

# Turbulent Mixing in a Stirred Tank

## Introduction

This tutorial demonstrates how mixing can be simulated in a stirred vessel by seeding a trace species from a point. The flow is modeled using the Rotating Machinery, Fluid Flow interface, which solves the Navier-Stokes equations on geometries with rotating parts such as impellers. The transport of the trace species is modeled using the Transport of Diluted Species interface. The trace species is added when the mixer is running in steady operation. The mixing time is evaluated by comparing the concentration in a measurement point to the average concentration in the vessel.

## Model Definition

#### MODEL GEOMETRY

Figure 1 shows the model geometry, which is a schematic cross section of a tank with a four-blade impeller. The tank has four baffles attached to the wall to enhance mixing. The mixer blades and the impellers are approximated to be infinitely thin. The seeding of the trace species is done at the marked seeding point. The tank also contains a measurement point, close to the wall, where the concentration can be probed.

The circle between the impeller and the tank wall is the assembly boundary where the mesh is allowed to slide when the impeller rotates.

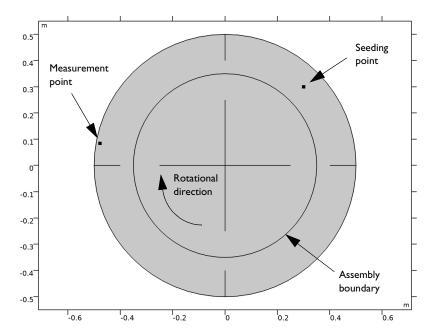


Figure 1: Model geometry.

#### DOMAIN EQUATION AND BOUNDARY CONDITIONS

The mixer fluid is water, and a rotational speed of 20 rpm is prescribed for the impeller. This rotation is achieved by prescribing the inner domain to be a rotating domain. The boundary between the inner and the outer domain is prescribed to be a continuity boundary that transfers momentum to the fluid in the outer domain.

The Reynolds number based on the impeller radius and the impeller tip speed is approximately  $1.9 \times 10^6$ , which means that the flow is turbulent. The k- $\varepsilon$  turbulence model is applied in this example.

There are two methods to reach operating conditions. One is to accelerate the impeller up to full speed and wait for the flow to reach a quasi steady-state. This approach is simple but can be time consuming. A computationally more efficient method is to first simulate the flow using the frozen rotor approach. Frozen rotor means that the impeller, or rotor, is frozen in position. The flow in the rotating domain is assumed to be stationary in terms of a rotating coordinate system. The effect of the rotation is then accounted for by Coriolis and centrifugal forces. This solution couples to the nonrotating parts where the flow is also assumed to be stationary, but in a nonrotating coordinate system. See the CFD Module User's Guide for more information about frozen rotor.

The result of a frozen rotor simulation is an approximation to the flow at operating conditions. The result depends on the angular position of the impeller and cannot represent transient effects. It is still a very good starting condition to reach operating conditions. Here, to make sure that the correct operating conditions are reached, a time dependent simulations is ran starting from the frozen rotor solution. The average flow quantities are inspected in order to determine when a quasi-steady state is reached.

A trace species is a species introduced in very small quantities. It is often of a sharp color to be clearly visible even in small amounts. A trace species is not supposed to affect the flow, and hence, the flow can be solved for first and then the trace species transport solved for subsequently. The seeding is performed by injection at the seeding point during one second. Then the mixing in the vessel is simulated for 40 revolutions. The degree of mixing is evaluated by comparing the averaged concentration to the concentration measured near the wall behind one of the baffles.

To reduce the computational effort, the fluid flow field is not solved for during the mixing. The flow field and turbulent diffusion during the last revolution of the flow simulation is reused repeatedly during the mixing stage.

Note that in order to be able to reuse the flow field in a periodic fashion, variables are redefined in the Equation View of the multiphysics coupling feature (Reacting Flow, Diluted Species).

