RBF Kernels: Generating a complex dataset

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Instructor



A bit about RBF Kernels

- Highly flexible kernel.
 - Can fit complex decision boundaries.
- Commonly used in practice.

Generate a complex dataset

- 600 points (x1, x2)
- x1 and x2 distributed differently

Generate boundary

Boundary consists of two equi-radial circles with a single point in common.

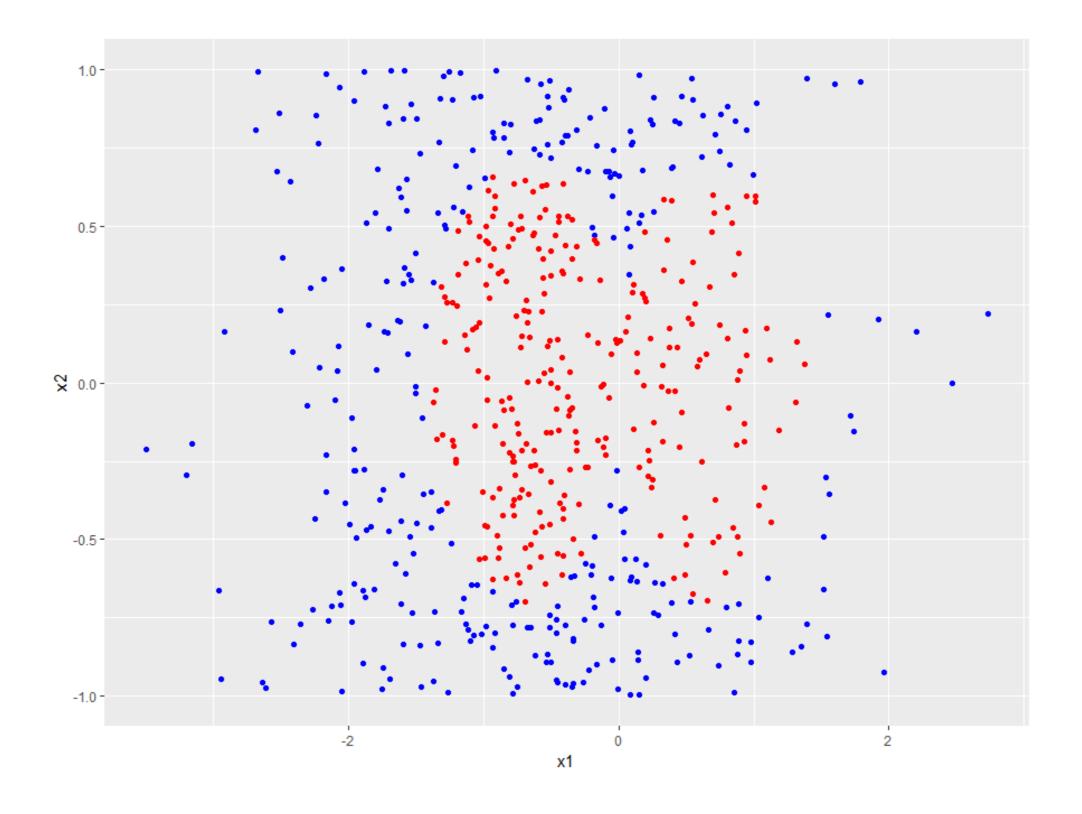
```
# Set radius and centers
radius <- 0.7
radius_squared <- radius ^ 2</pre>
center_1 <- c(-0.7, 0)
center_2 <- c(0.7, 0)
# Classify points
df$y <-
    factor(ifelse(
        (df$x1 - center_1[1]) ^ 2 + (df$x2 - center_1[2]) ^ 2 < radius_squared |
        (df$x1 - center_2[1]) ^ 2 + (df$x2 - center_2[2]) ^ 2 < radius_squared,
        -1, 1), levels = c(-1, 1))
```

