IM2 Book 1 Selected Answers

IM2 Dream Team

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1.
$$x = -3$$

3. (a)
$$x(x+4)$$

(b)
$$3x(x-5)$$

(c)
$$-x(2x+7)$$

4. (a)
$$x = 0, 4$$

(b)
$$x = 0, 5$$

(c)
$$x = 0, -\frac{7}{2}$$

	$2 \le x$	_	all values that are at least 2	_
5.	-4 < x < 0	_	_	(-4,0)
	x < 1	_	all values that are less than 1	$(-\infty,1)$

- 6. Answers may vary. Soln: (0,5). Non-soln: (0,0).
- 7. $4a^2, 2a^2$
- 8. (a) -
 - (b) $24 \le x$
- 9. (x+4)(x+1). 4 and 1 add to 5 and multiply to 4.

10.
$$x^2 + (q+p)x + pq$$
. $\nabla = (q+p)$. $\Delta = pq$.

- 11. (a) -
 - (b) $37 \le 37$
 - (c) -
 - (d) $x \ge 18$
- 12. $x = 1, -4, \frac{3}{2}$
- 13. (a) Answers may vary.

System soln: (2,4)

Soln to one eqn but not the other: (0,0)

Not a system soln: (0,0)

- (b) -
- (c) One solution.
- 14. Answers may vary.

$$\begin{cases} y = x \\ y = x + 1 \end{cases}$$

15. Answers may vary.

$$\begin{cases} y = x \\ 2y = 2x \end{cases}$$

- 16. $(3x)^2$
- 17. x > -5
- 18. (a) $x \le -10$
 - (b) $x \le -10$
- 19. (a) x = -4
 - (b) x = 3, 5
 - (c) x = -1, 7
- 20. (a) $(\frac{1}{2}, \frac{1}{3})$
 - (b) (1,-2)
- 21. (a)
 - (b) $y = x^2$
- 22. (a) f(2) = 5f(-4) = -1
 - (b) x = -1
- 23. (a) 2x + y = 3
 - (b) No solutions

	Words	Function Formula
24		f(x) = 2x
24.		f(x) = 5x - 1
	divide the input by 2 and add 5	

25. (a) f(-3) = 3 f(0) = 0f(2) = 2

(b)
$$x = \pm 4$$

- 26. (a) -
 - (b) 6
 - (c) $x = \pm 10$
- 27. (3x+4)(x-3)
- 28. (a) $-7 \le x$
 - (b) x < 4
- 29. (a) 5
 - (b) 12
 - (c) |x y|
- 30. No
- 31. $x \ge 0$
- 32. |a-b| = |b-a|
- 33. (4x+1)(x+5)
- 34. (a) 9 and 4
 - (b) 9 and -4
 - (c) x and 7
 - (d) x and 0
- 35. (a) -
 - (b) |x| > 6
 - (c) -

	_	all values that are 2 units away from -5	_	x = -3, -7
36.	x = 5	_	_	x = -5, 5
	x+1 = 2	all values that are 2 units away from -1	_	x = -3, 1

- 37. (a) All values that are 5 units away from 2.
 - (b) All values that are 10 units away from -4.
- 38. A = (2a+b)(a+3b)
- 39. (a) (x-2)(x-6)
 - (b) (3x-2)(2x+3)
 - (c) 2x(3x-1)
- 40. BC = 8, AC = 15, and AB = 17
- 41. (a) $x^2 16$
 - (b) $x^2 49$

(c)
$$9x^2 - 4$$

(d)
$$x^2 - a^2$$

42. (a)
$$(x-8)(x+8)$$

(b)
$$(x-c)(x+c)$$

(c)
$$(2x-5)(2x+5)$$

(d)
$$(ax-c)(ax+c)$$

	_	all values that are at most 2 units away from -5	-	$-7 \le x \le -3$
43.	$ x \ge 6$	-	_	x < -6 or x > 6
	$ x-1 \le 4$	all values that are at most 4 units away from 1	_	_

- 44. (a) -
 - (b) (0,0)
 - (c) $(-\infty, \infty)$
 - (d) y = 0
 - (e) $[0,\infty)$

45.
$$y = -x$$
, $y = x$

$$|x| = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$$

- 46. x = 12
- 47. (a) All values at most 2 units away from 7.

(b)
$$x > -2 \text{ or } x < -8$$

48.
$$(-2,2)$$
 $(3,7)$

(b)
$$|x - 52| \le 3$$

50. |x - y| = 12. Infinite.