## Results and Discussion

Figure 2 shows the frozen rotor velocity field. As expected, the highest velocity magnitude is found at the tip of the mixer blades. There are also clearly visible recirculation zones both before and behind the baffles.

Figure 3 shows the velocity field at the end of the fluid flow simulation (at t = 30 s, corresponding to 10 revolutions). The rotor position is the same as in Figure 2, and the results in the figures are similar. There are, however, differences. The most notable difference is that the recirculation zones before the baffles are smaller in Figure 3 than in Figure 2. The size and shape of the recirculation zones for the time-dependent simulation also vary with the position of the impeller.

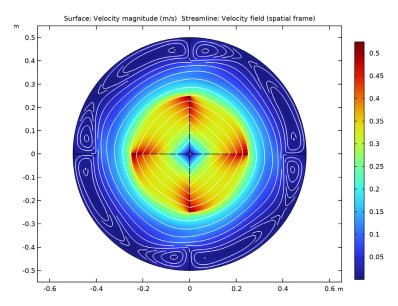


Figure 2: The velocity field obtained from the frozen rotor simulation.

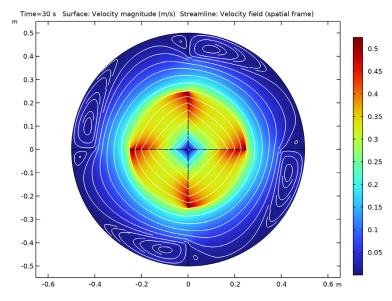


Figure 3: A snapshot of the time-dependent velocity field at t=30 s.

The average velocity and the average turbulent dynamic viscosity are plotted in Figure 4 to visualize the flow field development over time. The variables are normalized using the results from the frozen rotor solution. It can be noted that there is a drift over the first couple of rotations, but the magnitude of the variations is small. The frequency with which the impeller blades are passing the baffles is clearly seen in the velocity variations. The flow is noted to have reached a cyclic steady state after around seven revolutions. This implies that the last revolution of the simulation can confidently be used repeatedly for the mixing simulation.

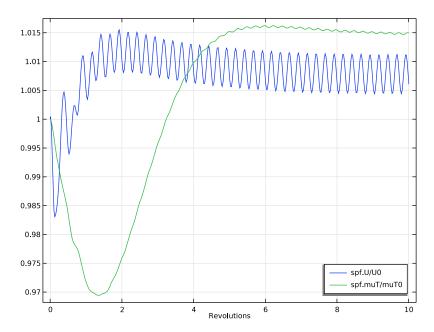


Figure 4: Flow development starting from the frozen rotor solution. The average velocity and average turbulent diffusion normalized by the respective initial values are shown.

Figure 5 shows four snapshots of the mixing process, with the time running from the upper-left to the lower-right picture. Since the velocity is rather slow at the seeding point (see also Figure 3), the initial transport is almost isotropic around the seeding point (t = 2 s). Some trace species is, however, entrained in the faster velocity field in the center of the mixer and becomes thereby spread in the azimuthal direction (t = 8 s). The slowest spreading is to the regions behind the left baffle, close to the measuring point, as well as behind the top baffle. Species in the space between the impeller blades is mixed poorly with

species in the outer region. This is a well-known phenomenon and is the reason why chemical substances are commonly added as close to the impeller axis as possible.

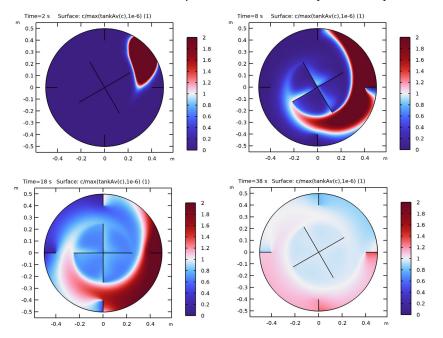


Figure 5: The mixing process. Surface plots of the trace species, normalized by the average concentration, at t = 2, 8, 18 and 38 seconds.

