Optimization of a Photonic Crystal for Demultiplexing

Introduction

Photonic crystal devices are periodic structures of alternating layers of materials with different refractive indices. This model demonstrates how to apply shape optimization to a photonic crystal. The objective function is to maximize the output power ratio between two narrow frequency bands, while constraining the loss from below. This is achieved by letting GaAs pillars change position but not shape. The implementation makes use of the **Free Shape Domain** and **Transformation** features, so that gradient-based optimization can be applied.

Model Definition

The objective function φ is defined in terms of the average magnitude of the output powers for a given wavelength, λ:

$$\varphi(\lambda) = \begin{cases} \varphi_A(\lambda) \text{ , for } \min(|\lambda - \lambda_1|, |\lambda - \lambda_2|) < \lambda_\Delta/n \\ \varphi_B(\lambda) \text{ , for } \lambda_\Delta/n \leq \min(|\lambda - \lambda_1|, |\lambda - \lambda_2|) \end{cases}$$

$$\varphi_A(\lambda) = \begin{cases} -\Phi_1(\lambda)/\psi \text{ , for } \lambda < (\lambda_1 + \lambda_2)/2 \\ -\Phi_2(\lambda)/\psi \text{ , for } (\lambda_1 + \lambda_2)/2 \leq \lambda \end{cases}$$

$$\varphi_B(\lambda) = (\Phi_1(\lambda) + \Phi_2(\lambda))/m - 2$$

$$\Phi_1(\lambda) = \int_{\text{port 1}} P_{\text{out}} ds \qquad \Phi_2(\lambda) = \int_{\text{port 2}} P_{\text{out}} ds$$

with the following constants: $\psi = 0.25$ nW/m, $m = 0.05$ nW/m, $n = 1.99$ and the bandwidth $\lambda_\Delta = 0.01$ μm. The wavelengths λ_1 and λ_2 are equal to 1 μm and 1.1 μm, respectively. The power outflow is denoted by P_{out}.

The objective thus is to minimize the maximum of a list of objective functions. The MMA optimization solver is well suited for such problems. The topology of the mesh is fixed to allow for gradient-based optimization. To simplify manufacturing, the shape of the cylinder is also fixed. Thus, the only thing that is allowed to change is the cylinder positions. If they are allowed to move far, they might collide and cause error messages about inverted elements or NaN/Inf values. To avoid this, the cylinders are constrained to move 50 nm in the x and y directions.

Results and Discussion

Figure 1 and Figure 2 show the z-component of the electric field in the optimized geometry for the two of the wavelengths.
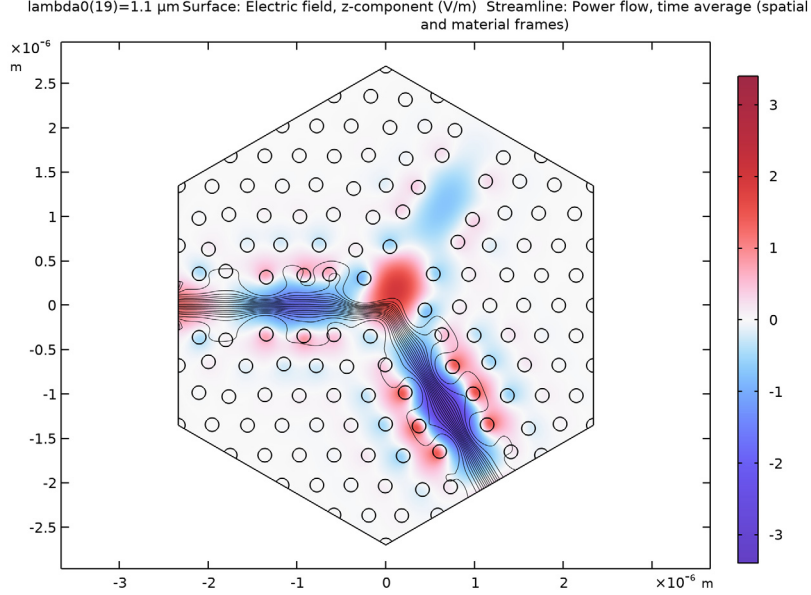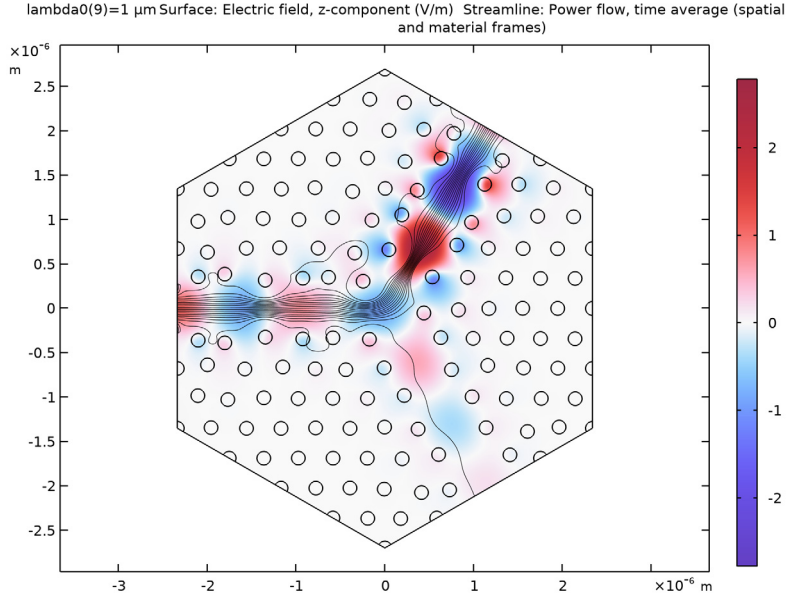
lambda0(19)=1.1 µm Surface: Electric field, z-component (V/m) Streamline: Power flow, time average (spatial and material frames)

Figure 1: The z-component of the electric field for the lower frequency band. The wave propagates to the lower output.

lambda0(9)=1 µm Surface: Electric field, z-component (V/m) Streamline: Power flow, time average (spatial and material frames)

Figure 2: The z-component of the electric field for the higher frequency band. The wave propagates to the upper output.

