

# Tire Inflation

## Introduction

Tires play a fundamental structural role in vehicle dynamics by transmitting loads to the ground, thus making it possible for traction and brake to develop. At the same time, tires must contribute to limit the effect of road irregularity, concurring to the overall vibration isolation capability of the vehicle. These two functions require modern tires to have substantial structural loading capability, while at the same time being compliant enough to provide better comfort with respect to a solid wheel. A tire is thus a complicated composite made of various types of soft rubber locally reinforced by stiff cords usually made by steel and nylon.

Tire simulation requires the use of appropriate nonlinear anisotropic constitutive models to describe the rubber behavior with the inclusion of the effect of the cord reinforcements. This model showcases how to use fibers in thin layers to model thin anisotropic composites embedded in a solid without explicitly drawing either the layer of material or the reinforcing fibers. In particular, this is used to model steel cords in tire belts that are used to provide structural support to the tire below the treads. Moreover, a curvilinear coordinate system is used to define the anisotropic material properties of the carcass ply.

# Model Definition

Both the geometry of the tire and the applied loads during inflation show axial symmetry. For this reason, you do not need to model the entire three dimensional tire, but a 2D axisymmetric model can be used to save computational time. Moreover, a plane of symmetry can be identified for the tire cross section. Figure 1 illustrates a simplified geometry of half of the cross section of a tire, along with the cross section of the rim in the locations where it enters in contact with the tire.

Note that when exploiting symmetries for reducing the computational cost in simulations care must be taken to check that the material properties show the same symmetry as exhibited by loads and geometry.

In the case of tires, the orientation of cords in the reinforcing plies usually induces displacements that have non zero components in the azimuthal direction, and that are not symmetric with respect to the plane of symmetry of the geometry. COMSOL Multiphysics provides a specific formulation for the 2D axisymmetric problem that allows to include the azimuthal "twist" without the need to switch to a full 3D model.

For what concerns the lack of symmetry with respect to the midplane of the cross section, it can be shown that by using an antisymmetry condition for the circumferential

displacement on the symmetry plane of the geometry, the difference in the solution obtained with respect to the one computed with a full cross section is very small.

In Figure 1 different colors have been used to highlight different domains, based on the material properties used.

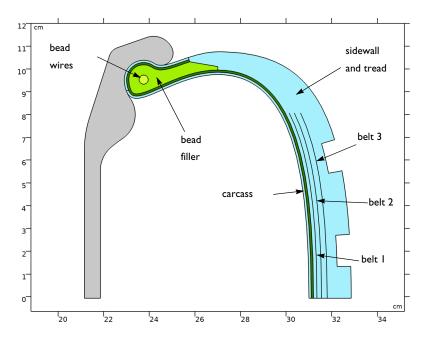


Figure 1: Geometry of the tire and rim cross sections.

The following modeling assumptions have been made:

- Sidewall and tread are assumed to be made by the same material, modeled with the Yeoh hyperelastic constitutive law
- Bead wires are modeled as a single uniform steel domain
- Bead filler can be also modeled with the Yeoh hyperelastic material modeled
- The carcass is modeled using a linear elastic transversely isotropic material model, that captures in a homogenized way the nylon and steel reinforcements
- The three belts are modeled as thin hyperelastic layers made by the same rubber as the sidewall and tread, with embedded steel cords
- The rim is considered to be rigid.

The material properties for each material domain are collected in Table 1 (Ref. 1 and Ref. 2).

TABLE I: MATERIAL PROPERTIES.

Material properties	Sidewall and tread	Bead	Carcass
$c_1$	I MPa	1.6 MPa	-
$c_2$	-0.3 MPa	-1.4 MPa	-
$c_3$	0.1 MPa	0.9 MPa	-
K	100 MPa	100 MPa	-
$\mathrm{E}_1$	-	-	7 GPa
$\mathrm{E}_2$	-	-	25 MPa
$v_1$	-	-	0.45
$v_2$	-	-	0.4
G	-	-	4 MPa

Table 2 collects the orientation of the cords in each belt with respect to the azimuthal direction. The orientation of the cords, along with the first principal direction of the transversely isotropic material used for the carcass are represented in Figure 2.

The tire is inflated to reach an inner pressure of 2 bar.

TABLE 2: ORIENTATION OF CORDS.