Visualizing the dataset

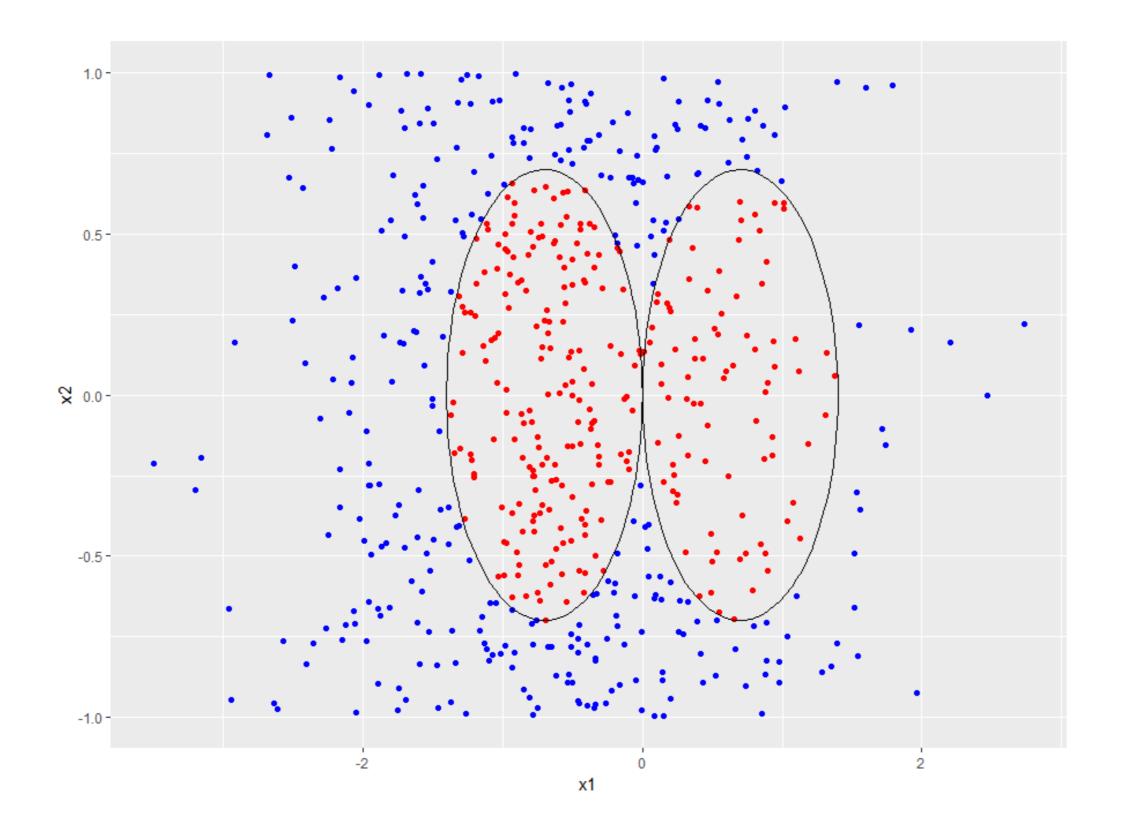
Visualize the dataset using ggplot; distinguish classes by color

```
library(ggplot2)

p <- ggplot(data = df, aes(x = x1, y = x2, color = y)) +
    geom_point() +
    guides(color = FALSE) +
    scale_color_manual(values = c("red", "blue"))</pre>
```



```
# Function to generate points on a circle
circle <- function(x1_center, x2_center, r, npoint = 100) {
   theta \leftarrow seq(0, 2 * pi, length.out = npoint)
   x1_circ <- x1_center + r * cos(theta)
   x2_circ <- x2_center + r * sin(theta)
   data.frame(x1c = x1_circ, x2c = x2_circ)
# Generate boundary and plot it
boundary_1 <- circle(x1_center = center_1[1], x2_center = center_1[2], r = radius)</pre>
p <- p +
     geom_path(data = boundary_1,
               aes(x = x1c, y = x2c),
               inherit.aes = FALSE)
boundary_2 <- circle(x1_center = center_2[1], x2_center = center_2[2], r = radius)
p <- p +
     geom_path(data = boundary_2,
               aes(x = x1c, y = x2c),
               inherit.aes = FALSE)
```





Time to practice!

