

Ground Heat Recovery for Radiant Floor Heating

Geothermal heating is an environmentally friendly and energy efficient method to supply modern and well insulated houses with heat. The investment costs are higher than for gas or oil heating so there is a need to investigate the possibilities of arranging heat collectors in the subsurface.

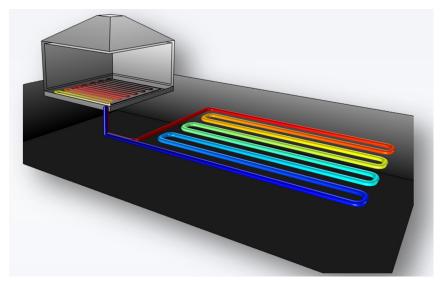


Figure 1: Example of heat recovery coils in a garden, connected to a dwelling via a heat pump.

This example compares three different patterns embedded in the subsurface. Typical thermal properties of an uppermost soil layer in a garden are used for the calculations.

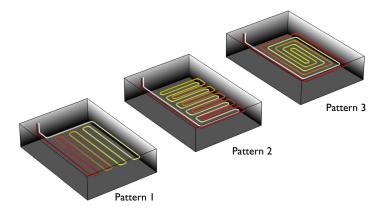


Figure 2: Patterns for the heat collectors.

Model Definition

The three patterns for the pipe arrangement are shown in Figure 2. The geometry subsequence functionality in COMSOL Multiphysics offers the possibility to perform the analysis over different pipe arrangements within the same model using a parametric sweep.

This model uses functions and events to describe the real operating conditions. For the subsurface, a temperature gradient with depth is prescribed. At the surface, a time dependent temperature is applied which corresponds to typical temperature variations in central Europe.

Assuming that the fluid properties are temperature-independent, the inlet temperature of the heat collector required to reach a certain heat extraction rate, P(t) is given by

$$T_{\rm in} = T_{\rm out} - \frac{P}{\rho C_p \dot{V}} \tag{1}$$

where ho and C_p the density and specific heat capacity for the fluid inside the pipes and \dot{V} the volumetric flow rate, here equal to 1 l/s.

The dynamic heat extraction is triggered according to a typical daily heat demand of a single-family house. The heat extraction process is active each day until the demanded heat is extracted. When the demand is reached, the heat extraction is stopped but the fluid flow in the pipes still continue at a lower rate. In this application, this flow rate during inaction of the pump is set to 1/10th of the operating flow rate, that is, 0.1 l/s.

Results and Discussion

The pipe temperature for the third pattern after two days is shown below.

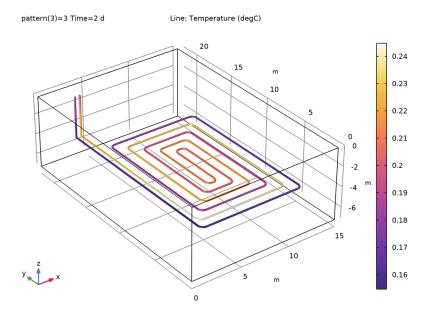


Figure 3 shows the outlet temperature over time for the third pattern. It is important to make sure that the fluid inside the pipes stays above a certain value. In this example, water is used as working fluid. However, during winter, the ambient temperature above the surface may reach values below 0 °C. In practical situations, antifreezes — such as glycerol

— are added to water and this application assumes that such additives do not modify its thermal properties.

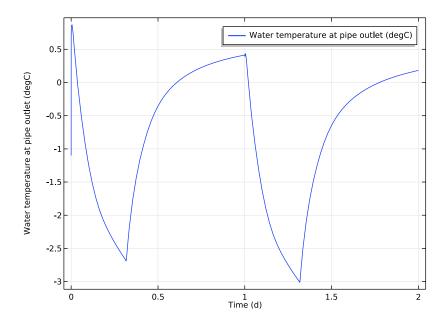


Figure 3: Outlet temperatures for the third pattern.

The temperature variations in Figure 3 correspond to the moments when the heater is turned on or off. The graph of the heater state in time is shown in Figure 4.

