

Sheet Metal Forming

Introduction

In sheet metal forming processes, the springback phenomena caused by the material elastic recovery behavior makes the formed part partially return to its original shape during the release of the forming load.

It is important to predict the springback accurately as the final deformed shape differs slightly from the shape given by the die at full forming load.

This model is a NAFEMS validation problem of sheet metal forming based on experimental data, see Ref. 1. The problem involves several nonlinearities such as boundary nonlinearity (contact), material nonlinearity (elastoplastic material) and geometric nonlinearity. Both 2D plane strain and 3D shell assumption are considered.

The target results consist in the forming angle, the angle after release, and the punch forces as function of the punch displacement.

Model Definition

The geometry consists of an assembly with three parts: the punch, the die, and a 1 mm metal sheet. Due to the symmetry, only one half of the geometry is represented for the 2D assumption and one quarter for the 3D one. Figure 1 shows the geometry used for the 3D problem, while Figure 2 shows the section cut used with the 2D plane strain problem.

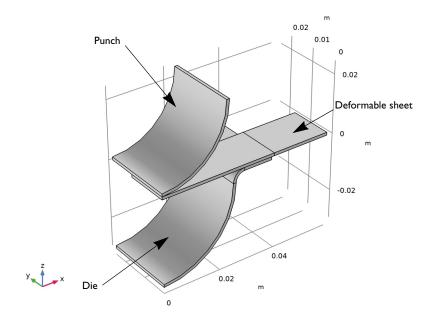


Figure 1: Model geometry: the punch at the top, the thin sheet in the middle, and the die at the bottom.

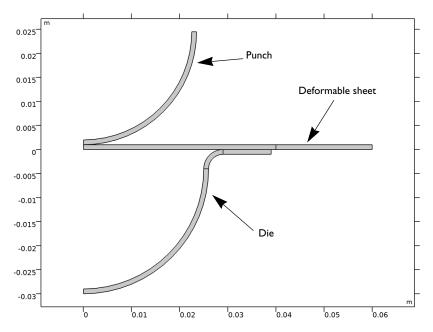


Figure 2: Section cut of the model geometry used for the 2D assumption.

The plane strain assumption is valid here, as the out-of-plane thickness of the sheet is large. Since the thickness of the plate is small compared to the curvature of the tool, moderate strains are expected even though the displacements and rotations are large.

The blank material used in the experiments is a 6111-T4 Aluminum alloy, having an isotropic Young's modulus of $70.5 \cdot 10^3$ MPa and a Poisson's ratio of 0.342. The yield stress of the material is 194 MPa and an Hollomon hardening function is used to represent the elastoplastic behavior. The Hollomon hardening function is a two-coefficient function described by

$$\sigma = K \varepsilon^n$$

Here K is 550.4 MPa and n is 0.223.

To improve the accuracy of the contact condition and forces, the augmented Lagrangian contact method is used. Friction between the thin sheet and the tools is defined using a Coulomb friction coefficient of 0.1342.

Experimental data for the forming angle and the angle after release are available, see Table 1.

TABLE I: ANGLE AT MAXIMUM PUNCH DISPLACEMENT AND AFTER RELEASE.

Forming angle (degrees)	Angle after release (degrees)
19.6–21.0	53.4–55.8

Data of the punch force are also available; these are stored in the text file sheet_metal_forming.txt available in the Nonlinear Structural Material Module's Application Library folder.

Results and Discussion

Figure 3 shows the residual stress distribution and deformed shape after the release for the problem including friction.

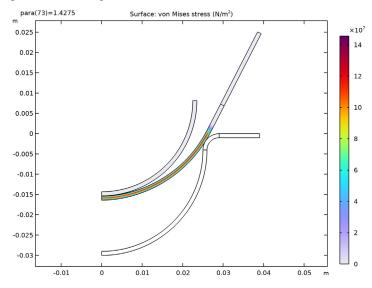


Figure 3: Von Mises stress and deformed shape after release for the 2D plane strain.

In Figure 4 you can see that the maximum value of the plastic strain is about 2%, which validates the small strain assumption.

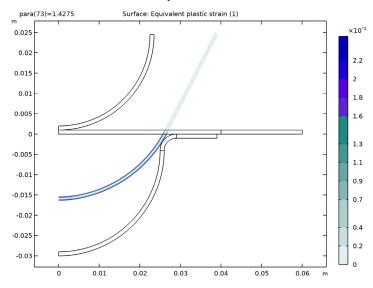


Figure 4: Equivalent plastic strain at maximum punch deflection.

Figure 5 and Figure 6 show the von Mises stress in the sheet computed with a 3D shell assumption. Notice the stress distribution along the y-direction that cannot be evaluated with the 2D plane strain assumption.

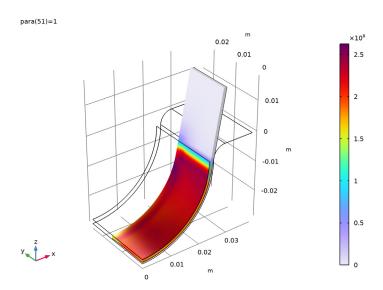


Figure 5: Von Mises stress and deformed shape at forming for the 3D shell problem.

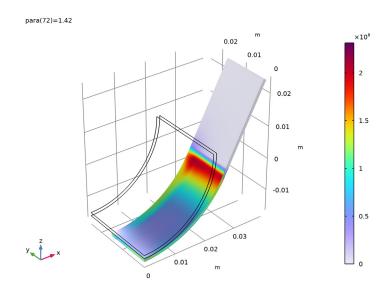


Figure 6: Von Mises stress and deformed shape after release for the 3D shell problem.

The computed angle at the maximum punch displacement and after release are listed in Table 2. These values are in good agreement with the experimental data and the numerical results discussed in Ref. 1.

