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5 partim
1  % Queens example
2  n_queens(N, Qs) :-
3      length(Qs, N),
4      Qs ins 1..N, % restricts all values in Qs to values from 1 to N (prevents Queens from being not on the board)
5      safe_queens(Qs).
6
7  safe_queens([]).
8  safe_queens([Q|Qs]) :- safe_queens(Qs, Q, 1), safe_queens(Qs).
9
10 safe_queens([], _, _).
11 safe_queens([Q|Qs], Q0, D0) :-
12     Q0 #\= 0, % Q0 is not equal to Q
13     abs(Q0 - Q) #\= D0, % absolute value of Q0 minus Q cannot be equal to the current diagonal
14     D1 #= D0 + 1, % increment the diagonal
15     safe_queens(Qs, Q0, D1). % recursively call on Qs, Q0, and D1 (incremented diagonal)
16
17 Safe queens gets called as the last statement of n_queens.
18 This call starts by going to the safe_queens which takes a
19 list argument and splits the list into its head and tail as
20 Q and Qs respectively (we are going to label the arguments
21 in this list [A, B, C, D]). Then safe_queens is called and the
22 form with 3 arguments, a list ([B, C, D]), a variable (A), and a 1
23 is called.
24
25 From here Qs is broken down further into its head (B) and tail ([C, D]).
26 A becomes labelled as Q0 and B becomes labelled as Q. the following
27 constraints are then applied
28
29 1. A is not equal to B
30 2. The absolute value of A - B is not equal to 1
31
32 D1 is then set as D0 + 1 (effectively incrementing D0), and safe_queens
33 with three arguments is recursively called with arguments [C, D], A, and D1 (1)
34
35 The following restraints are created by continuing to trace this recursive call
36
37 3. A is not equal to C
38 4. The absolute value of A - C is not equal to 2
39
40 5. A is not equal to D
41 6. The absolute value of A - D is not equal to 3
42
43 At this point we have finished the first safe_queens call in the safe_queens with
44 a single argument. This statement then recursively calls itself on the tail of the
45 list it received causing safe_queens to get called on the tail of the prior list.
46 This repeats until there are no more items in the tail of the list passed to safe
47 queens and we hit our base case. These are the resulting constraints of tracing
48 this algorithm.
49
50 7. B is not equal to C
51 8. The absolute value of B - C is not equal to 1
52
53 9. B is not equal to D
54 10. The absolute value of B - D is not equal to 2
55
56 11. C is not equal to D
57 12. The absolute value of C - D is not equal to 1

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59 % Sudoku puzzle solver
60 sudoku(Rows) :-
61     length(Rows, 9), maplist(same_length(Rows), Rows), % bind the rows to have length of 9
62                                     % bind each element in same length(Rows) to
63                                     % another element in Rows creating a 9x9
64                                     % grid for the sudoku puzzle
65
66     append(Rows, Vs), Vs ins 1..9, % append Rows and Vs, limit the domain of Vs
67                                     % to 1 through 9
68
69     maplist(all_distinct, Rows), % check that all Rows are distinct
70
71     transpose(Rows, Columns), % makes list of columns based on list of rows given
72
73     maplist(all_distinct, Columns), % check that all Columns are distinct
74
75     Rows = [As,Bs,Cs,Ds,Es,Fs,Gs,Hs,Is], % define Rows as A - I
76
77     blocks(As, Bs, Cs), % check that values in the 3 blocks (3x3 squares)
78                                     % found in rows A - C are unique
79
80     blocks(Ds, Es, Fs), % check that values in the 3 blocks found in rows
81                                     % D - F are unique
82
83     blocks(Gs, Hs, Is). % check that values in the 3 blocks found in rows
84                                     % G - I are unique
85
86     blocks([], [], []).
87     blocks([N1,N2,N3|Ns1], [N4,N5,N6|Ns2], [N7,N8,N9|Ns3]) :-
88         all_distinct([N1,N2,N3,N4,N5,N6,N7,N8,N9]), % check that values in a block are unique
89
90         blocks(Ns1, Ns2, Ns3). % recursively call block on tail (row with 3 elements removed)
91
92     problem([[_,_,_,_,_,_,_,_,_], % definition of problem to be solved
93             [_,_,_,_,3,_,8,5],
94             [_,_,1,_,2,_,_,_,_],
95             [_,_,_,5,_,7,_,_,_],
96             [_,_,4,_,_,_,1,_,_],
97             [_,9,_,_,_,_,_,_,_],
98             [5,_,_,_,_,_,7,3],
99             [_,_,2,_,1,_,_,_,_],
100             [_,_,_,_,4,_,_,_,9]]).
101
102 % The first line of sudoku binds the rows to have a length of 9 to give us the row size
103 % of our sudoku grid. An element the same length of the rows is then bound to rows
104 % providing the 9x9 grid for the sudoku puzzle to be held and solved in. Rows and Vs
105 % (our values for each spot in the grid) are then appended and Vs is given a constrained
106 % domain of values 1-9 (the valid values that can exist in the grid of a sudoku puzzle).
107 % all_distinct is then mapped to Rows to make sure that all the Rows are distinct.
108 % transpose then creates a list of columns based off of a list of rows given and these
109 % columns are checked to make sure that they are all distinct. We then define rows A - I
110 % in a list of rows. At this point we have created a sudoku puzzle with distinct rows
111 % and columns and the last thing to check is the 3x3 blocks existing around the edges
112 % and center of the puzzle. This is checked by putting rows A-C, D-F, and G-I into the blocks
113 % statement and check that the first, middle, and last 3 values of each are all distinct
114 % from the first, middle, and last 3 values of the others (all these values must be
115 % distinct as they are what constitutes a block). If this check passes then we are left with
116 % a valid sudoku puzzle.

