## Training Neural Networks I

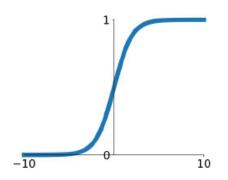


Fast Campus
Start Deep Learning with Tensorflow

#### **Activation Functions**

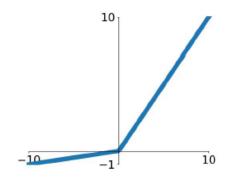
#### **Sigmoid**

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$



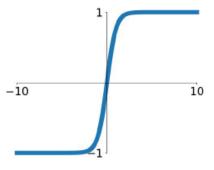
#### Leaky ReLU

 $\max(0.1x, x)$ 



#### tanh

tanh(x)

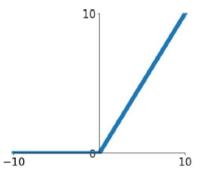


#### **Maxout**

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

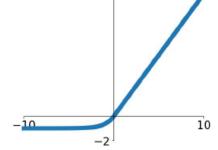
#### ReLU

 $\max(0, x)$ 

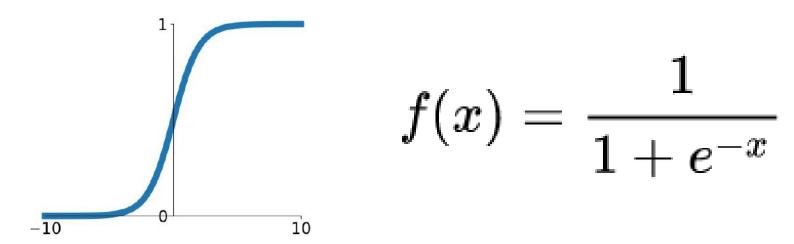


#### **ELU**

$$\begin{cases} x & x \ge 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



## Sigmoid

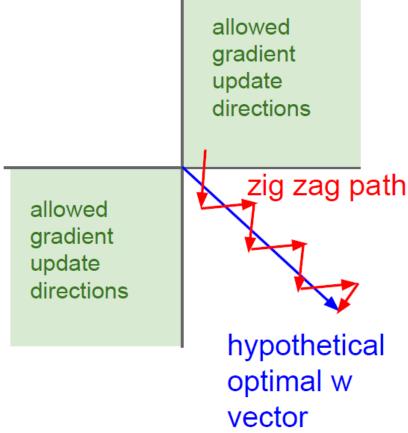


- Squashes numbers to range [o, 1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron
- 3 Problems
  - Saturated neurons "kill" the gradients
  - Sigmoid outputs are not zero-centered
  - Exp() is a bit compute expensive

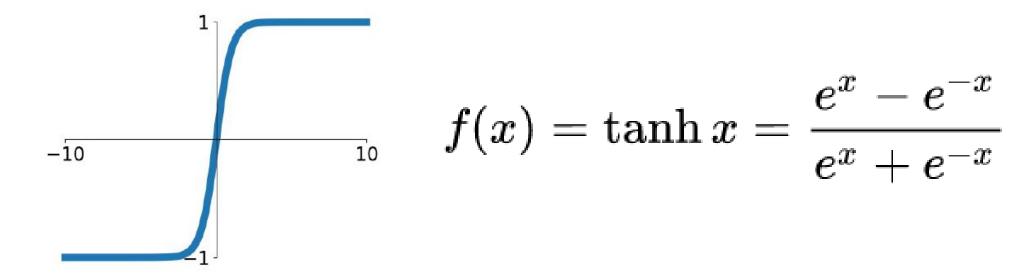
What happens when the input to a neuron is always positive

$$f\left(\sum_{\pmb{i}} w_{\pmb{i}} x_{\pmb{i}} + b
ight)$$

- What can we say about the gradients on w?
- → Always all positive or all negative
- This is also why you want zero-mean data

