

Shape Optimization of Coils

This model demonstrates how to design a coil geometry using gradient-based shape optimization. The objective is to achieve a uniform magnetic field along the coil axis and a field minimum near the axis ends. The model assumes azimuthal symmetry, but one can use the optimization result as inspiration for a 3D design.

Model Definition

The model is set up with six inner coils and one coil at each end with the opposite current direction. The current in the two outermost coils at each end is also optimized to mimic the effect of having coils with partial turns. The result of the shape optimization is shown in Figure 2, while the initial geometry for this model is shown in Figure 1.

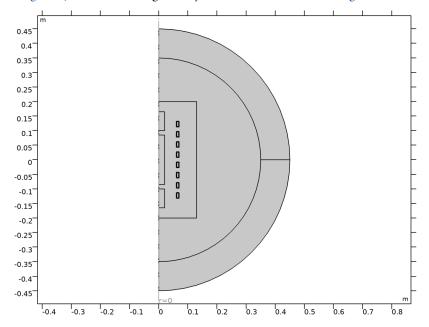


Figure 1: The initial geometry.

The Transformation and Free Shape Domain features are used to allow the coils to move in the radial direction. There are 8 control variables for the coil positions and one for the current in the outer coils. The IPOPT optimization can solve such problems fast.

The objective function, φ , consists of two terms:

$$\begin{split} \phi &= \phi_1 + \phi_2 \\ \phi_1 &= \int\limits_{\Omega_{inner}} (|\mathbf{B}| - \mathbf{B}_{avg})^2 d\Omega / \int\limits_{\Omega_{inner}} d\Omega \\ \mathbf{B}_{avg} &= \int\limits_{\Omega_{inner}} |\mathbf{B}| d\Omega / \int\limits_{\Omega_{inner}} d\Omega \\ \phi_2 &= \int\limits_{\Omega_{outer}} |\mathbf{B}| d\Omega / \int\limits_{\Omega_{outer}} d\Omega \end{split}$$

Results and Discussion

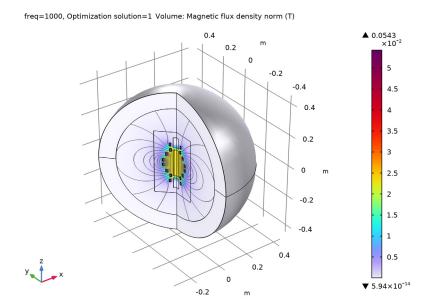


Figure 2: The optimized geometry.

Figure 2 shows the optimized design. The first and second objectives are reduced by around 90% and 50%, respectively. The strength of the magnetic field on the axis is illustrated in Figure 3.

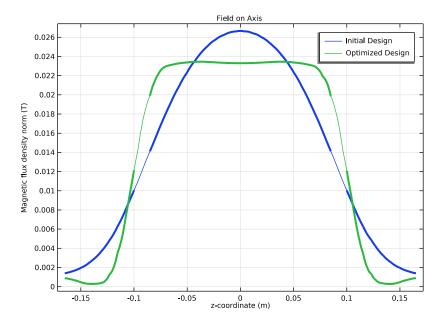


Figure 3: The optimization increases the magnetic field in the middle domain and decreases it in the outer domains.

Notes About the COMSOL Implementation

This model can be constructed in a way that exploits symmetry in the xy-plane, leading to a reduction in the computational time.

Application Library path: Optimization_Module/Shape_Optimization/ coil_shape_optimization

Modeling Instructions

From the File menu, choose New.

NEW

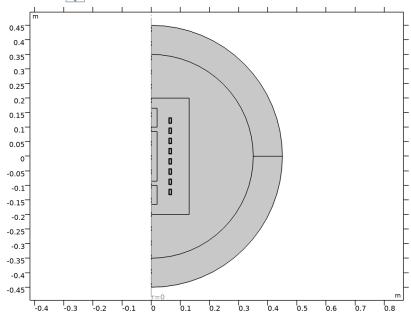
In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select AC/DC>Electromagnetic Fields>Magnetic Fields (mf).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click **Done**.

GEOMETRY I

- I In the Model Builder window, expand the Component I (compl)>Geometry I node.
- 2 Right-click Geometry I and choose Insert Sequence.
- 3 Browse to the model's Application Libraries folder and double-click the file coil_shape_optimization_geom_sequence.mph.
- 4 In the Geometry toolbar, click **Build All**.
- 5 Click the **Toom Extents** button in the **Graphics** toolbar.



