Generating a radially separable dataset

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Generating a 2d uniformly distributed set of points

- Generate a dataset with 200 points
 - o 2 predictors x1 and x2, uniformly distributed between -1 and 1.

Create a circular boundary

- Create a circular decision boundary of radius 0.7 units.
- Categorical variable y is +1 or -1 depending on the point lies outside or within boundary.

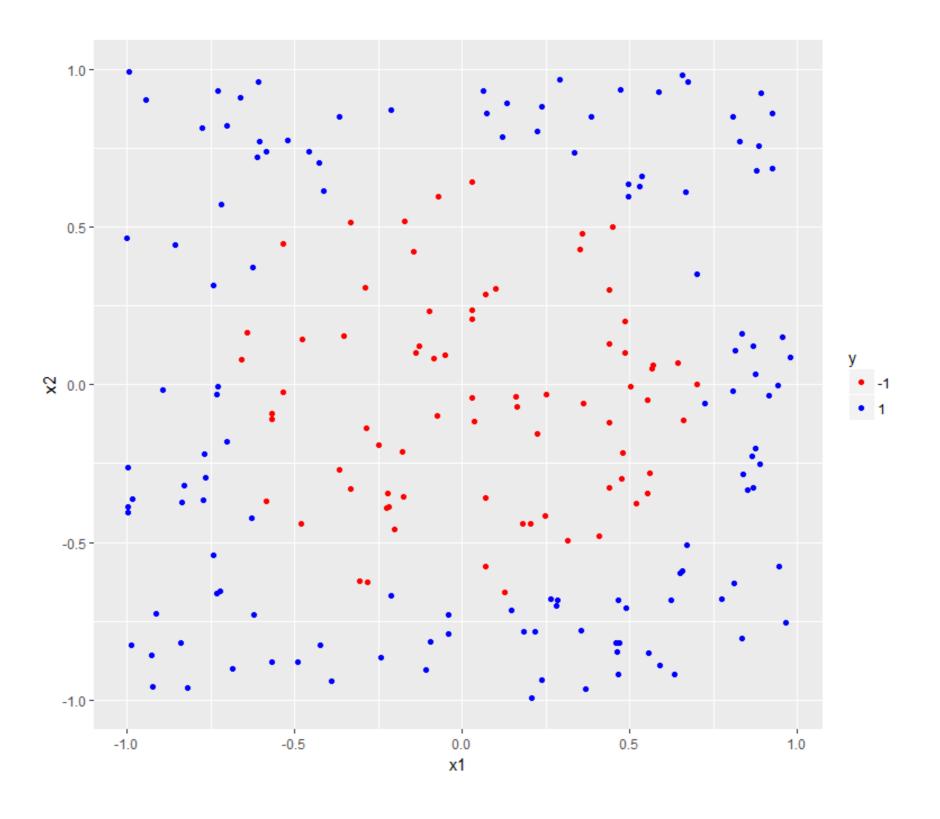
Plot the dataset

• Visualize using ggplot.

```
library(ggplot2)
```

• predictors plotted on 2 axes; classes distinguished by color.

```
# Build plot
p <- ggplot(data = df, aes(x = x1, y = x2, color = y)) +
        geom_point() +
        scale_color_manual(values = c("-1" = "red", "1" = "blue"))
# Display plot
p</pre>
```