Belt I	Belt 2	Belt 3
+20°	-20°	0°

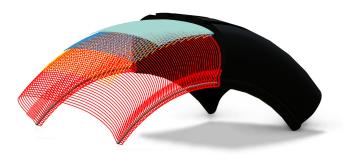


Figure 2: Cords orientation.

Figure 3 shows the twist displacement in the tire, and Figure 4 shows the von Mises stress in the cords and in the bead wires.

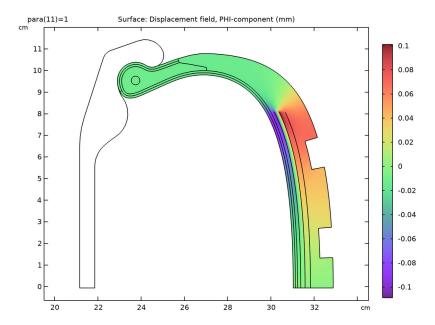


Figure 3: Azimuthal displacement.

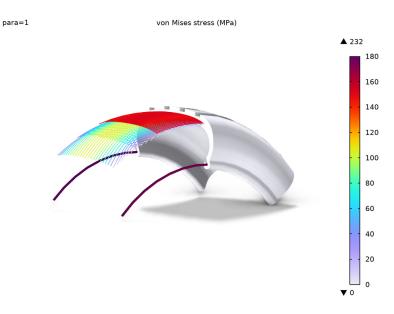


Figure 4: The von Mises stress at the end of inflation.

# Notes About the COMSOL Implementation

- You find the Include circumferential displacement check box in the Axial Symmetry **Approximation** section in the settings window of the Solid Mechanics interface. This allows you to enable the 2D axisymmetric formulation that includes the twist degree of freedom.
- You can add a Initial Stress and Strain node under Linear Elastic Material to model the prestress in the bead wires, resulting after the mounting of the tire on the rim.
- You can use a **Curvilinear Coordinates** interface to compute the direction of anisotropy in the carcass.
- To model the belts without explicitly drawing their thickness, you can simply add a **Thin** Layer and add a Hyperelastic Material to it. Use the Solid approximation to create a slit for the displacement variable at the selected boundary.
- Add three Fiber nodes to the Hyperelastic Material under the Thin Layer in order to model the three different orientations of the cords. You can directly specify the orientation

with respect to the boundary coordinate system without further computations. Choose a Linear elastic material model for the cords, to model steel.

• You find the Antisymmetry option under the Circumferential Condition section when you add the Symmetry Plane.

# References

- 1. T. Király, P. Primusz and C. Tóth, "Simulation of Static Tyre-Pavement Interaction Using Two FE Models of Different Complexity," Appl. Sci., vol. 12, no. 5, p. 2388, 2022.
- 2. H.S. Aldhufairi, O. Olatunbosun, and K. Essa, "Determination of a Tyre's Rolling Resistance Using Parallel Rheological Framework," SAE Technical Paper, no. 2019-01-5069, 2019.

Application Library path: Nonlinear Structural Materials Module/ Hyperelasticity/tire\_inflation

# Modeling Instructions

From the File menu, choose New.

## NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click 🔁 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click M Done.

### **GEOMETRY I**

First, import the geometry of the tire cross section and the geometry of the rim.

#### TIRE SECTION

- I In the Model Builder window, right-click Global Definitions and choose Geometry Parts> 2D Part.
- 2 In the Settings window for Part, type Tire Section in the Label text field.

Import I (impl)

- I In the **Home** toolbar, click  **Import**.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click Browse.
- **4** Browse to the model's Application Libraries folder and double-click the file tire inflation.mphbin.
- 5 In the Home toolbar, click **Build All**.

#### TIRE SECTION

In the Model Builder window, collapse the Global Definitions>Geometry Parts>Tire Section node.

#### RIM

- I In the Model Builder window, under Global Definitions right-click Geometry Parts and choose 3D Part.
- 2 In the Settings window for Part, type Rim in the Label text field.
- 3 Locate the Advanced section. From the Geometry representation list, choose CAD kernel.
- 4 In the Home toolbar, click Import.
- I In the Settings window for Import, locate the Import section.
- 2 Click **Browse**.
- **3** Browse to the model's Application Libraries folder and double-click the file wheel\_rim.x\_b.
- 4 In the Home toolbar, click **Build All**.