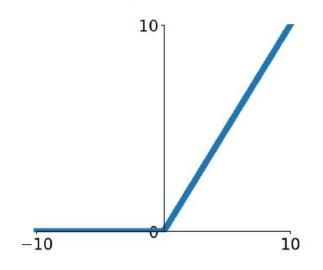


#### Tanh



- Squashes numbers to range [-1, 1]
- Zero centered
- Still kills gradient when saturated

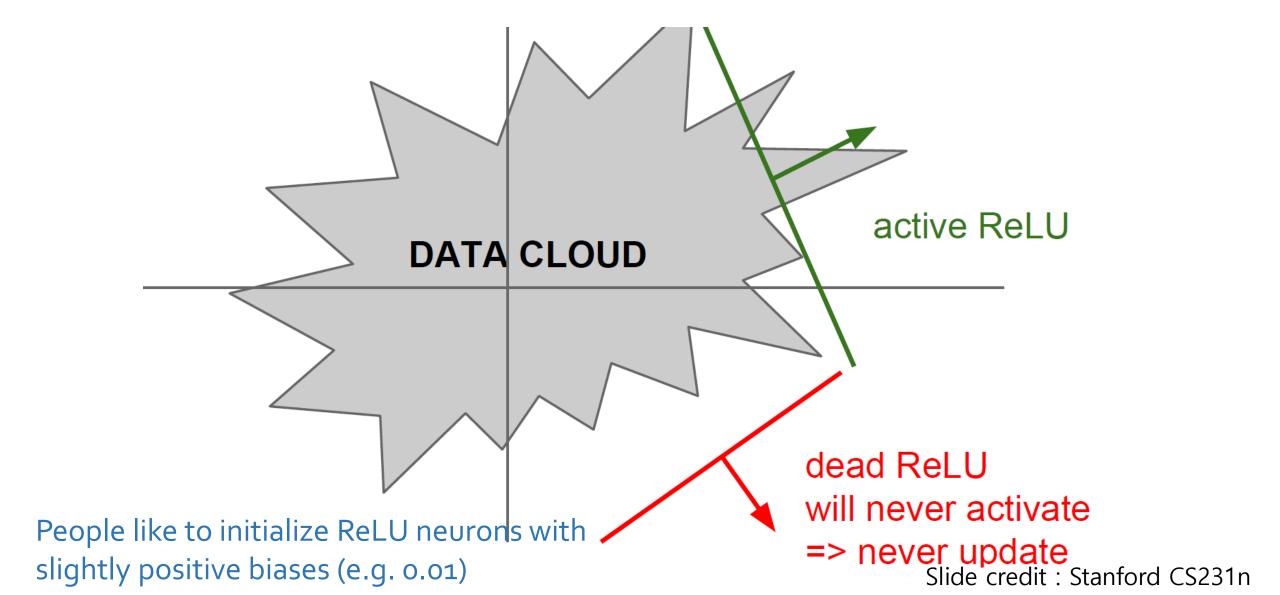
#### ReLU(Rectified Linear Unit)



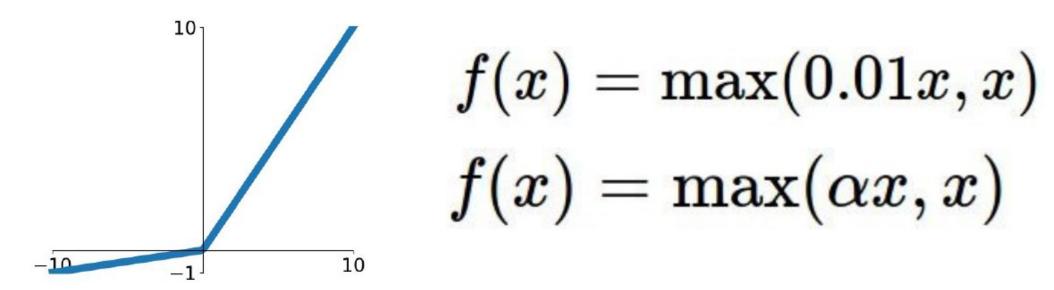
Computes f(x) = max(0,x)