The mixing development can be evaluated in Figure 5 where the concentration at the measurement position and the average concentration are plotted. As was noted in the previous figure it takes a number of rotations of the impeller before the species is spread to the measurement position. After about 14 rotations the concentration behind the baffle surpasses the averaged concentrations, and after around 30 rotations the average concentration has been reached.

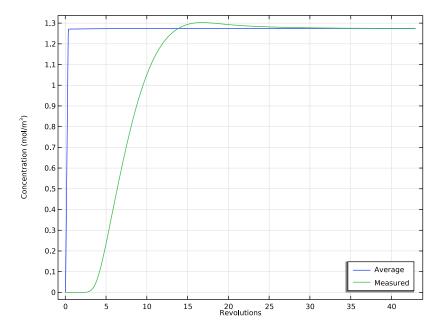


Figure 6: Concentration development during mixing. Comparing the average concentration in the tank to the one in the measurement point.

Application Library path: CFD\_Module/Single-Phase\_Flow/turbulent\_mixing

# Modeling Instructions

From the File menu, choose New.

## NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 20.
- 2 In the Select Physics tree, select Fluid Flow>Single-Phase Flow>Rotating Machinery, Fluid Flow>Turbulent Flow>Turbulent Flow, k-ε.
- 3 Click Add.

- 4 Click Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Frozen Rotor.
- 6 Click M Done.

#### **GLOBAL DEFINITIONS**

Import some model parameters from a text file.

#### Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file turbulent mixing parameters.txt.

#### GEOMETRY I

Circle I (c1)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type tank R.

Circle 2 (c2)

- I In the **Geometry** toolbar, click ( ) Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 0.7\*tank R.
- 4 Click | Build Selected.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- 2 In the Settings window for Difference, locate the Difference section.
- 3 Select the Keep objects to subtract check box.
- 4 Select the object cl only.
- **5** Click to select the **Activate Selection** toggle button for **Objects to subtract**.
- **6** Select the object **c2** only.

Line Segment I (Is I)

I In the Geometry toolbar, click \* More Primitives and choose Line Segment.

- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 From the Specify list, choose Coordinates.
- **4** Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 Locate the Starting Point section. In the x text field, type -tank R.
- 6 Locate the Endpoint section. In the x text field, type -tank\_R+baffle\_L.

#### Rotate I (rot1)

- I In the Geometry toolbar, click Transforms and choose Rotate.
- **2** Select the object **IsI** only.
- 3 In the Settings window for Rotate, locate the Rotation section.
- 4 Click Range.
- 5 In the Range dialog box, type 90 in the Start text field.
- 6 In the Step text field, type 90.
- 7 In the **Stop** text field, type 270.
- 8 Click Replace.
- **9** In the **Settings** window for **Rotate**, locate the **Input** section.
- 10 Select the Keep input objects check box.

## Point I (btl)

- I In the **Geometry** toolbar, click **Point**.
- 2 In the Settings window for Point, locate the Point section.
- 3 In the x text field, type inject x.
- 4 In the y text field, type inject y.
- 5 Click | Build Selected.

#### Point 2 (bt2)

- I In the **Geometry** toolbar, click **Point**.
- 2 In the Settings window for Point, locate the Point section.
- 3 In the x text field, type -tank R\*0.97.
- 4 Click **Build Selected**.

## Rotate 2 (rot2)

- I In the Geometry toolbar, click Transforms and choose Rotate.
- 2 Select the object **pt2** only.
- 3 In the Settings window for Rotate, locate the Rotation section.

- 4 In the Angle text field, type -10.
- 5 Click | Build Selected.

Union I (uni I)

I In the Geometry toolbar, click Booleans and Partitions and choose Union.

The final operation will later be set to **Form an assembly**. Union operations are therefore necessary to merge the domains and the lines.

