Use a function of your choice to complete this problem.

a. For your function f, generate data according to $y_i = f(t_i) + \epsilon_i$ where ϵ is Gaussian noise with zero mean and standard deviation 0.1. Fit the resulting data using ordinary least squares and the monomial basis up to t^8

b. Repeat the fitting above 1000 times (generating new data each time) and create histograms for the value of each θ

c. Repeat the previous two parts using the first eight Legendre polynomials

d. What can you conclude about the advantages and disadvantages of using monomials versus Legendre polynomials as basis functions?