STA610 Case Study 1

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Introduction

Prescription opioid abuse has recently become an epidemic in the United States. The price of illicit prescription opioids indicates the supply-demand relationship of the drug. This case study aims to explore the relationship between the unit price of drugs and other factors such as the quantity purchased, the location of the transaction, and strength of the drug. More specifically, our group's interest is to explore the factors related to the cost per milligram and the heterogeneity in the region. The dataset we will be using is provided by StreetRx, a reporting tool for people at large to anonymously report the price they paid or heard for diverted prescription drugs. Our drug of interest is Morphine which is used to "relieve moderate to severe pain and may be habit-forming," especially with prolonged use (MedlinePlus).

Data Cleaning & EDA

Missing Values

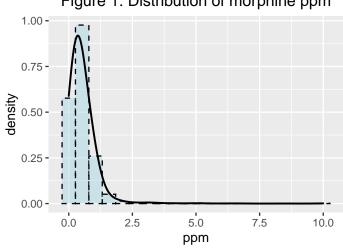
The subset of the StreetRx dataset pertaining to Morphine contains 9,268 observations with 13 variables. There are 13,443 empty cells, including both missing values and blank entries. To maintain the statistical power and avoid bias, our group decided to recode both the empty cells and "0 Reporter did not answer this question" in Primary_Reason (5061 in total) as "8 Prefer not to answer" and recode the empty cells in source (3942 in total) as "Blank" because of the high missing rates. Then, we removed other rows with missing values.

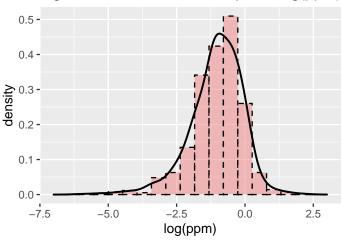
Additionally, we removed non-positive price values as well as price values greater than 10. Since the data is self-reported, these extremely expensive prices are likely due to users misunderstanding the system and reporting total price instead of unit price. The number of observations is now 5,582.

Response Variable: Price per milligram

Figure 1: Distribution of morphine ppm

Figure 2: Distribution of morphine log(ppm)





Whether we fit a hierarchical model or linear regression, the response variable should be normally distributed. Although the normality assumption pertains to the conditional distribution of our response variable, it's still beneficial to check the assumption for the marginal distribution as a very skewed marginal distribution could persist and affect the model's resulting conditional distribution. From the histogram on the left, the distribution of ppm is clearly right-skewed. Since ppm is strictly non-negative, a log transformation may be appropriate. We can see that the distribution of log(ppm), given above, appears to be much closer to the desired normal distribution.

Grouping Variable: city, state, and region

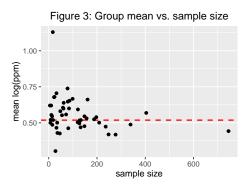
Since we want to analyze the heterogeneity in pricing by location, we have three choices of grouping variables, city, state, and USA_region.

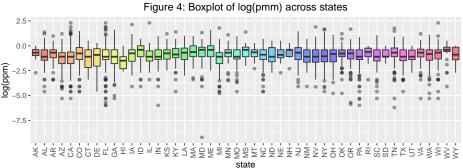
City

There are 1642 unique city values, and many cities have small sample size (i.e. less than 5 observations). We decide not to use city as the grouping variable (see appendix).

State

As for the state, we examined the sample sizes in each group and decided to filter out Puerto Rico and Vermont because they have less than 5 observations.



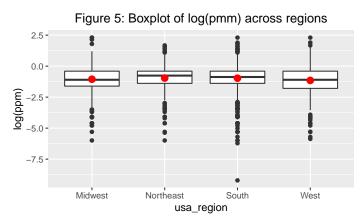


We then inspect the state-level differences more closely by plotting the group-level means against the sample sizes. We observed that the within-state means for states with smaller sample sizes vary a lot, while the withinstate means for states with higher sample sizes in general adhere more closely to the grand mean. This is conducive to the borrowing of information between states with a hierarchical model. From the above boxplot of log(ppm) against state, it is also evident that the log(ppm) distributions differ across states. This indicates the potential state-level differences in drug prices. Therefore, we decide to use state as our grouping variable at this stage.

Region

From the boxplot we see that the <code>log(ppm)</code> distributions differ slightly across regions, though not as much as across states. We may also consider using region as the grouping variable.

| | usa_region | n | mean |
|---|------------|------|--------|
| 1 | Midwest | 1168 | -1.056 |
| 2 | Northeast | 674 | -0.962 |
| 3 | South | 1953 | -0.972 |
| 4 | West | 1773 | -1.151 |

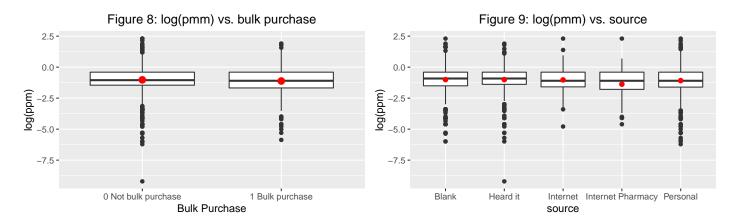


Date (price_date)

As for the price_date, we noticed some observations are prior to the establishment of StreetRx, which are likely incorrect inputs. We dropped the observations before 2010. For the remaining observations, we came up with two ways of data cleaning. The first choice is to choose a starting date and convert the feature as the date differences (date_diff) from that starting date. The second choice is to split this date variable into two components, year and quarter, to explore the trend of unit drug price over time and the seasonality.

Our visualizations suggested there is no clear indication that the log value of per milligram price of morphine varies along with date_diff. However, for different year and quarter, the log(ppm) value varies slightly (see appendix).

Bulk_purchase & Source



There is no need to conduct any data cleaning on bulk_purchase. From the boxplot we see that there is a slight trend that the drug price may be lower if purchased in bulk. Therefore, bulk_purchase might be a potential predictor.

For the feature source, we have recoded the missing value as "Blank" and the name of websites as "Internet". We also dropped the only observation whose source is "Drug Forum". The boxplot shows that the log(ppm) value varies among different sources (see appendix).

Dosage Strength & Primary Reason



From the scatter plot of log(ppm) against mgstr, there is a slight trend that the larger the dosage strength, the smaller the per milligram price. We have also noticed that mgstr only takes 16 discrete values. Therefore, we decided to transform it into 4 levels ("low", "medium", "medium high", and "high") based on the 0.25, 0.5, and 0.75 quantiles of mgstr. From the boxplot, the trend that the log(ppm) values decrease as the dosage strength increases is more clear when using these new levels.

For primary_reason, we have converted the empty cells and "0 Reporter did not answer this question" to "8 Prefer not to answer". The log(ppm) value varies among different reasons for purchasing morphine (see appendix).

Interaction

We also inspected how predictors interact with each other, i.e. whether the effect of one predictor on the unit price of morphine is influenced by any other predictor. We found that there might by potential interaction among dosage strength, and quarter, or quarter, and primary reason (see appendix). In the modeling part, we will check whether there are interactions in a more formal way.

Model

Initial Model & Model Selection

The goal of our analysis is to investigate factors related to the per milligram price of morphine and explore heterogeneity in pricing by location. As discussed in the EDA part, we do not have enough data to estimate the effects at the city level. Meanwhile, the drug prices do not seem to change significantly across regions. Thus, the state variable is the prefered choice of accounting for location. Since many states have relatively small sample sizes, a hierarchical model allows us to borrow information across states.

Comparing three full models with different grouping variables, the AIC and BIC score also suggest choosing state as the group-level variable.