2 Select the objects difl, lsl, ptl, rotl(l), rotl(2), rotl(3), and rot2 only.

Line Segment 2 (Is2)

- I In the Geometry toolbar, click \* More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- **3** From the **Specify** list, choose **Coordinates**.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 Locate the Starting Point section. In the x text field, type -0.25.
- **6** Locate the **Endpoint** section. In the **x** text field, type **0.25**.

Line Segment 3 (Is3)

- I In the Geometry toolbar, click \* More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 From the Specify list, choose Coordinates.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 Locate the Starting Point section. In the y text field, type -0.25.
- 6 Locate the **Endpoint** section. In the y text field, type 0.25.

Union 2 (uni2)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects c2, ls2, and ls3 only.

Form Union (fin)

The boundary between the rotating and nonrotating domains must be an assembly boundary so that the parts can move relative to each other.

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.

- 4 In the Geometry toolbar, click **Build All**.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Create a selection for the interior boundaries representing the impeller and baffles.

#### DEFINITIONS

Impeller and Baffles

- I In the **Definitions** toolbar, click **\( \frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- **4** Select Boundaries 1–4 and 13–16 only.
- 5 In the Label text field, type Impeller and Baffles.

Create an average operator to be used for computing average quantities in the tank.

Average I (aveob I)

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Average.
- 2 In the Settings window for Average, type tankAv in the Operator name text field.
- 3 Locate the Source Selection section. From the Selection list, choose All domains.

## ADD MATERIAL

- I In the Home toolbar, click **‡ Add Material** to open the **Add Material** window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Water, liquid.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click **‡ Add Material** to close the **Add Material** window.

#### MOVING MESH

Rotating Domain I

- I In the Model Builder window, under Component I (compl)>Moving Mesh click Rotating Domain I.
- 2 Select Domain 2 only.
- 3 In the Settings window for Rotating Domain, locate the Rotation section.
- **4** In the f text field, type -rpm.

## TURBULENT FLOW, K-ε(SPF)

Interior Wall I

- I In the Model Builder window, under Component I (compl) right-click Turbulent Flow, k- $\varepsilon$  (spf) and choose Interior Wall.
- 2 In the Settings window for Interior Wall, locate the Boundary Selection section.
- 3 From the Selection list, choose Impeller and Baffles.

Pressure Point Constraint I

- I In the Physics toolbar, click Points and choose Pressure Point Constraint.
- **2** Select Point 10 only.

The pressure level must be specified to obtain a unique solution since water is an incompressible liquid.

Hide the internal boundaries between the moving and the stationary part of the geometry. First copy the boundary selection from the continuity feature.

Flow Continuity I

- I In the Model Builder window, click Flow Continuity I.
- 2 In the Settings window for Flow Continuity, click to expand the Boundary Selection section.
- 3 Click Copy Selection.

## **DEFINITIONS**

Hide for Physics 1

- I In the Model Builder window, right-click View I and choose Hide for Physics.
- 2 In the Settings window for Hide for Physics, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, Press CTRL+V to paste the copied boundary selection.
- 6 click OK.

#### MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Fine.

4 Right-click Component I (compl)>Mesh I and choose Edit Physics-Induced Sequence.

Size 1

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Point.
- **4** Select Point 11 only.
- **5** Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type 3e-3.
- 8 Click **Build All**.

#### STUDY I

Steb 1: Frozen Rotor

In the **Home** toolbar, click **Compute**.

#### RESULTS

Velocity (sbf)

Create Figure 2 using the following steps.

Streamline 1

- I Right-click Velocity (spf) and choose Streamline.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.
- 3 From the Positioning list, choose Uniform density.
- 4 In the Separating distance text field, type 0.02.
- 5 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose White.
- 6 In the Velocity (spf) toolbar, click Plot.

Add a Time Dependent study.

Pressure (spf), Velocity (spf), Wall Resolution (spf)

- I In the Model Builder window, under Results, Ctrl-click to select Velocity (spf), Pressure (spf), and Wall Resolution (spf).
- 2 Right-click and choose **Group**.

