# IM2 Book 1 Selected Answers

## IM2 Dream Team

## October 25, 2025

1. 
$$x = -3$$

3. (a) 
$$x(x+4)$$

(b) 
$$3x(x-5)$$

(c) 
$$-x(2x+7)$$

4. (a) 
$$x = 0, 4$$

(b) 
$$x = 0, 5$$

(c) 
$$x = 0, -\frac{7}{2}$$

	$2 \le x$	_	all values that are at least 2	_
5.	-4 < x < 0	_	_	(-4,0)
	x < 1	_	all values that are less than 1	$(-\infty,1)$

6. Answers may vary. Soln: (0,5). Non-soln: (0,0).

7. 
$$4a^2, 2a^2$$

(b) 
$$24 \le x$$

9. (x+4)(x+1). 4 and 1 add to 5 and multiply to 4.

10. 
$$x^2 + (q+p)x + pq$$
.  $\nabla = (q+p)$ .  $\Delta = pq$ .

(b) 
$$37 \le 37$$

(d) 
$$x \ge 18$$

12. 
$$x = 1, -4, \frac{3}{2}$$

13. (a) Answers may vary.

System soln: (2,4)

Soln to one eqn but not the other: (0,0)

Not a system soln: (0,0)

- (b) -
- (c) One solution.
- 14. Answers may vary.

$$\begin{cases} y = x \\ y = x + 1 \end{cases}$$

15. Answers may vary.

$$\begin{cases} y = x \\ 2y = 2x \end{cases}$$

- 16.  $(3x)^2$
- 17. x > -5
- 18. (a)  $x \le -10$ 
  - (b)  $x \le -10$
- 19. (a) x = -4
  - (b) x = 3, 5
  - (c) x = -1, 7
- 20. (a)  $(\frac{1}{2}, \frac{1}{3})$ 
  - (b) (1,-2)
- 21. (a)
  - (b)  $y = x^2$
- 22. (a) f(2) = 5f(-4) = -1
  - (b) x = -1
- 23. (a) 2x + y = 3
  - (b) No solutions

	Words	Function Formula
24		f(x) = 2x
24.		f(x) = 5x - 1
	divide the input by 2 and add 5	

25. (a) 
$$f(-3) = 3$$
  
 $f(0) = 0$   
 $f(2) = 2$   
(b)  $x = \pm 4$ 

- 26. (a) -
  - (b) 6
  - (c)  $x = \pm 10$
- 27. (3x+4)(x-3)
- 28. (a)  $-7 \le x$ 
  - (b) x < 4
- 29. (a) 5
  - (b) 12
  - (c) |x y|
- 30. No
- 31.  $x \ge 0$
- 32. |a-b| = |b-a|
- 33. (4x+1)(x+5)
- 34. (a) 9 and 4
  - (b) 9 and -4
  - (c) x and 7
  - (d) x and 0
- 35. (a) -
  - (b) |x| > 6
  - (c) -

	_	all values that are 2 units away from -5	_	x = -3, -7
36.	x  = 5	_	_	x = -5, 5
	x+1  = 2	all values that are 2 units away from -1	_	x = -3, 1

- 37. (a) All values that are 5 units away from 2.
  - (b) All values that are 10 units away from -4.
- 38. A = (2a+b)(a+3b)
- 39. (a) (x-2)(x-6)
  - (b) (3x-2)(2x+3)
  - (c) 2x(3x-1)
- 40. BC = 8, AC = 15, and AB = 17
- 41. (a)  $x^2 16$ 
  - (b)  $x^2 49$

(c) 
$$9x^2 - 4$$

(d) 
$$x^2 - a^2$$

42. (a) 
$$(x-8)(x+8)$$

(b) 
$$(x-c)(x+c)$$

(c) 
$$(2x-5)(2x+5)$$

(d) 
$$(ax-c)(ax+c)$$

	_	all values that are at most 2 units away from -5	-	$-7 \le x \le -3$
43.	$ x  \ge 6$	-	_	x < -6  or  x > 6
	$ x-1  \le 4$	all values that are at most 4 units away from 1	_	_

- 44. (a) -
  - (b) (0,0)
  - (c)  $(-\infty, \infty)$
  - (d) y = 0
  - (e)  $[0,\infty)$

45. 
$$y = -x, y = x$$

$$|x| = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$$

- 46. x = 12
- 47. (a) All values at most 2 units away from 7.

