

Compression of an Elastoplastic Pipe

In offshore applications, it is sometimes necessary to quickly seal a pipe as part of the prevention of a blowout. This example shows a simulation in which a circular pipe is squeezed by a tool. The main target of the analysis is to find the remaining cross-section area through which a fluid can pass.

The tutorial serves as an example of an analysis involving very large plastic strains and contact.

Model Definition

The pipe has an external radius, R_0 , of 200 mm and a wall thickness of 25 mm. The pipe is compressed between the two sides of a tool that can be considered as rigid. The geometry is shown in Figure 1. The original position of the tool is 0.1 mm from the outer pipe wall. During the compression of the pipe, the width of the tool is decreased until the maximum available force, 6 MN, is reached. The tool is then retracted, while the pipe expands as an effect of elastic springback. Due to the symmetries, only one quarter of the geometry needs to be modeled. The problem is considered as 2D with the plane strain assumption.

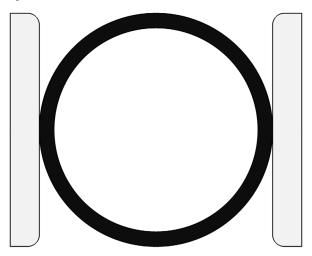


Figure 1: The geometry of the pipe and tool.

The pipe is modeled using an elastoplastic material model and is assumed to be made of stainless steel with the following properties:

TABLE I: MATERIAL DATA.

PROPERTY	VALUE
Young's modulus	195 GPa
Poisson's ratio	0.3
Yield stress	250 MPa
Ultimate tensile stress	616 MPa
Ultimate strain	0.52

The hardening curve is available as a text file containing pairs of data (plastic strain, stress), which can be imported as a function. The function is shown in Figure 2 below. This nonlinear hardening function $\sigma_h(\epsilon_{pe})$ is defined in the Materials node by an interpolation function. The stress is measured as true (Cauchy) stress, and the strain is measured as true (logarithmic) strain. The data can thus be used directly as input to COMSOL when large strain plasticity is used. Note that if the strain is above the ultimate strain, the curve is implicitly flat, so that deformation continues under constant stress.

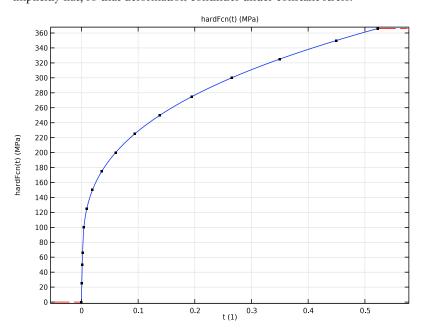


Figure 2: The hardening curve.

In order to be able to assess the sensitivity to the material data, a multiplier to the hardening curve is introduced in the model, although it has the value 1 throughout this analysis.

Results and Discussion

This example exhibits extremely large plastic strains. The deformation and stress state at the maximum compression are shown in Figure 3. The maximum stress displayed is above the ultimate tensile stress (616 MPa). This is caused by the extrapolation of the results from the integration points inside the elements, where the constitutive law is exactly fulfilled.

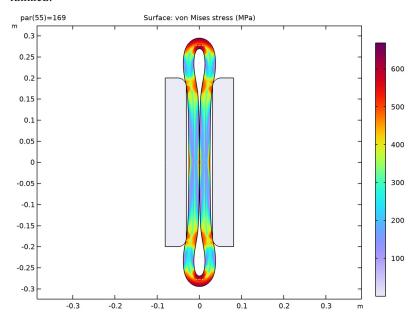


Figure 3: Distribution of von Mises stress at maximum compression.

The distribution of the equivalent plastic strain is shown in Figure 4 and Figure 5. As can be seen, the peak value above 1 is far above the ultimate strain (0.52). The majority of values above the ultimate strain are, however, located on the inside of the pipe, where the strain state is mainly in compression. At the outer edge of the pipe, the plastic strain approximately also exceeds the ultimate strain, but not to the same extent. There is thus a risk that cracks could start forming. The values of ultimate stress and strain are related to the specimen used for the testing (usually a cylindrical bar) and cannot directly be transferred to general multiaxial conditions.

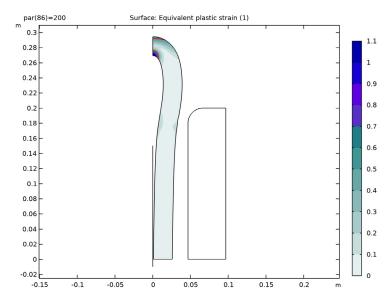


Figure 4: Equivalent plastic strain at the end of the process.