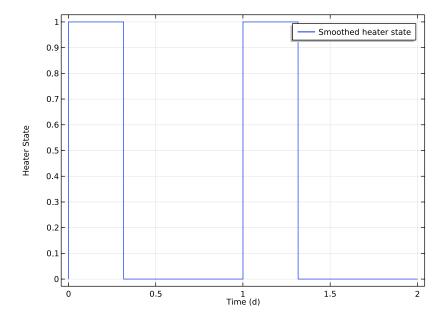


Figure 4: Heater state in time for the third pattern. A value of 0 indicates that the heater is turned off while I indicates that the heater is turned on.

The heater state itself depends on the daily heat production. As soon as the heat production reaches the daily demand, the heater state is turned off until the next day.

Figure 5 shows the heat production the two days of simulation time. Just after the daily requirement of 30 kWh, the production is stopped until the next day.

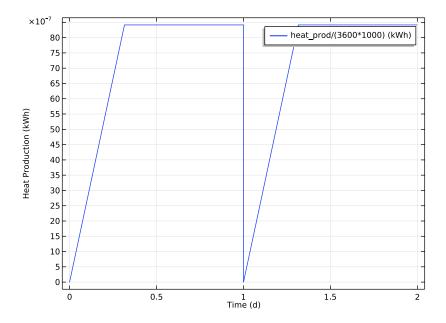


Figure 5: Heat production for the third pattern.

Notes About the COMSOL Implementation

This model uses several interpolation functions, which are based on rough estimations and local temperature variations, which may differ for your case. The functions needs to be replaced by your own measured data. Then, you need to make sure that the time stepping is still fine enough to resolve them.

Application Library path: Pipe Flow Module/Heat Transfer/ ground_heat_recovery

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 1 3D.
- 2 In the Select Physics tree, select Heat Transfer>Heat Transfer in Solids (ht).
- 3 Click Add.
- 4 In the Select Physics tree, select Heat Transfer>Heat Transfer in Pipes (htp).
- 5 Click Add.
- 6 In the Select Physics tree, select Mathematics>ODE and DAE Interfaces>Events (ev).
- 7 Click Add.
- 8 In the Select Physics tree, select Mathematics>ODE and DAE Interfaces> Global ODEs and DAEs (ge).
- 9 Click Add.
- 10 Click Study.
- II In the Select Study tree, select General Studies>Time Dependent.
- 12 Click **Done**.

GEOMETRY I

This example demonstrates how to use part import and programming to perform the simulation for different geometries. Start by importing the parts from a file, as shown below.

- I In the Geometry toolbar, click Load Part and choose Load Part.
- **2** Browse to the model's Application Libraries folder and double-click the file ground_heat_recovery_geom_sequence.mph.
- 3 In the Load Part dialog box, in the Select parts list, choose Pattern 1, Pattern 2, and Pattern 3.
- 4 Click OK.

GLOBAL DEFINITIONS

Parameters 1

Define the parameter that will be used to call the different patterns.

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
pattern	3	3	Parameter for selecting the pattern

This parameter is now used to import the different patterns into the work plane based on a logical expression.

Add the remaining parameters.

4 In the table, enter the following settings:

Name	Expression	Value	Description
d_pipe	36[mm]	0.036 m	Pipe diameter in soil
flowrate_pipe	1[1/s]	0.001 m³/s	Flow rate inside pipes
heat_demand	30[kW*h]	1.08E8 J	Daily heat demand
power	4[kW]	4000 W	Heat pump power
dt	30[s]	30 s	Smoothed heater state transition zone
depth	4[m]	4 m	Depth of heat exchanger
Tz_depth	0.5[K/m]	0.5 K/m	Temperature gradient
month	1	1	Month index
humidity	1	1	Soil humidity
k_soil	0.18[W/(m*K)]+(1.5- 0.18)*humidity	1.5 W/(m·K)	Soil thermal conductivity

GEOMETRY I

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 In the z-coordinate text field, type -depth.
- 4 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 5 In the New Cumulative Selection dialog box, type Pipes in the Name text field.

6 Click OK.

The above step ensures that, independently of the pattern you choose, the pipes are selected correctly.