The graphs in Figure 3 are based on an analysis, where the mesh has been regenerated in the deformed configuration. The purpose of this is to ensure that the optimization result does not rely on unphysical numerical effects.
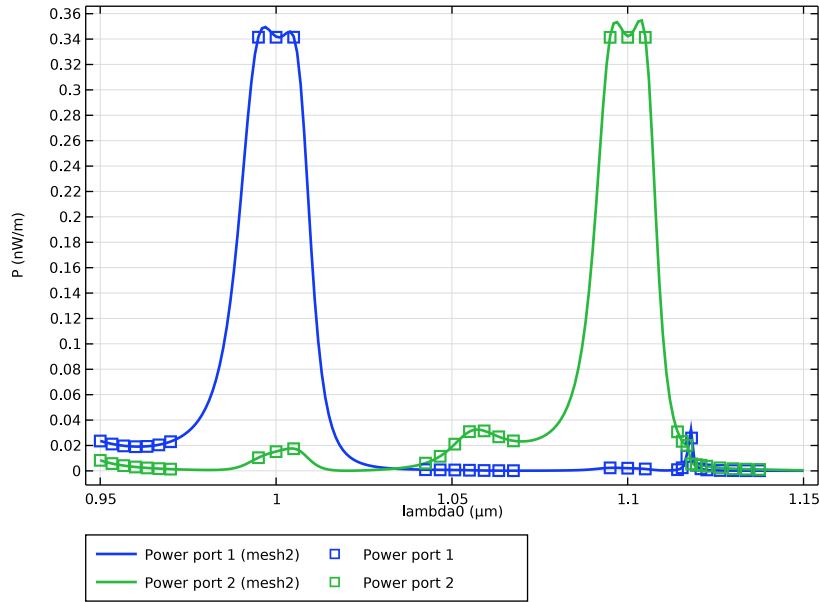
Figure 3: The two auxiliary objective functions are plotted as a function of the frequency. The points indicate the frequencies used to approximate the two frequency bands.

Reference

1. J.D. Joannopoulos, R.D. Meade, and J.N. Winn, *Photonic Crystals (Modeling the Flow of Light)*, Princeton University Press, 1995.

Application Library path: `Wave_Optics_Module/Couplers_Filters_and_Mirrors/photonic_crystal_demultiplexer_optimization`

Modeling Instructions

From the **File** menu, choose **New**.

NEW

In the **New** window, click ◈ **Model Wizard**.

1 In the **Model Wizard** window, click **2D**.

2 In the **Select Physics** tree, select **Optics>Wave Optics>Electromagnetic Waves, Frequency Domain (ewfd)**.

3 Click **Add**.

4 Click **Study**.

5 In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces> Wavelength Domain**.

6 Click **Done**.

GEOMETRY 1

Create the geometry. To simplify this step, insert a prepared geometry sequence.

1 In the **Geometry** toolbar, click **Insert Sequence** and choose **Insert Sequence**.

2 Browse to the model's Application Libraries folder and double-click the file `photonic_crystal_demultiplexer_optimization_geom_sequence.mph`.

3 In the **Geometry** toolbar, click **Build All**.

4 Click the **Zoom Extents** button in the **Graphics** toolbar.

5 In the **Model Builder** window, under **Component 1 (comp1)** click **Geometry 1**.
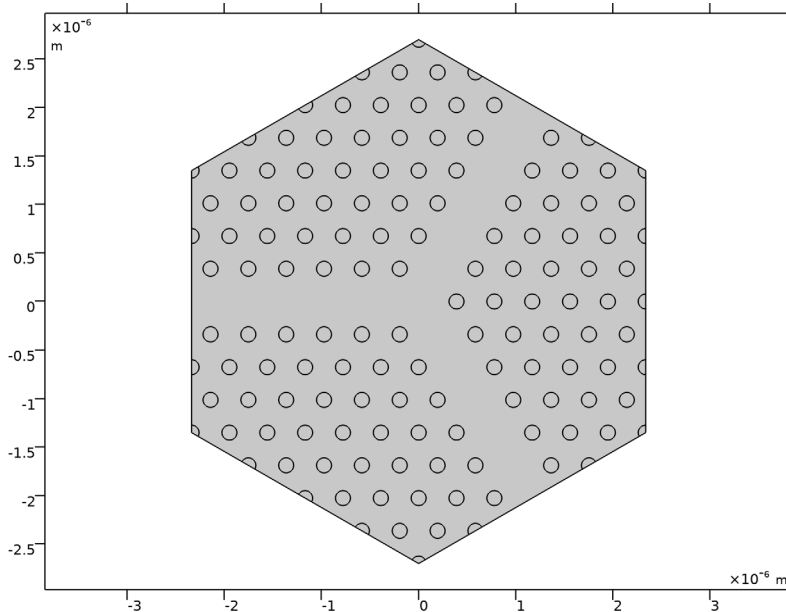
6 In the **Model Builder** window, collapse the **Geometry 1** node.

Air

1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.

2 In the **Settings** window for **Material**, type Air in the **Label** text field.

3 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Refractive index, real part	n_iso ; nii = n_iso, nij = 0	1	1	Refractive index

The pillars are made of Gallium arsenide (GaAs), which is available in the Optical Material Library. Follow the instructions below to add it to the model. Note that the refractive index of GaAs depends on the frequency.

ADD MATERIAL

1 In the **Home** toolbar, click ⬛ **Add Material** to open the **Add Material** window.

2 Go to the **Add Material** window.

3 In the tree, select **Optical>Inorganic Materials>As - Arsenides>Experimental data> GaAs (Gallium arsenide) (Papatryfonos et al. 2021: n,k 0.260-1.88 um)**.

4 Click **Add to Component** in the window toolbar.

5 In the **Home** toolbar, click ⬛ **Add Material** to close the **Add Material** window.

MATERIALS

GaAs (Gallium arsenide) (Papatryfonos et al. 2021: n,k 0.260-1.88 um) (mat2)

1 In the **Settings** window for **Material**, locate the **Geometric Entity Selection** section.

2 From the **Selection** list, choose **Circle 1**.

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EWFD)

1 In the **Model Builder** window, under **Component 1 (comp1)** click **Electromagnetic Waves, Frequency Domain (ewfd)**.

2 In the **Settings** window for **Electromagnetic Waves, Frequency Domain**, locate the **Components** section.

3 From the **Electric field components solved for** list, choose **Out-of-plane vector**.

Scattering Boundary Condition 1

1 In the **Physics** toolbar, click ⬤ **Boundaries** and choose **Scattering Boundary Condition**.

2 In the **Settings** window for **Scattering Boundary Condition**, locate the **Boundary Selection** section.

3 From the **Selection** list, choose **All boundaries**.

Scattering Boundary Condition 2

1 In the **Physics** toolbar, click ⬤ **Boundaries** and choose **Scattering Boundary Condition**.

2 In the **Settings** window for **Scattering Boundary Condition**, locate the **Boundary Selection** section.

3 From the **Selection** list, choose **Input Port**.

4 Locate the **Scattering Boundary Condition** section. From the **Incident field** list, choose **Wave given by E field**.