- Does not saturate
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice(e.g. 6x)
- Actually more biologically plausible than sigmoid
- Problems
  - Not zero-centered output
  - An annoyance dead ReLU

#### Dead ReLU

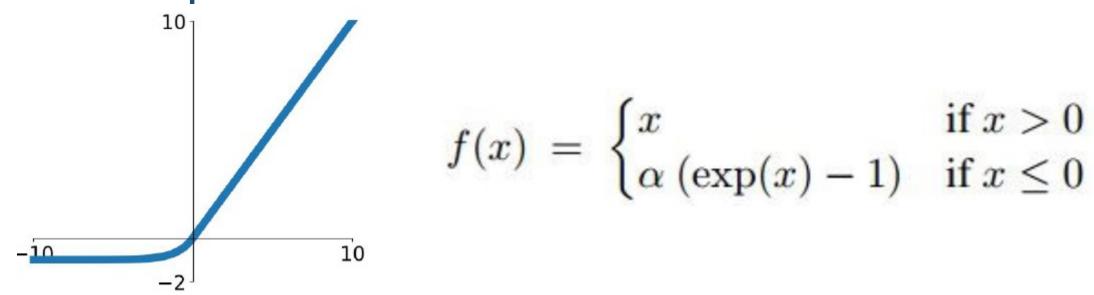


## Leaky ReLU, PReLU(Parametric-)



- Does not saturate
- Computationally efficient
- Converge much faster than sigmoid/tanh
- Will not 'die'

#### ELU(Exponential Linear Units)



- All benefits of ReLU
- Closer to zero mean output
- Computation requires exp()

