

Week 8: Halting Problem and Undecidability

Mathematical Logic Course

April 24, 2023

Introduction

- ▶ Welcome to Week 8 of our Mathematical Logic Course!
- ▶ This week, we'll explore the Halting Problem and Undecidability.
- ▶ We'll cover the following topics:
 - ▶ Statement and proof of the Halting Problem's undecidability
 - ▶ Reductions and other undecidable problems

The Halting Problem

- ▶ What is the Halting Problem?
- ▶ Formal definition of the Halting Problem
- ▶ Understanding the significance of the Halting Problem in computability theory

Undecidability of the Halting Problem

- ▶ Proof sketch of the undecidability of the Halting Problem
- ▶ The paradox of the self-referential machine
- ▶ Understanding the implications of undecidability

Reductions and Other Undecidable Problems

- ▶ The concept of reductions between problems
- ▶ Examples of problems that are reducible to the Halting Problem
- ▶ Exploring a variety of undecidable problems in computer science

Summary and Conclusion

- ▶ Recap of the topics covered in this lecture
- ▶ The Halting Problem and its undecidability
- ▶ Understanding the limits of algorithmic computation
- ▶ Next week, we'll explore Complexity Theory and P vs NP

Questions and Discussion

- ▶ Do you have any questions about today's lecture?
- ▶ Let's discuss the material and explore any questions you may have

Coding Exercises

- ▶ Exploring examples of undecidable problems in Python
- ▶ Understanding the concept of reductions through coding exercises