51. (a)
$$3x(x+4)$$

(b)
$$(x+5)(x+3)$$

(c)
$$2(x+1)(x-3)$$

(d)
$$9(x-2)(x+2)$$

52. 120

53.

$$|x+2| = \begin{cases} -x+2 & \text{if } x < -2\\ x+2 & \text{if } x \ge -2 \end{cases}$$

- 54. (a) x = -5, 5
 - (b) blob = -5, 5
- 55. Yes
- 56. f(x) = |x|
- 57. (a) 77 blocks
 - (b) 19 blocks
 - (c) -
 - (d) y = |x 91|
- 58. -
- $59. |l 12| \le 0.01$
- 60. (a) (-28, 12)
 - (b) $(-\infty,0] \cup [8,\infty)$
- 61. (a) a = -1, -6
 - (b) $x = \frac{-19}{2}, \frac{9}{2}$
- 62. $-1 \le a \le 6$
- 63. |x| = 3x = -3 or x = 3
- 64. No
- 65. (a) -
 - (b) y = |x 34|
 - (c) x = 18,50
- 66. x = -4, 4
- 67. (a) -
 - (b) vertex: (4,0)domain: $(-\infty,\infty)$ range: $[0,\infty)$ minimum value: y=0
 - (c) x = 4
- 68. (a) Shift f(x) left by 5
 - (b) (-5,0). Shift it left by 5.
- 69. x = 6, 1

$$|x-7| = \begin{cases} x-7 & \text{if } x \ge 7\\ -x+7 & \text{if } x < 7 \end{cases}$$

71.
$$(10,3)$$

72.
$$x = 4, -6$$

73.
$$x = -1, -4$$

74. Shift it right by 3

75.
$$g(x) = |x - h|$$

	x	x	x -2
	-3	3	1
	-2	2	0
76.	-1	1	-1
70.	0	0	-2
	1	1	-1
	2	2	0
	3	3	1

Translate f(x) down by 2.

77. (a)
$$\left(-\frac{4}{3}, \frac{4}{3}\right)$$

(b)
$$(-\infty, -\frac{84}{5}] \cup [\frac{56}{5}, \infty)$$

(c)
$$\left[-\frac{1}{2}, \frac{13}{2}\right]$$

78. (a)
$$x = -5, -4$$

(b)
$$x = -\frac{7}{2}, 3$$

(c)
$$x = -9, 9$$

(d)
$$x = -\frac{1}{4}, 4$$

79. Left graph:
$$y = |x|$$

Right graph: y = |x - 3|

80. Shift/translate the graph up by 3 Shift/translate the graph down by 5.

81.
$$f(x) = |x - 3|$$

82.
$$n^2$$

83.
$$x = -2, 4$$

 $x \in [-2, 4]$

84. (a) Shift/translate the graph up by k

(b) (0, k)Shift/translate (0, 0) up by k

	x	x	- x
	-3	3	-3
	-2	2	-2
85.	-1	1	-1
00.	0	0	0
	1	1	-1
	2	2	-2
	3	3	-3

You can reflect y = |x| over the x-axis.

86.
$$(2,0)$$
; $(-2,0)$, $(2,0)$

87.

$$g(x) = \begin{cases} -x - 2 \text{ if } x \le 0\\ x - 2 \text{ if } x > 0 \end{cases}$$

88. Shift f(x) to the right h and up k. Vertex: (h, k).

	x	x	2 x	0.5 x
	-3	3	6	1.5
	-2	2	4	1
89.	-1	1	2	0.5
09.	0	0	0	0
	1	1	2	0.5
	2	2	4	1
	3	3	6	1.5

You can vertically stretch |x| by a factor of 2 to get 2|x|. You can vertically compress |x| by a factor of 2 to get 0.5|x|.

- 90. (a) Vertically stretch |x| by a factor of a.
 - (b) Vertically stretch |x| by a factor of a and then reflect it over the x-axis.
- 91. 320, 210

92.
$$\begin{bmatrix} 320 & 98 & 135 \\ 405 & 110 & 120 \end{bmatrix}$$

- 93. (0, |h| + k)
- 94. Vertex: (0,0)

Vertex: (0,6). *x*-intercepts: (-2,0),(2,0)

95. (a) Shift |x| right by 1. Vertically stretch it by a factor of 2. Shift it down by 6.

- (b) -
- (c) Vertex: (1, -6)Domain: $(-\infty, \infty)$

Range: $[-6, \infty)$

Minimum-value: y = -6

- (d) (-2,0),(4,0)
- 96. (a) Shift f(x) right by 3. Reflect it over the x-axis. Shift it up by 5.
 - (b) -
 - (c) Vertex: (3, 5)

Domain: $(-\infty, \infty)$

Range: $(-\infty, 5]$ Maximum value: 5

- (d) (-2,0),(8,0)
- 97. a = -3

$$\begin{array}{c|ccccc}
 & x & |x| & x^2 \\
\hline
 & -2 & 2 & 4 \\
 & -1 & 1 & 1 \\
 & -\frac{1}{2} & \frac{1}{2} & \frac{1}{4} \\
 & 1 & 1 & 1 \\
 & 2 & 2 & 4 \\
\end{array}$$

Vertex: (0,0)