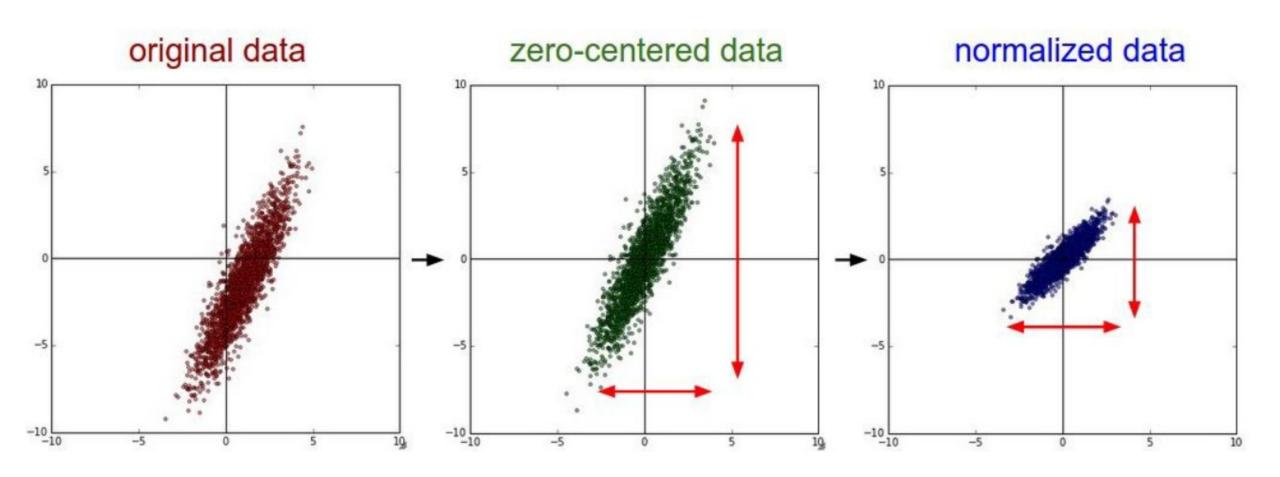
#### Maxout

- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

- Problem
  - Doubles the number of paramters/neuron

## **Data Preprocessing**



## In Practice for Images

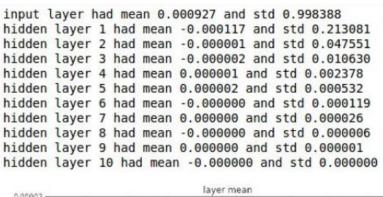
- E.g. consider CIFAR-10 example with [32, 32, 3] images
- Subtract the mean image (e.g. AlexNet)
  - Mean image = [32, 32, 3] array
- Subtract per-channel mean (e.g. VGGNet)
  - Mean along each channel = 3 numbers
- Not common to normalize variance

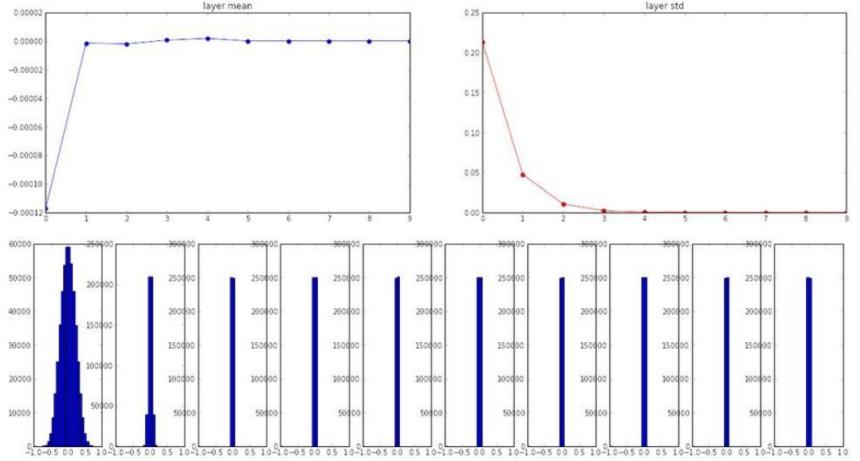
## Weight Initialization

- First idea: Small random numbers
  - Gaussian with zero mean and 1e-2 standard deviation

$$W = 0.01* np.random.randn(D,H)$$

- Let's look at some activation statistics
  - 10-layer network with 500 neurons on each layer
  - Using tanh activation funtion



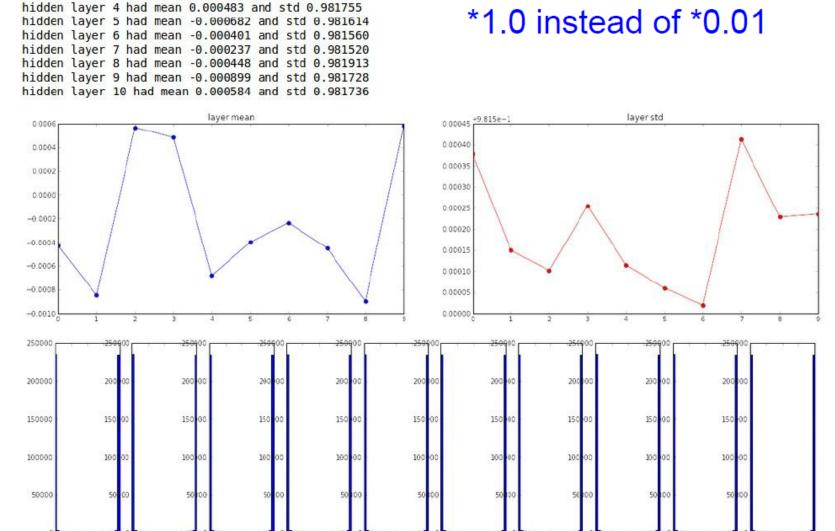


# All activations become zero!

Q: think about the backward pass. What do the gradients look like?

Hint: think about backward pass for a W\*X gate.