Our baseline model incorporates only the state-level random intercepts. For other individual-level predictors, we add one variable to the model each time and use both the Likelihood Ratio test and the BIC score to determine whether it should be added. The LRT is designed for nested models while the BIC score considers

Table 1: AIC and BIC for different grouping variables

| Grouping | AIC | BIC |
|----------|----------|----------|
| City | 15408.58 | 15428.46 |
| State | 15354.88 | 15374.76 |
| Region | 15400.48 | 15420.36 |

both the likelihood and the model complexity and gives a more general sense of model performance while also being consistent. Tables 1 and 2 display the results of model selection. We also used the full model as a starting point to perform stepwise backward elimination with the results agreeing with the previous model selection method. (See appendix).

Our final model incorporates the grouping variable state and the individual level predictors mgstr (recoded as 4 levels), as well as bulk_purchase, quarter, and source.

Table 2: Forward model selection

| Model | LRT.p.value | BIC |
|--|-------------|----------|
| (1 state) | | 15374.76 |
| (1 state) + mgstr2 | 0 | 14615.63 |
| $(1 state) + mgstr2 + bulk_purchase$ | 2e-04 | 14610.01 |
| $(1 state) + mgstr2 + bulk_purchase + year$ | 0.1079 | 14673.21 |
| $(1 state) + mgstr2 + bulk_purchase + quarter$ | 0.0213 | 14626.19 |
| $(1 state) + mgstr2 + bulk_purchase + date_diff$ | 0.1844 | 14616.87 |
| $(1 state) + mgstr2 + bulk_purchase + quarter + source$ | 7e-04 | 14641.45 |
| (1 state) + mgstr2 + bulk_purchase + quarter + source + primary_reason | 1 | 14681.42 |

Interactions

From the EDA, we see some potential interactions between predictors (see appendix). Here, we also tried to incorporate all possible two-way interactions into the model (one at a time), but non of them seem to pass the LRT test or improve the model BIC score (see appendix). To control the model complexity, we did not try any three-way or more complex interaction terms. Therefore, we decided not to add any interaction term into the final model.

Final Model

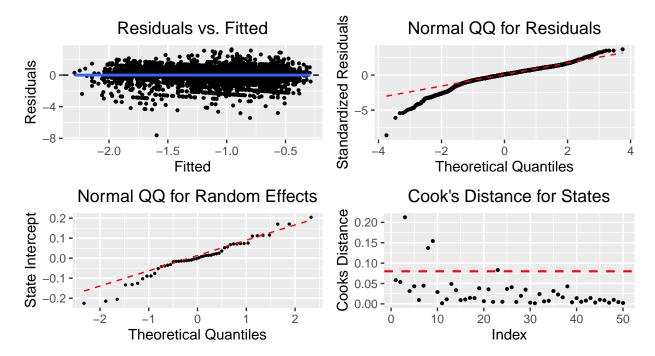
Our final model is

$$\begin{split} log(y_{ij}) = \beta_0 + b_{0j} + \beta_1 M_{ij} + \beta_2 B_{ij} + \beta_3 Q_{ij} + \beta_4 S_{ij} + \epsilon_{ij} \\ b_{0j} \stackrel{iid}{\sim} \mathcal{N}(0, \tau^2) \perp \epsilon_{ij} \stackrel{iid}{\sim} \mathcal{N}(0, \sigma^2) \end{split}$$

The response variable and predictors are defined as:

- $y_i j$: Per milligram price of morphine for individual i in state j
- M_{ij} : Dosage strength in mg of the units purchased, factored into 4 levels
- B_{ij} : Bulk purchase, an indicator for whether 10+ units were purchased at once
- Q_{ij} : Quarter of the reported purchase
- S_{ij} : Source of information (including first-hand and second-hand sources)

Model Diagnostics



- Residual vs. Fitted plot: The residuals are spread equally around the horizontal line, indicating there is no non-linear relationship.
- Normal QQ plot for residuals: The normality assumption is slightly met since our residuals adhere around the diagonal line representing normality but have heavy tails on both sides. We also have one data point that deviates severely from the diagonal line.
- Normal QQ plot for Random Effects: We can accept the random effects are normally distributed. But we still have three outliers.
- Cook's Distance: We have 3 highly influential states (Florida, Pennsylvania, and California) whose Cook's distance exceeds the $\frac{4}{n}$ cutoff, where n denotes the number of states.

To address the violated assumptions, we tried to remove the data point with the lowest residual and the influential groups. By removing the influential observation, the normality of the residuals improved a little bit, and the dots aligned more tightly to the diagonal line. However, removing the influential states does not drastically improve the normality of the residuals (see appendix). Moreover, the influential states have a considerable sample size (1382 observations). Therefore, we decide only to drop the individual level outlier but keep all the groups.

Conclusion

Fixed Effects

- Quarter (baseline: Quarter1): Compared with quarter 1, holding all other predictors unchanged, purchasing the morphine in quarter 2, the per milligram price of the drug will increase by a multiplicative effect of $e^{0.0853} = 1.0891$ (about 8.91%). Similarly, if the drug is purchased in quarter 3 or 4, the drug price will increase by 8.77% and 8.81%, respectively.
- Source (baseline: Blank): Compared with an unknown source, holding all other predictors unchanged, the per milligram drug price heard from other people will increase by a multiplicative effect of $e^{0.0633} = 1.0653$ (about 6.53%). Similarly, the price information obtained from the internet, internet pharmacy, or personal purchase will decrease by 0.41%, 27.58%, and 3.91%, respectively.

Table 3: Estimates of fixed effects

| | Estimate | exp(Estimate) | Std. Error | df | t value | Pr(> t) |
|------------------------------|----------|---------------|------------|-----------|----------|----------|
| (Intercept) | -0.6346 | 0.5301 | 0.0393 | 296.1819 | -16.1290 | 0.0000 |
| quarter2 | 0.0854 | 1.0891 | 0.0321 | 5550.5948 | 2.6578 | 0.0079 |
| quarter3 | 0.0841 | 1.0877 | 0.0332 | 5555.0726 | 2.5349 | 0.0113 |
| quarter4 | 0.0844 | 1.0881 | 0.0341 | 5551.1650 | 2.4759 | 0.0133 |
| sourceHeard it | 0.0633 | 1.0653 | 0.0335 | 5556.1197 | 1.8904 | 0.0588 |
| sourceInternet | -0.0041 | 0.9959 | 0.0625 | 5555.5822 | -0.0656 | 0.9477 |
| sourceInternet Pharmacy | -0.3227 | 0.7242 | 0.1016 | 5548.9347 | -3.1743 | 0.0015 |
| sourcePersonal | -0.0398 | 0.9609 | 0.0281 | 5557.7473 | -1.4157 | 0.1569 |
| mgstr22 medium | -0.3816 | 0.6827 | 0.0279 | 5549.1951 | -13.6631 | 0.0000 |
| mgstr23 medium high | -0.7000 | 0.4966 | 0.0365 | 5554.7006 | -19.1836 | 0.0000 |
| mgstr24 high | -1.1197 | 0.3264 | 0.0420 | 5559.7107 | -26.6889 | 0.0000 |
| bulk_purchase1 Bulk purchase | -0.1141 | 0.8922 | 0.0296 | 5557.9880 | -3.8488 | 0.0001 |

- Dosage Strength (baseline: Low): Compared with low dosage strength, holding all other predictors unchanged, the per milligram price of morphine will decrease by a multiplicative effect of $e^{-0.3816} = 0.6827$ (about 31.73%) if it has medium dosage strength. Similarly, if the dosage strength is medium-high or high, the drug price will decrease by 50.34% and 67.36%, respectively.
- Bulk Purchase (baseline: Not bulk purchase): Compared with non-bulk purchase, holding all other predictors unchanged, the unit price of morphine will decrease by a multiplicative effect of $e^{0.1141} = 0.8922$ (about 10.78%).