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Motivating the RBF kernel

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Quadratic kernel (default parameters)

- Partition data into test/train (not shown)
- Use degree 2 polynomial kernel (default params)

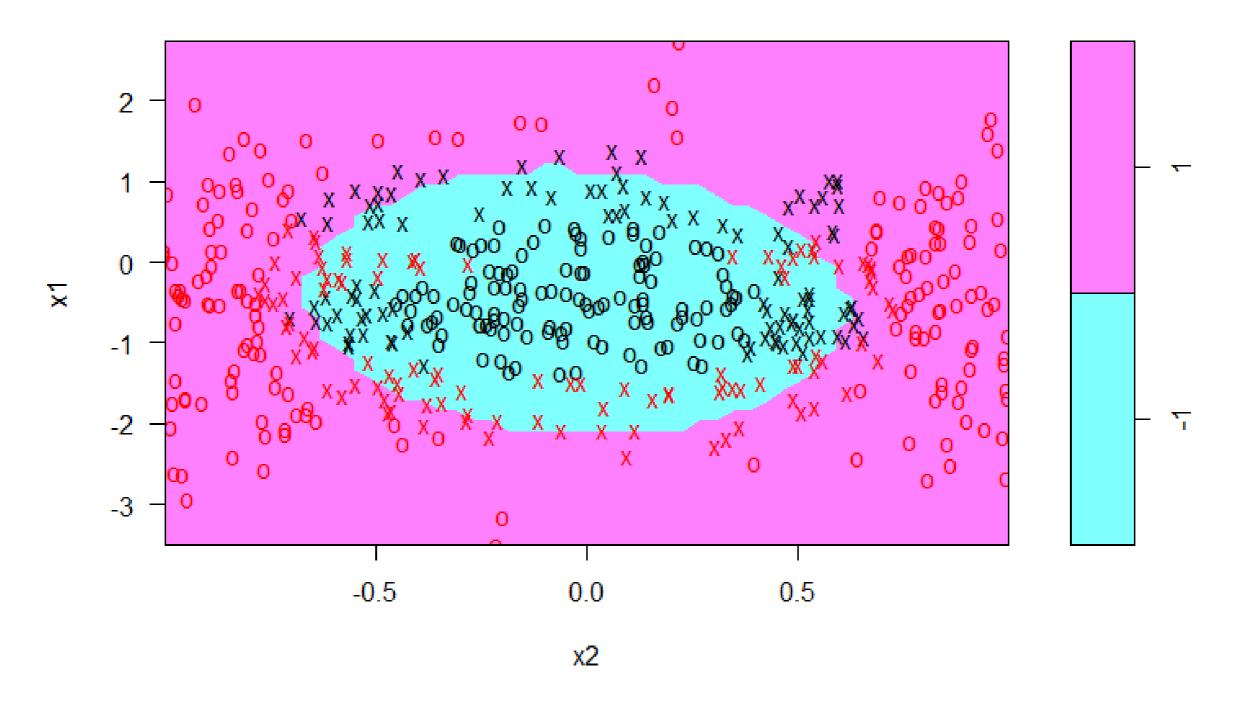
```
Number of Support Vectors: 204
```

```
# Predictions
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

0.8666667