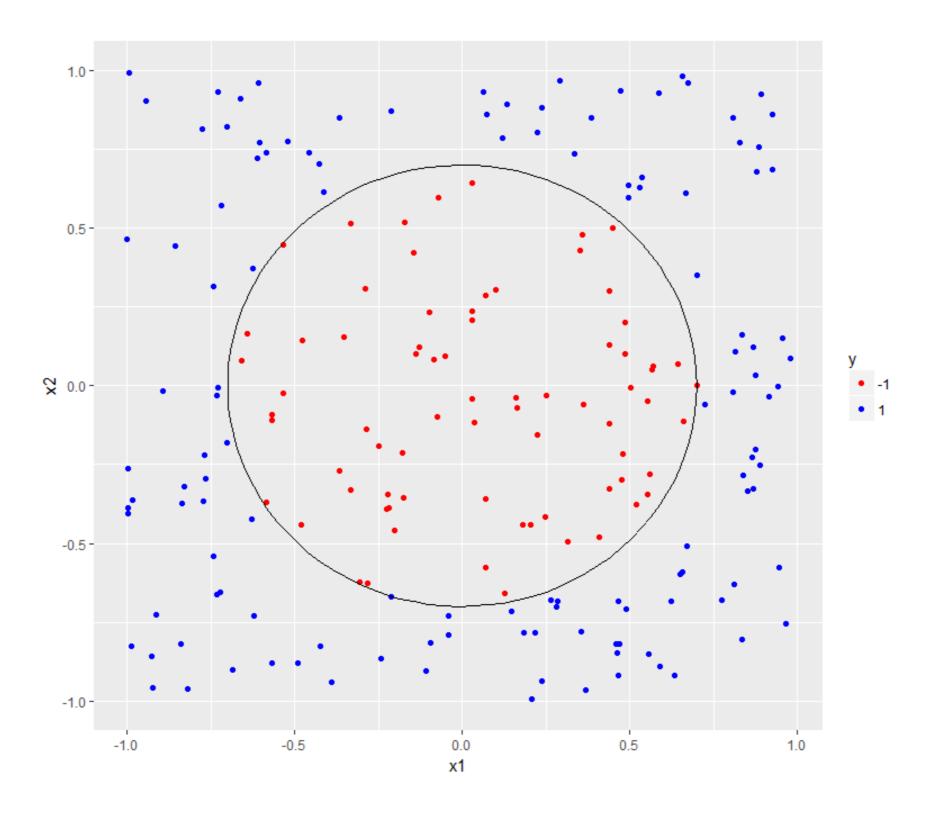
Adding a circular boundary - Part 1

• We'll create a function to generate a circle

```
# Function generates dataframe with points
# lying on a circle of radius r
circle <-
  function(x1_center, x2_center, r, npoint = 100) {
  # Angular spacing of 2*pi/npoint between points
  theta \leftarrow seq(0, 2 * pi, length.out = npoint)
  x1_circ <- x1_center + r * cos(theta)</pre>
  x2_circ <- x2_center + r * sin(theta)
  data.frame(x1c = x1_circ, x2c = x2_circ)
```

Adding a circular boundary - Part 2

- To add boundary to plot:
 - generate boundary using circle() function.
 - add boundary to plot using geom_path()



Time to practice!

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Linear SVMs on radially separable data

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Linear SVM, cost = 1

Partition radially separable dataset into training/test (seed = 10)

```
# Build default cost linear SVM on training set
svm_model <- svm(y ~ ., data = trainset, type = "C-classification", kernel = "linear")
svm_model</pre>
```