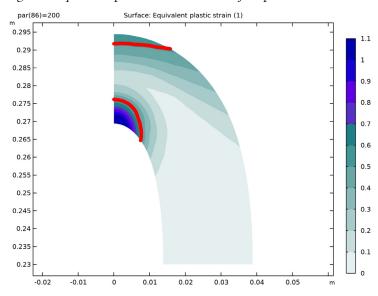


Figure 5: Equivalent plastic strain at the end of the process, detail. The red contour indicates the ultimate strain (0.52).

The final state after the retraction of the compression tool is shown in Figure 6. There is some reversed yielding during the unloading process. The springback effect is very small.

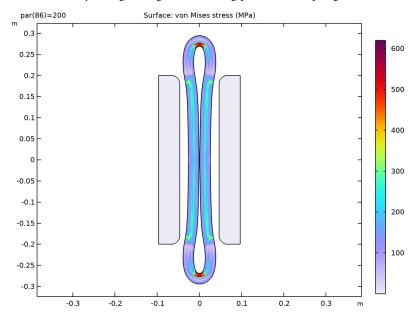


Figure 6: Deformed shape and residual stresses at the end of the process.

The load used to compress the pipe is computed from the reaction force on the tool, and it is shown in Figure 7. When the inside of the pipe makes contact with itself, the force rises steeply.

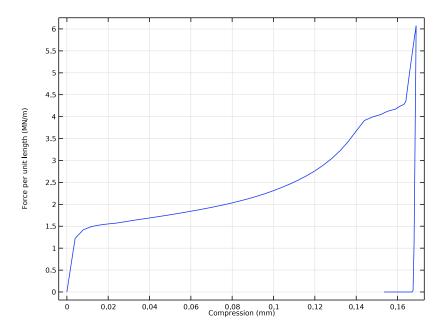


Figure 7: Applied force as function of the compression.

The change in the cross section area during the simulation is shown in Figure 8. The original area is 96211 mm². At the maximum compression, it is reduced to 4831 mm², and in the final state it is 6031 mm². Thus, the area increases by about 25% due to elastic springback. Still, the final cross section area is only 6% of the original. Due to the change in shape, the flow will be reduced even more, since the wall perimeter is essentially unchanged. The resistance to the flow is largest near the walls.

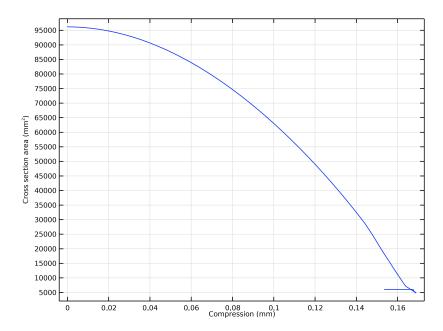


Figure 8: Development of the cross section area as function of compression.

Notes About the COMSOL Implementation

In order to capture when the maximum force from the indenter is reached, a state variable is used. The state variable is updated after each parameter step, and has an update expression that stores the parameter value when the maximum attainable force is reached.

Since symmetry is used, the possible self-contact inside the pipe is modeled as contact against the symmetry plane.

Application Library path: Nonlinear_Structural_Materials_Module/ Plasticity/compressed_elastoplastic_pipe

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click

 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description	
Ro	200[mm]	0.2 m	Outer radius	
thic	25[mm]	0.025 m	Pipe wall thickness	
Sy	250[MPa]	2.5E8 Pa	Yield stress	
hfact	1	I	Hardening curve multiplier	
maxLoad	6[MN]	6E6 N	The maximum load from the tool	
par	0	0	Solution parameter	

GEOMETRY I

Circle: Pipe

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, type Circle: Pipe in the Label text field.
- 3 Locate the Size and Shape section. In the Radius text field, type Ro.
- 4 In the Sector angle text field, type 90.

5 Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	thic

Delete Entities I (del1)

- I In the Model Builder window, right-click Geometry I and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Geometric entity level list, choose Domain.
- 4 On the object c1, select Domain 1 only.
- 5 Click Pauld Selected.

Rectangle: Tool

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, type Rectangle: Tool in the Label text field.
- 3 Locate the Size and Shape section. In the Width text field, type 0.05.
- 4 In the Height text field, type Ro.
- **5** Locate the **Position** section. In the **x** text field, type Ro+0.0001.