(b) 
$$x > -2 \text{ or } x < -8$$

48. 
$$(-2,2)$$
  $(3,7)$ 

(b) 
$$|x - 52| \le 3$$

50. |x - y| = 12. Infinite.

51. (a) 
$$3x(x+4)$$

(b) 
$$(x+5)(x+3)$$

(c) 
$$2(x+1)(x-3)$$

(d) 
$$9(x-2)(x+2)$$

52. 120

53.

$$|x+2| = \begin{cases} -x+2 & \text{if } x < -2\\ x+2 & \text{if } x \ge -2 \end{cases}$$

- 54. (a) x = -5, 5
  - (b) blob = -5, 5
- 55. Yes
- 56. f(x) = |x|
- 57. (a) 77 blocks
  - (b) 19 blocks
  - (c) -
  - (d) y = |x 91|
- 58. -
- 59.  $|l 12| \le 0.01$
- 60. (a) (-28, 12)
  - (b)  $(-\infty,0] \cup [8,\infty)$
- 61. (a) a = -1, -6
  - (b)  $x = \frac{-19}{2}, \frac{9}{2}$
- 62.  $-1 \le a \le 6$
- 63. |x| = 3x = -3 or x = 3
- 64. No
- 65. (a) -
  - (b) y = |x 34|
  - (c) x = 18,50
- 66. x = -4, 4
- 67. (a) -
  - (b) vertex: (4,0)domain:  $(-\infty, \infty)$ range:  $[0, \infty)$ minimum value: y = 0
  - (c) x = 4
- 68. (a) Shift f(x) left by 5
  - (b) (-5,0). Shift it left by 5.
- 69. x = 6, 1

$$|x-7| = \begin{cases} x-7 & \text{if } x \ge 7\\ -x+7 & \text{if } x < 7 \end{cases}$$

72. 
$$x = 4, -6$$

73. 
$$x = -1, -4$$

74. Shift it right by 3

75. 
$$g(x) = |x - h|$$

	x	x	x -2
	-3	3	1
	-2	2	0
76.	-1	1	-1
70.	0	0	-2
	1	1	-1
	2	2	0
	3	3	1

Translate f(x) down by 2.

77. (a) 
$$\left(-\frac{4}{3}, \frac{4}{3}\right)$$

(b) 
$$(-\infty, -\frac{84}{5}] \cup [\frac{56}{5}, \infty)$$

(c) 
$$\left[-\frac{1}{2}, \frac{13}{2}\right]$$

78. (a) 
$$x = -5, -4$$

(b) 
$$x = -\frac{7}{2}, 3$$

(c) 
$$x = -9, 9$$

(d) 
$$x = -\frac{1}{4}, 4$$

79. Left graph: 
$$y = |x|$$

Right graph: y = |x - 3|

80. Shift/translate the graph up by 3 Shift/translate the graph down by 5.

81. 
$$f(x) = |x - 3|$$

82. 
$$n^2$$

83. 
$$x = -2, 4$$
  
 $x \in [-2, 4]$ 

84. (a) Shift/translate the graph up by k

(b) (0, k)Shift/translate (0, 0) up by k

	$\boldsymbol{x}$	x	- x
	-3	3	-3
	-2	2	-2
85.	-1	1	-1
00.	0	0	0
	1	1	-1
	2	2	-2
	3	3	-3

You can reflect y = |x| over the x-axis.

86. 
$$(2,0)$$
;  $(-2,0)$ ,  $(2,0)$ 

87.

$$g(x) = \begin{cases} -x - 2 \text{ if } x \le 0\\ x - 2 \text{ if } x > 0 \end{cases}$$

88. Shift f(x) to the right h and up k. Vertex: (h, k).

	x	x	2 x	0.5 x
	-3	3	6	1.5
	-2	2	4	1
89.	-1	1	2	0.5
09.	0	0	0	0
	1	1	2	0.5
	2	2	4	1
	3	3	6	1.5

You can vertically stretch |x| by a factor of 2 to get 2|x|. You can vertically compress |x| by a factor of 2 to get 0.5|x|.

