

# Linear Algebra, Data Science, and Machine Learning

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## Errata

Last updated January 19, 2026

- Page 24: End of line after (2.23):

Change “chack” to “check”

- Page 84: Line before Theorem 4.8:

Change “Exercise 4.10.” to “Exercise 4.10 in Chapter 3.”

- Page 88: Line after (4.163):

Change “ $m \times m$  matrix.” to “ $n \times n$  matrix.”

- Page 99:

In the displayed formula in the proof of Proposition 4.30, the second equality should be an inequality:  $\dim \text{img}(AB) \geq \dim(\text{coimg } A \cap \text{img } B)$ . Thus, (1.16) proves the lower bound in (4.42), while the upper bound can be easily established directly.

- Page 102: Remark:

Change “two case” to “two cases”.

- Page 141: Equation with  $R \circ S$  on left hand side:

Change  $\mathbf{u}_j \mathbf{u}_j^T$  to  $\mathbf{u}_i \mathbf{u}_i^T$ .

- Page 141, line -5 and page 142, line 3:

Change “Exercise 1.17(d)” to “Exercise 1.17(e)”

- Page 188: Proof of Theorem 6.9:

Change  $b = \mathbf{y}^T \mathbf{f}$  to  $b = -\mathbf{y}^T \mathbf{f}$ .

- Page 190: Equation (6.19):

There is a missing minus sign, the equation should read

$$P(A \mathbf{y}) = \frac{1}{2} \mathbf{y}^T A^T H A \mathbf{y} - \mathbf{y}^T A^T \mathbf{f} + c.$$

- Page 190: Equation (6.21):

In this equation, it should be noted that  $\mathbf{b} = A^T \mathbf{f}$ .

- Page 191: Remark after Corollary 6.13:

Insert “in Chapter 4” after “Exercise 2.6”.

- Page 195:

Change “Proposition 6.17” to “Theorem 6.17”.

- Page 205: Exercise 4.8:

Change  $A$  to  $H$  twice:

$$\mathbf{x}_{k+1} = \mathbf{x}_k - \alpha_k(H\mathbf{x}_k - \mathbf{b}) \quad \text{and} \quad \mathbf{r}_k = H\mathbf{x}_k - \mathbf{b}.$$

- Page 206: Motivation for the Conjugate Gradient Method:

The formulas for the conjugate gradient method are all correct, but the derivation and motivation has an error. The method should minimize the corresponding quadratic function, and not the residual vector. The text starting right after Equation (6.65) and ending before “Starting with an initial guess...” should be replaced with the text below.

The conjugate gradient algorithm, to be derived below, computes the  $t_k$  and  $\mathbf{v}_k$  iteratively, so that the  $k$ -th approximation to the solution is

$$\mathbf{x}_k = \mathbf{x}_0 + t_1 \mathbf{v}_1 + \cdots + t_k \mathbf{v}_k, \quad \text{or, equivalently} \quad \mathbf{x}_k = \mathbf{x}_{k-1} + t_k \mathbf{v}_k,$$

where, once  $\mathbf{v}_k$  is specified,  $t_k$  is chosen to minimize the quadratic function (6.44). The secret is not to try to specify the conjugate basis vectors in advance, but rather to successively construct them during the course of the algorithm.

We begin with an initial guess  $\mathbf{x}_0$  — for example,  $\mathbf{x}_0 = \mathbf{0}$ . According to (6.45) the residual vector  $\mathbf{r}_0 = \mathbf{b} - H\mathbf{x}_0$  is the negative of the Euclidean gradient of  $P$  at the point  $\mathbf{x}_0$ , and hence indicates the direction of steepest decrease. We begin by updating our original guess by moving in this direction, taking  $\mathbf{v}_1 = \mathbf{r}_0$  as our first conjugate direction.