```
plot(svm_model, trainset)
```

SVM classification plot



Try higher degree polynomial

- Rule out odd degrees -3,5,9 etc.
- Try degree 4

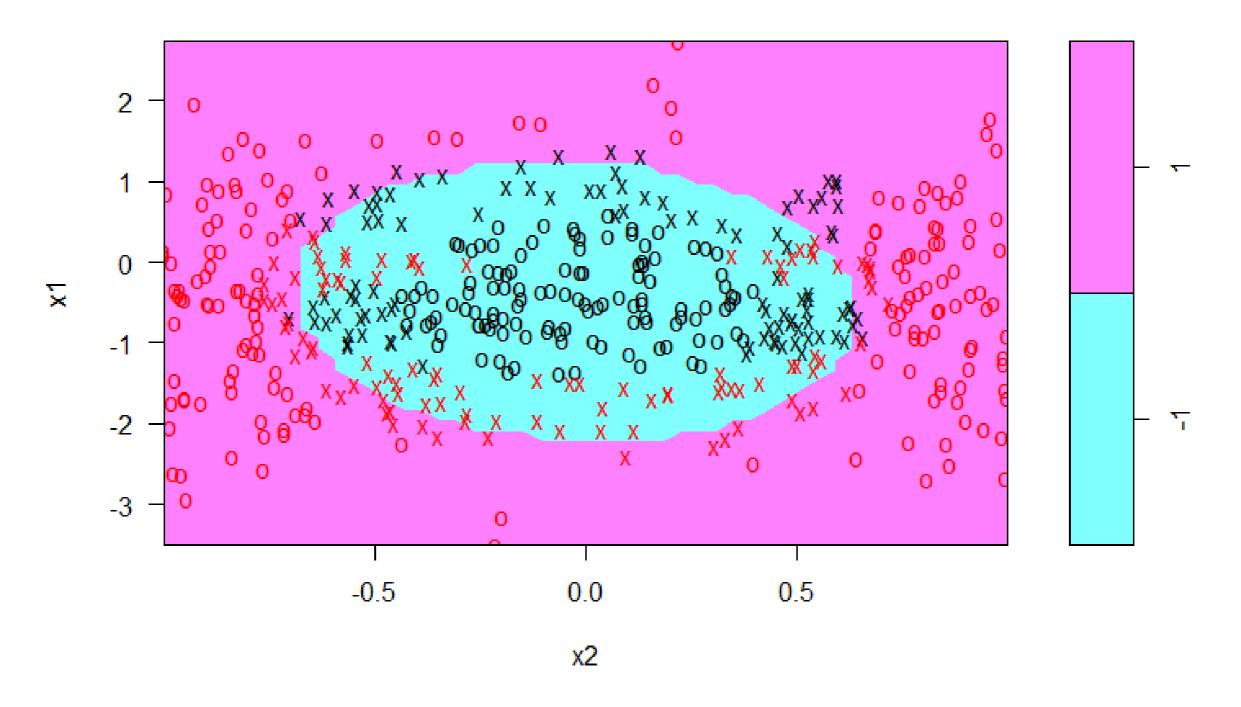
```
Number of Support Vectors: 203
```

```
# Predictions
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

```
0.8583333
```

```
plot(svm_model, trainset)
```

SVM classification plot

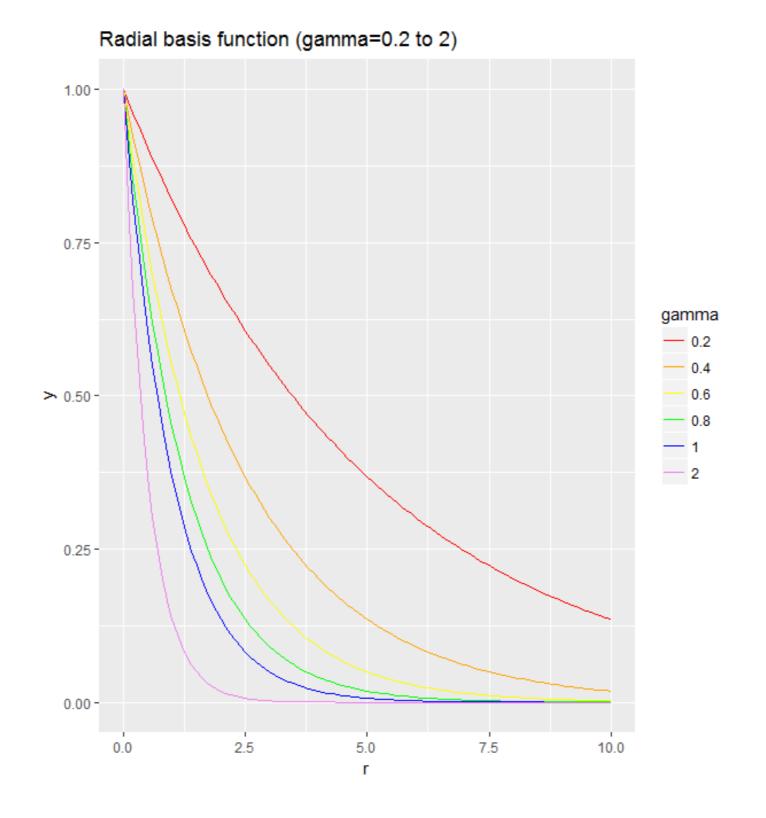


Another approach

- Heuristic: points close to each other have the same classification:
 - Akin to K-Nearest Neighbors algorithm.
- For a given point in the dataset, say X1 = (a, b):
 - The kernel should have a maximum at (a, b)
 - Should decay as one moves away from (a, b)
 - The rate of decay should be the same in all directions
 - The rate of decay should be tunable
- A simple function with this property is exp(-gamma * r), where r is the distance between X1 and any other point X