TABLE 2: COMPUTED ANGLE AT MAXIMUM PUNCH DISPLACEMENT AND AFTER RELEASE.

	Forming angle (degrees)	Angle after release (degrees)
Without friction	20.6	46.0
With friction	20.5	53.9
With friction (shell)	21.6	54.4

Figure 7 shows the punch forces versus the punch displacement. One can clearly notice the effect of friction in the applied load. Furthermore, the blank remains in contact with the tools much longer when friction forces are included.

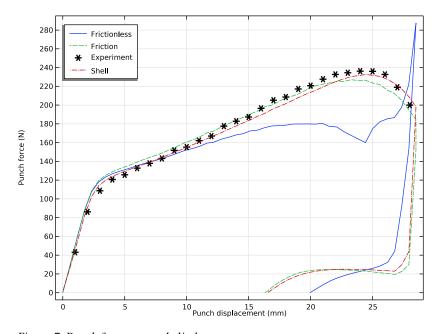


Figure 7: Punch force vs. punch displacement.

In the model without friction the computed forces in the forming process have two peaks. The forces keep on increasing to get the blank within the die; when the blank is sufficiently deformed, it requires a lower force to push down the blank in die. Just before the punch reaches the forming shape, the blank touches the bottom of the die and the force increases significantly to finish the forming step. In the release step, the punch forces keep decreasing with the punch going back to its original position.

When friction is added, the applied load history differs significantly. First of all, it requires higher loads to get the blank into the die. Secondly, only one peak is observed during the forming step, since the blank never touches the bottom of the die. During the release step, a maximum is also observed, which is explained by the friction force.

Figure 8 shows the position of the blank in the die for the frictionless problem. On the left side, the punch goes into the die (from top to bottom), this is the forming stage. On the right side, you can see the release stage when the punch is removed from the die (from top to bottom).

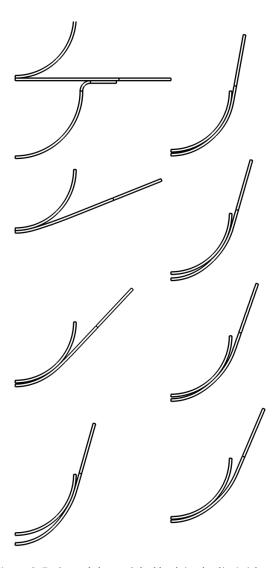


Figure 8: Deformed shape of the blank in the die (without friction).

Figure 9 shows the position of the blank in the die for the problem including friction. On the left side the punch goes into the die (from top to bottom). On the right side you can see the release stage when the punch is removed from the die (from top to bottom).

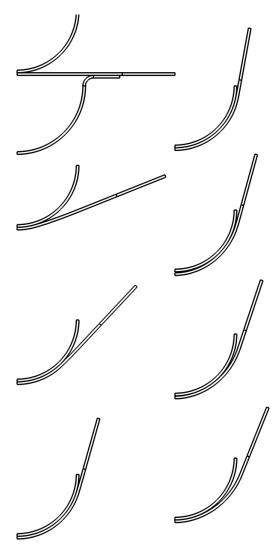


Figure 9: Deformed shape of the blank in the die (including friction).

Notes About the COMSOL Implementation

In the benchmark problem as described in Ref. 1, the plastic hardening is represented with the Hollomon law. Hollomon hardening is a good representation of material hardening for large strains. In the small strain region, however, the computed stress is negative. To

ensure the continuity between the elastic and the hardening material behavior, you use the tangent of the Hollomon curve to match no stress hardening at zero equivalent plastic strain.

Figure 10 shows the difference between the Hollomon hardening with the parameters provided in the model description and the hardening function including the smoothed transition used to implement the numerical model.

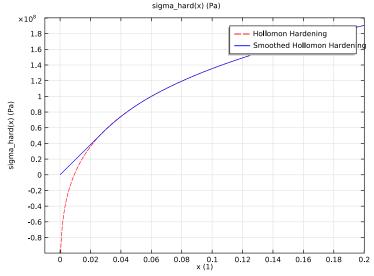


Figure 10: Hollomon hardening with smooth transition (blue) and without (dashed red).

Due to the combination of contact with friction, the elastoplastic material model, and geometric nonlinearity, the model requires manual contact and solver settings to obtain good convergence. Furthermore, the blank becomes unstable in the tool for certain deformation. To circumvent numerical problems, follow the suggestions below:

• Use manual tuning to define the penalty factor and disable relaxation to ensure a constant normal penalty factor. The default settings use softer penalty factor at every initial segregated iteration. Here use a constant value to keep the same stiffness between the initial guess and the computed solution. Using the penalty factor multiplier you can influence the convergence rate, a low value of the penalty factor multiplier improve the convergence at the cost of extra computation time, while a higher value speed up the computation. For this problem different values for the penalty factor multiplier are used: in the 2D case a value of 0.1 for the contact between the punch and the sheet and 0.02 for the contact between the die and the sheet. For the 3D case, the penalty factor for the contact between the punch and the sheet is set to 0.05.

Reference

1. A.W.A. Konter, Advanced Finite Element Contact Benchmarks, NAFEMS, 2006.

Application Library path: Nonlinear Structural Materials Module/ Plasticity/sheet metal forming

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click \Longrightarrow Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click M Done.

GLOBAL DEFINITIONS

Load all model parameters from a file containing parameters for the geometry and some material properties.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file sheet_metal_forming_parameters.txt.

PART I

I In the Model Builder window, right-click Global Definitions and choose Geometry Parts> 2D Part.

"Now build a 2D section of the model geometry, starting with the blank geometry.

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type L.
- **4** In the **Height** text field, type th.

Add an extra domain to get better mesh control in the blank.