Number of Support Vectors: 126

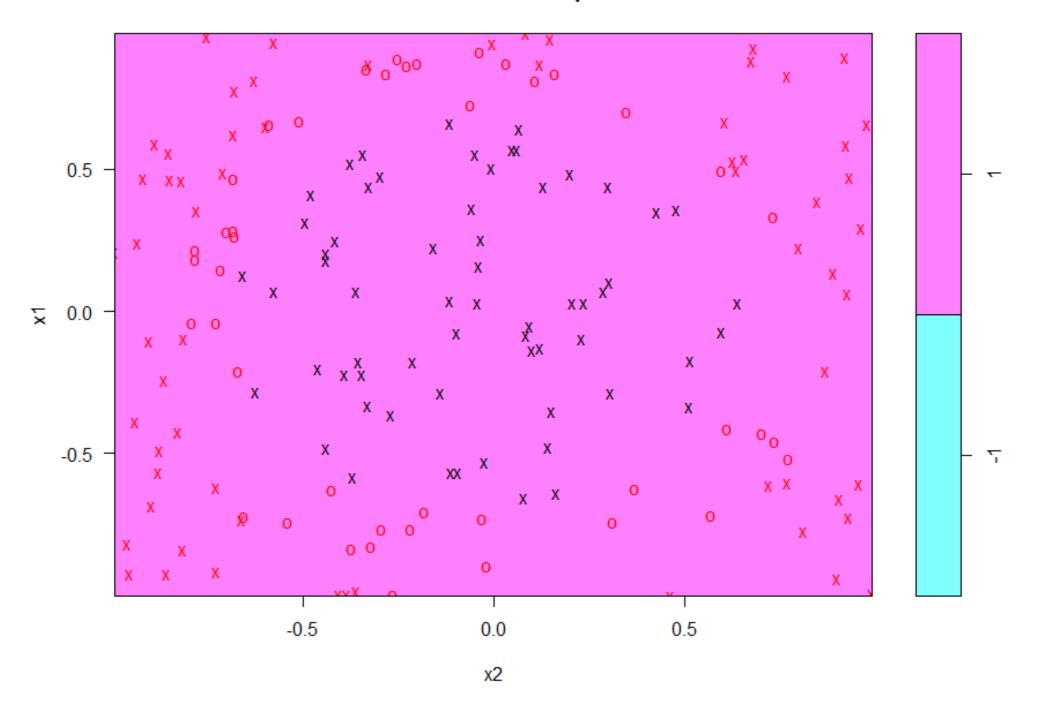
```
# Calculate accuracy on test set
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

0.6129032

```
plot(svm_model, trainset)
```



SVM classification plot



Linear SVM, cost = 100

```
svm_model <- svm(y ~ ., data = trainset, type = "C-classification", kernel = "linear")
svm_model</pre>
```

Number of Support Vectors: 136

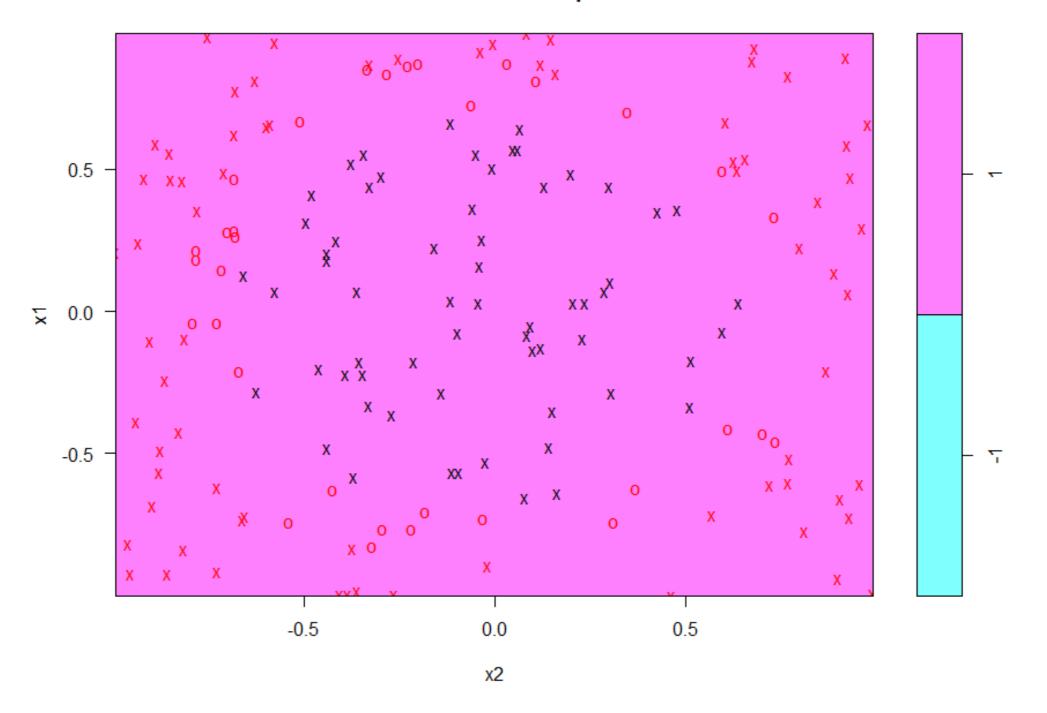
```
# Accuracy
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