Fillet I (fill)

- I In the **Geometry** toolbar, click **Fillet**.
- 2 On the object r1, select Point 4 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type Ro/10.

Polygon: Symmetry Contact Plane

- I In the Geometry toolbar, click / Polygon.
- 2 In the Settings window for Polygon, type Polygon: Symmetry Contact Plane in the **Label** text field.
- 3 Locate the Object Type section. From the Type list, choose Open curve.
- **4** Locate the **Coordinates** section. In the table, enter the following settings:

x (m)	y (m)	
0	0.15	
0	-0.01	

5 Click **Pauld Selected**.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 In the Geometry toolbar, click **Build All**.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

DEFINITIONS

Contact Pair I (b1)

- I In the Definitions toolbar, click Pairs and choose Contact Pair.
- 2 Select Boundaries 6 and 10 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.
- **4** Click to select the **Activate Selection** toggle button.
- **5** Select Boundary 5 only.

Contact Pair 2 (p2)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 Select Boundary 1 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.
- **4** Click to select the **Activate Selection** toggle button.
- **5** Select Boundary 4 only.

SOLID MECHANICS (SOLID)

Linear Elastic Material I

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.

Plasticity 1

- I In the Physics toolbar, click ___ Attributes and choose Plasticity.
- 2 Select Domain 1 only.
- 3 In the Settings window for Plasticity, locate the Plasticity Model section.
- 4 Find the Isotropic hardening model subsection. From the list, choose Hardening function.

MATERIALS

Material I (mat1)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	195[GPa]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.3	I	Young's modulus and Poisson's ratio
Density	rho	8000	kg/m³	Basic
Initial yield stress	sigmags	Sy	Pa	Elastoplastic material model

Add the hardening curve for the elastoplastic material.

- 4 In the Model Builder window, expand the Material I (mat I) node, then click Elastoplastic material model (ElastoplasticModel).
- 5 In the Settings window for Elastoplastic Material Model, locate the Model Inputs section.
- 6 Click + Select Quantity.
- 7 In the Physical Quantity dialog box, type plastic strain in the text field.
- 8 Click **Filter**.
- 9 In the tree, select Solid Mechanics>Equivalent plastic strain (1).
- IO Click OK.

Interpolation I (int I)

- I Right-click Component I (compl)>Materials>Material I (matl)> Elastoplastic material model (ElastoplasticModel) and choose Functions>Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 Click **Load from File**.
- **4** Browse to the model's Application Libraries folder and double-click the file compressed_elastoplastic_pipe_stress_strain.txt.
- 5 In the Function name text field, type hardFcn.
- 6 Locate the Interpolation and Extrapolation section. From the Interpolation list, choose Piecewise cubic.

7 Locate the **Units** section. In the **Argument** table, enter the following settings:

Argument	Unit
t	1

8 In the **Function** table, enter the following settings:

Function	Unit
hardFcn	MPa

9 Click Plot.

Material I (mat I)

- I In the Model Builder window, under Component I (compl)>Materials click Material I (mat I).
- 2 In the Settings window for Material, locate the Material Contents section.
- 3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Hardening function	sigmagh	hardFcn(epe)* hfact	Pa	Elastoplastic material model

Add a state variable to store the parameter value when the maximum load is reached.

GLOBAL DEFINITIONS

- I Click the **Show More Options** button in the **Model Builder** toolbar.
- 2 In the Show More Options dialog box, select General>Variable Utilities in the tree.
- 3 In the tree, select the check box for the node General>Variable Utilities.
- 4 Click OK.

State Variables I (state I)

- I In the Home toolbar, click a Variable Utilities and choose Global>State Variables.
- 2 In the Settings window for State Variables, locate the State Components section.
- **3** In the table, enter the following settings:

State	Initial value	Update expression	Description
peakParam 0		<pre>if(peakParam>0, peakParam,</pre>	Parameter value at max compression
		if(comp1.reacF>	
		maxLoad,par,0))	

4 From the Update list, choose At end of step.

Add variables computing the reaction force on the tool and the current pipe cross section.

DEFINITIONS

Integration | (intob|)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, type ReacInt in the Operator name text field.
- **3** Select Domain 2 only.
- 4 Locate the Advanced section. From the Method list, choose Summation over nodes.

Integration 2 (intob2)

- I In the Definitions toolbar, click // Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, type AreaInt in the Operator name text field.
- 3 Locate the Source Selection section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 4 only.