The geometry should now look like that in Figure 1.

GLOBAL DEFINITIONS

Geometry Parameters

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, type Geometry Parameters in the Label text field.

Parameters 2

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
f0	1[kHz]	1000 Hz	Frequency
lastTurns	0.5	0.5	Outer loop current factor
dmax	3[cm]	0.03 m	Maximum coil translation

ADD MATERIAL

- I In the Home toolbar, click **Add Material** to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- **4** Click **Add to Component** in the window toolbar.
- 5 In the tree, select Built-in>Copper.
- **6** Click **Add to Component** in the window toolbar.
- 7 In the Home toolbar, click 4 Add Material to close the Add Material window.

MATERIALS

Copper (mat2)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Selection list, choose Objects to Mirror.

MAGNETIC FIELDS (MF)

Coil I

- I In the Model Builder window, under Component I (compl) right-click Magnetic Fields (mf) and choose the domain setting Coil.
- 2 In the Settings window for Coil, locate the Domain Selection section.

- 3 From the Selection list, choose Inner Coils.
- 4 Locate the Coil section. Select the Coil group check box.
- **5** In the I_{coil} text field, type 1 [kA].

Coil 2

- I Right-click Coil I and choose Duplicate.
- 2 In the Settings window for Coil, locate the Domain Selection section.
- 3 From the Selection list, choose Outer Coils 2.
- **4** Locate the **Coil** section. In the $I_{\rm coil}$ text field, type 1[kA]*lastTurns.

In a 2D axisymmetric model, specifying a coil with a fraction of the total current is a way to represent a coil with partial turns. Similarly, specifying a current with the opposite sign represents a coil that is wound in the opposite direction.

Coil 3

- I Right-click Coil 2 and choose Duplicate.
- 2 In the Settings window for Coil, locate the Domain Selection section.
- 3 From the Selection list, choose Outer Coils.
- **4** Locate the **Coil** section. In the I_{coil} text field, type -1[kA]*lastTurns.

MESH I

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Infinite Domains.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Boundary Selection section.
- 3 From the Selection list, choose Infinite Domain Boundaries.

Free Triangular I

In the Mesh toolbar, click Free Triangular.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.

- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Deforming Domain.
- 5 Locate the Element Size section. From the Predefined list, choose Extremely fine.

Size 2

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Whole Axis.
- **5** Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type 0.004.
- 8 Click **Build All**.

COMPONENT I (COMPI)

Free Shape Domain 1

- I In the Physics toolbar, click of Optimization and choose Shape Optimization.
- 2 In the Settings window for Free Shape Domain, locate the Domain Selection section.
- 3 From the Selection list, choose Deforming Domain.

Transformation 1

- I In the Shape Optimization toolbar, click | Transformation.
- 2 In the Settings window for Transformation, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Objects to Mirror.
- **4** Locate the **Translation** section. In the table, enter the following settings:

	Lock	Lower bound (m)	Upper bound (m)
R		-dmax	dmax
Z		-coilSpace/4	coilSpace/4

5 Locate the Scaling section. From the Scaling type list, choose No scaling.

DEFINITIONS

Average inner magnetic field

I In the Definitions toolbar, click Probes and choose Domain Probe.

- 2 In the Settings window for Domain Probe, type Average inner magnetic field in the Label text field.
- 3 In the Variable name text field, type Bavg.
- 4 Locate the Source Selection section. From the Selection list, choose Rectangle 4.

Average squared deviation from average

- I Right-click Average inner magnetic field and choose Duplicate.
- 2 In the Settings window for Domain Probe, type Average squared deviation from average in the Label text field.
- 3 In the Variable name text field, type Bdev sq.
- 4 Locate the Expression section. In the Expression text field, type (mf.normB-Bavg)^2.

Average outer magnetic field

- I Right-click Average squared deviation from average and choose Duplicate.
- 2 In the Settings window for Domain Probe, type Average outer magnetic field in the Label text field.
- 3 In the Variable name text field, type Bouter.
- 4 Locate the Source Selection section. From the Selection list, choose Outer Objective Domain.
- **5** Locate the **Expression** section. In the **Expression** text field, type mf.normB.

Infinite Element Domain I (ie I)

- 2 In the Settings window for Infinite Element Domain, locate the Domain Selection section.
- 3 From the Selection list, choose Infinite Domains.

