

Fresnel Equations

A plane electromagnetic wave propagating through free space is incident at an angle upon an infinite dielectric medium. This model computes the reflection and transmission coefficients and compares the results to the Fresnel equations.

Model Definition

A plane wave propagating through free space (n = 1) as shown in Figure 1 is incident upon an infinite dielectric medium (n = 1.5) and is partially reflected and partially transmitted. If the electric field is *p-polarized* — that is, if the electric field vector is in the same plane as the Poynting vector and the surface normal — then there are no reflections at an incident angle of roughly 56°, known as the Brewster angle.

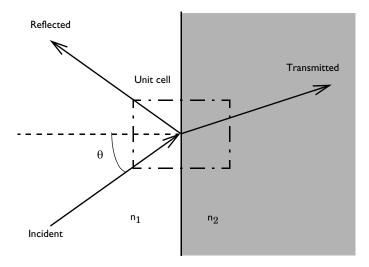


Figure 1: A plane wave propagating through free space incident upon an infinite dielectric medium.

Although, by assumption, space extends to infinity in all directions, it is sufficient to model a small unit cell, as shown in Figure 1; a Floquet-periodic boundary condition applies on the top and bottom unit-cell boundaries because the solution is periodic along the interface. This model uses a 3D unit cell and applies also a periodic boundary condition in the out-of-plane direction. However, this periodic boundary condition acts like a continuity condition. The angle of incidence ranges between 0–90° for both polarizations. For comparison, Ref. 1 and Ref. 2 provide analytic expressions for the reflectance and transmittance¹. Reflection and transmission coefficients for s-polarization and p-polarization are defined respectively as

$$\begin{split} r_s &= \frac{n_1 \cos \theta_{\text{incident}} - n_2 \cos \theta_{\text{transmitted}}}{n_1 \cos \theta_{\text{incident}} + n_2 \cos \theta_{\text{transmitted}}} \\ t_s &= \frac{2n_1 \cos \theta_{\text{incident}}}{n_1 \cos \theta_{\text{incident}} + n_2 \cos \theta_{\text{transmitted}}} \\ r_p &= \frac{n_2 \cos \theta_{\text{incident}} - n_1 \cos \theta_{\text{transmitted}}}{n_1 \cos \theta_{\text{transmitted}} + n_2 \cos \theta_{\text{incident}}} \\ t_p &= \frac{2n_1 \cos \theta_{\text{incident}}}{n_1 \cos \theta_{\text{transmitted}} + n_2 \cos \theta_{\text{incident}}} \end{split}$$

Reflectance and transmittance are defined as

$$R = |r|^{2}$$

$$T = \frac{n_{2}\cos\theta_{\text{transmitted}}}{n_{1}\cos\theta_{\text{incident}}}|t|^{2}$$

The Brewster angle at which $r_p = 0$ is defined as

$$\theta_B = \operatorname{atan} \frac{n_2}{n_1}$$

In the first part of the simulation, the Electromagnetic Waves, Frequency Domain interface will be used. The second part instead uses the Electromagnetic Waves, Beam Envelopes interface. Using the Electromagnetic Waves, Beam Envelopes interface, the model is simplified, replacing the glass substrate with an Impedance boundary condition. Furthermore, as the wave vectors for the incident and reflected waves are known, the simulation can be performed with a very coarse mesh.

^{1.} Note that depending on the sign convention for what is defined as a positive polarization for the reflected wave with in-plane (p-polarization), the sign for the reflection coefficient r_p can differ for different authors. However, the total field solution will always be the same.

Figure 2 is a combined plot of the y component of the electric-field distribution and the power flow visualized as an arrow plot for the TE case.

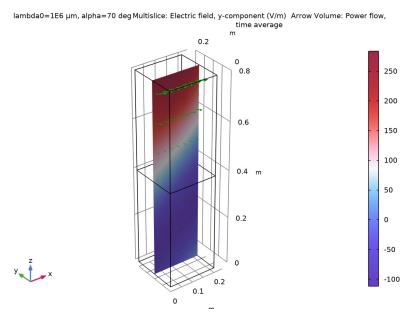


Figure 2: Electric field, E_y (slice) and power flow (arrows) for TE incidence at 70° inside the unit cell.

For the TM case, Figure 3 visualizes the *y* component of the magnetic-field distribution instead, again in combination with the power flow.

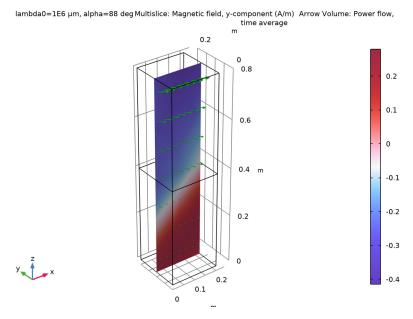


Figure 3: Magnetic field, H_y (slice) and power flow (arrows) for TM incidence at 70° inside the unit cell.

Note that the sum of reflectance and transmittance in Figure 4 and Figure 5 equals 1, showing conservation of power. Figure 5 also shows that the reflectance around 56° — the Brewster angle in the TM case — is close to zero.

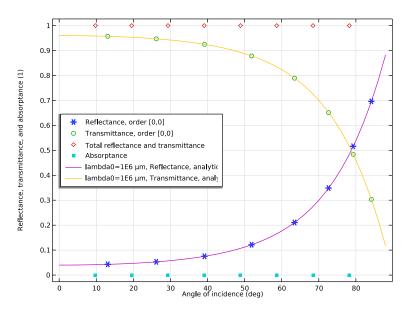


Figure 4: The reflectance and transmittance for TE incidence agree well with the analytic solutions.

