

Discharge and Self-Discharge of a Lead—Acid Battery

Lead-acid batteries are widely used as starter batteries for traction applications, such as for cars and trucks. The reason for this wide usage of lead-acid batteries is their low cost in combination with their performance robustness for a broad range of operating conditions. However, one drawback of this battery type is that the inherent thermodynamics of the battery chemistry causes the battery to self-discharge over time.

This example simulates a lead-acid battery at high (1200 A) and low (3 A) discharge rates, and the long-term self-discharge behavior with no applied external current (0 A).



Figure 1: Modeled geometry. The model is in 1D in the x direction.

Model Definition

Figure 1 shows the 1D model geometry. There are four domains: the positive porous electrode, the reservoir, the separator, and the negative porous electrode.

The model uses the Lead-Acid Battery interface for solving for the following unknown variables:

- ϕ_s the electronic potential
- ϕ_I the ionic potential
- ϵ the porosity (electrolyte volume fraction) of the porous electrodes
- c₁ the electrolyte concentration

ELECTROCHEMICAL REACTIONS

The main electrode reaction in the positive (PbO₂) electrode during discharge is

$$PbO_{2}(s) + HSO_{4}(aq) + 3H^{+}(aq) + 2e^{-} \rightarrow PbSO_{4}(s) + 2H_{2}O(l)$$

with an equilibrium potential that depends on the electrolyte concentration as shown in Figure 2.

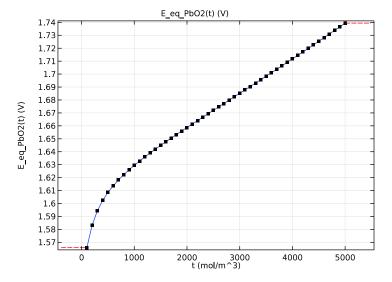


Figure 2: Equilibrium potential of the PbO_2 reaction as a function of electrolyte concentration in the positive electrode.

The combination of an aqueous solution and a high potential results in oxygen gas evolution at the positive electrode according to:

$${\rm H_2O}(l) \to \frac{1}{2}{\rm O}_2(g) + 2{\rm H}^+({\rm aq}) + 2e^- \qquad E_0 \,=\, 1.23\,{\rm V}$$

The main discharge reaction for the negative (Pb) electrode is:

$$Pb(s) + HSO_4(aq) \rightarrow PbSO_4(s) + H^+(aq) + 2e^{-1}$$

with an equilibrium potential that depends on the electrolyte concentration as shown in Figure 3.

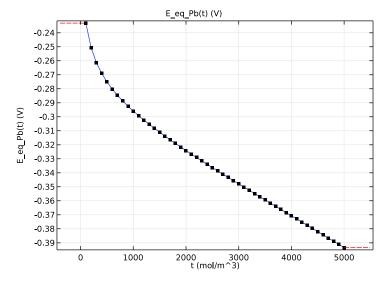


Figure 3: Equilibrium potential of the Pb reaction as a function of electrolyte concentration in the negative electrode.

This dependence of the equilibrium potential on the electrolyte concentration, for both discharge reactions, is present in the Materials Library for the Battery Design Module.

The low operating potential of the negative electrode results in hydrogen evolution according to:

$$2H^{+}(aq) + 2e^{-} \rightarrow H_{2}(g)$$
 $E_{0} = 0 \text{ V}$

For the gas evolution reaction, Butler-Volmer type kinetic expressions are used. For the main discharge reactions the default discharge reactions of the Lead-Acid Battery interface are used.

ELECTROLYTE TRANSPORT PARAMETERS

The electrolyte diffusion coefficient and the electrolyte conductivity vary with the concentration according to Figure 4 and Figure 5, respectively. This data is also present in the Materials Library for the Battery Design Module.