STUDY I

Step 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type f0.

Obtimization

- I In the Study toolbar, click optimization and choose Optimization.
- 2 In the Settings window for Optimization, locate the Optimization Solver section.
- **3** From the **Method** list, choose **MMA**.

- 4 Find the Solver settings subsection. From the Keep solutions list, choose Every Nth.
- 5 In the Save every Nth text field, type 1000. This effectively saves the first and last iteration.
- 6 Locate the Objective Function section. From the Objective scaling list, choose Initial solution based.
- 7 Click Add Expression in the upper-right corner of the Objective Function section. From the menu, choose Component I (compl)>Definitions>compl.Bdev_sq -Average squared deviation from average - $kg^2/(s^4 \cdot A^2)$.
- 8 Click Add Expression in the upper-right corner of the Objective Function section. From the menu, choose Component I (compl)>Definitions>compl.Bouter -Average outer magnetic field - T.

Take the square root of the Bdev sq, so that the two objectives get the same unit.

9 Locate the **Objective Function** section. In the table, enter the following settings:

Expression	Description	Evaluate for
sqrt(comp1.Bdev_sq)	Domain Probe 2	Frequency Domain

10 Locate the Control Variables and Parameters section. Click + Add. Initialize the study to generate a plot for use while solving.

II In the table, enter the following settings:

Parameter name	Initial value	Scale	Lower bound	Upper bound
lastTurns (Outer loop current factor)	0.5	1	0	1

12 Locate the Output While Solving section. From the Probes list, choose None.

13 In the Model Builder window, click Study 1.

14 In the Settings window for Study, type Shape Optimization in the Label text field.

15 In the Study toolbar, click t=0 Get Initial Value.

RESULTS

Shape Optimization

The plot shows the displacement. Add an **Annotation** feature to also show the value of the lastTurns parameter.

Annotation I

I In the Model Builder window, right-click Shape Optimization and choose Annotation.

- 2 In the Settings window for Annotation, locate the Annotation section.
- **3** In the **Text** text field, type eval(lastTurns).
- 4 Locate the Coloring and Style section. Clear the Show point check box.
- 5 From the Background color list, choose Gray.

SHAPE OPTIMIZATION

Obtimization

- I In the Model Builder window, under Shape Optimization click Optimization.
- 2 In the Settings window for Optimization, locate the Output While Solving section.
- **3** Select the **Plot** check box.
- 4 From the Plot group list, choose Shape Optimization.

Enable move limits to reduce the risk of inverted elements.

Solver Configurations

In the Model Builder window, expand the Shape Optimization>Solver Configurations node.

Solution I (soll)

- I In the Model Builder window, expand the Shape Optimization>Solver Configurations> Solution I (soll) node, then click Optimization Solver I.
- 2 In the Settings window for Optimization Solver, locate the Optimization Solver section.
- 3 Select the Move limits check box.
- 4 Select the Maximum number of outer iterations check box. In the associated text field, type 50.
- 5 Click **Compute**.

RESULTS

Magnetic Flux Density Norm, Revolved Geometry (mf)

- I In the Magnetic Flux Density Norm, Revolved Geometry (mf) toolbar, click Plot.
- 2 Click the **Zoom Extents** button in the **Graphics** toolbar.

Field on Axis

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Field on Axis in the Label text field.
- 3 Locate the Data section. From the Optimization solution list, choose First.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Line Graph 1

- I Right-click Field on Axis and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Whole Axis.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 5 In the Expression text field, type z.
- **6** Click to expand the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legends Initial Design

Line Graph 2

- I Right-click Line Graph I and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Shape Optimization/Solution I (soll).
- 4 From the Optimization solution list, choose Last.
- **5** Locate the **Legends** section. In the table, enter the following settings:

Legends Optimized Design

Line Graph 3

- I In the Model Builder window, right-click Field on Axis and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Inner Axis.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 5 In the Expression text field, type z.
- 6 Click to expand the Coloring and Style section. From the Color list, choose Cycle (reset).
- 7 From the Width list, choose 3.

Line Graph 4

- I Right-click Line Graph 3 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the Data section.

- 3 From the Dataset list, choose Shape Optimization/Solution I (soll).
- 4 From the Optimization solution list, choose Last.
- 5 Locate the Coloring and Style section. From the Color list, choose Cycle.