5 Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	40[mm]

- 6 Select the Layers to the left check box.
- 7 Clear the Layers on bottom check box.
- 8 Click | Build Selected.

Continue with the punch geometry.

Circle I (c1)

- I In the **Geometry** toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type R1.
- 4 In the Sector angle text field, type 90.
- **5** Locate the **Position** section. In the **y** text field, type R1+th.
- 6 Locate the Rotation Angle section. In the Rotation text field, type -90.
- 7 Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	th

8 Click | Build Selected.

Finally, draw the die geometry.

Circle 2 (c2)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type R2+th.
- 4 In the Sector angle text field, type 90.
- **5** Locate the **Position** section. In the **y** text field, type -R3.
- 6 Locate the Rotation Angle section. In the Rotation text field, type -90.
- 7 Locate the Layers section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	th

8 Click | Build Selected.

Circle 3 (c3)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type R3.
- 4 In the Sector angle text field, type 90.
- **5** Locate the **Position** section. In the **x** text field, type R2+R3.
- 6 In the y text field, type -R3.
- 7 Locate the Rotation Angle section. In the Rotation text field, type 90.
- **8** Locate the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	th

9 Click | Build Selected.

Rectangle 2 (r2)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 1 [cm].
- 4 In the Height text field, type th.
- **5** Locate the **Position** section. In the **x** text field, type R2+R3.
- **6** In the **y** text field, type -th.

7 Click | Build Selected.

Delete Entities I (dell)

- I In the Model Builder window, right-click Part I and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Geometric entity level list, choose Domain.
- 4 On the object c1, select Domain 1 only.
- **5** On the object **c2**, select Domain 1 only.
- **6** On the object **c3**, select Domain 1 only.
- 7 Click | Build Selected.

Union I (uni I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects dell(2), dell(3), and r2 only.

GEOMETRY I

Part Instance I (bil)

- I In the Geometry toolbar, click Part Instance and choose Part I.
- 2 In the Settings window for Part Instance, click **Part Build Selected**.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Clear the Create pairs check box.
- 5 Click | Build Selected.

DEFINITIONS

You can now add contact pairs to define on which boundary you expect the contact to happen.

Contact Pair I (pl)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 Select Boundary 20 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.

- **4** Click to select the **Activate Selection** toggle button.
- **5** Select Boundary 13 only.

Contact Pair 2 (p2)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 Select Boundaries 5, 8, and 9 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.
- **4** Click to select the **Activate Selection** toggle button.
- **5** Select Boundary 12 only.

GLOBAL DEFINITIONS

To define the punch displacement for the loading and the unloading stages, use an interpolation function that makes the displacement a function of a monotonic parameter.

Interpolation I (int I)

- I In the **Definitions** toolbar, click \bigwedge Interpolation.
- 2 In the Settings window for Interpolation, locate the Definition section.
- 3 In the Function name text field, type punch.
- **4** In the table, enter the following settings:

t	f(t)
0	0
0.98	-punch_max
1	-punch_max
2	0

5 Locate the **Units** section. In the **Function** table, enter the following settings:

Function	Unit
punch	mm

6 In the **Argument** table, enter the following settings:

Argument	Unit	
t	1	

ADD MATERIAL

I In the Home toolbar, click 🙀 Add Material to open the Add Material window.

- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Structural steel.
- 4 Right-click and choose Add to Global Materials.
- 5 In the Home toolbar, click **‡ Add Material** to close the **Add Material** window.

GLOBAL DEFINITIONS

Material 2 (mat2)

In the Model Builder window, under Global Definitions right-click Materials and choose Blank Material.

MATERIALS

Material Link I (matlnk I)

In the Model Builder window, under Component I (compl) right-click Materials and choose More Materials>Material Link.

Material Link 2 (matlnk2)

- I Right-click Materials and choose More Materials>Material Link.
- **2** Select Domains 4 and 5 only.
- 3 In the Settings window for Material Link, locate the Link Settings section.
- 4 From the Material list, choose Material 2 (mat2).

GLOBAL DEFINITIONS

Material 2 (mat2)

- I In the Model Builder window, under Global Definitions>Materials click Material 2 (mat2).
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	70.5[kN/mm^2]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.342	l	Young's modulus and Poisson's ratio
Density	rho	2700[kg/m^3]	kg/m³	Basic

- 4 Click to expand the Material Properties section. In the Material properties tree, select Solid Mechanics>Elastoplastic Material>Elastoplastic Material Model> Initial yield stress (sigmags).
- 5 Click + Add to Material.
- **6** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Initial yield stress	sigmags	sigma0	Pa	Elastoplastic material model

Use a piecewise constant function to define the hardening function with a smooth transition. At small equivalent plastic strain (lower than 3%) use a linear function; at higher values, use the Hollomon hardening function.

Piecewise I (pw I)

- I In the Model Builder window, expand the Material 2 (mat2) node.
- 2 Right-click Global Definitions>Materials>Material 2 (mat2)> Elastoplastic material model (ElastoplasticModel) and choose Functions>Piecewise.
- 3 In the Settings window for Piecewise, type sigma_hard in the Function name text field.
- 4 Locate the **Definition** section. From the **Extrapolation** list, choose **None**.
- 5 From the Smoothing list, choose Continuous first derivative.
- **6** Find the **Intervals** subsection. In the table, enter the following settings:

Start	End	Function
0	eps0	(K*eps0^n-sigma0)/eps0*x
eps0	0.5	K*x^n-sigma0

- 7 Locate the **Units** section. In the **Arguments** text field, type 1.
- 8 In the Function text field, type Pa.
- 9 Locate the Definition section. From the Extrapolation list, choose Nearest function.