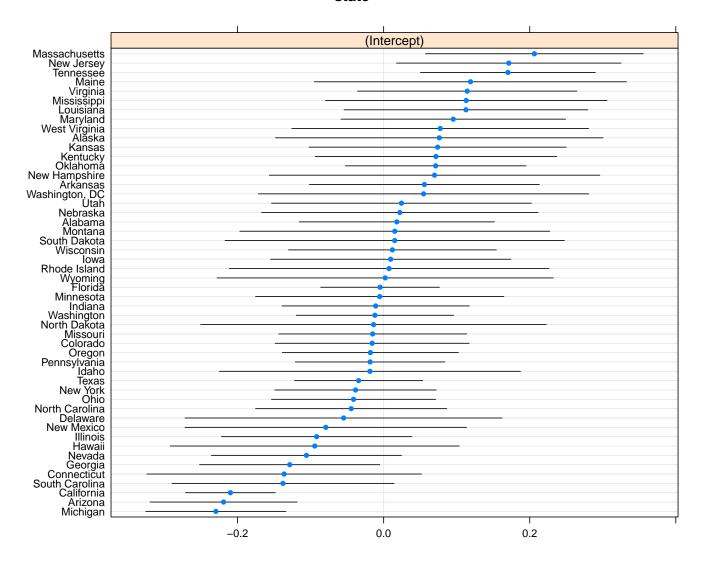
Random Effects

Table 4: Estimates of random effects

| | $	au^2$ | σ^2 |
|----------|---------|------------|
| Estimate | 0.0161 | 0.7772 |

The estimated across-state variance is $\hat{\tau^2} = 0.0161$, which also describes the variation attributed to the random intercept. The estimated within-state variance is $\hat{\sigma^2} = 0.7772$, which describes the unexplained variation. The estimated interclass correlation is $\frac{\hat{\tau^2}}{\hat{\tau^2} + \hat{\sigma^2}} \approx 0.02$. Therefore, we have little correlation within the same state.

state



From the random intercepts plot, we can see that states have different bases per milligram morphine prices. The prices ranges from $e^{-0.2297}=0.7948$ (Michigan) to $e^{0.2063}=1.2292$ (Massachusetts). These estimates are based on the baseline condition of all other predictors, which are purchasing in quarter 1, from an unknown source, with low dosage strength, and not purchased in bulk

Limitations

Our analysis and model have several limitations. Firstly, StreetRX provides only self-reported data, which is likely to be messy, biased, and lacking credibility. Although we borrow information across states via a hierarchical model, states with small sample sizes are still problematic. The within-state variance σ^2 is much larger than the across-state variance τ^2 , indicating that there is still much within-state variation left unexplained. This suggests that the per milligram price of morphine may depend on factors not on the state level. Having access to more predictors may help explain these variations and improve the model performance.

Another line

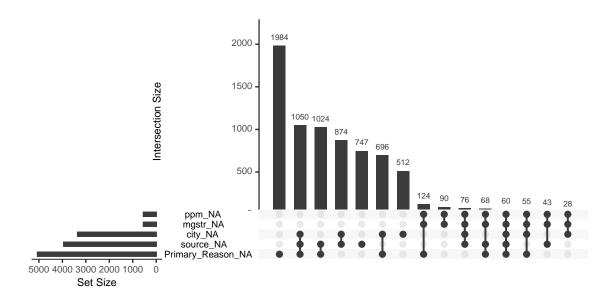
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Appendix

Additional tables and figures

Data Cleaning & EDA

Missing Values



Grouping Variable: city, state, and region

State

Date (price_date)

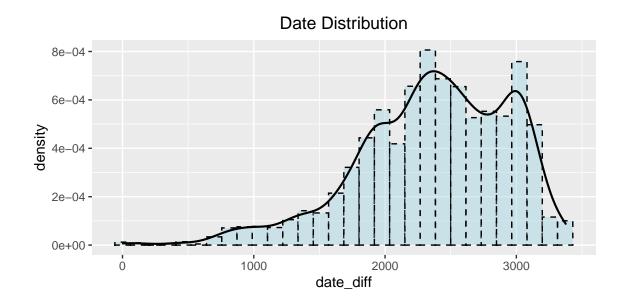
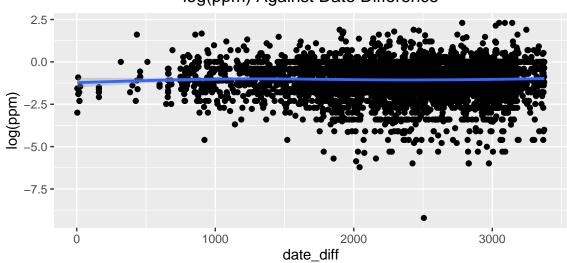


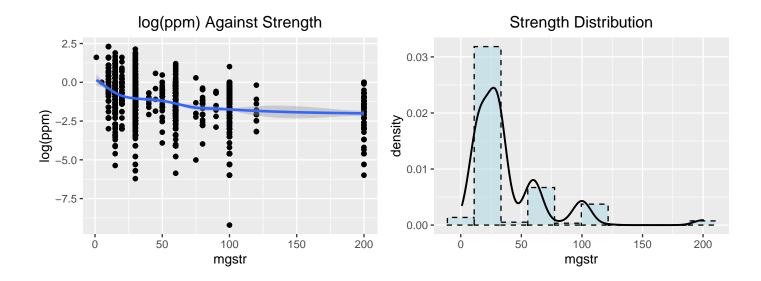
Table 5: Quantile of mgstr

| | mgstr |
|-----|-------|
| 25% | 15 |
| 50% | 30 |
| 75% | 60 |

log(ppm) Against Date Difference

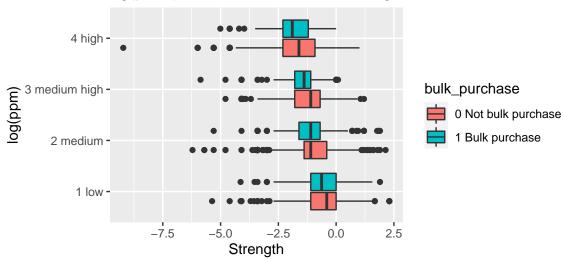


Dosage Strength & Primary Reason

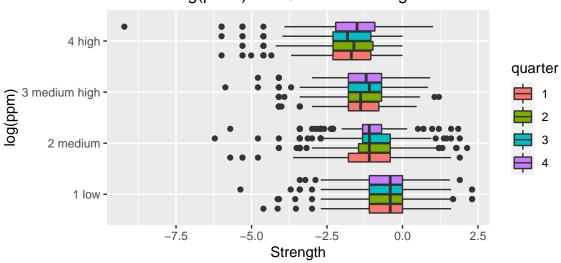


Interaction Plots

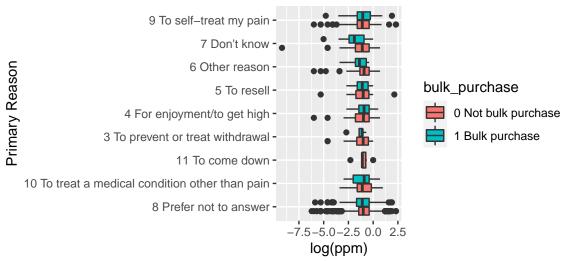
log(pmm) vs. Bulk Purchase x Strength



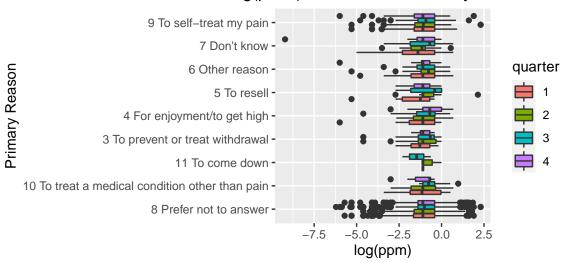
log(pmm) vs. Quarter x Strength



log(pmm) vs. Bulk Purchase x Primary Reason



log(pmm) vs. Quarter x Primary Reason



Model

Initial Model & Model Selection

Table 6: AIC and BIC for different grouping variables (full models)

| Grouping | AIC | BIC |
|----------|----------|----------|
| City | 14627.21 | 14931.96 |
| State | 14577.10 | 14881.85 |
| Region | 14610.16 | 14914.91 |