5 Specify the $\mathbf{E}_0$ vector as

0	x
0	y
1	z

MESH 1

In the **Model Builder** window, under **Component 1 (comp1)** right-click **Mesh 1** and choose **Build All**.

DEFINITIONS

Power Port 1

1 In the **Definitions** toolbar, click 📝 **Probes** and choose **Boundary Probe**.

2 In the **Settings** window for **Boundary Probe**, type Power Port 1 in the **Label** text field.

3 In the **Variable name** text field, type obj1.

4 Locate the **Probe Type** section. From the **Type** list, choose **Integral**.

5 Locate the **Source Selection** section. From the **Selection** list, choose **Output Port 1**.

6 Click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)>Electromagnetic Waves, Frequency Domain> Energy and power>ewfd.nPoav - Power outflow, time average - W/m²**.

7 Right-click **Power Port 1** and choose **Duplicate**.

Power Port 2

1 In the **Model Builder** window, under **Component 1 (comp1)>Definitions** click
Power Port 1.1 (bnd2).

2 In the **Settings** window for **Boundary Probe**, type Power Port 2 in the **Label** text field.

3 In the **Variable name** text field, type obj2.

4 Locate the **Source Selection** section. From the **Selection** list, choose **Output Port 2**.

GLOBAL DEFINITIONS

Wave Parameters

1 In the **Home** toolbar, click P¡ **Parameters** and choose **Add>Parameters**.

2 In the **Settings** window for **Parameters**, type Wave Parameters in the **Label** text field.

3 Locate the **Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
meshsz	lambda2/9	1.2222E-7 m	Mesh size
minPower	0.25[nW/m]	2.5E-10 W/m	Pass band power
maxPower	minPower/5	5E-11 W/m	Minimum out-of-band power
lambda1	1[um]	1E-6 m	First wavelength
lambda3	0.96*lambda1	9.6E-7 m	Out-of-band wavelength (lower)
lambda4	1.055*lambda1	1.055E-6 m	Out-of-band wavelength (center)
lambda5	1.1175*lambda1	1.1175E-6 m	Out-of-band wavelength (higher)
lambda6	1.13*lambda1	1.13E-6 m	Out-of-band wavelength (highest)
dWaveN	3	3	Frequencies per pass band
dWaveN3	4	4	Frequencies for first out-of-band constraint
dWaveN4	7	7	Frequencies for middle out-of-band constraint
dWaveN5	6	6	Frequencies for third out-of-band constraint
dWaveN6	5	5	Frequencies for last out-of-band constraint
dWave	0.01*lambda1	1E-8 m	Bandwidth for pass band

Name	Expression	Value	Description
dWave3	2*dWave	2E-8 m	Bandwidth for first out-of-band wavelengths
dWave4	2.5*dWave	2.5E-8 m	Bandwidth for middle out-of-band wavelengths
dWave5	dWave/1.5	6.6667E-9 m	Bandwidth for third out-of-band wavelengths
dWave6	1.5*dWave	I.5E-8 m	Bandwidth for last out-of-band wavelengths

MESH 1

1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.

2 In the **Settings** window for **Mesh**, locate the **Sequence Type** section.

3 From the list, choose **User-controlled mesh**.

Size

1 In the **Model Builder** window, under **Component 1 (comp1)>Mesh 1** click **Size**.

2 In the **Settings** window for **Size**, locate the **Element Size Parameters** section.

3 In the **Maximum element size** text field, type meshsz.

4 In the **Minimum element size** text field, type meshsz/2.

5 In the **Curvature factor** text field, type Inf.

Size 1

1 In the **Model Builder** window, click **Size 1**.

2 In the **Settings** window for **Size**, locate the **Geometric Entity Selection** section.

3 From the **Selection** list, choose **Circle 1**.

4 Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type meshsz/2.

5 In the **Minimum element size** text field, type meshsz/4.

6 Clear the **Maximum element growth rate** check box.

7 Clear the **Curvature factor** check box.

8 Clear the **Resolution of narrow regions** check box.

9 Click ▦ **Build All**.

Step 1: Wavelength Domain

1 In the **Model Builder** window, under **Study 1** click **Step 1: Wavelength Domain**.

2 In the **Settings** window for **Wavelength Domain**, locate the **Study Settings** section.

3 From the **Wavelength unit** list, choose **m**.

4 In the **Wavelengths** text field, type range(lambda1-50[nm],1[nm],lambda2+50[nm]).

5 Click to expand the **Results While Solving** section. From the **Probes** list, choose **None**.

6 In the **Model Builder** window, click **Study 1**.

7 In the **Settings** window for **Study**, type Initial Design in the **Label** text field.

8 In the **Home** toolbar, click ▬ **Compute**.

COMPONENT 1 (COMP1)

Free Shape Domain 1

1 In the **Physics** toolbar, click 🎯 **Optimization** and choose **Shape Optimization**.

2 In the **Settings** window for **Free Shape Domain**, locate the **Domain Selection** section.

3 Click 🖌 **Clear Selection**.

4 Click 📋 **Paste Selection**.

5 In the **Paste Selection** dialog box, type 2 in the **Selection** text field.

6 Click **OK**.

Transformation 1

1 In the **Shape Optimization** toolbar, click 🗔 **Transformation**.

2 In the **Settings** window for **Transformation**, locate the **Geometric Entity Selection** section.

3 From the **Selection** list, choose **Moving Domains**.

4 Locate the **Translation** section. In the table, enter the following settings:

	Lock	Lower bound (m)	Upper bound (m)
X		-5E-8	5E-8
Y		-5E-8	5E-8

5 Locate the **Scaling** section. From the **Scaling type** list, choose **No scaling**.

DEFINITIONS

Objectives

1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Definitions** and choose **Variables**.

2 In the **Settings** window for **Variables**, type Objectives in the **Label** text field.

3 Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
objA	if(lambda0<(lambda1+lambda2)/2,-obj1/minPower,-obj2/minPower)		Pass band objective
objB	(obj1+obj2)/maxPower-2		Out-of-band objective
obj	if(min(abs(lambda0-lambda1), abs(lambda0-lambda2))<dWave/1.99, objA,objB)		Objective function

ADD STUDY

1 In the **Home** toolbar, click ⌒⊗⥥ **Add Study** to open the **Add Study** window.

2 Go to the **Add Study** window.

3 Find the **Studies** subsection. In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces>Wavelength Domain**.

4 Click **Add Study** in the window toolbar.

Add also an empty study that will be edited and used later.