The next iterate is  $\mathbf{x}_1 = \mathbf{x}_0 + t_1 \mathbf{v}_1$ , and we choose the parameter  $t_1$  so that

$$\begin{aligned} P(\mathbf{x}_1) &= P(\mathbf{x}_0 + t_1 \mathbf{v}_1) = P(\mathbf{x}_0) + t_1 \mathbf{v}_1 \cdot (H\mathbf{x}_0 - \mathbf{b}) + \frac{1}{2} t_1^2 \mathbf{v}_1^T H \mathbf{v}_1 \\ &= P(\mathbf{x}_0) - t_1 \mathbf{v}_1 \cdot \mathbf{r}_0 + \frac{1}{2} t_1^2 \|\mathbf{v}_1\|_H^2 \end{aligned} \tag{6.66}$$

is as small as possible, which occurs when

$$t_1 = \frac{\mathbf{v}_1 \cdot \mathbf{r}_0}{\|\mathbf{v}_1\|_H^2} = \frac{\|\mathbf{r}_0\|_2^2}{\|\mathbf{v}_1\|_H^2}. \tag{6.67}$$

We can assume that  $t_1 \neq 0$ , since otherwise the residual  $\mathbf{r}_0 = \mathbf{0}$ , which would imply  $\mathbf{x}_0 = \mathbf{x}^*$  is the exact solution of the linear system, and there would be no reason to continue the procedure. We note that the updated residual can be expressed in the form

$$\mathbf{r}_1 = \mathbf{b} - H\mathbf{x}_1 = \mathbf{b} - H\mathbf{x}_0 - t_1 H \mathbf{v}_1 = \mathbf{r}_0 - t_1 H \mathbf{v}_1. \tag{6.68}$$

Observe that, in view of (6.67),

$$\mathbf{r}_0 \cdot \mathbf{r}_1 = \mathbf{v}_1 \cdot \mathbf{r}_1 = \mathbf{v}_1 \cdot \mathbf{r}_0 - t_1 \mathbf{v}_1 \cdot (H \mathbf{v}_1) = \mathbf{v}_1 \cdot \mathbf{r}_0 - t_1 \|\mathbf{v}_1\|_H^2 = 0, \tag{6.69}$$

and hence the initial residual — the first conjugate direction — is orthogonal to the first residual under the dot product.

The gradient descent algorithm would tell us to update  $\mathbf{x}_1$  by moving in the residual direction  $\mathbf{r}_1$ . In the conjugate gradient algorithm, we instead choose a direction  $\mathbf{v}_2$  which is conjugate, meaning  $H$ -orthogonal, to the first direction  $\mathbf{v}_1 = \mathbf{r}_0$ . Thus, as in the Gram–Schmidt process, we modify the residual direction by setting  $\mathbf{v}_2 = \mathbf{r}_1 + s_1 \mathbf{v}_1$ , where the scalar factor  $s_1$  is determined by the imposed orthogonality requirement:

$$0 = \langle \mathbf{v}_1, \mathbf{v}_2 \rangle_H = \langle \mathbf{v}_1, \mathbf{r}_1 + s_1 \mathbf{v}_1 \rangle_H = \langle \mathbf{v}_1, \mathbf{r}_1 \rangle_H + s_1 \langle \mathbf{v}_1, \mathbf{v}_1 \rangle_H = \langle \mathbf{r}_1, \mathbf{v}_1 \rangle_H + s_1 \|\mathbf{v}_1\|_H^2,$$

and hence we fix

$$s_1 = -\frac{\langle \mathbf{v}_1, \mathbf{r}_1 \rangle_H}{\|\mathbf{v}_1\|_H^2}.$$

Now, in view of (6.68) and (6.69),

$$\langle \mathbf{v}_1, \mathbf{r}_1 \rangle_H = \langle \mathbf{r}_1, \mathbf{v}_1 \rangle_H = \mathbf{r}_1^T H \mathbf{v}_1 = \mathbf{r}_1^T \left( \frac{\mathbf{r}_0 - \mathbf{r}_1}{t_1} \right) = -\frac{1}{t_1} \|\mathbf{r}_1\|_2^2,$$

while, by (6.67),

$$\|\mathbf{v}_1\|_H^2 = \frac{1}{t_1} \|\mathbf{r}_0\|_2^2.$$

Therefore, the second conjugate direction is also given by

$$\mathbf{v}_2 = \mathbf{r}_1 + s_1 \mathbf{v}_1, \quad \text{where} \quad s_1 = \frac{\|\mathbf{r}_1\|_2^2}{\|\mathbf{r}_0\|_2^2}.$$

We then update  $\mathbf{x}_2 = \mathbf{x}_1 + t_2 \mathbf{v}_2$ , where  $t_2$  is chosen in order to make  $P(\mathbf{x}_2)$  as small as possible. By a similar computation as in (6.66), this occurs when

$$t_2 = \frac{\mathbf{v}_2 \cdot \mathbf{r}_1}{\|\mathbf{v}_2\|_H^2} = \frac{\|\mathbf{r}_1\|_2^2}{\|\mathbf{v}_2\|_H^2},$$

where the second expression follows from the formula for  $\mathbf{v}_2$  and (6.69). Again, we can assume that  $t_2 \neq 0$ , as otherwise  $\mathbf{r}_1 = \mathbf{0}$  and  $\mathbf{x}_1$  would be the exact solution, in which case the algorithm should be terminated.