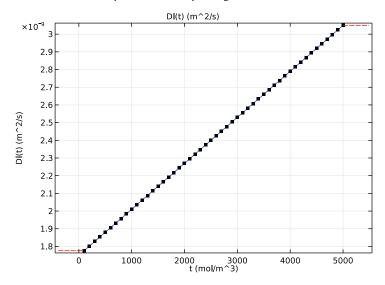


Figure 4: Electrolyte diffusion coefficient as a function of electrolyte concentration.

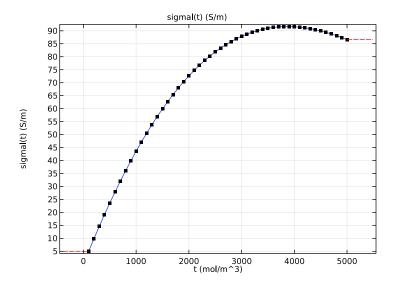


Figure 5: Electrolyte conductivity as a function of electrolyte concentration.

BOUNDARY AND INITIAL CONDITIONS

The outer boundary of the negative electrode is grounded and a discharge current is applied to the positive end terminal.

Three different discharge currents are simulated in three separate studies. The first study performs a C/20-discharge — a constant current in order to obtain a full discharge in 20 hours, followed by a one-hour relaxation period at zero external load. The second study simulates a high load 20C-discharge during 1 minute. In the third study the external load is set to zero and the simulation time is extended to one year to study the selfdischarge behavior.

Figure 6 shows the polarization plot of the cell. At the shut-off of the current the cell voltage first rises swiftly due to the sudden absence of activation and resistive losses, but after this the potential continues to rise slightly during a relaxation period.

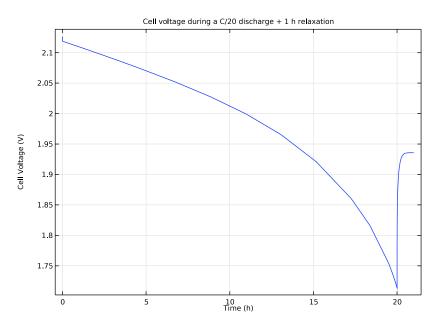


Figure 6: Cell voltage versus time for a C/20 discharge + 1-hour resting period.

Figure 7 depicts the reason for the slow rise in potential during the resting period. When the current is cut off at 20 h there is an electrolyte concentration gradient in the cell, but as electrolyte diffuses into the electrodes during the resting period the cell potential rises slightly.

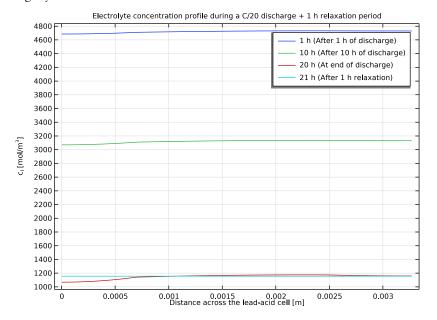


Figure 7: Electrolyte concentration profile at certain times during the C/20 discharge + 1hour relaxation simulation.

Figure 8 shows the state-of-charge variation in the electrodes during the C/20 simulation. At this relatively low discharge current the electrodes are discharged quite uniformly.

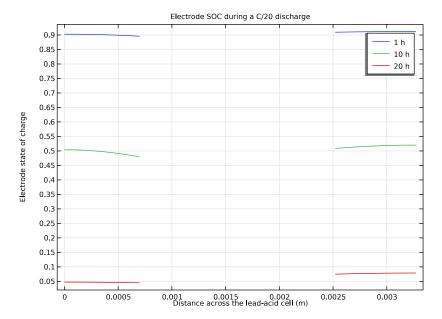


Figure 8: State-of-charge in the electrodes at 1, 10, and 20 h during the C/20 simulation.

When performing the 20C simulation the concentration (Figure 9) and state-of-charge gradients (Figure 10) are much higher. These very high currents causes the battery voltage

to drop significantly already after one minute due to electrolyte depletion in the positive electrode (even though two thirds of active electrode material is left in the electrodes).