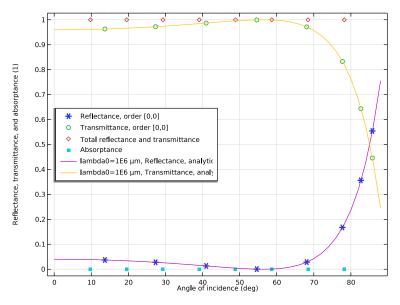


Figure 5: The reflectance and transmittance for TM incidence agree well with the analytic solutions. The Brewster angle is also observed at the expected location.

Figure 6 shows a TE field plot when the Electromagnetic Waves, Beam Envelopes interface is used. Here, the simulation is only performed for the air domain. The bottom glass domain is represented by an Impedance boundary condition, implemented for nonnormal propagation in the exterior (glass) material. This particular implementation of the Impedance boundary condition for the Electromagnetic Waves, Beam Envelopes interface is useful for truncating the simulation domain at an interface between two dielectric materials.

Since the wave vectors for the solution are known, the mesh consists of only one mesh element in the z direction.

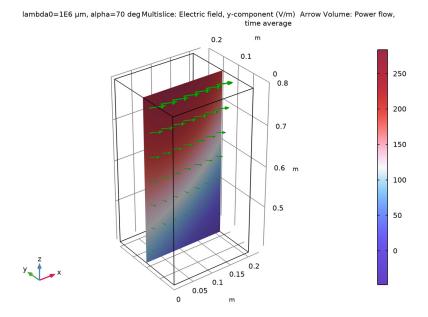


Figure 6: Electric field, E_{γ} (slice) and power flow (arrows) for TE incidence at 70° inside the unit cell when the Electromagnetic Waves, Beam Envelopes interface is used.

Figure 7 shows that the TE reflectance results for the Electromagnetic Waves, Beam Envelopes interface agree well with the simulation using the Electromagnetic Waves, Frequency Domain interface and the analytical results.

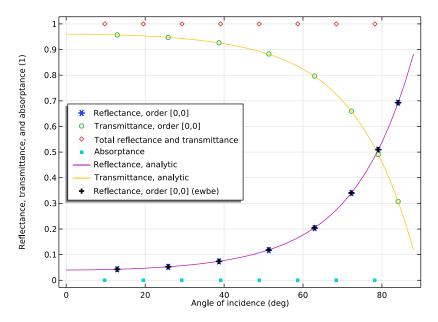


Figure 7: Same plot as Figure 5, but with the TE reflectance curve from the Electromagnetic Waves, Beam Envelopes interface also included.

References

- 1. J.D. Jackson, Classical Electrodynamics, 3rd Ed., Wiley, 1999.
- 2. B.E.A. Saleh and M.C. Teich, Fundamentals of Photonics, Wiley, 1991.

Application Library path: Wave_Optics_Module/Verification_Examples/ fresnel equations

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 1 3D.
- 2 In the Select Physics tree, select Optics>Wave Optics>Electromagnetic Waves, Frequency Domain (ewfd).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Wavelength Domain.
- 6 Click **Done**.

GLOBAL DEFINITIONS

Define some parameters that are useful when setting up the geometry and the study.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
n_air	1	I	Refractive index,
n_slab	1.5	1.5	Refractive index, slab
lda0	1[m]	l m	Wavelength
alpha	70[deg]	1.2217 rad	Angle of incidence
beta	<pre>asin(n_air*sin(alpha)/ n_slab)</pre>	0.67701 rad	Refraction angle
alpha_brewster	atan(n_slab/n_air)	0.98279 rad	Brewster angle, TM only
r_s	<pre>(n_air*cos(alpha)- n_slab*cos(beta))/ (n_air*cos(alpha)+ n_slab*cos(beta))</pre>	-0.54735	Reflection coefficient, TE
r_p	<pre>(n_slab*cos(alpha) - n_air*cos(beta)) / (n_air*cos(beta) + n_slab*cos(alpha))</pre>	-0.20613	Reflection coefficient, TM
t_s	<pre>(2*n_air*cos(alpha))/ (n_air*cos(alpha)+ n_slab*cos(beta))</pre>	0.45265	Transmission coefficient, TE
t_p	<pre>(2*n_air*cos(alpha))/ (n_air*cos(beta)+ n_slab*cos(alpha))</pre>	0.52925	Transmission coefficient, TM

The angle of incidence is updated while running the parametric sweep. The refraction (transmitted) angle is defined by Snell's law with the updated angle of incidence. The Brewster angle exists only for TM incidence, p-polarization (polarization is in the plane of incidence).

GEOMETRY I

First, create a block composed of two domains. Use layers to split the block.

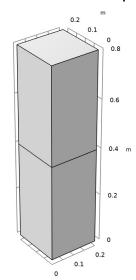
Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- **3** In the **Width** text field, type **0.2**.

- 4 In the **Depth** text field, type 0.2.
- 5 In the Height text field, type 0.8.
- **6** Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	0.4

- 7 Click Build All Objects.
- **8** Click the **Zoom Extents** button in the **Graphics** toolbar.





Choose wireframe rendering to get a better view of each boundary.

9 Click the Wireframe Rendering button in the Graphics toolbar.

MATERIALS

Now set up the material properties based on refractive index. The top half is filled with air.