Continuing in this manner, at the  $k$ -th stage for any  $k \geq 1$ , we have already constructed the conjugate vectors  $\mathbf{v}_1, \dots, \mathbf{v}_k$  that are mutually  $H$ -orthogonal, and the solution approximation  $\mathbf{x}_k$  as a suitable linear combination of them and the initial approximation  $\mathbf{x}_0$ . We further assume we inductively established the (dot product) orthogonality relations

$$\mathbf{v}_i \cdot \mathbf{r}_k = 0, \quad 1 \leq i \leq k, \quad \text{and} \quad \mathbf{r}_j \cdot \mathbf{r}_k = 0, \quad 0 \leq j < k.$$

The next conjugate direction is given by

$$\mathbf{v}_{k+1} = \mathbf{r}_k + s_k \mathbf{v}_k, \quad \text{where} \quad s_k = \frac{\|\mathbf{r}_k\|_2^2}{\|\mathbf{r}_{k-1}\|_2^2} \tag{6.70}$$

results from the  $H$ -orthogonality requirement:

$$\langle \mathbf{v}_i, \mathbf{v}_{k+1} \rangle_H = 0 \quad \text{for} \quad 1 \leq i \leq k.$$

The updated solution approximation is

$$\mathbf{x}_{k+1} = \mathbf{x}_k + t_{k+1} \mathbf{v}_{k+1}, \quad \text{where} \quad t_{k+1} = \frac{\mathbf{v}_{k+1} \cdot \mathbf{r}_k}{\|\mathbf{v}_{k+1}\|_H^2} = \frac{\|\mathbf{r}_k\|_2^2}{\|\mathbf{v}_{k+1}\|_H^2} \quad (6.71)$$

is then specified so as to make  $P(\mathbf{x}_{k+1})$  as small as possible. The second expression for  $t_{k+1}$  follows from (6.70) and the orthogonality of  $\mathbf{v}_k$  and  $\mathbf{r}_k$ . The new residual vector is

$$\mathbf{r}_{k+1} = \mathbf{b} - H\mathbf{x}_{k+1} = \mathbf{r}_k - t_{k+1} H\mathbf{v}_{k+1}. \quad (6.72)$$

The induction step is completed by establishing the new orthogonality relations. First, by the already established orthogonality of  $\mathbf{v}_i$  and  $\mathbf{r}_k$ , and the  $H$ -orthogonality of the  $\mathbf{v}_i$ ,

$$\mathbf{v}_i \cdot \mathbf{r}_{k+1} = \mathbf{v}_i \cdot \mathbf{r}_k - t_{k+1} \mathbf{v}_i \cdot (H\mathbf{v}_{k+1}) = \mathbf{v}_i \cdot \mathbf{r}_k - t_{k+1} \langle \mathbf{v}_i, \mathbf{v}_{k+1} \rangle_H = 0 \quad \text{for } 1 \leq i \leq k,$$

while, using the first formula for  $t_{k+1}$  in (6.71),

$$\mathbf{v}_{k+1} \cdot \mathbf{r}_{k+1} = \mathbf{v}_{k+1} \cdot \mathbf{r}_k - t_{k+1} \mathbf{v}_{k+1} \cdot (H\mathbf{v}_{k+1}) = \mathbf{v}_{k+1} \cdot \mathbf{r}_k - t_{k+1} \|\mathbf{v}_{k+1}\|_H^2 = 0.$$

This also implies  $\mathbf{r}_i \cdot \mathbf{r}_{k+1} = 0$  for  $0 \leq i \leq k$ , since  $\mathbf{r}_0 = \mathbf{v}_1$  while  $\mathbf{r}_i = \mathbf{v}_{i+1} - s_i \mathbf{v}_i$  for  $i \geq 1$ .

- Page 213:

Change  $x$  to  $\mathbf{x}$  on the line immediately below Eq. (6.79).

- Page 214: Definition 6.32:

Change the definition to read “is the  $n \times n$  self-adjoint matrix defined by the inequality”.