7 In the Settings window for Work Plane, click A Go to Plane Geometry.

```
Work Plane I (wpl)>If I (if1)
```

- I In the Work Plane toolbar, click | Programming and choose If + End If.
- 2 In the Settings window for If, locate the If section.
- 3 In the Condition text field, type pattern==1.

```
Work Plane I (wpl) > Import I (impl)
```

- I In the Work Plane toolbar, click | Import.
- 2 In the Settings window for Import, locate the Import section.
- **3** From the **Source** list, choose **Geometry sequence**.
- 4 From the Geometry list, choose Pattern 1.

```
Work Plane I (wpl)>Else If I (elseifI)
```

- I In the Model Builder window, right-click Plane Geometry and choose Programming> Else If.
- 2 In the Settings window for Else If, locate the Else If section.
- 3 In the Condition text field, type pattern==2.

```
Work Plane I (wb I) > Import 2 (imb2)
```

- I In the Work Plane toolbar, click Import.
- 2 In the Settings window for Import, locate the Import section.
- **3** From the **Source** list, choose **Geometry sequence**.
- 4 From the Geometry list, choose Pattern 2.

```
Work Plane I (wbl)>Else I (else I)
```

Right-click Plane Geometry and choose Programming>Else.

```
Work Plane I (wb I) > Import 3 (imb3)
```

- I In the Work Plane toolbar, click Import.
- 2 In the Settings window for Import, locate the Import section.
- 3 From the Source list, choose Geometry sequence.
- 4 From the Geometry list, choose Pattern 3.

Polygon I (poll)

- I In the Model Builder window, right-click Geometry I and choose More Primitives> Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- **3** In the table, enter the following settings:

x (m)	y (m)	z (m)
2.5	20	0
2.5	20	-depth

4 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Pipes.

Copy I (copy I)

- I In the Geometry toolbar, click Transforms and choose Copy.
- **2** Select the object **poll** only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type 0.5.
- 5 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Pipes.

Block I (blk I)

- I In the **Geometry** toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- **3** In the **Width** text field, type 15.
- 4 In the **Depth** text field, type 22.
- 5 In the **Height** text field, type depth+3[m].
- 6 Locate the **Position** section. In the **z** text field, type (depth+3[m]).
- 7 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. Click New.
- 8 In the New Cumulative Selection dialog box, type Ground in the Name text field.
- 9 Click OK.
- 10 In the Settings window for Block, click | Build All Objects.
- II Click the **Zoom Extents** button in the **Graphics** toolbar.

DEFINITIONS

Hide for Physics 1

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click View I and choose Hide for Physics.
- 3 In the Settings window for Hide for Physics, locate the Geometric Entity Selection section.
- 4 From the Geometric entity level list, choose Boundary.
- **5** Select Boundaries 1, 2, and 4 only.

GLOBAL DEFINITIONS

Define the functions for the surface temperature and the initial temperature.

Yearly Temperature Profile

- I In the Home toolbar, click f(X) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, type Yearly Temperature Profile in the Label text field.
- 3 Locate the **Definition** section. In the **Function name** text field, type T_z0.
- 4 Click Load from File.
- **5** Browse to the model's Application Libraries folder and double-click the file ground heat recovery T surface.txt.
- 6 Locate the Interpolation and Extrapolation section. From the Interpolation list, choose Piecewise cubic.
- 7 Locate the **Units** section. In the **Argument** table, enter the following settings:

Argument	Unit
t	a

8 In the **Function** table, enter the following settings:

Function	Unit
T_z0	degC

9 Click To Create Plot.

RESULTS

Temperature Profile

I In the Settings window for ID Plot Group, type Temperature Profile in the Label text field.

- 2 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 3 Locate the Plot Settings section.
- **4** Select the **x-axis label** check box. In the associated text field, type Month.

