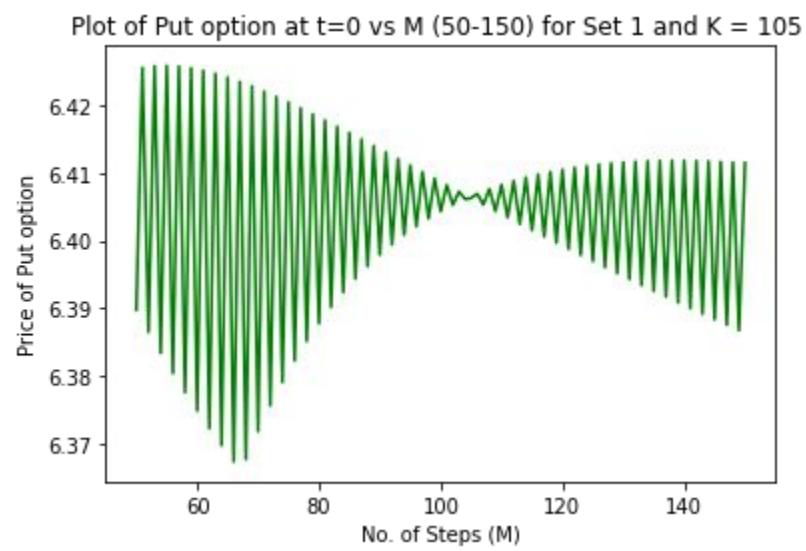
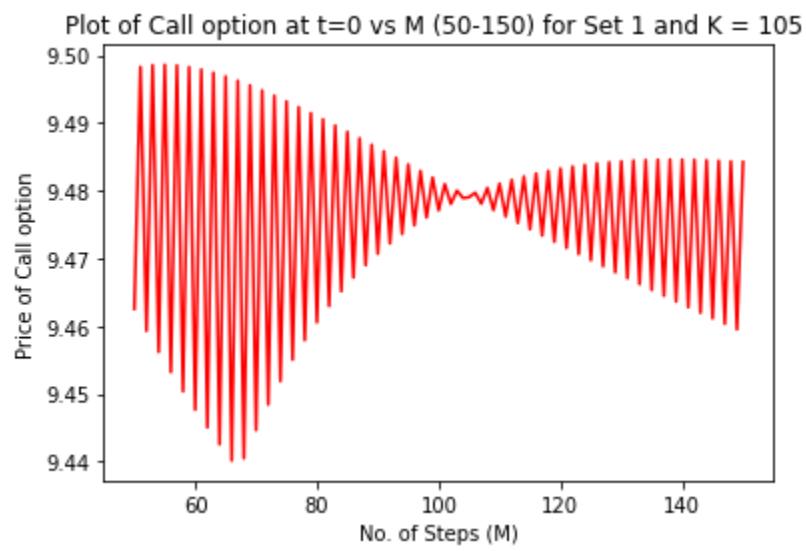
Plot of Call option at $t=0$ vs M (50-150) for Set 1 and $K = 100$

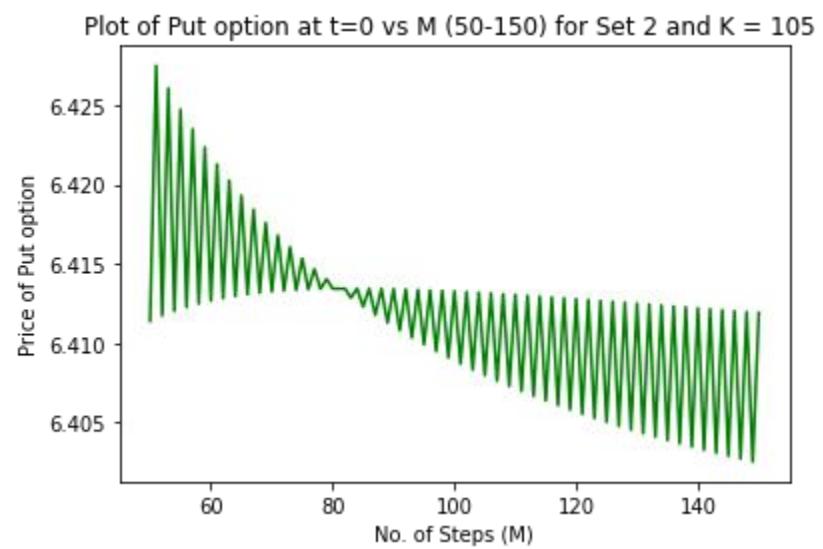
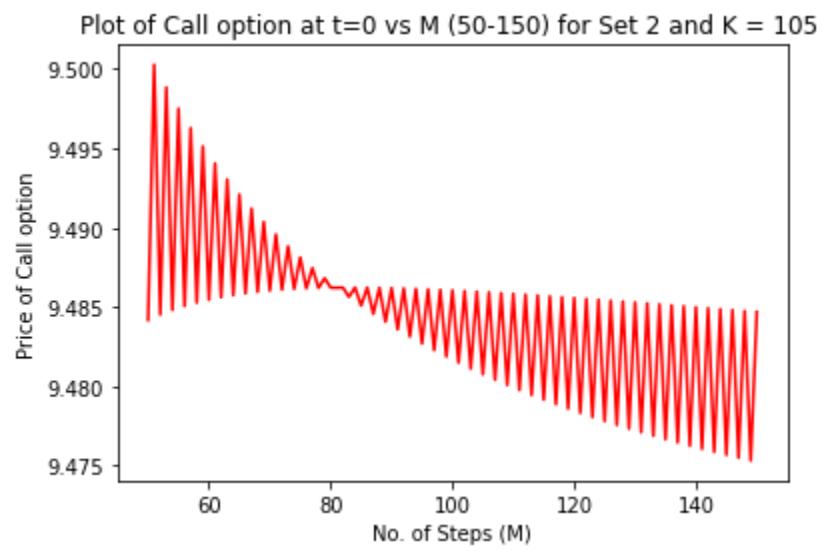


Plot of Put option at $t=0$ vs M (50-150) for Set 1 and $K = 100$





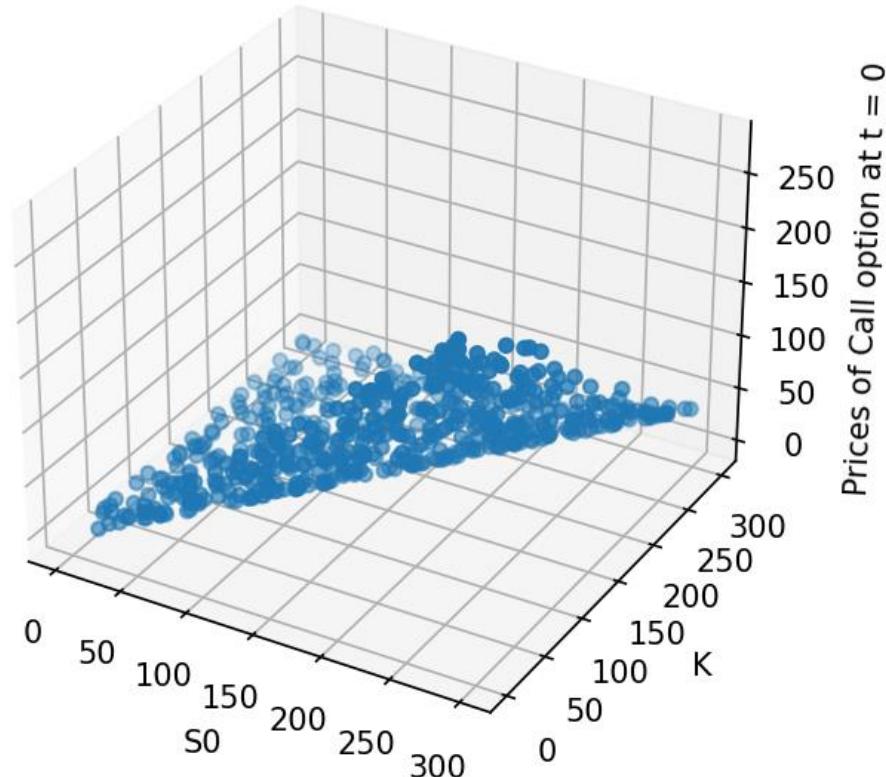




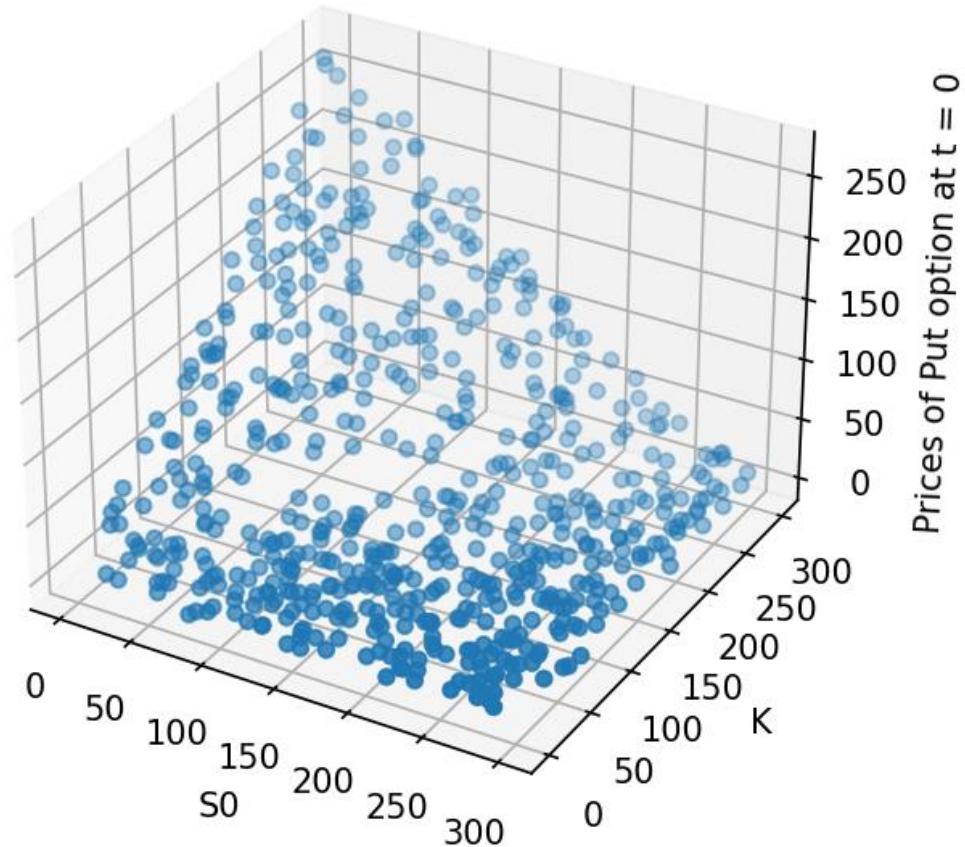
3D Plots (2 params at a time)

Figure 1

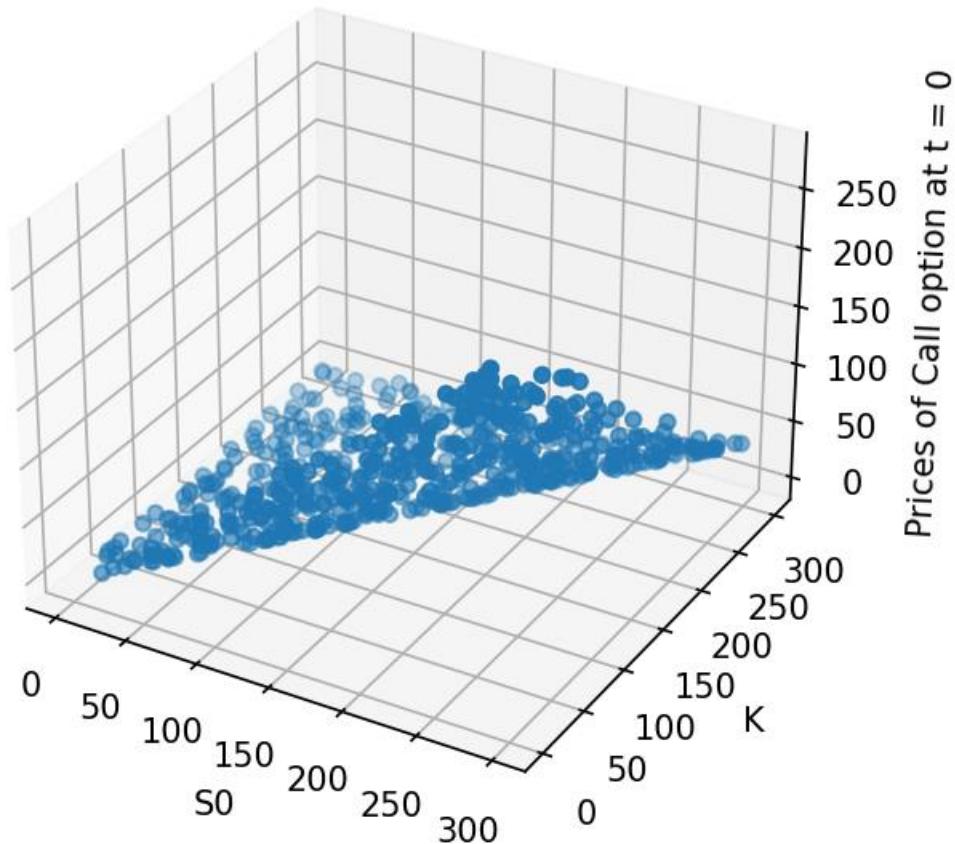
Initial Call Option Price vs S_0 and K for the set = 1



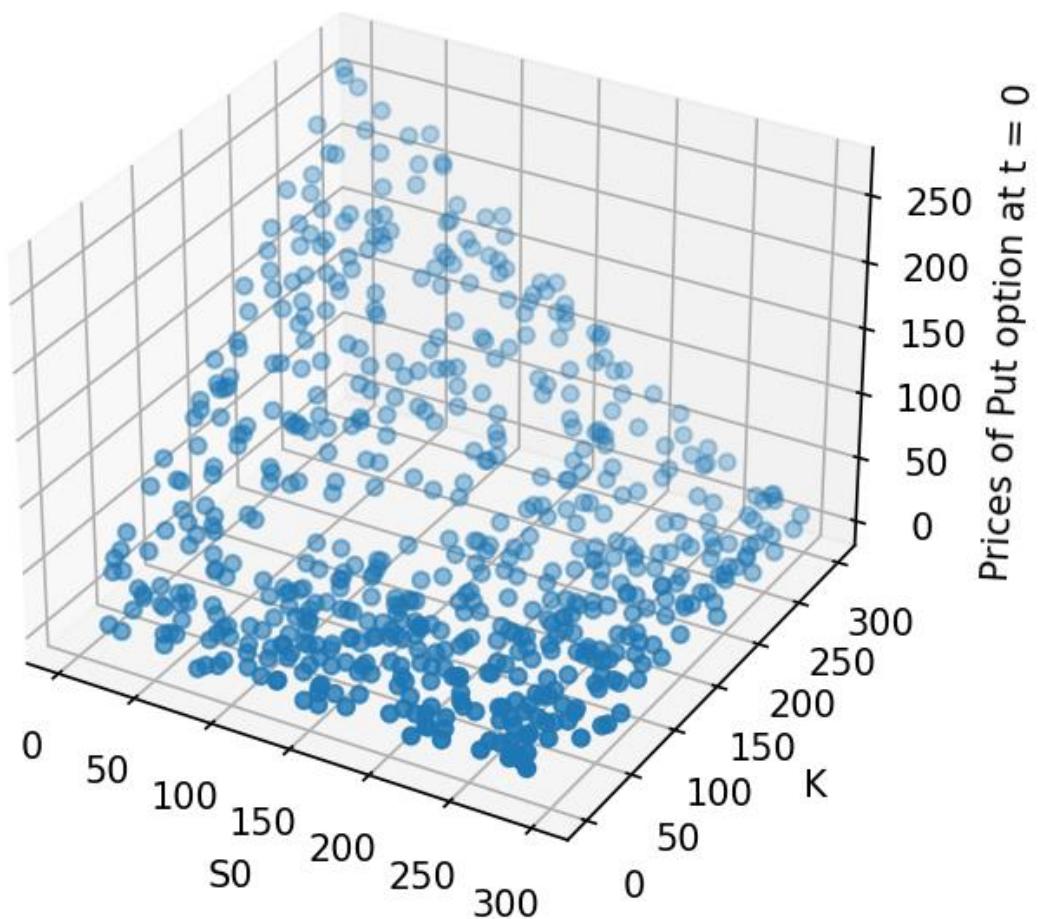
Initial Put Option Price vs S_0 and K for the set = 1



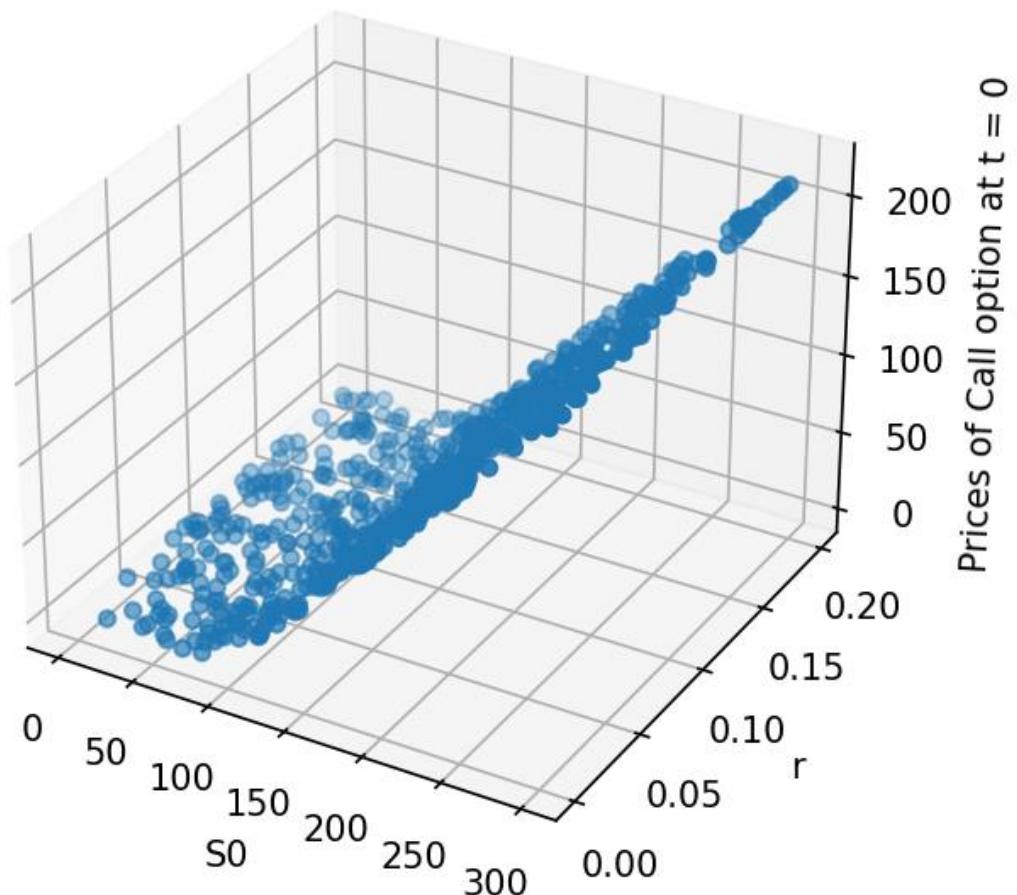
Initial Call Option Price vs S_0 and K for the set = 2



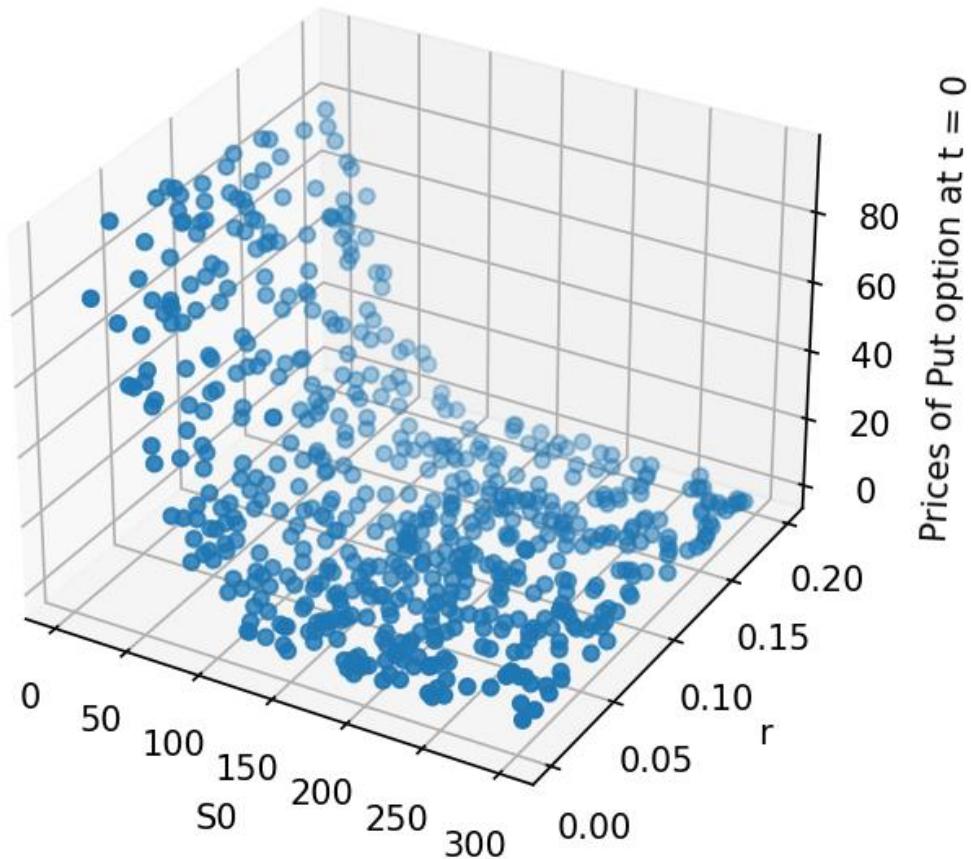
Initial Put Option Price vs S_0 and K for the set = 2



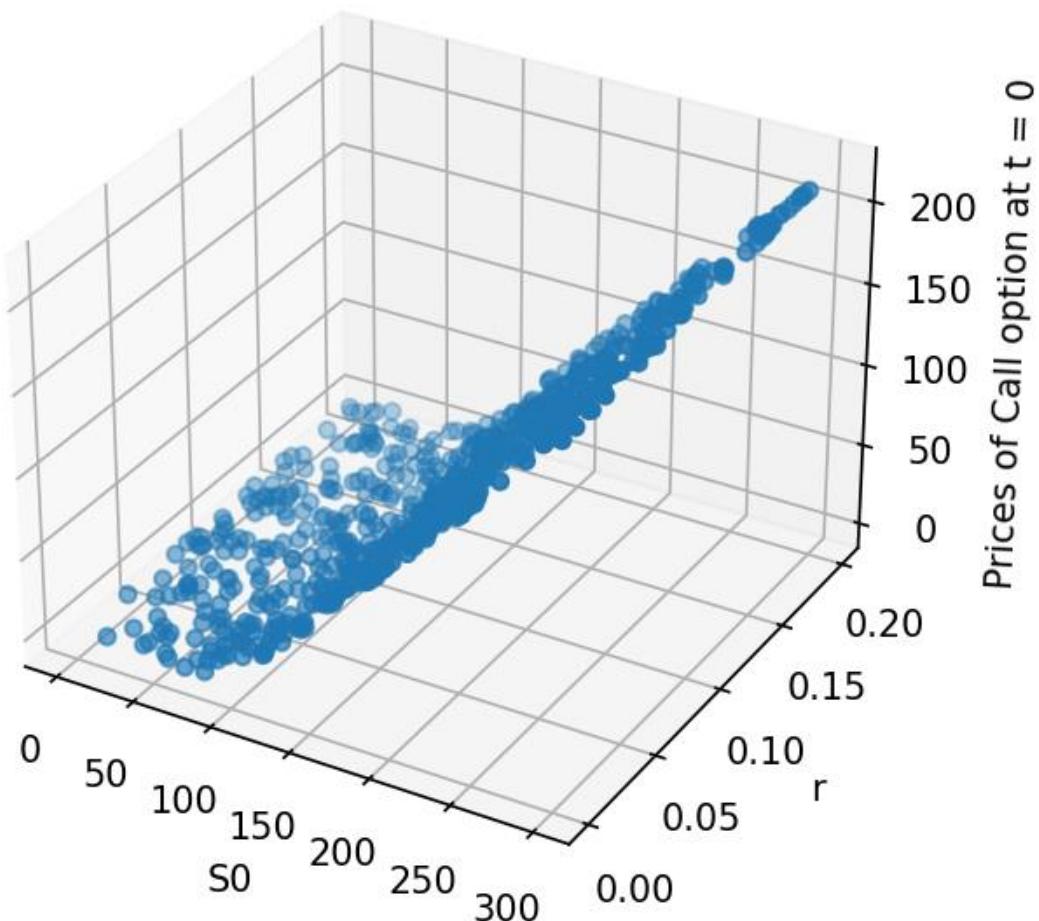
Initial Call Option Price vs S0 and r for the set = 1



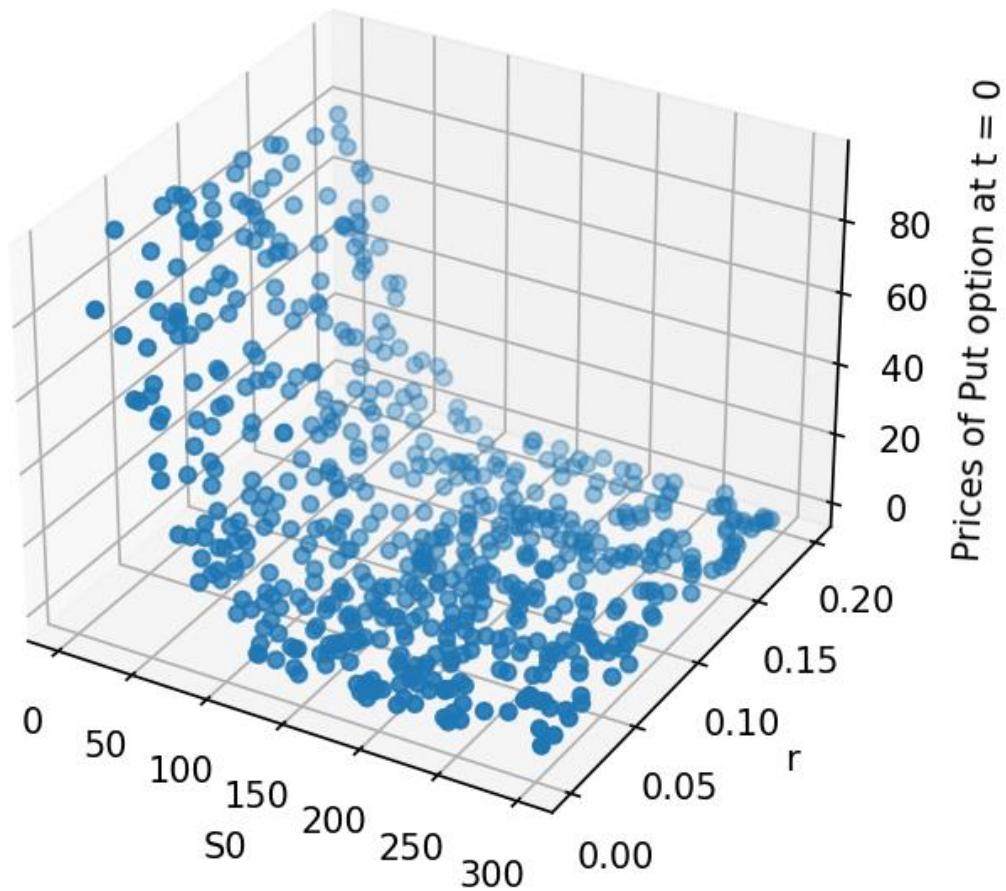
Initial Put Option Price vs S_0 and r for the set = 1



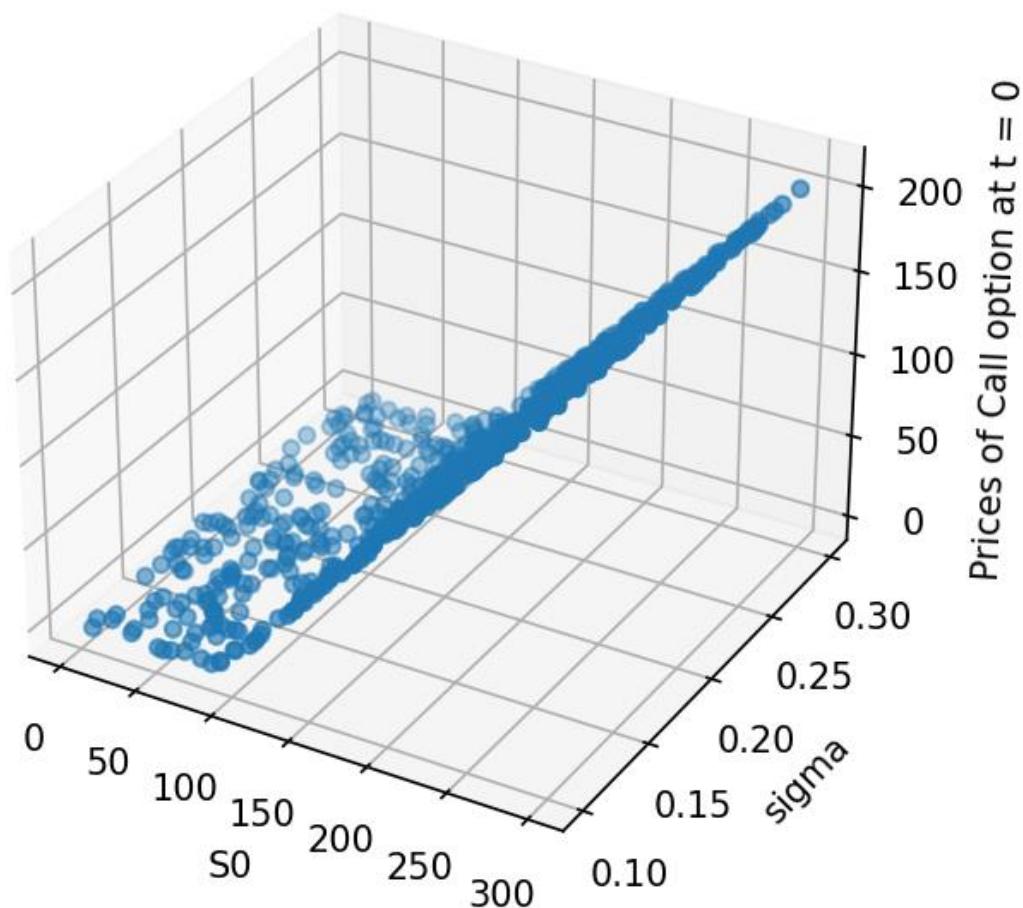
Initial Call Option Price vs S_0 and r for the set = 2



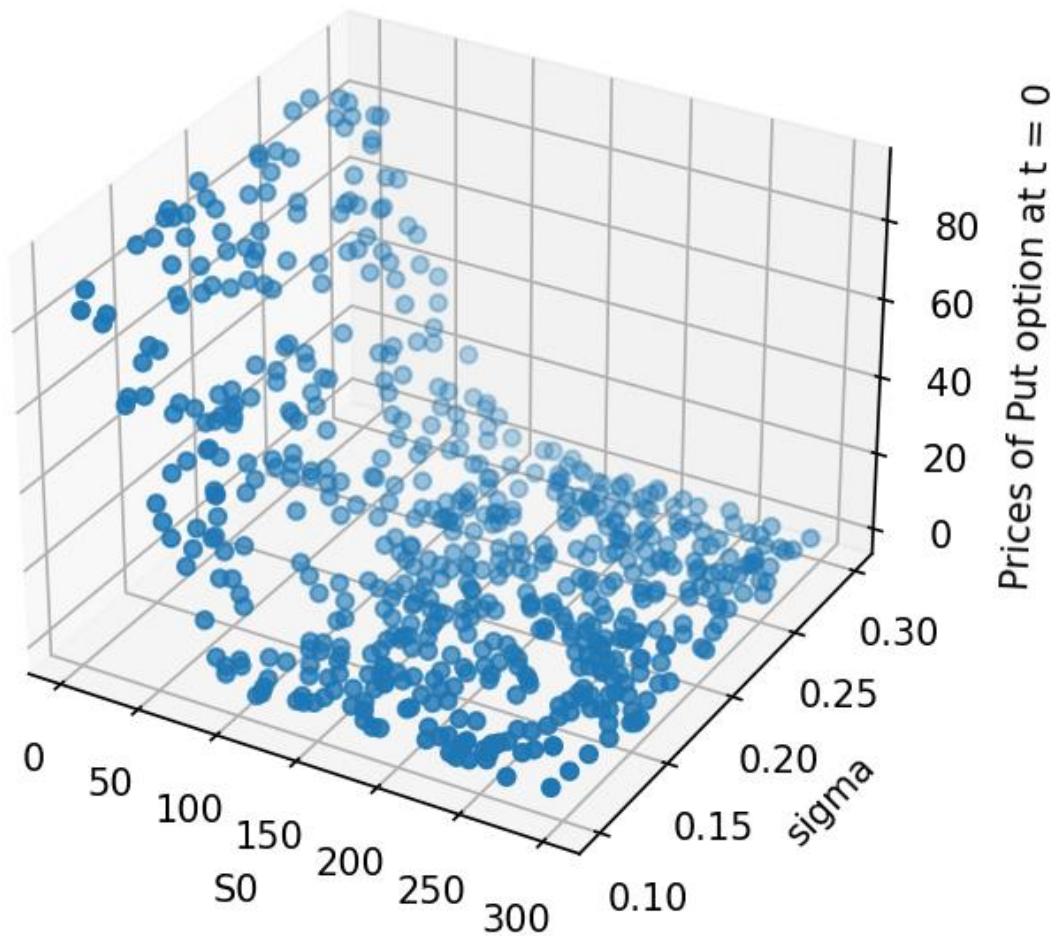
Initial Put Option Price vs S_0 and r for the set = 2



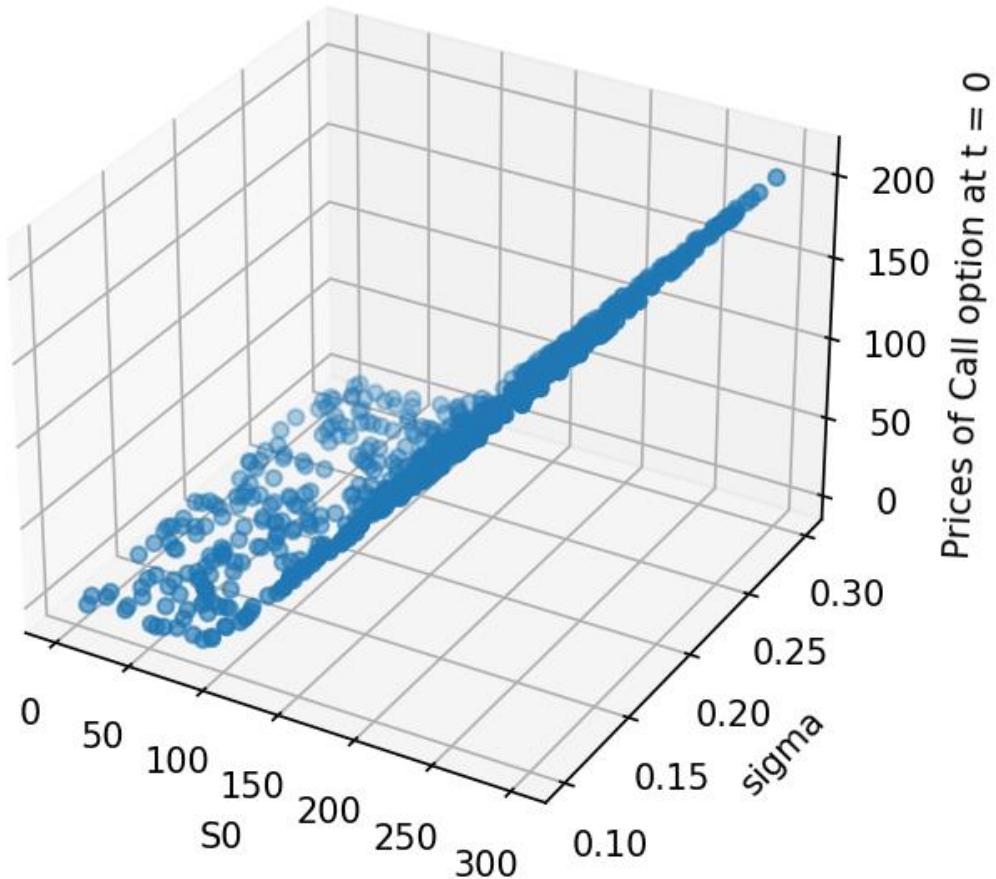
Initial Call Option Price vs S0 and sigma for the set = 1



