

In this problem, we will revisit the data in `bias_variance_trade.txt` to demonstrate generalized aliasing. Remember that the first and third columns are samples of the independent variable  $x$ , while the second and fourth columns are samples of the dependent variable  $y$  that correspond to those points.

- (a) Combine the two samples into one dataset and generate a system matrix assuming a basis of sines and cosines with frequency that increases with column number (i.e.  $\cos(x)$ ,  $\cos(2x)$ ,  $\cos(3x)$ , etc.). Your system matrix should have 1,000 columns. Do not print this matrix.
- (b) Use your programming language of choice to create an integer list of terms that are roughly equidistant in logarithmic space between 1 and 1,000. For each number of terms, produce a fit to the combined data set. Plot a representative subsample of these fits with the data used to produce them.
- (c) Assuming that the true signal is characterized by  $f(x) = e^{-6x^2} \cos(4\pi x)$ , calculate the Euclidean norm of the difference between the true signal and each of your models for 100 equally spaced samples between -1 and 1. Report the cost versus number of terms in a log-log plot.
- (d) Using the language of the General Aliasing Decomposition, explain the shape of the plot you produced in the prior part.