5 In the **Select Study** tree, select **Empty Study**.

6 Click **Add Study** in the window toolbar.

7 In the **Home** toolbar, click ⌒⊗⥥ **Add Study** to close the **Add Study** window.

INITIAL DESIGN

Disable the shape optimization for the first study.

Step 1: Wavelength Domain

1 In the **Model Builder** window, under **Initial Design** click **Step 1: Wavelength Domain**.

2 In the **Settings** window for **Wavelength Domain**, locate the **Physics and Variables Selection** section.

3 In the table, enter the following settings:

Physics interface	Solve for	Equation form
Electromagnetic Waves, Frequency Domain (ewfd)	√	Automatic (Frequency domain)
Deformed geometry (Component 1)		Automatic

STUDY 2

1 In the **Model Builder** window, under **Study 2** click **Step 1: Wavelength Domain**.

2 In the **Settings** window for **Wavelength Domain**, locate the **Study Settings** section.

3 In the **Wavelengths** text field, type range(lambda3-dWave3/2,dWave/(dWaveN3-1), lambda3+dWave3/2) range(lambda1-dWave/2,dWave/(dWaveN-1),lambda1+ dWave/2) range(lambda4-dWave4/2,dWave4/(dWaveN4-1),lambda4+dWave4/2) range(lambda2-dWave/2,dWave/(dWaveN-1),lambda2+dWave/2) range(lambda5-dWave5/2,dWave5/(dWaveN5-1),lambda5+dWave5/2) range(lambda6-dWave6/2,dWave6/(dWaveN6-1),lambda6+dWave6/2).

4 Locate the **Results While Solving** section. From the **Probes** list, choose **None**.

Shape Optimization

1 In the **Study** toolbar, click 🎯 **Optimization** and choose **Shape Optimization**.

2 In the **Settings** window for **Shape Optimization**, locate the **Optimization Solver** section.

3 In the **Maximum number of iterations** text field, type 50.

4 Click **Add Expression** in the upper-right corner of the **Objective Function** section. From the menu, choose **Component 1 (comp1)>Definitions>Variables>comp1.obj - Objective function - 1**.

5 Locate the **Objective Function** section. From the **Solution** list, choose **Maximum of objectives**.

This causes the solver to identify the frequency associated with the maximum objective function and prioritize this over the other frequencies (while still taking all frequencies into account).

6 Locate the **Output While Solving** section. From the **Probes** list, choose **None**.

7 In the **Model Builder** window, click **Study 2**.

8 In the **Settings** window for **Study**, type Shape Optimization in the **Label** text field.

9 In the **Study** toolbar, click ⊔₌ₒ **Get Initial Value**.

10 In the **Model Builder** window, click **Shape Optimization**.

11 In the **Settings** window for **Shape Optimization**, locate the **Output While Solving** section.

12 Select the **Plot** check box.

13 From the **Plot group** list, choose **Shape Optimization**.

Solver Configurations

It is easier to converge the problem using a Segregated solver.

In the **Model Builder** window, expand the **Shape Optimization>Solver Configurations** node.

Solution 2 (sol2)

1 In the **Model Builder** window, expand the **Shape Optimization>Solver Configurations> Solution 2 (sol2)** node, then click **Optimization Solver 1**.

2 In the **Settings** window for **Optimization Solver**, click to expand the **Advanced** section.

3 From the **Compensate for nojac terms** list, choose **Off**.

4 In the **Model Builder** window, expand the **Shape Optimization>Solver Configurations> Solution 2 (sol2)>Optimization Solver 1>Stationary 1** node.

5 Right-click **Stationary 1** and choose **Segregated**.

6 In the **Settings** window for **Segregated**, locate the **General** section.

7 From the **Termination technique** list, choose **Iterations**, to reduce the computational time.

8 Right-click **Segregated 1** and choose **Segregated Step**.

9 In the **Settings** window for **Segregated Step**, type Optimization in the **Label** text field.

10 Locate the **General** section. In the **Variables** list, select **Electric field (spatial and material frames) (comp1.E)**.

11 Under **Variables**, click **Delete**.

12 In the **Model Builder** window, under **Shape Optimization>Solver Configurations> Solution 2 (sol2)>Optimization Solver 1>Stationary 1>Segregated 1** click **Segregated Step 1**.

13 In the **Settings** window for **Segregated Step**, type Electric Fields in the **Label** text field.

14 Locate the **General** section. Under **Variables**, click **Add**.

15 In the **Add** dialog box, in the **Variables** list, choose **Electric field (spatial and material frames) (comp1.E)** and **Translation (geometry frame) (comp1.tsf1.move)**.

16 Click **OK**.

17 In the **Settings** window for **Segregated Step**, click **Compute**.

RESULTS

Shape Optimization/Solution 2 (sol2)

1 In the **Model Builder** window, expand the **Results>Datasets** node.

2 Right-click **Results>Datasets>Shape Optimization/Solution 2 (sol2)** and choose **Remesh Deformed Configuration**.

INITIAL DESIGN

Step 1: Wavelength Domain

In the **Model Builder** window, under **Initial Design** right-click **Step 1: Wavelength Domain** and choose **Copy**.

VERIFICATION

In the **Model Builder** window, right-click **Study 3** and choose **Paste Wavelength Domain**.

1 In the **Model Builder** window, under **Study 3** click **Step 1: Wavelength Domain**.

2 In the **Settings** window for **Wavelength Domain**, locate the **Physics and Variables Selection** section.

3 In the table, clear the **Solve for** check box for **Deformed geometry (Component 1)**.

4 Click to expand the **Values of Dependent Variables** section. Find the **Initial values of variables solved for** subsection. From the **Settings** list, choose **User controlled**.