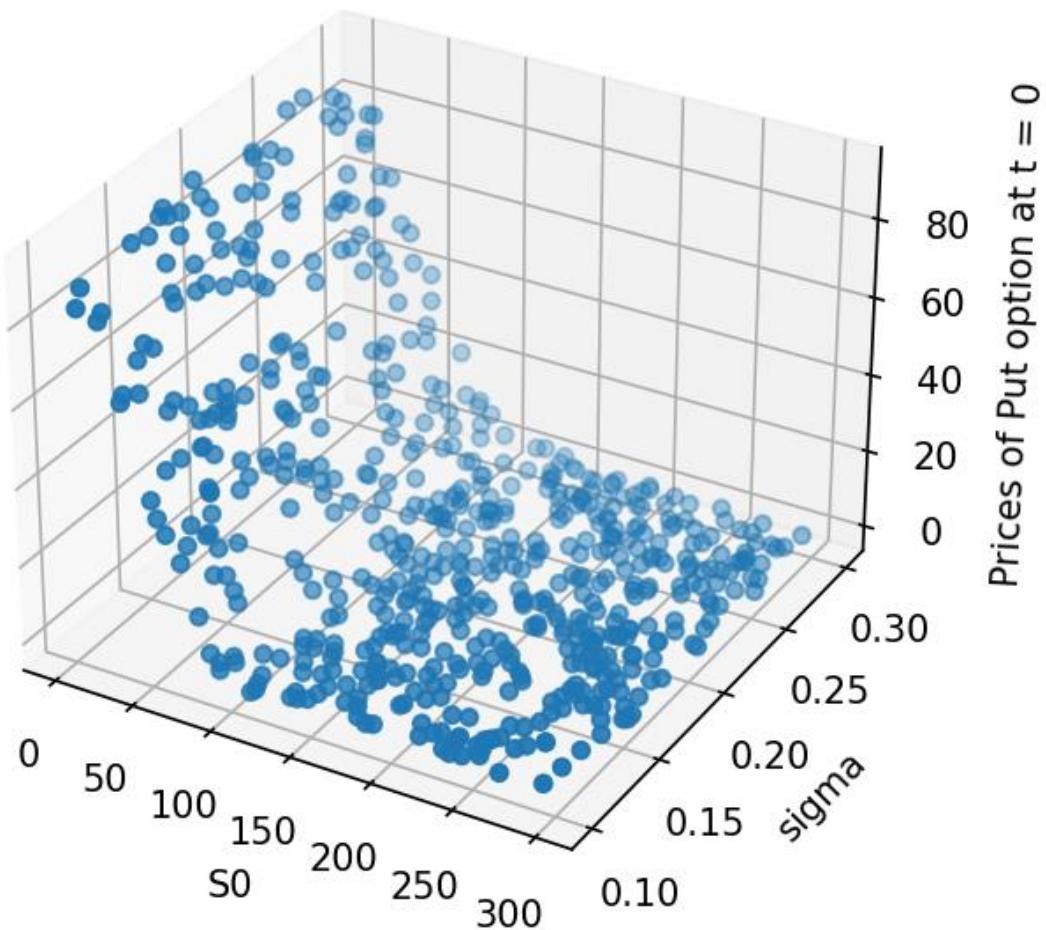
Initial Put Option Price vs S0 and sigma for the set = 1



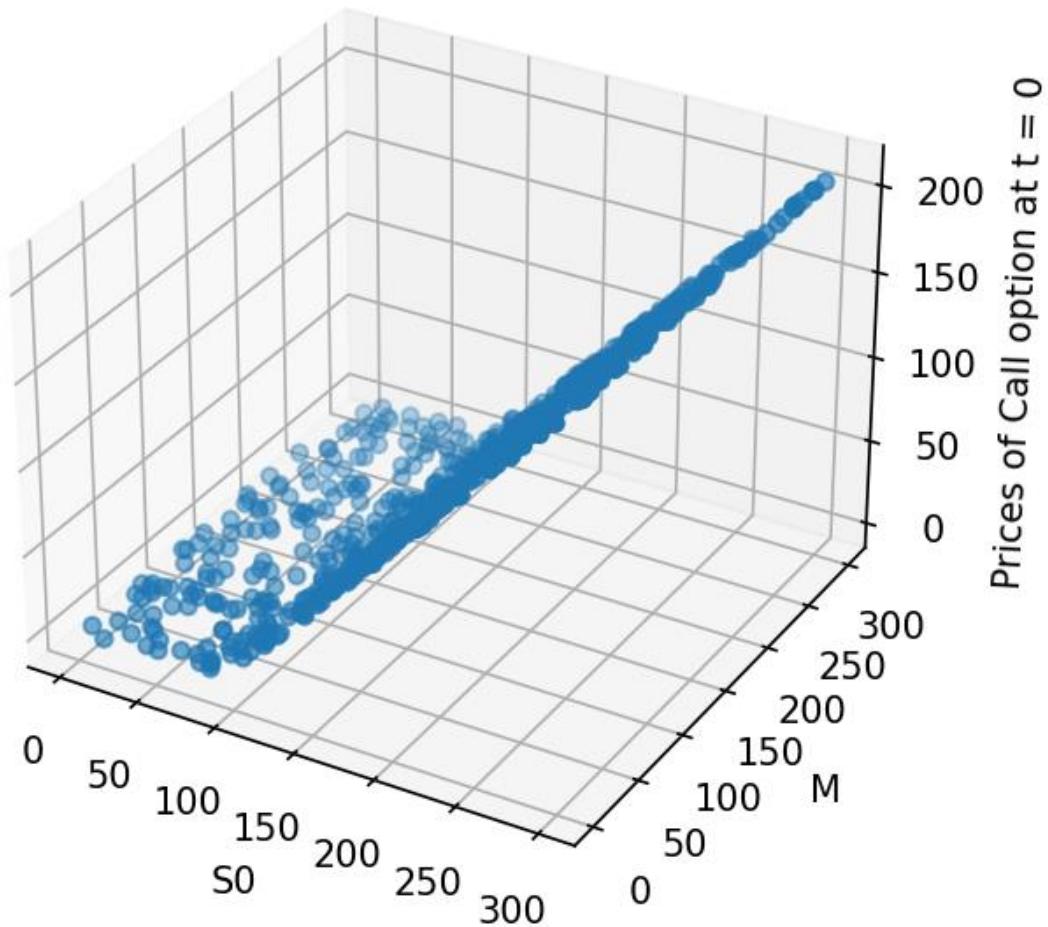
Initial Call Option Price vs S0 and sigma for the set = 2



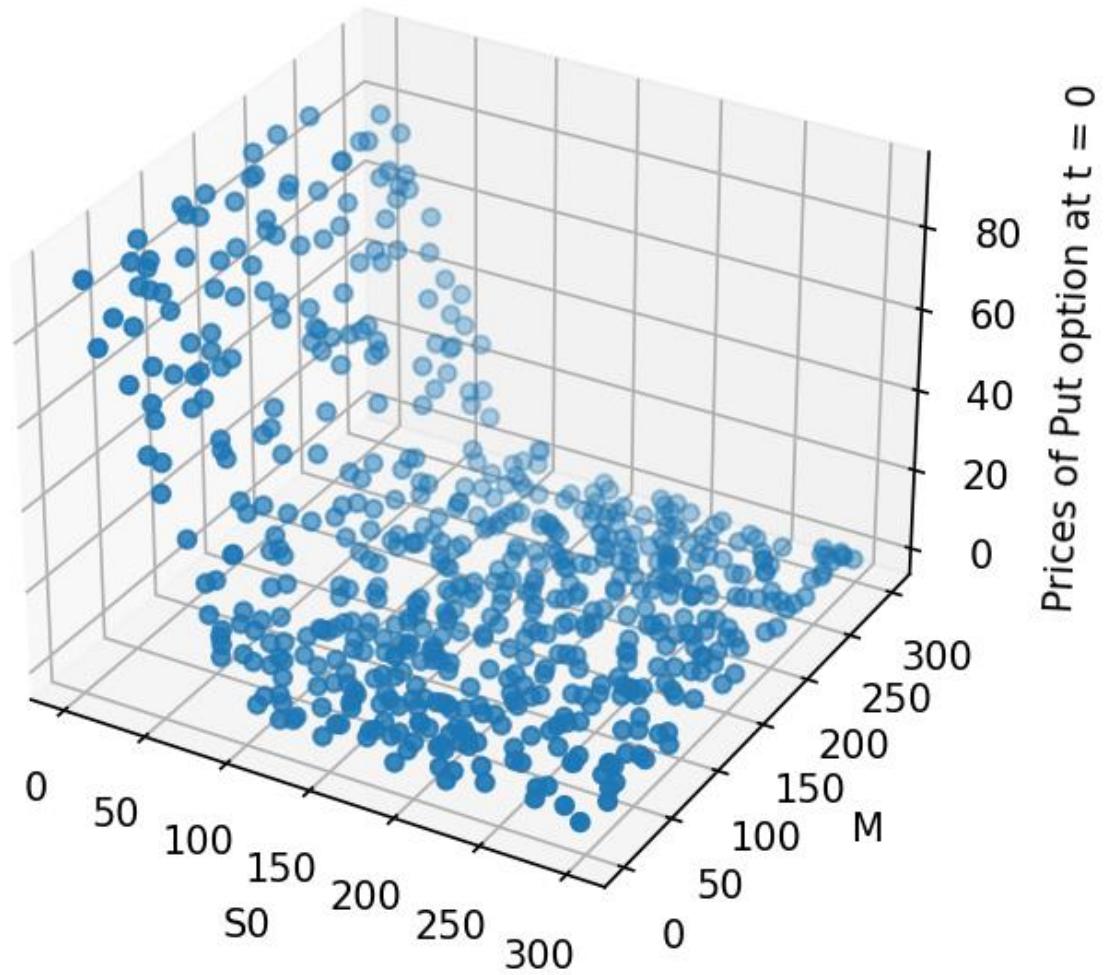
Initial Put Option Price vs S0 and sigma for the set = 2



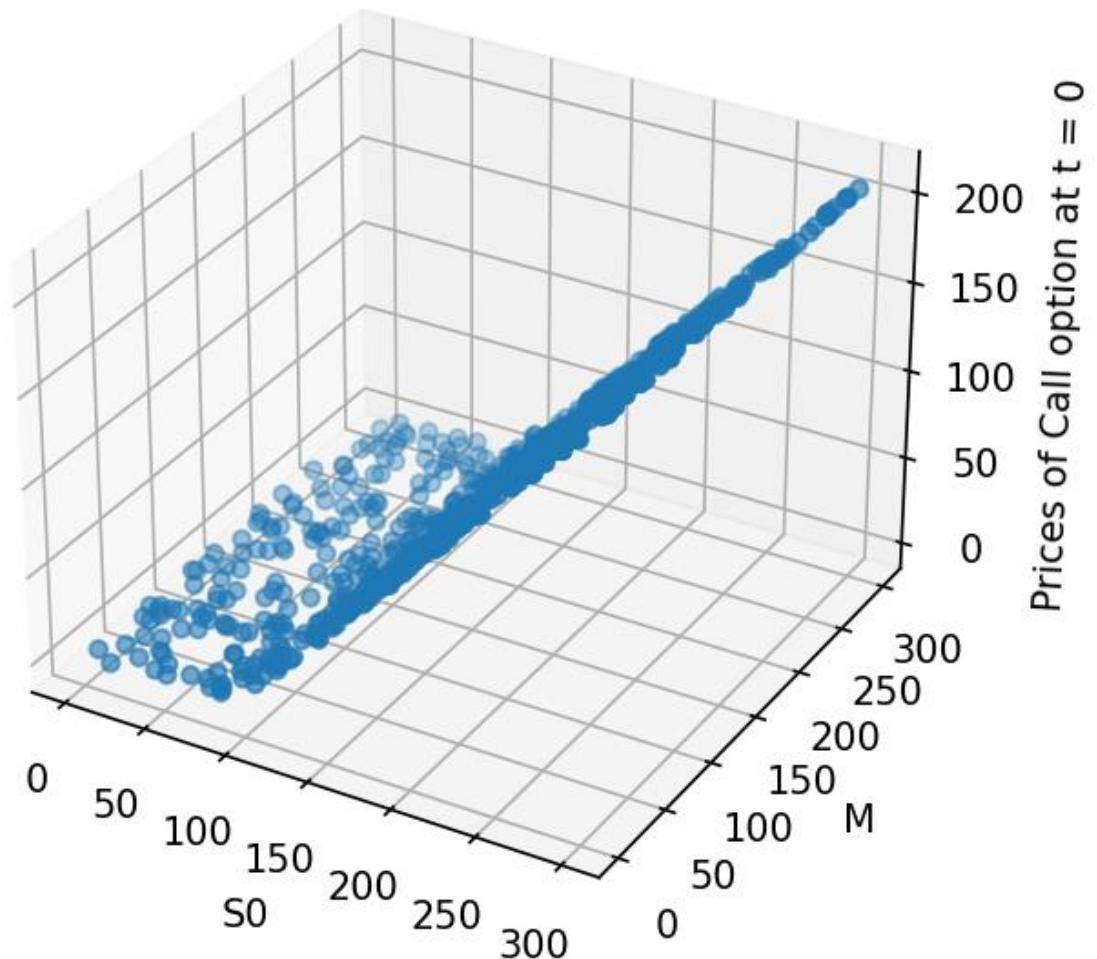
Initial Call Option Price vs S0 and M for the set = 1



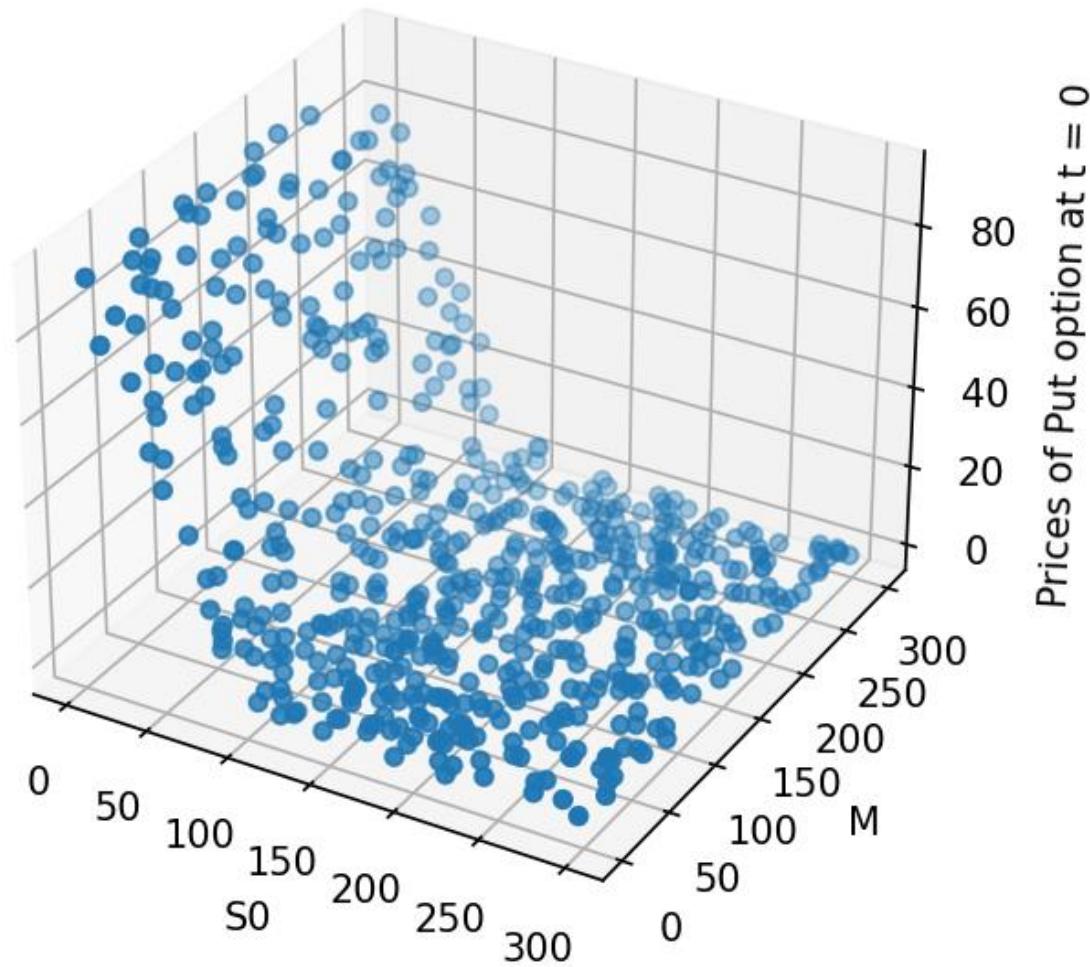
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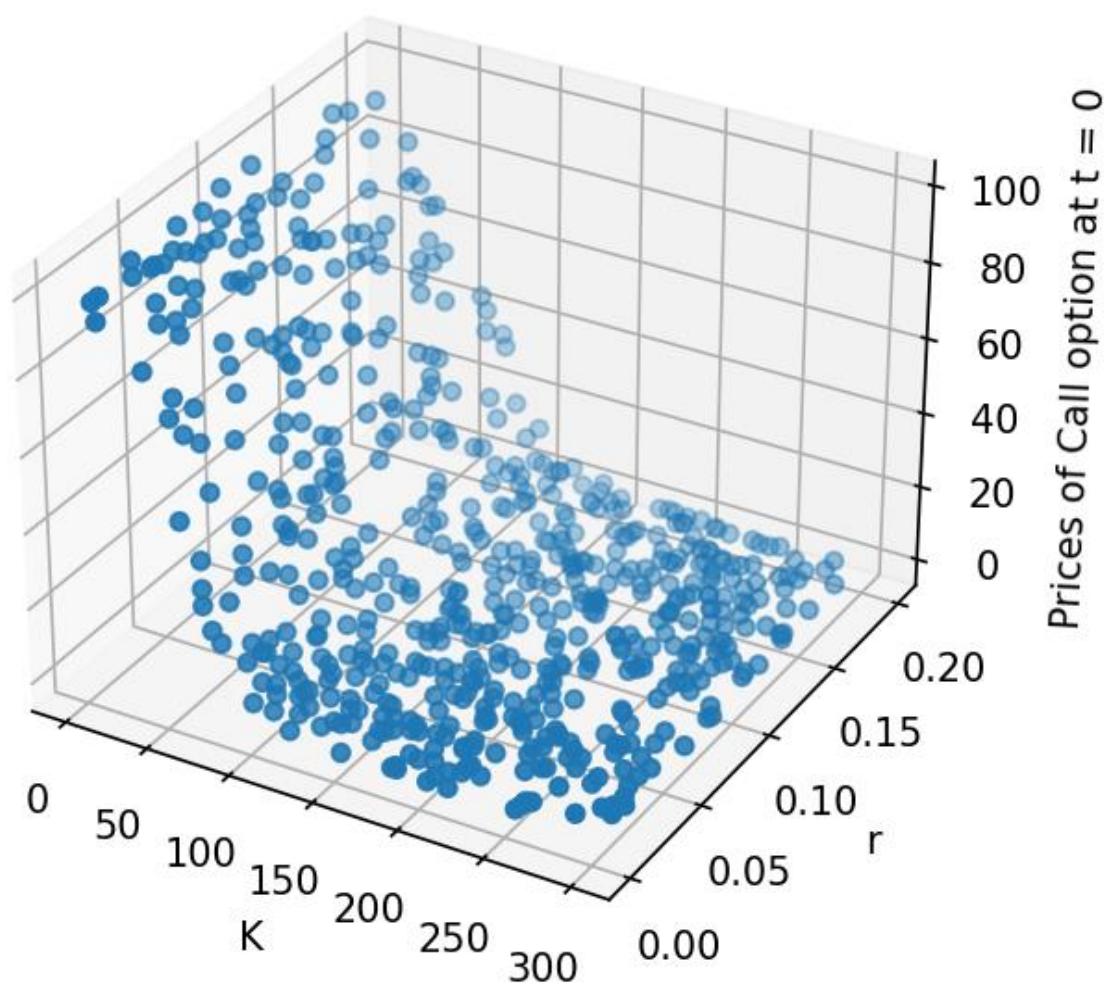
Initial Call Option Price vs S0 and M for the set = 2



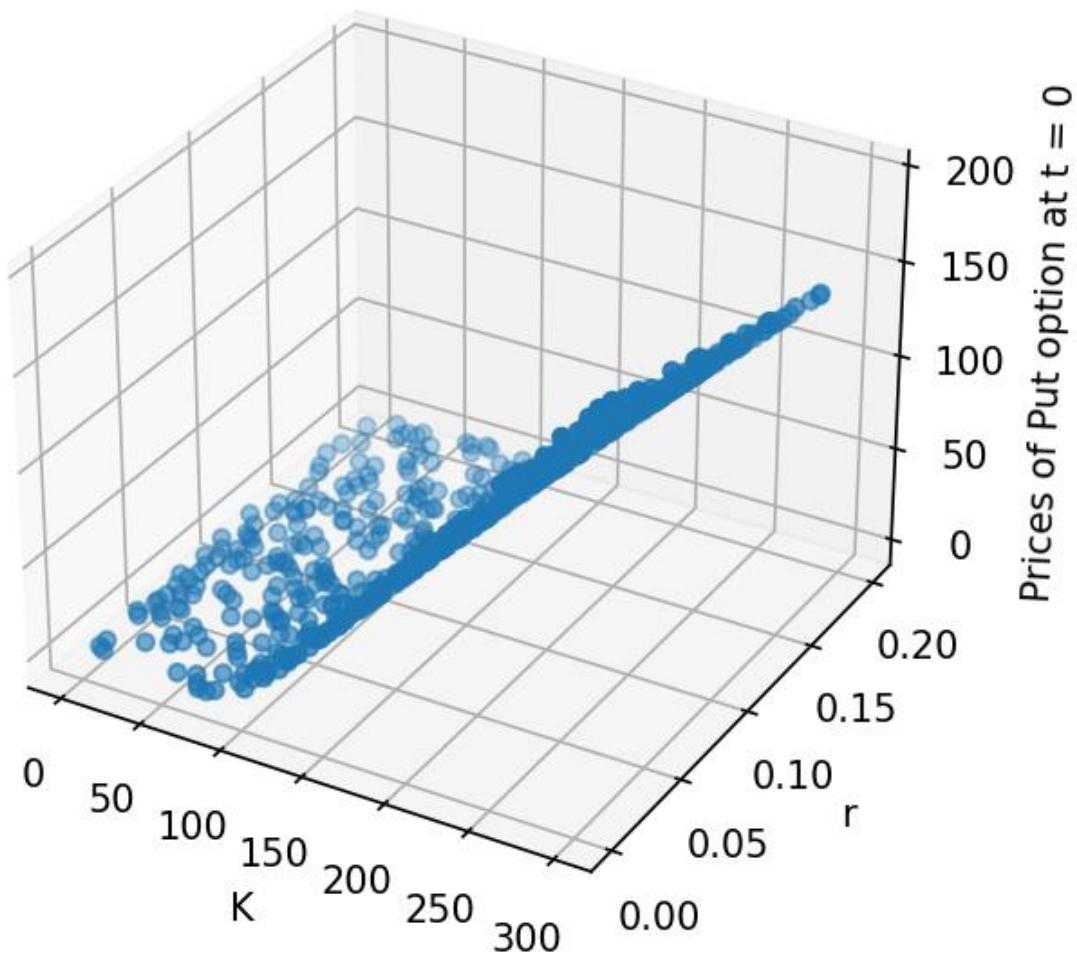
Initial Put Option Price vs S0 and M for the set = 2



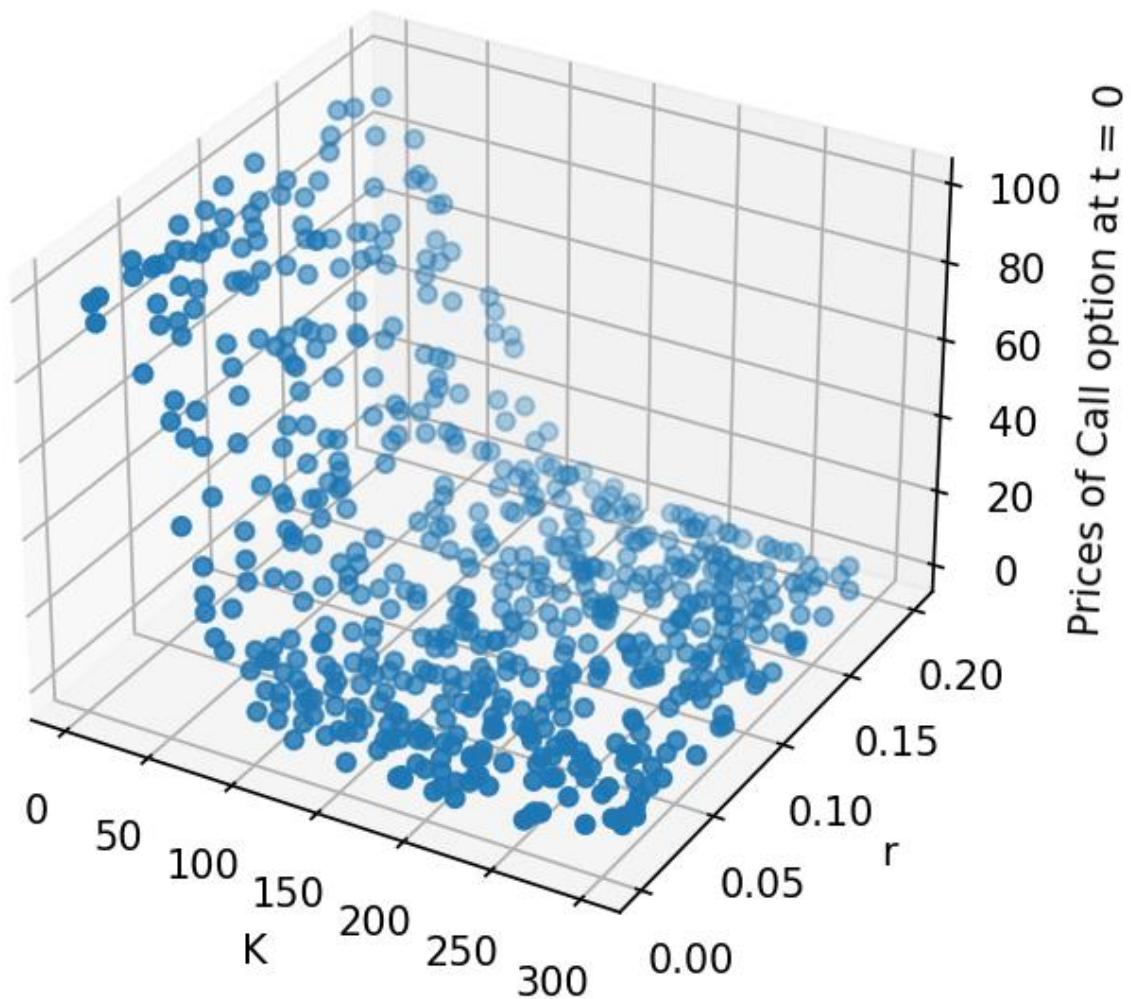
Initial Call Option Price vs K and r for the set = 1



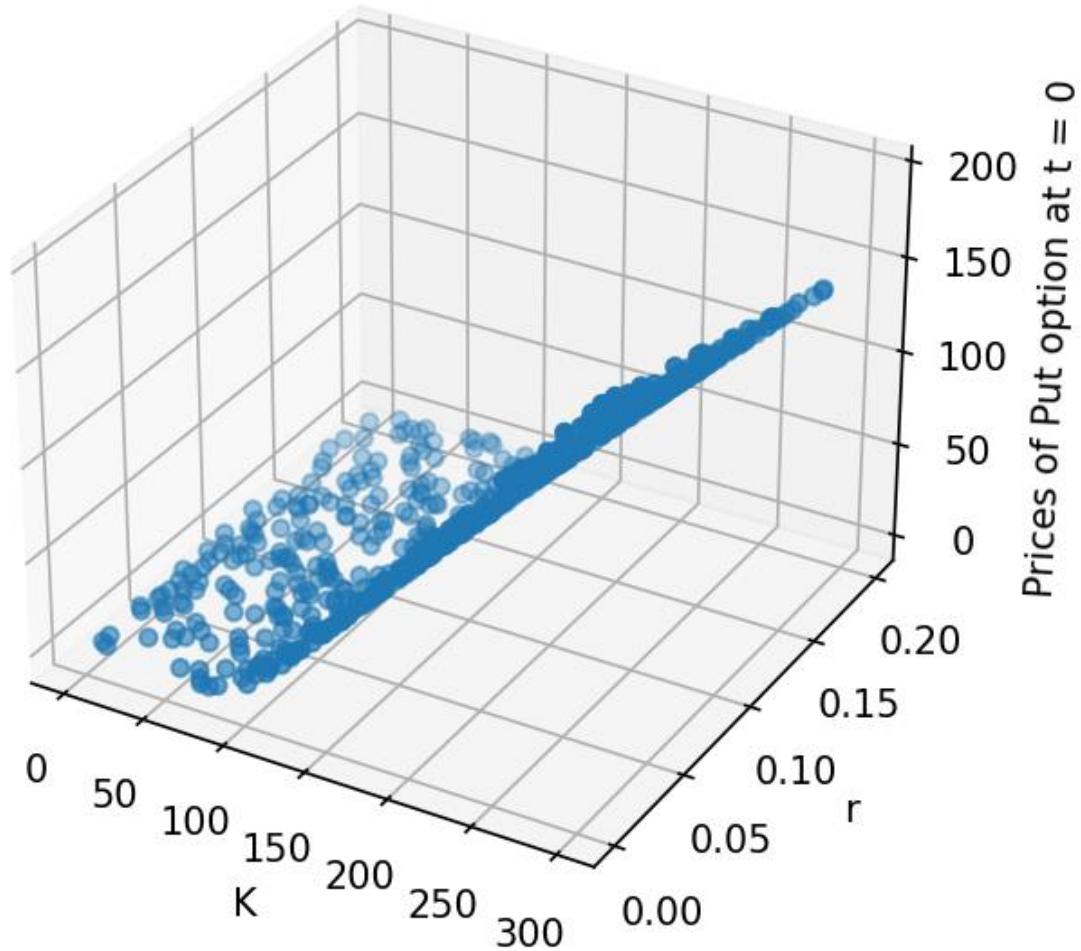
Initial Put Option Price vs K and r for the set = 1



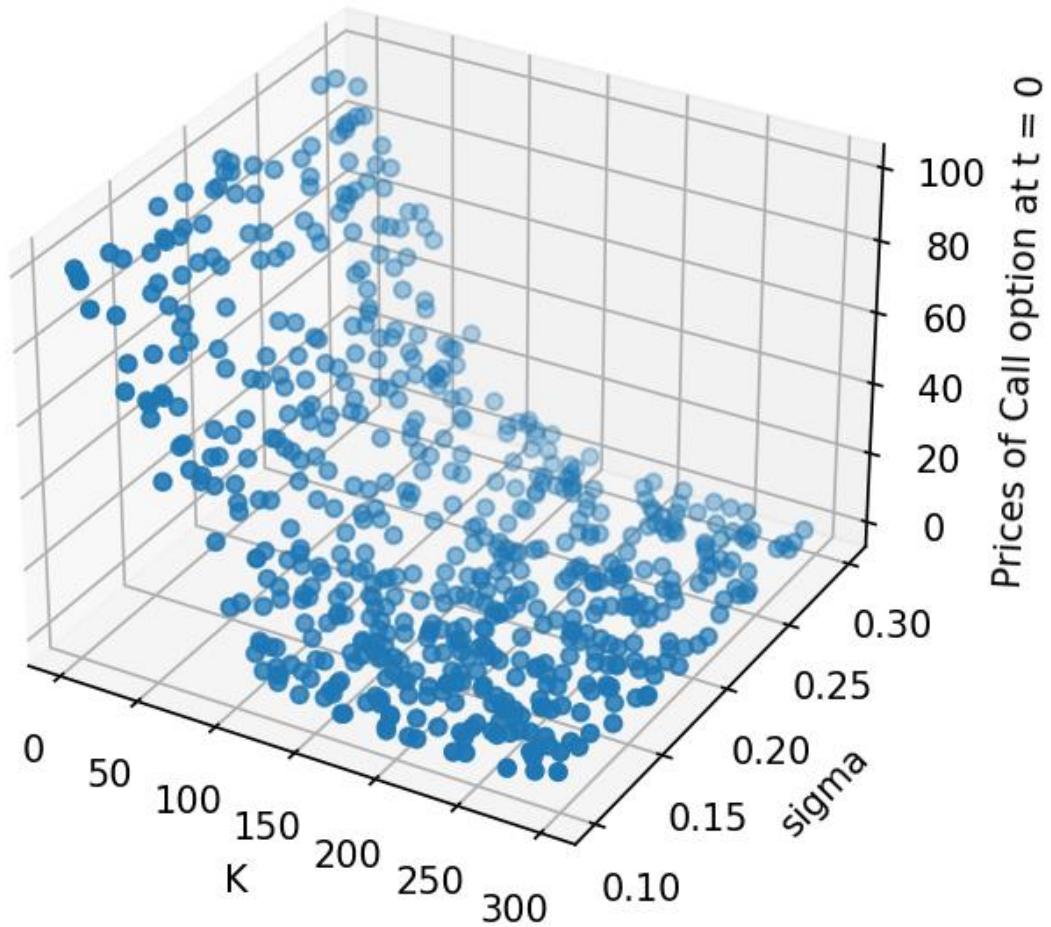
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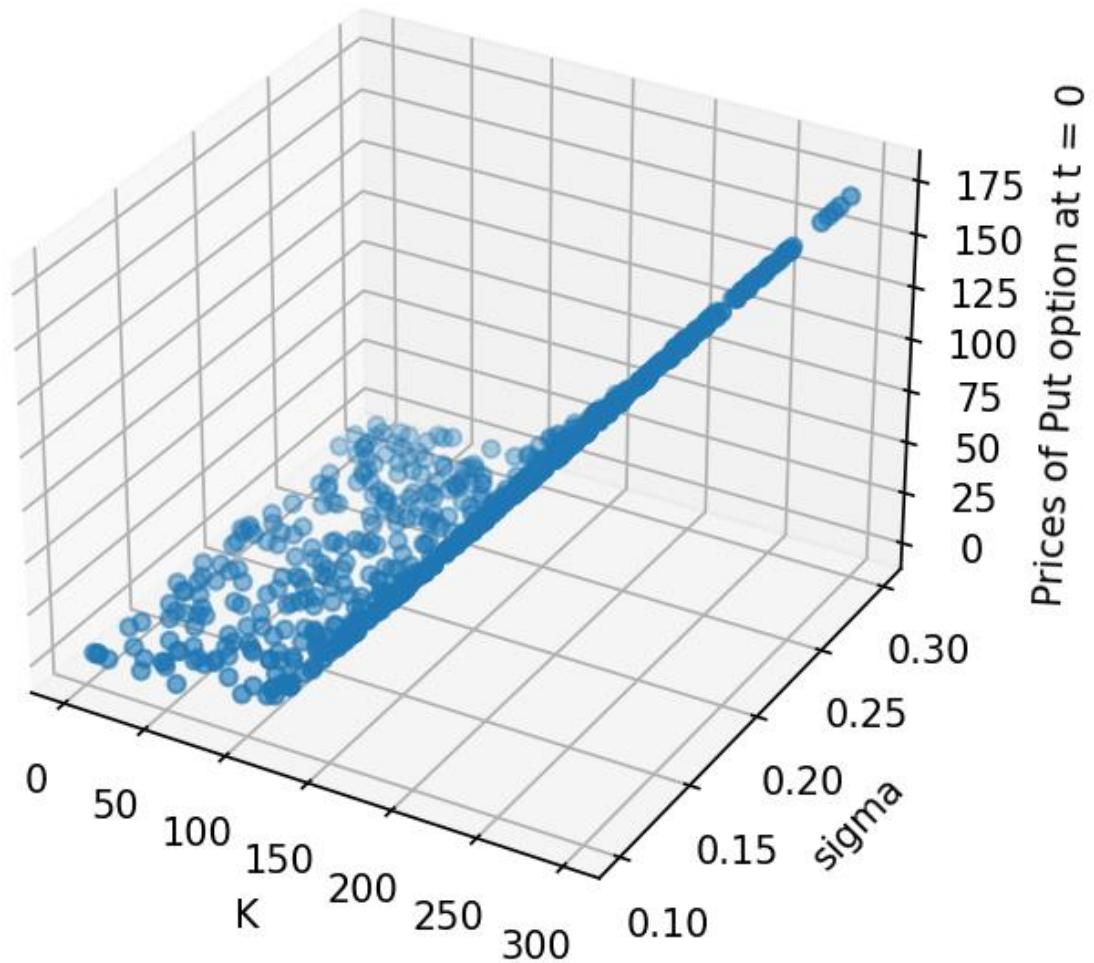
Initial Put Option Price vs K and r for the set = 2



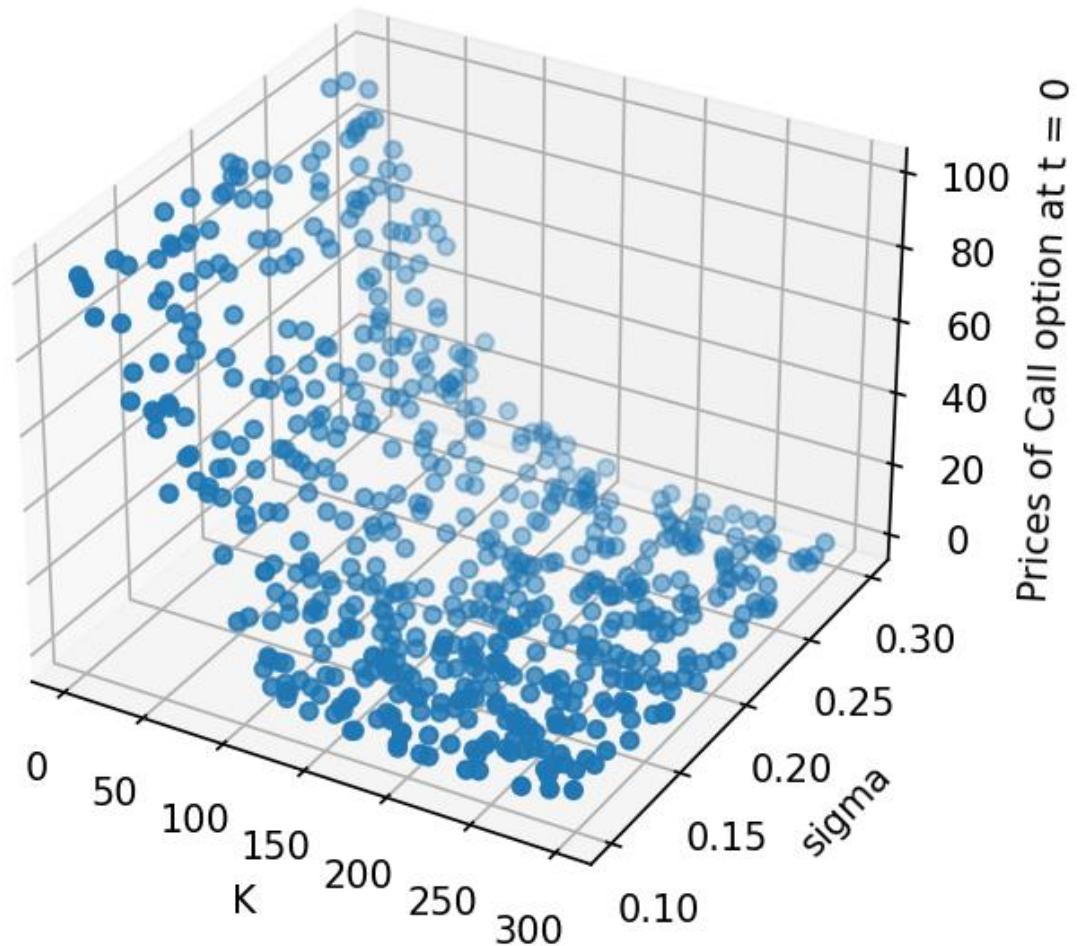
Initial Call Option Price vs K and sigma for the set = 1