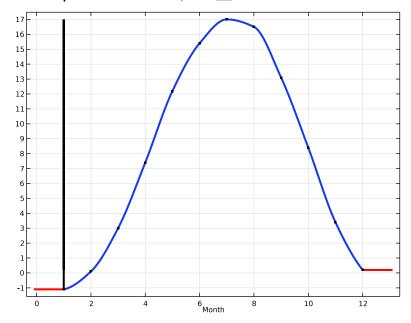
Function I

- I In the Model Builder window, expand the Temperature Profile node, then click Function I.
- 2 In the Settings window for Function, locate the y-Axis Data section.
- 3 In the Expression text field, type T_z0(root.t[a])[1/degC].
- 4 Locate the x-Axis Data section. In the Expression text field, type root.t*12.
- 5 In the Lower bound text field, type 1.
- **6** In the **Upper bound** text field, type 12.
- 7 In the **Description** text field, type Month.
- **8** Click to expand the **Coloring and Style** section. From the **Width** list, choose **3**.

Line Graph 1

- I In the Model Builder window, right-click Temperature Profile and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Grid ID 1.
- 4 Locate the y-Axis Data section. In the Expression text field, type T z0(root.t[a])[1/ degC].
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **6** In the **Expression** text field, type month.
- 7 Click to expand the Coloring and Style section. From the Color list, choose Black.
- **8** From the **Width** list, choose **3**.

9 In the **Temperature Profile** toolbar, click **Plot**.



GLOBAL DEFINITIONS

Depth Temperature Gradient

- I In the Home toolbar, click f(X) Functions and choose Global>Analytic.
- 2 In the Settings window for Analytic, type Depth Temperature Gradient in the Label text field.
- 3 In the Function name text field, type T0.
- 4 Locate the **Definition** section. In the **Expression** text field, type T_z0(month[a]/12)[1/ degC]+Tz_depth[m/K]*(-z).
- 5 In the Arguments text field, type z.
- **6** Locate the **Units** section. In the table, enter the following settings:

Argument	Unit
Z	m

7 In the Function text field, type degC.

8 Locate the **Plot Parameters** section. In the table, enter the following settings:

Plot	Argument	Lower limit	Upper limit	Fixed value	Unit
	z	-10	0	0	m

9 Click 🚮 Create Plot.

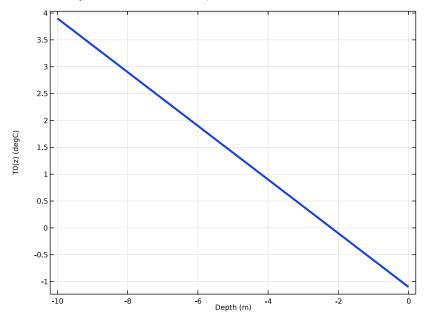
RESULTS

Temperature Gradient

- I In the Settings window for ID Plot Group, type Temperature Gradient in the Label text field.
- 2 Locate the Title section. From the Title type list, choose None.
- 3 Locate the Plot Settings section.
- 4 Select the x-axis label check box. In the associated text field, type Depth (m).

Function I

- I In the Model Builder window, expand the Temperature Gradient node, then click Function I.
- 2 In the Settings window for Function, locate the Coloring and Style section.
- **3** From the **Width** list, choose **3**.



GLOBAL DEFINITIONS

Smoothed Heaviside Function

- I In the Home toolbar, click f(X) Functions and choose Global>Step.
- 2 In the Settings window for Step, type Smoothed Heaviside Function in the Label text field.
- 3 Click to expand the Smoothing section. In the Size of transition zone text field, type 1.
- 4 Click Plot.

MATERIALS

Next, add the material properties for the subsurface and the fluid inside the pipes. The thermal and hydrodynamic properties for common cooling fluids are similar to the water properties. Use water from the built-in material library as the fluid inside the pipes.

ADD MATERIAL

- I In the Home toolbar, click Radd Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Water, liquid.

- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click **4** Add Material to close the Add Material window.

MATERIALS

Water, liquid (mat I)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Geometric entity level list, choose Edge.
- 3 From the Selection list, choose Pipes.

Soil

- I In the Model Builder window, right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Soil in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Selection list, choose Ground.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Thermal conductivity	k_iso ; kii = k_iso, kij = 0	k_soil	W/(m·K)	Basic
Density	rho	1742	kg/m³	Basic
Heat capacity at constant pressure	Ср	1175	J/(kg·K)	Basic

Set up the Heat Transfer in Solids interface. Set the initial conditions to the depth dependent temperature T_0 which you defined as a function before.