How does the RBF kernel vary with gamma (code)

```
#rhf function
rbf <- function(r, gamma) exp(-gamma * r)</pre>
ggplot(data.frame(r = c(-0, 10)), aes(r)) +
  stat_function(fun = rbf, args = list(gamma = 0.2), aes(color = "0.2")) +
  stat_function(fun = rbf, args = list(gamma = 0.4), aes(color = "0.4")) +
  stat_function(fun = rbf, args = list(gamma = 0.6), aes(color = "0.6")) +
  stat_function(fun = rbf, args = list(gamma = 0.8), aes(color = "0.8")) +
  stat_function(fun = rbf, args = list(gamma = 1), aes(color = "1")) +
  stat_function(fun = rbf, args = list(gamma = 2), aes(color = "2")) +
  scale_color_manual("gamma",
                     values = c("red", "orange", "yellow",
                                "green", "blue", "violet")) +
  ggtitle("Radial basis function (gamma = 0.2 to 2)")
```





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The RBF Kernel

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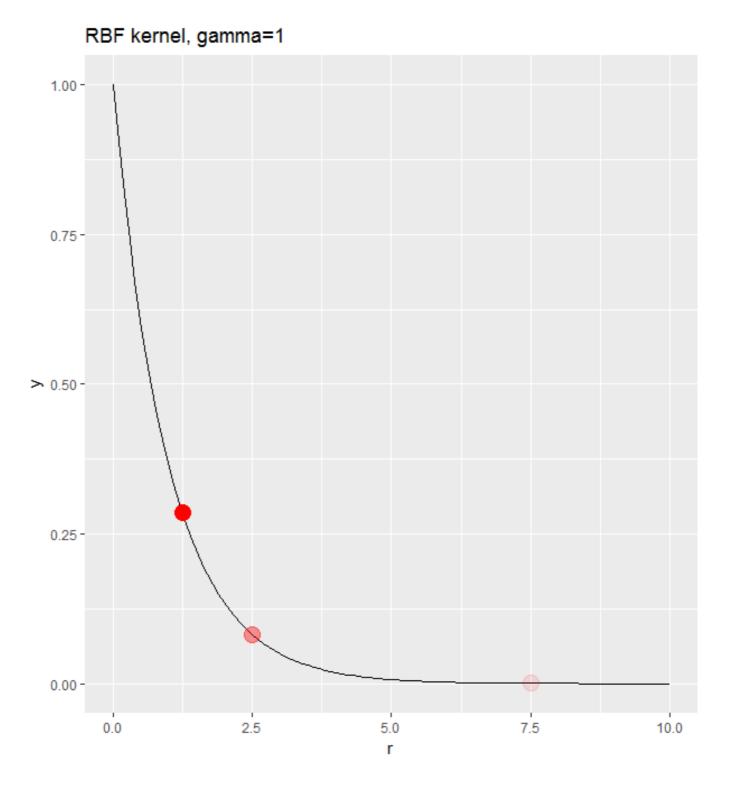


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RBF Kernel in a nutshell

- Decreasing function of distance between two points in dataset.
- Simulates k-NN algorithm.



Building an SVM using the RBF kernel

Build RBF kernel SVM for complex dataset

 Calculate training/test accuracy and plot against training dataset.

```
pred_train <- predict(svm_model, trainset)
mean(pred_train == trainset$y)</pre>
```