0.6129032

```
plot(svm_model, trainset)
```



SVM classification plot



A better estimate of accuracy

- Calculate average accuracy over a number of independent train/test splits.
- Check standard deviation of result to get an idea of variability.

Average accuracy for default cost SVM

```
accuracy <- rep(NA, 100)
set.seed(10)
for (i in 1:100) {
  df[, "train"] <- ifelse(runif(nrow(df)) < 0.8, 1, 0)</pre>
  trainset <- df[df$train == 1, ]
  testset <- df[df$train == 0, ]
  trainColNum <- grep("train", names(trainset))</pre>
  trainset <- trainset[, -trainColNum]</pre>
  testset <- testset[, -trainColNum]</pre>
  svm_model<- svm(y ~ ., data = trainset, type = "C-classification", cost = 1, kernel = "linear")
  pred_test <- predict(svm_model, testset)</pre>
  accuracy[i] <- mean(pred_test == testset$y)}</pre>
mean(accuracy)
sd(accuracy)
```

```
0.642843
0.07606017
```



How well does a linear SVM perform?

- Marginally better than a coin toss!
- We can use our knowledge of the boundary to do much better.

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The kernel trick

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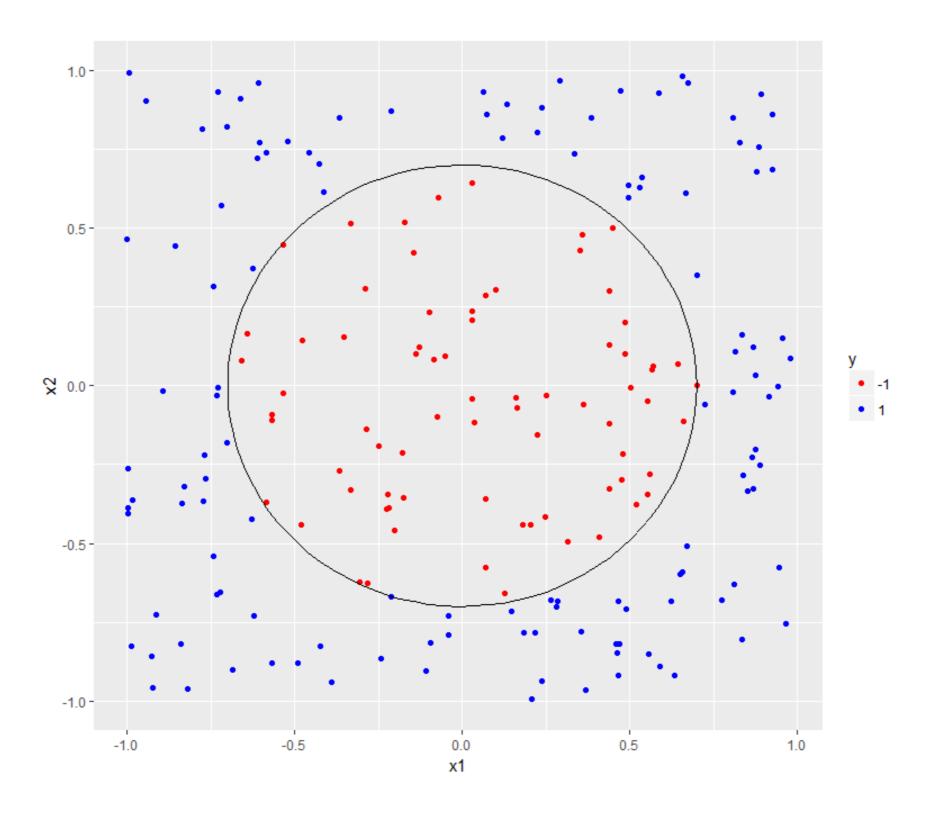


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The basic idea

- Devise a transformation that makes the problem linearly separable.
- We'll see how to do this for a radially separable dataset.