- 90. (a) Vertically stretch |x| by a factor of a.
  - (b) Vertically stretch |x| by a factor of a and then reflect it over the x-axis.
- $91.\ 320,\ 210$

92. 
$$\begin{bmatrix} 320 & 98 & 135 \\ 405 & 110 & 120 \end{bmatrix}$$

- 93. (0, |h| + k)
- 94. Vertex: (0,0)

Vertex: (0,6). *x*-intercepts: (-2,0),(2,0)

95. (a) Shift |x| right by 1. Vertically stretch it by a factor of 2. Shift it down by 6.

- (b) -
- (c) Vertex: (1, -6)Domain:  $(-\infty, \infty)$ Range:  $[-6, \infty)$

Minimum-value: y = -6

- (d) (-2,0),(4,0)
- 96. (a) Shift f(x) right by 3. Reflect it over the x-axis. Shift it up by 5.
  - (b) -
  - (c) Vertex: (3,5)Domain:  $(-\infty,\infty)$ Range:  $(-\infty,5]$ Maximum value: 5
  - (d) (-2,0),(8,0)
- 97. a = -3

$$\begin{array}{c|ccccc}
 & x & |x| & x^2 \\
\hline
 & -2 & 2 & 4 \\
 & -1 & 1 & 1 \\
 & -\frac{1}{2} & \frac{1}{2} & \frac{1}{4} \\
 & 1 & 1 & 1 \\
 & 2 & 2 & 4 \\
\end{array}$$

Vertex: (0,0)

Domain:  $(-\infty, \infty)$ 

Range:  $[0, \infty)$ 

Minimum value: 0

Axis of symmetry: x = 0

- 99. (a) y = |x 1| + 2
  - (b) y = -|x| + 1
  - (c) y = 2|x+3|-1

100. 
$$A + B = \begin{bmatrix} -1 & 3 \\ 6 & -2 \end{bmatrix} + \begin{bmatrix} 7 & 0 \\ 2 & -4 \end{bmatrix} = \begin{bmatrix} 6 & 3 \\ 8 & -6 \end{bmatrix}$$

$$A - B = \begin{bmatrix} -1 & 3 \\ 6 & -2 \end{bmatrix} - \begin{bmatrix} 7 & 0 \\ 2 & -4 \end{bmatrix} = \begin{bmatrix} -8 & 3 \\ 4 & 2 \end{bmatrix}$$

101. Vertex: (5, -3)

Domain:  $(-\infty, \infty)$ 

Range:  $[-3, \infty)$ 

Minimum: -3

*x*-intercepts:  $(\frac{1}{2}, 0), (\frac{19}{2}, 0)$ 

$$y = \begin{cases} \frac{2}{3}(x-5) - 3, & x \ge 5\\ -\frac{2}{3}(x-5) - 3, & x < 5 \end{cases}$$

102. Two: (0, h - k), (0, h + k)

	$\boldsymbol{x}$	$x^2$	$x^2 + 1$	$x^2 - 5$
	-2	4	5	-1
102	-1	1	2	-4
103.	0	0	1	-5
	1	1	2	-4
	2	4	5	-1

g(x): shift f(x) up by 1 f(x): shift f(x) down by 5

- 104. (a) 3 (b) -9
- 105. Intersections: (1,2), (5,2)Area = 8
- 106. (a) x = -1, 5(b)  $(-\infty, -1] \cup [5, \infty)$
- 107. (a) [0, 100]
  - (b) The midpoint of the road between Salina and Green River
  - (c) y = -|x 50| + 50
  - (d)  $d = -\frac{5}{6}|t 60| + 50$

Reflect f(x) over the x-axis.

	x	$x^2$	$2x^2$	$0.5x^{2}$
	-3	9	18	4.5
	-2	4	8	2
109.	-1	1	2	0.5
	0	0	0	0
	1	1	2	0.5
	2	4	8	2

g(x): Vertically stretch f(x) by a factor of 2.

h(x): Vertically compress f(x) by a factor of 2.