Interactions

Model Diagnostics

Diagnostic plots for model_g2 (drop one observation with the lowest residual in model_g)

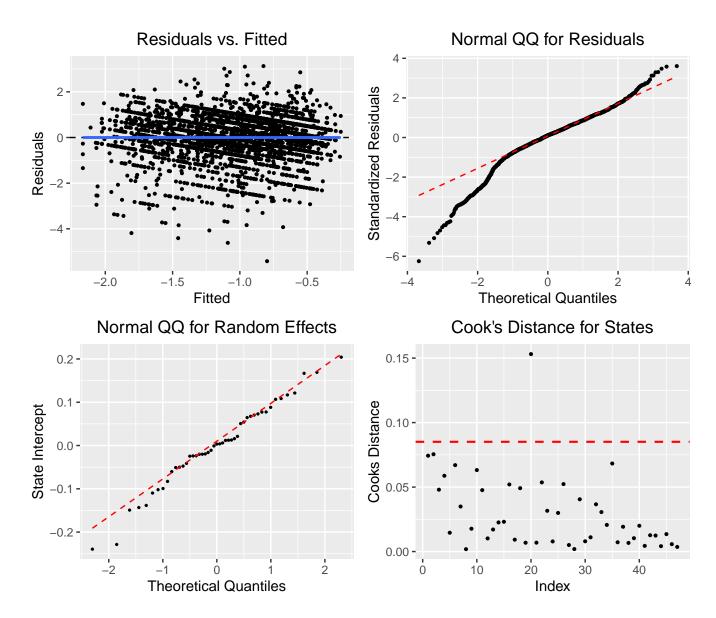
Diagnostic plots for model_g3 (drop influential states)

Table 7: Stepwise backward elimination results

| | Eliminated | Sum Sq | Mean Sq | NumDF | DenDF | F value | Pr(>F) |
|----------------|------------|----------|----------|-------|----------|----------|--------|
| date_diff | 1 | 0.0173 | 0.0173 | 1 | 5560.078 | 0.0221 | 0.8817 |
| year | 2 | 8.1386 | 0.9043 | 9 | 5549.587 | 1.1558 | 0.3191 |
| primary_reason | 3 | 11.3847 | 1.4231 | 8 | 5552.196 | 1.8156 | 0.0693 |
| quarter | 0 | 7.1468 | 2.3823 | 3 | 5554.311 | 3.0310 | 0.0282 |
| mgstr2 | 0 | 670.1758 | 223.3919 | 3 | 5554.045 | 284.2265 | 0.0000 |
| bulk_purchase | 0 | 12.1690 | 12.1690 | 1 | 5560.929 | 15.4829 | 0.0001 |
| source | 0 | 24.8908 | 1.3828 | 18 | 5550.635 | 1.7594 | 0.0243 |

Table 8: Interaction

| Model | LRT.p.value | BIC |
|---------------------------|-------------|----------|
| without interaction | | 14751.51 |
| + quarter x bulk_purchase | 0.1566 | 14772.17 |
| + quarter x mgstr2 | 0.4914 | 14820.71 |
| + bulk_purchase x mgstr2 | 0.1411 | 14771.93 |
| + quarter x source | 0.0022 | 14831.35 |
| + bulk_purchase x source | 0.5854 | 14783.18 |
| + source x mgstr2 | 0.9947 | 14948.55 |



Conclusion

Fixed Effects

Random Effects

Table 9: Estimates of fixed effects

| | Estimate | exp(Estimate) | Std. Error | df | t value | $\Pr(> t)$ |
|------------------------------|----------|---------------|------------|-----------|----------|-------------|
| (Intercept) | -0.6346 | 0.5301 | 0.0393 | 296.1819 | -16.1290 | 0.0000 |
| quarter2 | 0.0854 | 1.0891 | 0.0321 | 5550.5948 | 2.6578 | 0.0079 |
| quarter3 | 0.0841 | 1.0877 | 0.0332 | 5555.0726 | 2.5349 | 0.0113 |
| quarter4 | 0.0844 | 1.0881 | 0.0341 | 5551.1650 | 2.4759 | 0.0133 |
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| sourceInternet | -0.0041 | 0.9959 | 0.0625 | 5555.5822 | -0.0656 | 0.9477 |
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| mgstr24 high | -1.1197 | 0.3264 | 0.0420 | 5559.7107 | -26.6889 | 0.0000 |
| bulk_purchase1 Bulk purchase | -0.1141 | 0.8922 | 0.0296 | 5557.9880 | -3.8488 | 0.0001 |