Fluid Flow, Frozen Rotor

In the Settings window for Group, type Fluid Flow, Frozen Rotor in the Label text field.

#### DEFINITIONS

#### Variables 1

- I In the Model Builder window, under Component I (compl) right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
U0	<pre>withsol('sol1', tankAv(spf.U))</pre>	m/s	Average velocity, frozen rotor
muT0	<pre>withsol('sol1', tankAv(spf.muT))</pre>	Pa·s	Average turbulent dynamic viscosity, frozen rotor

#### Domain Probe: U

- I In the **Definitions** toolbar, click Probes and choose **Domain Probe**.
- 2 In the Settings window for Domain Probe, type Domain Probe: U in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type spf.U/U0.
- 4 Right-click Domain Probe: U and choose Duplicate.

#### Domain Probe: muT

- I In the Model Builder window, under Component I (compl)>Definitions click Domain Probe: U I (dom2).
- 2 In the Settings window for Domain Probe, type Domain Probe: muT in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type spf.muT/muT0.

#### ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

#### STUDY 2

In the Study toolbar, click In Show Default Plots.

## Step 1: Time Dependent

Store time steps at the end of the simulation when the flow field is expected to have reached a quasi steady state.

- I In the Model Builder window, under Study 2 click Step 1: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type 0 range(frev\_t0,rev\_dt,frev\_tEnd). Enable results while solving, and use the probes to monitor when a quasi steady state is reached.
- **4** Click to expand the **Results While Solving** section. Select the **Plot** check box.
- 5 From the Plot group list, choose Probe Plot Group 4.
- 6 From the Update at list, choose Time steps taken by solver.
- 7 From the Probes list, choose Manual. Start from the frozen rotor solution.
- 8 Click to expand the Values of Dependent Variables section. Find the **Initial values of variables solved for subsection.** From the **Settings** list, choose User controlled.
- **9** From the **Method** list, choose **Solution**.
- 10 From the Study list, choose Study 1, Frozen Rotor.
- II In the **Study** toolbar, click **Compute**.

#### RESULTS

Pressure (spf) I, Probe Plot Group 4, Velocity (spf) I, Wall Resolution (spf) I

- I In the Model Builder window, under Results, Ctrl-click to select Probe Plot Group 4, Velocity (spf) I, Pressure (spf) I, and Wall Resolution (spf) I.
- 2 Right-click and choose Group.

Fluid Flow, Time Dependent

In the Settings window for Group, type Fluid Flow, Time Dependent in the Label text field.

Probe Plot Group 4

- I In the Model Builder window, click Probe Plot Group 4.
- 2 In the Settings window for ID Plot Group, locate the Legend section.

3 From the Position list, choose Lower right.

Probe Table Graph 1

- I In the Model Builder window, expand the Probe Plot Group 4 node, then click Probe Table Graph 1.
- 2 In the Settings window for Table Graph, click to expand the Preprocessing section.
- **3** Find the **x-axis column** subsection. From the **Transformation** list, choose **Linear**.
- 4 In the Scaling text field, type rpm.

Probe Plot: Fluid flow development

- I In the Model Builder window, under Results>Fluid Flow, Time Dependent click Probe Plot Group 4.
- 2 In the Settings window for ID Plot Group, type Probe Plot: Fluid flow development in the Label text field.
- 3 Locate the Plot Settings section.
- **4** Select the **x-axis label** check box. In the associated text field, type Revolutions.

Probe Table Graph 1

- I In the Model Builder window, click Probe Table Graph I.
- 2 In the Settings window for Table Graph, click to expand the Legends section.
- 3 From the Legends list, choose Manual.
- **4** In the table, enter the following settings:

Legends		
spf.U/U0		
spf.muT/muT0		

5 In the Probe Plot: Fluid flow development toolbar, click Plot.

Velocity (spf) 1

Recreate Figure 3 using the following steps.

