Decision Trees

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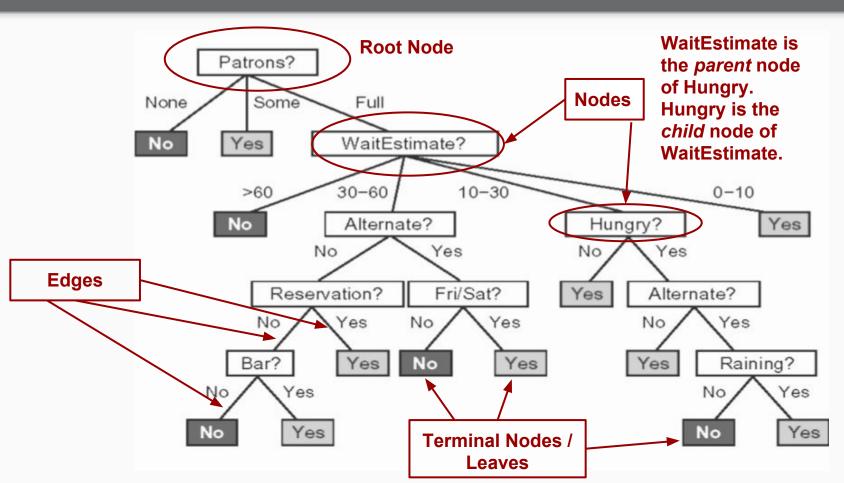




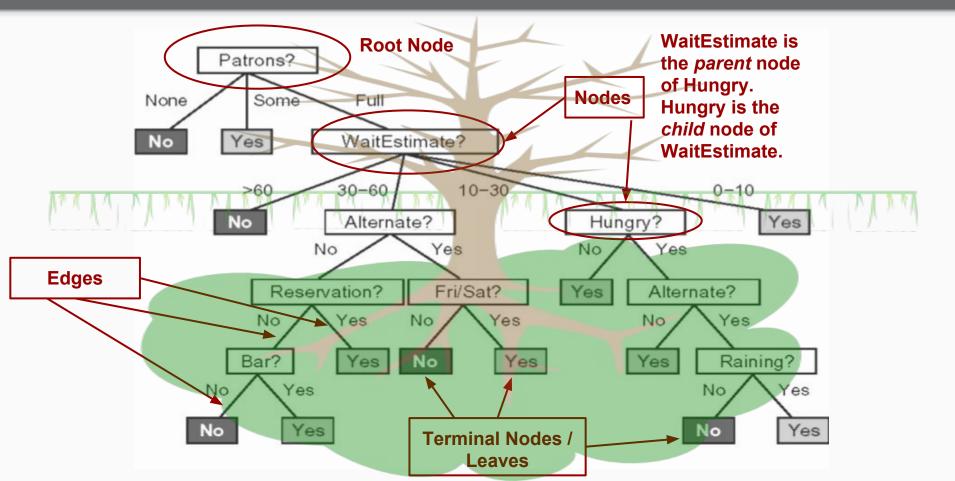
Learning Objectives

- Understand how the algorithm for decision trees works
- Be able to calculate Shannon entropy and information gain
- Explain the concept of recursion and how it relates to decision trees
- Know advantages & disadvantages of decision trees





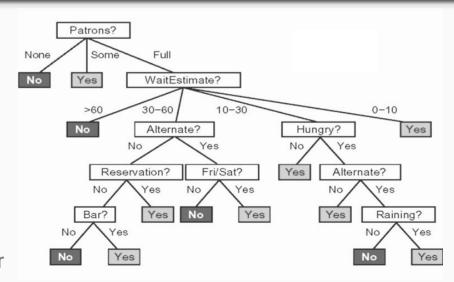




Decision Trees Overview

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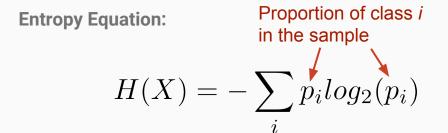
- Supervised learning
- Non-parametric model
- A series of sequential splits
- Each split based on a single feature
 - E.g., split by the wait estimate
- Splits are chosen to best separate the target variable
 - E.g., being hungry vs not being hungry is a good way to differentiate between whether you should go to the restaurant or not
- Target variable can be either categorical (classification tree) or numerical (regression tree)
- Overall goal: minimize error in your predictions of your target variable