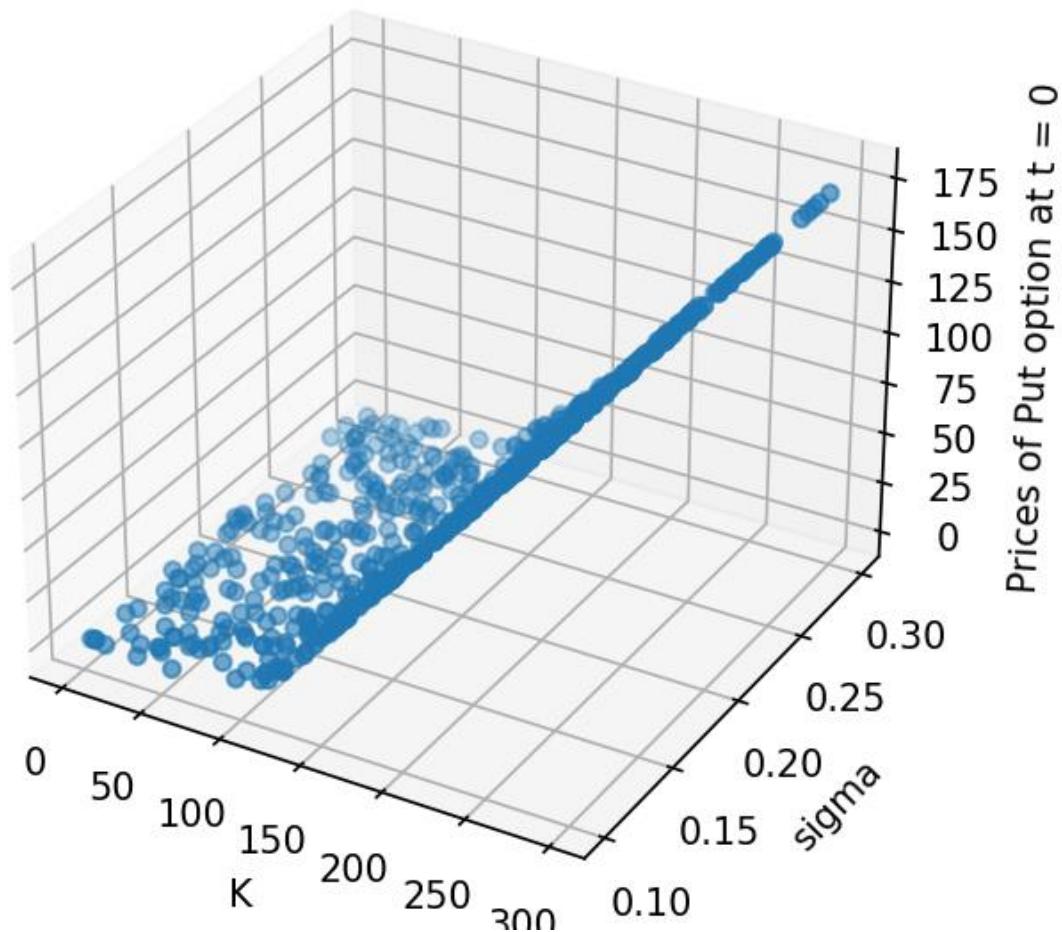
Initial Put Option Price vs K and sigma for the set = 1



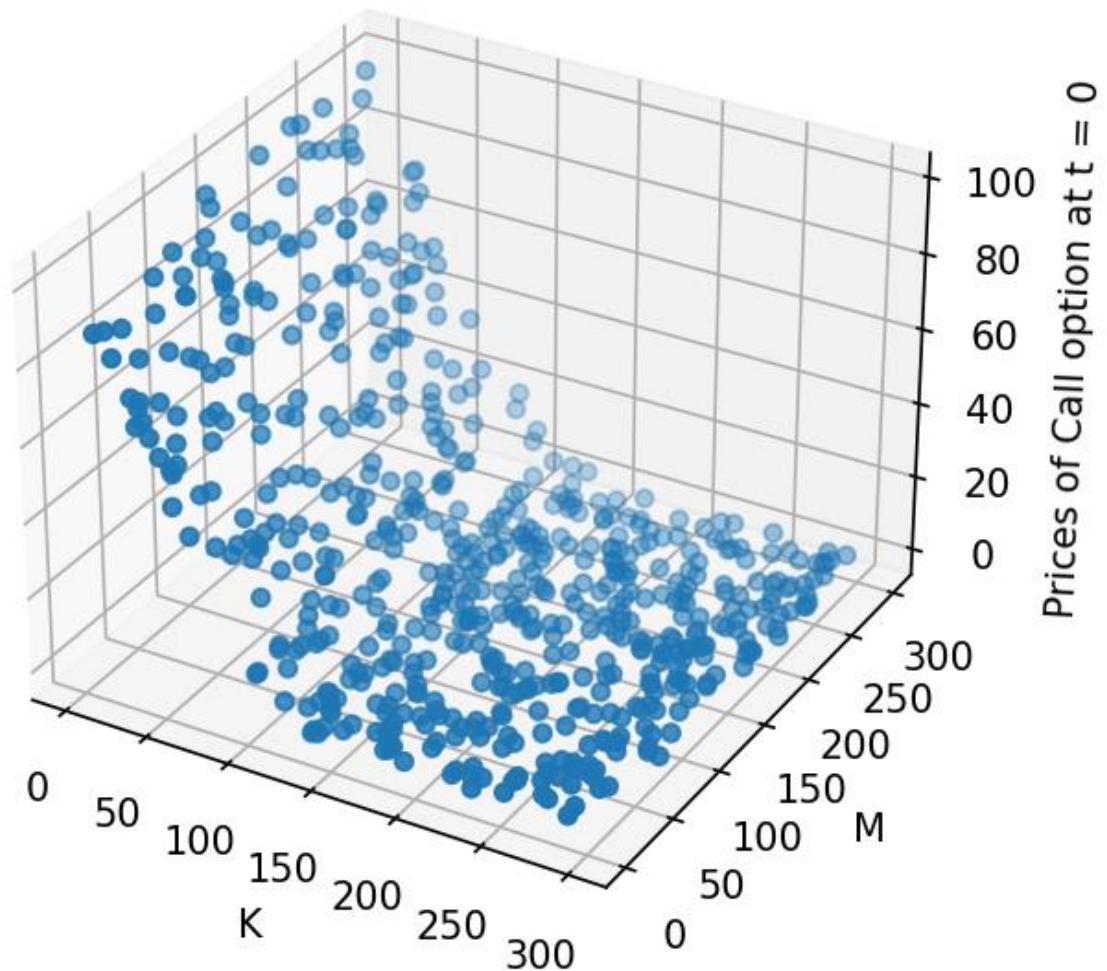
Initial Call Option Price vs K and sigma for the set = 2



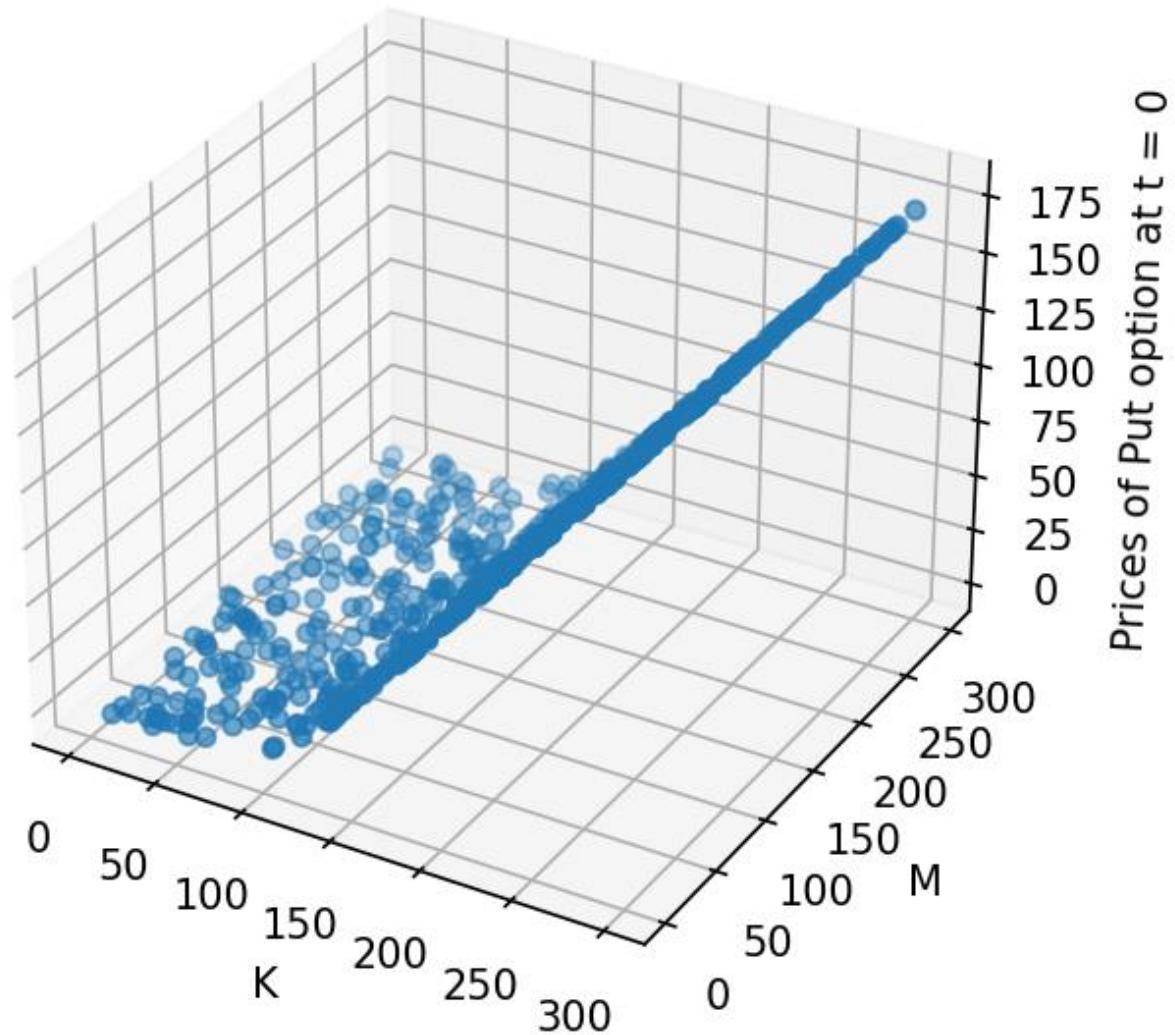
Initial Put Option Price vs K and sigma for the set = 2



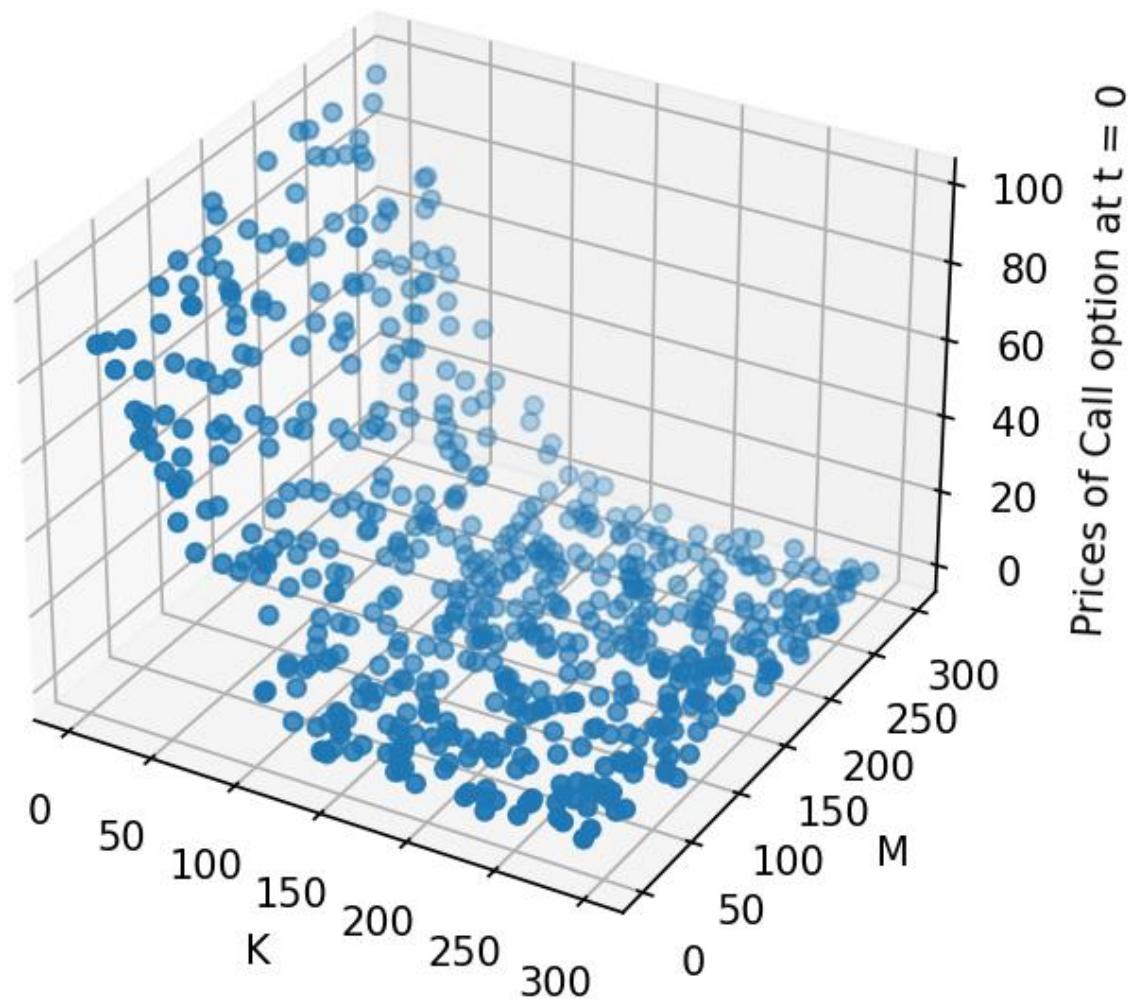
Initial Call Option Price vs K and M for the set = 1



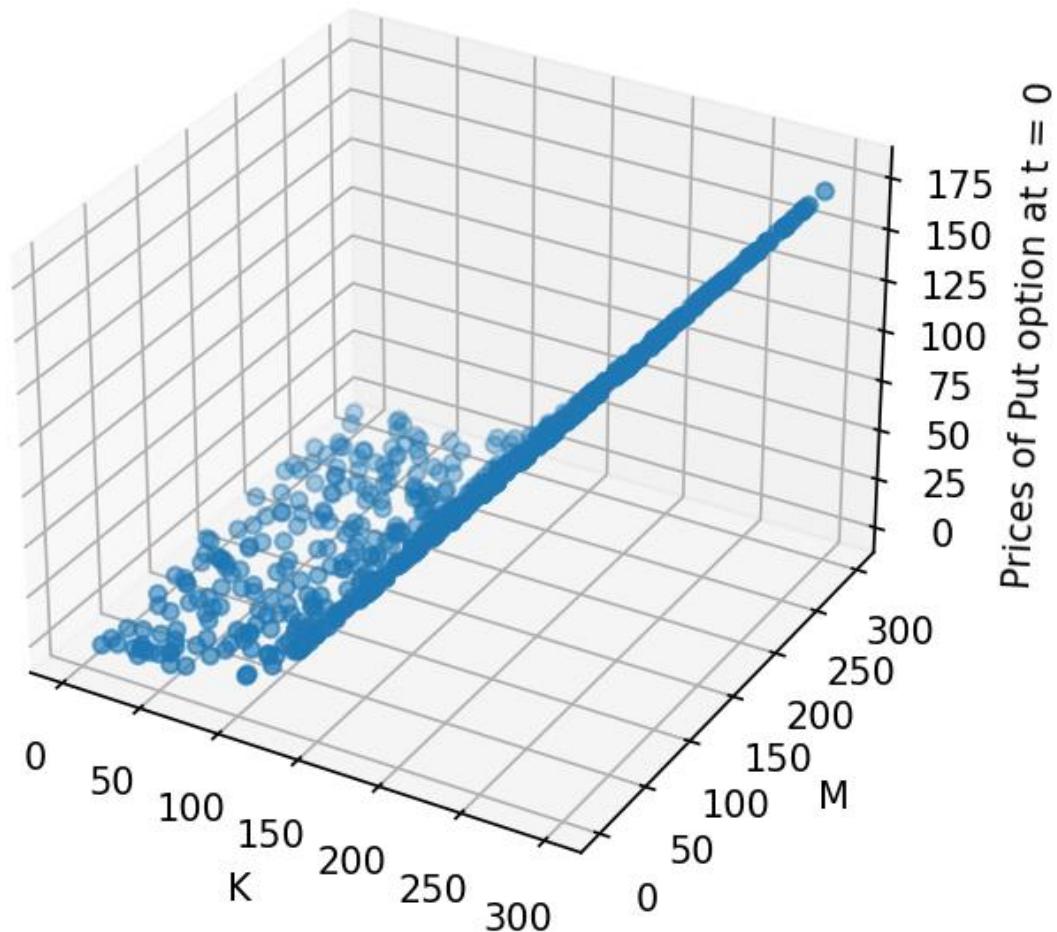
Initial Put Option Price vs K and M for the set = 1



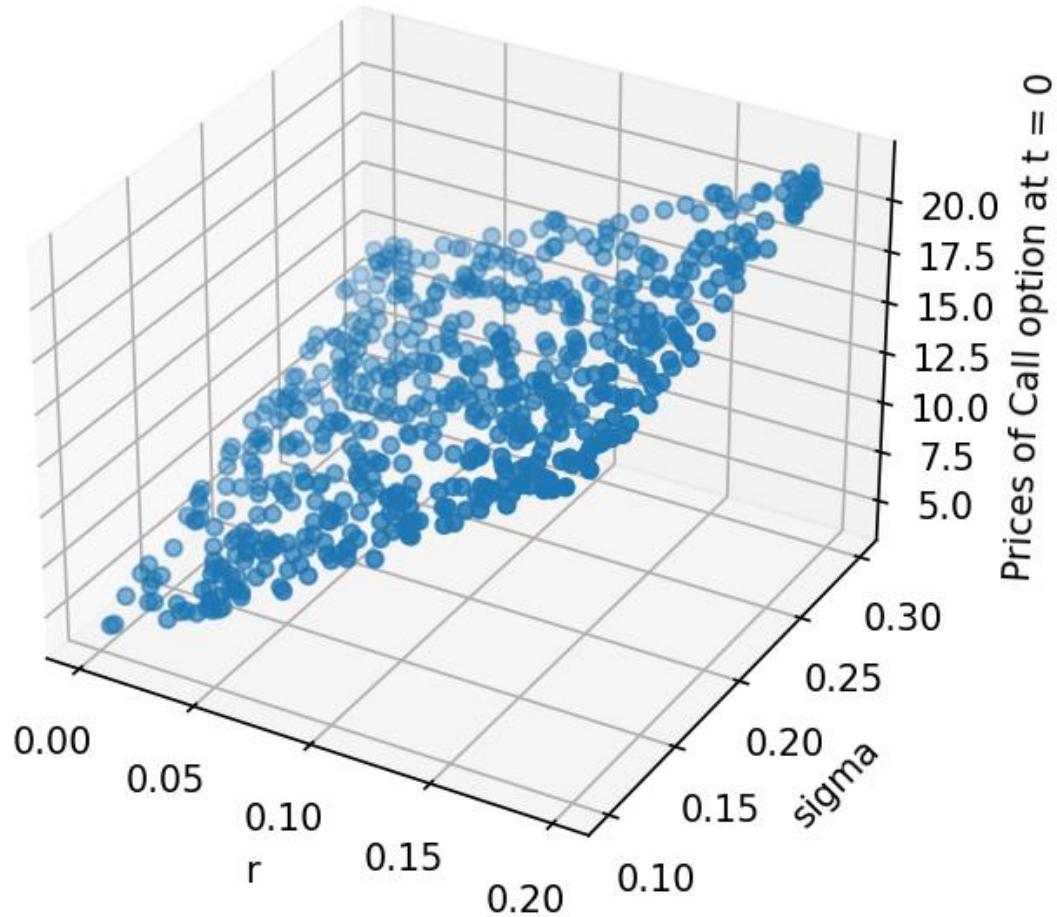
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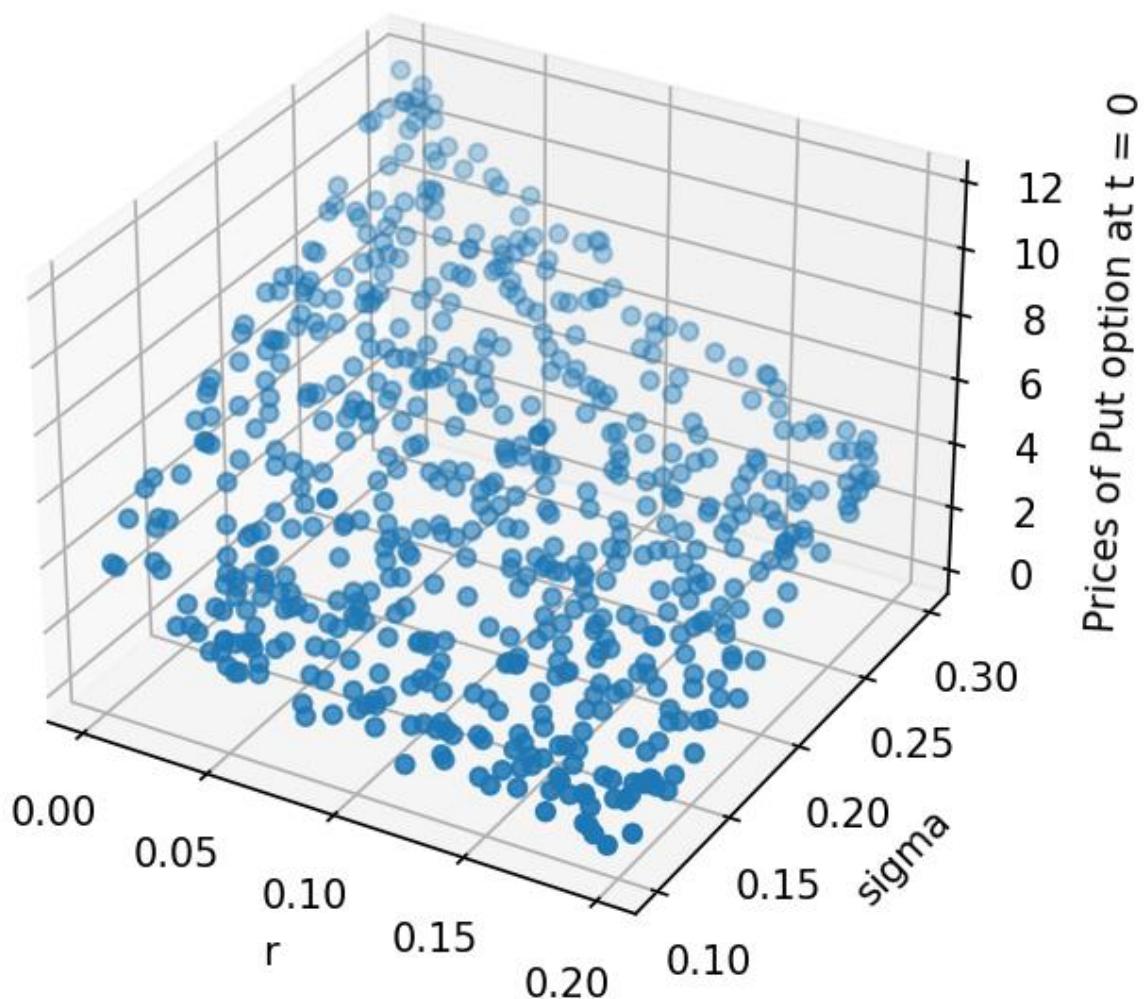
Initial Put Option Price vs K and M for the set = 2



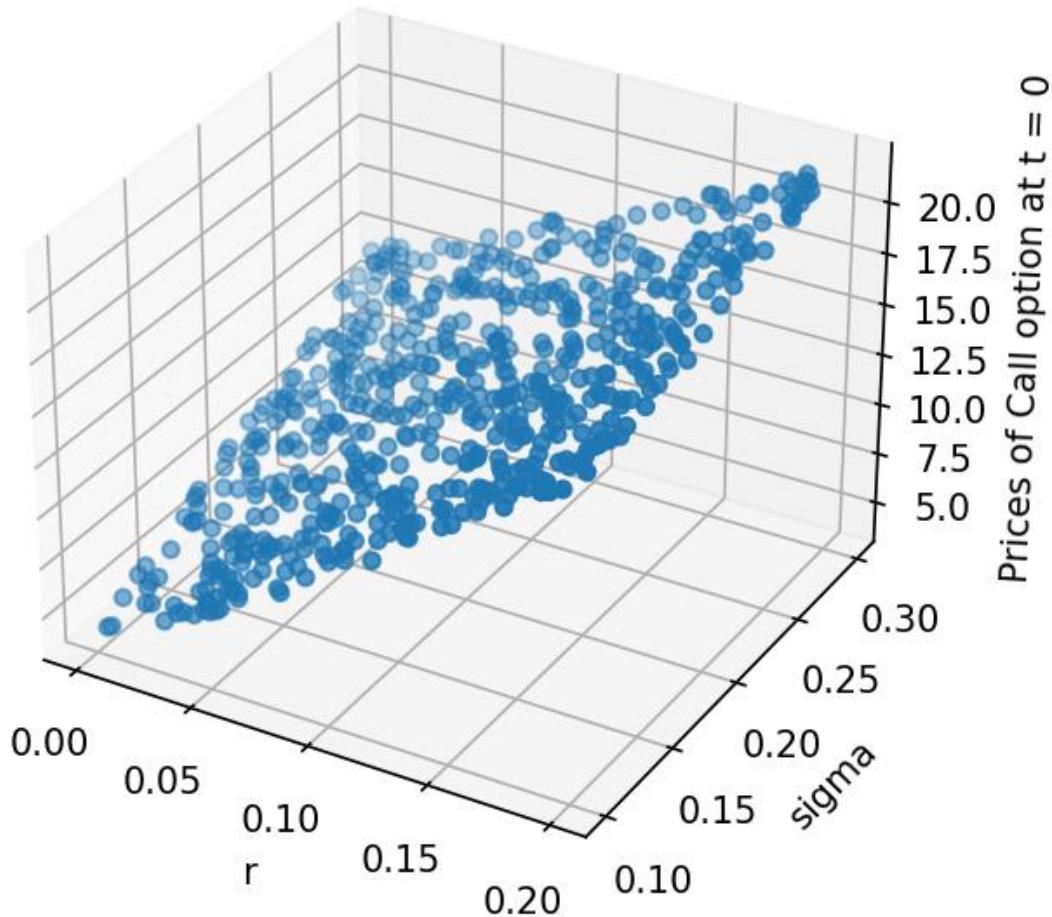
Initial Call Option Price vs r and sigma for the set = 1



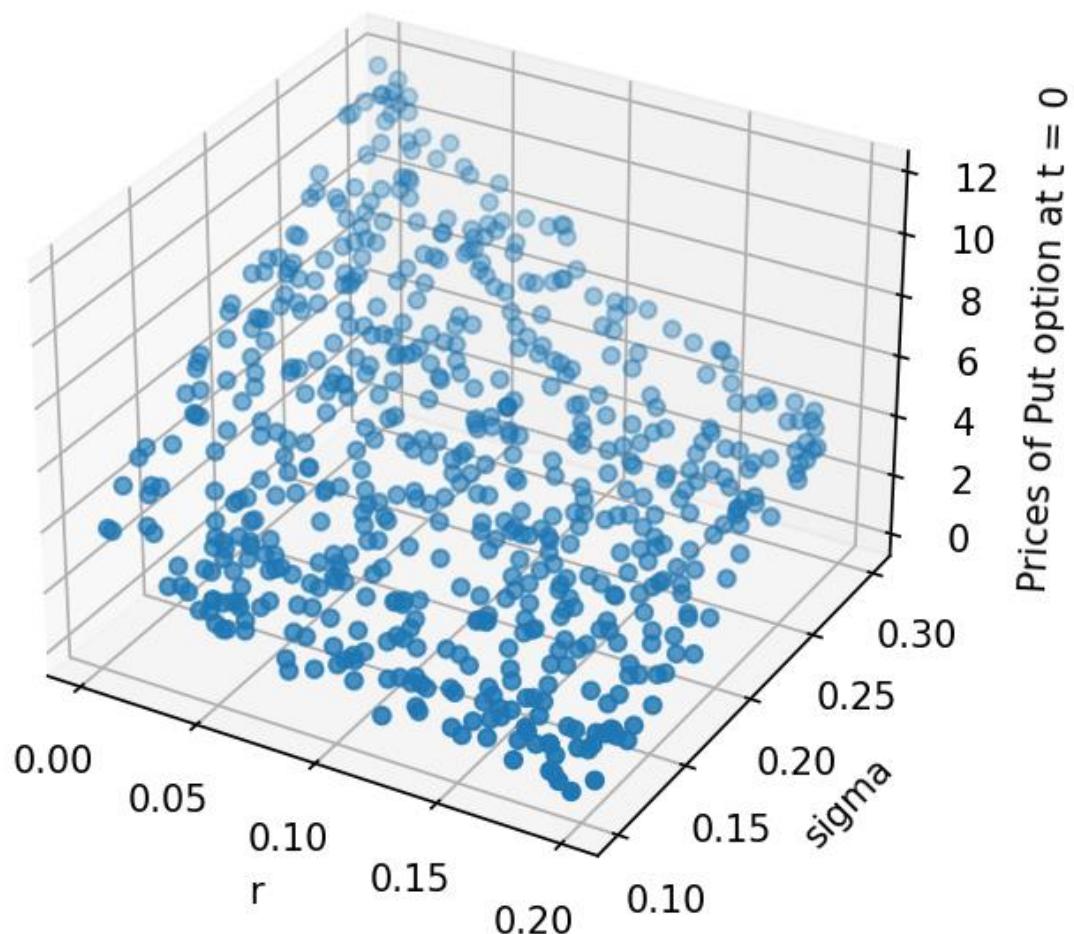
Initial Put Option Price vs r and sigma for the set = 1



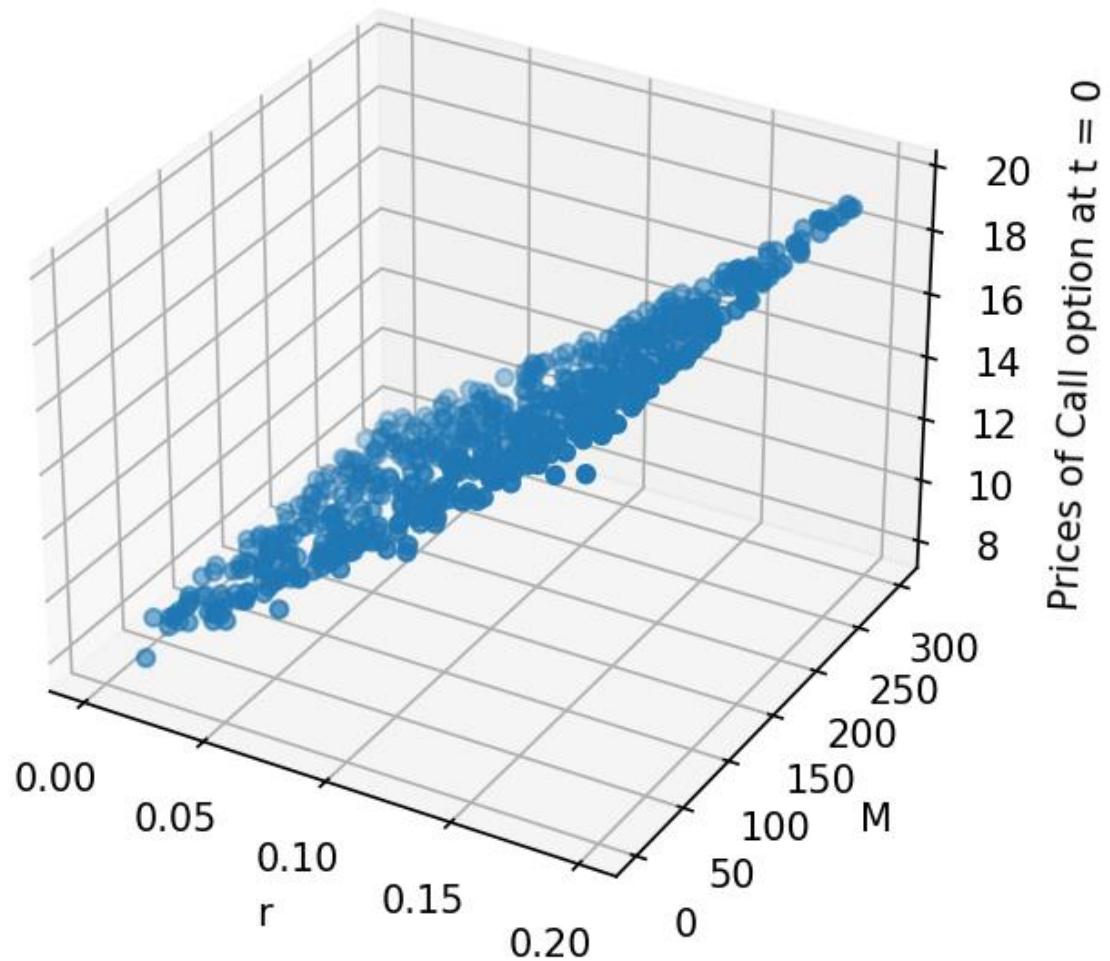
Initial Call Option Price vs r and sigma for the set =2



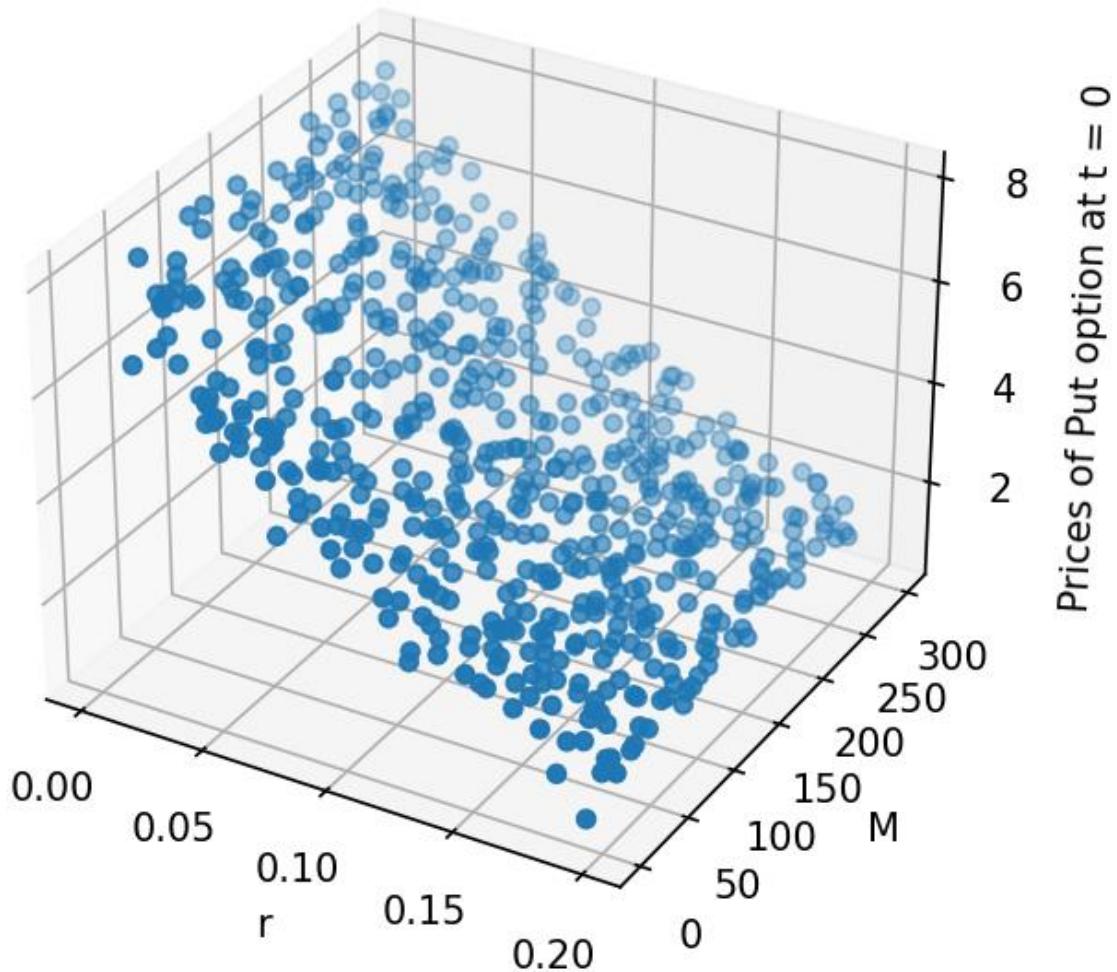
Initial Put Option Price vs r and sigma for the set = 2