## RIM

In the Model Builder window, collapse the Global Definitions>Geometry Parts>Rim node.

Generate the 2D axisymmetric geometry.

## 2D AXISYMMETRIC [TIRE]

I In the Model Builder window, click Component I (compl).

2 In the **Settings** window for **Component**, type 2D Axisymmetric [Tire] in the **Label** text field

#### **GEOMETRY I**

- I In the Model Builder window, under 2D Axisymmetric [Tire] (comp1) click Geometry 1.
- 2 In the Settings window for Geometry, locate the Units section.
- **3** From the **Length unit** list, choose **cm**.

Tire Section I (pil)

- I In the Geometry toolbar, click Part Instance and choose Tire Section.
- 2 In the Settings window for Part Instance, click 🖺 Build Selected.

In order to add the rim to the 2D axisymmetric component, you need to create a cross section of the 3D geometry.

## ADD COMPONENT

Right-click Tire Section I (pil) and choose 3D.

## 3D [RIM]

In the Settings window for Component, type 3D [Rim] in the Label text field.

#### **GEOMETRY 2**

- I In the Model Builder window, under 3D [Rim] (comp2) click Geometry 2.
- 2 In the Settings window for Geometry, locate the Units section.
- **3** From the **Length unit** list, choose **cm**.
- 4 Locate the Advanced section. From the Geometry representation list, choose CAD kernel.

Rim I (pil)

- I In the Geometry toolbar, click Part Instance and choose Rim.
- 2 In the Settings window for Part Instance, click 📳 Build Selected.

Set the plane of the cross section.

Work Plane I (wbl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose xz-plane.
- 4 Click | Build Selected.

#### **GEOMETRY I**

In the Model Builder window, under 2D Axisymmetric [Tire] (comp1) click Geometry 1.

Cross Section I (crol)

- I In the Geometry toolbar, click A Cross Section.
- 2 In the Settings window for Cross Section, click 📳 Build Selected.
- 3 Click the **Zoom Extents** button in the **Graphics** toolbar.

Delete Entities I (del1)

- I In the Model Builder window, right-click Geometry I and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Geometric entity level list, choose Domain.
- 4 On the object **crol**, select Domains 1–3 only.
- 5 Click **Build Selected**.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Only half of the domain will be included in the study by adopting a symmetry boundary condition. Modify the geometry accordingly.

Line Segment I (Is I)

- I In the Geometry toolbar, click : More Primitives and choose Line Segment.
- 2 On the object pil, select Point 80 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- 4 From the Specify list, choose Coordinates.
- 5 In the r text field, type 20.
- 6 In the z text field, type -7E-2.
- 7 Click | Build Selected.

Partition Objects I (par I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Partition Objects.
- 2 Select the objects dell and pil only.
- 3 In the Settings window for Partition Objects, locate the Partition Objects section.
- **4** Click to select the **Activate Selection** toggle button for **Tool objects**.
- **5** Select the object **Is1** only.
- 6 Click | Build Selected.

Delete Entities 2 (del2)

- I Right-click Geometry I and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click the Select Box button in the Graphics toolbar.
- 5 On the object parl(1), select Domain 1 only.
- 6 On the object parl(2), select Domains 1, 2, 6, 8, and 10 only.
- 7 Click | Build Selected.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Add now mesh control edges, needed later on in order to mesh properly the component.

Import I (impl)

- I In the Geometry toolbar, click Import.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click **Browse**.
- **4** Browse to the model's Application Libraries folder and double-click the file tire\_inflation\_meshcontrol.mphbin.
- 5 Locate the Selections of Resulting Entities section. Select the Resulting objects selection check box.
- 6 From the Show in physics list, choose Boundary selection.
- 7 Click | Build Selected.
- 8 Click the Zoom Extents button in the Graphics toolbar.

Union I (uni I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects del2(2) and impl only.
- 3 In the Settings window for Union, click | Build Selected.

An assembly is needed between the rim and the tire, in order to set properly the contact between them.

Form Union (fin)

- I In the Model Builder window, under 2D Axisymmetric [Tire] (comp1)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.

- 4 Clear the Create pairs check box.
- 5 Click | Build Selected.

