## IM2 Book 1 Selected Answers

## IM2 Dream Team

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1. 
$$x = -3$$

3. (a) 
$$x(x+4)$$

(b) 
$$3x(x-5)$$

(c) 
$$-x(2x+7)$$

4. (a) 
$$x = 0, 4$$

(b) 
$$x = 0, 5$$

(c) 
$$x = 0, -\frac{7}{2}$$

	$2 \le x$	_	all values that are at least 2	_
5.	-4 < x < 0	_	_	(-4,0)
	x < 1	_	all values that are less than 1	$(-\infty,1)$

6. Answers may vary. Soln: (0,5). Non-soln: (0,0).

7. 
$$4a^2, 2a^2$$

(b) 
$$24 \le x$$

9. (x+4)(x+1). 4 and 1 add to 5 and multiply to 4.

10. 
$$x^2 + (q+p)x + pq$$
.  $\nabla = (q+p)$ .  $\Delta = pq$ .

(b) 
$$37 \le 37$$

(d) 
$$x \ge 18$$

12. 
$$x = 1, -4, \frac{3}{2}$$

13. (a) Answers may vary.

System soln: (2,4)

Soln to one eqn but not the other: (0,0)

Not a system soln: (0,0)

- (b) -
- (c) One solution.
- 14. Answers may vary.

$$\begin{cases} y = x \\ y = x + 1 \end{cases}$$

15. Answers may vary.

$$\begin{cases} y = x \\ 2y = 2x \end{cases}$$

- 16.  $(3x)^2$
- 17. x > -5
- 18. (a)  $x \le -10$ 
  - (b)  $x \le -10$
- 19. (a) x = -4
  - (b) x = 3, 5
  - (c) x = -1, 7
- 20. (a)  $(\frac{1}{2}, \frac{1}{3})$ 
  - (b) (1, -2)
- 21. (a)
  - (b)  $y = x^2$
- 22. (a) f(2) = 5f(-4) = -1
  - (b) x = -1
- 23. (a) 2x + y = 3
  - (b) No solutions

	Words	Function Formula
24		f(x) = 2x
24.		f(x) = 5x - 1
	1 1 . 1 1 1 1	

divide the input by 2 and add 5

25. (a) 
$$f(-3) = 3$$
  
 $f(0) = 0$   
 $f(2) = 2$ 

(b) 
$$x = \pm 4$$

- 26. (a) -
  - (b) 6
  - (c)  $x = \pm 10$
- 27. (3x+4)(x-3)
- 28. (a)  $-7 \le x$ 
  - (b) x < 4
- 29. (a) 5
  - (b) 12
  - (c) |x y|
- 30. No
- 31.  $x \ge 0$
- 32. |a-b| = |b-a|
- 33. (4x+1)(x+5)
- 34. (a) 9 and 4
  - (b) 9 and -4
  - (c) x and 7
  - (d) x and 0
- 35. (a) -
  - (b) |x| > 6
  - (c) -

	_	all values that are 2 units away from -5		x = -3, -7
36.	x  = 5	_	_	x = -5, 5
	x+1  = 2	all values that are 2 units away from -1	_	x = -3, 1

- 37. (a) All values that are 5 units away from 2.
  - (b) All values that are 10 units away from -4.
- 38. A = (2a+b)(a+3b)
- 39. (a) (x-2)(x-6)
  - (b) (3x-2)(2x+3)
  - (c) 2x(3x-1)
- 40. BC = 8, AC = 15, and AB = 17
- 41. (a)  $x^2 16$ 
  - (b)  $x^2 49$

(c) 
$$9x^2 - 4$$

(d) 
$$x^2 - a^2$$

42. (a) 
$$(x-8)(x+8)$$

(b) 
$$(x-c)(x+c)$$

(c) 
$$(2x-5)(2x+5)$$

(d) 
$$(ax-c)(ax+c)$$

	_	all values that are at most 2 units away from -5	-	$-7 \le x \le -3$
43.	$ x  \ge 6$	_	_	x < -6  or  x > 6
	$ x-1  \le 4$	all values that are at most 4 units away from 1	_	_

- 44. (a) -
  - (b) (0,0)
  - (c)  $(-\infty, \infty)$
  - (d) y = 0
  - (e)  $[0,\infty)$

45. 
$$y = -x, y = x$$

$$|x| = \begin{cases} -x & \text{if } x < 0 \\ x & \text{if } x \ge 0 \end{cases}$$

- 46. x = 12
- 47. (a) All values at most 2 units away from 7.