Line Graph 3, Line Graph 4

- I In the Model Builder window, under Results>Field on Axis, Ctrl-click to select Line Graph 3 and Line Graph 4.
- 2 Right-click and choose **Duplicate**.

Line Graph 5

- I In the Settings window for Line Graph, locate the Selection section.
- 2 From the Selection list, choose Outer Axis.

Line Graph 6

- I In the Model Builder window, click Line Graph 6.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Outer Axis.
- 4 In the Field on Axis toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Compute the value of the objective functions before and after optimization.

Evaluation Group 1

In the Results toolbar, click Evaluation Group.

Global Evaluation 1

- I Right-click Evaluation Group I and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Definitions>Bdev_sq - Average squared deviation from average - kg²/(s⁴·A²).
- 3 Click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Definitions>Bouter - Average outer magnetic field -T.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
sqrt(Bdev_sq)	T	
Bouter	Т	Average outer magnetic field

5 In the Evaluation Group I toolbar, click **= Evaluate**.

Compute the value of the corners, so that one can construct an interpolation function for 3D verification.

Point Displacements

- I In the Results toolbar, click Evaluation Group.
- 2 In the Settings window for Evaluation Group, type Point Displacements in the Label text field.
- 3 Locate the Data section. From the Optimization solution list, choose Last.

Point Evaluation 1

- I Right-click Point Displacements and choose Point Evaluation.
- 2 In the Settings window for Point Evaluation, locate the Selection section.
- 3 From the Selection list, choose Lower left point.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
r	m	r-coordinate
Z	m	z-coordinate

5 In the Point Displacements toolbar, click **= Evaluate**.

Geometry Modeling Instructions

From the File menu, choose New.

NEW

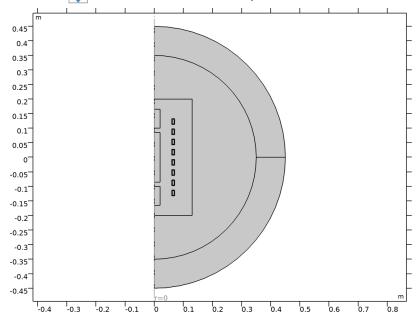
In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select AC/DC>Electromagnetic Fields>Magnetic Fields (mf).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click M Done.

GEOMETRY I

- I In the Model Builder window, expand the Component I (compl)>Geometry I node.
- 2 Right-click Geometry I and choose Insert Sequence.
- 3 Browse to the model's Application Libraries folder and double-click the file coil_shape_optimization_geom_sequence.mph.
- 4 In the Geometry toolbar, click | Build All.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.



The geometry should now look like that in Figure 1.

GLOBAL DEFINITIONS

Geometry Parameters

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, type Geometry Parameters in the Label text field.

Parameters 2

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
f0	1[kHz]	1000 Hz	Frequency
lastTurns	0.5	0.5	Outer loop current factor
dmax	3[cm]	0.03 m	Maximum coil translation

ADD MATERIAL

- I In the Home toolbar, click 👯 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select Built-in>Copper.
- 6 Click Add to Component in the window toolbar.
- 7 In the Home toolbar, click **Add Material** to close the Add Material window.

MATERIALS

Copper (mat2)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Selection list, choose Objects to Mirror.

MAGNETIC FIELDS (MF)

Coil I

- I In the Model Builder window, under Component I (compl) right-click Magnetic Fields (mf) and choose the domain setting Coil.
- 2 In the Settings window for Coil, locate the Domain Selection section.
- 3 From the Selection list, choose Inner Coils.
- **4** Locate the **Coil** section. Select the **Coil** group check box.
- **5** In the I_{coil} text field, type 1[kA].

Coil 2

- I Right-click Coil I and choose Duplicate.
- 2 In the Settings window for Coil, locate the Domain Selection section.
- 3 From the Selection list, choose Outer Coils 2.

4 Locate the **Coil** section. In the I_{coil} text field, type 1[kA]*lastTurns.

In a 2D axisymmetric model, specifying a coil with a fraction of the total current is a way to represent a coil with partial turns. Similarly, specifying a current with the opposite sign represents a coil that is wound in the opposite direction.

Coil 3

- I Right-click Coil 2 and choose Duplicate.
- 2 In the Settings window for Coil, locate the Domain Selection section.
- 3 From the Selection list, choose Outer Coils.
- **4** Locate the **Coil** section. In the I_{coil} text field, type -1[kA]*lastTurns.