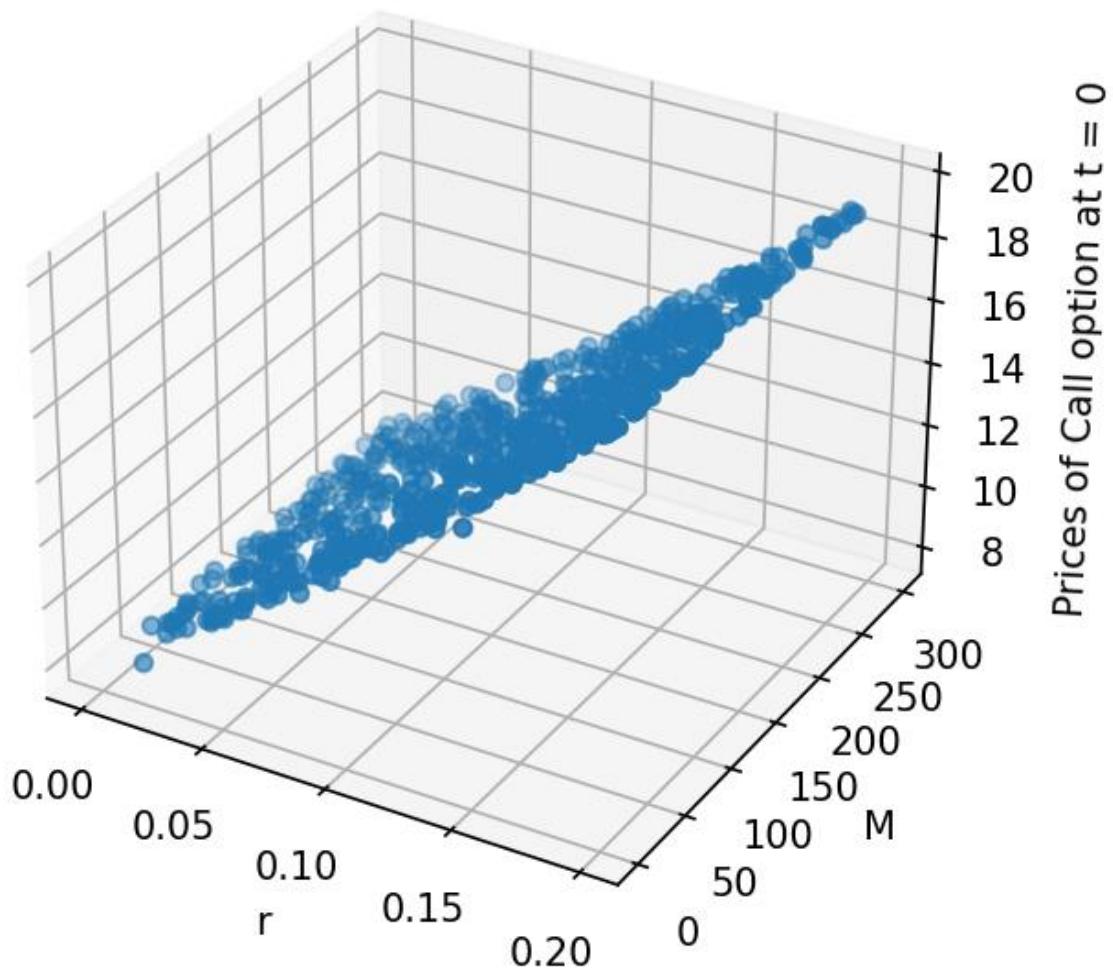
Initial Call Option Price vs r and M for the set = 1



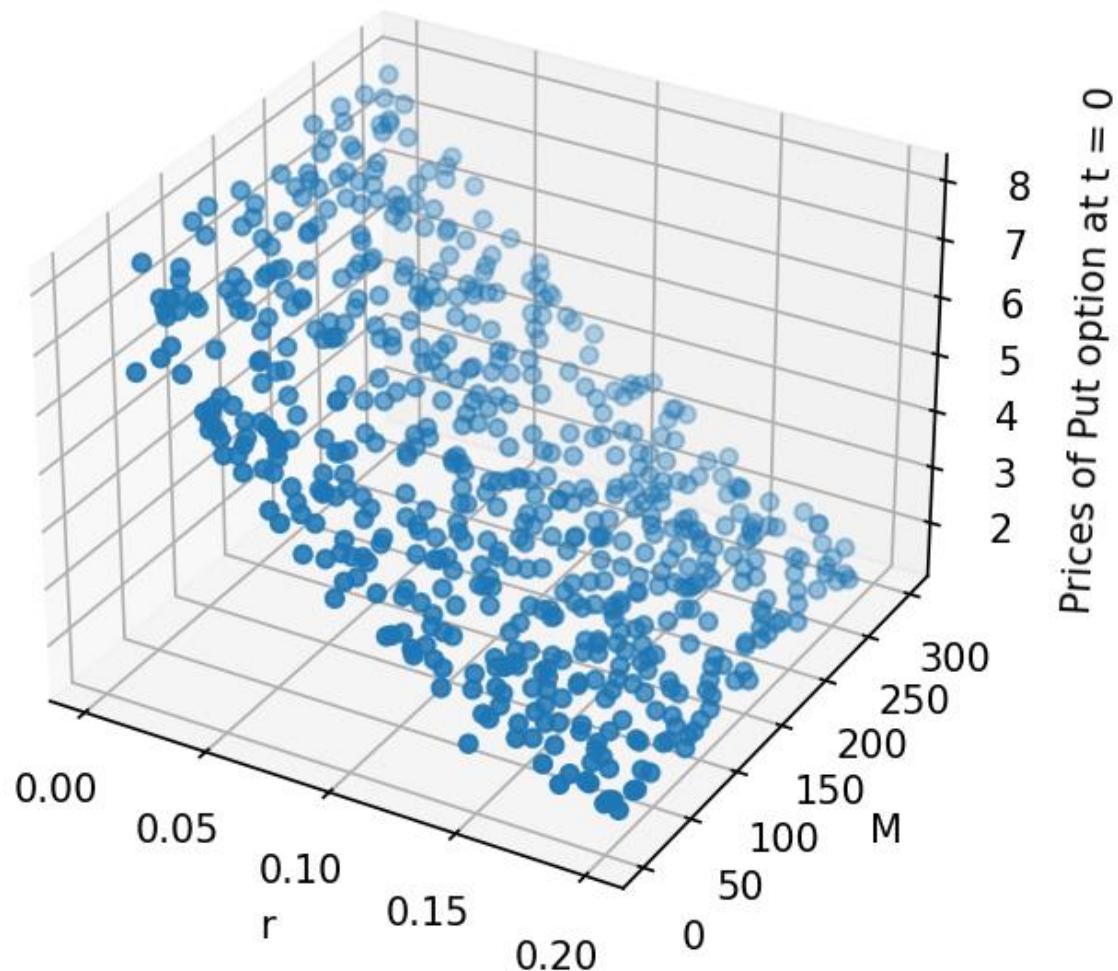
Initial Put Option Price vs r and M for the set = 1



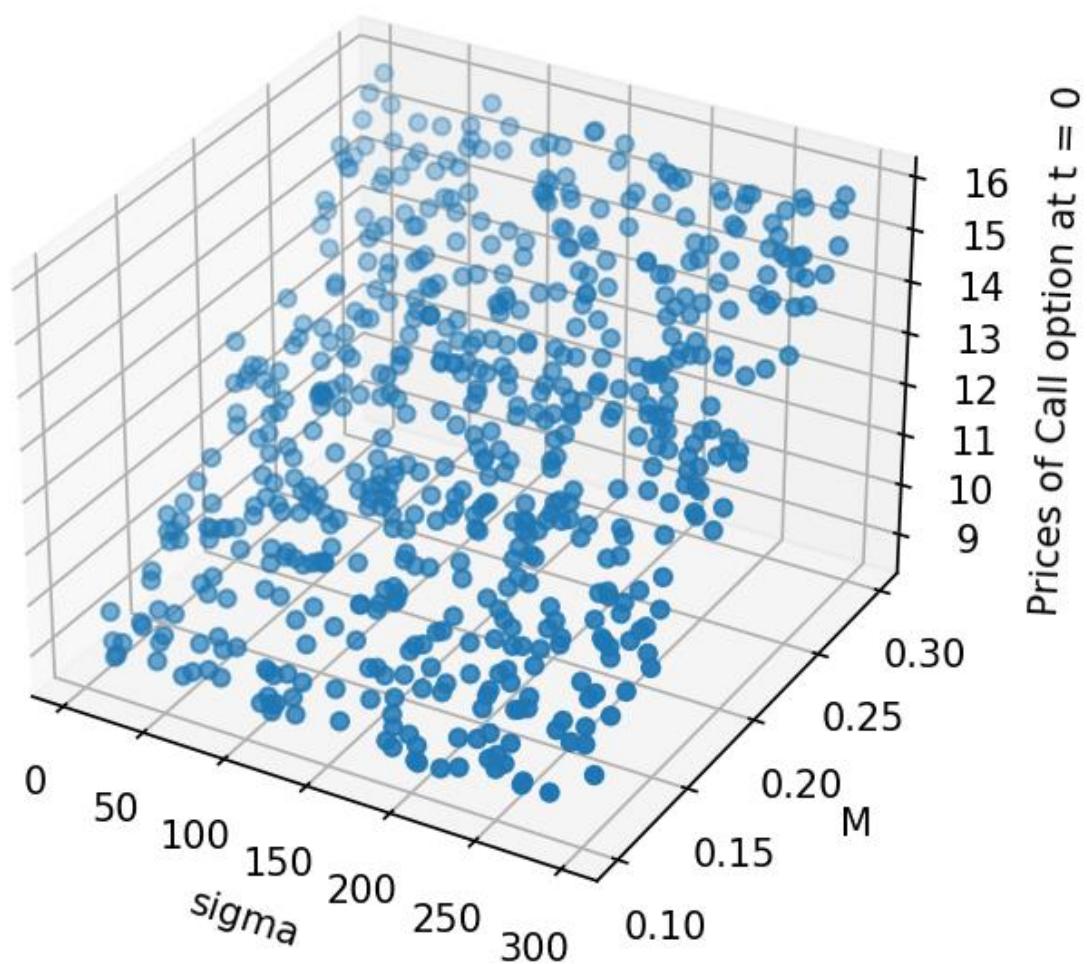
Initial Call Option Price vs r and M for the set = 2



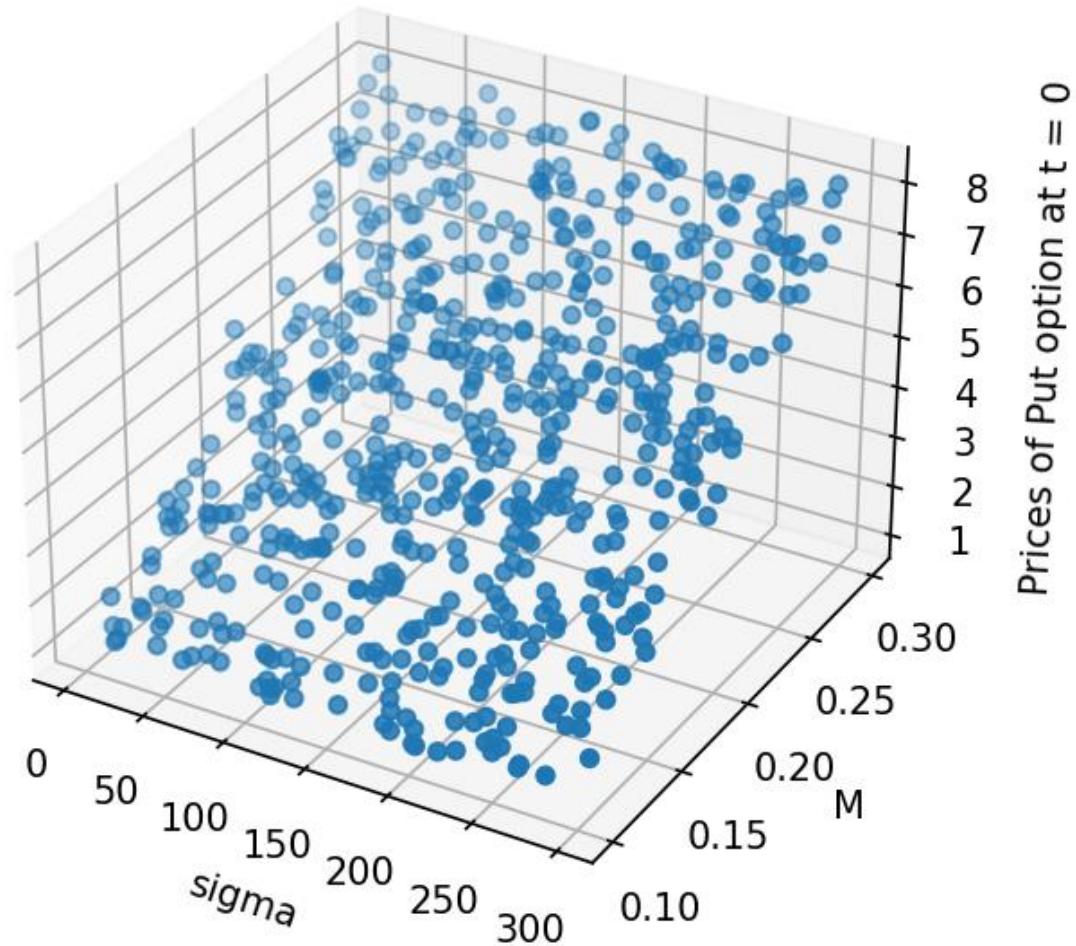
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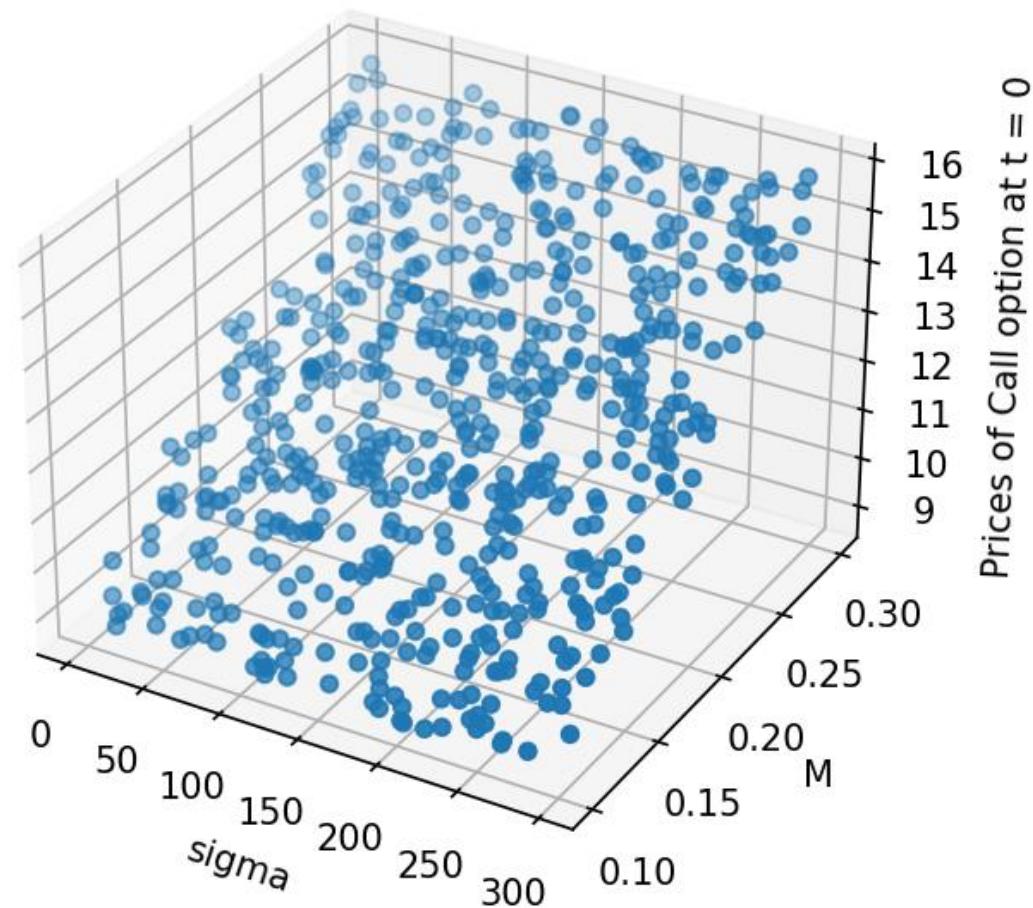
Initial Call Option Price vs sigma and M for the set = 1



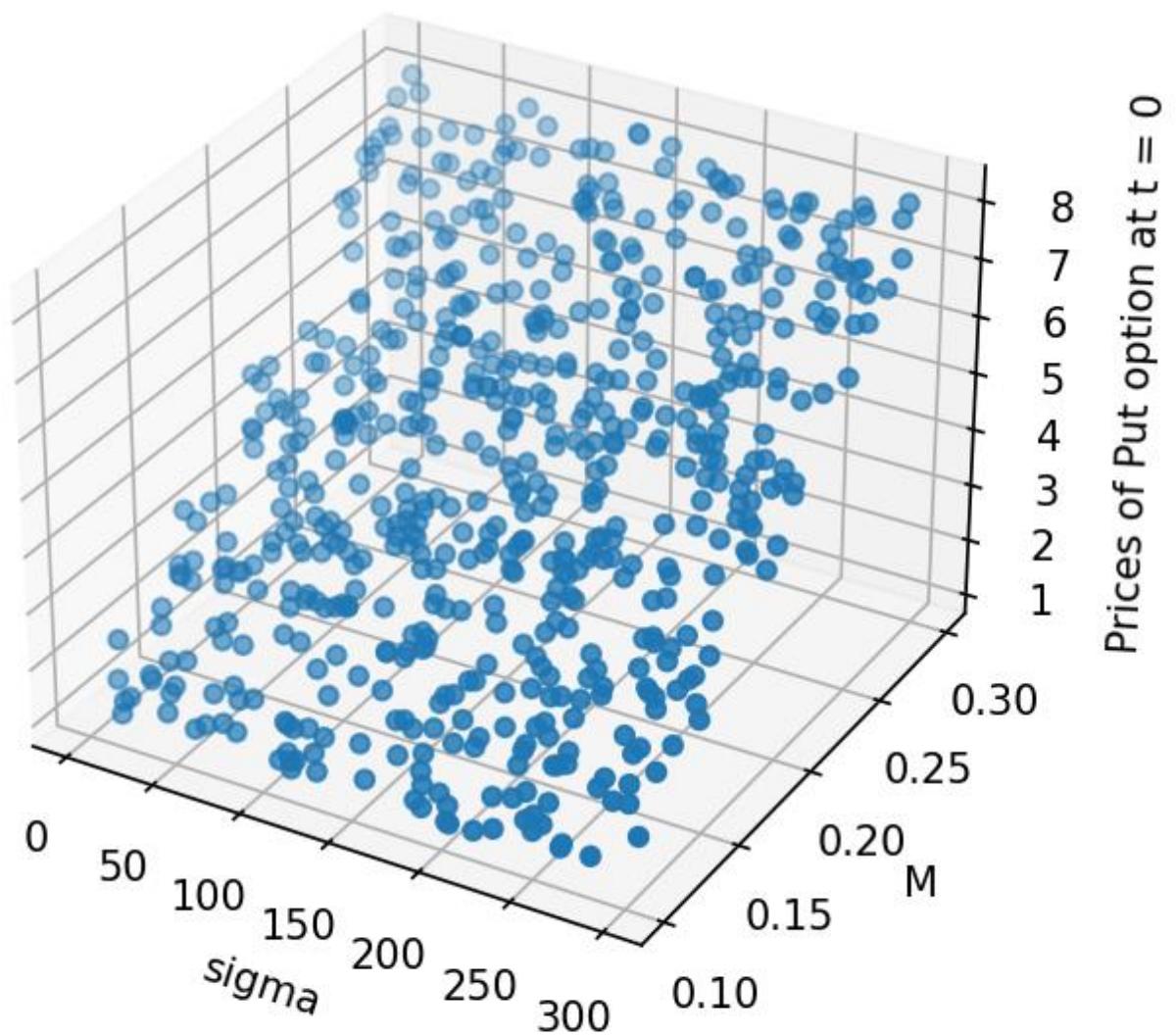
Initial Put Option Price vs sigma and M for the set = 1



Initial Call Option Price vs sigma and M for the set = 2

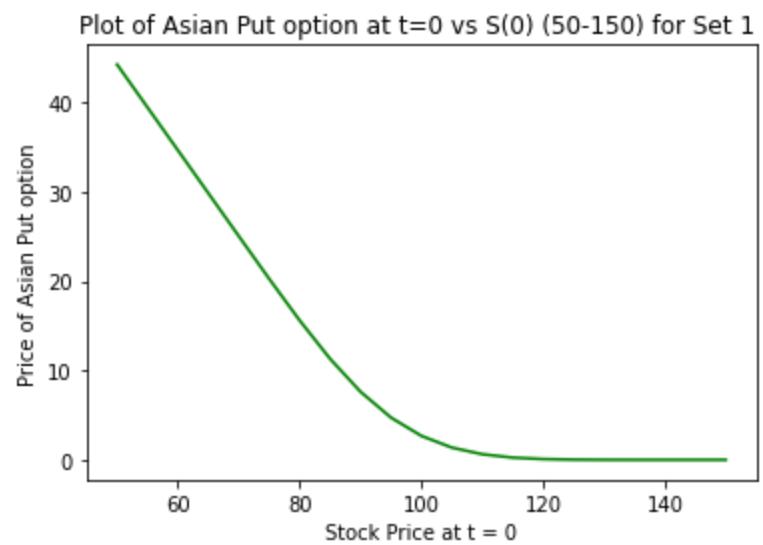
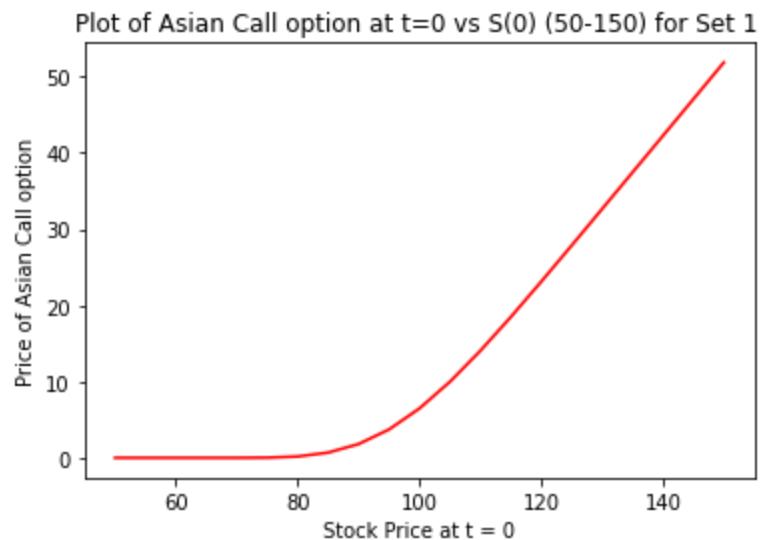


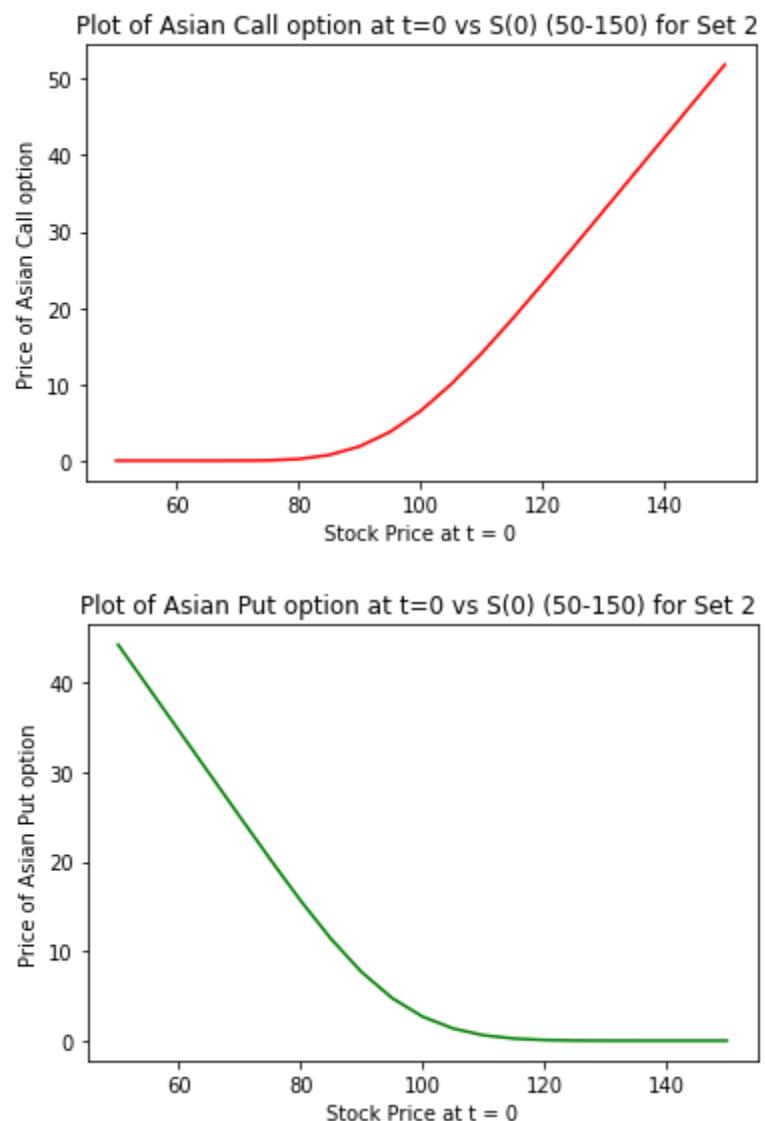
Initial Put Option Price vs sigma and M for the set = 2

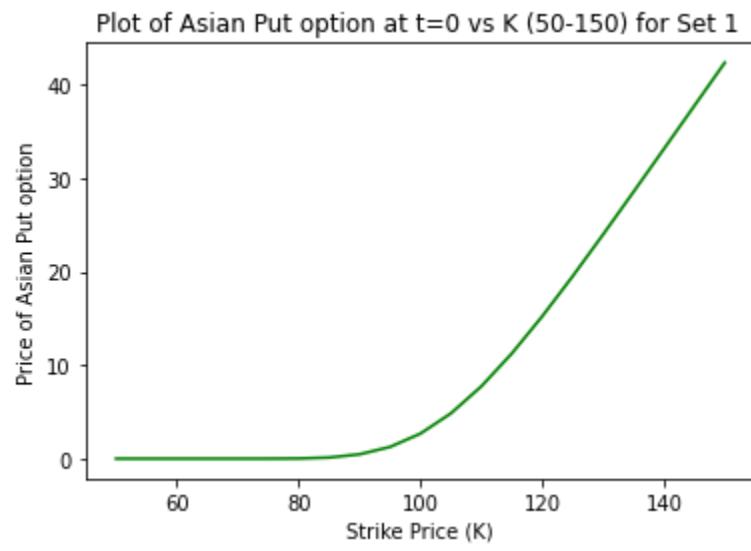
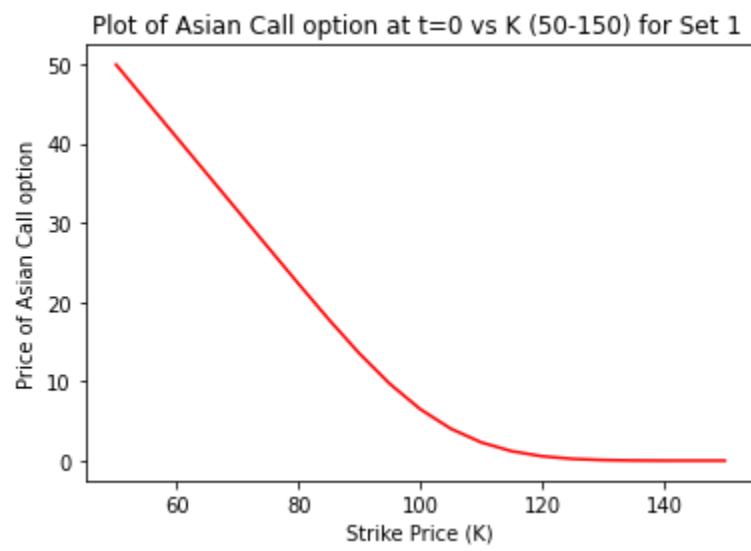


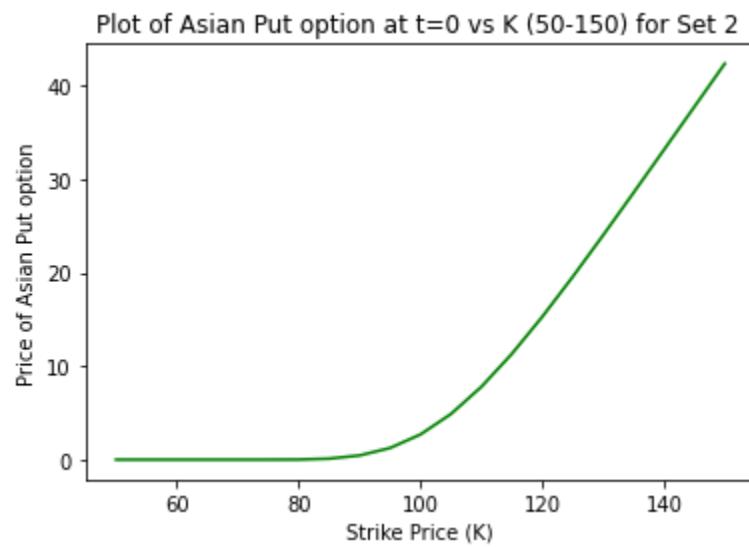
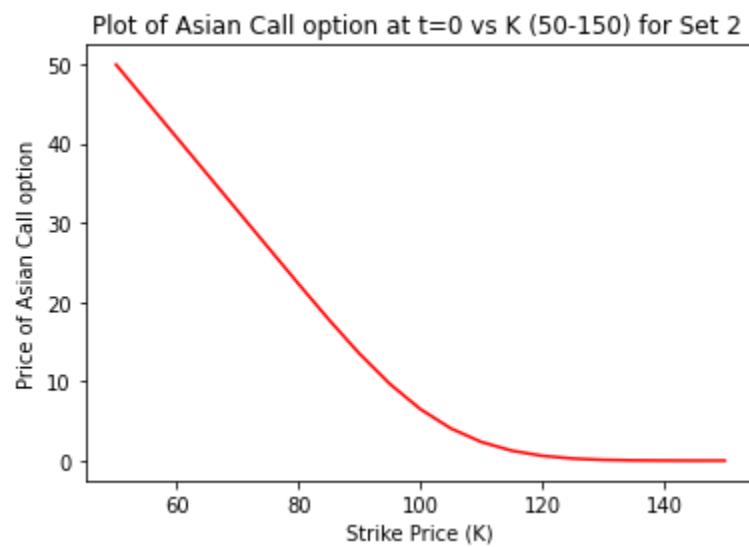
Question 2 Plots -

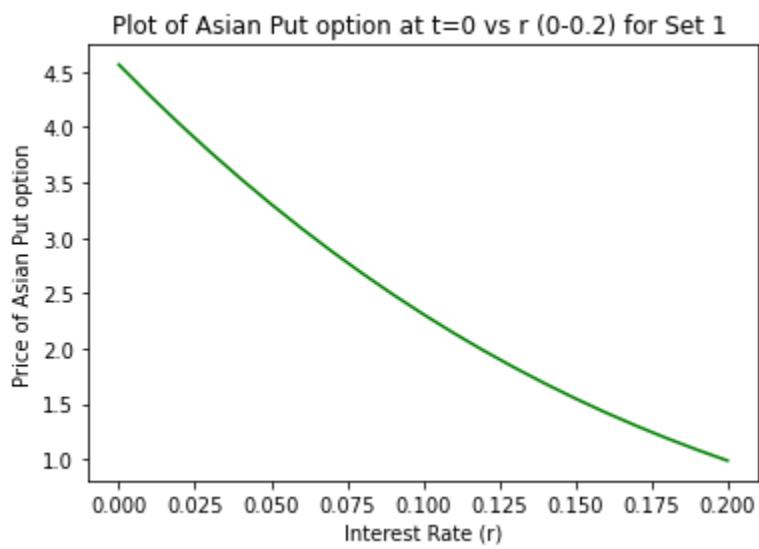
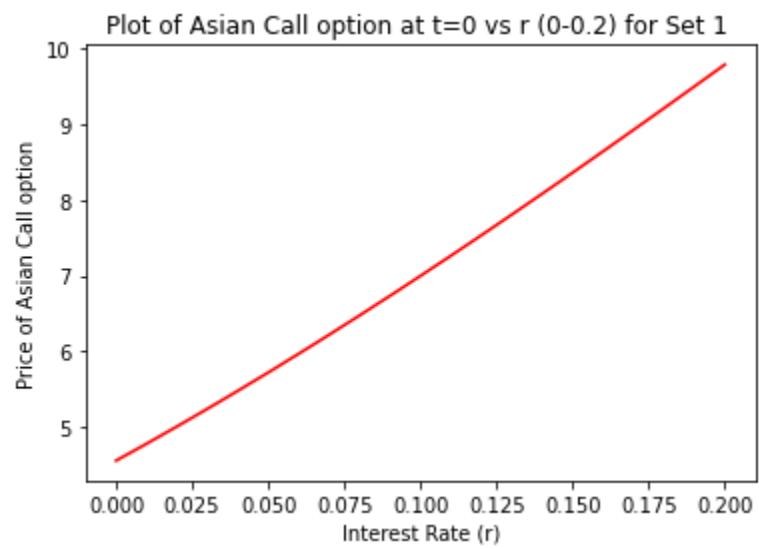
2D Plots (1 param at a time)

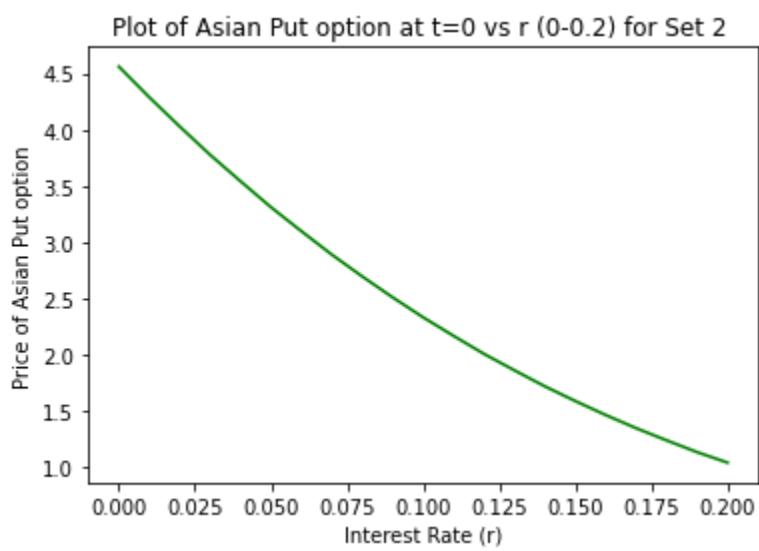
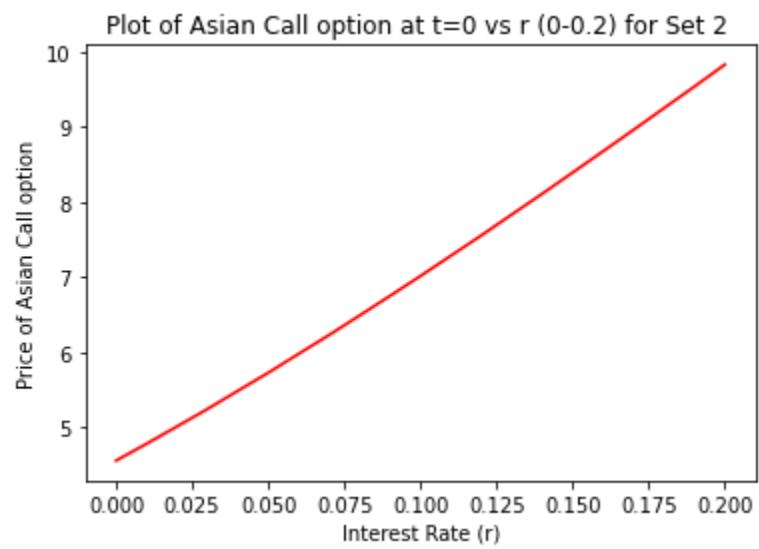


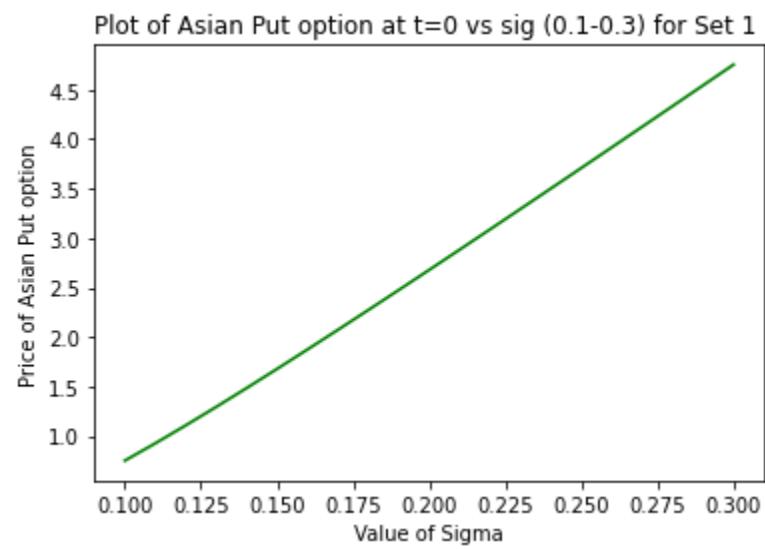
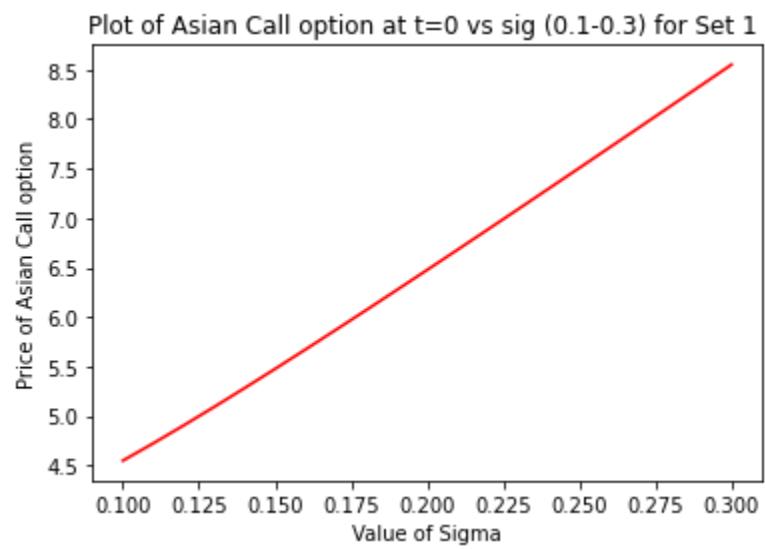