Air

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Air in the Label text field.
- **3** Select Domain 2 only.

4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Refractive index, real part	n_iso ; nii = n_iso, nij = 0	n_air	I	Refractive index
Refractive index, imaginary part	ki_iso ; kiii = ki_iso, kiij = 0	0	I	Refractive index

Glass

The bottom half is glass.

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Glass in the Label text field.
- 3 Select Domain 1 only.
- **4** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Refractive index, real part	n_iso ; nii = n_iso, nij = 0	n_slab	I	Refractive index
Refractive index, imaginary part	ki_iso ; kiii = ki_iso, kiij = 0	0	1	Refractive index

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD, TE)

Set up the physics based on the direction of propagation and the E-field polarization. First, assume a TE-polarized wave which is equivalent to s-polarization or perpendicular polarization. E_x and E_z are zero while E_y is dominant.

- I In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Frequency Domain (ewfd).
- 2 In the Settings window for Electromagnetic Waves, Frequency Domain, type Electromagnetic Waves, Frequency Domain (ewfd, TE) in the Label text field.

Port I

- I In the Physics toolbar, click **Boundaries** and choose Port.
- **2** Select Boundary 7 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Periodic.

For the first port, wave excitation is **on** by default.

5 Locate the **Port Mode Settings** section. Specify the ${\bf E}_0$ vector as

0	x
1	у
0	z

- **6** Locate the **Automatic Diffraction Order Calculation** section. In the n text field, type n_air.
- 7 Locate the Port Mode Settings section. In the α_1 text field, type alpha.

The maximum frequency in the setting window will be used only when **Compute Diffraction Order** button is clicked to generate **Diffraction Order** features representing higher order modes. In this model, no diffraction is expected from the given geometry, so this setting is ineffective.

Port 2

- I In the Physics toolbar, click **Boundaries** and choose Port.
- 2 Select Boundary 3 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Periodic.
- **5** Locate the **Port Mode Settings** section. Specify the \mathbf{E}_0 vector as

0	x
1	у
0	z

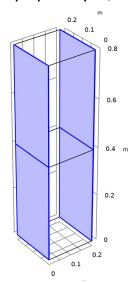
6 Locate the **Automatic Diffraction Order Calculation** section. In the n text field, type n_slab .

The bottom surface is an observation port. The S_{21} -parameter from Port 1 and Port 2 provides the transmission characteristics.

Periodic Condition I

- I In the Physics toolbar, click **Boundaries** and choose Periodic Condition.
- 2 Select Boundaries 1, 4, 10, and 11 only.
- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.

5 From the k-vector for Floquet periodicity list, choose From periodic port.

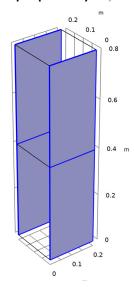




Periodic Condition 2

- I In the Physics toolbar, click **Boundaries** and choose Periodic Condition.
- 2 Select Boundaries 2, 5, 8, and 9 only.
- 3 In the Settings window for Periodic Condition, locate the Periodicity Settings section.
- 4 From the Type of periodicity list, choose Floquet periodicity.

5 From the k-vector for Floquet periodicity list, choose From periodic port.





STUDY I (EWFD, TE)

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study 1 (ewfd, TE) in the Label text field.

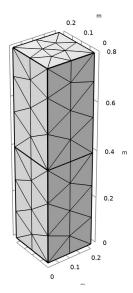
Step 1: Wavelength Domain

- I In the Model Builder window, under Study I (ewfd, TE) click Step I: Wavelength Domain.
- 2 In the Settings window for Wavelength Domain, locate the Study Settings section.
- 3 In the Wavelengths text field, type 1da0.
- 4 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 5 Click + Add.
- **6** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
alpha (Angle of incidence)	range(0,2[deg],88[deg])	deg

MESH I

In the Model Builder window, under Component I (compl) right-click Mesh I and choose **Build All.**





STUDY I (EWFD, TE)

In the **Home** toolbar, click **Compute**.

RESULTS

Electric Field (ewfd, TE)

I In the Settings window for 3D Plot Group, type Electric Field (ewfd, TE) in the Label text field.

The default plot is the E-field norm for the last solution, which corresponds to almost tangential incidence. Replace the expression with E_{ν} , add an arrow plot of the power flow (Poynting vector), and choose a more interesting angle of incidence for the plot.

Multislice 1

- I In the Model Builder window, expand the Electric Field (ewfd, TE) node, then click Multislice 1.
- 2 In the Settings window for Multislice, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain (ewfd, TE)>Electric>Electric field - V/m> ewfd.Ey - Electric field, y-component.

- 3 Locate the Multiplane Data section. Find the X-planes subsection. In the Planes text field, type 0.
- 4 Find the **Z-planes** subsection. In the **Planes** text field, type 0.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Wave>WaveLight in the tree.
- 7 Click OK.

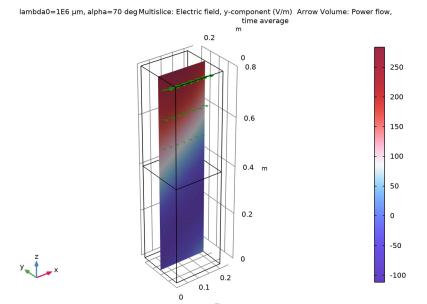
Arrow Volume 1

- I In the Model Builder window, right-click Electric Field (ewfd, TE) and choose Arrow Volume.
- 2 In the Settings window for Arrow Volume, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain (ewfd, TE)>Energy and power>ewfd.Poavx,..., ewfd.Poavz Power flow, time average.
- **3** Locate the **Arrow Positioning** section. Find the **Y grid points** subsection. In the **Points** text field, type 1.
- 4 Locate the Coloring and Style section. From the Color list, choose Green.