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118 % Knights and Knaves
119
120 /* You meet two people
121 Person A says at least one of the following is true:
122 |   that I am a knight or that Person B is a knight
123 Person B says Person A could say that I am a knave */
124 :- use_module(library(clpb)).
125
126 knights(1, [A,B]) :-
127     sat(A :- ((A :- 1) + (B :- 1))),
128     sat(B :- (A :- -B)).
129
130 % knights(1, [A,B]).
131 % A = B, B = 0
132
133 /* You meet three people
134 Person A says that Person B is a knave
135 Person B says that it is false that Person C is a knave
136 Person C says I am a knight or Person A is a knight */
137
138 knights(2, [A,B,C]) :-
139     sat(A :- -B),
140     sat(B :- C),
141     sat(C :- ((C :- 1) + (A :- 1))).
142
143 % knights(2, [A,B,C]).
144 % A = 0,
145 % B = C, C = 1
146
147 /* You meet 4 people
148 Person A tells you that Person C could say that Person B is a knave
149 Person B says that Person C is a knave
150 Person C says only a knave would say that Person D is a knave
151 Person D says I and Person A are different*/
152
153 knights(3, [A,B,C,D]) :-
154     sat(A :- (C :- -B)),
155     sat(B :- -C),
156     sat(C :- (1 :- -D)),
157     sat(D :- -A).
158
159 % knights(3, [A,B,C,D]).
160 % A = C, C = 1,
161 % B = D, D = 0

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1 :- use_module(library(clpfd)).
2
3 crypt1([H1|L1], [H2|L2], [H3|L3], L4) :-
4     L4 ins 0..9, % Give constraints on variable values in L4
5     H1 #\= 0, H2 #\= 0, H3 #\= 0, % Heads cannot have value 0
6     all_distinct(L4), % Variable values are distinct in L4
7     reverseWord([H1|L1], R1, []), % Reverse the 3 input words
8     reverseWord([H2|L2], R2, []),
9     reverseWord([H3|L3], R3, []),
10    helper(R1, R2, R3, 0). % Call to helper function that does the sum with reversed words one iteration at a time
11
12
13 reverseWord([], X, X). % base case: returns reversed list when entered list is empty
14 reverseWord([H|T], X, A) :- % recursive case: takes head and adds it to accumulator list
15     reverseWord(T, X, [H|A]).
16
17 % first word, second word, third word, num iterations, carry1, carry2
18 helper([], [], [C], C) :-
19     helper([], [H2|T2], [H3|T3], C) :-
20         H3 #= (H2 + C) mod 10,
21         H2 + C #= H3 + (C1*10),
22         helper([], T2, T3, C1).
23
24 helper([H1|T1], [], [H3|T3], C) :-
25     H3 #= (H2 + C) mod 10,
26     H2 + C #= H3 + (C1*10),
27     helper(T2, [], T3, C1).
28
29 helper([H1|T1], [H2|T2], [H3|T3], C) :-
30     H3 #= (H1 + H2 + C) mod 10,
31     H1 + H2 + C #= H3 + (C1*10),
32     helper(T1, T2, T3, C1).
33
34 /*
35 crypt1([S,E,N,D],[M,O,R,E],[M,O,N,E,Y],[D,N,E,S,R,O,M,Y]), labeling([ff],[D,N,E,S,R,O,M,Y]).
36 D = 7,
37 E = 5,
38 M = 1,
39 N = 6,
40 O = 0,
41 R = 8,
42 S = 9,
43 Y = 2
44 false <- this false shows that there are no other solutions
45
46 crypt1([T,H,I,S],[O,D],[M,O,R,K],[T,H,I,S,D,O,E,W,R,K]), labeling([ff],[T,H,I,S,D,O,E,W,R,K]).
47 O = 2,
48 E = 8,
49 H = 0,
50 I = 4,
51 K = 5,
52 O = 0,
53 R = 7,
54 S = 6,
55 T = 1,
56 W = 3
57 |
58 O = 2,
59 E = 8,
60 H = 0,
61 I = 4,
62 K = 5,
63 O = 6,
64 R = 7,
65 S = 9,
66 T = 1,
67 W = 3
68
69 This one had a lot of solutions so here are the first two
70 */

```