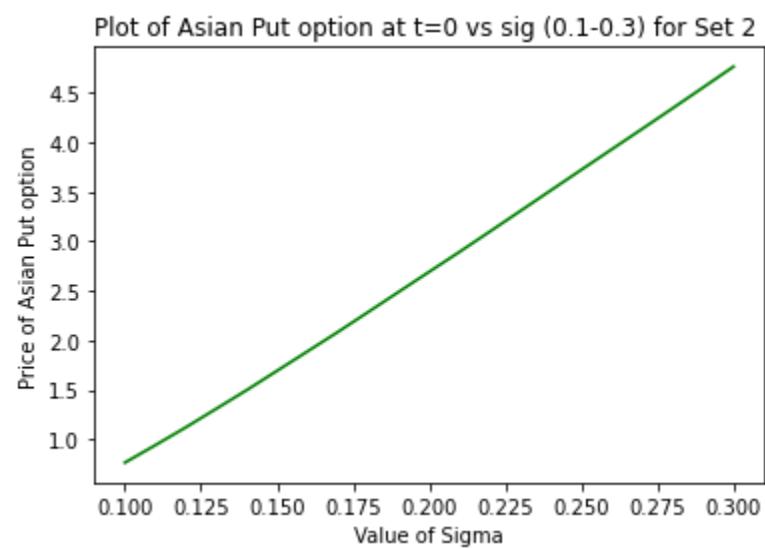
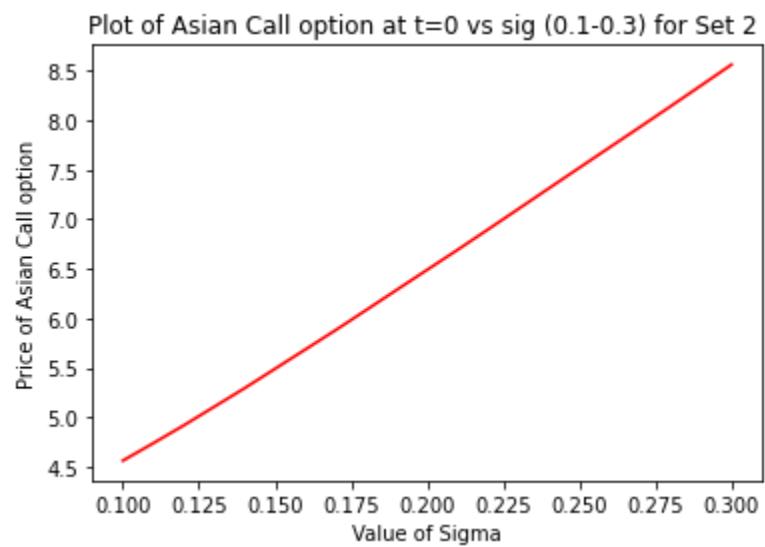


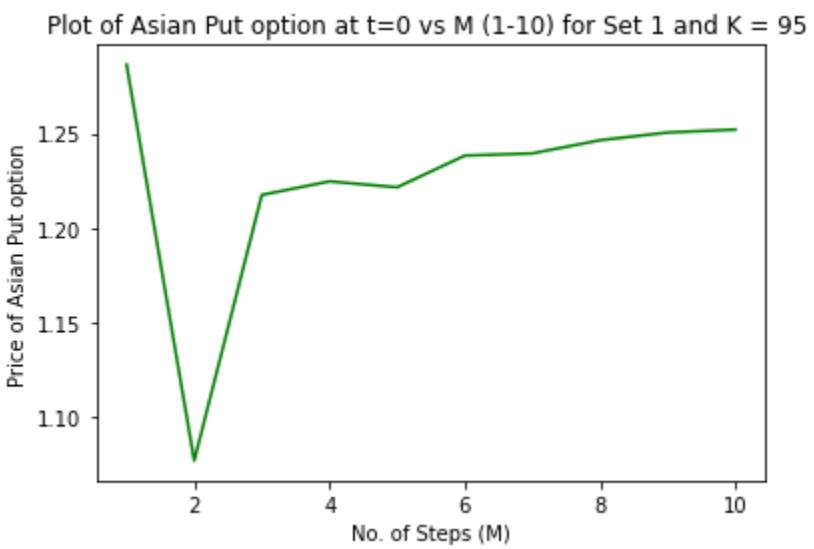
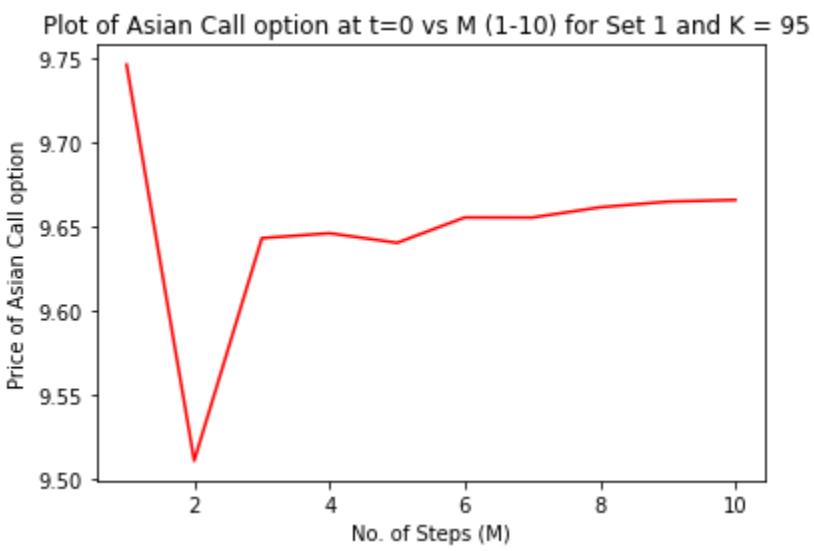




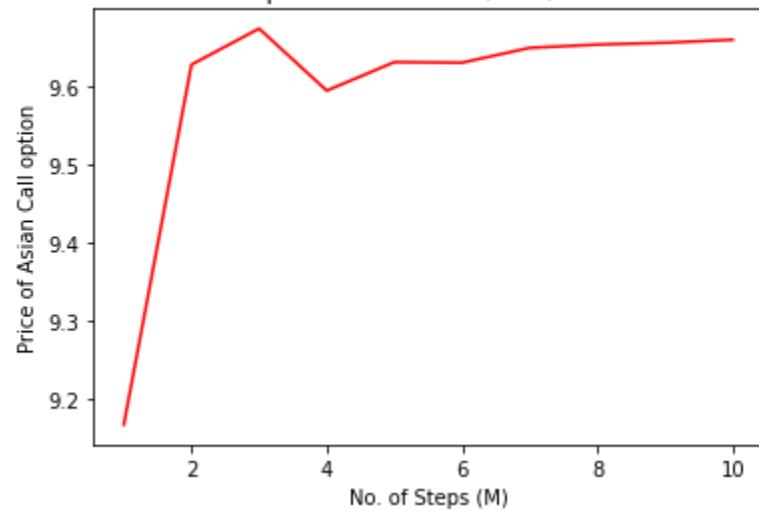




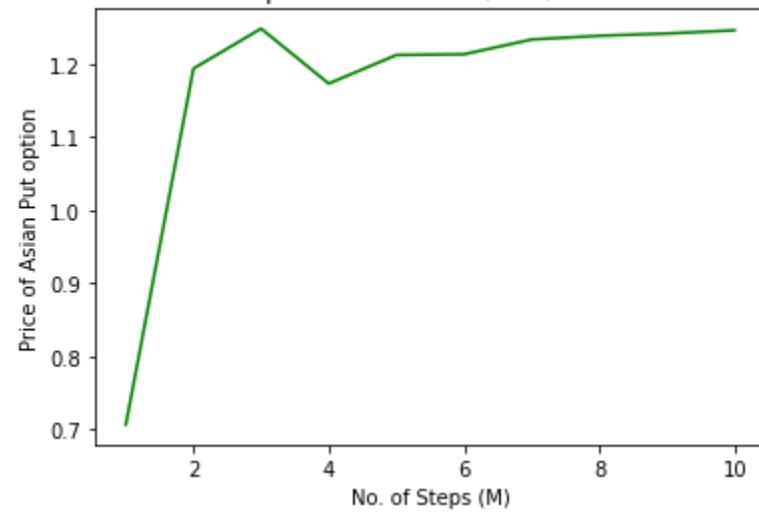




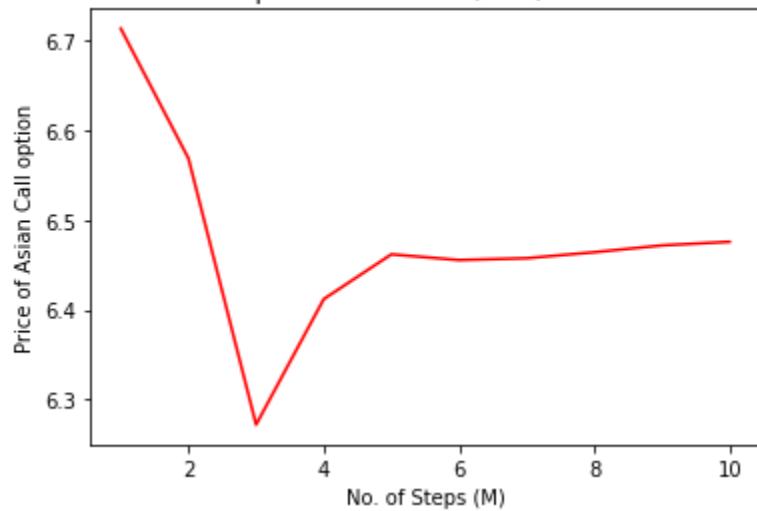
Plot of Asian Call option at $t=0$ vs M (1-10) for Set 2 and $K = 95$



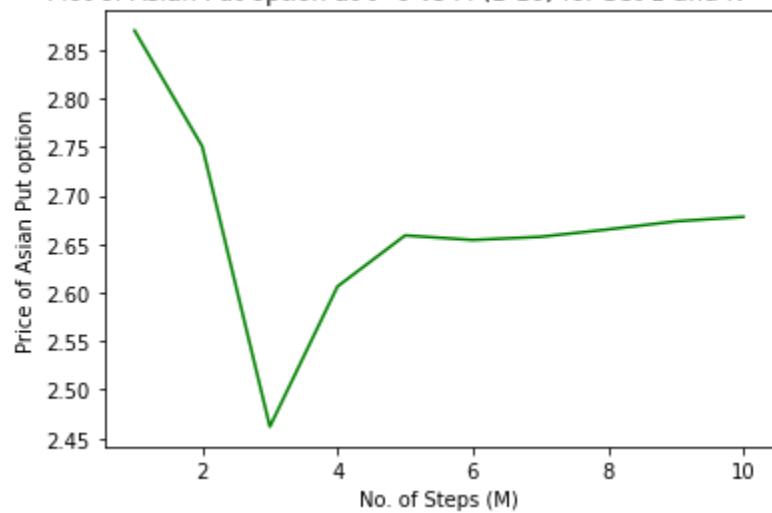
Plot of Asian Put option at $t=0$ vs M (1-10) for Set 2 and $K = 95$



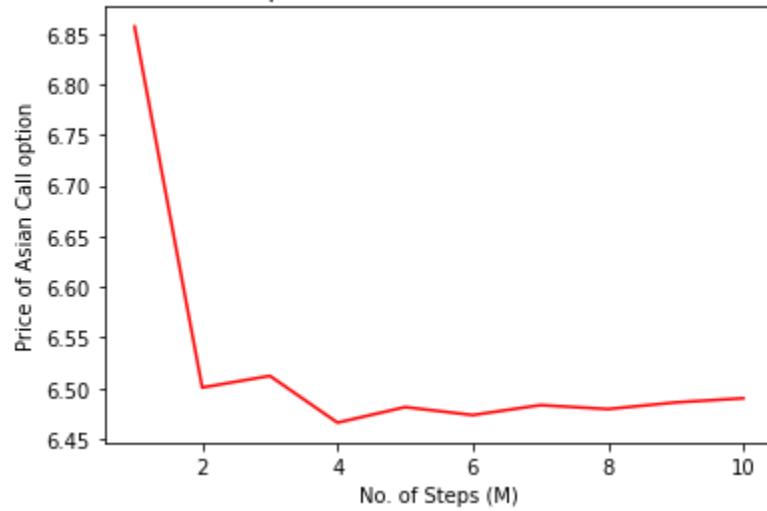
Plot of Asian Call option at $t=0$ vs M (1-10) for Set 1 and $K = 100$



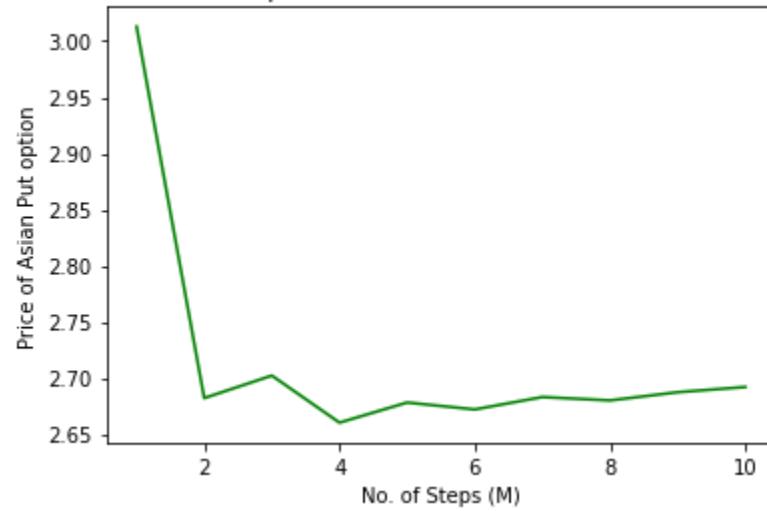
Plot of Asian Put option at $t=0$ vs M (1-10) for Set 1 and $K = 100$



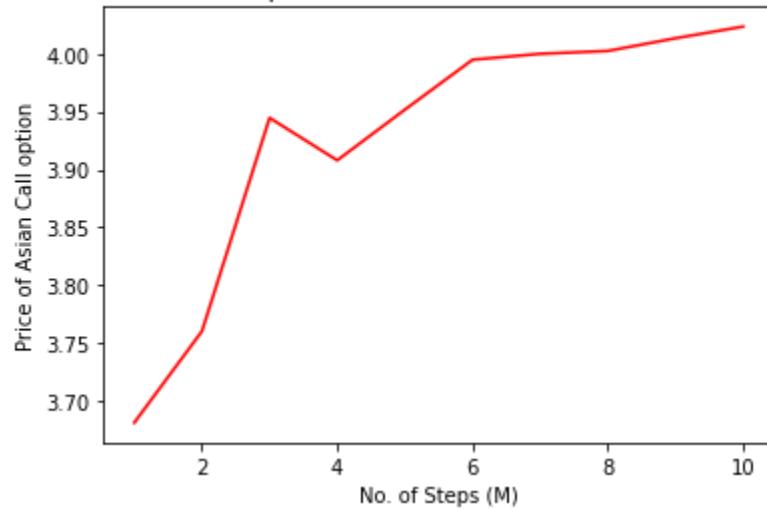
Plot of Asian Call option at $t=0$ vs M (1-10) for Set 2 and $K = 100$



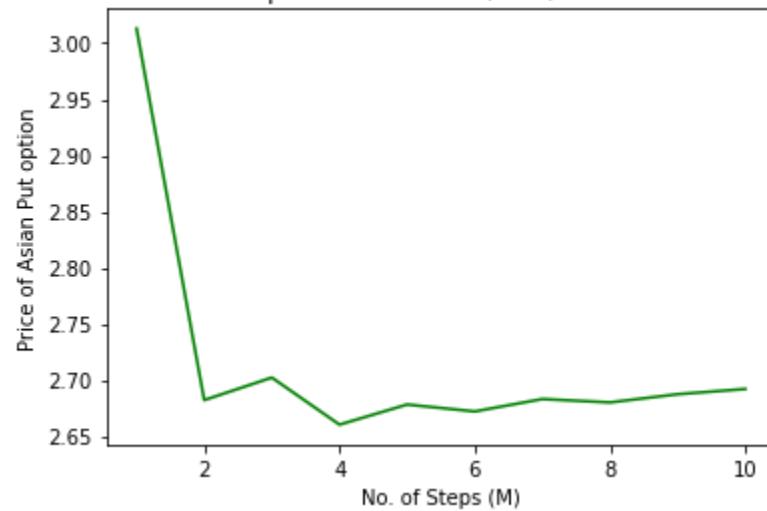
Plot of Asian Put option at $t=0$ vs M (1-10) for Set 2 and $K = 100$



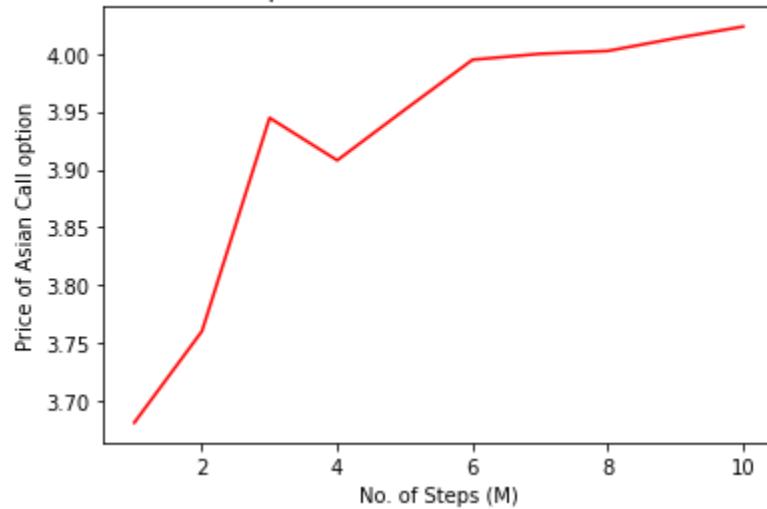
Plot of Asian Call option at $t=0$ vs M (1-10) for Set 1 and $K = 105$



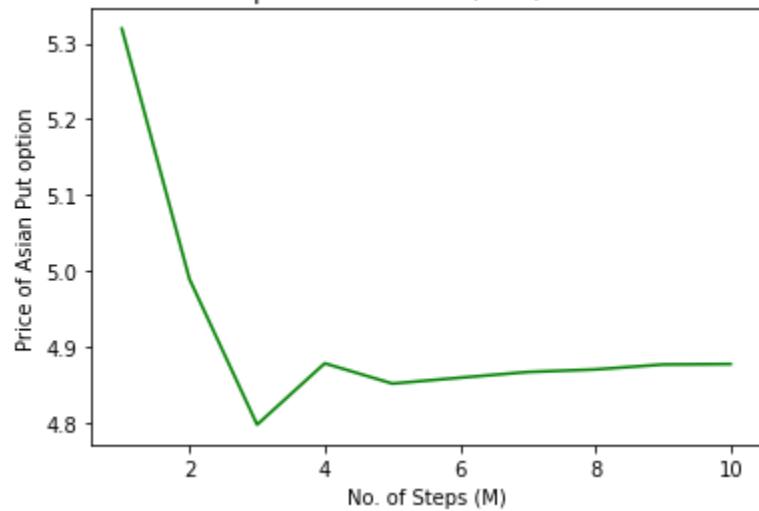
Plot of Asian Put option at $t=0$ vs M (1-10) for Set 2 and $K = 100$



Plot of Asian Call option at $t=0$ vs M (1-10) for Set 1 and $K = 105$

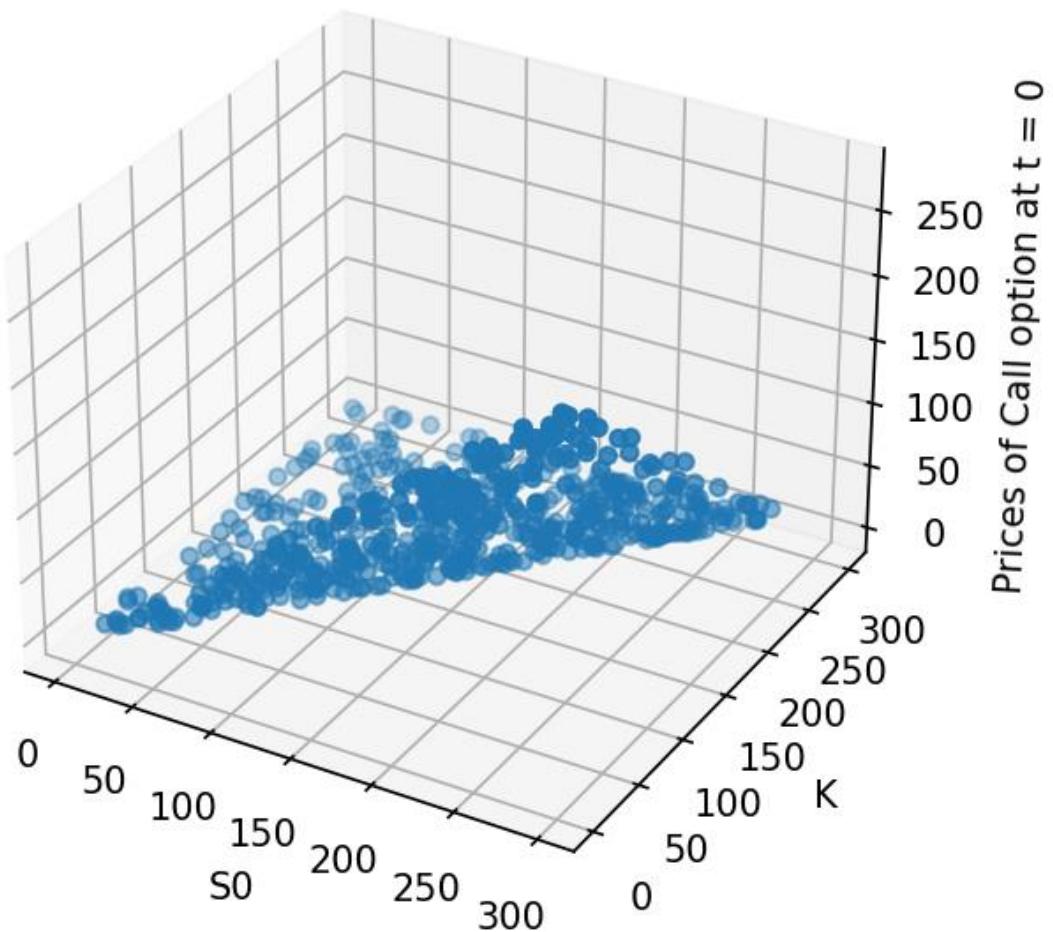


Plot of Asian Put option at $t=0$ vs M (1-10) for Set 2 and $K = 105$

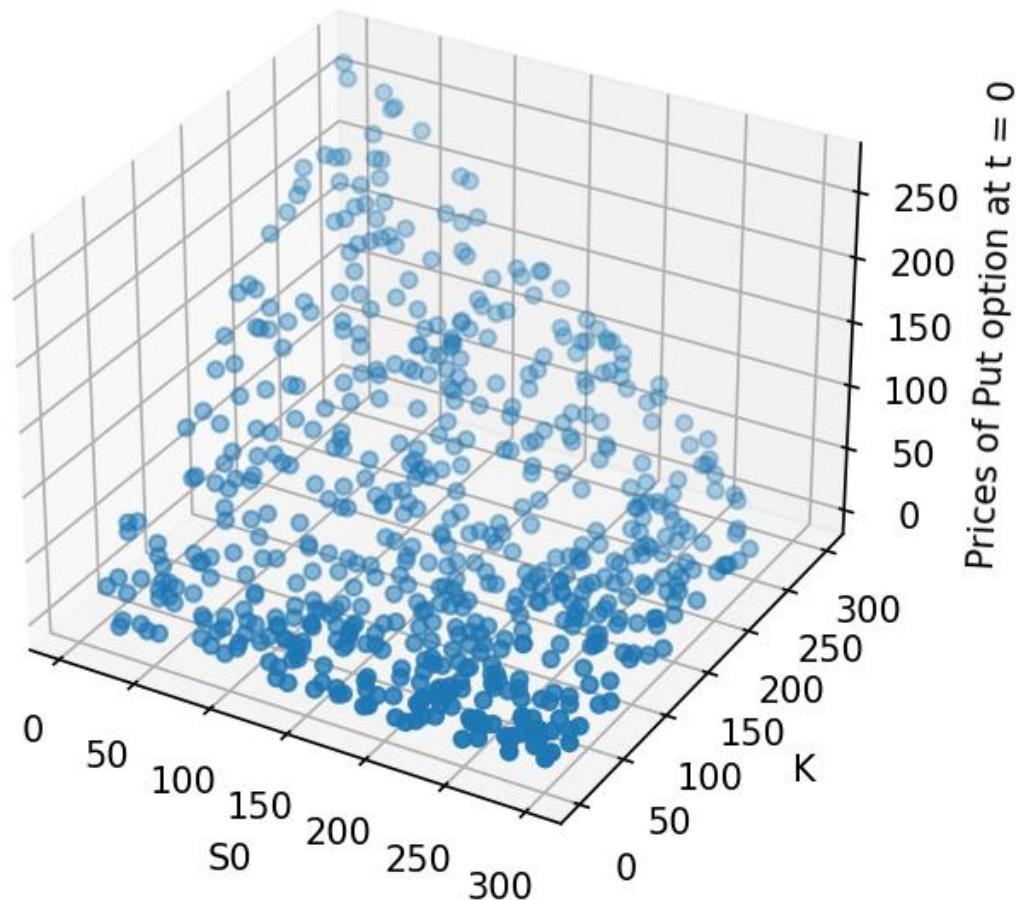


3D Plots (2 params at a time)

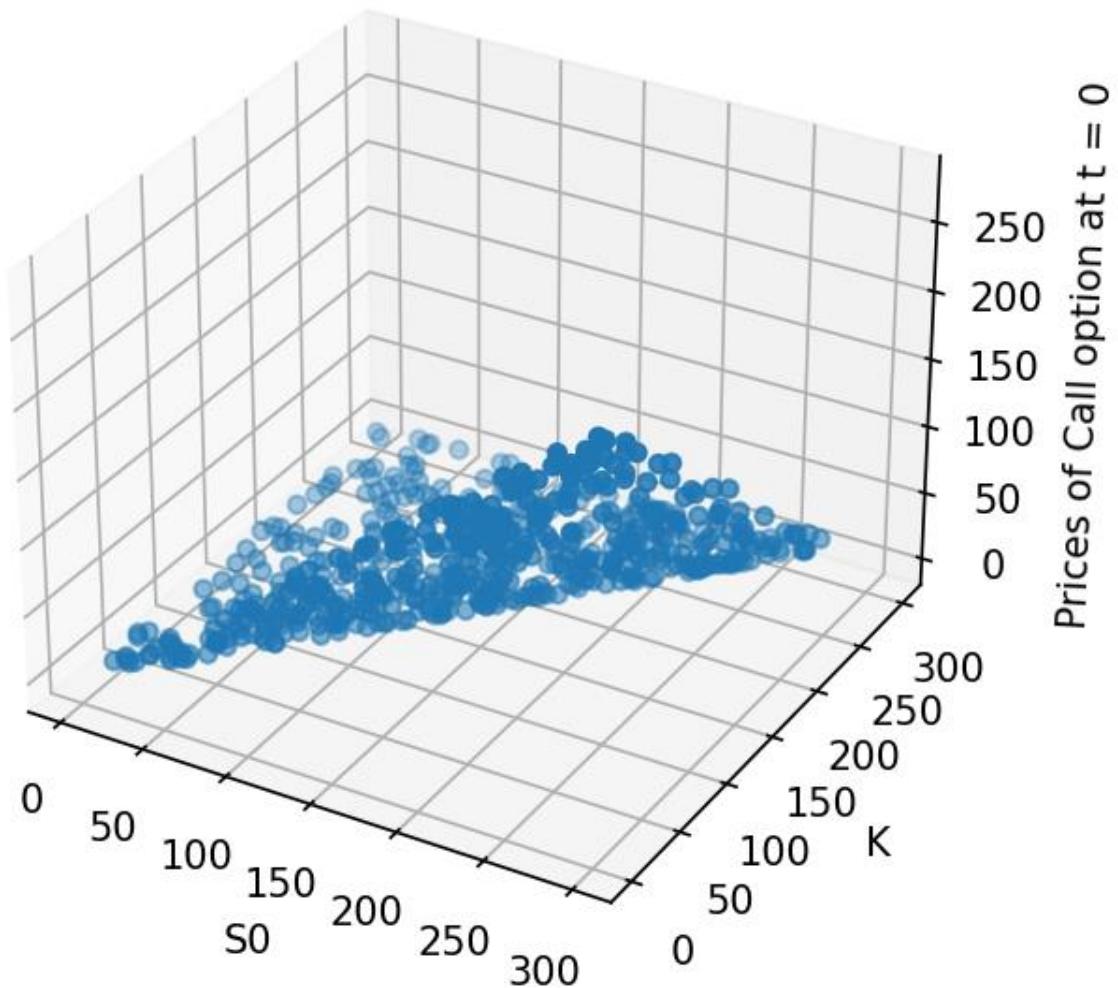
Initial Call Option Price vs S_0 and K for the set = 1



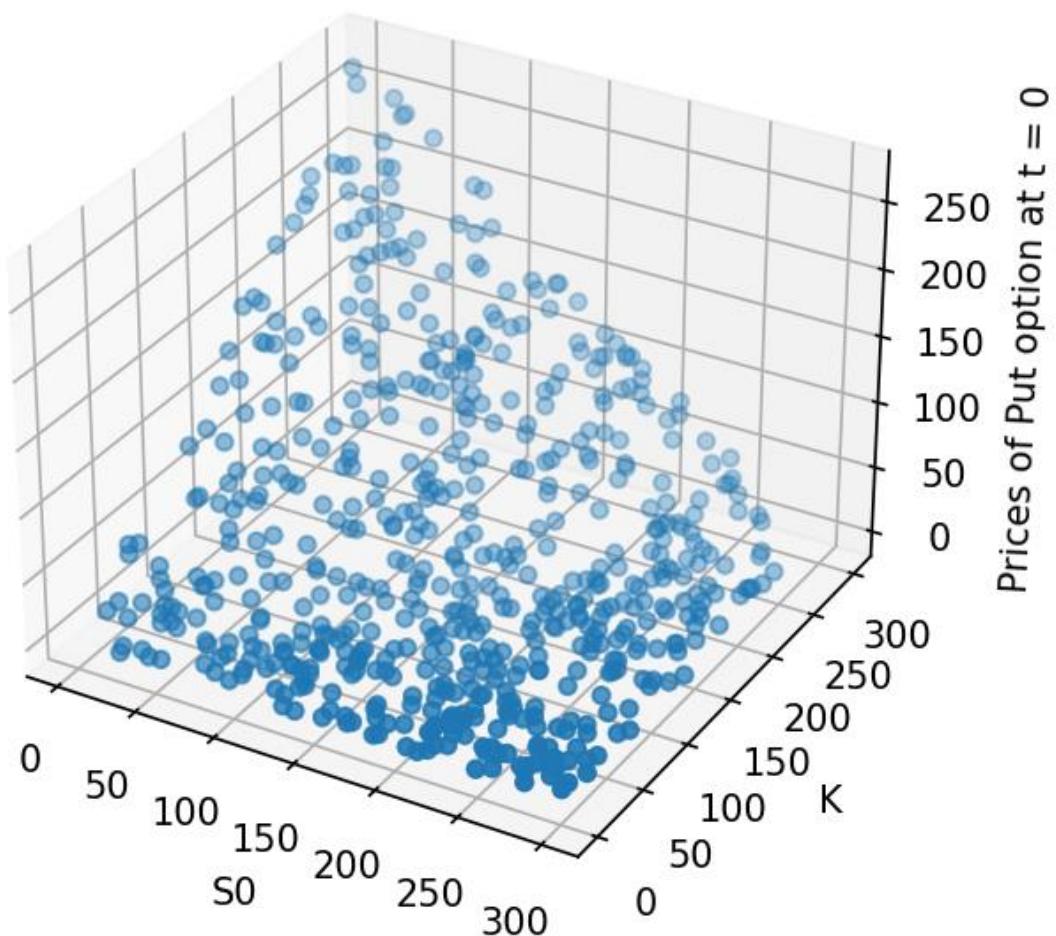
Initial Put Option Price vs S_0 and K for the set = 1



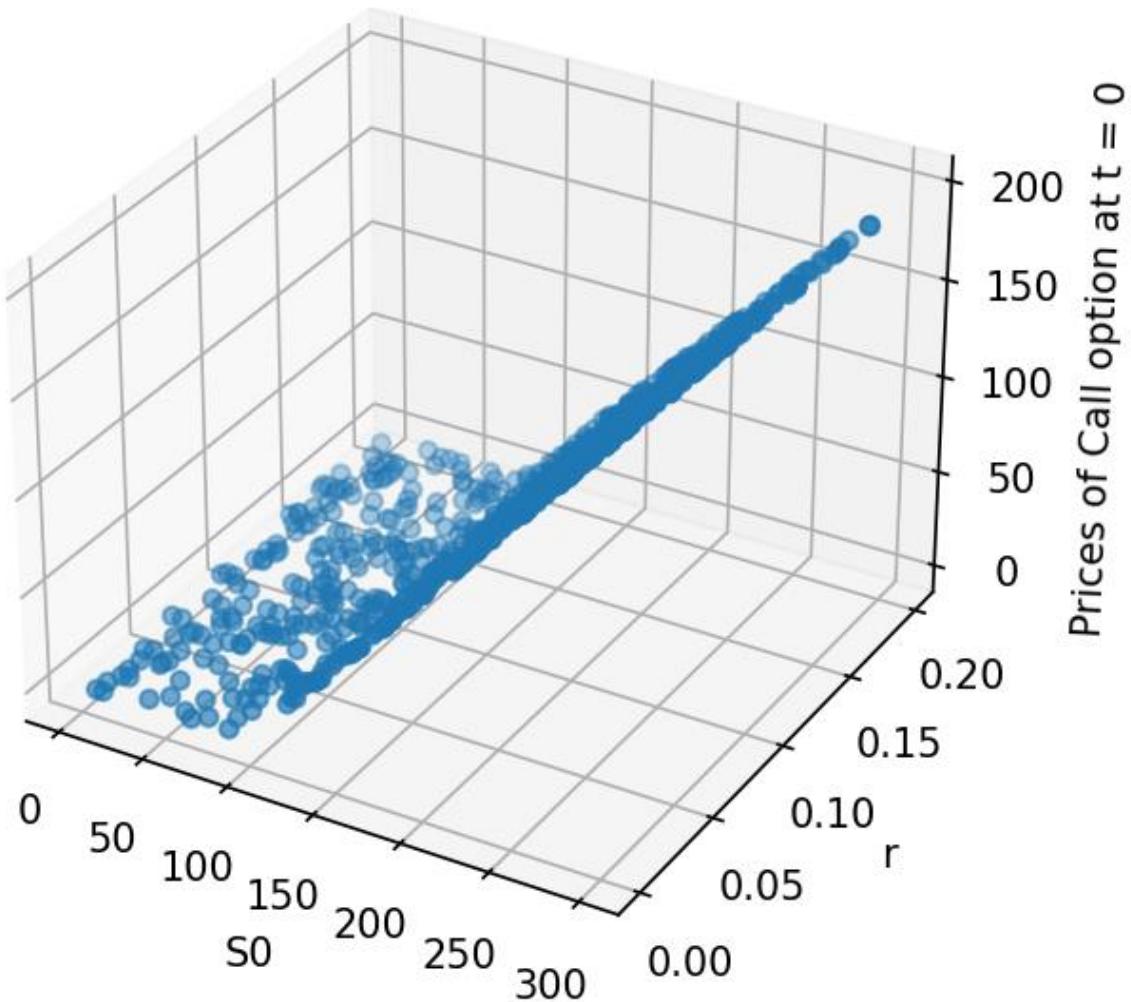
Initial Call Option Price vs S_0 and K for the set = 2