Electric Field (ewfd, TE)

- I In the Model Builder window, click Electric Field (ewfd, TE).
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Parameter value (alpha (deg)) list, choose 70.
- 4 In the Electric Field (ewfd, TE) toolbar, click Plot.

5 Click the **Zoom Extents** button in the **Graphics** toolbar.



The plot should look like that in Figure 2.

Reflectance, Transmittance, and Absorptance (ewfd, TE)

A 1D plot with the reflection and transmission versus the angle of incidence is added by default.

- I In the Model Builder window, under Results click Reflectance, Transmittance, and Absorptance (ewfd).
- 2 In the Settings window for ID Plot Group, type Reflectance, Transmittance, and Absorptance (ewfd, TE) in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose None.
- 4 Locate the Plot Settings section. Select the x-axis label check box.
- 5 Locate the Legend section. From the Position list, choose Middle left.

Global I

- I In the Model Builder window, expand the Reflectance, Transmittance, and Absorptance (ewfd, TE) node, then click Global I.
- 2 In the Settings window for Global, click to expand the Coloring and Style section.
- 3 Find the Line style subsection. From the Line list, choose None.

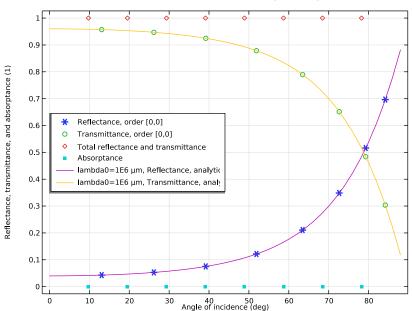
- 4 Find the Line markers subsection. From the Marker list, choose Cycle.
- 5 From the Positioning list, choose Interpolated.

Global 2

- I In the Model Builder window, right-click Reflectance, Transmittance, and Absorptance (ewfd, TE) and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
abs(r_s)^2		Reflectance, analytic
n_slab*cos(beta)/(n_air* cos(alpha))*abs(t_s)^2		Transmittance, analytic

- 4 Locate the x-Axis Data section. From the Unit list, choose °.



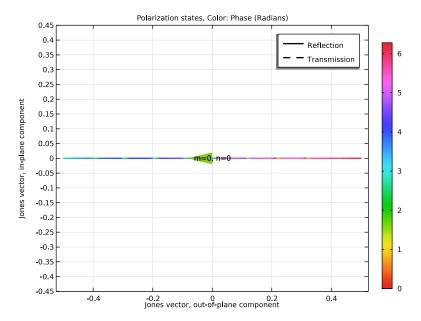
Compare the resulting plots with Figure 4.

Polarization Plot (ewfd, TE)

I In the Model Builder window, under Results click Polarization Plot (ewfd).

- 2 In the Settings window for ID Plot Group, type Polarization Plot (ewfd, TE) in the Label text field.
- 3 In the Polarization Plot (ewfd, TE) toolbar, click Plot.

The polarization plot shows that the field is linearly polarized, with a pure out-of-plane polarization. The out-of-plane component of the Jones vector represents the amplitude of a wave polarized in the y direction, whereas the in-plane component represents the amplitude of a wave with a polarization that is orthogonal to both the out-of-plane direction and the propagation direction, resulting in a polarization in the x-z plane.



ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD, TE) (EWFD)

The following instructions are for the case of a TM-polarized wave (p-polarization or parallel polarization). In this case, E_v is zero while E_x and E_z characterize the wave. In other words, H_y is dominant while H_x and H_z have no effect. Thus, the H-field is perpendicular to the plane of incidence and it is convenient to specify the port mode fields as the H-field.

In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Frequency Domain (ewfd, TE) (ewfd) and choose Copy.

COMPONENT I (COMPI)

In the Model Builder window, right-click Component I (compl) and choose Paste Electromagnetic Waves, Frequency Domain.

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD2, TM)

- I In the Messages from Paste dialog box, click OK.
- 2 In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Frequency Domain (ewfd, TE) I (ewfd2).
- 3 In the Settings window for Electromagnetic Waves, Frequency Domain, type Electromagnetic Waves, Frequency Domain (ewfd2, TM) in the Label text field.

Port I

- I In the Model Builder window, expand the Component I (compl)>Electromagnetic Waves, Frequency Domain (ewfd2, TM) (ewfd2) node, then click Port I.
- 2 In the Settings window for Port, locate the Port Mode Settings section.
- 3 From the Input quantity list, choose Magnetic field.
- **4** Specify the \mathbf{H}_0 vector as

0	x
1	у
0	z

Port 2

- I In the Model Builder window, click Port 2.
- 2 In the Settings window for Port, locate the Port Mode Settings section.
- 3 From the Input quantity list, choose Magnetic field.
- **4** Specify the \mathbf{H}_0 vector as

0	x
1	у
0	z

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Empty Study.

- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2 (EWFD2, TM)

In the Settings window for Study, type Study 2 (ewfd2, TM) in the Label text field.

STUDY I (EWFD, TE)

Step 1: Wavelength Domain

In the Model Builder window, under Study I (ewfd, TE) right-click

Step 1: Wavelength Domain and choose Copy.