- Page 225: Equation 6.109:

Change  $\mu^2$  to  $\mu$ .

- Page 270: Equation 7.53:

There are missing terms on the right hand side that are independent of  $w_i$  (and so do not affect any subsequent computations). The equation and the 2 lines that follow should read as follows:

$$\|X\mathbf{w} - \mathbf{y}\|^2 + \lambda \|\mathbf{w}\|_1 = \|\mathbf{v}_i\|^2 w_i^2 - 2w_i b_i + \lambda |w_i| + c, \quad (0.1)$$

for any  $i = 1, \dots, n$ , where

$$b_i = \mathbf{v}_i \cdot \left( \mathbf{y} - \sum_{j \neq i} w_j \mathbf{v}_j \right) \quad \text{and} \quad c = \|\mathbf{y} - \sum_{j \neq i} w_j \mathbf{v}_j\|^2 + \lambda \sum_{j \neq i} |w_j|.$$

- Page 274: Line -8:

Change “from the raining data” to “from the training data”

- Page 275: Equation 7.61:

$\mathbf{x} \in \mathbb{R}^m$  to  $\mathbf{x} \in \mathbb{R}^n$

- Page 275: Equation 7.62:

Change the equation to read

$$\min_{\substack{\mathbf{w} \in \mathbb{R}^n \\ b \in \mathbb{R}}} \left\{ \|\mathbf{w}\|^2 \mid y_i(\mathbf{x}_i \cdot \mathbf{w} - b) \geq 1, \quad i = 1, \dots, m \right\}.$$

- Page 275: Equation 7.63:

Change the equation to read

$$\min_{\mathbf{w}, b} \left\{ \|\mathbf{w}\|^2 \mid \mathbf{z} \cdot \mathbf{w} - b \geq 1, \quad \mathbf{z} \cdot \mathbf{w} + b \geq 1 \right\}.$$

- Page 284: Figure 7.24:

Add  $k = 1$  to the caption.

- Page 300: Line directly above Theorem 7.17:

Remove the text “, as well as soft-margin SVM (7.64)”. Technically soft-margin SVM does not fit into this loss function due to the extra parameter  $b$ .

- Page 301: Displayed equation after equation 7.63:

Change  $\mathcal{K}_\phi(\mathbf{x}, \mathbf{x}_j)$  to  $\mathcal{K}_\phi(\mathbf{x}_i, \mathbf{x}_j)$

- Page 302: Definition 7.18:

The definition of Mercer kernel should be amended to include a requirement that  $\mathcal{K}$  is continuous.

- Page 304: Line after equation 7.101:

Change “a chosen kernel function” to “a chosen Mercer kernel function”

- Page 306: Theorem 7.22:

The assumptions on convexity/concavity of  $F$  should be switched, and  $D$  must be nonempty. Also, while the result in Fan [72] holds for nonconvex sets  $D$ , Fan has a more general notion of convex/concave functions than we have given in the book, so to be more clear we also assume  $D$  is convex. The correct statement of the theorem should read.

**Theorem 7.22.** *Let  $D \subset \mathbb{R}^m$  be convex, compact, i.e., closed and bounded, and nonempty. Let  $F: D \times \mathbb{R}^n \rightarrow \mathbb{R}$  be continuous, and suppose that  $F(\mathbf{x}, \mathbf{y})$  is convex as a function of  $\mathbf{y}$  for each fixed  $\mathbf{x} \in D$ , while  $F(\mathbf{x}, \mathbf{y})$  is concave, i.e.,  $-F(\mathbf{x}, \mathbf{y})$  is convex, as a function of  $\mathbf{x}$  for each fixed  $\mathbf{y} \in \mathbb{R}^n$ . Then,*

$$\min_{\mathbf{y} \in \mathbb{R}^n} \max_{\mathbf{x} \in D} F(\mathbf{x}, \mathbf{y}) = \max_{\mathbf{x} \in D} \min_{\mathbf{y} \in \mathbb{R}^n} F(\mathbf{x}, \mathbf{y}).$$

As a side note, Theorem 7.22 is one place in the book where the minimum is really an infimum.

For an elementary self-contained proof of Theorem 7.22 in the setting required in the book, we refer to the note [1]. In particular, this note explains saddle points for minimax problems,

which are important for understanding the formula for  $b$  on page 307 in the book.

