

Meta-MeTTa: an operational semantics for MeTTa

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Abstract. We make the case for a reflective multi-agent formalism.

1 Towards a common language

Three of the most successful branches of scientific discourse all agree on the shape of a model adequate for expressing and effecting computation. Physics, computer science, and mathematics all use the same standard shape. A model adequate for computation comes with an algebra of states and “laws of motion.”

One paradigmatic example from physics is Hilbert spaces and the Schroedinger equation. In computer science and mathematics the algebra of states is further broken down into a monad (the free algebra of states) and an algebra of the monad recorded as some equations on the free algebra.

Computer science represents laws of motion, aka state transitions, as rewrite rules exploiting the structure of states to determine transitions to new states. Mainstream mathematics is a more recognizable generalization of physics, coding state transitions, aka behavior, via morphisms (including automorphisms) between state spaces.

But all three agree to a high degree of specificity on what ingredients go into a formal presentation adequate for effecting computation.

1.1 Examples from computer science

λ -calculus TBD

π -calculus TBD

rho-calculus

The JVM TBD

2 A presentation of the semantics of MeTTa

A presentation of the semantics of MeTTa must therefore provide a monad describing the algebra of states, a structural equivalence quotienting the algebra of states, and some rewrite rules describing state transitions. Such a description is the minimal description that meets the standard for describing models of computation. Note that to present such a description requires at least that much expressive power in the system used to formalize the presentation. That is, the system used to present a model of computation is itself a model of computation admitting a presentation in terms of an algebra of states and some rewrites. This is why a meta-circular evaluator is a perfectly legitimate presentation. That is, a presentation of MeTTa’s semantics in MeTTa is perfectly legitimate. Meta-circular presentations are more difficult to unpack, which is why such presentations are typically eschewed, but they are admissible. In fact, a meta-circular evaluator may be the most pure form of presentation.

But, this fact has an important consequence. No model that is at least Turing complete can be “lower level” than any

2.1 Rationale for such a presentation

The rationale for such a presentation is not simply that this is the way it's done. Instead, the benefits include

- an effective (if undecidable) notion of program equality;
- an independent specification allowing implementations;
- meta-level computation, including type checking, model checking, macros, computational reflection, etc.

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