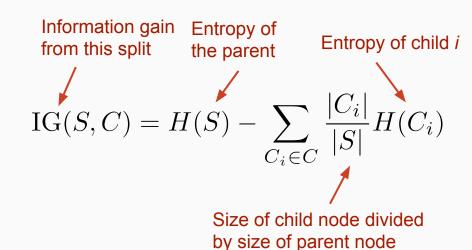
Defining Concepts

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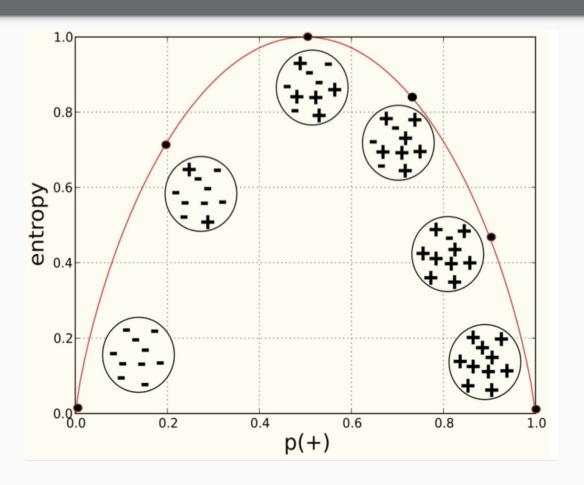
- Entropy a measurement of the diversity in a sample
 - High entropy a sample that is partly made up of dogs and partly made up of horses
 - Low entropy a sample that is 100% dogs
- Decision trees split the data on features to decrease entropy as much as possible
 - We are trying to separate the classes, e.g.,
 split the dogs from the horses
- Information gain a way to measure how much we reduced the entropy by splitting the data in a particular way
 - If we decrease the entropy by a large amount, then we have a large information gain
 - Information gain = parent_entropy mean_child_entropy



Information Gain Equation:







- If the probability of the positive class is 0, entropy is also 0.
- If the probability of the positive class is 1, entropy is 0.
- If the probability of the positive class is 0.5, entropy is at its highest value, 1.0.

The Decision Tree Algorithm

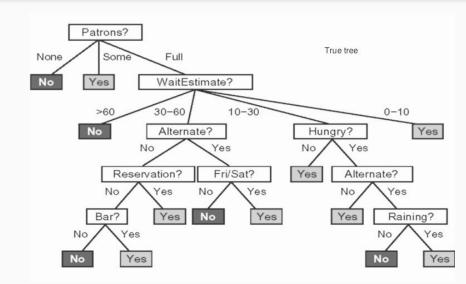


Consider all possible splits on all features

- a. If a feature is categorical, split on value or not value.
- b. If a feature is numeric, split at a threshold: >threshold or <=threshold

2. Calculate & choose the "best" split

- Classification trees the best split is the split that has the highest information gain when moving from parent to child nodes
- b. Regression trees the best split is the split that has the largest reduction in variance when moving from parent to child nodes



Classification Tree: The Splitting Process

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Features:



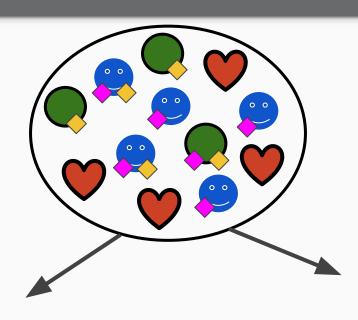


Target Variable Categories:









What feature can we split on to maximize information gain?