STUDY 2 (EWFD2, TM)

In the Model Builder window, right-click Study 2 (ewfd2, TM) and choose Paste Wavelength Domain.

- I In the Model Builder window, under Study 2 (ewfd2, TM) click Step 1: Wavelength Domain.
- 2 In the Settings window for Wavelength Domain, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Electromagnetic Waves, Frequency Domain (ewfd, TE) (ewfd).
- 4 In the Home toolbar, click **Compute**.

RESULTS

Magnetic Field (ewfd2, TM)

In the Settings window for 3D Plot Group, type Magnetic Field (ewfd2, TM) in the Label text field.

Multislice 1

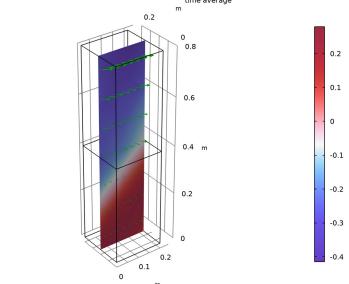
- I In the Model Builder window, expand the Magnetic Field (ewfd2, TM) node, then click Multislice 1.
- 2 In the Settings window for Multislice, locate the Expression section.
- 3 In the Expression text field, type ewfd2.Hy.
- 4 Locate the Multiplane Data section. Find the X-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. In the **Planes** text field, type 0.
- 6 Locate the Coloring and Style section. Click | Change Color Table.

- 7 In the Color Table dialog box, select Wave>WaveLight in the tree.
- 8 Click OK.

Arrow Volume 1

- I In the Model Builder window, right-click Magnetic Field (ewfd2, TM) and choose Arrow Volume.
- 2 In the Settings window for Arrow Volume, locate the Expression section.
- 3 In the X-component text field, type ewfd2. Poavx.
- 4 In the Y-component text field, type ewfd2. Poavy.
- 5 In the **Z-component** text field, type ewfd2.Poavz.
- 6 Locate the Arrow Positioning section. Find the Y grid points subsection. In the Points text field, type 1.
- 7 Locate the Coloring and Style section. From the Color list, choose Green.

lambda0=1E6 µm, alpha=88 deg Multislice: Magnetic field, y-component (A/m) Arrow Volume: Power flow, time average



This reproduces Figure 3.

Reflectance, Transmittance, and Absorptance (ewfd2, TM)

I In the Model Builder window, under Results click Reflectance, Transmittance, and Absorptance (ewfd2).

- 2 In the Settings window for ID Plot Group, type Reflectance, Transmittance, and Absorptance (ewfd2, TM) in the Label text field.
- 3 Locate the Title section. From the Title type list, choose None.
- 4 Locate the Plot Settings section. Select the x-axis label check box.
- 5 Locate the Legend section. From the Position list, choose Middle left.

Global I

- I In the Model Builder window, expand the Reflectance, Transmittance, and Absorptance (ewfd2, TM) node, then click Global 1.
- 2 In the Settings window for Global, locate the Coloring and Style section.
- **3** Find the **Line style** subsection. From the **Line** list, choose **None**.
- 4 Find the Line markers subsection. From the Marker list, choose Cycle.
- **5** From the **Positioning** list, choose **Interpolated**.

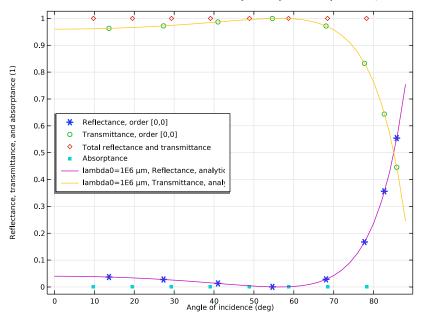
Global 2

- I In the Model Builder window, right-click Reflectance, Transmittance, and Absorptance (ewfd2, TM) and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
abs(r_p)^2		Reflectance, analytic
n_slab*cos(beta)/(n_air* cos(alpha))*abs(t_p)^2		Transmittance, analytic

4 Locate the x-Axis Data section. From the Unit list, choose °.

5 In the Reflectance, Transmittance, and Absorptance (ewfd2, TM) toolbar, click Plot.



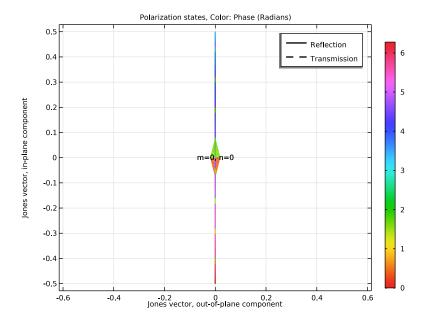
The plot should look like Figure 5. The Brewster angle is observed around 56 degrees, which is close to the analytic value.

Polarization Plot (ewfd2, TM)

- I In the Model Builder window, under Results click Polarization Plot (ewfd2).
- 2 In the Settings window for ID Plot Group, type Polarization Plot (ewfd2, TM) in the Label text field.

3 In the Polarization Plot (ewfd2, TM) toolbar, click Plot.

Also in this case, the polarization plot shows that the field is linearly polarized, in this case with a pure in-plane polarization.