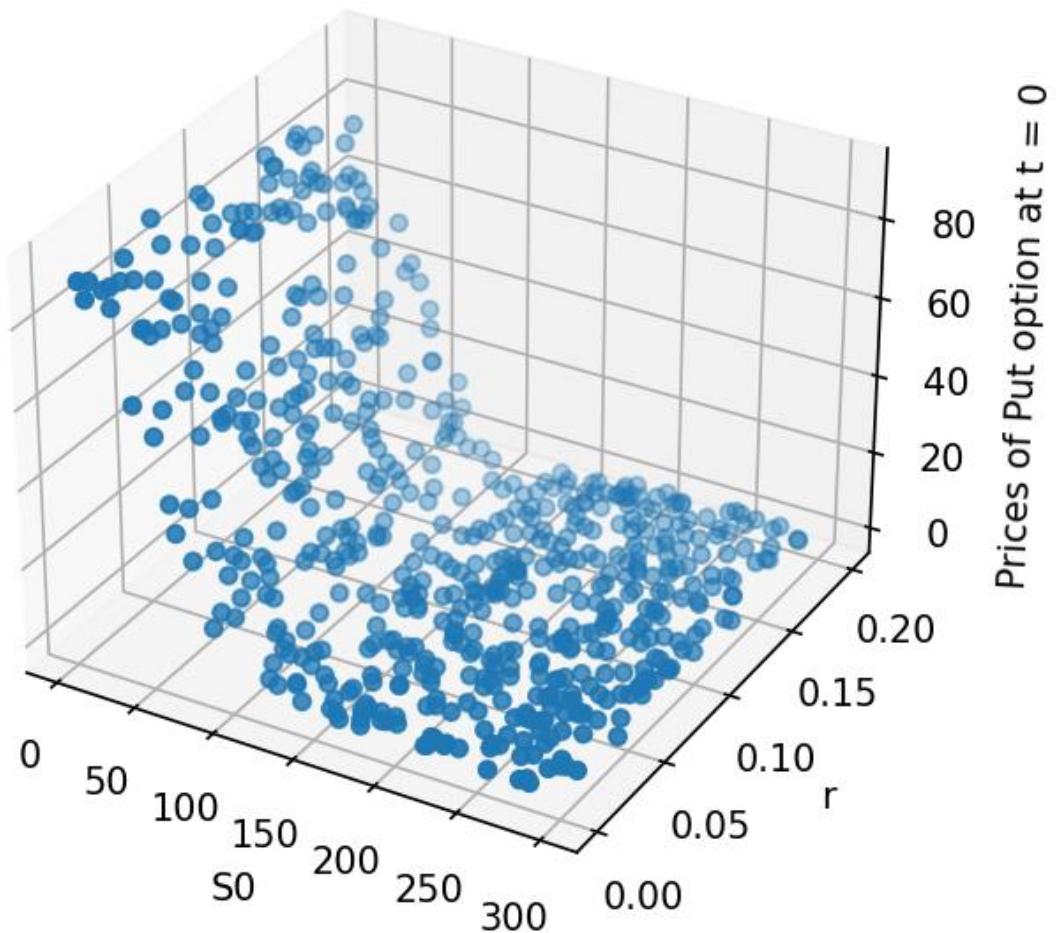
Initial Put Option Price vs S_0 and K for the set = 2



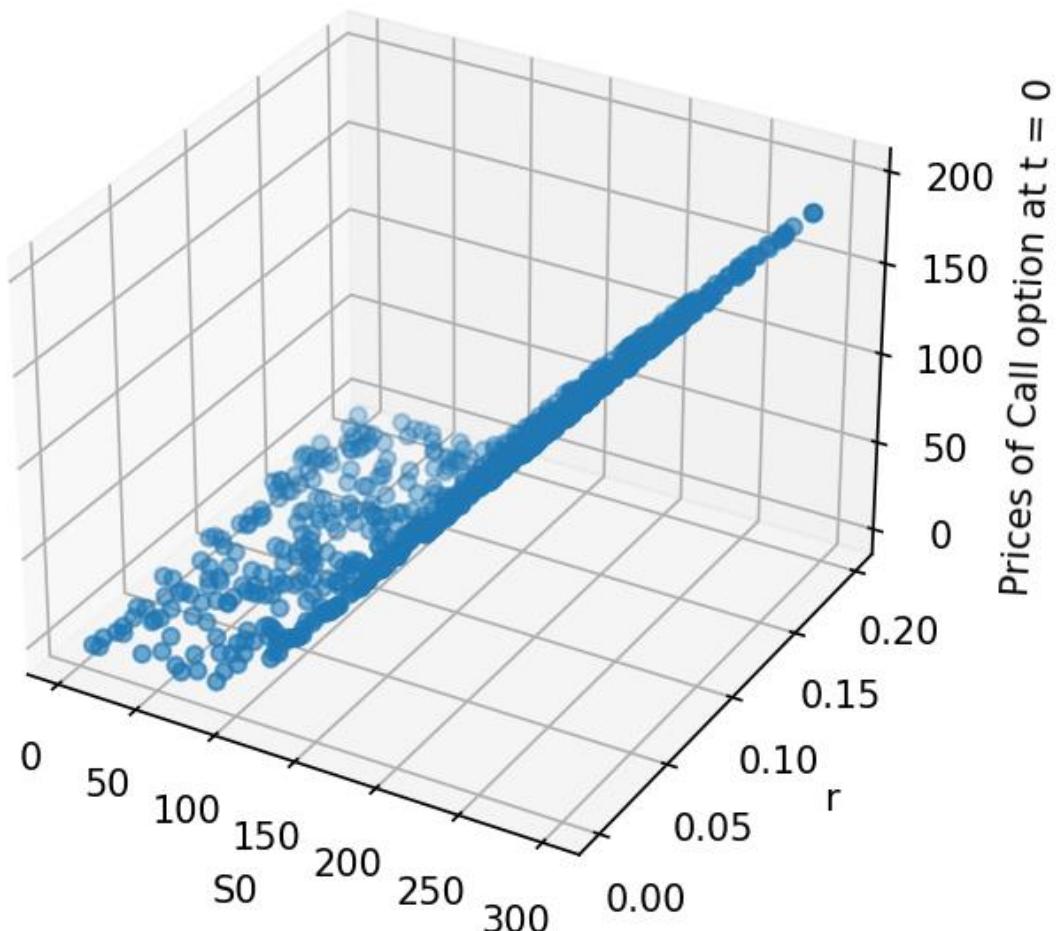
Initial Call Option Price vs S_0 and r for the set = 1



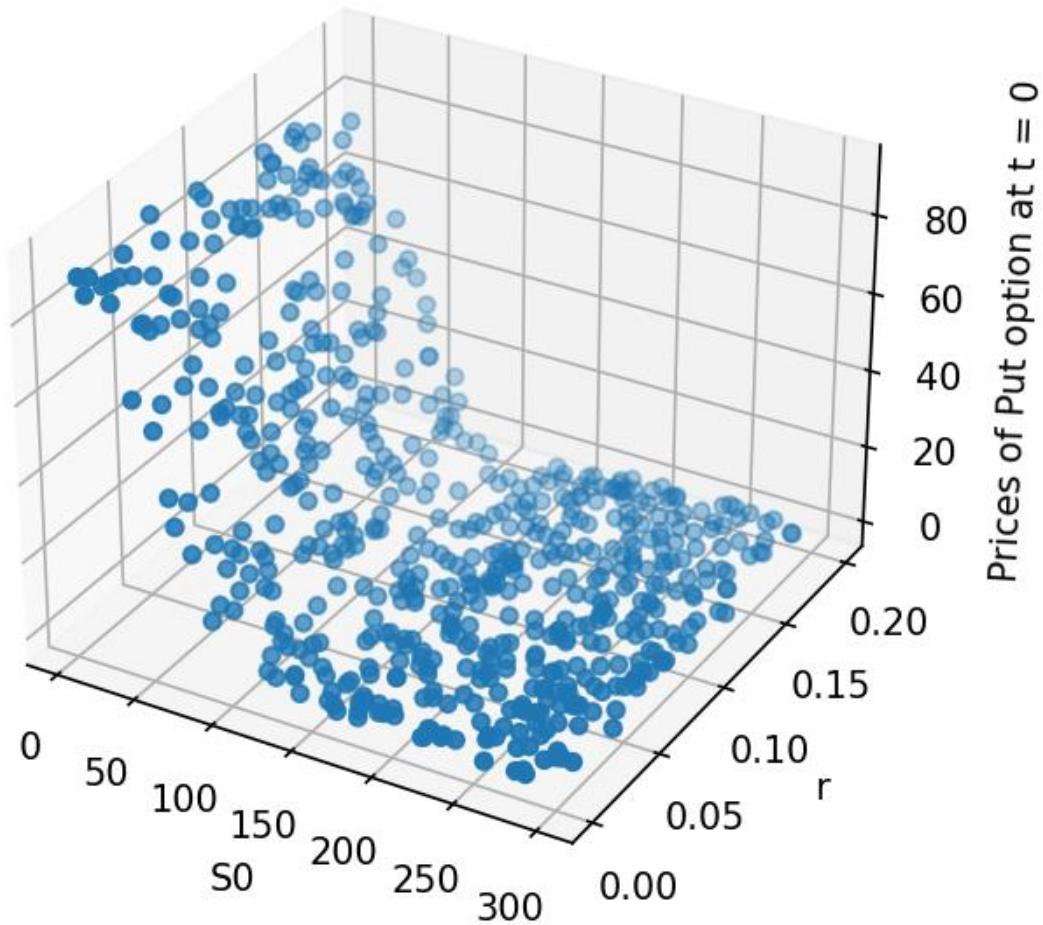
Initial Put Option Price vs S_0 and r for the set = 1



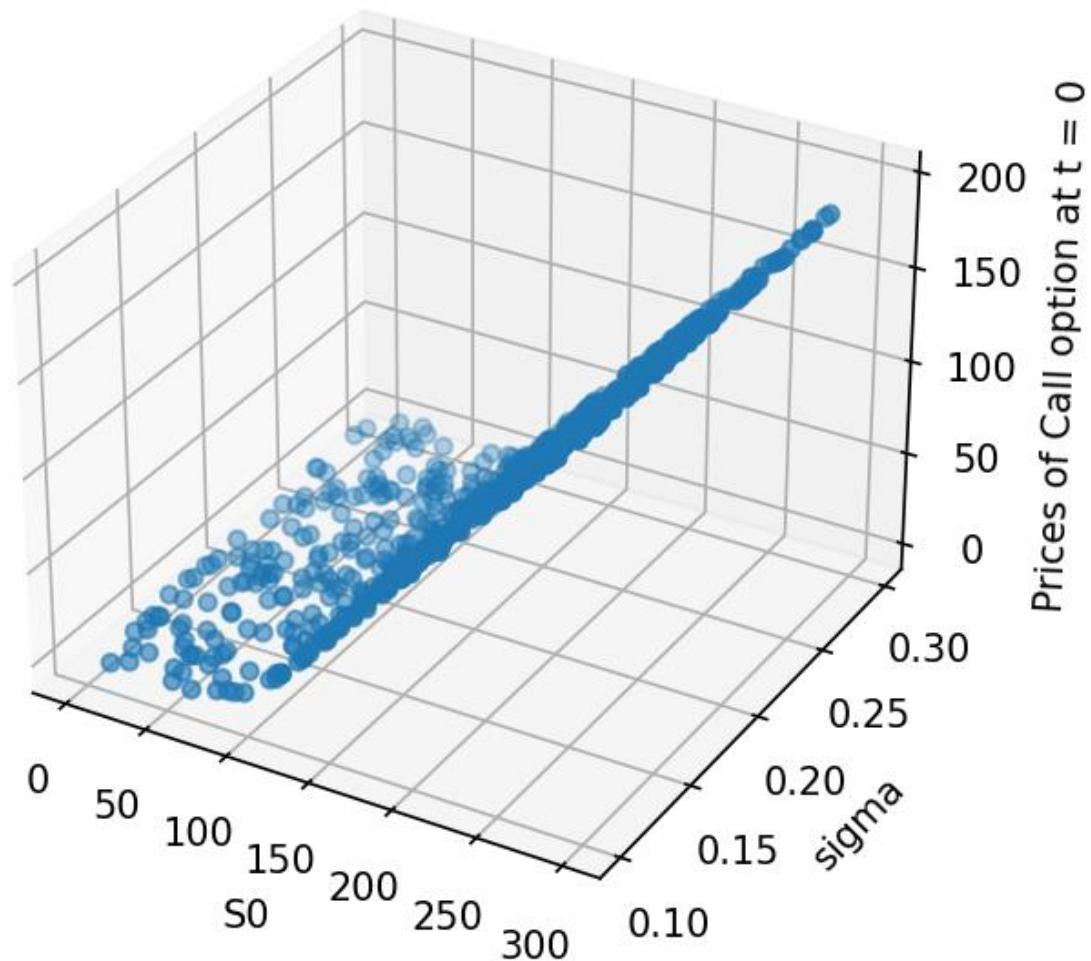
Initial Call Option Price vs S_0 and r for the set = 2



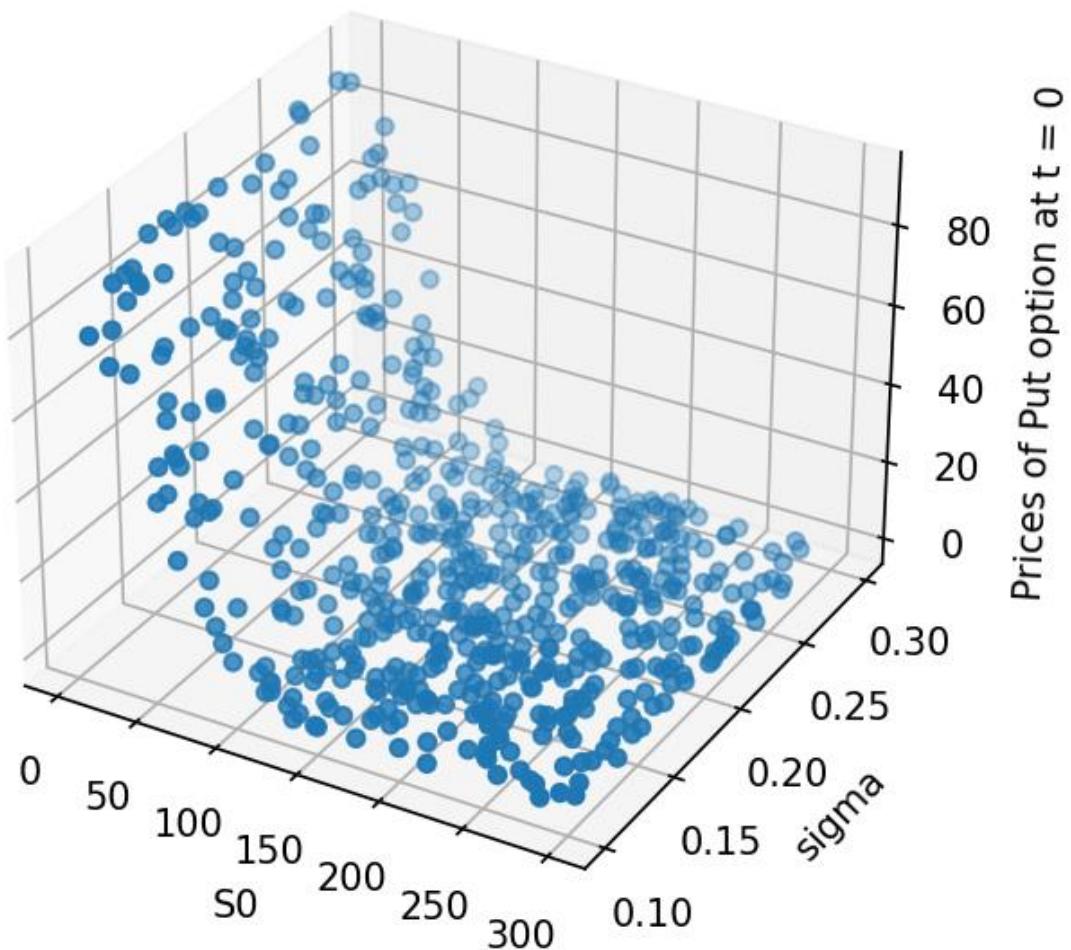
Initial Put Option Price vs S_0 and r for the set = 2



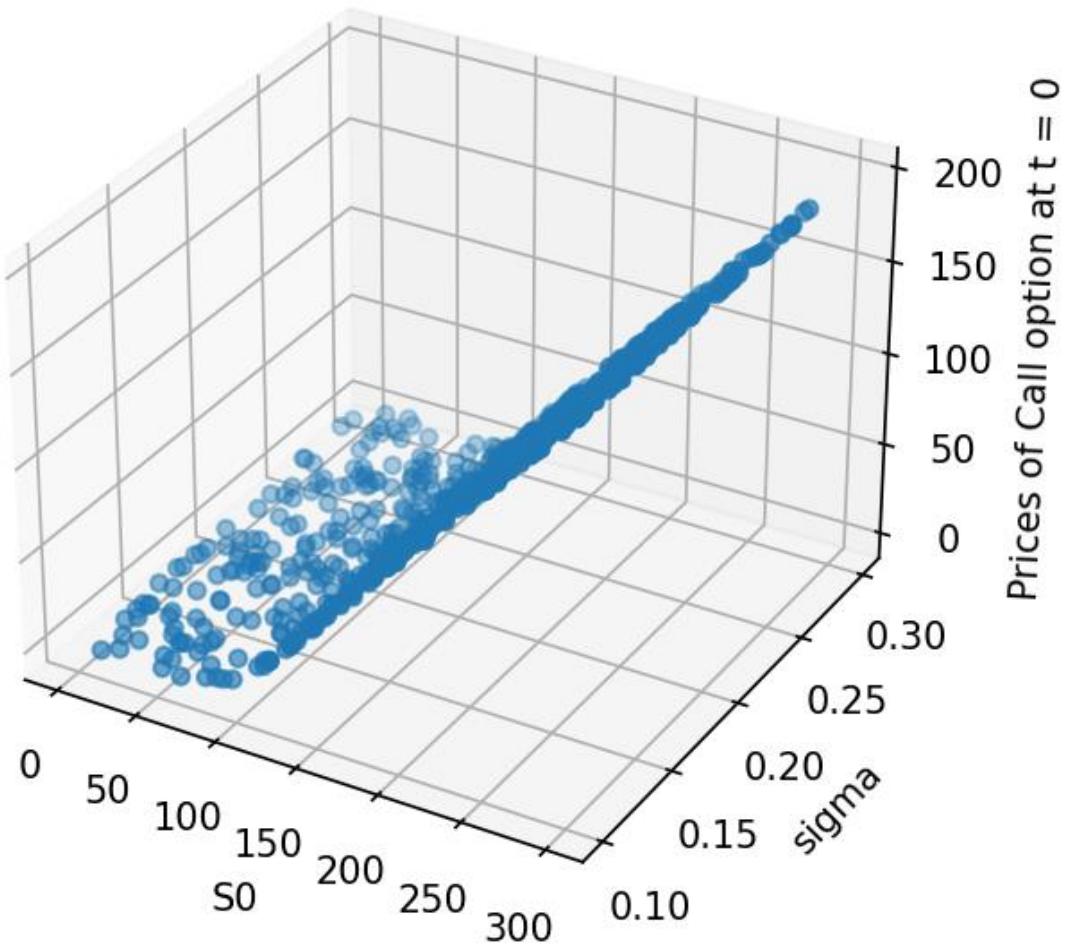
Initial Call Option Price vs S0 and sigma for the set = 1



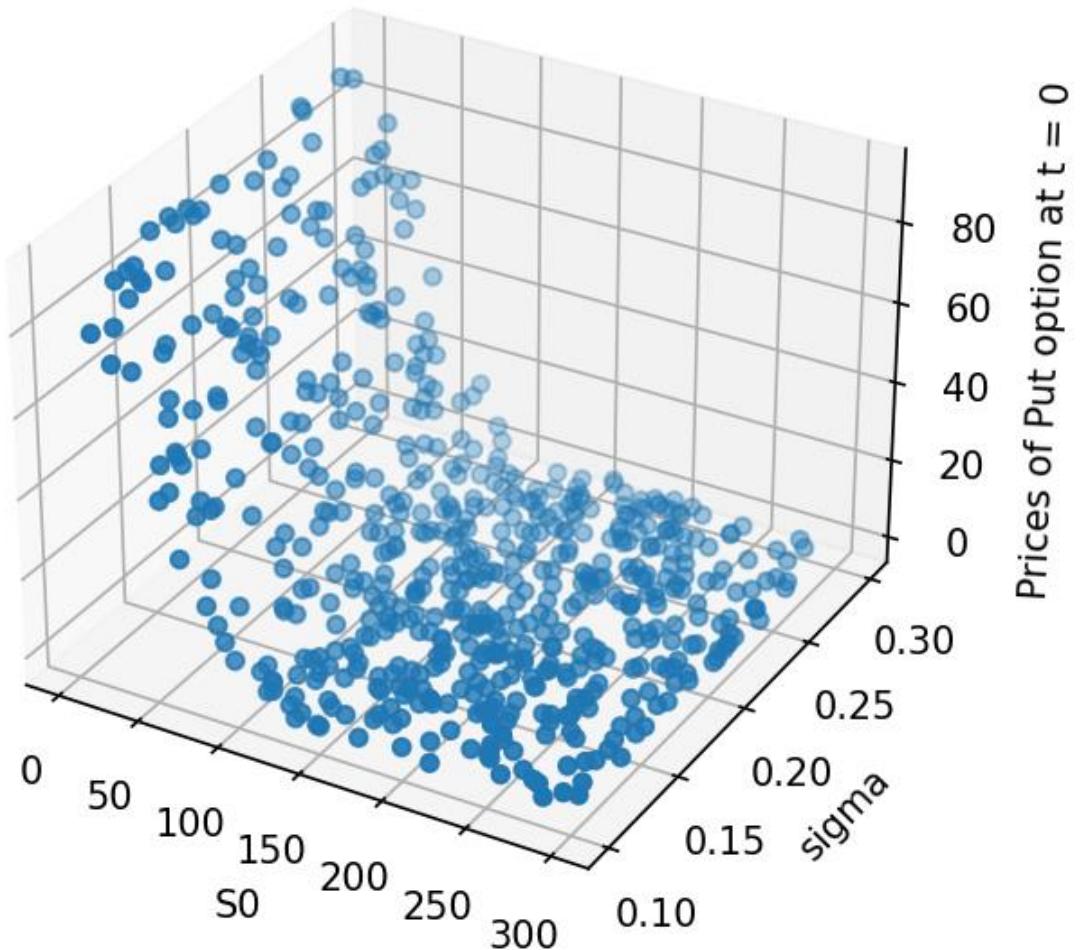
Initial Put Option Price vs S0 and sigma for the set = 1



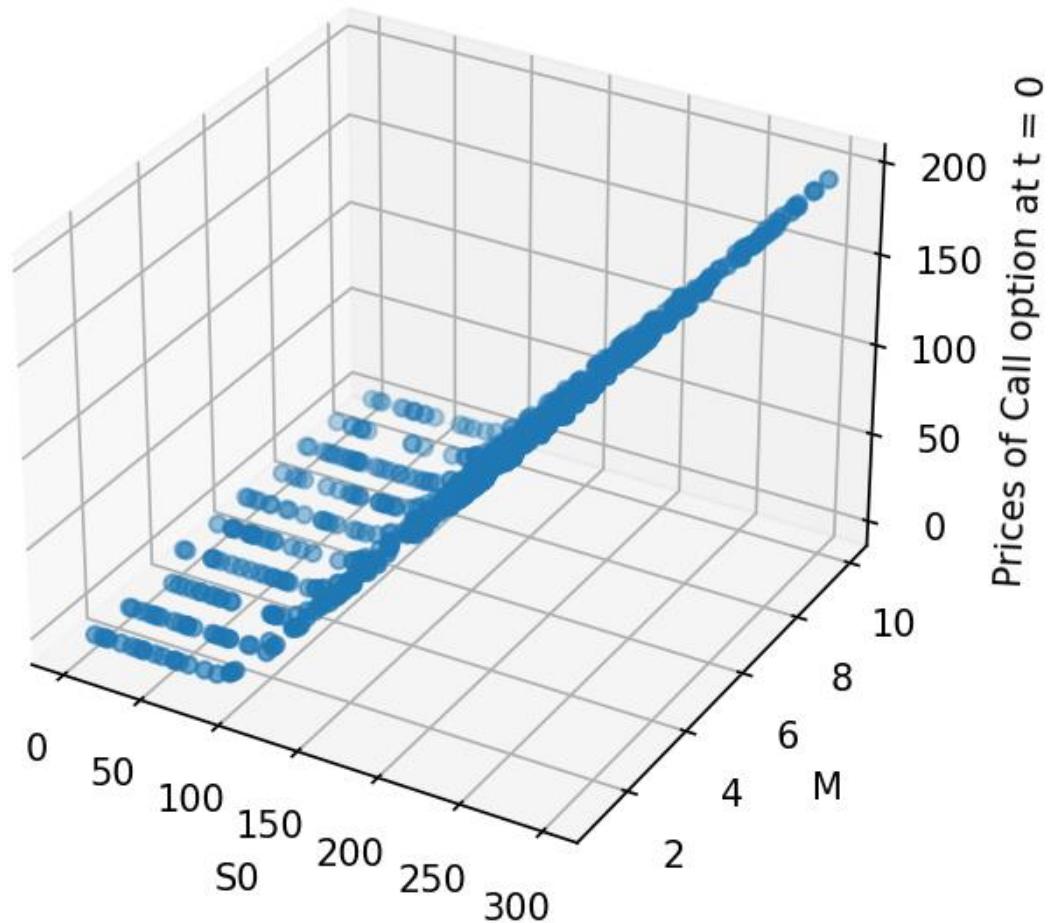
Initial Call Option Price vs S_0 and sigma for the set = 2



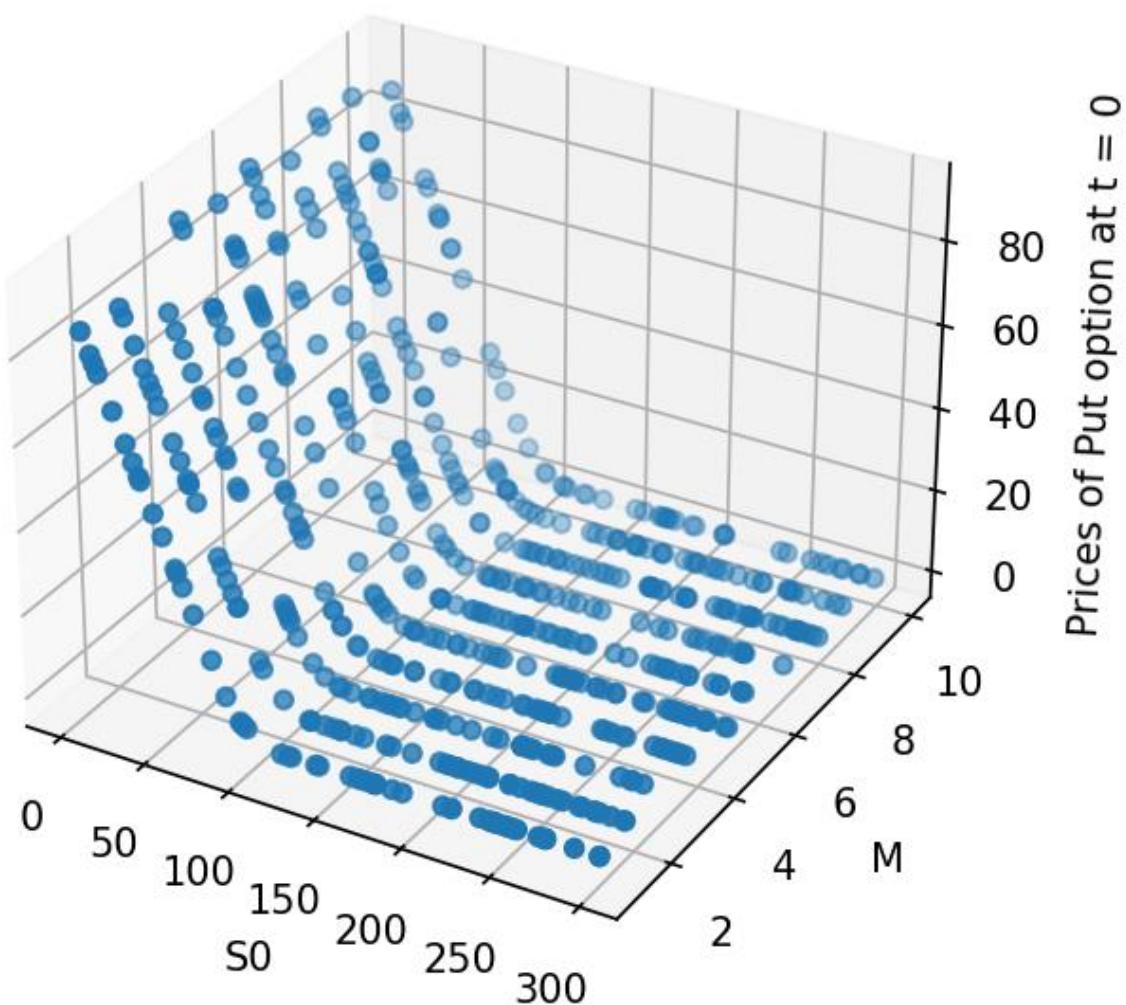
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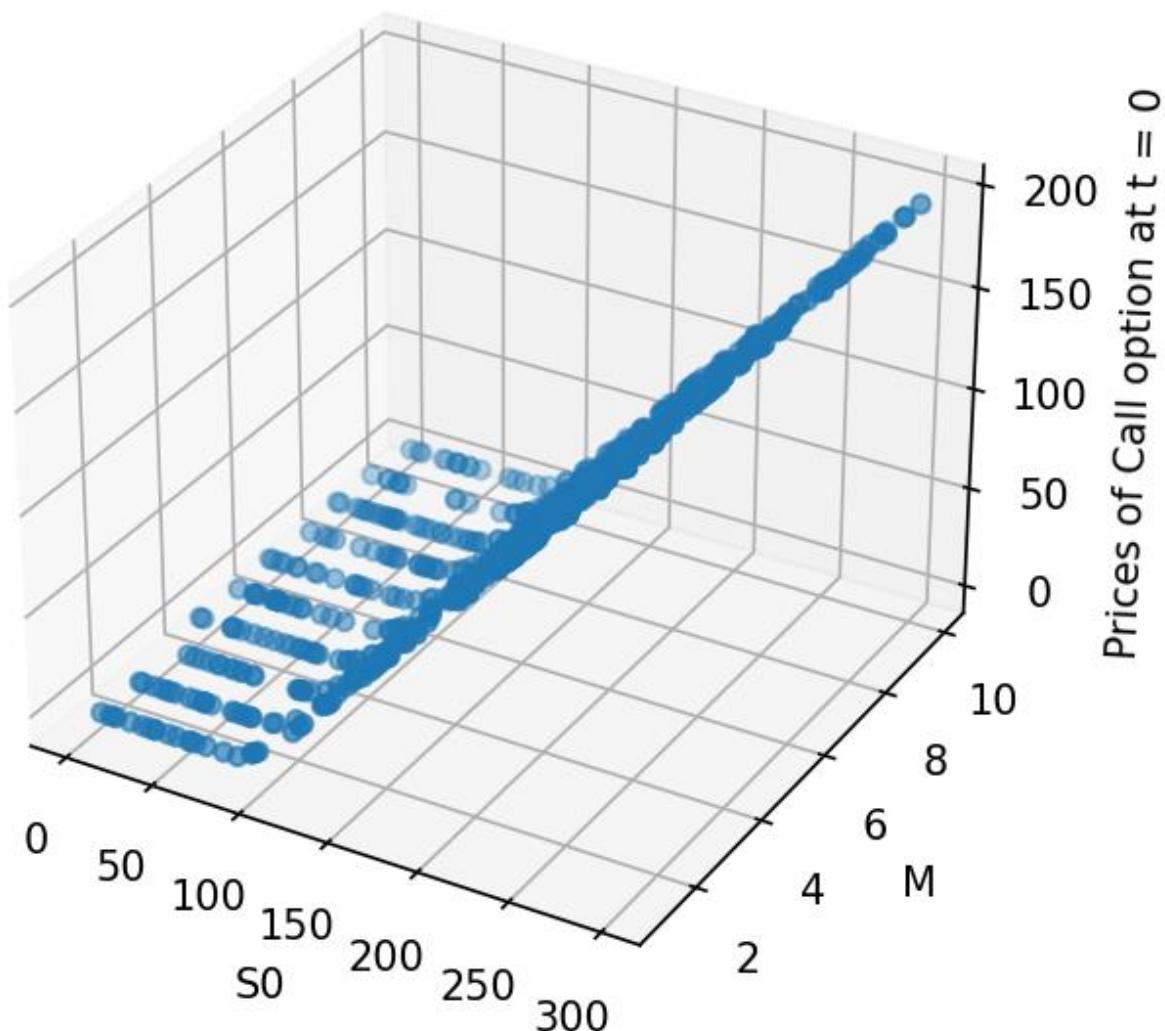
Initial Call Option Price vs S0 and M for the set = 1



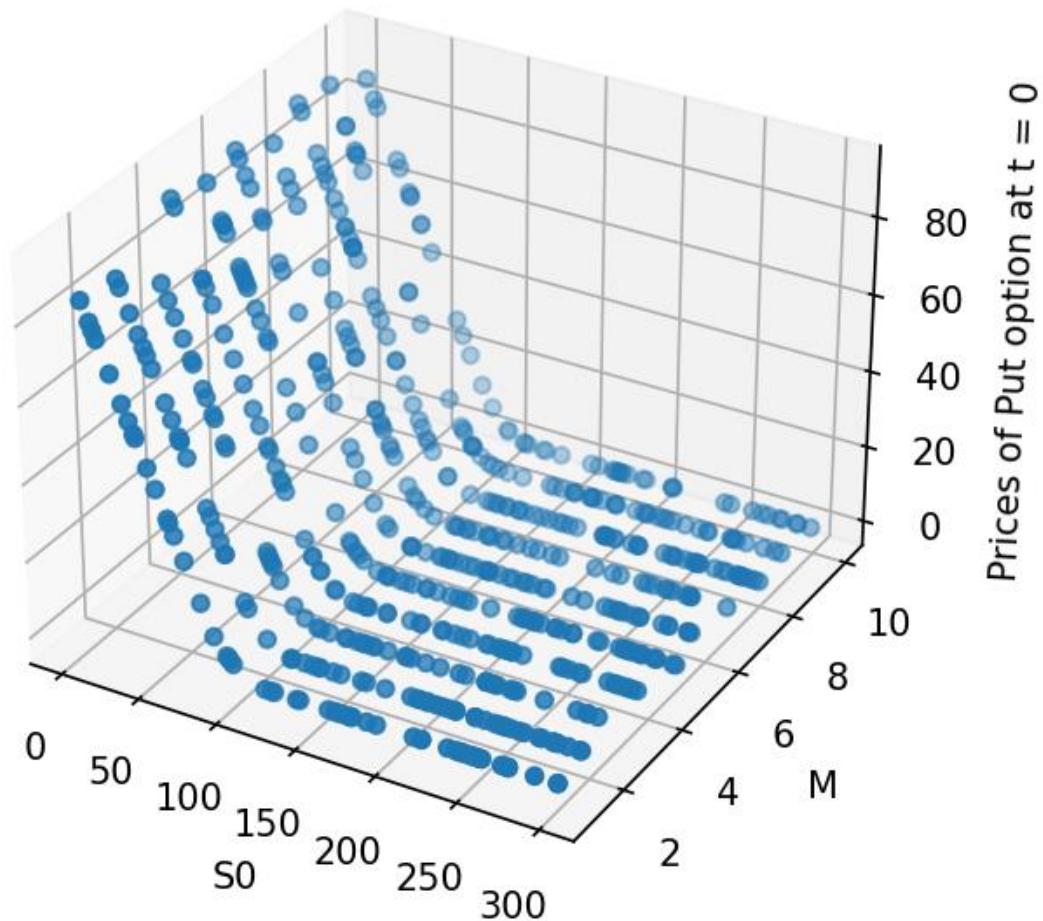
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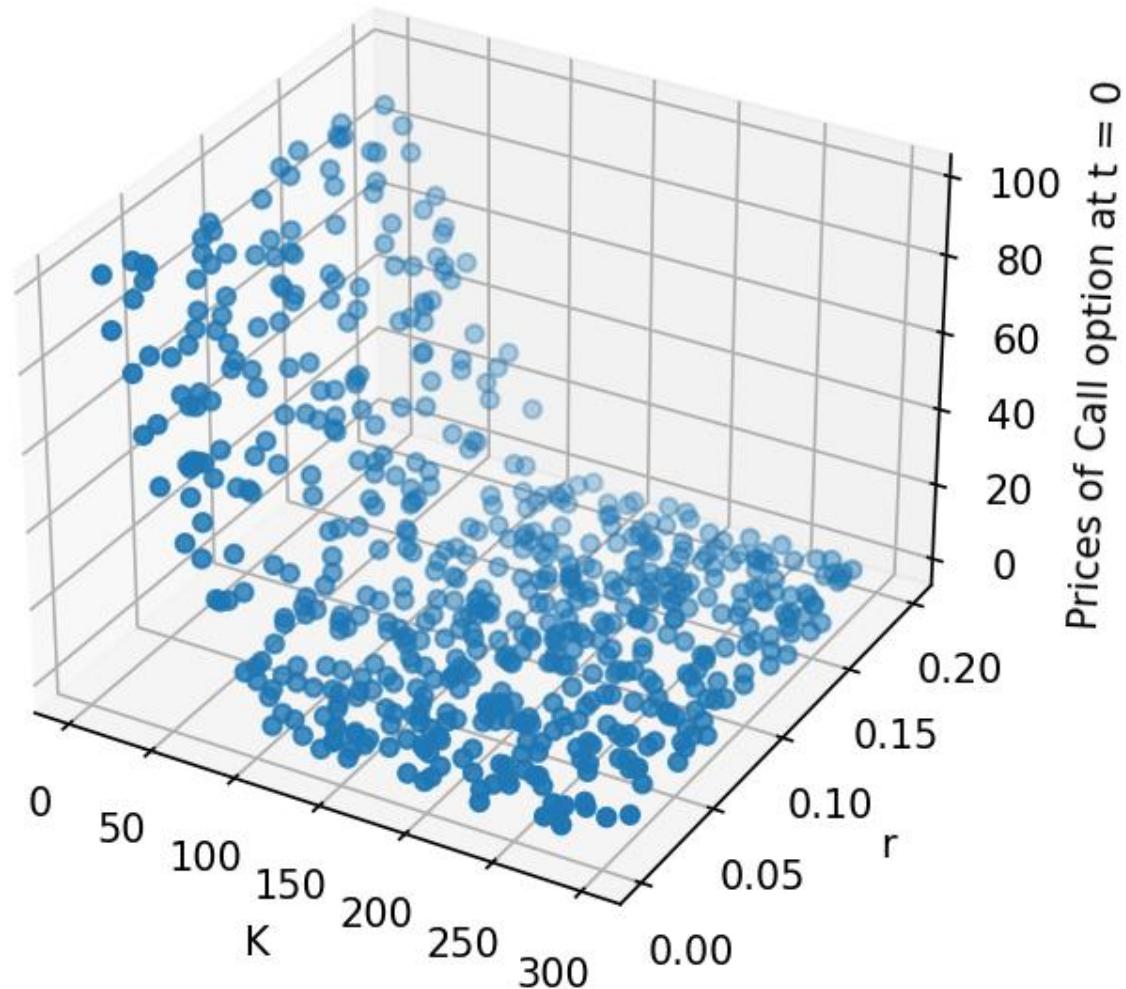
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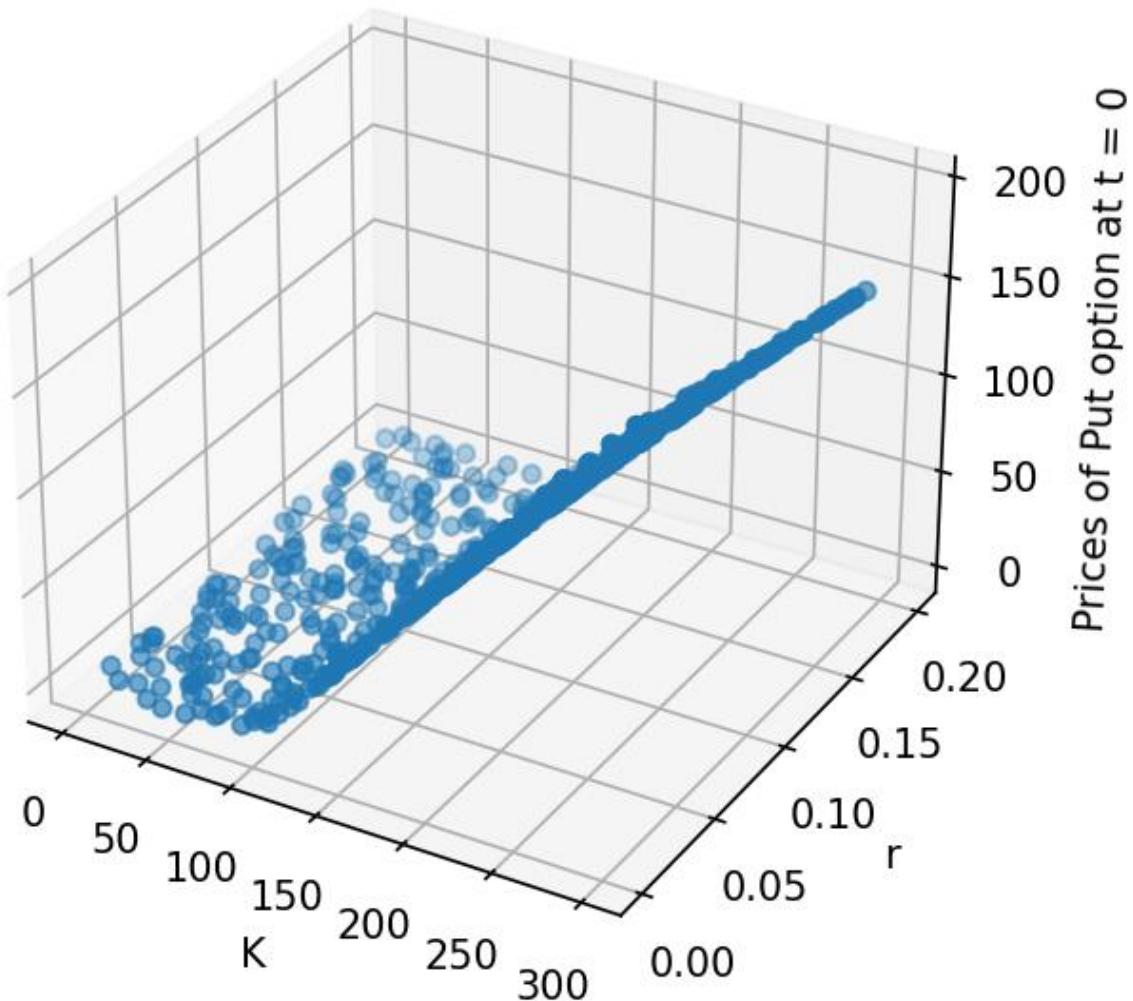
Initial Put Option Price vs S_0 and M for the set = 2