5 From the **Method** list, choose **Solution**.

6 From the **Study** list, choose **Shape Optimization, Wavelength Domain**.

7 Find the **Values of variables not solved for** subsection. From the **Settings** list, choose **User controlled**.

8 From the **Method** list, choose **Solution**.

9 From the **Study** list, choose **Shape Optimization, Wavelength Domain**.

10 Click to expand the **Store in Output** section. In the table, enter the following settings:

Interface	Output
Electromagnetic Waves, Frequency Domain (ewfd)	Selection

11 Click to select row number 1 in the table.

12 Under **Selections**, click ➕ **Add**.

13 In the **Add** dialog box, in the **Selections** list, choose **Output Port 1** and **Output Port 2**.

14 Click **OK**.

15 In the **Settings** window for **Wavelength Domain**, locate the **Store in Output** section.

16 In the table, enter the following settings:

Interface	Output
Deformed geometry (Component 1)	Selection

17 Click to select row number 2 in the table.

18 Under **Selections**, click ╋ **Add**.

19 In the **Add** dialog box, in the **Selections** list, choose **Output Port 1** and **Output Port 2**.

20 Click **OK**.

21 In the **Settings** window for **Wavelength Domain**, click to expand the **Mesh Selection** section.

22 In the table, enter the following settings:

Component	Mesh
Component 1	Mesh 2

23 In the **Model Builder** window, click **Study 3**.

24 In the **Settings** window for **Study**, type Verification in the **Label** text field.

25 Locate the **Study Settings** section. Clear the **Generate default plots** check box.

26 In the **Home** toolbar, click ▬ **Compute**.

RESULTS

Electric Field (initial)

1 In the **Model Builder** window, under **Results** click **Electric Field (ewfd)**.

2 In the **Settings** window for **2D Plot Group**, type Electric Field (initial) in the **Label** text field.

Surface 1

1 In the **Model Builder** window, expand the **Electric Field (initial)** node, then click **Surface 1**.

2 In the **Settings** window for **Surface**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)> Electromagnetic Waves, Frequency Domain>Electric>Electric field - V/m>ewfd.Ez - Electric field, z-component**.

3 Locate the **Coloring and Style** section. Click ▐▐▌ **Change Color Table**.

4 In the **Color Table** dialog box, select **Wave>WaveLight** in the tree.

5 Click **OK**.

Streamline 1

1 In the **Model Builder** window, right-click **Electric Field (ewfd) 1** and choose **Streamline**.

2 In the **Settings** window for **Streamline**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)> Electromagnetic Waves, Frequency Domain>Energy and power>ewfd.Poavx,ewfd.Poavy - Power flow, time average (spatial and material frames)**.

3 Locate the **Selection** section. From the **Selection** list, choose **Input Port**.

4 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Type** list, choose **Tube**.

5 Select the **Radius scale factor** check box.

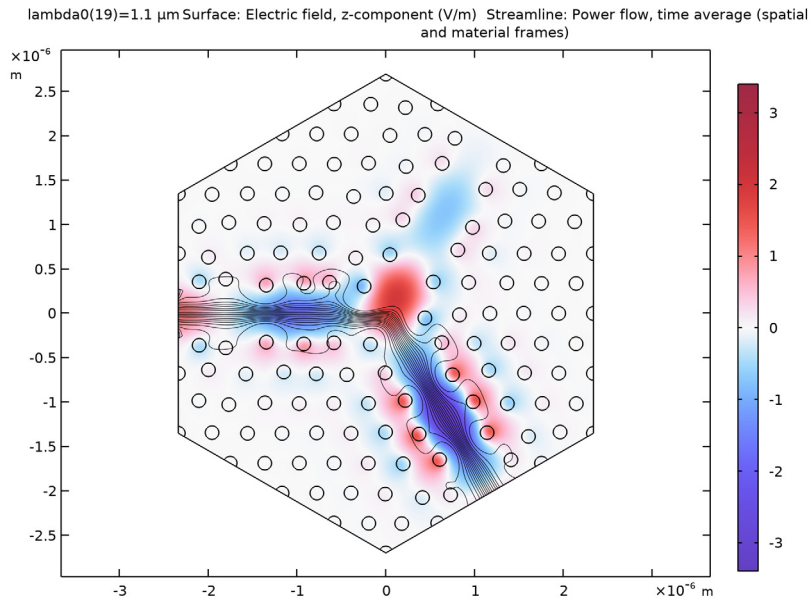**6** In the **Tube radius expression** text field, type 3e-9.

Surface 1

1 In the **Model Builder** window, click **Surface 1**.

2 In the **Settings** window for **Surface**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)> Electromagnetic Waves, Frequency Domain>Electric> Electric field (spatial and material frames) - V/m>ewfd.Ez - Electric field, z-component**.

3 Locate the **Coloring and Style** section. From the **Scale** list, choose **Linear symmetric**.

4 Click ▌▌▌ **Change Color Table**.

5 In the **Color Table** dialog box, select **Wave>WaveLight** in the tree.
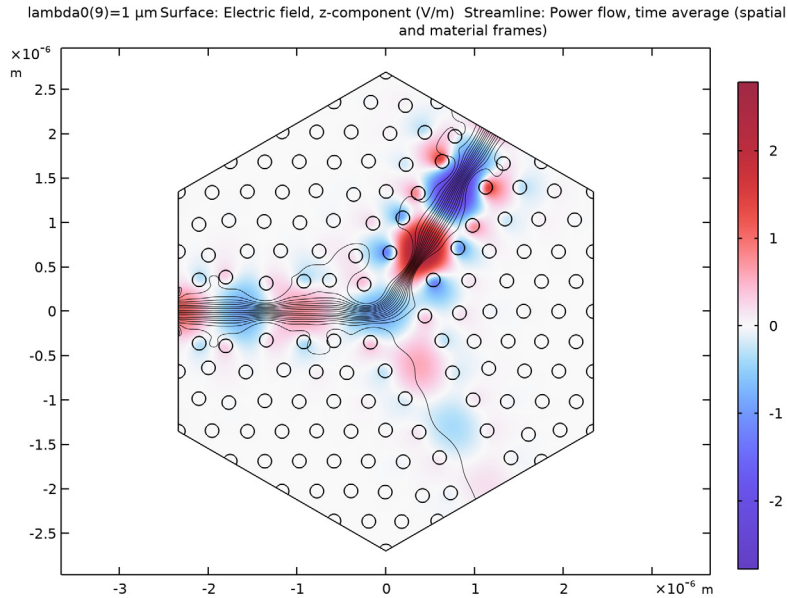
6 Click **OK**.

Electric Field (optimized)

1 In the **Model Builder** window, under **Results** click **Electric Field (ewfd) 1**.

2 In the **Settings** window for **2D Plot Group**, type Electric Field (optimized) in the **Label** text field.

3 Locate the **Data** section. From the **Parameter value (lambda0 (µm))** list, choose **1.1**.

4 In the **Electric Field (optimized)** toolbar, click ▣ **Plot**.

5 Click the ⊕ **Zoom Extents** button in the **Graphics** toolbar.

lambda0(19)=1.1 µm Surface: Electric field, z-component (V/m) Streamline: Power flow, time average (spatial and material frames)

6 From the **Parameter value (lambda0 (µm))** list, choose **1**.

7 In the **Electric Field (optimized)** toolbar, click **Plot**.

lambda0(9)=1 μm Surface: Electric field, z-component (V/m) Streamline: Power flow, time average (spatial and material frames)

Create a new plot **1D Plot Group** for the spectrum.