# w = np.random.randn(fan\_in, fan\_out) \* 1.0 # layer initialization input layer had mean 0.001800 and std 1.001311 hidden layer 1 had mean -0.000430 and std 0.981879 hidden layer 2 had mean -0.000849 and std 0.981649 hidden layer 3 had mean 0.000566 and std 0.981601

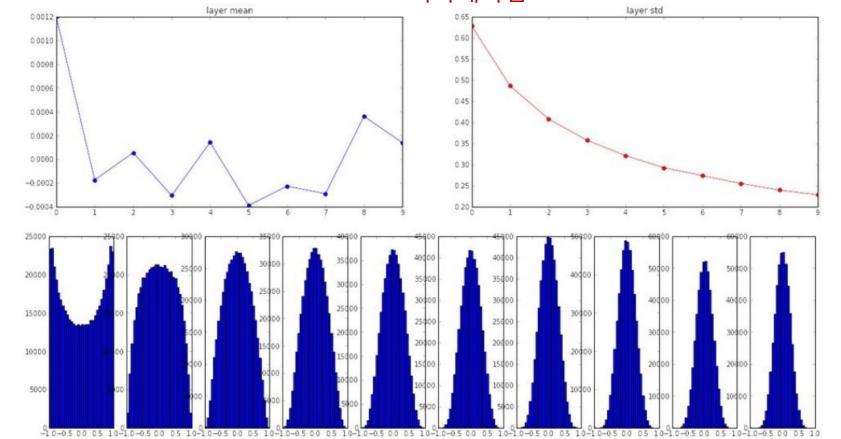


Almost all neurons completely saturated, either -1 and 1. Gradients will be all zero.

input layer had mean 0.001800 and std 1.001311
hidden layer 1 had mean 0.001198 and std 0.627953
hidden layer 2 had mean -0.000175 and std 0.486051
hidden layer 3 had mean 0.000055 and std 0.407723
hidden layer 4 had mean -0.000306 and std 0.357108
hidden layer 5 had mean 0.000142 and std 0.320917
hidden layer 6 had mean -0.000389 and std 0.292116
hidden layer 7 had mean -0.000228 and std 0.273387
hidden layer 8 had mean -0.000291 and std 0.254935
hidden layer 9 had mean 0.000361 and std 0.239266
hidden layer 10 had mean 0.000139 and std 0.228008

W = np.random.randn(fan\_in, fan\_out) / np.sqrt(fan\_in) # layer initialization

Input neuron 수가 다른데 같은 initialization 값을 사용하는 것은 문제가 있음 → input 이 많으면 더 작은 weight 값으로 시작해야함 "Xavier initialization" [Glorot et al., 2010]