Variables 1

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
reacF	-2*ReacInt(solid.RFx)	N	Applied force from tool
area	AreaInt(-x*solid.nx)*4	m²	Current cross section area for flow
disp	<pre>if(peakParam,peakParam- (par-peakParam)/2, par)[mm]</pre>		Compression function

SOLID MECHANICS (SOLID)

Symmetry I

- I In the Physics toolbar, click Boundaries and choose Symmetry.
- **2** Select Boundaries 2 and 3 only.

Prescribed Displacement: Compression

- In the Physics toolbar, click **Domains** and choose **Prescribed Displacement**.
- 2 In the Settings window for Prescribed Displacement, type Prescribed Displacement: Compression in the Label text field.
- **3** Select Domain 2 only.
- 4 Locate the Prescribed Displacement section. From the Displacement in x direction list, choose Prescribed.
- 5 From the Displacement in y direction list, choose Prescribed.
- **6** In the u_{0x} text field, type -disp.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Sequence Type section.
- **3** From the list, choose **User-controlled mesh**.

Free Triangular 1

- I In the Model Builder window, under Component I (compl)>Mesh I click Free Triangular I.
- 2 In the Settings window for Free Triangular, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domain 2 only.

Distribution I

- I Right-click Free Triangular I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Boundary Selection section.
- 3 From the Selection list, choose All boundaries.
 - A minimal resolution is needed for the tool, since the whole domain is under displacement control. On the curved boundary, however, a fine resolution is needed.
- 4 Locate the Distribution section. In the Number of elements text field, type 1.

Distribution 2

- I Right-click Free Triangular I and choose Distribution.
- 2 Select Boundary 10 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 30.

Mapped I

In the Mesh toolbar, click Mapped.

Distribution 1

- I Right-click Mapped I and choose Distribution.
- **2** Select Boundaries 4 and 5 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 80.

Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- 2 Select Boundaries 2 and 3 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 8.
- 6 In the Element ratio text field, type 2.
- **7** Select the **Symmetric distribution** check box.

The symmetry boundary must also be meshed because of the contact, even though there is no physics attached to it.

Edge 1

- I In the Mesh toolbar, click A More Generators and choose Edge.
- 2 Select Boundary 1 only.

Distribution 1

- I Right-click **Edge I** and choose **Distribution**.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 In the Number of elements text field, type 1.
- 4 Click Build All.

STUDY I

Steb 1: Stationary

Set up an auxiliary continuation sweep for the parameter par. We do not know exactly how many parameter steps that are needed, but the last ones will be cheap to compute, since the tool is no longer in contact with the pipe.

I In the Model Builder window, under Study I click Step I: Stationary.

- 2 In the Settings window for Stationary, click to expand the Study Extensions section.
- 3 Select the Auxiliary sweep check box.
- 4 Click + Add.
- **5** In the table, enter the following settings:

Parameter name	Parameter value list
par (Solution parameter)	range(0,4,152) range(154,1,200)

- 6 Click to expand the Results While Solving section. Select the Plot check box.
- 7 In the Study toolbar, click $\underset{=0}{\overset{\cup}{}}$ Get Initial Value.

ADD PREDEFINED PLOT

- I In the Home toolbar, click Add Predefined Plot to open the Add Predefined Plot window.
- 2 Go to the Add Predefined Plot window.
- 3 In the tree, select Study I/Solution I (soll)>Solid Mechanics> Equivalent Plastic Strain (solid) and Study I/Solution I (sol1)>Solid Mechanics> Contact Forces (solid).
- 4 Click Add Plot in the window toolbar.
- 5 In the Home toolbar, click Add Predefined Plot to close the Add Predefined Plot window.

STUDY I

Solution I (soll)

- I In the Model Builder window, expand the Study I>Solver Configurations node.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Study I>Solver Configurations> Solution I (soll)>Stationary Solver I node, then click Parametric I.
- 4 In the Settings window for Parametric, click to expand the Continuation section.
- **5** From the **Predictor** list, choose **Linear**.
- **6** Select the **Tuning of step size** check box.
- 7 In the **Initial step size** text field, type 1.
- 8 In the Maximum step size text field, type 1.

Mirror the solution twice to get a full view of the pipe.

RESULTS

Mirror 2D I

- I In the Results toolbar, click More Datasets and choose Mirror 2D.
- 2 In the Settings window for Mirror 2D, click to expand the Advanced section.
- 3 Select the Remove elements on the symmetry axis check box.

Mirror 2D 2

In the **Results** toolbar, click **More Datasets** and choose **Mirror 2D**.