Spectrum

1 In the **Home** toolbar, click **Add Plot Group** and choose **1D Plot Group**.

2 In the **Settings** window for **1D Plot Group**, type Spectrum in the **Label** text field.

3 Locate the **Data** section. From the **Dataset** list, choose **Verification/Solution 3 (sol3)**.

4 Click to expand the **Title** section. From the **Title type** list, choose **None**.

5 Locate the **Plot Settings** section.

6 Select the **y-axis label** check box. In the associated text field, type P (nW/m).

7 Locate the **Legend** section. From the **Layout** list, choose **Outside graph axis area**.

8 From the **Position** list, choose **Bottom**.

9 In the **Number of rows** text field, type 2.

Global 1

1 Right-click **Spectrum** and choose **Global**.

2 In the **Settings** window for **Global**, click **Add Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1)>Definitions>obj1 - Power Port 1 - W/m**.

3 Click **Add Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1)>Definitions>obj2 - Power Port 2 - W/m**.

4 Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
obj1	nW/m	Power port 1 (mesh2)
obj2	nW/m	Power port 2 (mesh2)

5 Locate the **x-Axis Data** section. From the **Unit** list, choose **µm**.

6 Click to expand the **Coloring and Style** section. From the **Width** list, choose **2**.

7 Right-click **Global 1** and choose **Duplicate**.

Global 2

1 In the **Model Builder** window, click **Global 2**.

2 In the **Settings** window for **Global**, locate the **Data** section.

3 From the **Dataset** list, choose **Shape Optimization/Solution 2 (sol2)**.

4 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **None**.

5 Find the **Line markers** subsection. From the **Marker** list, choose **Square**.

6 From the **Color** list, choose **Cycle (reset)**.

7 Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
obj1	nW/m	Power port 1
obj2	nW/m	Power port 2

8 In the **Spectrum** toolbar, click **Plot**.

9 Click the ⊕ **Zoom Extents** button in the **Graphics** toolbar.
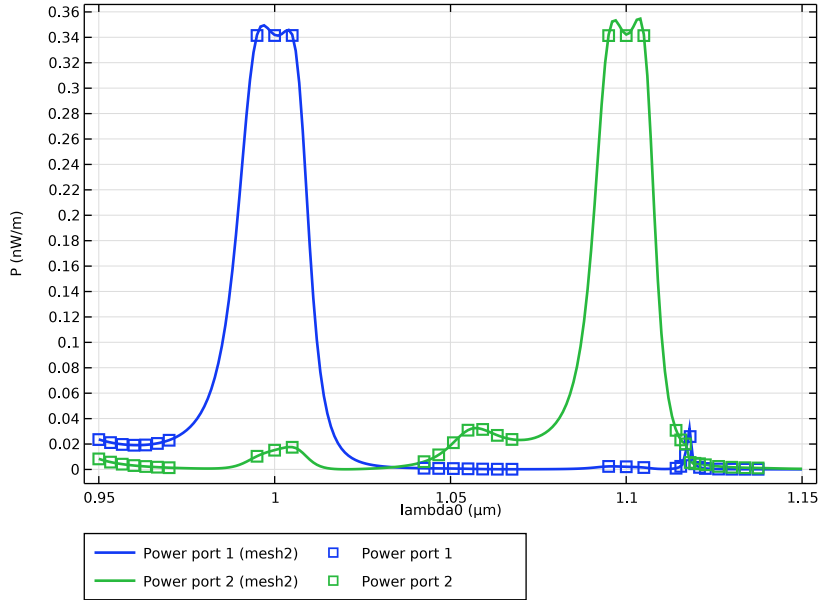
Shape Optimization

Finally, create a new **2D Plot Group** for the thumbnail.

1 In the **Model Builder** window, under **Results** right-click **Shape Optimization** and choose **Duplicate**.

Thumbnail

1 In the **Model Builder** window, under **Results** click **Shape Optimization 1**.

2 In the **Settings** window for **2D Plot Group**, type `Thumbnail` in the **Label** text field.

3 Locate the **Plot Settings** section. Clear the **Plot dataset edges** check box.

Line 1

1 In the **Model Builder** window, expand the **Thumbnail** node, then click **Line 1**.

2 In the **Settings** window for **Line**, locate the **Coloring and Style** section.

3 From the **Line type** list, choose **Tube**.

4 In the **Tube radius expression** text field, type `5e-9`.

5 Select the **Radius scale factor** check box.

6 Right-click **Line 1** and choose **Duplicate**.

Line 2

1 In the **Model Builder** window, click **Line 2**.

2 In the **Settings** window for **Line**, locate the **Coloring and Style** section.

3 From the **Color** list, choose **Gray**.

Deformation 1

1 Right-click **Line 2** and choose **Deformation**.

2 In the **Settings** window for **Deformation**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)> Definitions>Transformation 1>tsf1.dXg,tsf1.dYg - Boundary displacement (geometry frame)**.

3 Locate the **Expression** section. In the **X-component** text field, type `-tsf1.dXg`.

4 In the **Y-component** text field, type `-tsf1.dYg`.

5 Locate the **Scale** section.

6 Select the **Scale factor** check box. In the associated text field, type 1.

Color Expression 1

1 In the **Model Builder** window, expand the **Results>Thumbnail> Translation (Transformation 1)** node, then click **Color Expression 1**.

2 In the **Settings** window for **Color Expression**, locate the **Expression** section.

3 In the **Expression** text field, type `sqrt(material.dX^2+material.dY^2)`.

4 Click to expand the **Range** section. Clear the **Manual color range** check box.

Filter 1

1 In the **Model Builder** window, right-click **Line 1** and choose **Filter**.

2 In the **Settings** window for **Filter**, locate the **Element Selection** section.

3 In the **Logical expression for inclusion** text field, type `(abs(X)<1e-6)*(abs(Y)<1e-6)`.

4 Right-click **Filter 1** and choose **Copy**.

Translation (Transformation 1)

In the **Model Builder** window, under **Results>Thumbnail** right-click **Translation (Transformation 1)** and choose **Paste Filter**.