HEAT TRANSFER IN SOLIDS (HT)

Initial Values 1

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Solids (ht) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the T text field, type TO(z).

The surface temperature, also defined as a function T_z0, varies in time.

Temperature I

- I In the Physics toolbar, click **Boundaries** and choose **Temperature**.
- 2 Select Boundary 4 only.

- 3 In the Settings window for Temperature, locate the Temperature section.
- **4** In the T_0 text field, type $T_z0(t+month[a]/12)$.

Heat Flux I

- I In the Physics toolbar, click Boundaries and choose Heat Flux.
- 2 Select Boundary 3 only.
- 3 In the Settings window for Heat Flux, locate the Heat Flux section.
- **4** In the q_0 text field, type -ht.k_iso*Tz_depth.

HEAT TRANSFER IN PIPES (HTP)

- I In the Model Builder window, under Component I (compl) click Heat Transfer in Pipes (htp).
- 2 In the Settings window for Heat Transfer in Pipes, locate the Edge Selection section.
- 3 From the Selection list, choose Pipes.

Heat Transfer I

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Pipes (htp) click Heat Transfer I.
- 2 In the Settings window for Heat Transfer, locate the Heat Convection and Conduction section.
- 3 In the u text field, type flowrate pipe*(1/10+heater state smoothed*9/10)/ htp.A.

Pipe Properties 1

- I In the Model Builder window, click Pipe Properties I.
- 2 In the Settings window for Pipe Properties, locate the Pipe Shape section.
- 3 From the list, choose Circular.
- **4** In the d_i text field, type d_pipe.

DEFINITIONS

Use a nonlocal integration coupling for evaluating the outlet temperature. Then the inlet temperature for the pipes can be evaluated according to Equation 1.

Integration I (intobl)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.

4 Select Point 11 only.

Integration 2 (intob2)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 7 only.

Variables 1

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Description
heater_state _smoothed	<pre>if(heater_state,1,step1((mod(t+ dt/2,1[d])-dt)/dt))*if(t_stop> 0,1-step1((t-(t_stop+dt/2))/ dt),1)</pre>	Smoothed heater state
T_out	intop1(T2)	Water temperature at pipe outlet
T_in	<pre>nojac(T_out-power* heater_state_smoothed/ (intop1(htp.rho)* intop1(htp.Cp)*flowrate_pipe))</pre>	Inlet temperature for pipes

HEAT TRANSFER IN PIPES (HTP)

Temperature I

- I In the Model Builder window, under Component I (compl)>Heat Transfer in Pipes (htp) click Temperature 1.
- 2 In the Settings window for Temperature, locate the Temperature section.
- **3** In the T_{in} text field, type T_in.

Initial Values 1

- I In the Model Builder window, click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- 3 In the T2 text field, type T0(z).

Heat Outflow I

I In the Physics toolbar, click Points and choose Heat Outflow.

2 Select Point 11 only.

Wall Heat Transfer 1

- I In the Physics toolbar, click **Edges** and choose **Wall Heat Transfer**.
- 2 In the Settings window for Wall Heat Transfer, locate the Edge Selection section.
- 3 From the Selection list, choose Pipes.

Internal Film Resistance 1

In the Physics toolbar, click 💂 Attributes and choose Internal Film Resistance.

Wall Heat Transfer 1

In the Model Builder window, click Wall Heat Transfer I.

Wall Layer 1

- I In the Physics toolbar, click 🖳 Attributes and choose Wall Layer.
- 2 In the Settings window for Wall Layer, locate the Specification section.
- **3** From the *k* list, choose **User defined**.
- 4 In the text field, type 400.
- **5** From the Δw list, choose **User defined**.
- 6 In the text field, type 3.25[mm].

MULTIPHYSICS

Pipe Wall Heat Transfer I (pwhtcl)

In the Physics toolbar, click A Multiphysics Couplings and choose Edge> Pipe Wall Heat Transfer.

EVENTS (EV)

In the Model Builder window, under Component I (compl) click Events (ev).

Discrete States 1

- I In the Physics toolbar, click A Global and choose Discrete States.
- 2 In the Settings window for Discrete States, locate the Discrete States section.
- **3** In the table, enter the following settings:

Name	Initial value (u0)
heater_state	0

Indicator States 1

I In the Physics toolbar, click Global and choose Indicator States.