- Page 307: Equation (7.112):

Change  $\sum_{i=1}^n$  to  $\sum_{i=1}^m$ .

- Page 307: Remark 7.23:

Replace “exactly those” with “a subset of the”.

- Page 309:

Change  $\sum_{i=1}^n$  to  $\sum_{i=1}^m$ .

- Page 319: Section 8.8.1. Kernel Principal Component Analysis

Throughout this section there should be a standing assumption that  $d \geq m$  (i.e., the feature dimension is at least as large as the number of data points). Also, we can of course only define the principal components  $\mathbf{q}_i$  when  $\lambda_i > 0$ , and we should also check that  $\mathbf{v}_1, \dots, \mathbf{v}_k$  are orthogonal. Thus, lines -10 through -5 should be replaced with the text below.

Notice that

$$\mathbf{v}_i \cdot \mathbf{v}_j = (\underline{Z}^T \mathbf{p}_i)^T \underline{Z}^T \mathbf{p}_j = \mathbf{p}_i^T \underline{Z} \underline{Z}^T \mathbf{p}_j = \lambda_j \mathbf{p}_i \cdot \mathbf{p}_j.$$

Thus, if  $\lambda_1, \dots, \lambda_k > 0$ , then  $\mathbf{v}_1, \dots, \mathbf{v}_k$  are orthogonal and the top  $k$  principal components of the feature vector data  $\mathbf{z}_1, \dots, \mathbf{z}_m$  are given by the corresponding unit vectors

$$\mathbf{q}_i = \frac{\mathbf{v}_i}{\|\mathbf{v}_i\|} = \lambda_i^{-1/2} \underline{Z}^T \mathbf{p}_i \quad \text{for } i = 1, \dots, k.$$

- Page 320: Figure 8.8:

Add the line “The colors in the second and third figures in each row indicate which cluster each point is from in the original data depicted on the left.” to the figure caption for clarity.

- Page 320: Kernel PCA and Whitening

The version of kernel PCA described in the book includes whitening. There is also a version without whitening. It is worth making a comment about this. The following paragraph fits nicely at the end of Subsection 8.1.1, after the second to last paragraph in the section.

It is important to note that the method described above is kernel PCA with *whitening*. Indeed, provided  $\lambda_k > 0$ , so  $J\mathbf{p}_i = \mathbf{p}_i$  for  $i = 1, \dots, k$ , we have  $JP_k = P_k$  and so the covariance matrix of the kernel PCA data is

$$S_{P_k} = P_k^T P_k = I,$$

since the columns of  $P_k$  are orthonormal vectors. To produce a non-whitened version of kernel PCA, which is the standard setting for PCA, we define  $Q_k = P_k \Sigma_k$ , where  $\Sigma_k = \text{diag}(\sqrt{\lambda_1}, \dots, \sqrt{\lambda_k}) = \text{diag}(\sigma_1, \dots, \sigma_k)$ . Then the covariance matrix of  $Q_k$  is given by

$$S_{Q_k} = Q_k^T Q_k = \Sigma_k P_k^T P_k \Sigma_k = \Sigma_k^2,$$

which is the same as for PCA (see (8.7)).

- Page 320: Theorem 8.4:

The formula for  $\mathbf{q}_i$  should read  $\mathbf{q}_i = \lambda_i^{-1/2} Z^T \mathbf{p}_i$ .

- Page 326: line after (8.18):

Change “follows from (2.41).” to “follows from (2.40).”

- Page 333: Equation (8.33):

Change  $Q$  to  $Q^T$ .

- Page 333: Equation (8.34):

Change  $Q_k$  to  $Q_k^T$ .

- Page 346, Exercise 4.1:

Delete “How does the accuracy change with the number of principal components used?”

- Page 352:

Change “is inversely proportional to similarity” to “decreases as similarity increases”.

- Page 358:

Switch reference to first and second graph in Figure 9.1: “Thus, the first graph has 4 nodes and 6 edges — the two central edges do not meet; the second has 5 nodes and 8 edges;”

- Page 359, line 6:

Change  $m = \#\mathcal{N}$  to  $m = \#\mathcal{N} \geq 1$

- Page 359, line 8:

Change  $e = \#\mathcal{E}$  to  $e = \#\mathcal{E} \geq 0$  and change  $\mathcal{E} \simeq \{1, \dots, e\}$ . to  $\mathcal{E} \simeq \{1, \dots, e\}$ , with  $\mathcal{E} = \emptyset$  if there are no edges:  $e = 0$ .