Streamline I

- I In the Model Builder window, right-click Velocity (spf) I and choose Streamline.
- 2 In the Settings window for Streamline, locate the Streamline Positioning section.
- **3** From the **Positioning** list, choose **Uniform density**.
- 4 In the Separating distance text field, type 0.02.

- 5 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose White.
- 6 In the Velocity (spf) I toolbar, click Plot.

#### **DEFINITIONS**

Rectangle I (rect1)

- I In the Home toolbar, click f(x) Functions and choose Local>Rectangle.
- 2 In the Settings window for Rectangle, locate the Parameters section.
- 3 In the Lower limit text field, type 0.1.
- 4 In the **Upper limit** text field, type 1.1.
- 5 Click to expand the Smoothing section. In the Size of transition zone text field, type 0.2.

Domain Probe : c\_av

- I In the Definitions toolbar, click Probes and choose Domain Probe.
- 2 In the Settings window for Domain Probe, type Domain Probe : c av in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type c.
- 4 Click to expand the Table and Window Settings section. From the Output table list, choose New table.
- 5 Click + Add Table.
- 6 From the Plot window list, choose New window.
- 7 Click + Add Plot Window.

Point Probe : c

- I In the **Definitions** toolbar, click Probes and choose **Point Probe**.
- 2 In the Settings window for Point Probe, type Point Probe : c in the Label text field.
- 3 Locate the Probe Type section. From the Type list, choose Integral.
- 4 Locate the Source Selection section. Click Clear Selection.
- **5** Select Point 2 only.
- **6** Locate the **Expression** section. In the **Expression** text field, type c.
- 7 Click to expand the Table and Window Settings section. From the Output table list, choose Table 2.
- 8 From the Plot window list, choose Probe Plot 2.
- 9 Click Go to Source.

#### RESULTS

#### Probe Table 2

- I In the Model Builder window, under Results>Tables click Table 2.
- 2 In the Settings window for Table, type Probe Table 2 in the Label text field.

#### ADD PHYSICS

- I In the Home toolbar, click Add Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Chemical Species Transport>Transport of Diluted Species (tds).
- 4 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Study I and Study 2.
- **5** Click **Add to Component I** in the window toolbar.
- 6 In the Home toolbar, click Add Physics to close the Add Physics window.

## TRANSPORT OF DILUTED SPECIES (TDS)

Thin Impermeable Barrier 1

- I Right-click Component I (compl)>Transport of Diluted Species (tds) and choose Interior Surfaces>Thin Impermeable Barrier.
- 2 In the Settings window for Thin Impermeable Barrier, locate the Boundary Selection section.
- 3 From the Selection list, choose Impeller and Baffles.

Line Mass Source L

- I In the Physics toolbar, click Points and choose Line Mass Source.
- **2** Select Point 11 only.
- 3 In the Settings window for Line Mass Source, locate the Species Source section.
- **4** In the  $\dot{q}_{1,c}$  text field, type rect1(t[1/s]).

#### MULTIPHYSICS

Reacting Flow, Diluted Species 1 (rfd1)

In the Physics toolbar, click A Multiphysics Couplings and choose Domain>Reacting Flow, **Diluted Species.** 

#### ADD STUDY

I In the Home toolbar, click Add Study to open the Add Study window.

- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- **4** Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** check box for Turbulent Flow, k- $\varepsilon$  (spf).
- 5 Click Add Study in the window toolbar.
- 6 In the Home toolbar, click Add Study to close the Add Study window.

Next, set up the study step for the mixing to periodically re-use the fluid flow solution from the last rotation in Study 2.

#### STUDY 3

## Step 1: Time Dependent

- I In the Settings window for Time Dependent, locate the Study Settings section.
- 2 In the Output times text field, type range(0, rev\_t/3, rev\_t\*mix\_revs).
- **3** Locate the **Results While Solving** section. Select the **Plot** check box.
- 4 From the Update at list, choose Time steps taken by solver.
- 5 From the Probes list, choose Manual.
- 6 In the Probes list, choose Domain Probe: U (dom1) and Domain Probe: muT (dom2).
- 7 Under Probes, click Delete.
- 8 Locate the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- **9** From the **Method** list, choose **Solution**.
- 10 From the Study list, choose Study 2, Time Dependent.
- II From the Time (s) list, choose Automatic (all solutions).