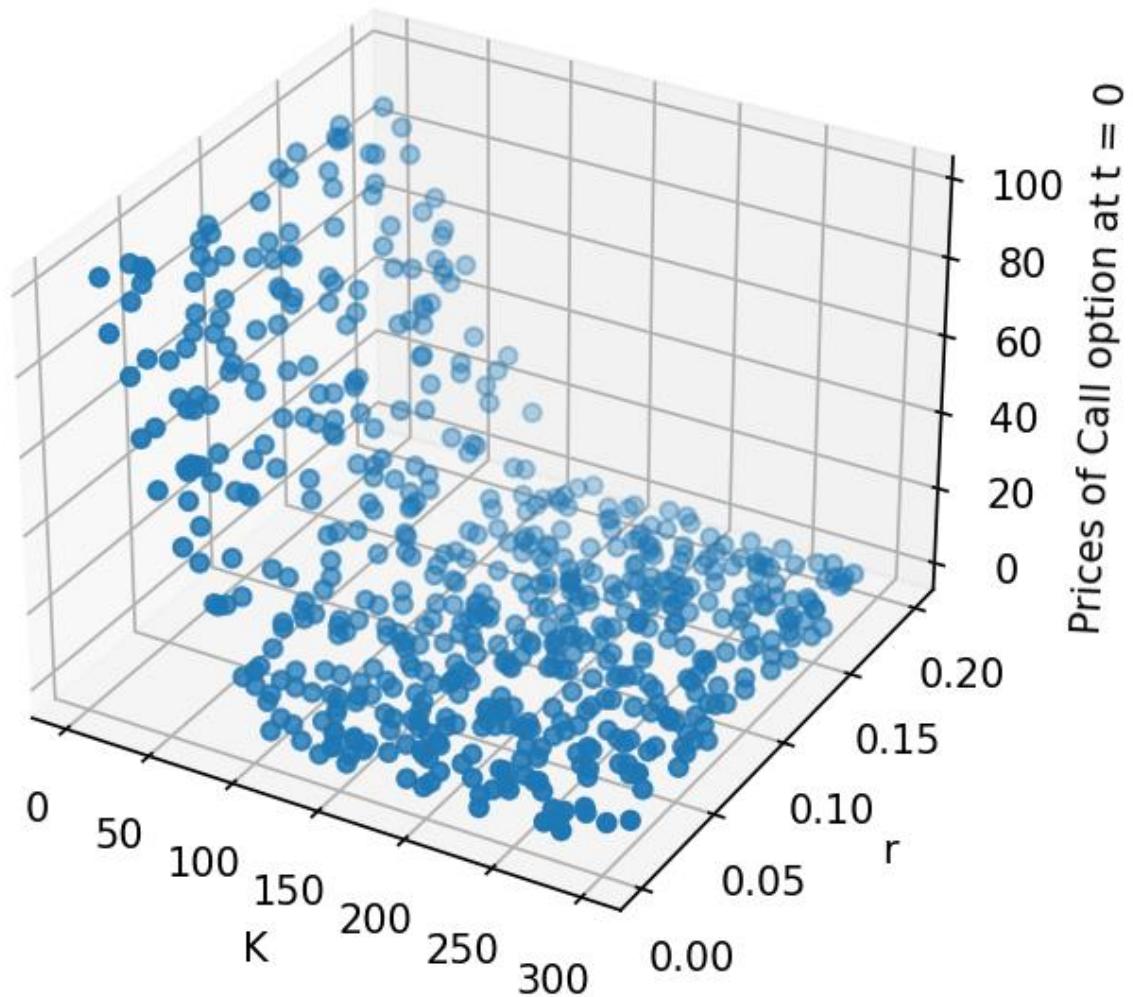
Initial Call Option Price vs K and r for the set = 1



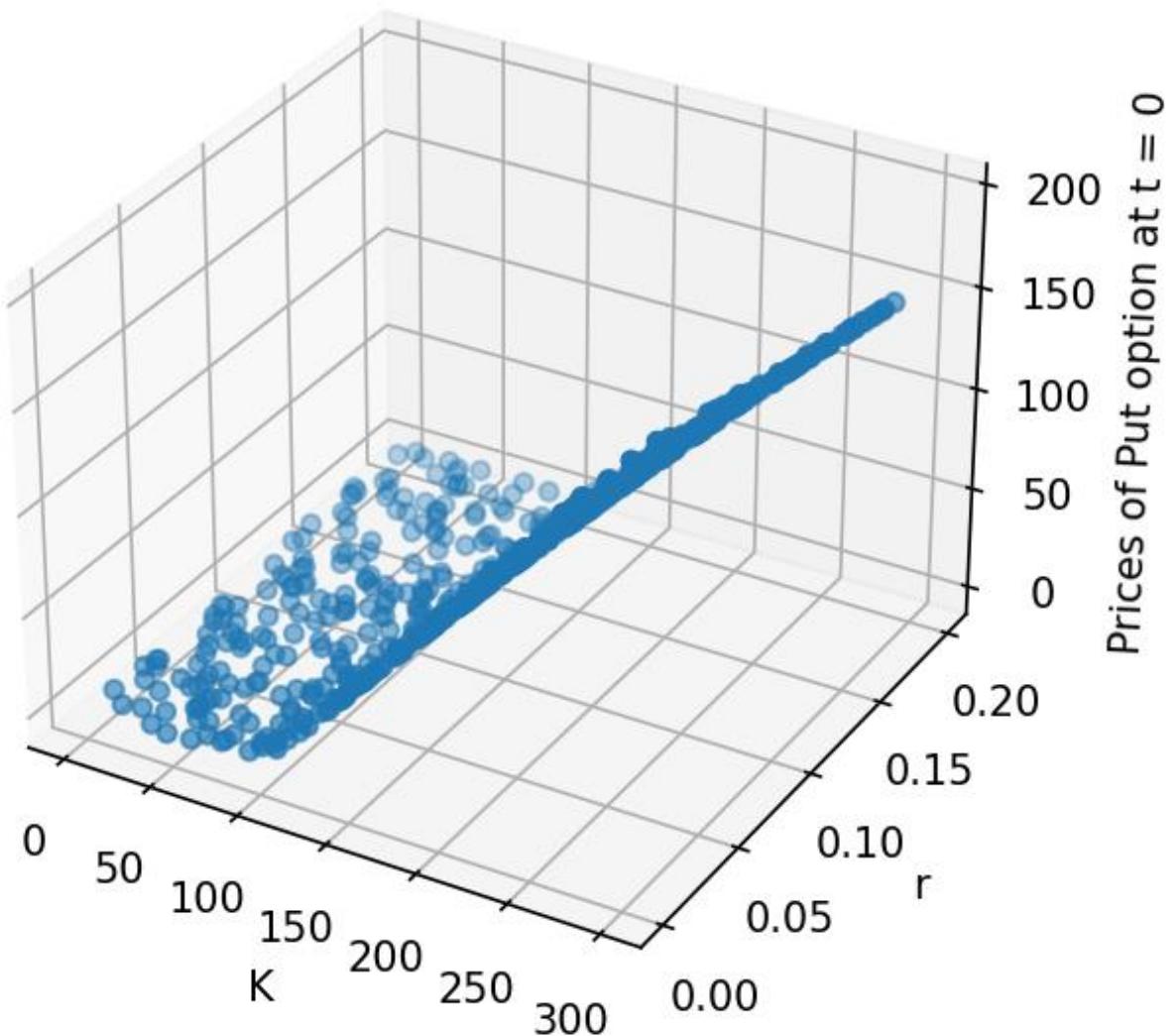
Initial Put Option Price vs K and r for the set = 1



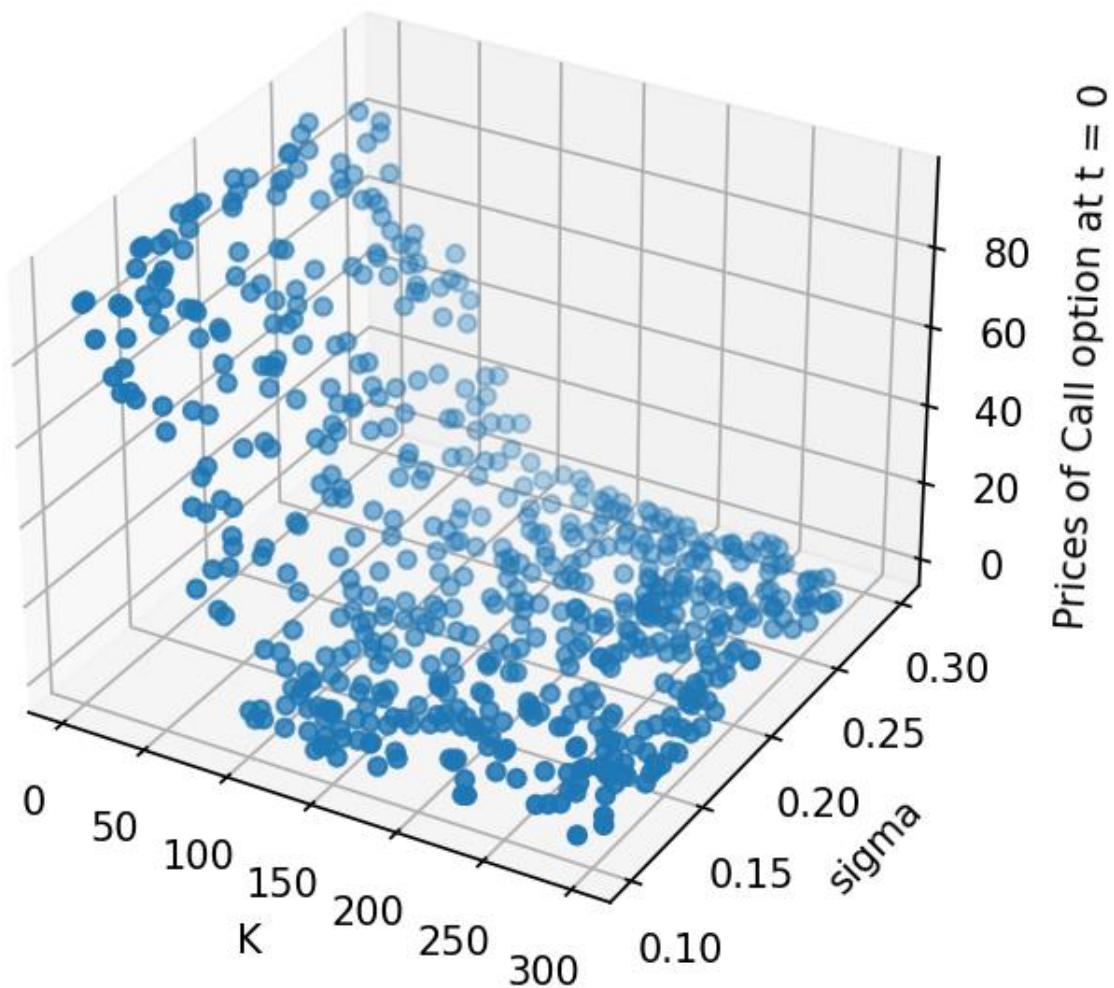
Initial Call Option Price vs K and r for the set = 2



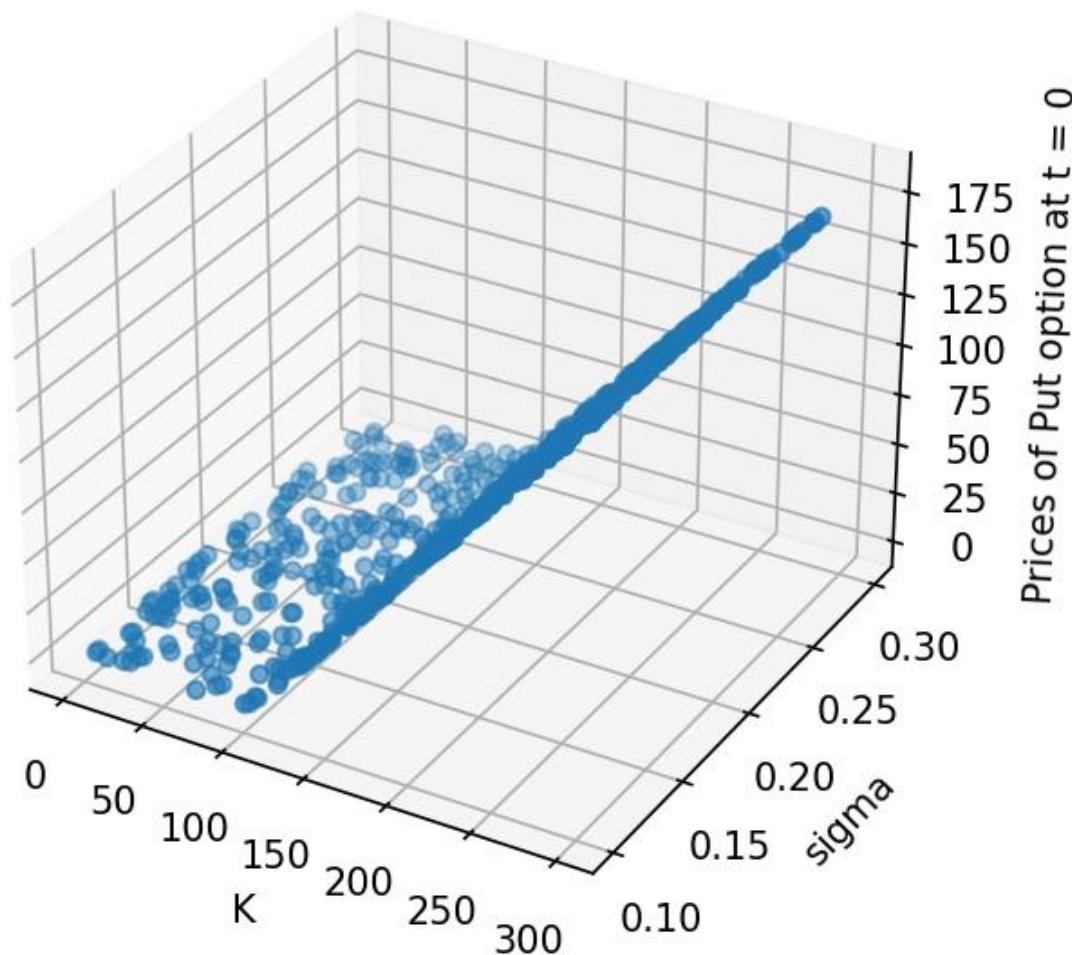
Initial Put Option Price vs K and r for the set = 2



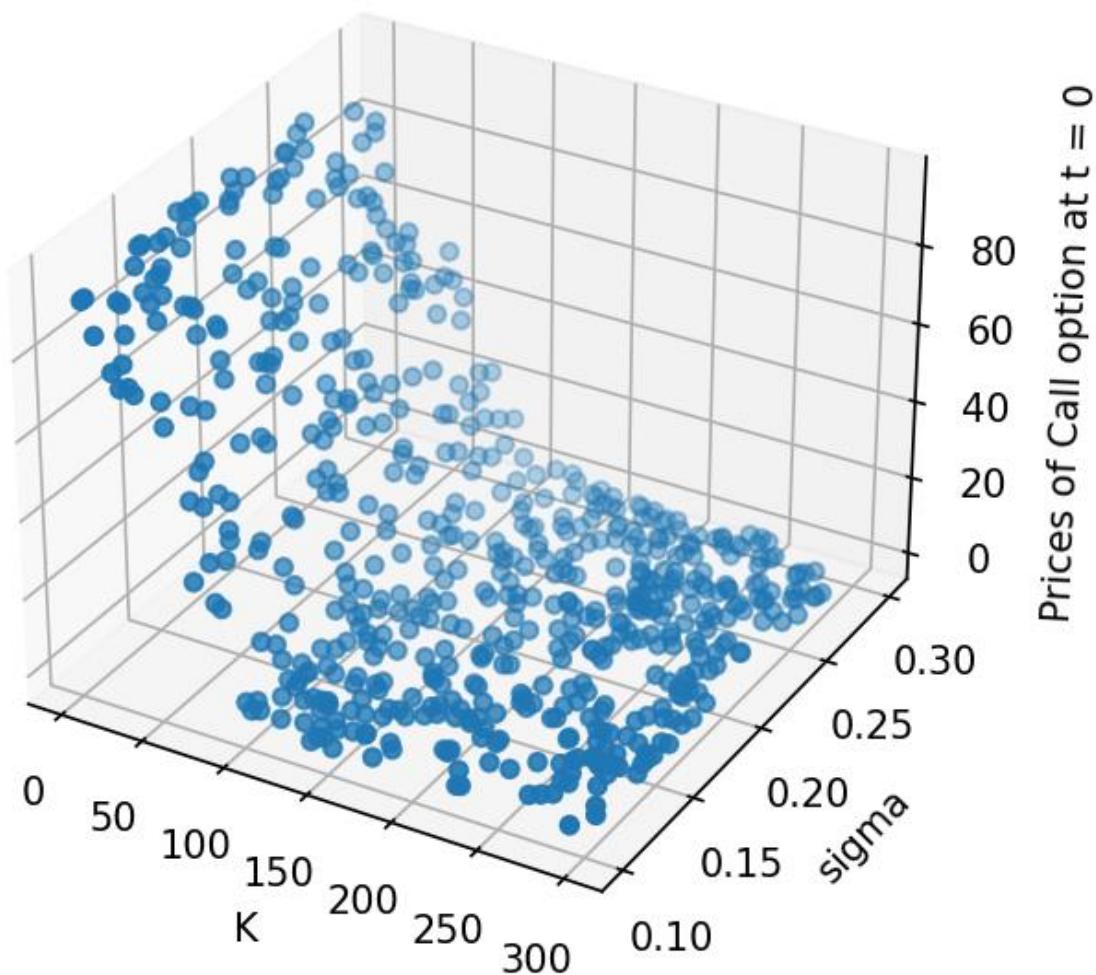
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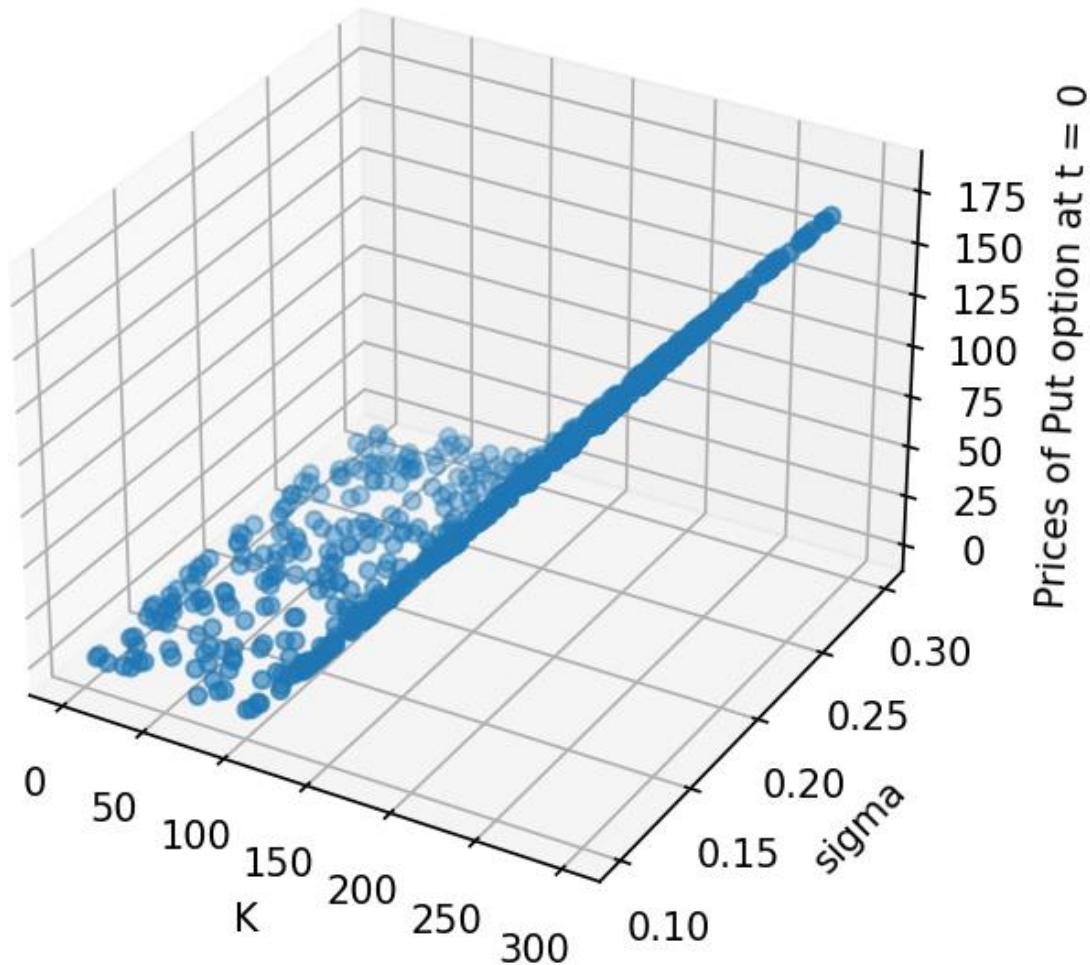
Initial Put Option Price vs K and sigma for the set = 1



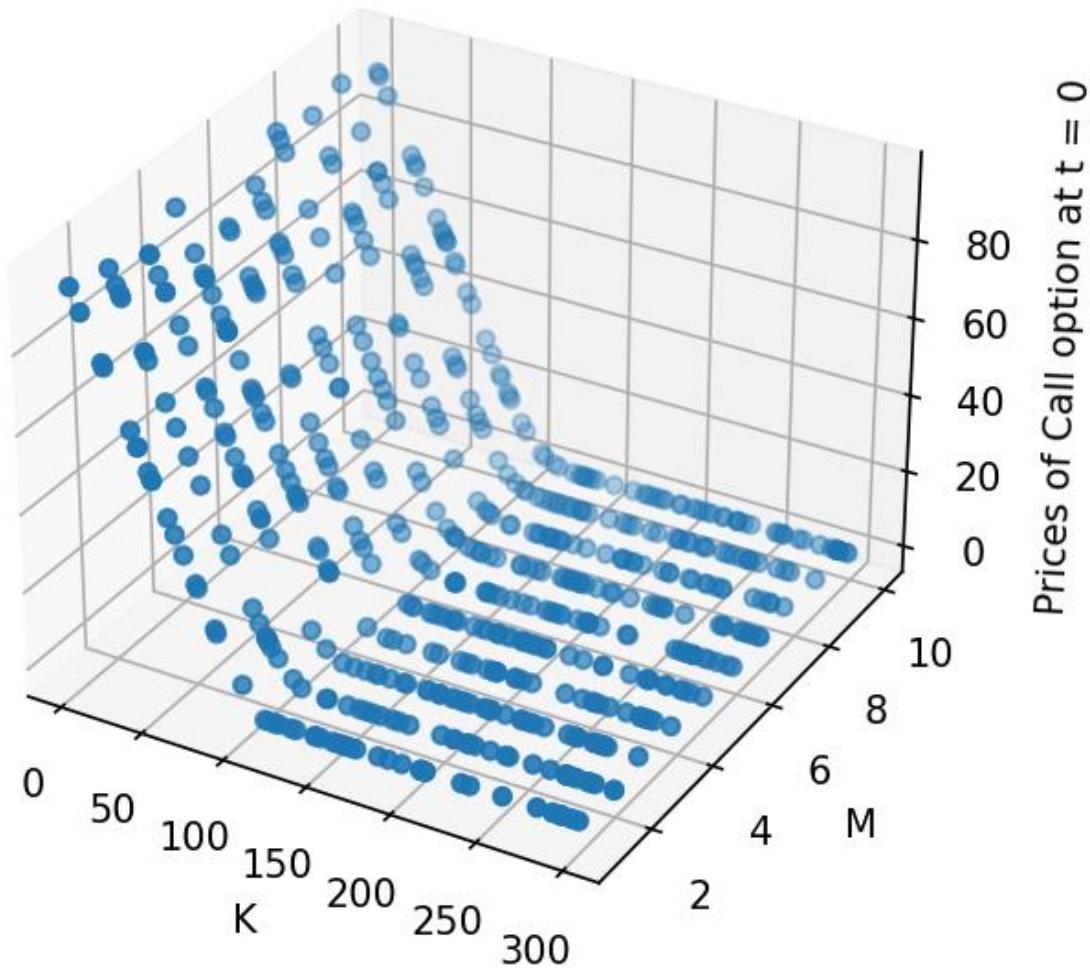
Initial Call Option Price vs K and sigma for the set = 2



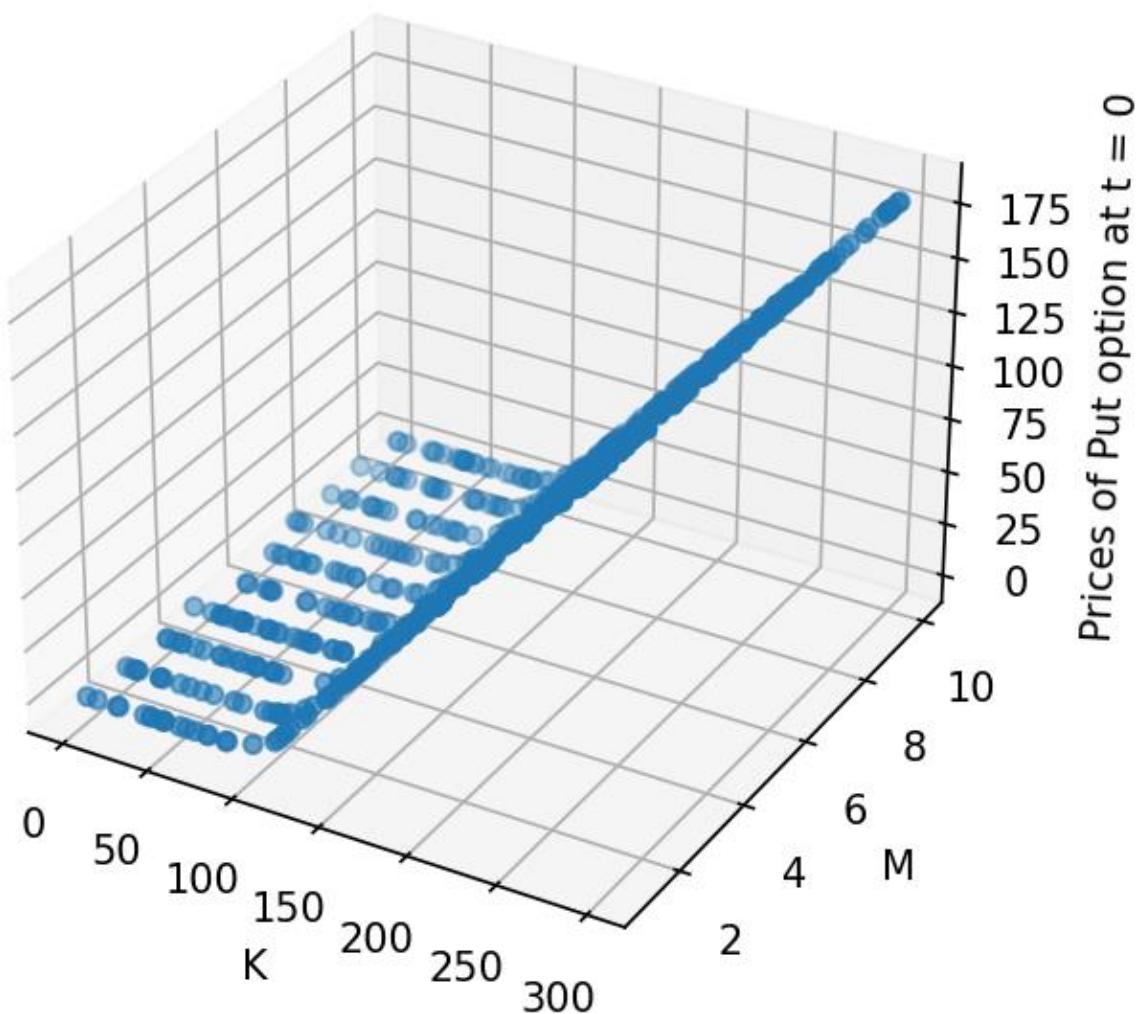
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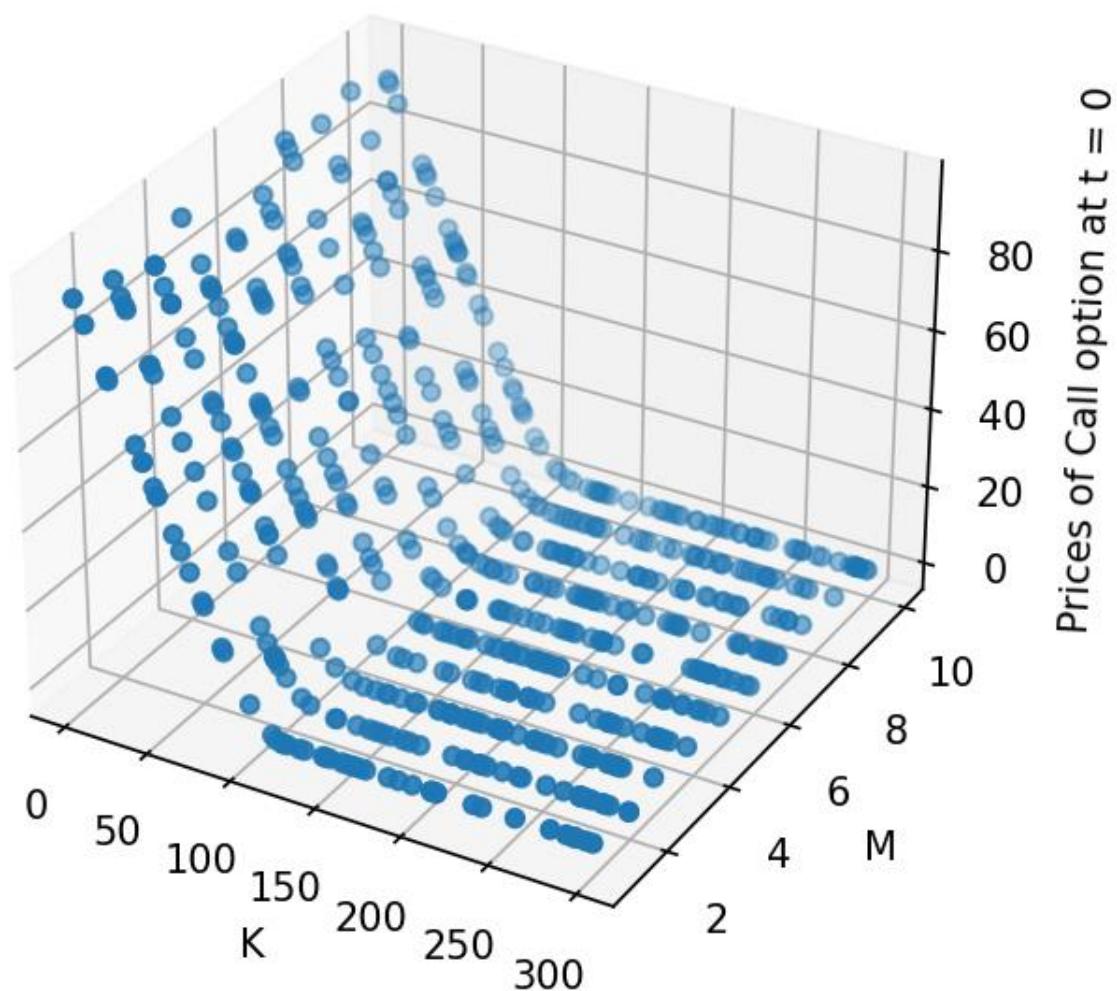
Initial Call Option Price vs K and M for the set = 1



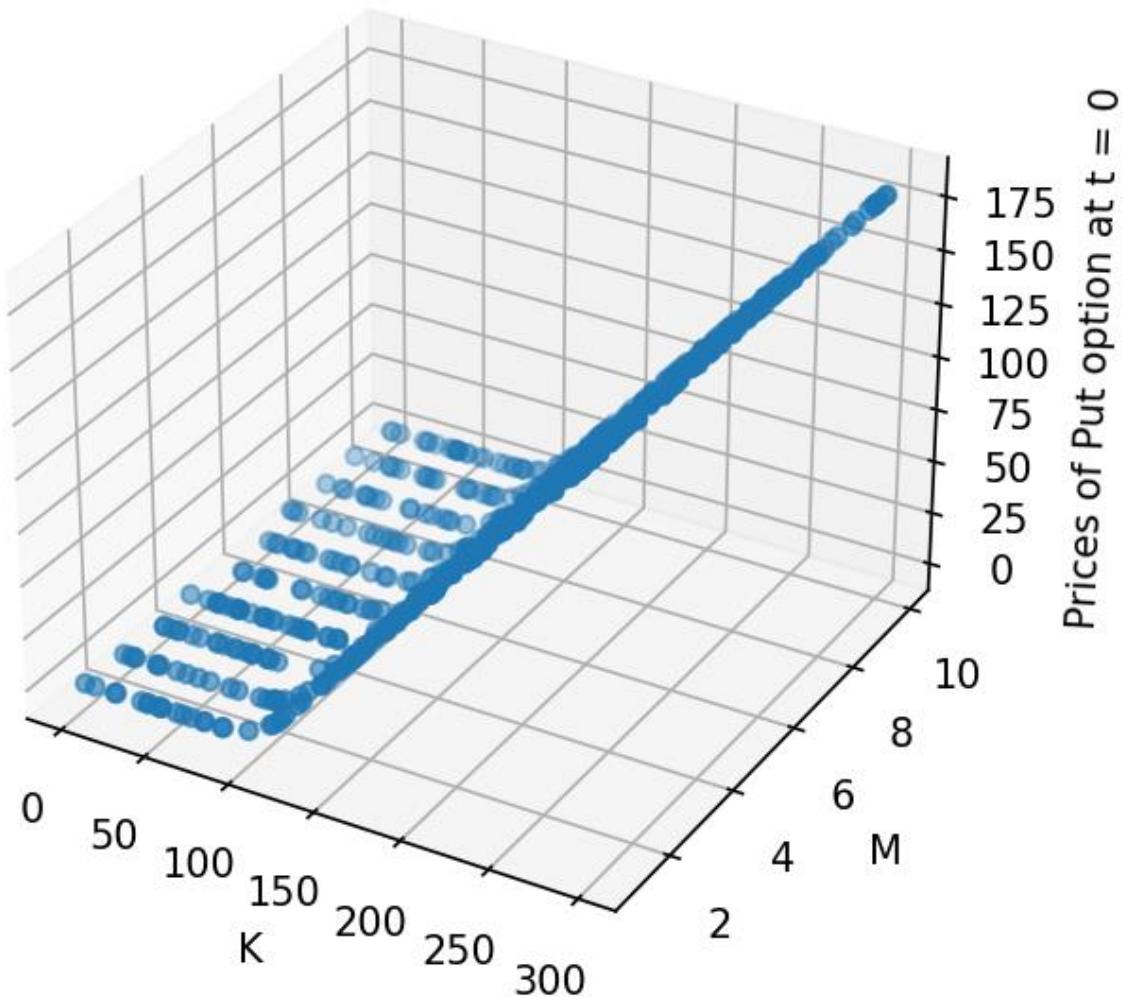
Initial Put Option Price vs K and M for the set = 1