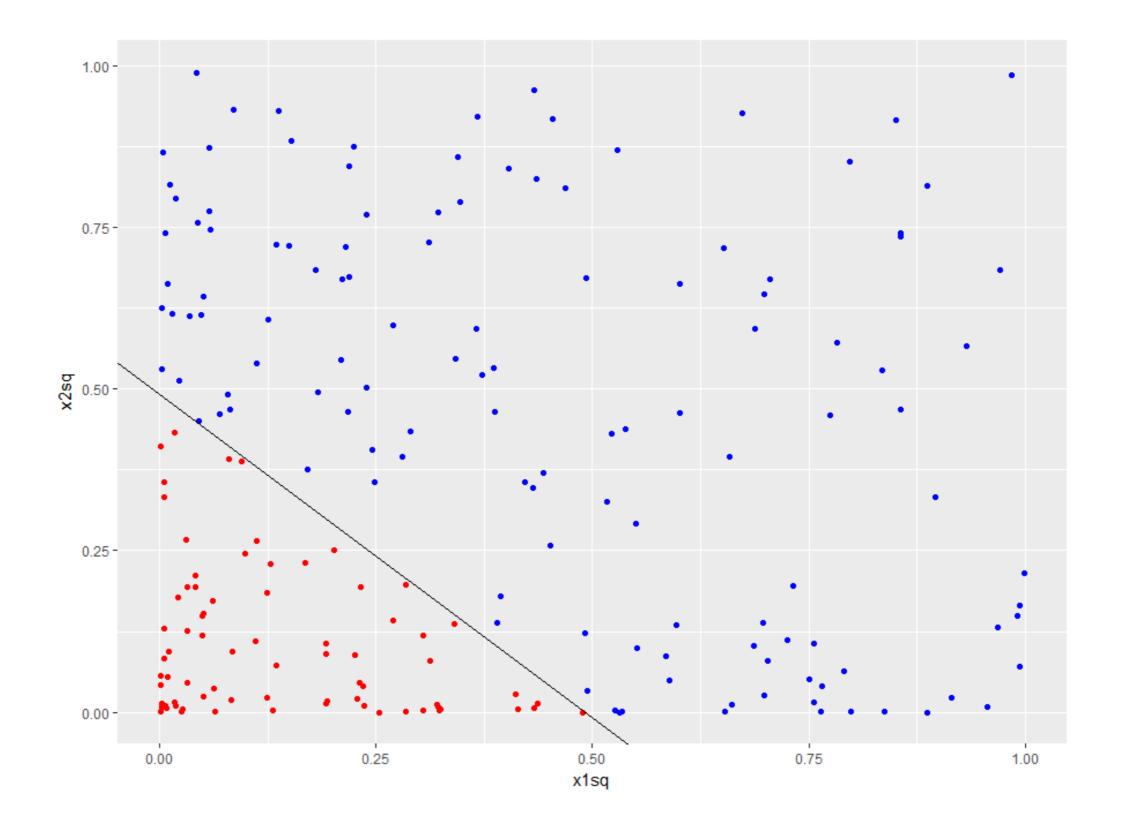
Transforming the problem

- Equation of boundary is $x_1^2+x_2^2=0.49$
- ullet Map x_1^2 to a new variable X_1 and x_2^2 to X_2
- ullet The equation of boundary in the X_1-X_2 space becomes...
- $X_1 + X_2 = 0.49$ (a line!!)