Material 2 (mat2)

- I In the Model Builder window, under Global Definitions>Materials>Material 2 (mat2) click Elastoplastic material model (ElastoplasticModel).
- 2 In the Settings window for Elastoplastic Material Model, locate the Model Inputs section.
- 3 Click + Select Quantity.
- 4 In the Physical Quantity dialog box, type plastic strain in the text field.

- 5 Click **Filter**.
- 6 In the tree, select Solid Mechanics>Equivalent plastic strain (1).
- 7 Click OK.
- 8 In the Model Builder window, click Material 2 (mat2).
- 9 In the Settings window for Material, locate the Material Contents section.
- **10** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Hardening function	sigmagh	sigma_hard (epe)	Pa	Elastoplastic material model

SOLID MECHANICS (SOLID)

- I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).
- **2** Select Domains 4–6 only.
- 3 In the Settings window for Solid Mechanics, locate the Thickness section.
- **4** In the d text field, type w sheet.

Linear Elastic Material I

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.

Plasticity 1

- I In the Physics toolbar, click Attributes and choose Plasticity.
- 2 Select Domains 4 and 5 only.
- 3 In the Settings window for Plasticity, locate the Plasticity Model section.
- 4 Find the Isotropic hardening model subsection. From the list, choose Hardening function.

Symmetry I

- I In the Physics toolbar, click Boundaries and choose Symmetry.
- 2 Select Boundaries 1, 11, and 18 only.

Prescribed Displacement I

- I In the Physics toolbar, click **Domains** and choose **Prescribed Displacement**.
- 2 Select Domain 6 only.
- 3 In the Settings window for Prescribed Displacement, locate the Prescribed Displacement section.
- 4 From the Displacement in x direction list, choose Prescribed.

- 5 From the Displacement in y direction list, choose Prescribed.
- **6** In the u_{0y} text field, type punch (para).

For such a problem (using continuation parameter), a constant penalty factor is preferred. Set it with a lower value than the default to improve the stability.

Contact I

- I In the Model Builder window, click Contact I.
- 2 In the Settings window for Contact, locate the Contact Method section.
- 3 From the list, choose Augmented Lagrangian.
- 4 Locate the Contact Pressure Penalty Factor section. From the Penalty factor control list, choose Manual tuning.
- **5** In the f_p text field, type 0.1.
- 6 From the Use relaxation list, choose Never.
- 7 Right-click Contact I and choose Duplicate.

Contact 2

- I In the Model Builder window, click Contact 2.
- 2 In the Settings window for Contact, locate the Pair Selection section.
- 3 Under Pairs, click + Add.
- 4 In the Add dialog box, select Contact Pair 2 (p2) in the Pairs list.
- 5 Click OK.
- 6 In the Settings window for Contact, locate the Contact Pressure Penalty Factor section.
- 7 In the $f_{\rm D}$ text field, type 2e-2.

MESH I

Mapped I

In the Mesh toolbar, click Mapped.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 Select Boundary 13 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 50.

Distribution 2-5

1 Proceed to add four additional distributions with the following settings:

Name	Boundary	Number of elements
Distribution 2	1, 18	1
Distribution 3	8 20	25
Distribution 4	11	5
Distribution 5	9	10

2 Click Build All.

DEFINITIONS

The blank deformation angle is the slope of the line between the points (4e-2, 0) and (6e-2,0). Use integration coupling variables to evaluate the spatial coordinates at these points.

Integration I (intob1)

- I In the Definitions toolbar, click // Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 11 only.

Integration 2 (intob2)

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 13 only.

Variables 1

- I In the **Definitions** toolbar, click **a= Local Variables**.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
angle	<pre>2*atan((intop2(x)-intop1(x))/ (intop2(y)-intop1(y)))</pre>	rad	Blank deformation angle

FRICTIONLESS

I In the Model Builder window, click Study I.

2 In the Settings window for Study, type Frictionless in the Label text field.

Step 1: Stationary

- I In the Model Builder window, under Frictionless click Step 1: Stationary.
- 2 In the Settings window for Stationary, click to expand the Results While Solving section.
- **3** Select the **Plot** check box. Set up an auxiliary continuation sweep for the para parameter.
- 4 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 5 Click + Add.
- **6** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Punch displacement parameter)	1e-4 range(2e-2,2e-2, 1.5)	

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
- 3 In the Model Builder window, expand the Frictionless>Solver Configurations> Solution I (soll)>Stationary Solver I node, then click Parametric I.
- 4 In the Settings window for Parametric, click to expand the Continuation section.
- **5** Select the **Tuning of step size** check box.
- 6 In the Initial step size text field, type 1e-4.
- 7 In the Minimum step size text field, type 1e-4.
- 8 In the Maximum step size text field, type 2e-2.
- 9 From the Predictor list, choose Linear.
- 10 Right-click Frictionless>Solver Configurations>Solution I (soll)>Stationary Solver I> Parametric I and choose Stop Condition.
- II In the Settings window for Stop Condition, locate the Stop Expressions section.
- 12 Click + Add.

I3 In the table, enter the following settings:

Stop expression	Stop if	Active	Description
min(comp1.solid.Tnm ax_p1, comp1.solid.Tnmax_p 2)-(para>1)	Negative (<0)	V	Stop expression 1

14 Locate the Output at Stop section. From the Add solution list, choose Step after stop.

I5 Clear the **Add warning** check box.

16 Click **Compute**.

RESULTS

Stress (Frictionless)

The default plot shows the von Mises stress, equivalent plastic strain, and contact pressure after the release. For better clarity, disable the equivalent plastic strain, which will be plotted separately.

- I In the Settings window for 2D Plot Group, type Stress (Frictionless) in the Label

ADD PREDEFINED PLOT

- In the Home toolbar, click Add Predefined Plot to open the Add Predefined Plot window.
- 2 Go to the Add Predefined Plot window.
- 3 In the tree, select Frictionless/Solution I (soll)>Solid Mechanics> Equivalent Plastic Strain (solid).
- 4 Click Add Plot in the window toolbar.