(b) 
$$x > -2 \text{ or } x < -8$$

48. 
$$(-2,2)$$
  $(3,7)$ 

(b) 
$$|x - 52| \le 3$$

50. |x - y| = 12. Infinite.

51. (a) 
$$3x(x+4)$$

(b) 
$$(x+5)(x+3)$$

(c) 
$$2(x+1)(x-3)$$

(d) 
$$9(x-2)(x+2)$$

52. 120

53.

$$|x+2| = \begin{cases} -x+2 & \text{if } x < -2\\ x+2 & \text{if } x \ge -2 \end{cases}$$

- 54. (a) x = -5, 5
  - (b) blob = -5, 5
- 55. Yes
- 56. f(x) = |x|
- 57. (a) 77 blocks
  - (b) 19 blocks
  - (c) -
  - (d) y = |x 91|
- 58. -
- 59.  $|l 12| \le 0.01$
- 60. (a) (-28, 12)
  - (b)  $(-\infty,0] \cup [8,\infty)$
- 61. (a) a = -1, -6
  - (b)  $x = \frac{-19}{2}, \frac{9}{2}$
- 62.  $-1 \le a \le 6$
- 63. |x| = 3x = -3 or x = 3
- 64. No
- 65. (a) -
  - (b) y = |x 34|
  - (c) x = 18,50
- 66. x = -4, 4
- 67. (a) -
  - (b) vertex: (4,0)domain:  $(-\infty, \infty)$ range:  $[0, \infty)$ minimum value: y = 0
  - (c) x = 4
- 68. (a) Shift f(x) left by 5
  - (b) (-5,0). Shift it left by 5.
- 69. x = 6, 1

$$|x-7| = \begin{cases} x-7 & \text{if } x \ge 7\\ -x+7 & \text{if } x < 7 \end{cases}$$

72. 
$$x = 4, -6$$

73. 
$$x = -1, -4$$

75. 
$$g(x) = |x - h|$$

Translate f(x) down by 2.

77. (a) 
$$\left(-\frac{4}{3}, \frac{4}{3}\right)$$

(b) 
$$(-\infty, -\frac{84}{5}] \cup [\frac{56}{5}, \infty)$$

(c) 
$$\left[-\frac{1}{2}, \frac{13}{2}\right]$$

78. (a) 
$$x = -5, -4$$

(b) 
$$x = -\frac{7}{2}, 3$$

(c) 
$$x = -9, 9$$

(d) 
$$x = -\frac{1}{4}, 4$$

79. Left graph: 
$$y = |x|$$

Right graph: 
$$y = |x - 3|$$

81. 
$$f(x) = |x - 3|$$

82. 
$$n^2$$

83. 
$$x = -2, 4$$
  
 $x \in [-2, 4]$ 

84. (a) Shift/translate the graph up by 
$$k$$

(b) (0, k)Shift/translate (0, 0) up by k

	$\boldsymbol{x}$	x	- x
	-3	3	-3
	-2	2	-2
85.	-1	1	-1
00.	0	0	0
	1	1	-1
	2	2	-2
	3	3	-3

You can reflect y = |x| over the x-axis.

86. 
$$(2,0)$$
;  $(-2,0)$ ,  $(2,0)$ 

87.

$$g(x) = \begin{cases} -x - 2 \text{ if } x \le 0\\ x - 2 \text{ if } x > 0 \end{cases}$$

88. Shift f(x) to the right h and up k. Vertex: (h, k).

	$\boldsymbol{x}$	x	2 x	0.5 x
	-3	3	6	1.5
	-2	2	4	1
90	-1	1	2	0.5
89.	0	0	0	0
	1	1	2	0.5
	2	2	4	1
	3	3	6	1.5

You can vertically stretch |x| by a factor of 2 to get 2|x|. You can vertically compress |x| by a factor of 2 to get 0.5|x|.

- 90. (a) Vertically stretch |x| by a factor of a.
  - (b) Vertically stretch |x| by a factor of a and then reflect it over the x-axis.
- 91. 320, 210

92. 
$$\begin{bmatrix} 320 & 98 & 135 \\ 405 & 110 & 120 \end{bmatrix}$$

- 93. (0, |h| + k)
- 94. Vertex: (0,0)

Vertex: (0,6). *x*-intercepts: (-2,0),(2,0)

95. (a) Shift |x| right by 1. Vertically stretch it by a factor of 2. Shift it down by 6.

- (b) -
- (c) Vertex: (1, -6)Domain:  $(-\infty, \infty)$ Range:  $[-6, \infty)$ Minimum-value: y = -6
- (4) ( 2.0) (4.0)
- (d) (-2,0),(4,0)