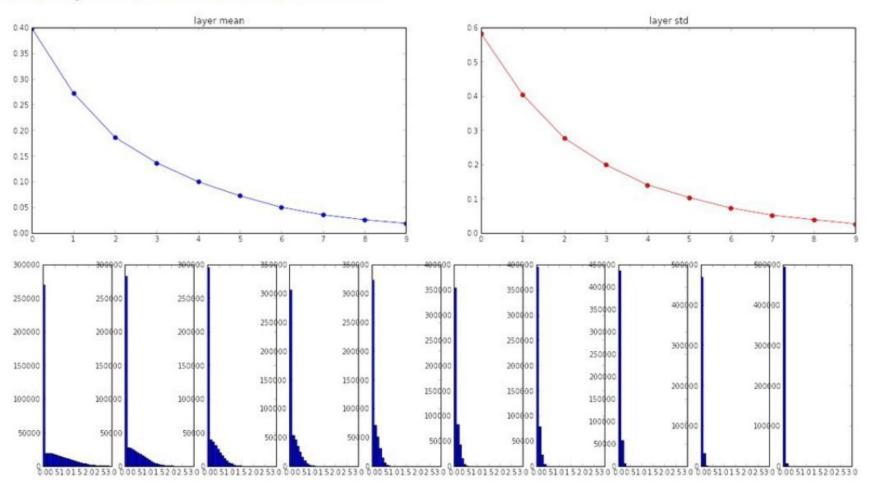


Reasonable initialization. (Mathematical derivation assumes linear activations)

```
input layer had mean 0.000501 and std 0.999444
hidden layer 1 had mean 0.398623 and std 0.582273
hidden layer 2 had mean 0.272352 and std 0.403795
hidden layer 3 had mean 0.186076 and std 0.276912
hidden layer 4 had mean 0.136442 and std 0.198685
hidden layer 5 had mean 0.099568 and std 0.140299
hidden layer 6 had mean 0.072234 and std 0.103280
hidden layer 7 had mean 0.049775 and std 0.072748
hidden layer 8 had mean 0.035138 and std 0.051572
hidden layer 9 had mean 0.025404 and std 0.038583
hidden layer 10 had mean 0.018408 and std 0.026076
```

```
W = np.random.randn(fan_in, fan_out) / np.sqrt(fan_in) # layer initialization
```

## but when using the ReLU nonlinearity it breaks.



## Weight Initialization

- Xavier Initialization
  - Activation function은 linear라고 가정하고, in/out의 variance를 같게 해보자

forward: 
$$Var(W_i) = \frac{1}{n} = \frac{1}{n_{\rm in}}$$

backward: 
$$Var(W_i) = \frac{1}{n_{\text{out}}}$$

Navier 
$$Var(W_i) = rac{2}{n_{
m in} + n_{
m out}}$$

## Weight Initialization

- He Initialization
  - Activation function을 ReLU나 PReLU로 하고, variance를 같게 해보자

ReLU

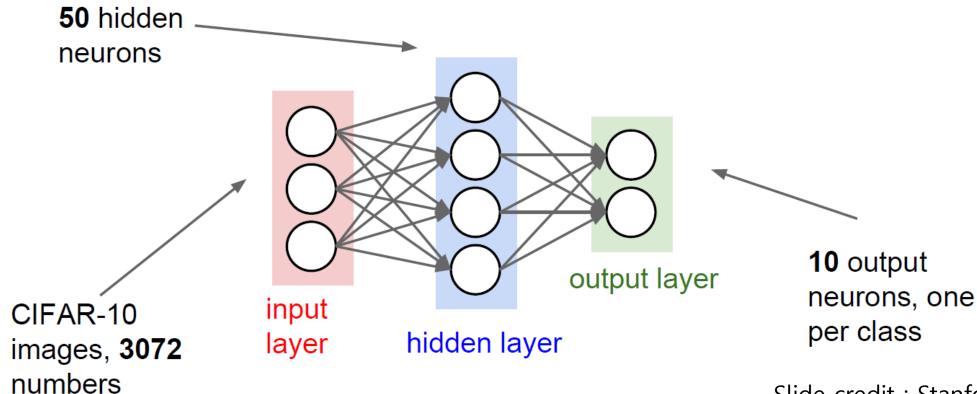
$$Var[w_l] = \frac{2}{n_l} \implies \text{standard deviation (std)} = \sqrt{\frac{2}{n_l}}$$

$$W_l \sim \mathcal{N}\left(0, \sqrt{\frac{2}{n_l}}\right) \text{ and } \mathbf{b} = 0$$

PReLU 
$$\frac{1}{2}(1+a^2)n_l \underline{Var[w_l]} =$$

## Babysitting the Learning Process

- Preprocess the data
- 2. Choose the architecture
  - How many layers? How many hidden neurons? ...