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Proportion of class i in the sample $H(X) = -\sum_{i} p_{i} log_{2}(p_{i})$



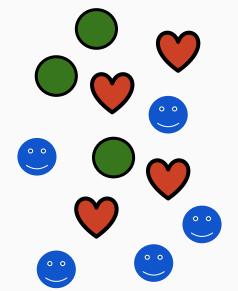
$$P(\bigcirc) = 3/12 = 0.25$$

$$P(\heartsuit) = 4/12 = 0.33$$

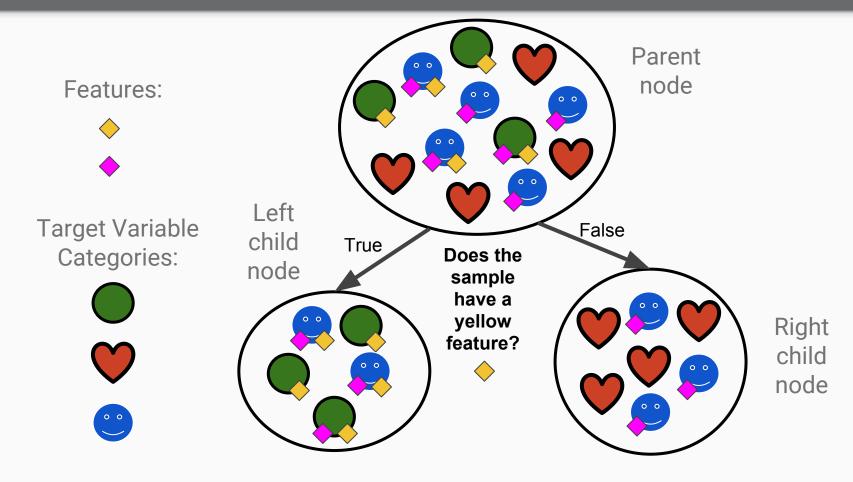
$$P(\bigcirc) = 5/12 = 0.42$$

$$H = -0.25*log_2(0.25) + -0.33*log_2(0.33) + -0.42*log_2(0.42)$$

H = 1.55

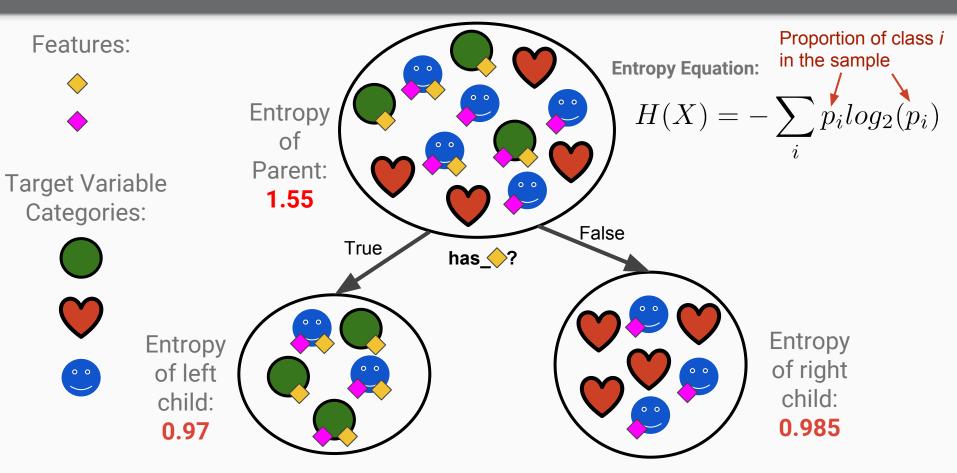


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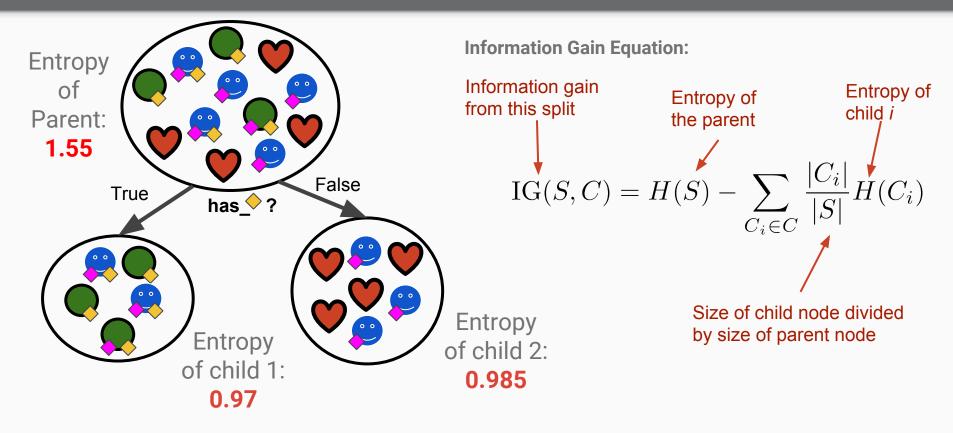