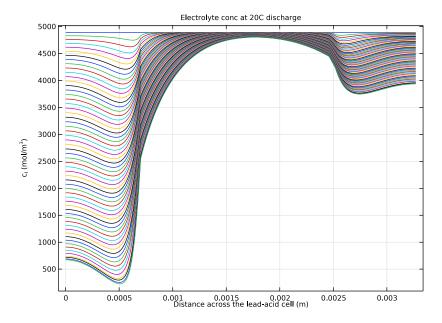


Figure 9: Electrolyte concentration profile (one profile curve per second) during a 20C discharge until cell voltage falls below 1.5 V.

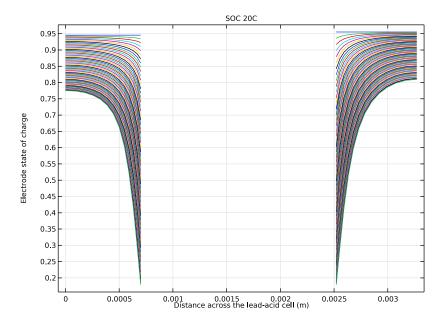


Figure 10: State-of-charge decrease during the 20C discharge simulation.

Figure 11 compares the discharge curves of the three simulations on a log t scale. The 20C cell voltage is much lower than the C/20 curve due to higher internal resistive and activation losses. The self-discharge curve indicates a moderate cell voltage drop after a year, Figure 12 shows that the state-of-charge of the positive electrode has decreased by over 25% during the same period.

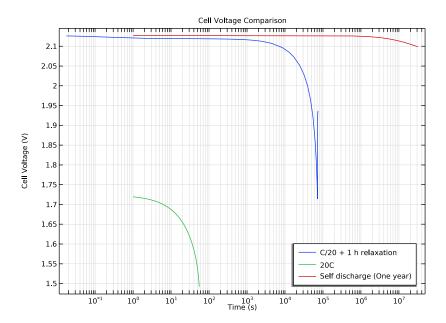


Figure 11: Discharge curves (cell voltage versus time) for the three simulations.

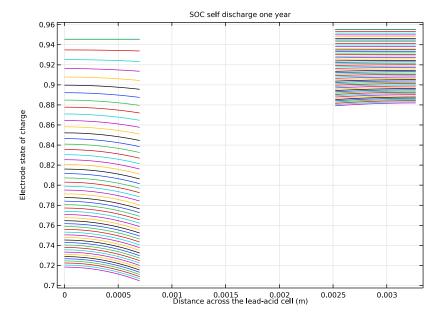


Figure 12: State-of-charge during the one-year self-discharge simulation.

Reference

1. M. Cugnet, S. Laruelle, S. Grugeon, B. Sahut, J. Sabatier, J.M. Tarascon, and A. Oustaloup, "A Mathematical Model for the Simulation of New and Aged Automotive Lead–Acid Batteries," *J. Electrochem. Soc.*, vol. 156, pp. A974–A985, 2009.

Application Library path: Battery_Design_Module/Batteries,_General/pb_acid_battery_1d

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click ID.
- 2 In the Select Physics tree, select Electrochemistry>Batteries>Lead-Acid Battery (leadbat).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Time Dependent with Initialization.
- 6 Click M Done.

GLOBAL DEFINITIONS

Load the parameter values to be used in the model from a file.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file pb_acid_battery_1d_parameters.txt.

Step I (step I)

Use a step function to switch off the applied discharge current at 20 h.

- I In the Home toolbar, click f(X) Functions and choose Global>Step.
- 2 In the Settings window for Step, locate the Parameters section.
- 3 In the Location text field, type 20*3600.
- 4 In the From text field, type 1.
- 5 In the To text field, type 0.

GEOMETRY I

Interval I (i1)

- I In the Model Builder window, under Component I (compl) right-click Geometry I and choose Interval.
- 2 In the Settings window for Interval, locate the Interval section.
- 3 From the Specify list, choose Interval lengths.

4 In the table, enter the following settings:

Lengths (m)			
L_pos			
L_res			
L_sep			
L_neg			

5 Click **Build All Objects**.

GEOMETRY I

In the Model Builder window, collapse the Component I (compl)>Geometry I node.