RESULTS

Deformation I

- I In the Model Builder window, expand the Equivalent Plastic Strain (solid) node.
- 2 Right-click Surface I and choose Deformation.
- 3 In the Settings window for Deformation, locate the Scale section.
- **4** Select the **Scale factor** check box. In the associated text field, type 1.

Evaluate the forming angle and the angle after release.

The instruction below shows how to evaluate the forming angle and the angle after release.

Deformation Angle (Frictionless)

- I In the Model Builder window, expand the Results>Datasets node.
- 2 Right-click Results>Derived Values and choose Global Evaluation.
- 3 In the Settings window for Global Evaluation, type Deformation Angle (Frictionless) in the Label text field.
- 4 Locate the Data section. From the Parameter selection (para) list, choose From list.
- 5 In the Parameter values (para) list, choose I and I.3.
- 6 Click Replace Expression in the upper-right corner of the Expressions section. From the menu, choose Component I (compl)>Definitions>Variables>angle -Blank deformation angle - rad.
- 7 Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description	
angle	deg	Blank deformation angle	

8 Click = Evaluate.

Deformation Angle (Frictionless)

- I In the Model Builder window, expand the Results>Tables node, then click Table I.
- 2 In the Settings window for Table, type Deformation Angle (Frictionless) in the **Label** text field.

Now plot the punch forces versus the punch displacement as in Figure 7.

Punch Force vs. Displacement

- I In the Results toolbar, click \(\subseteq ID Plot Group. \)
- 2 In the Settings window for ID Plot Group, type Punch Force vs. Displacement in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose None.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the **Plot Settings** section.
- 6 Select the x-axis label check box. In the associated text field, type Punch displacement (mm).
- 7 Select the y-axis label check box. In the associated text field, type Punch force (N).

8 Locate the Legend section. From the Position list, choose Upper left.

Global I

- I Right-click Punch Force vs. Displacement and choose Global.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Frictionless/Solution I (soll).
- 4 Locate the y-Axis Data section. In the table, enter the following settings:

Expression	Unit	Description
2*solid.dcnt2.T_toty	N	

- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **6** In the **Expression** text field, type -punch(para).
- **7** From the **Unit** list, choose **mm**.
- 8 Click to expand the Legends section. From the Legends list, choose Manual.
- **9** In the table, enter the following settings:

Legends	
Frictionless	

10 In the Punch Force vs. Displacement toolbar, click **10** Plot.

Now include friction in the problem.

SOLID MECHANICS (SOLID)

Contact I

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Contact I.

Friction 1

- I In the Physics toolbar, click ___ Attributes and choose Friction.
- 2 In the Settings window for Friction, locate the Friction Parameters section.
- 3 In the μ text field, type 0.1348.

Contact 2

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Contact 2.

Friction 1

- I In the Physics toolbar, click Attributes and choose Friction.
- 2 In the Settings window for Friction, locate the Friction Parameters section.
- 3 In the μ text field, type 0.1348.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

FRICTION

- I In the Model Builder window, click Study 2.
- 2 In the Settings window for Study, type Friction in the Label text field.

Step 1: Stationary

- I In the Model Builder window, under Friction click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Results While Solving section.
- **3** Select the **Plot** check box.
- 4 From the Plot group list, choose Default.
- 5 Locate the Study Extensions section. Select the Auxiliary sweep check box.
- 6 Click + Add.
- 7 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Punch displacement parameter)	1e-4 range(2e-2,2e-2, 1.5)	

Solution 2 (sol2)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution 2 (sol2) node.
- 3 In the Model Builder window, expand the Friction>Solver Configurations> Solution 2 (sol2)>Stationary Solver I node, then click Parametric I.
- 4 In the Settings window for Parametric, locate the Continuation section.
- **5** Select the **Tuning of step size** check box.

- 6 In the Initial step size text field, type 2e-2.
- 7 In the Minimum step size text field, type 1e-5.
- 8 In the Maximum step size text field, type 2e-2.
- 9 From the Predictor list, choose Linear.
- 10 Right-click Friction>Solver Configurations>Solution 2 (sol2)>Stationary Solver 1> Parametric I and choose Stop Condition.
- II In the Settings window for Stop Condition, locate the Stop Expressions section.
- 12 Click + Add.
- **I3** In the table, enter the following settings:

Stop expression	Stop if	Active	Description
min(comp1.solid.Tnm ax_p1, comp1.solid.Tnmax_p 2)-(para>1)	Negative (<0)	V	Stop expression 1

- 14 Locate the Output at Stop section. From the Add solution list, choose Step after stop.
- **15** Clear the **Add warning** check box.
- 16 In the Study toolbar, click In the Study toolbar, click In the Study toolbar, click

Steb 1: Stationary

- I In the Model Builder window, under Friction click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Results While Solving section.
- 3 From the Plot group list, choose Stress (solid).
- 4 In the Study toolbar, click **Compute**.

RESULTS

Stress (Friction)

- I In the Settings window for 2D Plot Group, type Stress (Friction) in the Label text field.
- 2 In the Stress (Friction) toolbar, click Plot.

ADD PREDEFINED PLOT

- I Go to the Add Predefined Plot window.
- 2 In the tree, select Friction/Solution 2 (sol2)>Solid Mechanics> Equivalent Plastic Strain (solid).

3 Click Add Plot in the window toolbar.

RESULTS

Deformation I

- I In the Model Builder window, expand the Equivalent Plastic Strain (solid) I node.
- 2 Right-click Surface I and choose Deformation.
- 3 In the Settings window for Deformation, locate the Scale section.
- 4 Select the Scale factor check box. In the associated text field, type 1.
- 5 In the Equivalent Plastic Strain (solid) I toolbar, click Plot.