COMPONENT I (COMPI)

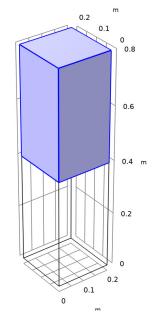
Now, add a simulation using the Electromagnetic Waves, Beam Envelopes interface. In this simulation, the Impedance boundary condition is added to the interface between the air and the glass domain and the simulation is only performed for the air domain. This example demonstrates that the Impedance boundary condition for the Electromagnetic Waves, Beam Envelopes interface can be used for truncating the simulation domain at a boundary between two dielectric material domains.

ADD PHYSICS

- I In the Home toolbar, click Add Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Optics>Wave Optics>Electromagnetic Waves, Beam Envelopes (ewbe).
- 4 Click Add to Component I in the window toolbar.
- 5 In the Home toolbar, click and Physics to close the Add Physics window.

ELECTROMAGNETIC WAVES, BEAM ENVELOPES (EWBE, TE)

- I In the Settings window for Electromagnetic Waves, Beam Envelopes, type Electromagnetic Waves, Beam Envelopes (ewbe, TE) in the Label text field.
- **2** Select Domain 2 only, to only perform the simulation for the air domain.



 ${\bf 3}\;$ Locate the Wave Vectors section. Specify the ${\bf k}_1$ vector as

ewbe.k0*sin(alpha)	х
0	у
-ewbe.k0*cos(alpha)	z

4 Specify the \mathbf{k}_2 vector as

ewbe.k1x	x
ewbe.k1y	у
-ewbe.k1z	z

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD, TE) (EWFD)

Port 1

In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (ewfd, TE) (ewfd) right-click Port I and choose Copy.

ELECTROMAGNETIC WAVES, BEAM ENVELOPES (EWBE, TE) (EWBE)

In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe) and choose Paste Port.

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD, TE) (EWFD)

Periodic Condition 1

In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (ewfd, TE) (ewfd) right-click Periodic Condition I and choose Copy.

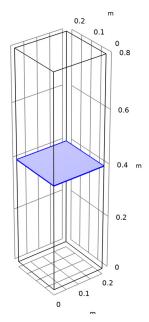
ELECTROMAGNETIC WAVES, BEAM ENVELOPES (EWBE, TE) (EWBE)

- I In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe) and choose Paste Periodic Condition.
- 2 Copy and paste also Periodic Condition 2 from Electromagnetic Waves, Frequency Domain (ewfd, TE) to Electromagnetic Waves, Beam Envelopes (ewbe).
- 3 In the Model Builder window, click Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe).

Impedance Boundary Condition I

In the Physics toolbar, click Boundaries and choose Impedance Boundary Condition.

2 Select Boundary 6 only.



- 3 In the Settings window for Impedance Boundary Condition, locate the Propagation Direction section.
- 4 From the list, choose From wave vector, to make the Impedance Boundary Condition also work for nonnormal propagation in the exterior (glass) material.

MATERIALS

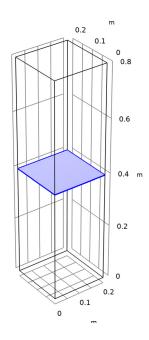
Glass (mat2)

In the Model Builder window, under Component I (compl)>Materials right-click Glass (mat2) and choose Duplicate.

Glass (Boundary)

- I In the Model Builder window, under Component I (compl)>Materials click Glass I (mat3).
- 2 In the Settings window for Material, type Glass (Boundary) in the Label text field.
- 3 Locate the Geometric Entity Selection section. From the Geometric entity level list, choose Boundary.

4 Select Boundary 6 only.





MESH I

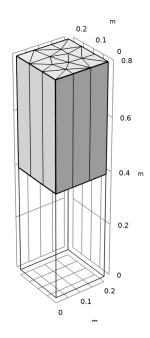
For the Electromagnetic Waves, Beam Envelopes interface a single mesh element is required, as the prescribed wave vectors match the full-wave solution.

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 In the table, clear the Use check box for Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe).

MESH 2

- I In the Mesh toolbar, click Add Mesh and choose Add Mesh.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 In the table, clear the Use check boxes for Electromagnetic Waves, Frequency Domain (ewfd, TE) (ewfd) and Electromagnetic Waves, Frequency Domain (ewfd2, TM) (ewfd2).
- 4 Locate the Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe) section. In the N_T text field, type 1.
- **5** In the N_L text field, type 1.

6 Click Build All.





ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Empty Study.
- 4 Click Add Study in the window toolbar.

STUDY 3 (EWBE, TE)

In the Settings window for Study, type Study 3 (ewbe, TE) in the Label text field.

STUDY 2 (EWFD2, TM)

Step 1: Wavelength Domain

In the Model Builder window, under Study 2 (ewfd2, TM) right-click

Step 1: Wavelength Domain and choose **Copy**.

STUDY 3 (EWBE, TE)

In the Model Builder window, right-click Study 3 (ewbe, TE) and choose Paste Wavelength Domain.

- I In the Model Builder window, under Study 3 (ewbe, TE) click Step 1: Wavelength Domain.
- 2 In the Settings window for Wavelength Domain, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Electromagnetic Waves, Frequency Domain (ewfd2, TM) (ewfd2).
- 4 Click to expand the **Mesh Selection** section. In the table, enter the following settings:

Component	Mesh
Component I	Mesh 2

- 5 In the Home toolbar, click Add Study to close the Add Study window.
- 6 In the Home toolbar, click **Compute**.

RESULTS

Electric Field (ewbe, TE)

- I In the Settings window for 3D Plot Group, type Electric Field (ewbe, TE) in the Label text field.
- 2 Locate the Data section. From the Parameter value (alpha (deg)) list, choose 70.