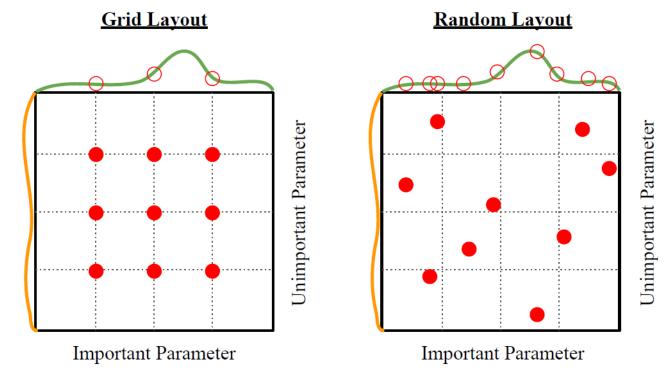
## Babysitting the Learning Process

- 3. Double check that the loss is reasonable
  - Initial loss must be about —log(1/n) w/o regularization loss
  - w/ regularization loss, loss must increase
- 4. Let's try to train now  $\rightarrow$  make sure that you can overfit very small portion of the training data
  - Take the small examples(e.g. 20) from training set
  - Turn off regularization
  - Use simple vanilla sgd

## Babysitting the Learning Process

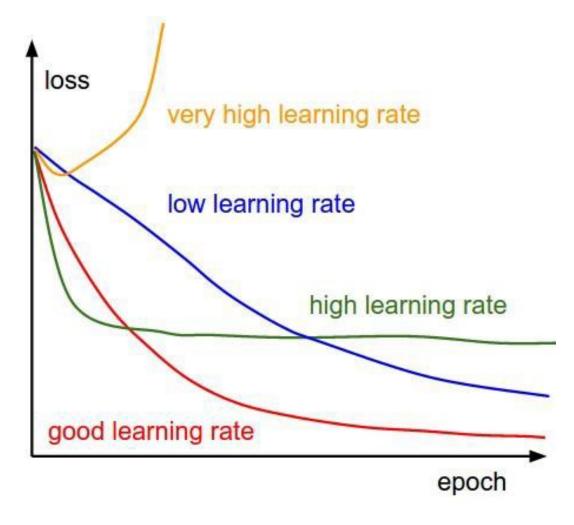
#### 5. Search a good learning rate(cross-validation strategy)

- First stage : only a few epochs to get rough idea of what params work
- Second stage : longer running time, finer search
- Random Search vs Grid Search → Use Random Search!



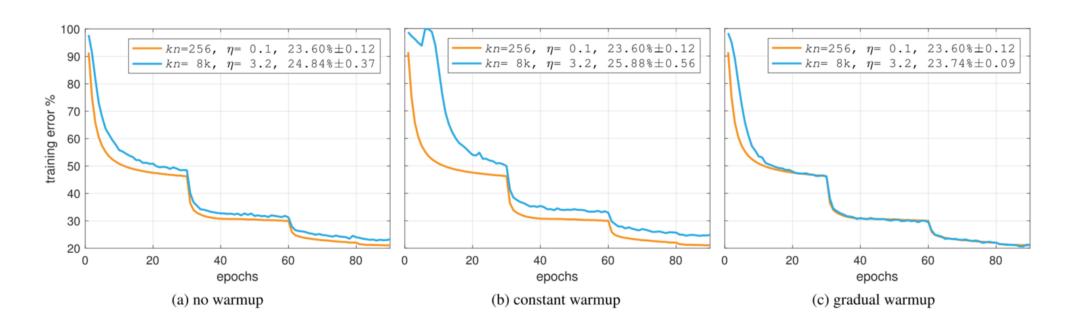
## Learning Rate

• learning rate에 따라서 최종 결과가 달라짐



## Learning Rate Decay

- Learning rate이 너무 크면 수렴을 못할 가능성이 있고, 너무 작으면 local minima 혹은 saddle point에서 못빠져나옴
- Learning Rate Decay
  - 처음에는 크게 움직이다가 일정 조건이 되면 learning rate을 낮춰서 점점 작게 움직이는 방법



## Cyclic Learning Rate

- Learning rate decay로 saddle point를 빠져나갈 수 있을까?
- Saddle point에서는 learning rate을 키워서 빠져나가는 것이 효과 적일 수 있음 → Learning rate을 주기적으로 변경해보자