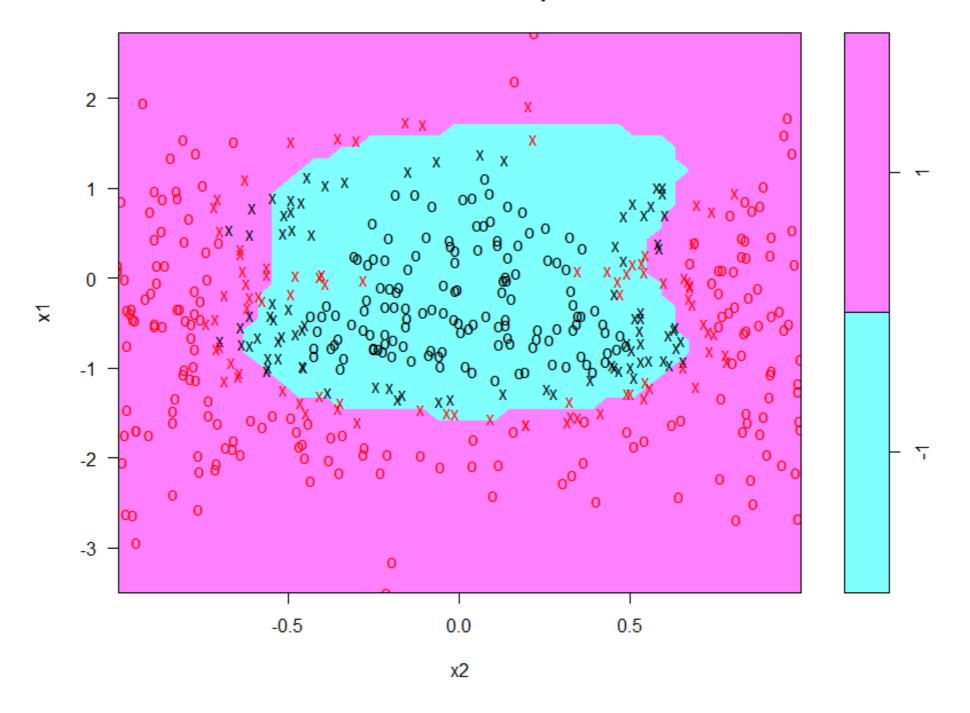
0.93125

```
pred_test <- predict(svm_model, testset)
mean(pred_test == testset$y)</pre>
```

0.9416667

```
#plot decision boundary
plot(svm_model, trainset)
```

SVM classification plot



Refining the decision boundary

Tune gamma and cost using tune.svm()

Print best parameters

```
# Print best values of cost and gamma
tune_out$best.parameters$cost
```

tune_out\$best.parameters\$gamma

5

The tuned model

Build tuned model using best.parameters

Calculate test accuracy

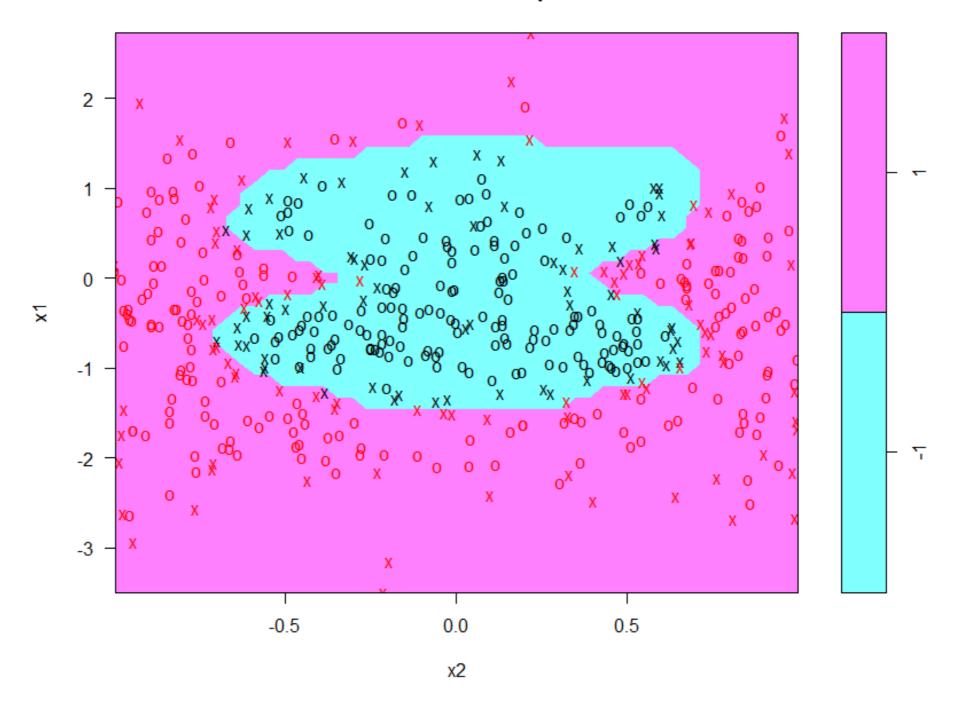
```
mean(pred_test == testset$y)
```

0.95

Plot decision boundary

```
plot(svm_model, trainset)
```

SVM classification plot



Time to practice!

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