- Page 379: Remark 9.19:

Change wording in second line: “ $D = \text{diag } \mathbf{d}$ , then the”, and correct next to last line: “ $\tilde{\mathbf{d}} = W^T \mathbf{1}$  is the incoming degree vector,”

- Page 388: End of line 3:

Change “and 0 if” to “and  $-b$  if”

- Page 388: Equation (9.35):

Change  $\frac{m^2}{(m-k)^2}(m-k)$  to  $\frac{k^2}{(m-k)^2}(m-k)$

- Page 394: Line 3:

Change “Thus” to “On the other hand, we already know  $\mathbf{1} \in \ker M$ ; moreover, if  $\mathbf{z} \in \ker W$ , then  $\mathbf{d}^T \mathbf{z} = \mathbf{1}^T W^T \mathbf{z} = \mathbf{1}^T W \mathbf{z} = 0$ , and hence  $M \mathbf{z} = \mathbf{0}$ . We conclude that”

- Page 394: Paragraph before Theorem 9.35:

Replace the sentence “When no such groups exist, the modularity is negative for *all* subsets of the graph, and the modularity matrix  $M$  is *negative semidefinite*.” with “When no such groups exist, the modularity is negative for *all* subsets of the graph. This happens when the modularity matrix  $M$  is *negative semidefinite*.”

- Page 394: Line before Theorem 9.35:

Change “Theorem 5.29” to “Theorem 5.43”.

- Page 394: Theorem 9.35:

The theorem is not true as an “if and only if” statement. The first line of the theorem should be replaced with “If the modularity matrix  $M$  is negative semidefinite then”.

- Page 415: Remark 9.56

The remark is trivial, since the only weight matrix that is positive semidefinite is the zero matrix, since we do not allow loops. To be more clear, the remark should be replaced with the text below.

**Remark 9.56.** If the weight matrix  $W$  is positive semidefinite, then we can furthermore say that the eigenvalues of  $L_{\text{rw}}$  and  $L_{\text{sym}}$  belong to the interval  $[0, 1]$ . Indeed, in this case, the matrix  $D^{-1/2}WD^{-1/2}$  is also positive semidefinite, and so the eigenvalues of the symmetric normalized graph Laplacian matrix  $L_{\text{sym}} = I - D^{-1/2}WD^{-1/2}$  can be no greater than one. On the other hand, since we do not allow loops, the diagonal entries of  $W$  are all zero, and so the only positive semidefinite weight matrix is the zero matrix,  $W = O$ , and hence  $L_{\text{sym}} = I$  reduces to the identity matrix! However, if we for the moment allow weight matrices with nonzero (but still nonnegative) diagonal entries, then the remark still applies. An important example is the weight matrix with radial basis function kernel, introduced in Section 7.6, which has entries  $w_{ij} = \exp[-\|\mathbf{x}_i - \mathbf{x}_j\|^2/(2\varepsilon^2)]$ , and is positive semidefinite. ▲

- Page 457: Lemma 9.79:

Change  $\lambda_0, \dots, \lambda_{n+1}$  to  $\lambda_0, \dots, \lambda_n$

- Page 475: Lemma 9.88:

Change “Let  $\mathbf{g} = (\gamma_1, \gamma_2, \dots, \gamma_m)^T \in \mathbb{R}^m$  be the vector containing the eigenvalues  $\gamma_j$  of  $A$ . Then  $\gamma_j = \mathbf{q}_j^T A \mathbf{q}_j$ , and” to “Let  $\mathbf{g} = (\gamma_1, \gamma_2, \dots, \gamma_m)^T \in \mathbb{R}^m$ , where  $\gamma_j = \mathbf{q}_j^T A \mathbf{q}_j$ . Then  $\gamma_1, \dots, \gamma_m$  are the eigenvalues of  $A$  and”

- Page 541, Eq. (10.94):

Remove extra left parenthesis, so equation should read

$$\Phi(\mathbf{x}) = \prod_{i=1}^n \theta(x_i) = \prod_{i=1}^n (1 - |x_i|)_+.$$

- Page 543, line -6:  
Remove first “the” in “...it is the only the lower intrinsic...”.

### Acknowledgements:

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# Bibliography

- [1] J. Calder. An Elementary Proof of a Minimax Theorem. *arXiv:2511.19416*, 2025. [[arXiv](#)].