- 2 In the Settings window for Indicator States, locate the Indicator Variables section.
- **3** In the table, enter the following settings:

Name	g(v,vt,vtt,t)	Initial value (u0)
heat_diff	heat_demand-heat_prod	heat_demand

Explicit Event 1

- I In the Physics toolbar, click A Global and choose Explicit Event.
- 2 In the Settings window for Explicit Event, locate the Event Timings section.
- **3** In the t_i text field, type dt.
- 4 In the T text field, type 24[h].
- **5** Locate the **Reinitialization** section. In the table, enter the following settings:

Variable	Expression	
heater_state	1	
t_stop	t	
heat_prod	0	

Implicit Event 1

- I In the Physics toolbar, click A Global and choose Implicit Event.
- 2 In the Settings window for Implicit Event, locate the Event Conditions section.
- 3 In the Condition text field, type heat_diff<0.
- **4** Locate the **Reinitialization** section. In the table, enter the following settings:

Variable	Expression
heater_state	0

GLOBAL ODES AND DAES (GE)

Global Equations I (ODEI)

- I In the Model Builder window, under Component I (compl) > Global ODEs and DAEs (ge) click Global Equations I (ODEI).
- 2 In the Settings window for Global Equations, locate the Global Equations section.
- **3** In the table, enter the following settings:

Name	f(u,ut,utt,t) (I)	Initial value (u_0) (1)	Initial value (u_t0) (1/s)
heat_prod	power*heater_state-heat_prodt	0	0

- 4 Locate the Units section. Click Select Dependent Variable Quantity.
- 5 In the Physical Quantity dialog box, type energy in the text field.
- 6 Click **Filter**.
- 7 In the tree, select General>Energy (J).
- 8 Click OK.
- 9 In the Settings window for Global Equations, locate the Units section.
- 10 Click Select Source Term Quantity.
- II In the Physical Quantity dialog box, type power in the text field.
- 12 Click **Filter**.
- 13 In the tree, select General>Power (W).
- 14 Click OK.

Global Equations 2 (ODE2)

- I In the Global ODEs and DAEs toolbar, click (Global Equations.
- 2 In the Settings window for Global Equations, locate the Global Equations section.
- **3** In the table, enter the following settings:

Name	f(u,ut,utt,t) (1)	Initial value (u_0) (I)	Initial value (u_t0) (I/s)
t_stop	heater_state-t_stopt	0	0

- 4 Locate the Units section. Click Select Dependent Variable Quantity.
- 5 In the Physical Quantity dialog box, type time in the text field.
- 6 Click **Filter**.
- 7 In the tree, select General>Time (s).
- 8 Click OK.

DEFINITIONS

Define the probes to monitor the outlet temperature, heat production, and heater state while solving.

Outlet Temberature

- I In the Definitions toolbar, click Probes and choose Global Variable Probe.
- 2 In the Settings window for Global Variable Probe, type Outlet Temperature in the Label text field.

- 3 Click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Definitions>Variables>T_out -Water temperature at pipe outlet - K.
- 4 Locate the Expression section. From the Table and plot unit list, choose degC.
- 5 Click to expand the Table and Window Settings section. From the Output table list, choose New table.
- 6 From the Plot window list, choose New window.

Heat Production

- I In the Definitions toolbar, click Probes and choose Global Variable Probe.
- 2 In the Settings window for Global Variable Probe, type Heat Production in the Label text field.
- 3 Locate the Expression section. From the Table and plot unit list, choose kWh.
- 4 Locate the Table and Window Settings section. From the Output table list, choose New table.
- 5 From the Plot window list, choose New window.

Heater State

- I In the Definitions toolbar, click Probes and choose Global Variable Probe.
- 2 In the Settings window for Global Variable Probe, type Heater State in the Label text field.
- 3 Click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Definitions>Variables>heater_state_smoothed -Smoothed heater state.
- 4 Locate the Table and Window Settings section. From the Output table list, choose New table.
- 5 From the Plot window list, choose New window.