- 110. (a) Friday: \$2,250 Saturday: \$7,100
  - Sunday: \$5,650
  - (b)  $[120, 210] \cdot [10, 5] = 120(10) + 210(5) = $2, 250$
- 111. Shift f(x) up by c.
  - Vertex: (0, c)Range:  $[c, \infty)$ Minimum: c
- 112. (a)
  - (b) (32,55)
  - (c) (21,55]
  - (d) [45, 65]
- 113. Vertically stretch the graph by a factor of 3. Shift it up by 6.
  - 1
- 114. (a)
  - 1
  - 3 9

 $\boldsymbol{x}$ 

The values of  $x^2$  are useful as inputs for the  $g(x) = \sqrt{x}$  table.

- (b) Vertex: None
  - Domain:  $[0, \infty)$
  - Range:  $[0, \infty)$
  - Min: 0

It does not have an axis of symmetry.

- 115.  $a = \frac{3}{2}$
- 116. It's the total revenue that the zoo made on Sunday.
- 117.

$$\begin{bmatrix} 120(10) + 210(5) \\ 400(10) + 620(5) \\ 320(10) + 490(5) \end{bmatrix} = \begin{bmatrix} 2,250 \\ 7,100 \\ 5,650 \end{bmatrix}$$

118. Vertex: 
$$(0,0)$$

Max: 64

Axis of symmetry: x = 0x-intercepts: (-4,0), (0,4)

#### 119. Skip

120. Highest: 
$$y = x^2 + 1$$
  
Middle:  $y = \frac{1}{2}x^2$   
Lowest:  $y = -x^2 - 2$ 

#### 121. Shift the graph right by h

122. Shift 
$$f(x)$$
 right by 3

Domain of  $f: [0, \infty)$ 

Domain of  $g: [3, \infty)$ 

123.

$$\begin{bmatrix} 16\\20 \end{bmatrix}$$

124.

$$\begin{bmatrix} 5x - 2y \\ 3x + 4y \end{bmatrix}$$

125. No. The number of columns in A must equal the number of rows in B.

126. (a) 
$$(1,9), (7,9)$$

(b) 
$$x = 1, 7$$

$$127. -$$

129. 
$$h(x) = -2(x+2)^2$$

130. 
$$x = -2$$
  $(-4, 4)$ 

131. (a) 
$$(x+5)(x+5) = (x+5)^2$$
,  $5 = \frac{10}{2}$ ,  $\sqrt{25}$ 

(b) 
$$(x+6)(x+6) = (x+6)^2$$
,  $6 = \frac{12}{2}$ ,  $\sqrt{36}$ 

(c) 
$$(x-7)(x-7) = (x-7)^2$$
,  $-7 = \frac{-14}{2}$ ,  $-\sqrt{49}$ 

132.

$$\begin{bmatrix} 1 & 6 \\ -7 & -3 \end{bmatrix}$$

133. (a) Shift 
$$f(x)$$
 down by 4.

(b) 
$$h(x) = -(x+2)^2 - 7$$

- 134. (a) x = 1, 4
  - (b) (1,3), (4,6)
  - (c) -
- 135. Domain:  $[4, \infty)$ Range:  $[3, \infty)$
- 136.  $a = -\frac{1}{2}$
- 137. -
- 138.  $\left(-\frac{4}{3}, \frac{7}{3}\right), \left(\frac{8}{3}, -\frac{1}{3}\right)$
- 139. (a)  $x^2 16x + 64 = (x 8)^2$ 
  - (b)  $x^2 + 10x + 25 = (x+5)^2$
  - (c)  $x^2 5x + \frac{25}{4} = (x \frac{5}{2})^2$
- 140. (-4,0),(2,0)
- 141. (a) 2x(x-4)(x+4)
  - (b)  $(x+12)^2$
  - (c) (3x+1)(3x-2)
- 142. Sum:  $\begin{bmatrix} 8 & -2 \\ 1 & 2 \end{bmatrix}$