MESH I

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Infinite Domains.

Distribution 1

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Boundary Selection section.
- 3 From the Selection list, choose Infinite Domain Boundaries.

Free Triangular 1

In the Mesh toolbar, click Free Triangular.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 From the Selection list, choose Deforming Domain.
- 5 Locate the Element Size section. From the Predefined list, choose Extremely fine.

Size 2

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.

- 4 From the Selection list, choose Whole Axis.
- **5** Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type 0.004.
- 8 Click III Build All.

COMPONENT I (COMPI)

Free Shape Domain I

- I In the Physics toolbar, click of Optimization and choose Shape Optimization.
- 2 In the Settings window for Free Shape Domain, locate the Domain Selection section.
- 3 From the Selection list, choose Deforming Domain.

Transformation 1

- I In the Shape Optimization toolbar, click Transformation.
- 2 In the Settings window for Transformation, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Objects to Mirror.
- **4** Locate the **Translation** section. In the table, enter the following settings:

	Lock	Lower bound (m)	Upper bound (m)
R		-dmax	dmax
Z		-coilSpace/4	coilSpace/4

5 Locate the Scaling section. From the Scaling type list, choose No scaling.

DEFINITIONS

Average inner magnetic field

- I In the **Definitions** toolbar, click **Probes** and choose **Domain Probe**.
- 2 In the Settings window for Domain Probe, type Average inner magnetic field in the Label text field.
- 3 In the Variable name text field, type Bavg.
- 4 Locate the Source Selection section. From the Selection list, choose Rectangle 4.

Average squared deviation from average

- I Right-click Average inner magnetic field and choose Duplicate.
- 2 In the Settings window for Domain Probe, type Average squared deviation from average in the Label text field.

- 3 In the Variable name text field, type Bdev sq.
- 4 Locate the Expression section. In the Expression text field, type (mf.normB-Bavg)^2.

Average outer magnetic field

- I Right-click Average squared deviation from average and choose Duplicate.
- 2 In the Settings window for Domain Probe, type Average outer magnetic field in the **Label** text field.
- 3 In the Variable name text field, type Bouter.
- 4 Locate the Source Selection section. From the Selection list, choose Outer Objective Domain.
- **5** Locate the **Expression** section. In the **Expression** text field, type mf.normB.

Infinite Element Domain I (iel)

- I In the Definitions toolbar, click ^{↑∞} Infinite Element Domain.
- 2 In the Settings window for Infinite Element Domain, locate the Domain Selection section.
- 3 From the Selection list, choose Infinite Domains.

STUDY I

Steb 1: Frequency Domain

- I In the Model Builder window, under Study I click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- **3** In the **Frequencies** text field, type **f**0.

Optimization

- I In the Study toolbar, click optimization and choose Optimization.
- 2 In the Settings window for Optimization, locate the Optimization Solver section.
- 3 From the Method list, choose MMA.
- 4 Find the Solver settings subsection. From the Keep solutions list, choose Every Nth.
- 5 In the Save every Nth text field, type 1000. This effectively saves the first and last iteration.
- 6 Locate the Objective Function section. From the Objective scaling list, choose Initial solution based.
- 7 Click Add Expression in the upper-right corner of the Objective Function section. From the menu, choose Component I (compl)>Definitions>compl.Bdev_sq -Average squared deviation from average - kg²/(s⁴·A²).

8 Click Add Expression in the upper-right corner of the Objective Function section. From the menu, choose Component I (compl)>Definitions>compl.Bouter -Average outer magnetic field - T.

Take the square root of the Bdev sq, so that the two objectives get the same unit.

9 Locate the **Objective Function** section. In the table, enter the following settings:

Expression	Description	Evaluate for
sqrt(comp1.Bdev_sq)	Domain Probe 2	Frequency Domain

10 Locate the **Control Variables and Parameters** section. Click + Add.

Initialize the study to generate a plot for use while solving.

II In the table, enter the following settings:

Parameter name	Initial value	Scale	Lower bound	Upper bound
lastTurns (Outer loop current factor)	0.5	1	0	1

12 Locate the Output While Solving section. From the Probes list, choose None.

13 In the Model Builder window, click Study 1.

14 In the Settings window for Study, type Shape Optimization in the Label text field.

15 In the Study toolbar, click $\underset{=}{\overset{\cup}{\cup}}$ Get Initial Value.

RESULTS

Shape Optimization

The plot shows the displacement. Add an **Annotation** feature to also show the value of the lastTurns parameter.