Domain: $(-\infty, \infty)$

Range: $[0, \infty)$

Minimum value: 0

Axis of symmetry: x = 0

- 99. (a) y = |x 1| + 2
 - (b) y = -|x| + 1
 - (c) y = 2|x+3|-1

100.
$$A + B = \begin{bmatrix} -1 & 3 \\ 6 & -2 \end{bmatrix} + \begin{bmatrix} 7 & 0 \\ 2 & -4 \end{bmatrix} = \begin{bmatrix} 6 & 3 \\ 8 & -6 \end{bmatrix}$$

$$A-B = \begin{bmatrix} -1 & 3 \\ 6 & -2 \end{bmatrix} - \begin{bmatrix} 7 & 0 \\ 2 & -4 \end{bmatrix} = \begin{bmatrix} -8 & 3 \\ 4 & 2 \end{bmatrix}$$

101. Vertex: (5, -3)

Domain: $(-\infty, \infty)$

Range: $[-3, \infty)$

Minimum: -3

x-intercepts: $(\frac{1}{2}, 0), (\frac{19}{2}, 0)$

$$y = \begin{cases} \frac{2}{3}(x-5) - 3, & x \ge 5\\ -\frac{2}{3}(x-5) - 3, & x < 5 \end{cases}$$

102. Two: (0, h - k), (0, h + k)

	\boldsymbol{x}	x^2	$x^2 + 1$	$x^2 - 5$
	-2	4	5	-1
102	-1	1	2	-4
103.	0	0	1	-5
	1	1	2	-4
	2	4	5	-1

g(x): shift f(x) up by 1 f(x): shift f(x) down by 5

- 104. (a) 3 (b) -9
- 105. Intersections: (1, 2), (5, 2)Area = 8

106. (a)
$$x = -1, 5$$

(b) $(-\infty, -1] \cup [5, \infty)$

- 107. (a) [0, 100]
 - (b) The midpoint of the road between Salina and Green River

(c)
$$y = -|x - 50| + 50$$

(d)
$$d = -\frac{5}{6}|t - 60| + 50$$

$$\begin{array}{c|ccccc}
 & x & x^2 & -x^2 \\
\hline
 & -3 & 9 & -9 \\
 & -2 & 4 & -4 \\
\hline
 & 108. & -1 & 1 & -1 \\
 & 0 & 0 & 0 \\
 & 1 & 1 & -1 \\
 & 2 & 4 & -4 \\
\end{array}$$

Reflect f(x) over the x-axis.

	x	x^2	$2x^2$	$0.5x^{2}$
	-3	9	18	4.5
	-2	4	8	2
109.	-1	1	2	0.5
	0	0	0	0
	1	1	2	0.5
	2	4	8	2

g(x): Vertically stretch f(x) by a factor of 2.

h(x): Vertically compress f(x) by a factor of 2.

- 110. (a) Friday: \$2,250 Saturday: \$7,100
 - Saturday: \$7,10 Sunday: \$5,650
 - (b) $[120, 210] \cdot [10, 5] = 120(10) + 210(5) = $2,250$
- 111. Shift f(x) up by c.
 - Vertex: (0, c)Range: $[c, \infty)$
 - Minimum: c
- 112. (a) -
 - (b) (32,55)
 - (c) (21, 55]
 - (d) [45, 65]
- 113. Vertically stretch the graph by a factor of 3. Shift it up by 6.
 - $\begin{array}{c|c}
 x & x \\
 -3 & 9 \\
 -2 & 4
 \end{array}$
- 114. (a) $\begin{bmatrix} -1 & 1 \\ 0 & 0 \end{bmatrix}$
 - 1 1
 - $\begin{bmatrix} 2 \\ 3 \end{bmatrix} \begin{bmatrix} 4 \\ 9 \end{bmatrix}$
 - $\begin{array}{c|c}
 x & \sqrt{x} \\
 \hline
 0 & 0 \\
 1 & 1
 \end{array}$
 - $\begin{array}{c|cccc}
 4 & 2 \\
 9 & 3 \\
 16 & 4
 \end{array}$
 - The values of x^2 are useful as inputs for the $g(x) = \sqrt{x}$ table.
 - (b) Vertex: None
 - Domain: $[0, \infty)$
 - Range: $[0, \infty)$
 - Min: 0
 - It does not have an axis of symmetry.
- 115. $a = \frac{3}{2}$
- 116. It's the total revenue that the zoo made on Sunday.
- 117.

$$\begin{bmatrix} 120(10) + 210(5) \\ 400(10) + 620(5) \\ 320(10) + 490(5) \end{bmatrix} = \begin{bmatrix} 2, 250 \\ 7, 100 \\ 5, 650 \end{bmatrix}$$

118. Vertex: (0,0)

Max: 64

Axis of symmetry: x = 0*x*-intercepts: (-4,0), (0,4)

119. Skip

120. Highest: $y = x^2 + 1$ Middle: $y = \frac{1}{2}x^2$ Lowest: $y = -x^2 - 2$

121. Shift the graph right by h