ADD MATERIAL

Next, add the materials data for the sulfuric acid electrolyte, the positive lead oxide electrode and the negative lead electrode.

- I In the Home toolbar, click **Add Material** to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Battery>Electrolytes>Sulfuric Acid (Lead-Acid Battery).
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select Battery>Electrodes>Pb (Negative, Lead-Acid Battery).
- **6** Click **Add to Component** in the window toolbar.
- 7 In the tree, select Battery>Electrodes>Pb02 (Positive, Lead-Acid Battery).
- **8** Click **Add to Component** in the window toolbar.
- 9 In the Home toolbar, click **‡ Add Material** to close the **Add Material** window.

MATERIALS

Pb (Negative, Lead-Acid Battery) (mat2)

- I In the Model Builder window, under Component I (compl)>Materials click Pb (Negative, Lead-Acid Battery) (mat2).
- 2 Select Domain 4 only.

PbO2 (Positive, Lead-Acid Battery) (mat3)

- I In the Model Builder window, click Pb02 (Positive, Lead-Acid Battery) (mat3).
- **2** Select Domain 1 only.

LEAD-ACID BATTERY (LEADBAT)

Positive Porous Flectrode 1

- I In the Model Builder window, under Component I (compl) right-click Lead-Acid Battery (leadbat) and choose Porous Electrode>Positive Porous Electrode.
- 2 Select Domain 1 only.
- 3 In the Settings window for Positive Porous Electrode, locate the Electrolyte Properties section.
- 4 From the Electrolyte material list, choose Sulfuric Acid (Lead-Acid Battery) (mat I).
- 5 In the ex text field, type ex.
- **6** Locate the **Electrode Properties** section. In the ε_0 text field, type eps_pos_min.
- 7 In the ε_{max} text field, type eps_pos_max.
- 8 In the exm text field, type exm.
- **9** Click the **Show More Options** button in the **Model Builder** toolbar.
- 10 In the Show More Options dialog box, in the tree, select the check box for the node Physics>Advanced Physics Options.
- II Click OK.
- 12 In the Settings window for Positive Porous Electrode, click to expand the **Equilibrium Potential Handling (Primary Condition)** section.
- 13 From the Equilibrium potential based on list, choose First reaction.

Separator I

- I In the Physics toolbar, click **Domains** and choose **Separator**.
- **2** Select Domain 3 only.
- 3 In the Settings window for Separator, locate the Separator section.
- 4 In the ε_{sep} text field, type eps_sep.
- 5 In the ex text field, type ex sep.

Negative Porous Electrode 1

- I In the Physics toolbar, click Domains and choose Negative Porous Electrode.
- 2 Select Domain 4 only.
- 3 In the Settings window for Negative Porous Electrode, locate the Electrolyte Properties section.
- 4 From the Electrolyte material list, choose Sulfuric Acid (Lead-Acid Battery) (mat I).
- 5 In the ex text field, type ex.

- **6** Locate the **Electrode Properties** section. In the ϵ_0 text field, type eps_neg_min.
- 7 In the ε_{max} text field, type eps_neg_max.
- 8 In the exm text field, type exm.
- 9 Click to expand the Equilibrium Potential Handling (Primary Condition) section. From the Equilibrium potential based on list, choose First reaction.

Porous Electrode Reaction I

Now, set up the electrode reactions and the double layer capacitance for the electrodes. Start with the positive electrode discharge reaction.

- I In the Model Builder window, under Component I (compl)>Lead-Acid Battery (leadbat)>
 Positive Porous Electrode I click Porous Electrode Reaction I.
- 2 In the Settings window for Porous Electrode Reaction, locate the Electrode Kinetics section.
- 3 From the Kinetics expression type list, choose Lead-acid battery discharge.
- **4** In the $i_{0,ref}(T)$ text field, type i0_ref_pos.
- **5** In the α_a text field, type alpha_a_pos.
- **6** In the α_c text field, type alpha_c_pos.
- **7** In the $c_{l,ref}$ text field, type cl_ref.
- **8** In the γ text field, type gamma_pos.
- **9** Locate the **Active Specific Surface Area** section. In the $a_{v,max}$ text field, type a_max_pos.
- **IO** In the ζ text field, type morph pos.