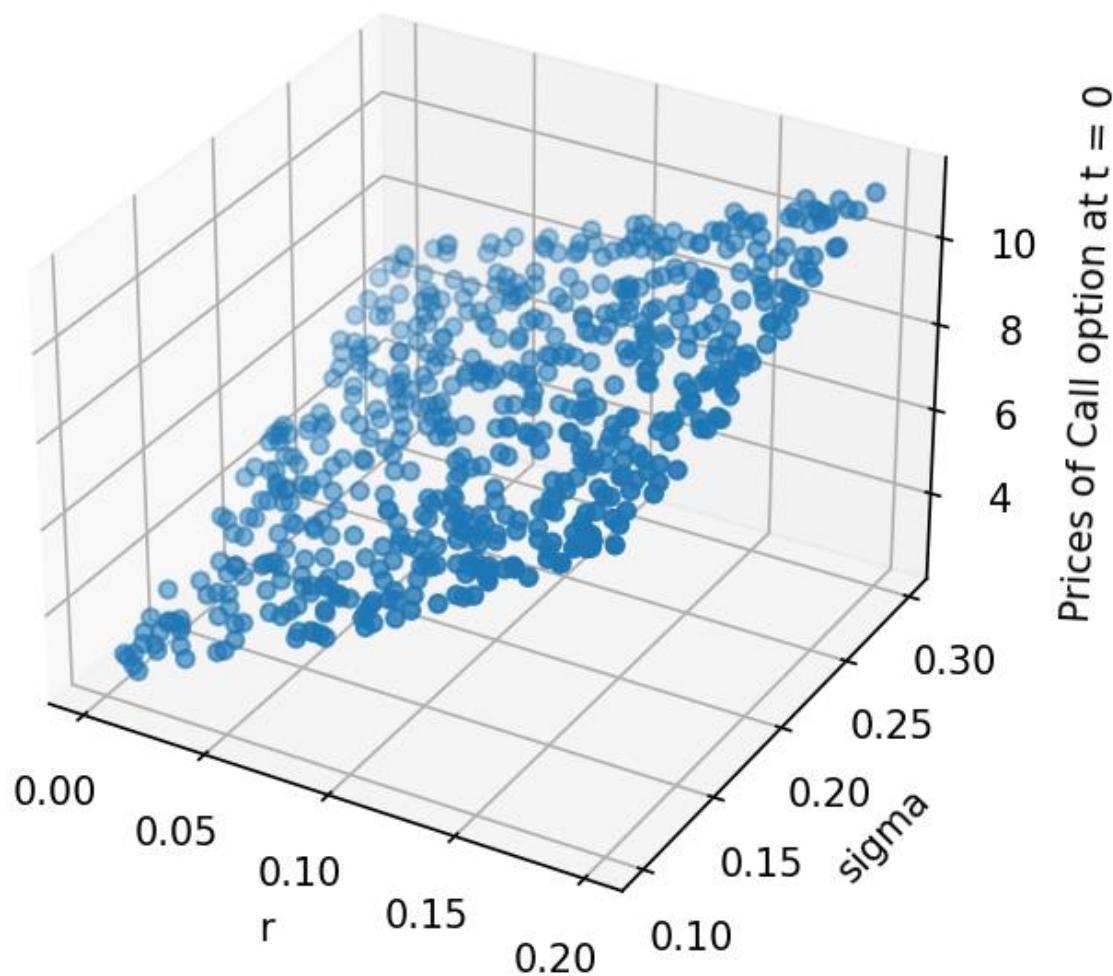
Initial Call Option Price vs K and M for the set = 2



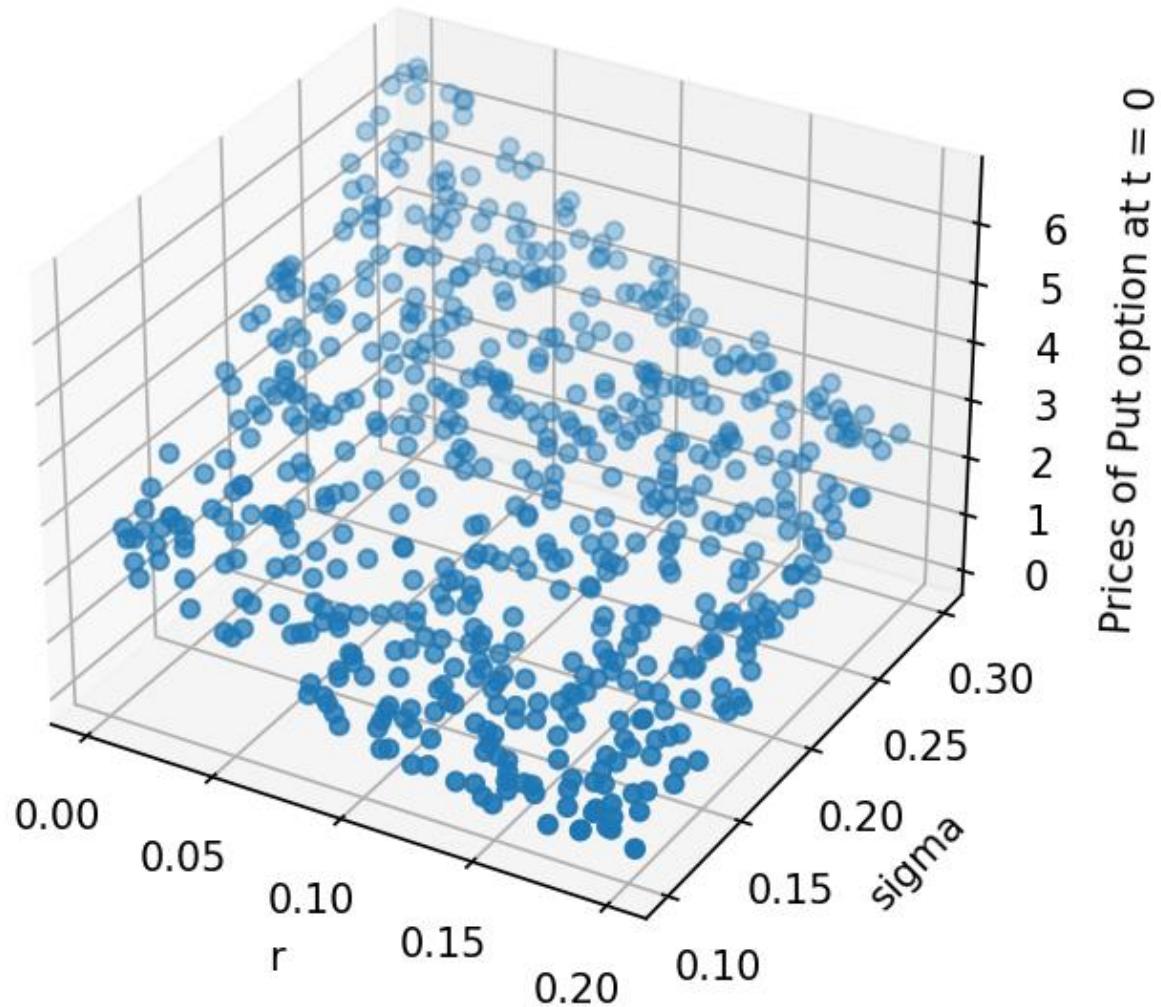
Initial Put Option Price vs K and M for the set = 2



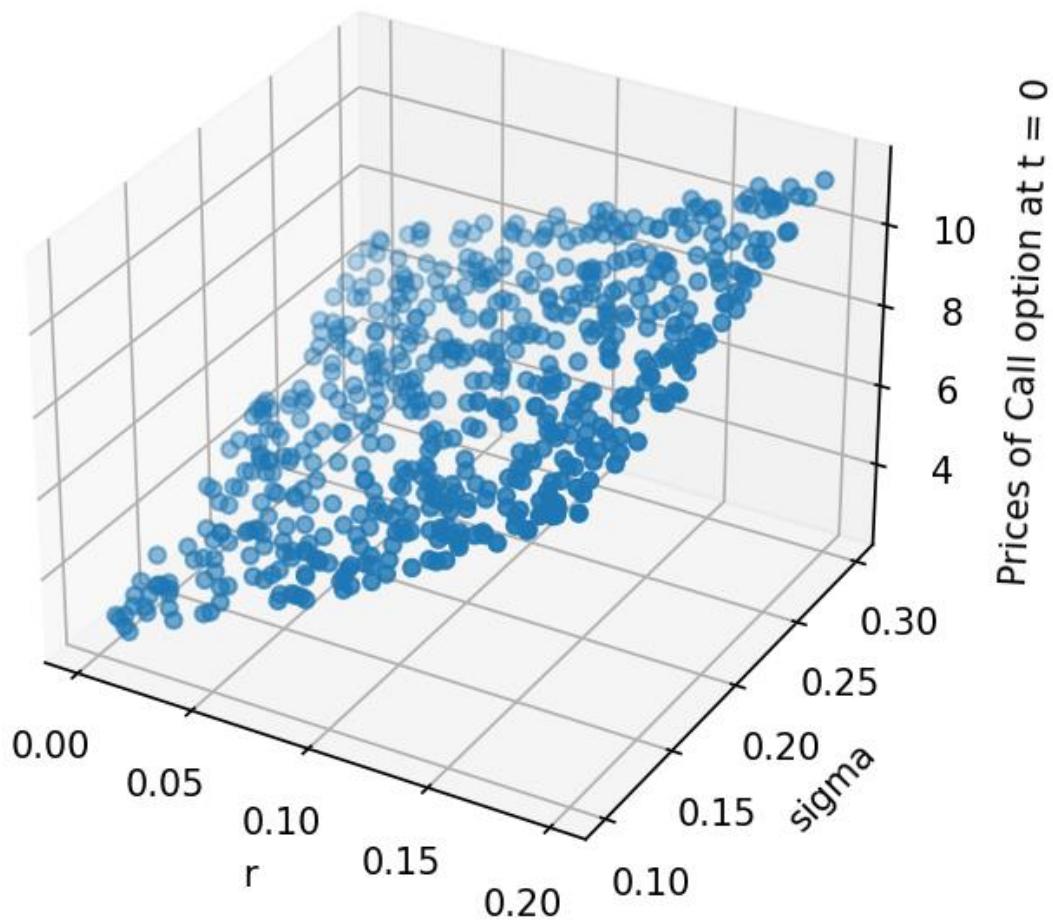
Initial Call Option Price vs r and σ for the set = 1



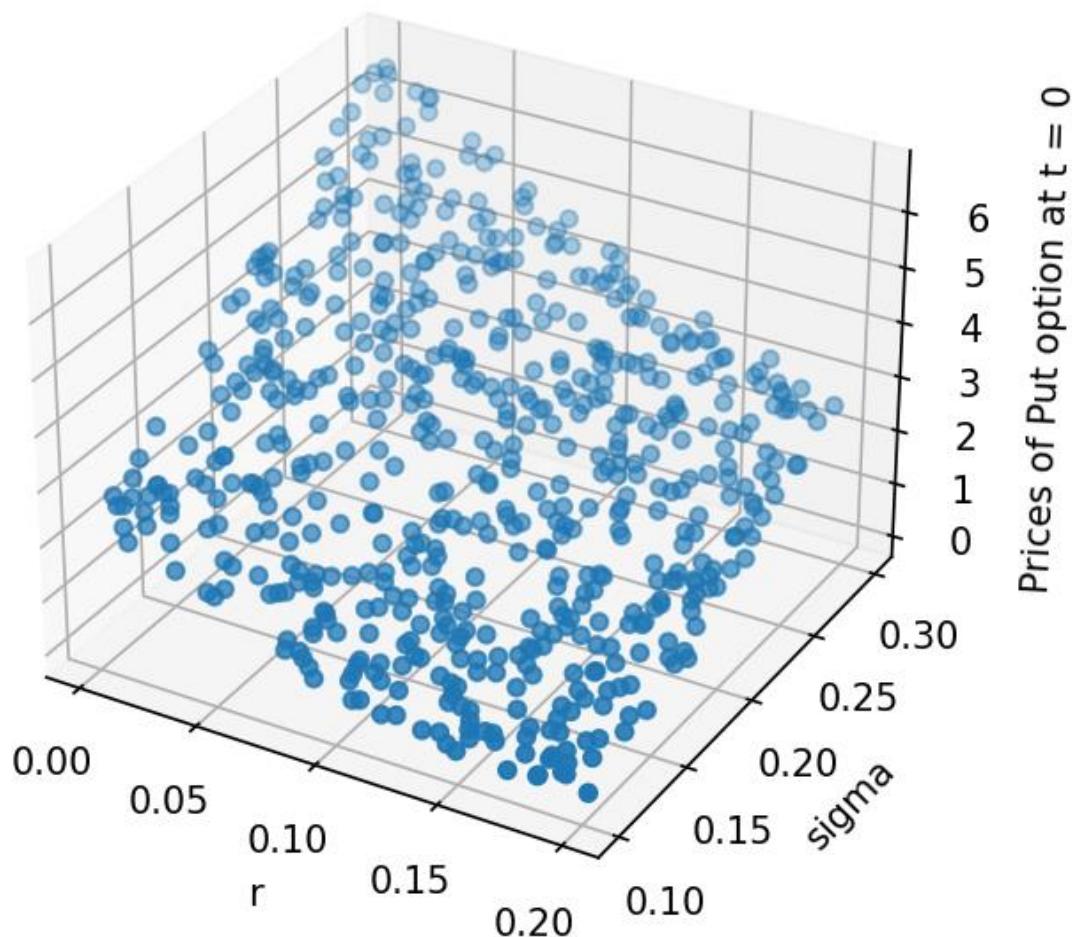
Initial Put Option Price vs r and sigma for the set = 1



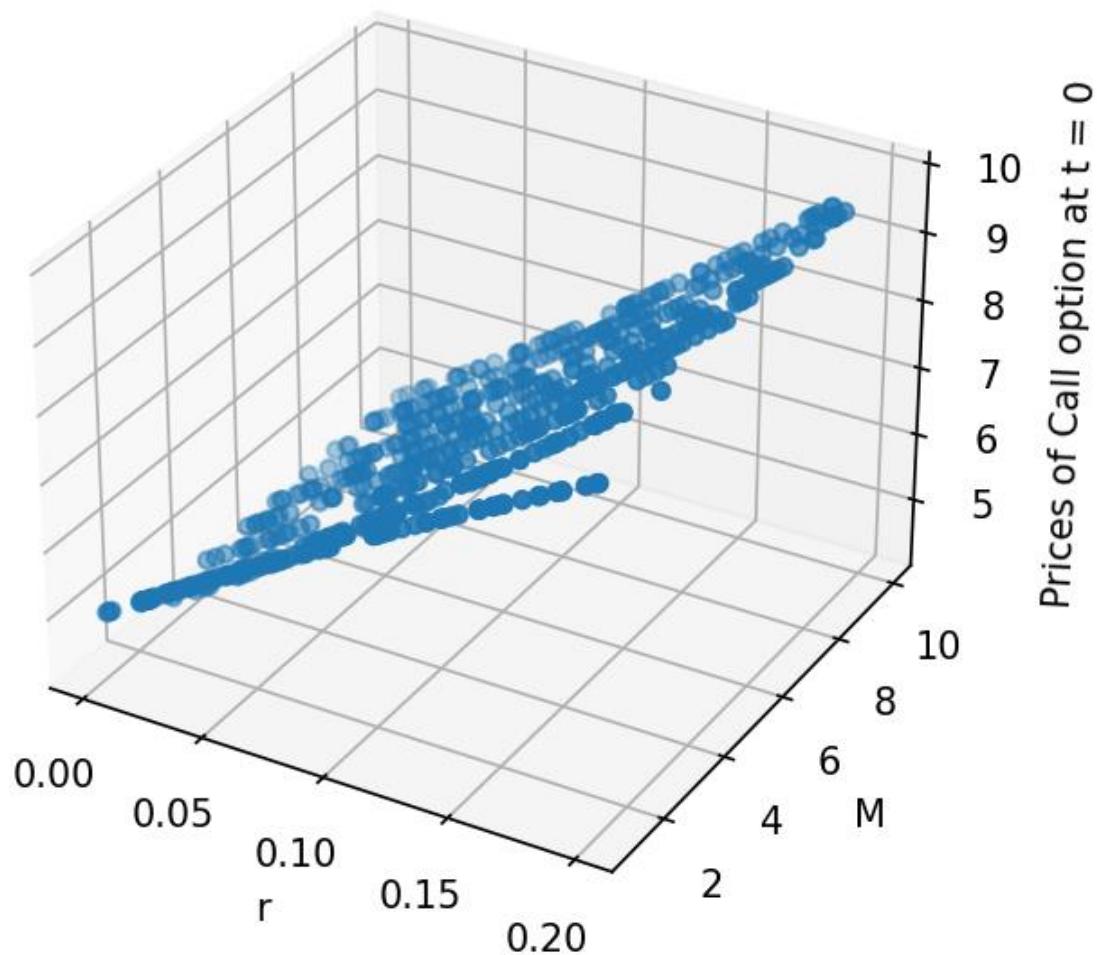
Initial Call Option Price vs r and sigma for the set = 2



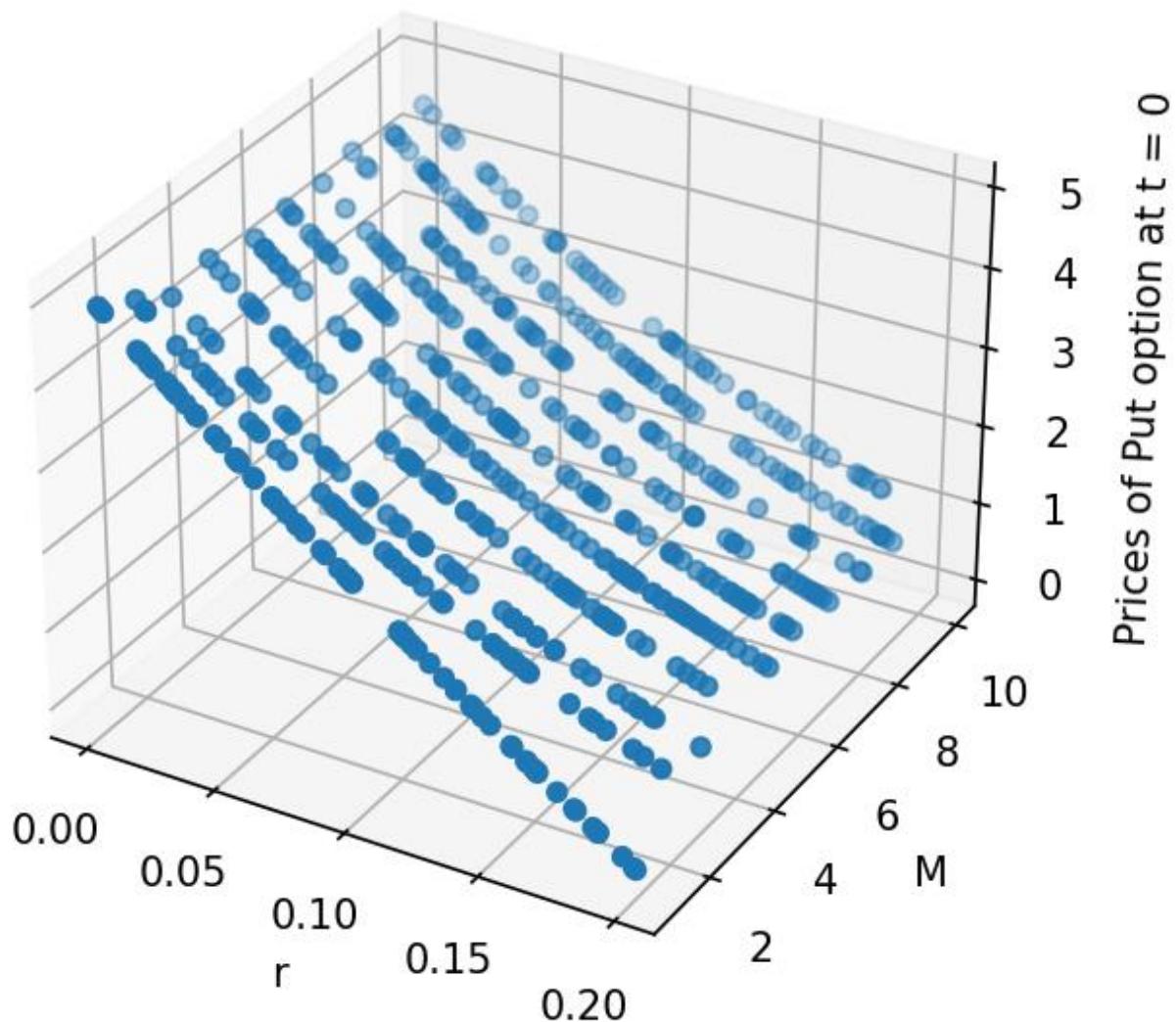
Initial Put Option Price vs r and sigma for the set = 2



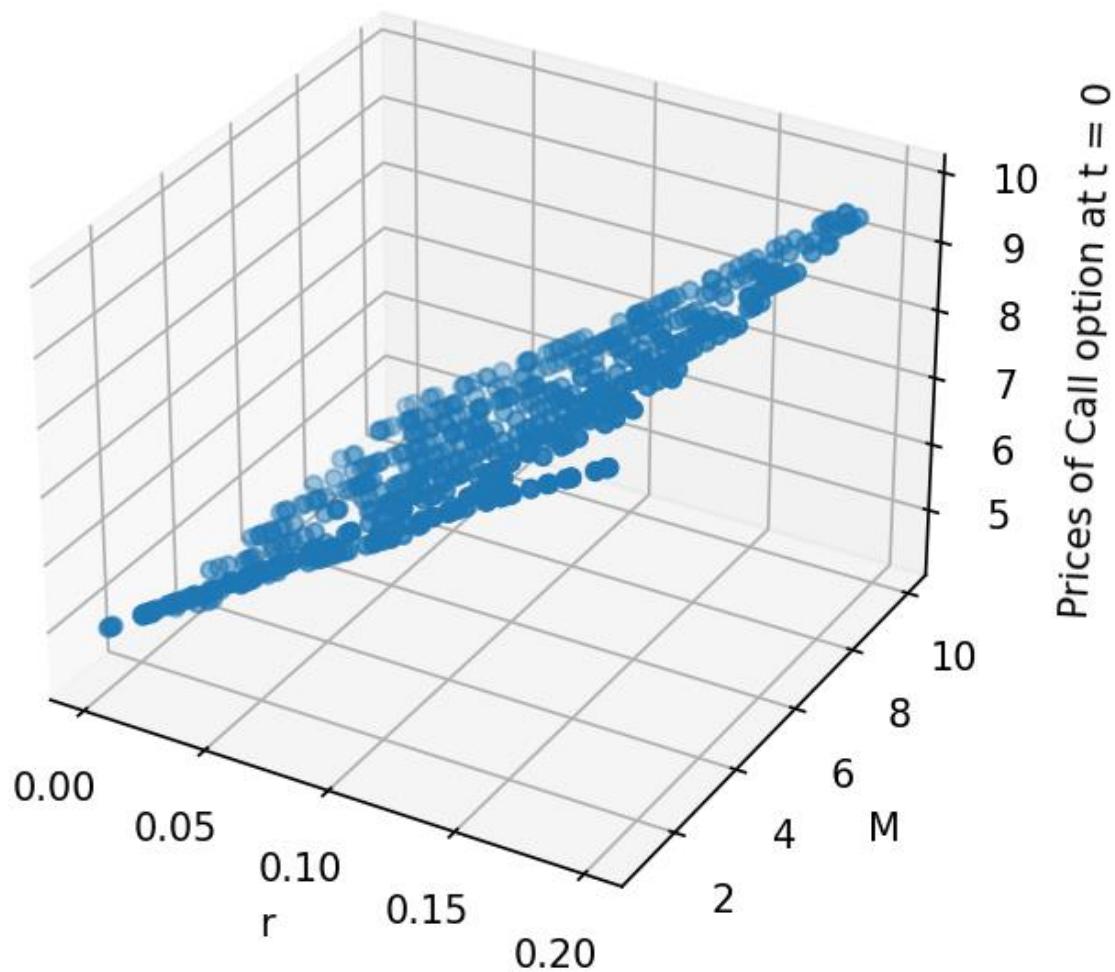
Initial Call Option Price vs r and M for the set = 1



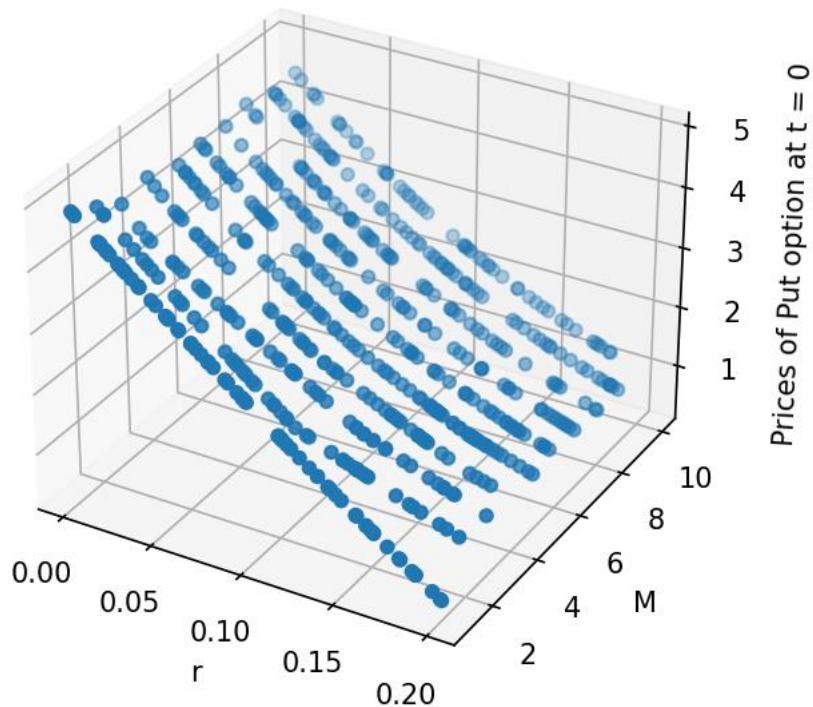
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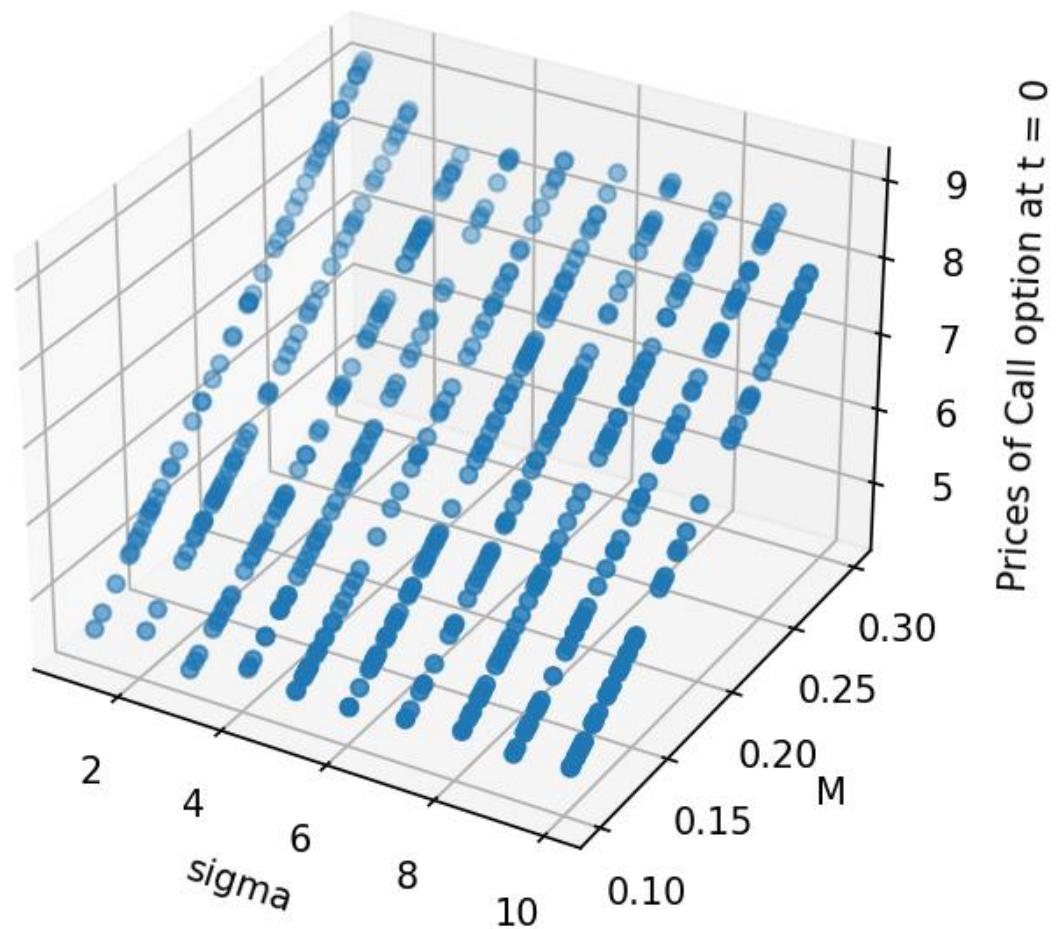
Initial Call Option Price vs r and M for the set = 2



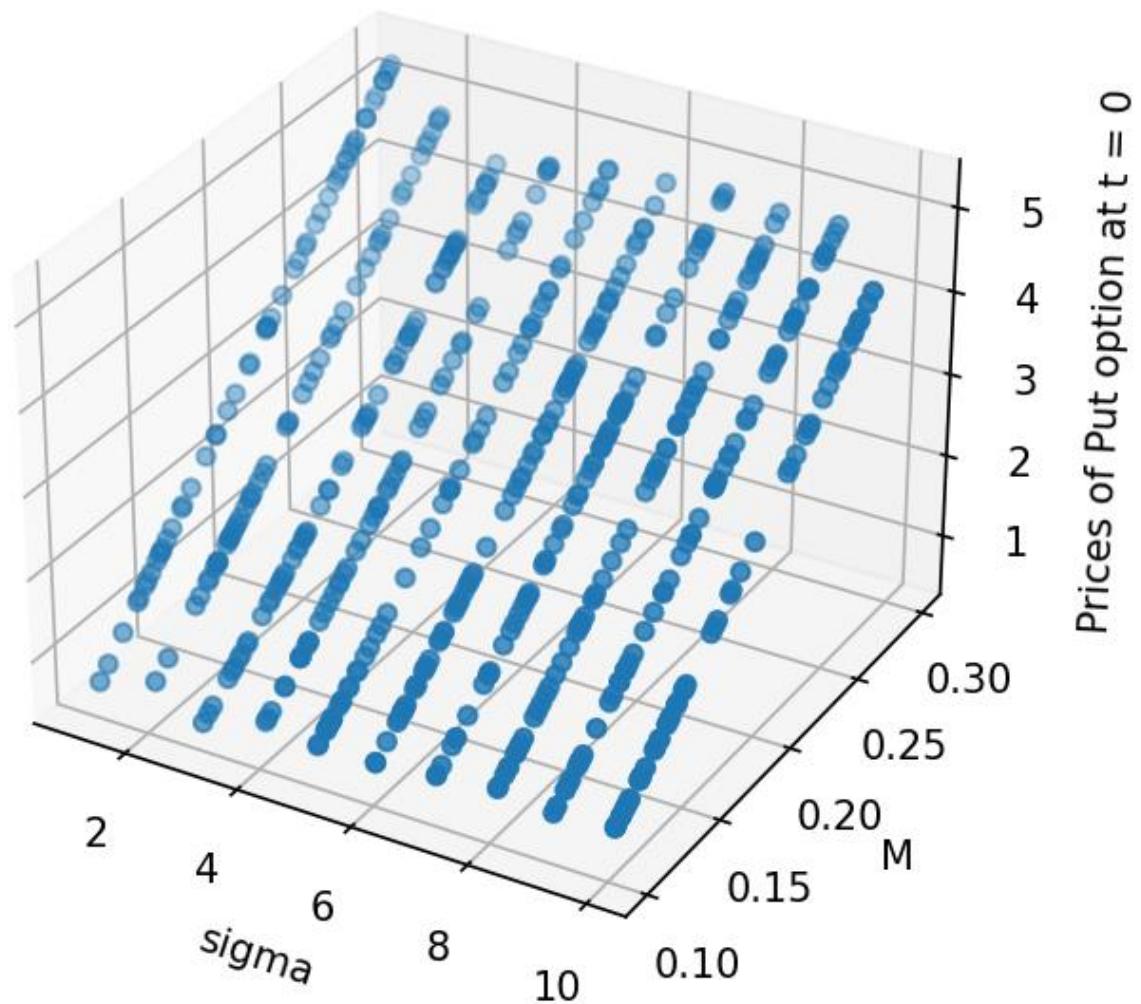
Initial Put Option Price vs r and M for the set = 2



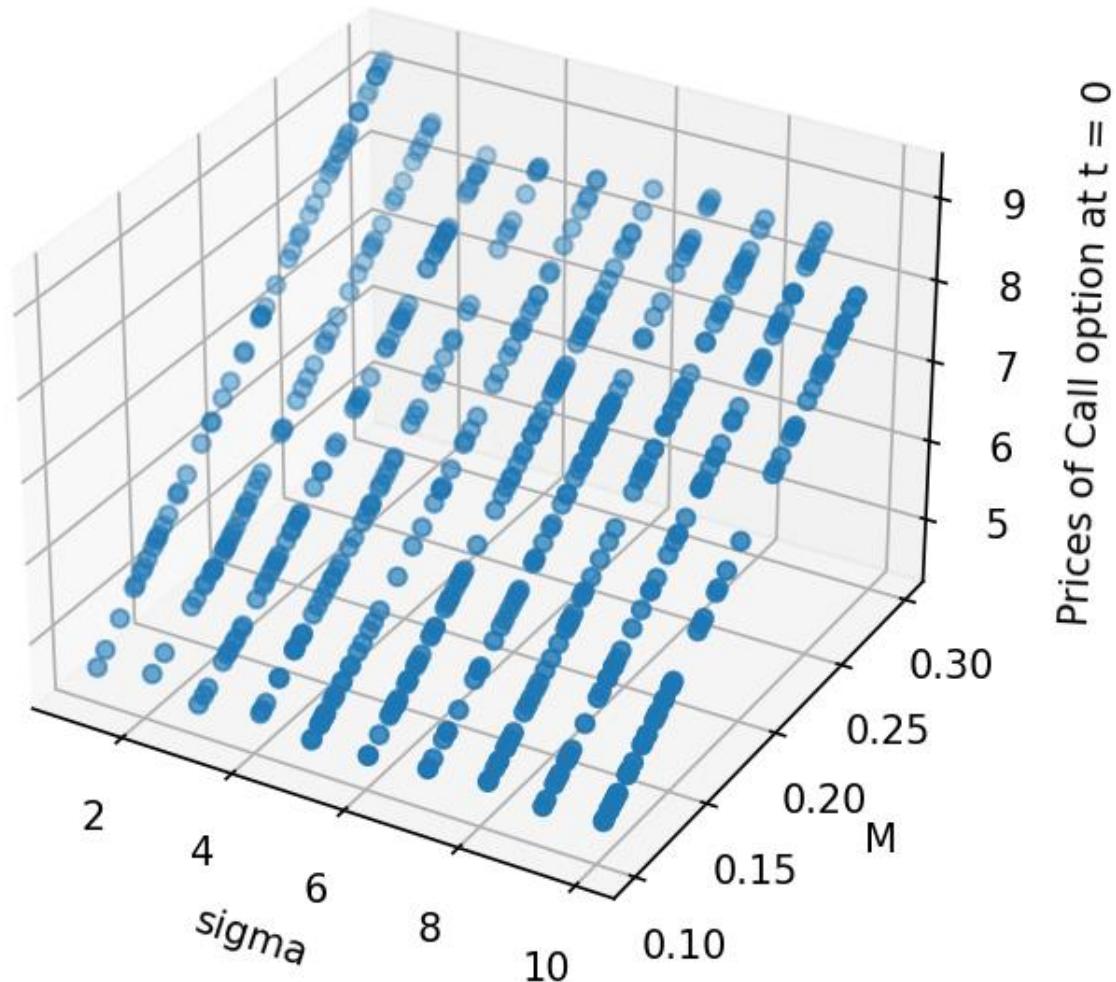
Initial Call Option Price vs sigma and M for the set = 1



Initial Put Option Price vs sigma and M for the set = 1



Initial Call Option Price vs sigma and M for the set = 2



Initial Put Option Price vs sigma and M for the set = 2