Annotation I

- I In the Model Builder window, right-click Shape Optimization and choose Annotation.
- 2 In the Settings window for Annotation, locate the Annotation section.
- **3** In the **Text** text field, type eval(lastTurns).
- 4 Locate the Coloring and Style section. Clear the Show point check box.
- 5 From the Background color list, choose Gray.

SHAPE OPTIMIZATION

Obtimization

I In the Model Builder window, under Shape Optimization click Optimization.

- 2 In the Settings window for Optimization, locate the Output While Solving section.
- **3** Select the **Plot** check box.
- 4 From the Plot group list, choose Shape Optimization.

Enable move limits to reduce the risk of inverted elements.

Solver Configurations

In the Model Builder window, expand the Shape Optimization>Solver Configurations node.

Solution I (soll)

- I In the Model Builder window, expand the Shape Optimization>Solver Configurations> Solution I (soll) node, then click Optimization Solver I.
- 2 In the Settings window for Optimization Solver, locate the Optimization Solver section.
- 3 Select the Move limits check box.
- 4 Select the Maximum number of outer iterations check box. In the associated text field, type 50.
- 5 Click **Compute**.

RESULTS

Magnetic Flux Density Norm, Revolved Geometry (mf)

- I In the Magnetic Flux Density Norm, Revolved Geometry (mf) toolbar, click Plot.
- 2 Click the Zoom Extents button in the Graphics toolbar.

Field on Axis

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Field on Axis in the Label text field.
- 3 Locate the Data section. From the Optimization solution list, choose First.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Line Graph 1

- I Right-click Field on Axis and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Whole Axis.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **5** In the **Expression** text field, type z.
- 6 Click to expand the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.

8 In the table, enter the following settings:

Legends Initial Design

Line Graph 2

- I Right-click Line Graph I and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Shape Optimization/Solution I (soll).
- 4 From the Optimization solution list, choose Last.
- **5** Locate the **Legends** section. In the table, enter the following settings:

Legends Optimized Design

Line Graph 3

- I In the Model Builder window, right-click Field on Axis and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Inner Axis.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **5** In the **Expression** text field, type z.
- 6 Click to expand the Coloring and Style section. From the Color list, choose Cycle (reset).
- **7** From the **Width** list, choose **3**.

Line Graph 4

- I Right-click Line Graph 3 and choose Duplicate.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Shape Optimization/Solution I (soll).
- 4 From the Optimization solution list, choose Last.
- 5 Locate the Coloring and Style section. From the Color list, choose Cycle.

Line Graph 3, Line Graph 4

- I In the Model Builder window, under Results>Field on Axis, Ctrl-click to select Line Graph 3 and Line Graph 4.
- 2 Right-click and choose **Duplicate**.

Line Graph 5

- I In the Settings window for Line Graph, locate the Selection section.
- 2 From the Selection list, choose Outer Axis.

Line Graph 6

- I In the Model Builder window, click Line Graph 6.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Outer Axis.
- 4 In the Field on Axis toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Compute the value of the objective functions before and after optimization.

Evaluation Group 1

In the Results toolbar, click Evaluation Group.

Global Evaluation 1

- I Right-click Evaluation Group I and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)> Definitions>Bdev_sq - Average squared deviation from average - kg²/(s⁴·A²).
- 3 Click Add Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Definitions>Bouter - Average outer magnetic field -T.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
sqrt(Bdev_sq)	Т	
Bouter	Т	Average outer magnetic field

5 In the Evaluation Group I toolbar, click **= Evaluate**.

Compute the value of the corners, so that one can construct an interpolation function for 3D verification.

Point Displacements

- I In the Results toolbar, click Evaluation Group.
- 2 In the Settings window for Evaluation Group, type Point Displacements in the Label text field.

3 Locate the Data section. From the Optimization solution list, choose Last.

Point Evaluation 1

- I Right-click Point Displacements and choose Point Evaluation.
- 2 In the Settings window for Point Evaluation, locate the Selection section.
- **3** From the **Selection** list, choose **Lower left point**.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
r	m	r-coordinate
Z	m	z-coordinate

5 In the Point Displacements toolbar, click **= Evaluate**.