Positive Porous Electrode I

These steps set up the oxygen evolution reaction, occurring on the positive electrode:

I In the Model Builder window, click Positive Porous Electrode I.

Porous Electrode Reaction 2

- I In the Physics toolbar, click ____ Attributes and choose Porous Electrode Reaction.
- 2 In the Settings window for Porous Electrode Reaction, locate the Equilibrium Potential section.
- **3** From the $E_{\rm eq}$ list, choose **User defined**. In the associated text field, type 1.23.
- 4 Locate the Electrode Kinetics section. From the Kinetics expression type list, choose Butler-Volmer.
- **5** In the i_0 text field, type i0_02*(c1/c1_ref)^2.
- **6** In the α_a text field, type alpha_02.

- 7 In the α_c text field, type alpha_02.
- 8 Locate the Active Specific Surface Area section. In the a_v text field, type a_max_pos* (epsilon-eps_pos_min)/(eps_pos_max-eps_pos_min).
- **9** Locate the Stoichiometric Coefficients section. In the v_{H+} text field, type -2.
- **10** In the v_{HSO4} text field, type 0.
- II In the v_{H2O} text field, type 1.
- 12 In the v_{PbO2} text field, type 0.
- **I3** In the v_{PhSO4} text field, type 0.
- 14 Click to expand the Heat of Reaction section. From the list, choose User defined.

Positive Porous Electrode I

In the Model Builder window, click Positive Porous Electrode 1.

Porous Matrix Double Layer Capacitance I

- I In the Physics toolbar, click Attributes and choose Porous Matrix Double Layer Capacitance.
- 2 In the Settings window for Porous Matrix Double Layer Capacitance, locate the Porous Matrix Double Layer Capacitance section.
- **3** In the $C_{\rm dl}$ text field, type C_dl_pos.
- **4** In the $a_{v,dl}$ text field, type a_max_pos.

Porous Electrode Reaction 1

Set up the negative electrode discharge reaction in the following way:

- I In the Model Builder window, under Component I (compl)>Lead-Acid Battery (leadbat)> Negative Porous Electrode I click Porous Electrode Reaction I.
- 2 In the Settings window for Porous Electrode Reaction, locate the Electrode Kinetics section.
- 3 From the Kinetics expression type list, choose Lead-acid battery discharge.
- **4** In the $i_{0,ref}(T)$ text field, type i0_ref_neg.
- **5** In the α_a text field, type alpha_a_neg.
- **6** In the α_c text field, type alpha_c_neg.
- **7** In the $c_{1 \text{ ref}}$ text field, type cl_ref.
- **8** In the γ text field, type gamma_neg.
- **9** Locate the **Active Specific Surface Area** section. In the $a_{v,max}$ text field, type a_max_neg.
- **IO** In the ζ text field, type morph_neg.

Negative Porous Electrode 1

Set up the hydrogen evolution reaction on the negative electrode in the following way:

I In the Model Builder window, click Negative Porous Electrode I.

Porous Electrode Reaction 2

- I In the Physics toolbar, click ____ Attributes and choose Porous Electrode Reaction.
- 2 In the Settings window for Porous Electrode Reaction, locate the Equilibrium Potential section.
- **3** From the $E_{\rm eq}$ list, choose **User defined**. In the associated text field, type 0.
- 4 Locate the **Electrode Kinetics** section. From the **Kinetics expression type** list, choose **Butler-Volmer**.
- **5** In the i_0 text field, type i0_H2*cl/cl_ref.
- **6** In the α_a text field, type alpha_H2.
- 7 In the α_c text field, type alpha_H2.
- 8 Locate the Active Specific Surface Area section. In the $a_{\rm v}$ text field, type a_max_neg* (epsilon-eps_neg_min)/(eps_neg_max-eps_neg_min).
- **9** Locate the **Stoichiometric Coefficients** section. In the v_{H+} text field, type -2.
- **10** In the v_{HSO4} text field, type 0.
- II In the v_{Ph} text field, type 0.
- 12 In the v_{PbSO4} text field, type 0.
- 13 Click to expand the Heat of Reaction section. From the list, choose User defined.