Table 10: Estimated random intercepts

| grpvar term grp condval condsd exp(condval) state (Intercept) Massachusetts 0.2063 0.0761 1.2292 state (Intercept) New Jersey 0.1713 0.0784 1.1869 state (Intercept) Tennessee 0.1702 0.0611 1.1855 state (Intercept) Maine 0.1189 0.1091 1.1263 state (Intercept) Wriginia 0.1140 0.0766 1.1212 state (Intercept) Mississippi 0.1130 0.0984 1.1197 state (Intercept) Maryland 0.0953 0.0784 1.1000 state (Intercept) West Virginia 0.0774 0.1037 1.0805 state (Intercept) Maska 0.0762 0.1145 1.0792 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0738 | - | Ι, | | 1 1 | 1 1 | / 1 1 |
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| state (Intercept) Mississippi 0.1130 0.0984 1.1197 state (Intercept) Louisiana 0.1127 0.0851 1.1193 state (Intercept) Maryland 0.0953 0.0784 1.1000 state (Intercept) West Virginia 0.0774 0.1037 1.0805 state (Intercept) Alaska 0.0762 0.1145 1.0702 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Vashington, DC 0.0546 0.1154 1.0561 state (Intercept) Wabhington 0.0221 0.0966 1.0224 <td>state</td> <td>(Intercept)</td> <td></td> <td></td> <td></td> <td></td> | state | (Intercept) | | | | |
| state (Intercept) Louisiana 0.1127 0.0851 1.1193 state (Intercept) Maryland 0.0953 0.0784 1.1000 state (Intercept) West Virginia 0.0774 0.1037 1.0805 state (Intercept) Klaska 0.0762 0.1145 1.0792 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Webraska 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0181 0.0682 1.0182 | state | (Intercept) | Virginia | | 0.0766 | |
| state (Intercept) Maryland 0.0953 0.0784 1.1000 state (Intercept) West Virginia 0.0774 0.1037 1.0805 state (Intercept) Alaska 0.0762 0.1145 1.0792 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0152 0.1083 1.0153 <td>state</td> <td>(Intercept)</td> <td>Mississippi</td> <td>0.1130</td> <td>0.0984</td> <td>1.1197</td> | state | (Intercept) | Mississippi | 0.1130 | 0.0984 | 1.1197 |
| state (Intercept) West Virginia 0.0774 0.1037 1.0805 state (Intercept) Alaska 0.0762 0.1145 1.0792 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Webraska 0.0224 0.0908 1.0247 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 | state | (Intercept) | Louisiana | 0.1127 | 0.0851 | 1.1193 |
| state (Intercept) Alaska 0.0762 0.1145 1.0792 state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) Wisconsin 0.0152 0.1185 1.0153 <td>state</td> <td>(Intercept)</td> <td>Maryland</td> <td>0.0953</td> <td>0.0784</td> <td>1.1000</td> | state | (Intercept) | Maryland | 0.0953 | 0.0784 | 1.1000 |
| state (Intercept) Kansas 0.0739 0.0898 1.0767 state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Weahington, DC 0.0546 0.1154 1.0561 state (Intercept) Weahington 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0182 0.1083 1.0153 state (Intercept) Wisconsin 0.0152 0.1185 1.0121 <td>state</td> <td>(Intercept)</td> <td>West Virginia</td> <td>0.0774</td> <td>0.1037</td> <td>1.0805</td> | state | (Intercept) | West Virginia | 0.0774 | 0.1037 | 1.0805 |
| state (Intercept) Kentucky 0.0716 0.0843 1.0743 state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington 0.0224 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0181 0.0682 1.0182 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Washington 0.0096 0.0839 1.0097 </td <td>state</td> <td>(Intercept)</td> <td>Alaska</td> <td>0.0762</td> <td>0.1145</td> <td>1.0792</td> | state | (Intercept) | Alaska | 0.0762 | 0.1145 | 1.0792 |
| state (Intercept) Oklahoma 0.0712 0.0631 1.0738 state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Washington 0.0244 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Montana 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 <td>state</td> <td>(Intercept)</td> <td>Kansas</td> <td>0.0739</td> <td>0.0898</td> <td>1.0767</td> | state | (Intercept) | Kansas | 0.0739 | 0.0898 | 1.0767 |
| state (Intercept) New Hampshire 0.0697 0.1154 1.0721 state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Utah 0.0244 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Wyoming 0.0021 0.1177 1.0074 state (Intercept) Minnesota -0.0049 0.0415 0.9951 | state | (Intercept) | Kentucky | 0.0716 | 0.0843 | 1.0743 |
| state (Intercept) Arkansas 0.0558 0.0804 1.0573 state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Utah 0.0244 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Minnesota -0.0049 0.0415 0.9946 | state | (Intercept) | Oklahoma | 0.0712 | 0.0631 | 1.0738 |
| state (Intercept) Washington, DC 0.0546 0.1154 1.0561 state (Intercept) Utah 0.0244 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9891 | state | (Intercept) | New Hampshire | 0.0697 | 0.1154 | 1.0721 |
| state (Intercept) Utah 0.0244 0.0908 1.0247 state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 | state | (Intercept) | Arkansas | 0.0558 | 0.0804 | 1.0573 |
| state (Intercept) Nebraska 0.0221 0.0966 1.0224 state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0139 0.1207 0.9862 | state | (Intercept) | Washington, DC | 0.0546 | 0.1154 | 1.0561 |
| state (Intercept) Alabama 0.0181 0.0682 1.0182 state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9862 | state | (Intercept) | Utah | 0.0244 | 0.0908 | 1.0247 |
| state (Intercept) Montana 0.0152 0.1083 1.0153 state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9862 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Nebraska | 0.0221 | 0.0966 | 1.0224 |
| state (Intercept) South Dakota 0.0152 0.1185 1.0153 state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Alabama | 0.0181 | 0.0682 | 1.0182 |
| state (Intercept) Wisconsin 0.0120 0.0726 1.0121 state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Montana | 0.0152 | 0.1083 | 1.0153 |
| state (Intercept) Iowa 0.0096 0.0839 1.0097 state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | South Dakota | 0.0152 | 0.1185 | 1.0153 |
| state (Intercept) Rhode Island 0.0074 0.1117 1.0074 state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Wisconsin | 0.0120 | 0.0726 | 1.0121 |
| state (Intercept) Wyoming 0.0021 0.1175 1.0021 state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Iowa | 0.0096 | 0.0839 | 1.0097 |
| state (Intercept) Florida -0.0049 0.0415 0.9951 state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Rhode Island | 0.0074 | 0.1117 | 1.0074 |
| state (Intercept) Minnesota -0.0054 0.0867 0.9946 state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Wyoming | 0.0021 | 0.1175 | 1.0021 |
| state (Intercept) Indiana -0.0109 0.0655 0.9891 state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Florida | -0.0049 | 0.0415 | 0.9951 |
| state (Intercept) Washington -0.0119 0.0550 0.9881 state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Minnesota | -0.0054 | 0.0867 | 0.9946 |
| state (Intercept) North Dakota -0.0139 0.1207 0.9862 | state | (Intercept) | Indiana | -0.0109 | 0.0655 | 0.9891 |
| | state | (Intercept) | Washington | -0.0119 | 0.0550 | 0.9881 |
| state (Intercept) Missouri -0.0150 0.0657 0.9851 | state | (Intercept) | North Dakota | -0.0139 | 0.1207 | 0.9862 |
| | state | (Intercept) | Missouri | -0.0150 | 0.0657 | 0.9851 |

| state | (Intercept) | Colorado | -0.0157 | 0.0677 | 0.9844 |
|-------|-------------|----------------|---------|--------|--------|
| state | (Intercept) | Oregon | -0.0181 | 0.0615 | 0.9820 |
| state | (Intercept) | Pennsylvania | -0.0185 | 0.0523 | 0.9816 |
| state | (Intercept) | Idaho | -0.0188 | 0.1051 | 0.9814 |
| state | (Intercept) | Texas | -0.0342 | 0.0448 | 0.9663 |
| state | (Intercept) | New York | -0.0385 | 0.0564 | 0.9623 |
| state | (Intercept) | Ohio | -0.0412 | 0.0573 | 0.9596 |
| state | (Intercept) | North Carolina | -0.0444 | 0.0668 | 0.9565 |
| state | (Intercept) | Delaware | -0.0548 | 0.1108 | 0.9466 |
| state | (Intercept) | New Mexico | -0.0792 | 0.0984 | 0.9239 |
| state | (Intercept) | Illinois | -0.0917 | 0.0666 | 0.9124 |
| state | (Intercept) | Hawaii | -0.0944 | 0.1009 | 0.9100 |
| state | (Intercept) | Nevada | -0.1057 | 0.0664 | 0.8997 |
| state | (Intercept) | Georgia | -0.1287 | 0.0629 | 0.8793 |
| state | (Intercept) | Connecticut | -0.1363 | 0.0960 | 0.8726 |
| state | (Intercept) | South Carolina | -0.1379 | 0.0775 | 0.8712 |
| state | (Intercept) | California | -0.2098 | 0.0313 | 0.8107 |
| state | (Intercept) | Arizona | -0.2192 | 0.0514 | 0.8031 |
| state | (Intercept) | Michigan | -0.2297 | 0.0490 | 0.7948 |

Codes

library(tidyverse)
library(janitor)

morph_data <- streetrx %>%

```
library(gridExtra)
library(cowplot)
library(knitr)
require(magrittr)
require(dplyr)
library(kableExtra)
library(readr)
library(tidyr)
library(broom)
library(lme4)
library(glmmTMB)
library(sjPlot)
library(brms)
library(coda)
library(rstan)
library(tidybayes)
library(naniar)
library(olsrr)
library(lmerTest)
require(lattice)
# devtools::install_github("goodekat/redres")
#library(redres)
load('streetrx.RData')
na_check <- streetrx %>%
  filter(api_temp == 'morphine') %>%
  mutate_all( list( ~na_if(., '') ) ) %>%
  droplevels()
dim(na_check)
sum(is.na(na_check))
sum(is.na(na_check$Primary_Reason))
sum(is.na(na_check$source))
sum(is.na(na_check))
gg_miss_upset(na_check)
# subset for group drug
```