Line 2
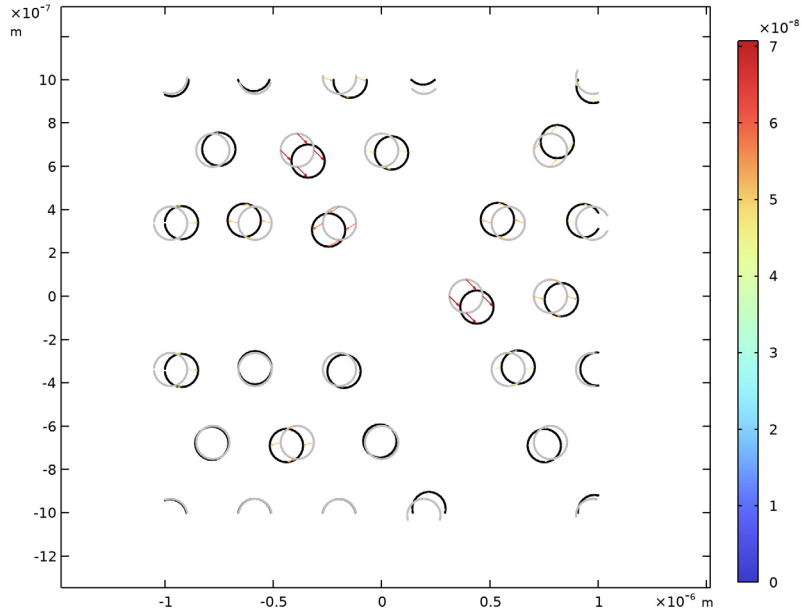
In the **Model Builder** window, right-click **Line 2** and choose **Paste Filter**.

Filter 1

1 In the **Model Builder** window, click **Filter 1**.

2 In the **Thumbnail** toolbar, click ◧ **Plot**.

3 Click the ⊹ **Zoom Extents** button in the **Graphics** toolbar.

4 Click the ⊕ **Zoom In** button in the **Graphics** toolbar.

Geometry Modeling Instructions

From the **File** menu, choose **New**.

NEW

In the **New** window, click ◈ **Blank Model**.

GLOBAL DEFINITIONS

Parameters 1

1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.

2 In the **Settings** window for **Parameters**, locate the **Parameters** section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
lambda2	1.1[um]	1.1E-6 m	Second wavelength
W	4.25*lambda2	4.675E-6 m	Design domain width
rHole	0.07*lambda2	7.7E-8 m	Hole radius
nCircles	6	6	Circles per channel
dPeriod	W/nCircles/2	3.8958E-7 m	Periodicity

ADD COMPONENT

In the **Home** toolbar, click ◈ **Add Component** and choose **2D**.

GEOMETRY 1

Polygon 1 (pol1)

1 In the **Geometry** toolbar, click ╱╎ **Polygon**.

2 In the **Settings** window for **Polygon**, locate the **Coordinates** section.

3 In the table, enter the following settings:

x (m)	y (m)
-W/2	sin(5/6*pi)*W/2*2/sqrt(3)
0	W/2*2/sqrt(3)
W/2	sin(1/6*pi)*W/2*2/sqrt(3)
W/2	sin(-1/6*pi)*W/2*2/sqrt(3)
0	-W/2*2/sqrt(3)
-W/2	sin(-5/6*pi)*W/2*2/sqrt(3)

4 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** check box.

Circle 1 (c1)

1 In the **Geometry** toolbar, click ⊙ **Circle**.

2 In the **Settings** window for **Circle**, locate the **Size and Shape** section.

3 In the **Radius** text field, type rHole.

4 Locate the **Position** section. In the **x** text field, type -W/2.

5 In the **y** text field, type -2*dPeriod*sin(pi/3)*round(W/dPeriod/sin(pi/3)/3).

6 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** check box.

Move 1 (mov1)

1 In the **Geometry** toolbar, click ⟳ **Transforms** and choose **Move**.

2 In the **Settings** window for **Move**, locate the **Input** section.

3 From the **Input objects** list, choose **Circle 1**.

4 Select the **Keep input objects** check box.

5 Locate the **Displacement** section. In the **x** text field, type `cos(pi/3)*dPeriod`.

6 In the **y** text field, type `sin(pi/3)*dPeriod`.

Array 1 (arr1)

1 In the **Geometry** toolbar, click ⟳ **Transforms** and choose **Array**.

2 In the **Settings** window for **Array**, locate the **Input** section.

3 From the **Input objects** list, choose **Circle 1**.

4 Locate the **Size** section. In the **x size** text field, type `round(W/dPeriod)+1`.

5 In the **y size** text field, type `round(W/dPeriod)`.

6 Locate the **Displacement** section. In the **x** text field, type `dPeriod`.

7 In the **y** text field, type `2*sin(pi/3)*dPeriod`.

All Objects

1 In the **Geometry** toolbar, click ⬛ **Selections** and choose **Box Selection**.

2 In the **Settings** window for **Box Selection**, type `All Objects` in the **Label** text field.

3 Locate the **Geometric Entity Level** section. From the **Level** list, choose **Object**.

Circles to Delete, Row 1

1 In the **Geometry** toolbar, click ⬛ **Selections** and choose **Box Selection**.

2 In the **Settings** window for **Box Selection**, type `Circles to Delete, Row 1` in the **Label** text field.

3 Locate the **Box Limits** section. In the **x maximum** text field, type `2*rHole`.

4 In the **y minimum** text field, type `-rHole*1.01`.

5 In the **y maximum** text field, type `rHole*1.01`.

6 Locate the **Output Entities** section. From the **Include entity if** list, choose **Entity inside box**.

Rotate 1 (rot1)

1 In the **Geometry** toolbar, click **Transforms** and choose **Rotate**.

2 In the **Settings** window for **Rotate**, locate the **Input** section.

3 From the **Input objects** list, choose **Circle 1**.

4 Locate the **Rotation** section. In the **Angle** text field, type 120.

Circles to Delete, Row 1 (boxsel2)

In the **Model Builder** window, right-click **Circles to Delete, Row 1 (boxsel2)** and choose **Duplicate**.

Circles to Delete, Row 2

1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** click **Circles to Delete, Row 1.1 (boxsel3)**.

2 In the **Settings** window for **Box Selection**, type Circles to Delete, Row 2 in the **Label** text field.

Rotate 1 (rot1)

In the **Model Builder** window, right-click **Rotate 1 (rot1)** and choose **Duplicate**.

Circles to Delete, Row 2 (boxsel3)

In the **Model Builder** window, right-click **Circles to Delete, Row 2 (boxsel3)** and choose **Duplicate**.

Circles to Delete, Row 3

1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** click **Circles to Delete, Row 2.1 (boxsel4)**.