Negative Porous Electrode 1

In the Model Builder window, click Negative Porous Electrode 1.

Porous Matrix Double Layer Capacitance 1

- I In the Physics toolbar, click Attributes and choose Porous Matrix Double Layer Capacitance.
- 2 In the Settings window for Porous Matrix Double Layer Capacitance, locate the Porous Matrix Double Layer Capacitance section.
- **3** In the $C_{\rm dl}$ text field, type C_dl_neg.
- 4 In the $a_{v.dl}$ text field, type a_max_neg.

GLOBAL DEFINITIONS

Default Model Inputs

Set up the temperature value used in the entire model.

- I In the Model Builder window, under Global Definitions click Default Model Inputs.
- 2 In the Settings window for Default Model Inputs, locate the Browse Model Inputs section.
- 3 In the tree, select General>Temperature (K) minput.T.
- 4 Find the Expression for remaining selection subsection. In the Temperature text field, type Τ.

LEAD-ACID BATTERY (LEADBAT)

Now, provide the boundary conditions. Ground the negative electrode and set a current density at the positive electrode.

Electric Ground 1

- I In the Physics toolbar, click Boundaries and choose Electric Ground.
- **2** Select Boundary 5 only.

Electrode Current Density I

- I In the Physics toolbar, click Boundaries and choose Electrode Current Density.
- **2** Select Boundary 1 only.
- 3 In the Settings window for Electrode Current Density, locate the Electrode Current Density section.
- **4** In the $i_{n,s}$ text field, type I_disch*step1(t/1[s]).

Initial Values 2

Finally, provide initial conditions for the battery at the start of the discharge.

- I In the Physics toolbar, click Domains and choose Initial Values.
- **2** Select Domains 1 and 2 only.
- 3 In the Settings window for Initial Values, locate the Initial Values section.
- **4** In the *cl* text field, type cl init.
- 5 In the *epsilon* text field, type eps pos init.

Initial Values 1

- I In the Model Builder window, click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the *cl* text field, type cl init.

4 In the *epsilon* text field, type eps neg init.

STUDY I

Start by setting up a 21 h study using the C/20 current setting from the parameter file.

Step 2: Time Dependent

- I In the Model Builder window, under Study I click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0, 1800, 21*3600).

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.
 - Store the actual steps taken by the solver to make sure to capture any sudden steep voltage changes.
- 3 In the Model Builder window, under Study I>Solver Configurations>Solution I (sol1) click
 Time-Dependent Solver I.
- 4 In the Settings window for Time-Dependent Solver, locate the General section.
- 5 From the Times to store list, choose Steps taken by solver.
- 6 In the Study toolbar, click **Compute**.

RESULTS

Cell voltage C/20

- I In the Settings window for ID Plot Group, type Cell voltage C/20 in the Label text field.
- **2** Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 3 In the Title text area, type Cell voltage during a C/20 discharge + 1 h relaxation.
- 4 Locate the Plot Settings section.
- **5** Select the **x-axis label** check box. In the associated text field, type Time (h).
- 6 Select the y-axis label check box. In the associated text field, type Cell Voltage (V).

Point Graph 1

- I In the Model Builder window, expand the Cell voltage C/20 node, then click Point Graph I.
- 2 In the Settings window for Point Graph, locate the x-Axis Data section.
- 3 From the Parameter list, choose Expression.

- 4 In the Expression text field, type t/3600.
- 5 In the Cell voltage C/20 toolbar, click Plot.