knitr::opts_chunk\$set(warning=FALSE, message = FALSE, cache = TRUE)

```
filter(api_temp == 'morphine')
morph_data$Primary_Reason <- droplevels(morph_data$Primary_Reason)</pre>
levels(morph_data$Primary_Reason)[1] <- "8 Prefer not to answer"</pre>
levels(morph_data$Primary_Reason)[2] <- "8 Prefer not to answer"</pre>
morph_data$source <- droplevels(morph_data$source)</pre>
levels(morph_data$source)[1] <- "Blank"</pre>
morph_data <- morph_data %>%
  filter(between(ppm, 0.000001, 10)) %>%
  mutate_all( list( ~na_if(., '') ) ) %>%
  drop_na() %>%
  clean_names() %>%
  mutate(
    quarter=substring(yq_pdate, 5, 5),
    year=substring(yq_pdate, 1, 4),
    state=recode_factor(droplevels(state), 'USA'='Unknown')
  )
nrow(morph_data)
sum(morph_data$ppm <=0)</pre>
```

```
# remove extreme outliers based on quantiles
# untransformed density
p1 <- morph_data %>%
  ggplot(aes(x=ppm)) +
    geom_histogram(
      aes(y=..density..),
      color='black',
      linetype='dashed',
      size=0.5,
      fill='lightblue',
      alpha=0.5,
      bins=20
    geom_density(size=0.75, bw=0.3) +
    ggtitle("Figure 1: Distribution of morphine ppm") +
    theme(plot.title = element_text(hjust = 0.5))
# log-transformed density
p2 <- morph_data %>%
  ggplot(aes(x=log(ppm))) +
    geom_histogram(
      aes(y=..density..),
      color='black',
      linetype='dashed',
```

```
size=0.5,
      fill='lightcoral',
      alpha=0.5,
      bins=20
    geom_density(size=0.75, bw=0.3) +
    xlim(-7, 3) +
    ggtitle("Figure 2: Distribution of morphine log(ppm)") +
    theme(plot.title = element_text(hjust = 0.5))
grid.arrange(p1, p2, ncol=2)
length(unique(morph_data$city))
length(unique(morph_data$state))
length(unique(morph_data$usa_region))
state_size <- morph_data %>%
  group_by(state) %>%
  summarise(n = n(), .groups = "drop") %>%
  arrange(n) %>%
  pivot_wider(
   names_from=state,
    values_from=n
  )
state_size %>%
  dplyr::select(1:5) %>%
  kable(
    caption = '5 States with Smallest Sample Size',
    align='c',
    booktabs=TRUE) %>%
  kable_styling(latex_options = c('hold_position'))
# remove low sample size states
morph_data <- morph_data %>%
  mutate(state=as.character(state)) %>%
  filter(!state %in% c(
    'Puerto Rico', 'Vermont'
  ))
morph_state <- morph_data %>%
  filter(state %in% state.name) %>%
  mutate(state_abv=state.abb[match(state,state.name)])
grand_mean <- mean(morph_state$ppm)</pre>
p3 <- morph_state %>%
  group_by(state_abv) %>%
  summarise(n = n(), mean = mean(ppm)) %>%
  ggplot(aes(x=n, y=mean)) +
```

```
geom_hline(
      aes(yintercept=grand_mean),
      linetype='dashed',
      color='red',
      size=0.75
    ) +
    geom_point() +
    labs(x='sample size', y='mean log(ppm)') +
    ggtitle("Figure 3: Group mean vs. sample size") +
    theme(plot.title = element_text(hjust = 0.5))
p4 <- morph_state %>%
  ggplot(aes(y=log(ppm), x=state_abv)) +
    geom_boxplot(
      fill=rainbow(49),
      alpha=0.5
    ) +
    scale_x_discrete(guide=guide_axis(angle = 90)) +
    ggtitle("Figure 4: Boxplot of log(pmm) across states") +
    theme(plot.title = element_text(hjust = 0.5)) +
    labs(x='state')
cowplot::plot_grid(p3, p4, rel_widths = c(1, 2))
t1 <- morph_state %>%
  group_by(usa_region) %>%
  summarise(n=n(), mean=round(mean(log(ppm)), 3)) %>%
  tableGrob()
p5 <- morph_state %>%
  ggplot(aes(y=log(ppm), x=usa_region)) +
    geom_boxplot() +
    stat_summary(
      fun.y=mean,
      geom='point',
      color='red',
      size=3
    ) +
    ggtitle("Figure 5: Boxplot of log(pmm) across regions") +
    theme(plot.title = element_text(hjust = 0.5))
grid.arrange(t1, p5, ncol=2, widths=c(2, 2))
min(as.Date(morph_data$price_date, "%m/%d/%y")) #2013-01-01
morph_data %>% group_by(year) %>% summarise(n = n())
# remove data prior to 2010
morph_data <- morph_data %>%
  mutate(Year=as.character(year)) %>%
  filter(!year %in% c(
```

```
1969, 2000, 2002, 2005
))
# date_diff
morph_data <- morph_data %>%
  mutate(date_diff = as.numeric()
    as.Date(morph_data$price_date, "%m/%d/%y") - as.Date("2010-01-01")
    )
  )
morph_data %>%
  ggplot(aes(x=date_diff)) +
    geom_histogram(
      aes(y=..density..),
      color='black',
      linetype='dashed',
      size=0.5,
      fill='lightblue',
      alpha=0.5,
      bins=30
    ) +
    geom_density(size=0.75, bw=100) +
  ggtitle("Date Distribution") +
  theme(plot.title = element_text(hjust = 0.5))
morph_data %>%
  ggplot(aes(x=date_diff, y=log(ppm))) +
    geom_point() +
    geom_smooth() +
    theme_bw()
yearplot <- morph_data %>%
  ggplot(aes(x = year, y = log(ppm))) +
  geom_boxplot() +
  labs(x='Year') +
  stat_summary(
    fun.y=mean,
    geom='point',
    color='red',
    size=3
  ) +
  ggtitle("Figure 6: log(pmm) vs. years") +
  theme(plot.title = element_text(hjust = 0.5))
quarterplot <- morph_data %>%
  ggplot(aes(x = quarter, y = log(ppm))) +
  geom_boxplot() +
  labs(
    x='Quarter',
```

```
y=' '
  ) +
  stat_summary(
    fun.y=mean,
    geom='point',
    color='red',
    size=3
  ) +
  ggtitle("Figure 7: log(pmm) vs. quarters") +
  theme(plot.title = element_text(hjust = 0.5))
grid.arrange(yearplot, quarterplot, ncol=2)
plot1 <- morph_data %>%
  ggplot(aes(x = bulk_purchase,y = log(ppm))) +
  geom_boxplot() +
  labs(x='Bulk Purchase') +
  stat_summary(
    fun.y=mean,
    geom='point',
    color='red',
    size=3
  ggtitle("Figure 8: log(pmm) vs. bulk purchase") +
  theme(plot.title = element_text(hjust = 0.5))
# unique(morph_data$source)
# combine internet levels into single level
morph_data <- morph_data %>%
  mutate(source=replace(
    source, !source %in% c(
      "Blank",
      'Personal',
      'Heard it',
      'Internet',
      'Internet Pharmacy',
      'Drug forum'
    ), 'Internet'
  )) %>%
  droplevels()
morph_data <- morph_data %>%
  mutate(source=as.character(source)) %>%
  filter(source != "Drug forum")
plot2 <- morph_data %>%
  ggplot(aes(x = source,y = log(ppm))) +
  geom_boxplot() +
```

```
stat_summary(
    fun.y=mean,
    geom='point',
    color='red',
    size=2
  ) +
  ggtitle("Figure 9: log(pmm) vs. source") +
  theme(plot.title = element_text(hjust = 0.5))
grid.arrange(plot1, plot2, ncol =2)
morph_data %>%
  ggplot(aes(x=mgstr, y=log(ppm))) +
    geom_point() +
    geom_smooth() +
    theme_bw()
# morph_data %>%
    ggplot(aes(x=log(mgstr), y=log(ppm))) +
#
      geom_point() +
#
      qeom\_smooth() +
#
      theme_bw()
morph_data %>%
  ggplot(aes(x=mgstr)) +
    geom_histogram(
      aes(y=..density..),
      color='black',
      linetype='dashed',
      size=0.5,
      fill='lightblue',
      alpha=0.5,
      bins=10
    ) +
    geom_density(size=0.75, bw=7.5) +
    labs(title='mgstr Distribution') +
  labs(title='log(pmm) vs. sources') +
    theme_bw()
# check for random slopes
morph_data %>% ggplot(aes(x = mgstr, y = log(ppm))) +
  geom_point() +
```

```
morph_data %>% ggplot(aes(x = mgstr, y = log(ppm))) +
  geom_point() +
  geom_smooth() +
  theme_bw() +
  facet_wrap('usa_region', scales = "fixed")
```

```
morph_data %>%
  group_by(mgstr) %>%
  summarize(n = n()) %>%
  pivot_wider(
```

```
names_from=mgstr,
  values_from=n
) %>%
kable(
  caption='Sample Size for mgstr Levels',
  align='c',
  booktabs=TRUE
) %>%
kable_styling(latex_options = c('hold_position'))

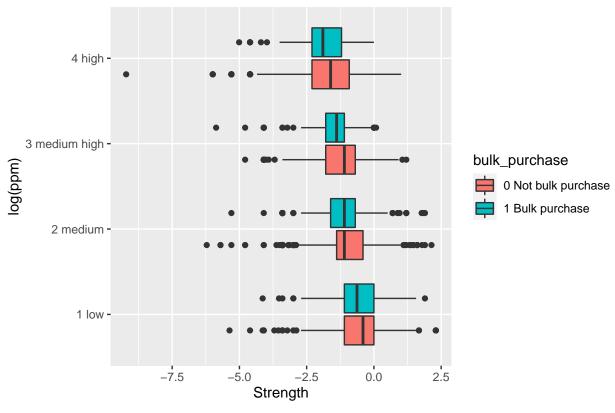
# inspect mgstr value quantiles
quantile(morph_data$mgstr, c(0.25, 0.5, 0.75)) %>%
  data.frame() %>%
  rename('mgstr'='.') %>%
  kable()
```

```
## here we decide to re-code mgstr by quantile
morph_data <- morph_data %>%
  mutate(mgstr2 = case_when(
    mgstr <= 15
                             ~ "1 low",
    mgstr >15 & mgstr <= 30 ~ "2 medium",
    mgstr >30 & mgstr <= 60 ~ "3 medium high",</pre>
                         ~ "4 high")
   mgstr > 60
  )
plot1 <- morph_data %>%
  ggplot(aes(x=mgstr2 ,y=log(ppm))) +
  geom_boxplot() +
  labs(y="log(ppm)", x="Strength") +
  stat_summary(
    fun.y=mean,
    geom='point',
    color='red',
    size=3
  ) +
  ggtitle("log(pmm) vs. strength") +
  theme(plot.title = element_text(hjust = 0.5))
plot2 <- morph_data %>%
  ggplot(aes(x = primary_reason,y =log(ppm))) +
  geom_boxplot() +
  coord_flip() +
  labs(x = "log(ppm)", y = "Reason") +
    stat_summary(
      fun.y=mean,
      geom='point',
      color='red',
      size=3
    ) +
  ggtitle("log(pmm) vs. reasons") +
```