Plot in X1-X2 space - code

- ullet Use ${ t ggplot()}$ to plot the dataset in X_1-X_2 space
- Equation of boundary $X_2 = -X_1 + 0.49$:
 - \circ slope = -1
 - $\circ yintercept = 0.49$

```
p <- ggplot(data = df4, aes(x = x1sq, y = x2sq, color = y)) +
   geom_point() +
   scale_color_manual(values = c("red", "blue")) +
   geom_abline(slope = -1, intercept = 0.49)</pre>
```





The Polynomial Kernel - Part 1

- Polynomial kernel: (gamma * (u.v) + coef0) ^ degree
 - degree is the degree of the polynomial
 - o gamma and coef0 are tuning parameters
 - o u, v are vectors (datapoints) belonging to the dataset
- We can guess we need a 2nd degree polynomial (transformation)

Kernel functions

- The math formulation of SVMs requires transformations with specific properties.
- Functions satisfying these properties are called kernel functions
- Kernel functions are generalizations of vector dot products
- *Basic idea** use a kernel that separates the data well!

Radially separable dataset - quadratic kernel

- 80/20 train/test split
- Build a quadratic SVM for the radially separable dataset:
 - Set degree = 2
 - Set default values of cost, gamma and coef0 (1, 1/2 and 0)

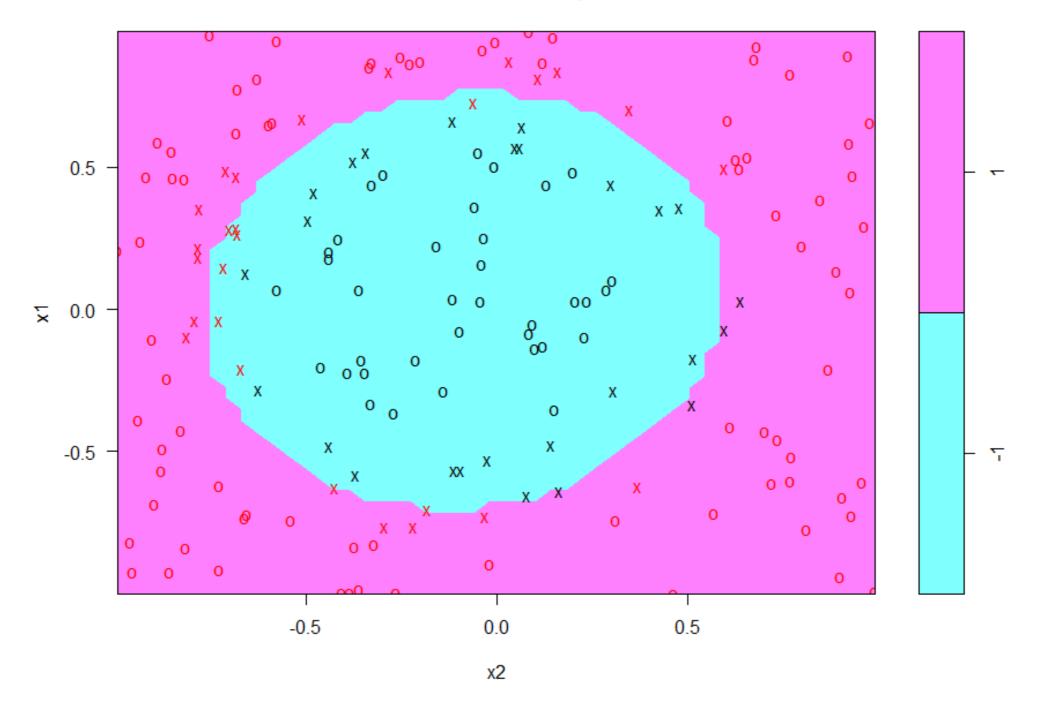
```
svm_model <- svm(y ~ ., data = trainset, type = "C-classification", kernel = "polynomial", degree = 2)
# Predictions
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

0.9354839