Product: 
$$\begin{bmatrix} 12 & 2 \\ 2 & -3 \end{bmatrix}$$

- 143. (5,0),(0,1)
- 144. Domain:  $(-\infty, 0]$ Range:  $[0, \infty)$
- 145. -
- 146. (a)  $x = 3 \pm \sqrt{11}$ 
  - (b)  $x = 3 \pm \sqrt{11}$
  - (c)  $x = 3 \pm \sqrt{11}$
- 147.  $x = 2 \pm \sqrt{6}$
- 148. No
- 149.

$$\begin{bmatrix} 1 & 2 \\ 3 & 3 \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 5 \\ 6 \end{bmatrix}$$

150. (a) x = 0, 10

- (b) A.O.S.: x = 5Vertex: (5, -25)
- (c) -
- 151. x = 5
- 152. (a) (0,0), (0,4), (-2,-4)
  - (b)  $(0,0),(3,0),(\frac{3}{2},-\frac{9}{2})$
  - (c)  $(0,0), (-\frac{7}{2},0), (-\frac{7}{4},\frac{49}{8})$
- 153.  $x = h \pm \sqrt{-\frac{k}{a}}$
- 154. (a)  $x = 4 \pm \sqrt{19}$ 
  - (b)  $x = -5 \pm \sqrt{36}$
  - (c)  $x = \frac{5}{2} \pm \frac{1}{2}\sqrt{33}$
- 155.  $x = -\frac{3}{5} \pm \sqrt{\frac{14}{25}}$
- 156. (a)

$$\begin{bmatrix} 2 & 3 \\ -1 & 5 \end{bmatrix}$$

(b)

$$\begin{bmatrix} 2 & 3 \\ -1 & 5 \end{bmatrix}$$

157.

$$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

- 158. (a)  $0 = a(0^2) + b(0) + c$ 
  - (b) a = 1
    - b = 1
  - (c)  $y = x^2 + x$
- 159. Greatest height: 3 units above the ground Distance: 12 units away
- 160. x-intercepts: (-2,0),(4,0)

Axis of symmetry: x = 1

The axis of symmetry runs through the midpoint of the x-intercepts.

161. (a) x-intercepts:  $(0,0), (-\frac{b}{a},0)$ Axis of symmetry:  $x=-\frac{b}{2a}$ 

(b) Translate it up by c

Axis of symmetry:  $x = -\frac{b}{2a}$ 

162. 
$$2(x-2)^2 - 7$$

163. 
$$3(x+\frac{2}{3})^2-\frac{7}{3}$$

164. (a) 
$$x = -\frac{1}{2}, 3$$

(b) 
$$x = -\frac{1}{2}, 3$$

165. The multiplicative inverse of  $\frac{2}{3}$  is  $\frac{3}{2}$ . No, zero doesn't have a multiplicative inverse.

166.

$$\begin{bmatrix} -1 & 2 \\ -3 & 5 \end{bmatrix}$$

167.  $y = x^2 - 2x + 3$  is  $y = x^2 - 2x$  translated up by 3.

168. 
$$y = 2x^2 - 6x + 2$$

169. (a) 
$$y = -0.002x(x - 250)$$

(b) 250 yards away Domain:  $x \in [0, 250]$ 

(c) 
$$\frac{125}{4}$$
 yards

170. 
$$x = -\frac{b}{2} \pm \sqrt{\frac{b^2}{4} - c}$$

171. (a) 
$$p^2(p-2)(p+2)$$

(b) 
$$w(w-5)(w+3)$$

(c) 
$$y(4-3z)(4+3z)$$

(d) 
$$2(x+5)^2$$

172. (a) 
$$x = 7 \pm \sqrt{3}$$

(b) 
$$x = -\frac{5}{3}, -2$$

(c) 
$$x = \pm \sqrt{6}$$

173. 
$$\left(\frac{m+n}{2}, -\frac{a}{4}(m-n)^2\right)$$

174.

$$\begin{bmatrix} 3 & 4 \\ 1 & 2 \end{bmatrix}^{-1} = \begin{bmatrix} 1 & -2 \\ -\frac{1}{2} & \frac{3}{2} \end{bmatrix}$$

175. (a) 
$$x = 1 \pm \sqrt{10}$$

(b) 
$$x = -1, 3$$

(c) 
$$x \in [-1, 3]$$