Interaction Plot

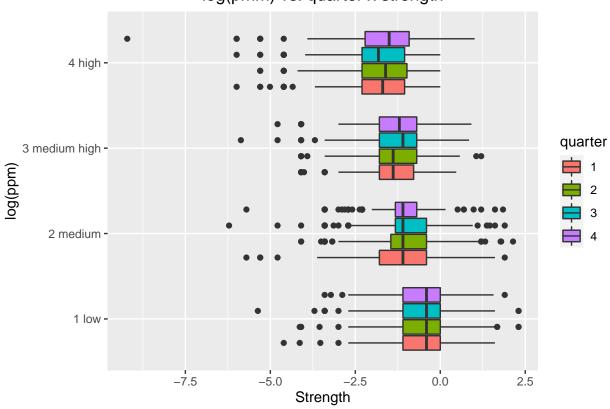
```
morph_data %>%
   ggplot(aes(x = mgstr2,y =log(ppm), fill = bulk_purchase)) +
   geom_boxplot() +
   coord_flip() +
   labs(x = "log(ppm)", y = "Strength") +
   ggtitle("log(pmm) vs. bulk purchase x strength") +
   theme(plot.title = element_text(hjust = 0.5))
```

log(pmm) vs. bulk purchase x strength



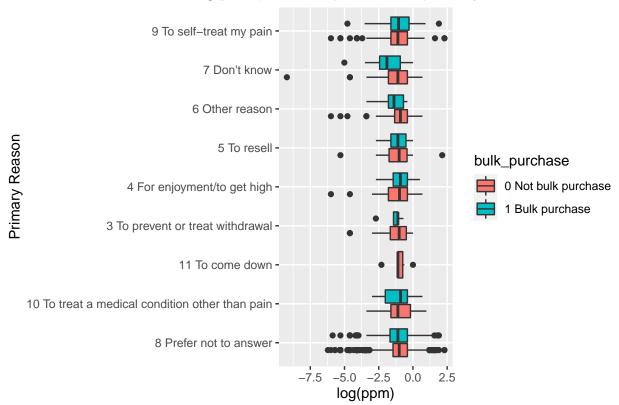
```
morph_data %>%
   ggplot(aes(x = mgstr2,y =log(ppm), fill = quarter)) +
   geom_boxplot() +
   coord_flip() +
   labs(x = "log(ppm)", y = "Strength") +
   ggtitle("log(pmm) vs. quarter x strength") +
   theme(plot.title = element_text(hjust = 0.5))
```

log(pmm) vs. quarter x strength



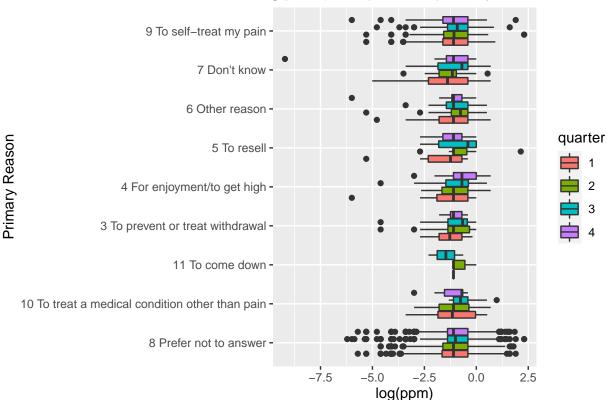
```
morph_data %>%
   ggplot(aes(x = primary_reason,y =log(ppm), fill = bulk_purchase)) +
   geom_boxplot() +
   coord_flip() +
   labs(x = "Primary Reason", y = "log(ppm)") +
   ggtitle("log(pmm) vs. bulk purchase x primary reason") +
   theme(plot.title = element_text(hjust = 0.5))
```

log(pmm) vs. bulk purchase x primary reason



```
morph_data %>%
   ggplot(aes(x = primary_reason,y =log(ppm), fill = quarter)) +
   geom_boxplot() +
   coord_flip() +
   labs(x = "Primary Reason", y = "log(ppm)") +
   ggtitle("log(pmm) vs. quarter x primary reason") +
   theme(plot.title = element_text(hjust = 0.5))
```