```
# Visualize model
plot(svm_model, trainset)
```



SVM classification plot



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Tuning SVMs

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Objective of tuning

- Hard to find optimal values of parameters manually for complex kernels.
- Objective: to find optimal set of parameters using tune.svm() function.

Tuning in a nutshell

- How it works:
 - o set a range of search values for each parameter. Examples: $cost = 10^{-1:3}$, gamma = c(0.1,1,10), coef0 = c(0.1,1,10)
 - Build an SVM model for each possible combination of parameter values and evaluate accuracy.
 - Return the parameter combination that yields the best accuracy.
- Computationally intensive procedure!

- Tune SVM model for the radially separable dataset created earlier
 - Built polynomial kernel SVM in previous lesson
 - Accuracy of SVM was ~94%.
- Can we do better by tuning gamma, cost and coef0?

```
0.1
10
1
```

• Build SVM model using best values of parameters from tune.svm().

```
svm_model <- svm(y ~ ., data = trainset, type = "C-classification", kernel = "polynomial", degree = 2,
    cost = tune_out$best.parameters$cost,
    gamma = tune_out$best.parameters$gamma,
    coef0 = tune_out$best.parameters$coef0)</pre>
```

evaluate training and test accuracy

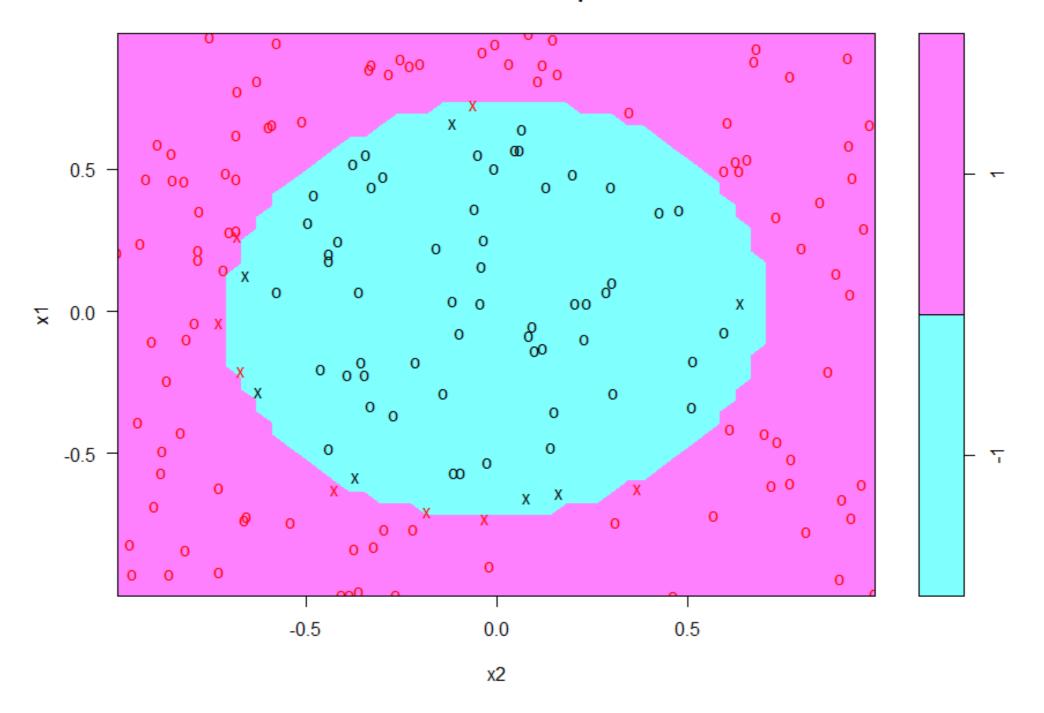
```
pred_train <- predict(svm_model, trainset)
mean(pred_train == trainset$y)
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

```
1
0.9677419
```

```
#plot using svm plot
plot(svm_model, trainset)
```



SVM classification plot



Time to practice!

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