Calculating Entropy for each Node

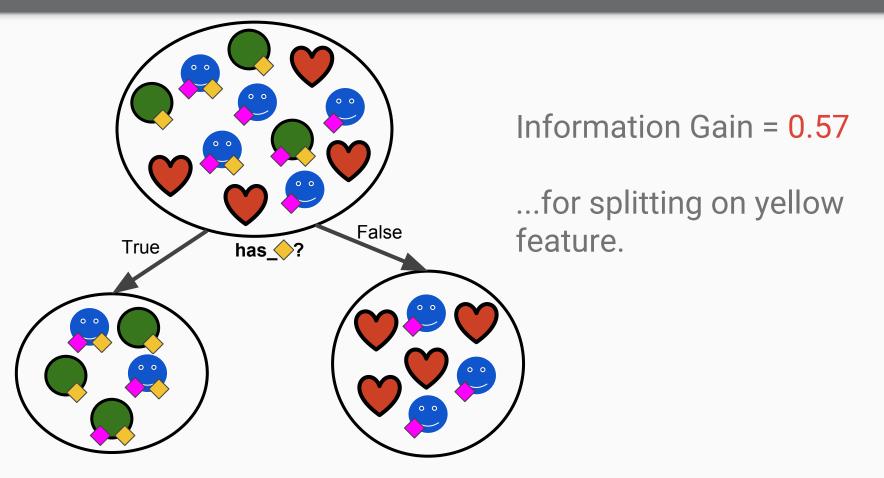
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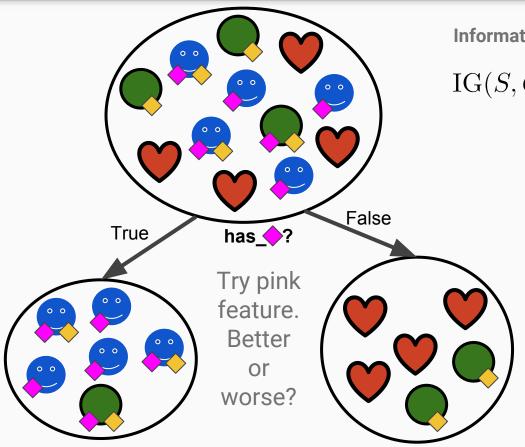






 $IG(parent, \{child_1, child_2\}) = 1.55 - 5/12 * 0.97 - 7/12 * 0.985 = 0.57$

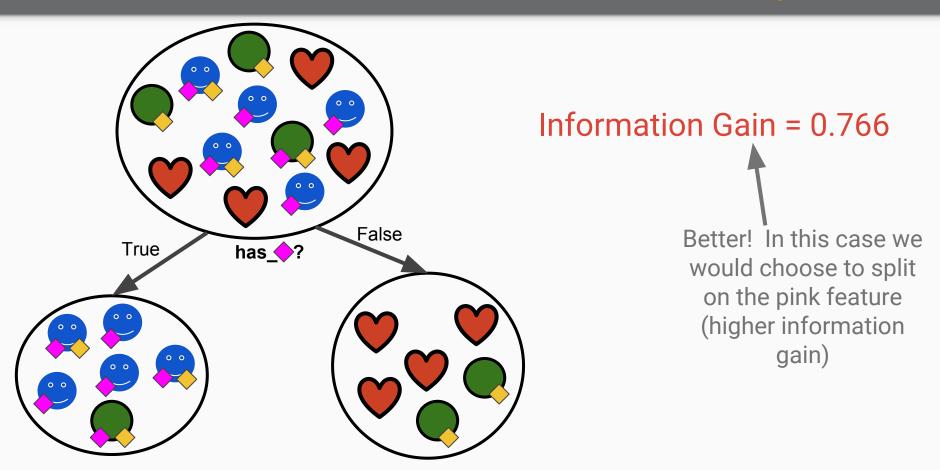




Information Gain Equation:

$$IG(S,C) = H(S) - \sum_{C_i \in C} \frac{|C_i|}{|S|} H(C_i)$$

What is the information gain for splitting on the pink feature?