## Solution 3 (sol3)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution 3 (sol3) node, then click Time-Dependent Solver 1.
- 3 In the Settings window for Time-Dependent Solver, click to expand the Advanced section.
- 4 Select the Periodic values of variables not solved for check box.
- 5 In the Start time text field, type frev tEnd-rev t.

- 6 In the Interval length text field, type rev\_t.
- 7 In the Study toolbar, click Show Default Plots.

#### RESULTS

Concentration (tds)

Plot the dataset edges on the spatial frame to make them follow the rotation.

- I In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 2 From the Frame list, choose Spatial (x, y, z).

Now solve for the injection and mixing of the passive trace species.

#### STUDY 3

Step 1: Time Dependent

- I In the Model Builder window, under Study 3 click Step 1: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Results While Solving section.
- 3 From the Plot group list, choose Concentration (tds).
- 4 In the Study toolbar, click **Compute**.

## RESULTS

Concentration (tds), Probe Plot Group 8

- I In the Model Builder window, under Results, Ctrl-click to select Probe Plot Group 8 and Concentration (tds).
- 2 Right-click and choose **Group**.

Species Mixing, Time Dependent

In the Settings window for Group, type Species Mixing, Time Dependent in the Label text field.

Probe Table Graph 1

- I In the Model Builder window, expand the Probe Plot Group 8 node, then click Probe Table Graph 1.
- 2 In the Settings window for Table Graph, locate the Preprocessing section.
- 3 Find the x-axis column subsection. From the Transformation list, choose Linear.
- 4 In the Scaling text field, type rpm.

## Probe Plot: Mixing

- I In the Model Builder window, under Results>Species Mixing, Time Dependent click Probe Plot Group 8.
- 2 In the Settings window for ID Plot Group, type Probe Plot: Mixing in the Label text field.
- 3 Locate the Plot Settings section.
- 4 Select the x-axis label check box. In the associated text field, type Revolutions.
- 5 Select the y-axis label check box. In the associated text field, type Concentration (mo1/m < sup > 3 < / sup >).
- 6 Locate the Legend section. From the Position list, choose Lower right.
- 7 In the Probe Plot: Mixing toolbar, click **Plot**.

## Probe Table Graph 1

- I In the Model Builder window, click Probe Table Graph I.
- 2 In the Settings window for Table Graph, locate the Legends section.
- 3 From the Legends list, choose Manual.
- **4** In the table, enter the following settings:

## Legends Average Measured

5 In the Probe Plot: Mixing toolbar, click **Plot**.

#### Concentration (tds)

The following steps create an animation that contains the plots in Figure 5.

#### Surface I

- I In the Model Builder window, expand the Concentration (tds) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type c/max(tankAv(c), 1e-6).
- 4 Click to expand the Range section. Select the Manual color range check box.
- **5** In the **Minimum** text field, type **0**.
- **6** In the **Maximum** text field, type 2.
- 7 Locate the Coloring and Style section. Click Change Color Table.
- 8 In the Color Table dialog box, select Wave>Wave in the tree.

#### 9 Click OK.

#### Streamline I

In the Model Builder window, right-click Streamline I and choose Disable.

#### Animation I

- I In the Results toolbar, click Animation and choose File.
- 2 In the Settings window for Animation, locate the Target section.
- 3 From the Target list, choose Player.
- 4 Locate the Scene section. From the Subject list, choose Concentration (tds). Set the frames to be displayed for as long as the time between the saved solutions.
- 5 Locate the Playing section. In the Display each frame for text field, type 0.15.
- 6 Locate the Frames section. From the Frame selection list, choose All.
- 7 Click the Play button in the Graphics toolbar.