## The Plasma Blackout Problem Equation Cheat Sheet Jack Nelson

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Intro to the Blackout Problem

## Plasma Electron Frequency

$$\omega_e = \sqrt{\frac{n_e e^2}{\epsilon_0 m_e}} \ rad/sec \tag{1}$$

This can be approximated as

$$f_e \approx 9\sqrt{n_e} \; Hz$$
 (2)

## Lorentz Windows

These are the equations used by Kim et. al. in the computer modeling of a plasma sheath in the vicinity of an  $\mathbf{E} \times \mathbf{B}$  field <sup>1</sup>.

## **Ion Transport Equations**

$$\nabla \cdot (\mathbf{V_i} n) = 0 \tag{3}$$

$$m_i n(\mathbf{V_i} \cdot \nabla \mathbf{V_i}) = en(\mathbf{E} + \mathbf{V_i} \times \mathbf{B}) - m_i n \nu_c \mathbf{V_i}$$
(4)

**Current Density of Plasma Sheath** The current density of the plasma is derived from the generalized Ohm's Law, and includes the Hall effect:

$$\mathbf{j} = \sigma \left( \mathbf{E} + \frac{kT_e}{e} \nabla \ln n - \frac{\mathbf{j} \times \mathbf{B}}{en} + (\mathbf{V_i} \times \mathbf{B}) \right)$$
 (5)

The x and z components of the current density used in the 2D simulations simplify to:

$$j_x = \sigma \left( E_x + \frac{kT_e}{e} \frac{\partial \ln n}{\partial x} - V_y B_z \right) \tag{6}$$

$$j_z = \sigma \left( E_z + \frac{kT_e}{e} \frac{\partial \ln n}{\partial z} \right) \tag{7}$$

**Current Density Conservation** 

$$\nabla \cdot \mathbf{j} = 0 \tag{8}$$

References

[1] M. Kim, M. Keidar, and I. D. Boyd, "Analysis of an Electromagnetic Mitigation Scheme for Reentry Telemetry Through Plasma," 2008.

<sup>1</sup> M. Kim, M. Keidar, and I. D. Boyd, "Analysis of an Electromagnetic Mitigation Scheme for Reentry Telemetry Through Plasma," 2008