Electric Field

- I In the Model Builder window, expand the Electric Field (ewbe, TE) node, then click Electric Field.
- 2 In the Settings window for Multislice, locate the Expression section.
- 3 In the Expression text field, type ewbe. Ey.
- 4 Locate the Multiplane Data section. Find the X-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. In the **Planes** text field, type 0.
- 6 Locate the Coloring and Style section. Click | Change Color Table.
- 7 In the Color Table dialog box, select Wave>WaveLight in the tree.
- 8 Click OK.

Arrow Volume 1

In the Model Builder window, under Results>Magnetic Field (ewfd2, TM) right-click Arrow Volume I and choose Copy.

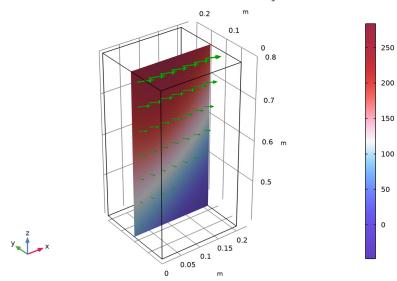
Electric Field (ewbe, TE)

In the Model Builder window, under Results right-click Electric Field (ewbe, TE) and choose Paste Arrow Volume.

Arrow Volume 1

- I In the Model Builder window, click Arrow Volume I.
- 2 In the Settings window for Arrow Volume, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Beam Envelopes (ewbe, TE)>Energy and power>ewbe.Poavx,..., ewbe.Poavz - Power flow, time average.

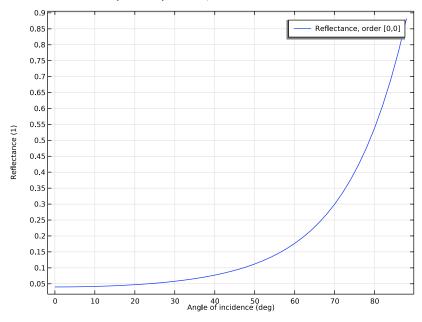
lambda0=1E6 µm, alpha=70 deg Multislice: Electric field, y-component (V/m) Arrow Volume: Power flow,



Reflectance (ewbe, TE)

- I In the Model Builder window, under Results click Reflectance (ewbe).
- 2 In the Settings window for ID Plot Group, type Reflectance (ewbe, TE) in the Label text field.

3 In the Reflectance (ewbe, TE) toolbar, click Plot.



Global I We will now compare this plot to the other TE reflectance plot.

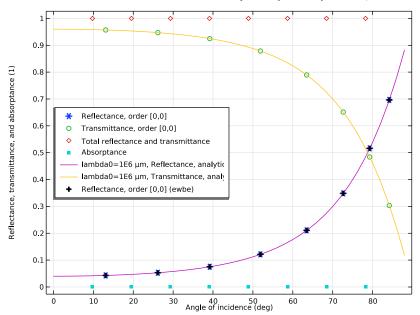
In the Model Builder window, under Results>Reflectance, Transmittance, and Absorptance (ewfd, TE) right-click Global I and choose Duplicate.

Global 3

- I In the Model Builder window, click Global 3.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study 3 (ewbe, TE)/Solution 3 (sol3).
- 4 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Electromagnetic Waves, Beam Envelopes (ewbe, TE)>Ports>Reflectance, by order>ewbe.Rorder_0_0 - Reflectance, order [0,0].
- **5** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
ewbe.Rorder_0_0	1	Reflectance, order [0,0] (ewbe)

6 In the Reflectance, Transmittance, and Absorptance (ewfd, TE) toolbar, click **1** Plot.

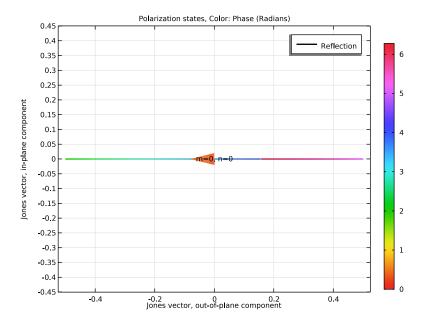


Notice that the reflectance curve for the Electromagnetic Waves, Beam Envelopes interface reproduces the other reflectance curves.

Polarization Plot (ewbe, TE)

- I In the Model Builder window, under Results click Polarization Plot (ewbe).
- 2 In the Settings window for ID Plot Group, type Polarization Plot (ewbe, TE) in the Label text field.

3 In the Polarization Plot (ewbe, TE) toolbar, click Plot.



ELECTROMAGNETIC WAVES, BEAM ENVELOPES (EWBE, TE) (EWBE)

The following instructions are for the p-polarization (TM) case for the Electromagnetic Waves, Beam Envelopes interface.

In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe) and choose Copy.

COMPONENT I (COMPI)

In the Model Builder window, right-click Component I (compl) and choose Paste Electromagnetic Waves, Beam Envelopes.

ELECTROMAGNETIC WAVES, BEAM ENVELOPES (EWBE2, TM)

- I In the Messages from Paste dialog box, click OK.
- 2 In the Model Builder window, under Component I (compl) click Electromagnetic Waves, Beam Envelopes (ewbe, TE) I (ewbe2).
- 3 In the Settings window for Electromagnetic Waves, Beam Envelopes, type Electromagnetic Waves, Beam Envelopes (ewbe2, TM) in the Label text field.

