## **IM2 Book 3 Selected Answers**

## Mr. Spence

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- 1.  $10\sqrt{2}$
- 2. (a)  $A = \left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right), B = \left(\frac{\sqrt{3}}{2}, \frac{1}{2}\right)$ 
  - (b) cos()
  - (c) sin()
- 3. (a) cos(40°)
  - (b) sin(40°)
- 4. (a)  $m_{OA} = 1$ ,  $m_{OB} = \frac{\sqrt{3}}{3}$ 
  - (b) tan()
- 5. 470 ft
- 6.  $\frac{3}{5}$
- 7. Length of line: 3.42 ft
  Distance to bobber: 9.40 ft
- 8. 23.82 ft
- 9. (a)  $\pi$ ; (-1,0)
  - (b)  $\frac{\pi}{2}$ ; (0,1)
- 10. –
- 11. -
- 12. -
- 13.  $\cos A = \frac{\sqrt{21}}{5}$ ,  $\tan A = \frac{2}{\sqrt{21}}$ ,  $\sin^2 A + \cos^2 A = 1$
- 14. (a) 79 ft
  - (b)  $7,873 \text{ ft}^2$
  - (c) 135 ft
- 15. 67°

- 16. 21.6°
- 17. No
- 18. 54.8 ft
- 19.  $\frac{2\pi}{3}$
- 20.  $\frac{6\pi}{5}$ ,  $\frac{9\pi}{5}$
- $21. \sin^2\theta + \cos^2\theta = 1$
- 22. length = 5.22; Area = 12.68
- 23.  $\frac{ab\sin C}{2}$
- 24.  $9.9 \text{ in}^2$
- 25. (-1,0), (-1,0)
- 26. –
- 27.  $\pi \alpha$
- 28. (a) (0,1)
  - (b)  $\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right)$
  - (c)  $\left(\frac{-1}{2}, \frac{\sqrt{3}}{2}\right)$
  - (d)  $\left(\frac{-\sqrt{3}}{2}, \frac{-1}{2}\right)$
- 29. (a)  $\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$ ;  $\cos\theta$  gives the x-coordinate;  $\sin\theta$  gives the y-coordinate
  - (b)  $\cos \frac{3\pi}{4} = \frac{-\sqrt{2}}{2}$ ,  $\sin \frac{3\pi}{4} = \frac{\sqrt{2}}{2}$
- 30. (a) AD = b x,  $BD = \sqrt{a^2 x^2}$ 
  - (b)  $c^2 = a^2 + b^2 2bx$
  - (c)  $c^2 = a^2 + b^2 2ab\cos C$
- 31. 5.01 in.
- 32. (a)  $\left(\frac{1}{2}, \frac{\sqrt{3}}{2}\right)$ ,  $m = \sqrt{3}$ 
  - (b)  $tan \theta$
- 33. 205°
- 34. (a)  $\sin \frac{2\pi}{3} = \frac{\sqrt{3}}{2}$ ,  $\cos \frac{2\pi}{3} = \frac{-1}{2}$ ,  $\tan \frac{2\pi}{3} = -\sqrt{3}$ 
  - (b)  $\sin \frac{4\pi}{3} = \frac{-\sqrt{3}}{2}$ ,  $\cos \frac{4\pi}{3} = \frac{-1}{2}$ ,  $\tan \frac{4\pi}{3} = \sqrt{3}$
- 35. (a)  $\sin 135^\circ = \frac{\sqrt{2}}{2}$ ,  $\cos 135^\circ = \frac{-\sqrt{2}}{2}$ ,  $\tan 135^\circ = -1$

(b) 
$$\sin 225^\circ = -\frac{\sqrt{2}}{2}$$
,  $\cos 225^\circ = \frac{-\sqrt{2}}{2}$ ,  $\tan 225^\circ = 1$ 

36. (a) 
$$\left(\frac{\sqrt{3}}{2}, -\frac{1}{2}\right)$$
,  $m = -\frac{\sqrt{3}}{3}$ 

(b) 
$$\sin\left(-\frac{\pi}{6}\right) = -\frac{1}{2}$$
,  $\cos\left(-\frac{\pi}{6}\right) = \frac{\sqrt{3}}{2}$ ,  $\tan\left(-\frac{\pi}{6}\right) = -\frac{\sqrt{3}}{3}$ 

37. 
$$\sin\left(-\frac{2\pi}{3}\right) = -\frac{\sqrt{3}}{2}$$
,  $\cos\left(\frac{5\pi}{2}\right) = 0$ ,  $\tan\left(\frac{2\pi}{3}\right) = -\sqrt{3}$ 

38. 
$$\cos A = -\frac{\sqrt{91}}{10}$$
,  $\tan A = -\frac{3}{\sqrt{91}}$ 

40. side length = 
$$16.8 \text{ cm}$$
, Area =  $91.3 \text{ cm}^2$ 

42. (a) 
$$c = p + q$$

(b) 
$$c = |p - q|$$

(c) 
$$c = \sqrt{p^2 + q^2}$$

43. (a) 
$$\sin 60^\circ = \sin 120^\circ = \frac{\sqrt{3}}{2}$$

(b) 
$$\sin 30^\circ = \sin 150^\circ = \frac{1}{2}$$

44. 
$$\sin \theta = \sin (\pi - \theta)$$

45. 
$$\cos\theta = -\cos(\pi - \theta)$$

46. 
$$\tan \theta = \tan (\theta + \pi)$$

47. 
$$\cos x = -\frac{\sqrt{4-a^2}}{2}$$
,  $\tan x = -\frac{a}{\sqrt{4-a^2}}$ 

48. (a) 
$$\frac{\pi}{6}$$
,  $\frac{5\pi}{6}$ 

(b) 
$$\sin(x) = \frac{1}{2}$$

49. 
$$\frac{\pi}{3}$$
,  $\pi - \frac{\pi}{3}$ 

50. 
$$\cos 280^{\circ} \approx 0.174$$
,  $\cos 100^{\circ} = \cos 260^{\circ} \approx -0.174$ ,  $\sin 190^{\circ} \approx -0.174$ 

51. (a) 
$$\cos 310^{\circ} < \cos 311^{\circ}$$

(b) 
$$\sin 76^{\circ} > \sin 106^{\circ}$$

(c) 
$$\sin 81^\circ = \sin 99^\circ$$

(d) 
$$\tan 89^{\circ} > \tan 71^{\circ}$$

52. 
$$BC = 4.01$$

- (c)  $\frac{\sqrt{3}}{2}$  (d)  $\frac{\sqrt{2}}{2}$
- 54. (a)  $\frac{\sqrt{3}}{2}$ (b)  $\frac{\sqrt{3}}{2}$ (c)  $-\sqrt{3}$ (d)  $\frac{\sqrt{2}}{2}$
- 55. (a)  $\theta = \frac{5\pi}{6}, \frac{7\pi}{6}$ 
  - (b)  $\theta = 0, \pi$
  - (c)  $\theta = \frac{3\pi}{2}$
- 56. (a)  $\theta = 0^{\circ}, 180^{\circ}$ 
  - (b)  $\theta = 135^{\circ}, 225^{\circ}$
  - (c)  $\theta = 45^{\circ}, 225^{\circ}$