You can now evaluate the angle at the forming and after-release stages.

Deformation Angle (Frictionless)

In the Model Builder window, under Results>Derived Values right-click Deformation Angle (Frictionless) and choose Duplicate.

Deformation Angle (Friction)

- In the Model Builder window, under Results>Derived Values click
 Deformation Angle (Frictionless) 1.
- 2 In the Settings window for Global Evaluation, type Deformation Angle (Friction) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Friction/Solution 2 (sol2).
- 4 In the Parameter values (para) list, choose I and I.42.
- 5 Click ▼ next to **= Evaluate**, then choose **New Table**.

Deformation Angle (Friction)

- I In the Model Builder window, under Results>Tables click Table 2.
- 2 In the Settings window for Table, type Deformation Angle (Friction) in the Label text field.

Global I

In the Model Builder window, under Results>Punch Force vs. Displacement right-click Global I and choose Duplicate.

Global 2

- I In the Model Builder window, click Global 2.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Friction/Solution 2 (sol2).

- 4 Click to expand the Coloring and Style section. Find the Line style subsection. From the Line list, choose Dashed.
- **5** Locate the **Legends** section. In the table, enter the following settings:

Legends Friction

6 In the Punch Force vs. Displacement toolbar, click **Plot**.

Add a table in which to store the benchmark experimental data.

Punch Force (Experiment)

- I In the Results toolbar, click **Table**.
- 2 In the Settings window for Table, type Punch Force (Experiment) in the Label text field.
- 3 Locate the Data section. Click Import.
- **4** Browse to the model's Application Libraries folder and double-click the file sheet metal forming.txt.

Experiment

- I In the Model Builder window, right-click Punch Force vs. Displacement and choose Table Graph.
- 2 In the Settings window for Table Graph, type Experiment in the Label text field.
- 3 Locate the Data section. From the Table list, choose Punch Force (Experiment).
- 4 Locate the Coloring and Style section. Find the Line style subsection. From the Line list, choose None.
- **5** From the **Color** list, choose **From theme**.
- 6 Find the Line markers subsection. From the Marker list, choose Cycle.
- 7 Click to expand the **Legends** section. Select the **Show legends** check box.
- 8 From the Legends list, choose Manual.
- **9** In the table, enter the following settings:

Legends Experiment

10 In the **Punch Force vs. Displacement** toolbar, click **Plot**.

Friction is now included in the model. To compute the solution without friction in the first study again, you need to make sure that the friction nodes are disabled in the model for this specific study. This is convenient if you need to close the model and reopen it later.

FRICTIONLESS

Step 1: Stationary

- I In the Model Builder window, under Frictionless click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 3 Select the Modify model configuration for study step check box.
- 4 In the tree, select Component I (compl)>Solid Mechanics (solid), Controls spatial frame> Contact I>Friction I.
- 5 Right-click and choose Disable.
- 6 In the tree, select Component I (compl)>Solid Mechanics (solid), Controls spatial frame> Contact 2>Friction 1.
- 7 Right-click and choose Disable.

ADD COMPONENT

In the Model Builder window, right-click the root node and choose Add Component>3D.

GEOMETRY 2

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose xz-plane.
- **4** Locate the **Unite Objects** section. Clear the **Unite objects** check box.

Work Plane I (wbl)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wpl)>Part Instance I (pil)

- I In the Work Plane toolbar, click Part Instance and choose Part I.
- 2 In the Settings window for Part Instance, click | Build Selected.
- 3 Click the **Zoom Extents** button in the **Graphics** toolbar.

Extrude | (extl)

- I In the Model Builder window, under Component 2 (comp2)>Geometry 2 right-click Work Plane I (wpl) and choose Extrude.
- 2 Select the object wpl.pil(1) only.
- 3 In the Settings window for Extrude, locate the Distances section.
- **4** In the table, enter the following settings:

Distances (m) w sheet/2

- **5** Select the **Reverse direction** check box.
- 6 Click Pauld Selected.

Extrude 2 (ext2)

- I In the Geometry toolbar, click **Extrude**.
- 2 In the Settings window for Extrude, locate the Distances section.
- **3** In the table, enter the following settings:

Distances (m) w_tools/2

- 4 Select the Reverse direction check box.
- 5 Click | Build Selected.

Form Union (fin)

- I In the Model Builder window, under Component 2 (comp2)>Geometry 2 click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Clear the Create pairs check box.

DEFINITIONS (COMP2)

Contact Pair 3 (p3)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 Select Boundary 30 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.
- **4** Click to select the **Activate Selection** toggle button.

5 Select Boundary 19 only.

Contact Pair 4 (p4)

- I In the **Definitions** toolbar, click **Pairs** and choose **Contact Pair**.
- 2 Select Boundaries 4, 7, and 14 only.
- 3 In the Settings window for Pair, locate the Destination Boundaries section.
- **4** Click to select the **Activate Selection** toggle button.
- **5** Select Boundary 19 only.

GLOBAL DEFINITIONS

Material 2 (mat2)

In the Model Builder window, under Global Definitions>Materials right-click Material 2 (mat2) and choose Duplicate.