2 In the **Settings** window for **Box Selection**, type Circles to Delete, Row 3 in the **Label** text field.

Rotate 2 (rot2)

In the **Model Builder** window, right-click **Rotate 2 (rot2)** and choose **Duplicate**.

Circles to Delete, Rows

1 In the **Geometry** toolbar, click **Selections** and choose **Union Selection**.

2 In the **Settings** window for **Union Selection**, type Circles to Delete, Rows in the **Label** text field.

3 Locate the **Input Entities** section. Click ✛ **Add**.

4 In the **Add** dialog box, in the **Selections to add** list, choose **Circles to Delete, Row 1**, **Circles to Delete, Row 2**, and **Circles to Delete, Row 3**.

5 Click **OK**.

Delete Entities 1 (del1)

1 In the **Model Builder** window, right-click **Geometry 1** and choose **Delete Entities**.

2 In the **Settings** window for **Delete Entities**, locate the **Entities or Objects to Delete** section.

3 From the **Geometric entity level** list, choose **Domain**.

4 From the **Selection** list, choose **Circles to Delete, Rows**.

Union 1 (uni1)

1 In the **Geometry** toolbar, click ▤ **Booleans and Partitions** and choose **Union**.

2 In the **Settings** window for **Union**, locate the **Union** section.

3 From the **Input objects** list, choose **All Objects**.

Difference Selection 1 (difsel1)

1 In the **Geometry** toolbar, click ⬚ **Selections** and choose **Difference Selection**.

2 In the **Settings** window for **Difference Selection**, locate the **Input Entities** section.

3 Click the ＋ **Add** button for **Selections to add**.

4 In the **Add** dialog box, select **Circle 1** in the **Selections to add** list.

5 Click **OK**.

6 In the **Settings** window for **Difference Selection**, locate the **Input Entities** section.

7 Click the ＋ **Add** button for **Selections to subtract**.

8 In the **Add** dialog box, select **Polygon 1** in the **Selections to subtract** list.

9 Click **OK**.

Delete Entities 2 (del2)

1 Right-click **Geometry 1** and choose **Delete Entities**.

2 In the **Settings** window for **Delete Entities**, locate the **Entities or Objects to Delete** section.

3 From the **Geometric entity level** list, choose **Domain**.

4 From the **Selection** list, choose **Difference Selection 1**.

Input Port

1 In the **Geometry** toolbar, click ⋰ **More Primitives** and choose **Line Segment**.

2 In the **Settings** window for **Line Segment**, type Input Port in the **Label** text field.

3 Locate the **Starting Point** section. From the **Specify** list, choose **Coordinates**.

4 In the **x** text field, type -W/2.

5 In the **y** text field, type -dPeriod/2.

6 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.

7 In the **x** text field, type -W/2.

8 In the **y** text field, type dPeriod/2.

9 Locate the **Selections of Resulting Entities** section. Select the **Resulting objects selection** check box.

10 Right-click **Input Port** and choose **Duplicate**.

Output Port 1

1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** click **Input Port 1 (ls2)**.

2 In the **Settings** window for **Line Segment**, type Output Port 1 in the **Label** text field.

3 Locate the **Starting Point** section. In the **x** text field, type W/4-dPeriod/2*cos(pi*5/6).

4 In the **y** text field, type (W/2*2/sqrt(3)+sin(1/6*pi)*W/2*2/sqrt(3))/2-dPeriod/2*sin(pi*5/6).

5 Locate the **Endpoint** section. In the **x** text field, type W/4+dPeriod/2*cos(pi*5/6).

6 In the **y** text field, type (W/2*2/sqrt(3)+sin(1/6*pi)*W/2*2/sqrt(3))/2+dPeriod/2*sin(pi*5/6).

7 Right-click **Output Port 1** and choose **Duplicate**.

Output Port 2

1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** click **Output Port 1.1 (ls3)**.

2 In the **Settings** window for **Line Segment**, type Output Port 2 in the **Label** text field.

3 Locate the **Starting Point** section. In the **y** text field, type (-W/2*2/sqrt(3)-sin(1/6*pi)*W/2*2/sqrt(3))/2-dPeriod/2*sin(-pi*5/6).

4 Locate the **Endpoint** section. In the **y** text field, type (-W/2*2/sqrt(3)-sin(1/6*pi)*W/2*2/sqrt(3))/2+dPeriod/2*sin(-pi*5/6).

Circle Boundaries

1 In the **Geometry** toolbar, click ▧ **Selections** and choose **Adjacent Selection**.

2 In the **Settings** window for **Adjacent Selection**, type Circle Boundaries in the **Label** text field.

3 Locate the **Input Entities** section. Click ╬ **Add**.

4 In the **Add** dialog box, select **Circle 1** in the **Input selections** list.

5 Click **OK**.

Polygon Boundaries

1 In the **Geometry** toolbar, click **Selections** and choose **Adjacent Selection**.

2 In the **Settings** window for **Adjacent Selection**, type `Polygon Boundaries` in the **Label** text field.

3 Locate the **Input Entities** section. Click ╋ **Add**.

4 In the **Add** dialog box, select **Polygon 1** in the **Input selections** list.

5 Click **OK**.

Domain Boundaries

1 In the **Geometry** toolbar, click **Selections** and choose **Adjacent Selection**.

2 In the **Settings** window for **Adjacent Selection**, type `Domain Boundaries` in the **Label** text field.

3 Locate the **Input Entities** section. From the **Geometric entity level** list, choose **Boundary**.

4 Click ╋ **Add**.

5 In the **Add** dialog box, select **Polygon Boundaries** in the **Input selections** list.

6 Click **OK**.

7 In the **Settings** window for **Adjacent Selection**, locate the **Output Entities** section.

8 From the **Geometric entity level** list, choose **Adjacent domains**.

Moving Domains

1 In the **Geometry** toolbar, click **Selections** and choose **Complement Selection**.

2 In the **Settings** window for **Complement Selection**, type `Moving Domains` in the **Label** text field.

3 Locate the **Input Entities** section. Click ╋ **Add**.

4 In the **Add** dialog box, select **Domain Boundaries** in the **Selections to invert** list.

5 Click **OK**.

Free Shape Domains

1 In the **Geometry** toolbar, click **Selections** and choose **Disk Selection**.

2 In the **Settings** window for **Disk Selection**, type `Free Shape Domains` in the **Label** text field.

Form Union (fin)

1 In the **Model Builder** window, click **Form Union (fin)**.

2 In the **Settings** window for **Form Union/Assembly**, click **Build Selected**.

3 Click the ⬚ **Zoom Extents** button in the **Graphics** toolbar.

The model geometry is now complete.