Comparing Types of Information Gain

Shannon Entropy - Measures the diversity of a sample

$$H(X) = -\sum_{i} p_i log_2(p_i)$$

Information Gain Using Shannon

Entropy

$$IG(S,C) = H(S) - \sum_{C_i \in C} \frac{|C_i|}{|S|} H(C_i)$$

Gini Index - Measures the probability of misclassifying a single element if it was randomly labeled according to the distribution of classes in the sample

$$Gini(S) = 1 - \sum_{i \in S} p_i^2$$

Information Gain Using Gini Index

$$IG(S, C) = Gini(S) - \sum_{C_i \in C} \frac{|C_i|}{|S|} Gini(C_i)$$

Recursion: When a Function Calls Itself

```
def f(x):
 1 1 1
 This function returns x!.
 INPUT: 5
 OUTPUT: 120
  1 1 1
                  Base case
 else:
      return x *
                 Recursive call
```

```
INPUT: f(5)
```

Different ways to write the exact same function:

$$f(x) = \begin{cases} 1, & \text{if } x \le 1\\ xf(x-1), & \text{otherwise} \end{cases}$$

$$f(x) = \prod_{i=1}^{x} i$$

Decision Tree Pseudocode



```
function BuildTree:
 if every item in the dataset is in the same class
 or there is no feature left on which to split the data:
     return a leaf node with the class label
 else:
     find the best feature and value to split the data on
     split the dataset
     create a node
     for each split
         call BuildTree and add the result as a child of the node
     return node
```

Pruning: Preventing Overfitting

- Trees will overfit by default unless you direct them otherwise
- Pruning involves a bias-variance trade-off
- Pre-pruning ideas (pruning while you build the tree)
 - Leaf size: stop splitting when the number of samples left gets small enough
 - Depth: stop splitting at a certain depth (after a certain number of splits)
 - o Purity: stop splitting if enough of the examples are the same class
 - Gain threshold: stop splitting when the information gain becomes too small
- Post-pruning ideas (pruning after you've finished building the tree)
 - Merge terminal nodes if doing so decreases error in your test set
 - Set the maximum number of terminal nodes; this is a form of regularization



Algorithm Options for Decision Trees

- ID3: category features only, information gain, multi-way splits
- C4.5: continuous and categorical features, information gain, missing data okay, pruning
- CART: continuous and categorical features and targets, gini index, binary splits only



Advantages & Disadvantages of Decision Trees

Advantages:

- Easy to interpret
- Non-parametric/more flexible model
- Can incorporate both numerical and categorical features*
- Prediction is computationally cheap
- Can handle missing values and outliers*
- Can handle irrelevant features and multicollinearity

Disadvantages:

- Computationally expensive to train
- Greedy algorithm looks for the simplest, quickest model and may miss the best model (i.e., converges at local maxima instead of global maxima)
- Often overfits
- Deterministic i.e., you'll get the same model every time you run it

Decision Trees in sklearn



- Uses the CART algorithm (see http://scikit-learn.org/stable/modules/tree.html#tree, section 1.10.6)
- Uses Gini Index by default (but you can change it to entropy if you'd like)
- You can prune by varying the following hyperparameters: max_depth, min_samples_split, min_samples_leaf, max_leaf_nodes
- Must use dummy variables for categorical features
 - E.g., a column with ['Red', 'Green', 'Blue'] would need to be coded as separate variables -Is_it_red (Y/N), Is_it_green (Y/N), Is_it_blue (Y/N)
 - See 'Feature Binarization and Encoding Categorical Features' at http://scikit-learn.org/stable/modules/preprocessing.html
- Does not support missing values (even though CART typically does)
- Only supports binary splits



Check in Questions

- Explain how the algorithm for decision trees works.
- How is Shannon entropy calculated?
- How is information gain calculated?
- What is recursion? How does it relate to decision trees?
- What are some advantages of decision trees?
- What are some disadvantages of decision trees?