Mirror 2D 2

- I In the Model Builder window, click Mirror 2D 2.
- 2 In the Settings window for Mirror 2D, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 1.
- 4 Locate the Axis Data section. In row Point 2, set x to 1 and y to 0.
- 5 Locate the Advanced section. Select the Remove elements on the symmetry axis check box.

Stress (solid)

- I In the Model Builder window, under Results click Stress (solid).
- 2 In the Settings window for 2D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 2.
- **4** Click the **Zoom Extents** button in the **Graphics** toolbar.

Surface I

- I In the Model Builder window, expand the Stress (solid) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose MPa.

STUDY I

I In the **Home** toolbar, click **Compute**.

Check the remaining cross section area.

RESULTS

Remaining Cross-Section Area

I In the Results toolbar, click Evaluation Group.

- 2 In the Settings window for Evaluation Group, type Remaining Cross-Section Area in the Label text field.
- 3 Locate the Data section. From the Parameter selection (par) list, choose Last.

Global Evaluation 1

- I Right-click Remaining Cross-Section Area and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Expressions section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
area	mm^2	

4 In the Remaining Cross-Section Area toolbar, click **= Evaluate**.

Stress (solid)

- I In the Model Builder window, under Results click Stress (solid).
- 2 In the Stress (solid) toolbar, click Plot. Plot the stress at the maximum compression. This gives Figure 5.
- 3 In the Settings window for 2D Plot Group, locate the Data section.
- 4 From the Parameter value (par) list, choose 169.
- 5 In the Stress (solid) toolbar, click Plot.

Create an animation of the compression process.

Animation I

In the Stress (solid) toolbar, click Animation and choose Player.

Equivalent Plastic Strain (solid)

- I In the Model Builder window, under Results click Equivalent Plastic Strain (solid).
- 2 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 3 From the Frame list, choose Spatial (x, y, z).
- 4 In the Equivalent Plastic Strain (solid) toolbar, click Plot.

Surface I

- I In the Model Builder window, expand the Equivalent Plastic Strain (solid) node, then click Surface 1.
- 2 In the Settings window for Surface, click to expand the Range section.
- 3 Select the Manual color range check box.
- **4** In the **Maximum** text field, type 1.1.

Deformation I

- I Right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box. In the associated text field, type 1.

Contour I

- I In the Model Builder window, right-click Equivalent Plastic Strain (solid) and choose Contour.
- 2 In the Settings window for Contour, locate the Expression section.
- **3** In the **Expression** text field, type solid.epeGp.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- **5** Locate the **Levels** section. In the **Total levels** text field, type 1.
- **6** From the **Entry method** list, choose **Levels**.
- 7 In the Levels text field, type 0.52.
- 8 Locate the Coloring and Style section. From the Contour type list, choose Tube.
- **9** Select the **Radius scale factor** check box.
- 10 In the Tube radius expression text field, type 5e-4.
- II From the Coloring list, choose Uniform.
- 12 Clear the Color legend check box.
- 13 Click to expand the Inherit Style section. From the Plot list, choose Surface 1.
- 14 Clear the Color check box.

Deformation I

- I Right-click Contour I and choose Deformation.
- 2 In the Equivalent Plastic Strain (solid) toolbar, click **Plot**.
- 3 Click the **Zoom Extents** button in the **Graphics** toolbar.

Create a graph of the applied force as function of the compression.

Compression Force

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Compression Force in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 4 Locate the Plot Settings section.

- 5 Select the y-axis label check box. In the associated text field, type Force per unit length (MN/m).
- 6 Select the x-axis label check box. In the associated text field, type Compression (mm).
- 7 Locate the **Legend** section. Clear the **Show legends** check box.

Global I

- I Right-click Compression Force and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Definitions> Variables>reacF - Applied force from tool - N.
- **3** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
reacF	MN	Applied force from tool

- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **5** In the **Expression** text field, type disp.
- **6** In the Compression Force toolbar, click **Plot**.

Compression Force

In the Model Builder window, right-click Compression Force and choose Duplicate.

Flow Area

- I In the Model Builder window, under Results click Compression Force I.
- 2 In the Settings window for ID Plot Group, type Flow Area in the Label text field.
- 3 Locate the Plot Settings section. In the y-axis label text field, type Cross section area (mm²).

Global I

- I In the Model Builder window, expand the Flow Area node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
area	mm^2	Current cross section area for flow

4 In the Flow Area toolbar, click Plot.