MESH I

Edge I

- I In the Mesh toolbar, click A More Generators and choose Edge.
- 2 In the Settings window for Edge, locate the Edge Selection section.
- **3** From the **Selection** list, choose **Pipes**.

Size 1

I Right-click **Edge** I and choose **Size**.

- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Points 7 and 11 only.
- 5 Locate the Element Size section. From the Predefined list, choose Extremely fine.
- **6** Click the **Custom** button.
- 7 Locate the Element Size Parameters section.
- 8 Select the Maximum element size check box. In the associated text field, type 0.25.

Size 2

- I In the Model Builder window, right-click Edge I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra fine.
- 4 Click the **Custom** button.
- 5 Locate the Element Size Parameters section.
- **6** Select the **Maximum element size** check box. In the associated text field, type **0.5**.
- 7 Select the Minimum element size check box. In the associated text field, type 0.02.

Free Tetrahedral I

In the Mesh toolbar, click A Free Tetrahedral.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** From the **Predefined** list, choose **Fine**.
- 4 In the Model Builder window, right-click Mesh I and choose Build All.

STUDY I

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.

4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
pattern (Parameter for selecting the pattern)	1 2 3	

Step 1: Time Dependent

- I In the Model Builder window, click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** From the **Time unit** list, choose **d**.
- 4 Click Range.
- 5 In the Range dialog box, type 3[h] in the Step text field.
- 6 In the **Stop** text field, type 2.
- 7 Click Replace.

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node, then click Time-Dependent Solver I.
- 3 In the Settings window for Time-Dependent Solver, click to expand the Time Stepping section.
- 4 Select the Initial step check box. In the associated text field, type 0.1[s]. For better accuracy, force the time-dependent solver to use time steps shorter than 30 min.
- 5 From the Maximum step constraint list, choose Constant.
- 6 In the Maximum step text field, type 30[min].

To solve the problem efficiently, relax the nonlinear setting.

- 7 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Time-Dependent Solver I node, then click Fully Coupled I.
- 8 In the Settings window for Fully Coupled, click to expand the Method and Termination section.
- 9 In the Damping factor text field, type 1.
- 10 From the Jacobian update list, choose Minimal.
- II In the **Study** toolbar, click **Compute**.

RESULTS

Transparency I

- I In the Model Builder window, expand the Results>Temperature (ht) node.
- **2** Right-click **Volume I** and choose **Transparency**.

Line 1

- I In the Model Builder window, expand the Temperature (htp) node, then click Line I.
- 2 In the Settings window for Line, locate the Expression section.
- 3 From the Unit list, choose degC.
- 4 In the Temperature (htp) toolbar, click **Plot**.

Surface I

In the Model Builder window, right-click Temperature (pwhtcl) and choose Surface.

Slice 1

In the Model Builder window, right-click Slice I and choose Disable.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose degC.
- 4 Click to expand the Inherit Style section. From the Plot list, choose Line 1.

Line 1

- I In the Model Builder window, click Line I.
- 2 In the Settings window for Line, locate the Expression section.
- 3 From the Unit list, choose degC.
- 4 Locate the Coloring and Style section. In the Radius scale factor text field, type 5.
- 5 In the Temperature (pwhtcl) toolbar, click Plot.

Outlet Temperature

- I In the Model Builder window, under Results click Probe Plot Group 3.
- 2 In the Settings window for ID Plot Group, type Outlet Temperature in the Label text field.

This plot group corresponds to that of Figure 3.

3 In the Outlet Temperature toolbar, click Plot.

Heat Production

- I In the Model Builder window, under Results click Probe Plot Group 4.
- 2 In the Settings window for ID Plot Group, type Heat Production in the Label text field.
- 3 Locate the Plot Settings section.
- **4** Select the **y-axis label** check box. In the associated text field, type **Heat** Production (kWh).
- 5 In the Heat Production toolbar, click Plot.

Heater State

- I In the Model Builder window, under Results click Probe Plot Group 5.
- 2 In the Settings window for ID Plot Group, type Heater State in the Label text field.
- 3 Locate the Plot Settings section.
- 4 Select the y-axis label check box. In the associated text field, type Heater State.
- 5 In the Heater State toolbar, click Plot.