Material 3 (mat3)

- I In the Model Builder window, click Material 3 (mat3).
- 2 In the Settings window for Material, click to expand the Material Properties section.
- 3 In the Material properties tree, select Geometric Properties>Shell.
- 4 Click + Add to Material.
- **5** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Isotropic tangent modulus	Et		Pa	Elastoplastic material model
Kinematic tangent modulus	Ek		Pa	Elastoplastic material model
Thickness	lth	th	m	Shell
Density	rho	2700[kg/ m^3]	kg/m³	Basic
Young's modulus	Е	70.5[kN/ mm^2]	Pa	Young's modulus and Poisson's ratio
Poisson's ratio	nu	0.342	I	Young's modulus and Poisson's ratio
Initial yield stress	sigmags	sigma0	Pa	Elastoplastic material model
Hardening function	sigmagh	sigma_hard (epe)	Pa	Elastoplastic material model

Property	Variable	Value	Unit	Property group
Hill's coefficients	{Hillcoefficients I, Hillcoefficients 2, Hillcoefficients 3, Hillcoefficients 4, Hillcoefficients 5, Hillcoefficients 6}	{0, 0, 0, 0, 0, 0, 0, 0, 0}	m²·s ⁴ /kg²	Elastoplastic material model
Initial tensile and shear yield stresses	{ys1, ys2, ys3, ys4, ys5, ys6}	{0, 0, 0, 0, 0, 0, 0, 0, 0}	N/m²	Elastoplastic material model
Rotation	Irot	0.0	deg	Shell
Mesh elements	Ine	2	ı	Shell

MATERIALS

Material Link 3 (matlnk3)

- I In the Model Builder window, under Component 2 (comp2) right-click Materials and choose More Materials>Material Link.
- 2 In the Settings window for Material Link, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 30 only.

GLOBAL DEFINITIONS

Material 3 (mat3)

In the Model Builder window, under Global Definitions>Materials right-click Material 3 (mat3) and choose Copy.

MATERIALS

In the Model Builder window, under Component 2 (comp2) right-click Materials and choose Paste Material.

Material 3 (mat4)

- I In the Model Builder window, under Component 2 (comp2)>Materials click Material 3 (mat4).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundaries 19 and 24 only.

ADD PHYSICS

- I In the Home toolbar, click Add Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Structural Mechanics>Shell (shell).
- 4 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Frictionless and Friction.
- 5 Click Add to Component 2 in the window toolbar.
- 6 In the Home toolbar, click and Physics to close the Add Physics window.

SHELL (SHELL)

- I In the Settings window for Shell, locate the Boundary Selection section.
- 2 Click Clear Selection.
- 3 Select Boundaries 19, 24, and 30 only.

Thickness and Offset I

- I In the Model Builder window, under Component 2 (comp2)>Shell (shell) click Thickness and Offset I.
- 2 In the Settings window for Thickness and Offset, locate the Thickness and Offset section.
- **3** In the d_0 text field, type th.
- 4 From the Position list, choose Top surface on boundary.

Linear Elastic Material, Layered 1

- I In the Physics toolbar, click Boundaries and choose Linear Elastic Material, Layered.
- **2** Select Boundaries 19 and 24 only.

MATERIALS

Material 3 (mat4)

- I In the Model Builder window, under Component 2 (comp2)>Materials click Material 3 (mat4).
- 2 In the Settings window for Material, locate the Orientation and Position section.
- 3 From the Coordinate system list, choose Boundary System 2 (sys2).
- 4 From the Position list, choose Top side on boundary.

SHELL (SHELL)

Linear Elastic Material, Layered I

- I Click the Show More Options button in the Model Builder toolbar.
- 2 In the Show More Options dialog box, in the tree, select the check box for the node Physics>Advanced Physics Options.
- 3 Click OK.
- 4 In the Model Builder window, under Component 2 (comp2)>Shell (shell) click Linear Elastic Material, Layered I.
- 5 In the Settings window for Linear Elastic Material, Layered, click to expand the Out-of-Plane Strain section.
- 6 Select the Solve for out-of-plane strain components check box.

Plasticity 1

- I In the Physics toolbar, click 🕞 Attributes and choose Plasticity.
- 2 Select Boundaries 19 and 24 only.
- 3 In the Settings window for Plasticity, locate the Plasticity Model section.
- 4 Find the Isotropic hardening model subsection. From the list, choose Hardening function.

Prescribed Displacement/Rotation 1

- I In the Physics toolbar, click **Boundaries** and choose Prescribed Displacement/ Rotation.
- 2 Select Boundary 30 only.
- 3 In the Settings window for Prescribed Displacement/Rotation, locate the Prescribed Displacement section.
- 4 From the Displacement in x direction list, choose Prescribed.
- 5 From the Displacement in y direction list, choose Prescribed.
- 6 From the Displacement in z direction list, choose Prescribed.
- **7** In the u_{0z} text field, type punch (para).

Symmetry I

- I In the Physics toolbar, click **Edges** and choose Symmetry.
- 2 Select Edges 30, 31, and 39 only.

Contact I

- I In the Model Builder window, click Contact I.
- 2 In the Settings window for Contact, locate the Contact Surface section.

- 3 From the Contact surface, destination list, choose Bottom.
- 4 Locate the Contact Pressure Penalty Factor section. From the Penalty factor control list, choose Automatic, soft.

Friction 1

- I In the Physics toolbar, click 🖳 Attributes and choose Friction.
- 2 In the Settings window for Friction, locate the Friction Parameters section.
- 3 In the μ text field, type 0.1342.
- 4 Locate the Friction Force Penalty Factor section. From the Penalty factor control list, choose From parent.

Contact I

Right-click Contact I and choose Duplicate.

Contact 2

- I In the Model Builder window, click Contact 2.
- 2 In the Settings window for Contact, locate the Pair Selection section.
- 3 Under Pairs, click + Add.
- 4 In the Add dialog box, select Contact Pair 4 (p4) in the Pairs list.
- 5 Click OK.
- 6 In the Settings window for Contact, locate the Contact Surface section.
- 7 From the Contact surface, destination list, choose Top.

MESH 2

Mapped I

- I In the Mesh toolbar, click More Generators and choose Mapped.
- **2** Select Boundaries 4, 7, 14, 19, 24, and 30 only.