Port I

- I In the Model Builder window, expand the Component I (compl)>Electromagnetic Waves, Beam Envelopes (ewbe2, TM) (ewbe2) node, then click Port 1.
- 2 In the Settings window for Port, locate the Port Mode Settings section.
- 3 From the Input quantity list, choose Magnetic field.
- **4** Specify the \mathbf{H}_0 vector as

0	x
1	у
0	z

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Empty Study.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 4 (EWBE2, TM)

In the Settings window for Study, type Study 4 (ewbe2, TM) in the Label text field.

STUDY 3 (EWBE, TE)

Step 1: Wavelength Domain

In the Model Builder window, under Study 3 (ewbe, TE) right-click

Step 1: Wavelength Domain and choose **Copy**.

STUDY 4 (EWBE2, TM)

In the Model Builder window, right-click Study 4 (ewbe2, TM) and choose Paste Wavelength Domain.

- I In the Model Builder window, under Study 4 (ewbe2, TM) click Step 1: Wavelength Domain.
- 2 In the Settings window for Wavelength Domain, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Electromagnetic Waves, Beam Envelopes (ewbe, TE) (ewbe).

4 In the Home toolbar, click **Compute**.

RESULTS

Magnetic Field (ewbe2, TM)

- I In the Settings window for 3D Plot Group, type Magnetic Field (ewbe2, TM) in the Label text field.
- 2 Locate the Data section. From the Parameter value (alpha (deg)) list, choose 70.

Electric Field

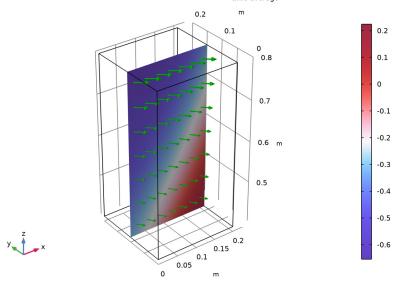
- I In the Model Builder window, expand the Magnetic Field (ewbe2, TM) node, then click Electric Field.
- 2 In the Settings window for Multislice, locate the Expression section.
- 3 In the Expression text field, type ewbe2. Hy.
- 4 Locate the Multiplane Data section. Find the X-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. In the **Planes** text field, type 0.
- **6** Locate the Coloring and Style section. Click Change Color Table.
- 7 In the Color Table dialog box, select Wave>WaveLight in the tree.
- 8 Click OK.

Arrow Volume 1

- I In the Model Builder window, right-click Magnetic Field (ewbe2, TM) and choose Arrow Volume.
- 2 In the Settings window for Arrow Volume, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Electromagnetic Waves, Beam Envelopes (ewbe2, TM)>Energy and power>ewbe2.Poavx,..., ewbe2.Poavz - Power flow, time average.
- 3 Locate the Arrow Positioning section. Find the Y grid points subsection. In the Points text field, type 1.
- 4 Locate the Coloring and Style section. From the Color list, choose Green.

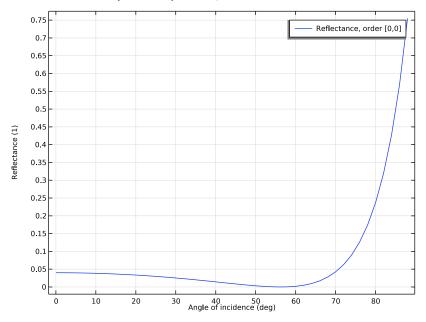
5 In the Magnetic Field (ewbe2, TM) toolbar, click Plot.

 $lambda0 = 1E6\ \mu\text{m, alpha} = 70\ deg\ Multislice:\ Magnetic\ field,\ y-component\ (A/m)\ Arrow\ Volume:\ Power\ flow,$ time average



Reflectance (ewbe2, TM)

- I In the Model Builder window, under Results click Reflectance (ewbe2).
- 2 In the Settings window for ID Plot Group, type Reflectance (ewbe2, TM) in the Label text field.



Global I Now compare this plot to the other TM reflectance plot.

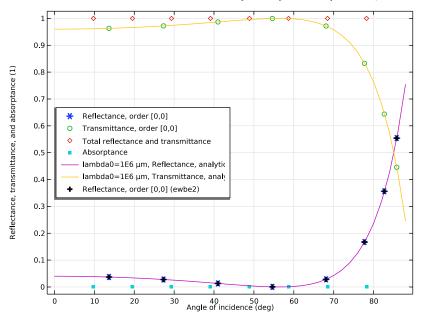
In the Model Builder window, under Results>Reflectance, Transmittance, and Absorptance (ewfd2, TM) right-click Global I and choose Duplicate.

Global 3

- I In the Model Builder window, click Global 3.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study 4 (ewbe2, TM)/Solution 4 (sol4).
- 4 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Electromagnetic Waves, Beam Envelopes (ewbe2, TM)>Ports>Reflectance, by order>ewbe2.Rorder_0_0 - Reflectance, order [0,0].
- **5** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
ewbe2.Rorder_0_0	1	Reflectance, order [0,0] (ewbe2)

6 In the Reflectance, Transmittance, and Absorptance (ewfd2, TM) toolbar, click Plot.



Again, the reflectance curve for the Electromagnetic Waves, Beam Envelopes interface reproduces well the other reflectance curves.

Polarization Plot (ewbe2, TM)

- I In the Model Builder window, under Results click Polarization Plot (ewbe2).
- 2 In the Settings window for ID Plot Group, type Polarization Plot (ewbe2, TM) in the Label text field.