Electrolyte conc C/20

- I In the Model Builder window, under Results click Electrolyte Salt Concentration (leadbat).
- 2 In the Settings window for ID Plot Group, type Electrolyte conc C/20 in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Manual.
- 4 In the Title text area, type Electrolyte concentration profile during a C/20 discharge + 1 h relaxation period.
- 5 Locate the Plot Settings section.
- 6 Select the x-axis label check box. In the associated text field, type Distance across the lead-acid cell [m].
- 7 Select the y-axis label check box. In the associated text field, type c₁ [mol/m³].

Line Graph 1

- I In the Model Builder window, expand the Electrolyte conc C/20 node, then click Line Graph 1.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- 4 From the Time selection list, choose Interpolated.
- 5 In the Times (s) text field, type 3600.
- **6** Click to expand the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legends 1 h (After 1 h of discharge)

9 Right-click Line Graph I and choose Duplicate.

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Times (s) text field, type 10*3600.

4 Locate the **Legends** section. In the table, enter the following settings:

```
Legends
10 h (After 10 h of discharge)
```

5 Right-click Line Graph 2 and choose Duplicate.

Line Graph 3

- I In the Model Builder window, click Line Graph 3.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Times (s) text field, type 20*3600.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Leg	gen	ds			
20	h	(At	end	of	discharge)

5 Right-click Line Graph 3 and choose Duplicate.

Line Graph 4

- I In the Model Builder window, click Line Graph 4.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Times (s) text field, type 21*3600.
- **4** Locate the **Legends** section. In the table, enter the following settings:

```
Legends
21 h (After 1 h relaxation)
```

5 In the Electrolyte conc C/20 toolbar, click Plot.

Electrode SOC during a C/20 discharge

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Electrode SOC during a C/20 discharge in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.
- 4 Locate the **Plot Settings** section.
- **5** Select the **x-axis label** check box. In the associated text field, type **Distance across** the lead-acid cell (m).
- 6 Select the y-axis label check box. In the associated text field, type Electrode state of charge.

Line Graph 1

- I Right-click Electrode SOC during a C/20 discharge and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- **4** From the **Time selection** list, choose **Interpolated**.
- 5 In the Times (s) text field, type 3600.
- 6 Locate the Selection section. From the Selection list, choose All domains.
- 7 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Lead-Acid Battery>leadbat.soc -Electrode state of charge - I.
- **8** Locate the **Legends** section. Select the **Show legends** check box.
- 9 From the Legends list, choose Manual.
- **10** In the table, enter the following settings:

Legends 1 h

II Right-click Line Graph I and choose Duplicate.

Line Grabh 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Times (s) text field, type 10*3600.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends 10 h

5 Right-click Line Graph 2 and choose Duplicate.

Line Graph 3

- I In the Model Builder window, click Line Graph 3.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Times (s) text field, type 20*3600.

4 Locate the **Legends** section. In the table, enter the following settings:

Legends				
20	h			

5 In the Electrode SOC during a C/20 discharge toolbar, click Plot.

GLOBAL DEFINITIONS

Now set up the 20C study by changing the current. Also add a nonlocal coupling for use in a stop condition to stop the simulation when the cell voltage drops below 1.5 V.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 In the table, enter the following settings:

Name	Expression	Value	Description
C_factor	20	20	Current multiplicative factor

DEFINITIONS

Integration I (intop I)

- I In the Definitions toolbar, click // Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- **4** Select Boundary 1 only.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Time Dependent with Initialization.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2

Step 2: Time Dependent

I In the Model Builder window, under Study 2 click Step 2: Time Dependent.

- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0, 1, 60).

Solution 3 (sol3)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution 3 (sol3) node.
- 3 Right-click Study 2>Solver Configurations>Solution 3 (sol3)>Time-Dependent Solver I and choose Stop Condition.
- 4 In the Settings window for Stop Condition, locate the Stop Expressions section.
- 5 Click + Add.
- **6** In the table, enter the following settings:

Stop expression	Stop if	Active	Description
<pre>comp1.intop1(comp1.phis)<1 .5</pre>	True (>=I)	√	Stop expression 1

Specify that the solution is to be stored both before and after the stop condition is reached.