Distribution I

- I Right-click Mapped I and choose Distribution.
- **2** Select Edges 1, 4, 21, 49, and 50 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 1.

Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- **2** Select Edges 5 and 51 only.

- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 25.

Distribution 3

- I Right-click Mapped I and choose Distribution.
- **2** Select Edge 11 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 10.

Distribution 4

- I Right-click Mapped I and choose Distribution.
- **2** Select Edge 31 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 50.

Distribution 5

- I Right-click Mapped I and choose Distribution.
- **2** Select Edge 30 only.
- 3 In the Settings window for Distribution, click | Build Selected.

DEFINITIONS (COMP2)

Integration 3 (intob3)

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 21 only.

Integration 4 (intob4)

- I In the **Definitions** toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 25 only.

Variables 2

- I In the Model Builder window, right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.

3 In the table, enter the following settings:

Name	Expression	Unit	Description
angle_shell	<pre>2*atan((intop4(x)-intop3(x))/ (intop4(z)-intop3(z)))</pre>	rad	Blank deformation angle (shell)

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Find the Physics interfaces in study subsection. In the table, clear the Solve check box for Solid Mechanics (solid).
- 5 Click Add Study in the window toolbar.
- 6 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 3

Steb 1: Stationary

- I In the Settings window for Stationary, locate the Study Extensions section.
- 2 Select the Auxiliary sweep check box.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Punch displacement parameter)	1e-4 range(2e-2,2e-2, 1.5)	

- 5 In the Model Builder window, click Study 3.
- 6 In the Settings window for Study, type Friction (shell) in the Label text field.

Solution 3 (sol3)

- 2 In the Model Builder window, expand the Solution 3 (sol3) node.
- 3 In the Model Builder window, expand the Friction (shell)>Solver Configurations> Solution 3 (sol3)>Stationary Solver I node, then click Parametric I.
- 4 In the Settings window for Parametric, locate the Continuation section.

- **5** Select the **Tuning of step size** check box.
- 6 In the Initial step size text field, type 2e-2.
- 7 In the Minimum step size text field, type 1e-5.
- 8 In the Maximum step size text field, type 2e-2.
- 9 From the Predictor list, choose Linear.
- 10 Right-click Friction (shell)>Solver Configurations>Solution 3 (sol3)>Stationary Solver I> Parametric I and choose Stop Condition.
- II In the Settings window for Stop Condition, locate the Stop Expressions section.
- 12 Click + Add.
- **13** In the table, enter the following settings:

Stop expression	Stop if	Active	Description
min(comp2.shell.Tnm ax_p3, comp2.shell.Tnmax_p 4)-(para>1)	Negative (<0)	V	Stop expression 1

- 14 Locate the Output at Stop section. From the Add solution list, choose Step after stop.
- **I5** Clear the **Add warning** check box.
- 16 In the Study toolbar, click In Show Default Plots.

Steb 1: Stationary

- I In the Model Builder window, under Friction (shell) click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Results While Solving section.
- **3** Select the **Plot** check box.
- 4 From the Plot group list, choose Stress (shell).
- 5 In the Study toolbar, click **Compute**.

RESULTS

Surface I

- I In the Model Builder window, expand the Stress (shell) node.
- 2 Right-click Surface I and choose Delete.

Stress (shell)

- I In the Model Builder window, under Results click Stress (shell).
- 2 In the Stress (shell) toolbar, click **Plot**.

- 3 In the Settings window for 3D Plot Group, locate the Data section.
- 4 From the Dataset list, choose Friction (shell)/Solution 3 (4) (sol3).
- 5 From the Parameter value (para) list, choose 1.

Surface 2

- I In the Model Builder window, click Surface 2.
- 2 In the Stress (shell) toolbar, click Plot.

ADD PREDEFINED PLOT

- I Go to the Add Predefined Plot window.
- 2 In the tree, select Friction (shell)/Solution 3 (4) (sol3)>Shell> Equivalent Plastic Strain (shell).
- 3 Click Add Plot in the window toolbar.
- 4 In the Home toolbar, click Add Predefined Plot to close the Add Predefined Plot window.

RESULTS

Deformation I

- I In the Model Builder window, expand the Equivalent Plastic Strain (shell) node.
- 2 Right-click Surface I and choose Deformation.
- 3 In the Settings window for Deformation, locate the Expression section.
- **4** In the **x-component** text field, type **shell.u**.
- 5 In the y-component text field, type shell.v.
- **6** In the **z-component** text field, type **shell.w**.
- 7 Locate the **Scale** section.
- 8 Select the Scale factor check box. In the associated text field, type 1.

Deformation Angle (Friction)

In the Model Builder window, under Results>Derived Values right-click **Deformation Angle (Friction)** and choose **Duplicate**.

Deformation angle (Shell)

I In the Model Builder window, under Results>Derived Values click Deformation Angle (Friction) I.

- 2 In the Settings window for Global Evaluation, type Deformation angle (Shell) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Friction (shell)/ Solution 3 (4) (sol3).
- 4 In the Parameter values (para) list, choose I and I.4.
- **5** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
angle_shell	deg	Blank deformation angle (shell)

6 Click ▼ next to **= Evaluate**, then choose **New Table**.

Global 2

In the Model Builder window, under Results>Punch Force vs. Displacement right-click **Global 2** and choose **Duplicate**.

Global 3

- I In the Model Builder window, click Global 3.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Friction (shell)/Solution 3 (4) (sol3).
- 4 Locate the y-Axis Data section. In the table, enter the following settings:

Expression	Unit	Description
4*shell.dcnt2.T_totz	N	

- 5 Locate the Coloring and Style section. Find the Line style subsection. From the Line list, choose Dash-dot.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends Shell

7 In the Punch Force vs. Displacement toolbar, click **Plot**.