log(pmm) vs. quarter x primary reason



```
# group by region
mod_full_3 <- lmer(data=morph_data, log(ppm) ~ (1 | usa_region) + date_diff +
                      quarter + year + mgstr2 +
                bulk_purchase + primary_reason + source, REML=F)
aic_score <- sapply(c(mod full_1, mod full_2, mod_full_3), AIC)
bic_score <- sapply(c(mod_full_1, mod_full_2, mod_full_3), BIC)</pre>
data.frame('Grouping' = c('City', 'State', 'Region'), 'AIC' = aic_score,
           'BIC' = bic_score) %>%
  kable() %>%
    kable_styling(latex_options = c("hold_position", "striped"))
modelAll <- lmer(log(ppm) ~ quarter + primary_reason + mgstr2 + bulk_purchase</pre>
                 + year + date_diff + source + (1|state), data = morph_data,
                 REML=F)
step(modelAll)
model <- c("(1|state)",</pre>
           "(1|state) + mgstr2",
           "(1|state) + mgstr2 + bulk_purchase",
           "(1|state) + mgstr2 + bulk_purchase + year",
           "(1|state) + mgstr2 + bulk_purchase + quarter",
           "(1|state) + mgstr2 + bulk_purchase + date_diff",
           "(1|state) + mgstr2 + bulk_purchase + quarter + source",
           "(1|state) + mgstr2 + bulk purchase + quarter + source +
           primary_reason")
LRT <- c("",
         round(anova(modela,modelb)$`Pr(>Chisq)`[2],4),
         round(anova(modelb, modelc) $ Pr(>Chisq) [2],4),
         round(anova(modelc,modeld)$`Pr(>Chisq)`[2],4),
         round(anova(modelc, modele) $ Pr(>Chisq) [2],4),
         round(anova(modelc, modelf)$`Pr(>Chisq)`[2],4),
         round(anova(modele, modelg)$`Pr(>Chisq)`[2],4),
         round(anova(modelg,modelh)$`Pr(>Chisq)`[2],4))
BIC_score1 <- sapply(c(modela, modelb, modelc, modeld, modele, modelf, modelg,
                       modelh), BIC)
data.frame("Model" = model, 'LRT p-value' = LRT, 'BIC' = BIC_score1) %>%
  kable(caption = "Forward model selection") %>%
    kable_styling(latex_options = c("hold_position", "striped"))
modelg <- lmer(log(ppm) ~ quarter + source + mgstr2 + bulk_purchase +</pre>
                  (1|state), data = morph_data, REML=F)
plot_qq <- function(model) {</pre>
  df <- data.frame(</pre>
    res=residuals(model, scaled=TRUE)
  )
  p <- ggplot(df, aes(sample=res)) +</pre>
```

```
stat_qq(
      size=0.75
    stat_qq_line(
      linetype='dashed',
      color='red',
      size=0.5
    ) +
    labs(
      x='Theoretical Quantiles',
      y='Standardized Residuals'
    ggtitle("Normal QQ for Residuals") +
    theme(plot.title = element_text(hjust = 0.5))
  return(p)
}
plot_ranef_qq <- function(model) {</pre>
  df <- data.frame(</pre>
    res=ranef(model)[[1]][[1]]
  )
  p <- ggplot(df, aes(sample=res)) +</pre>
    stat_qq(
      size=0.5
    ) +
    stat_qq_line(
      linetype='dashed',
      color='red',
      size=0.5
    ) +
    labs(
      x='Theoretical Quantiles',
      y='State Intercept'
    ggtitle("Normal QQ for Random Effects") +
  theme(plot.title = element_text(hjust = 0.5))
  return(p)
}
plot_res_fit <- function(model) {</pre>
  df <- data.frame(</pre>
    res=residuals (model),
    fit=fitted(model)
  )
  p <- ggplot(df, aes(x=fit, y=res)) +</pre>
    geom_point(
```

```
size=0.75
    ) +
    geom_hline(
      yintercept=0,
      linetype="dashed"
    geom_smooth() +
    labs(
      x='Fitted',
      y='Residuals'
    ) +
    ggtitle("Residuals vs. Fitted") +
  theme(plot.title = element_text(hjust = 0.5))
  return(p)
}
plot_scale_loc <- function(model) {</pre>
  df <- data.frame(</pre>
    res=sqrt(residuals(model, scaled=TRUE)),
    fit=fitted(model)
  )
  p <- ggplot(df, aes(x=fit, y=res)) +</pre>
    geom_point(
      size=0.75
    ) +
    geom_smooth() +
    labs(
      x='Fitted',
      y=expression(sqrt('Standardized Residuals'))
    ggtitle("Scale-Location") +
  theme(plot.title = element_text(hjust = 0.5))
  return(p)
}
plot_res_dens <- function(model) {</pre>
  df <- data.frame(</pre>
    res=residuals(model)
  )
  p <- ggplot(df, aes(x=res)) +</pre>
    geom_density() +
    labs(
      x='Residuals',
      y='Density'
    ) +
    ggtitle("Residuals Density") +
  theme(plot.title = element_text(hjust = 0.5))
```

```
return(p)
}
plot_cooks_distance <- function(model1){</pre>
  model_inf<- influence(model1, group = "state")</pre>
  data <- model.frame(model1)</pre>
  cooks_distance <- cooks.distance(model_inf)</pre>
  cutline <- 4 / length(unique(data$state))</pre>
  infindiv <- cooks_distance > cutline
  p <- ggplot(data=NULL, aes(x=1:length(unique(data$state)), y=cooks_distance)) +</pre>
    geom_point(
      size=0.75
    ) +
    geom_hline(
      yintercept=cutline,
      linetype='dashed',
      color='red',
      size=0.75
    ) +
    labs(
      x='Index',
      y='Cooks Distance'
  ggtitle("Cook's Distance for States") +
  theme(plot.title = element_text(hjust = 0.5))
  return(p)
}
model_diag <- function(model) {</pre>
  p1 <- plot_res_fit(model)</pre>
  p2 <- plot_qq(model)
  p3 <- plot_ranef_qq(model)</pre>
  p4 <- plot_cooks_distance(model)</pre>
  cowplot::plot_grid(p1, p2, p3, p4, nrow=2)
}
model_diag(modelg)
```

```
model_g2_inf<- influence(model_g2, group = "state")</pre>
cooks_distance <- cooks.distance(model_g2_inf)</pre>
cutline <- 4 / length(unique(morph_data2$state))</pre>
infindiv <- cooks_distance > cutline
ggplot(data=NULL, aes(x=1:length(unique(morph_data2$state)), y=cooks_distance)) +
  geom_point() +
  geom_hline(
    yintercept=cutline,
    linetype='dashed',
    color='red',
    size=0.75
  ) +
  labs(
   x='Index',
    y='Cooks Distance'
  ) +
  theme_bw()
data.frame(
  rownames(model_g2_inf$`fixed.effects[-state]`),
  round(cooks_distance, 4),
  infindiv
) %>%
  filter(infindiv == TRUE) %>%
  dplyr::select(1:2) %>%
  rename(`State`=1, `Cook's Distance`=2) %>%
  kable() %>%
  kable_classic(full_width=FALSE)
# remove three most influential states
morph_data3 <- morph_data2 %>%
  filter(!state %in% c('Florida', 'California', 'Pennsylvania'))
model_g3 <- lmer(log(ppm) ~ quarter + source + mgstr2 + bulk_purchase +</pre>
                    (1|state), data = morph_data3, REML=F)
model_diag(model_g3)
# view coefficient estimates
view_coef <- function(model) {</pre>
  summary(model)$coefficients %>%
    as.data.frame() %>%
    mutate(`exp(Estimate)`=exp(Estimate)) %>%
    relocate(`exp(Estimate)`, .after=Estimate) %>%
    kable(caption = "Estimates of fixed effects",
      digits = 4) %>%
   kable_classic(full_width=FALSE)
}
```

```
# view parameter estimates
view_params <- function(model) {</pre>
  params <- summary(model)$varcor %>%
    as.data.frame() %>%
    dplyr::select(vcov)
  params <- t(params)</pre>
  rownames(params) <- c('Estimate')</pre>
  kable(params,
        caption = "Estimates of random effects",
        col.names = c('$\\tau^2$', '$\\sigma^2$'),
        digits = 4,
        format = 'latex',
        escape = FALSE) %>%
  kable_classic(full_width=FALSE)
}
view_coef(model_g2) %>%
  kable_styling(latex_options = c("hold_position","striped"))
view_params(model_g2) %>%
  kable_styling(latex_options = c("hold_position","striped"))
# view intercept estimates and intervals
dotplot(ranef(model_g2, condVar = TRUE))$state
```