- 7 Locate the Output at Stop section. From the Add solution list, choose Steps before and after stop.
- 8 Clear the Add warning check box.
- 9 In the Study toolbar, click **Compute**.

RESULTS

Electrolyte conc at 20C discharge

- I In the Model Builder window, under Results click Electrolyte Salt Concentration (leadbat).
- 2 In the Settings window for ID Plot Group, type Electrolyte conc at 20C discharge in the Label text field.
- 3 Locate the Plot Settings section.
- 4 Select the x-axis label check box. In the associated text field, type Distance across the lead-acid cell (m).
- 5 Select the y-axis label check box. In the associated text field, type c₁ (mo1/m < sup > 3 < / sup >).
- 6 Locate the Title section. From the Title type list, choose Label.

SOC 20C

- I In the Home toolbar, click In Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type SOC 20C in the Label text field.
- **3** Locate the **Title** section. From the **Title type** list, choose **Label**.
- 4 Locate the Plot Settings section.
- 5 Select the **x-axis label** check box. In the associated text field, type Distance across the lead-acid cell (m).
- 6 Select the y-axis label check box. In the associated text field, type Electrode state of charge.

Line Graph 1

- I Right-click **SOC 20C** and choose **Line Graph**.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution 3 (sol3).
- 4 Locate the Selection section. From the Selection list, choose All domains.
- 5 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Lead-Acid Battery>leadbat.soc Electrode state of charge 1.
- 6 In the SOC 20C toolbar, click Plot.

GLOBAL DEFINITIONS

For the self-discharge study, set the current to 0 and add a new study node.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
C_factor	0	0	Current multiplicative factor

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Time Dependent with Initialization.

- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 3

Step 2: Time Dependent

- I In the Model Builder window, under Study 3 click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type 0 range (1,7*24*3600,365*24*3600).
- 4 In the Model Builder window, click Study 3.
- 5 In the Settings window for Study, locate the Study Settings section.
- **6** Clear the **Generate default plots** check box.
- 7 In the Home toolbar, click **Compute**.

RESULTS

Cell Voltage Comparison

- I In the Home toolbar, click <a>In Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Cell Voltage Comparison in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.
- 4 Locate the Plot Settings section.
- 5 Select the x-axis label check box. In the associated text field, type Time (s).
- 6 Select the y-axis label check box. In the associated text field, type Cell Voltage (V).
- 7 Locate the Axis section. Select the x-axis log scale check box.
- 8 Locate the Legend section. From the Position list, choose Lower right.

Point Graph 1

- I Right-click Cell Voltage Comparison and choose Point Graph.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- 4 Select Boundary 1 only.
- 5 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Lead-Acid Battery>phis - Electric potential - V.
- **6** Click to expand the **Legends** section. Select the **Show legends** check box.

- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

```
Legends
C/20 + 1 h relaxation
```

9 Right-click **Point Graph I** and choose **Duplicate**.

Point Graph 2

- I In the Model Builder window, click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution 3 (sol3).
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends 20C

5 Right-click Point Graph 2 and choose Duplicate.

Point Graph 3

- I In the Model Builder window, click Point Graph 3.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Study 3/Solution 5 (sol5).
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends Self discharge (One year)

SOC self discharge one year

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type SOC self discharge one year in the **Label** text field.
- **3** Locate the **Title** section. From the **Title type** list, choose **Label**.
- 4 Locate the Plot Settings section.
- 5 Select the x-axis label check box. In the associated text field, type Distance across the lead-acid cell (m).

6 Select the y-axis label check box. In the associated text field, type Electrode state of charge.

Line Graph 1

- I Right-click SOC self discharge one year and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study 3/Solution 5 (sol5).
- 4 Locate the Selection section. From the Selection list, choose All domains.
- 5 Click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Lead-Acid Battery>leadbat.soc -Electrode state of charge - I.
- 6 In the SOC self discharge one year toolbar, click Plot.