Mesh Control Edges I (mcel)

- I In the Geometry toolbar, click \times \text{Virtual Operations} and choose Mesh Control Edges.
- 2 In the Settings window for Mesh Control Edges, locate the Input section.
- 3 From the Edges to include list, choose Import 1.
- 4 Click | Build Selected.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Set the contact pair between rim and tire.

## **DEFINITIONS (COMPI)**

Contact Pair I (pl)

- I In the Model Builder window, expand the 2D Axisymmetric [Tire] (compl)>Definitions
- 2 Right-click 2D Axisymmetric [Tire] (comp1)>Definitions and choose Pairs>Contact Pair.
- **3** Select Boundaries 7, 8, and 10 only.
- 4 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 5 In the Settings window for Pair, locate the Destination Boundaries section.
- **6** Click to select the **Activate Selection** toggle button.
- 7 Select Boundaries 30, 31, 44, and 46 only.

Add material properties.

#### **GLOBAL DEFINITIONS**

Steel [Bead Wires]

- I In the Model Builder window, under Global Definitions right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Steel [Bead Wires] in the Label text field.
- 3 Click to expand the Material Properties section. In the Material properties tree, select Basic Properties>Young's Modulus.
- 4 Click + Add to Material.
- 5 In the Material properties tree, select Basic Properties>Poisson's Ratio.
- 6 Click + Add to Material.

- 7 In the Material properties tree, select Basic Properties>Density.
- 8 Click + Add to Material.
- **9** Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	210[GPa]	Pa	Basic
Poisson's ratio	nu	0.3	I	Basic
Density	rho	7800[kg/m^3]	kg/m³	Basic

10 Right-click Steel [Bead Wires] and choose Duplicate.

## Steel [Cords]

- I In the Model Builder window, under Global Definitions>Materials click Steel [Bead Wires] I (mat2).
- 2 In the Settings window for Material, type Steel [Cords] in the Label text field.
- **3** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Young's modulus	E	170[GPa]	Pa	Basic

## Rubber [Sidewall and Tread]

- I In the Model Builder window, right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Rubber [Sidewall and Tread] in the Label text field.
- 3 Click to expand the Material Properties section. In the Material properties tree, select Solid Mechanics>Hyperelastic Material>Yeoh.
- 4 Click + Add to Material.
- **5** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Model parameters	cIYE	1[MPa]	Pa	Yeoh
Model parameters	c2YE	-0.3[MPa]	Pa	Yeoh
Model parameters	c3YE	0.1[MPa]	Pa	Yeoh

- 6 Locate the Material Properties section. In the Material properties tree, select Solid Mechanics>Linear Elastic Material>Bulk Modulus and Shear Modulus> Bulk modulus (K).
- 7 Click + Add to Material.

**8** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Bulk modulus	K	100[MPa]	N/m²	Bulk modulus and shear modulus

- 9 Locate the Material Properties section. In the Material properties tree, select Basic Properties>Density.
- 10 Click + Add to Material.
- II Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	1100[kg/m^3]	kg/m³	Basic

12 Right-click Rubber [Sidewall and Tread] and choose Duplicate.

## Rubber [Bead]

- I In the Model Builder window, under Global Definitions>Materials click Rubber [Sidewall and Tread] I (mat4).
- 2 In the Settings window for Material, type Rubber [Bead] in the Label text field.
- **3** Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Model parameters	cIYE	1.6[MPa]	Pa	Yeoh
Model parameters	c2YE	-1.4[MPa]	Pa	Yeoh
Model parameters	c3YE	0.9[MPa]	Pa	Yeoh

## Reinforced Rubber [Carcass]

- I In the Model Builder window, right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, type Reinforced Rubber [Carcass] in the Label text field.
- 3 Click to expand the Material Properties section. In the Material properties tree, select Solid Mechanics>Linear Elastic Material>Transversely Isotropic.
- 4 Click + Add to Material.
- 5 In the Material properties tree, select Basic Properties>Density.
- 6 Click + Add to Material.

7 Locate the Material Contents section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	1750[kg/ m^3]	kg/m³	Basic
Young's modulus	{Evect1, Evect2}	{7[GPa], 25[MPa]}	Pa	Transversely isotropic
Poisson's ratio	{nuvect1, nuvect2}	{0.45, 0.4}	I	Transversely isotropic
Shear modulus	GvectI	4[MPa]	N/m²	Transversely isotropic

Assign material properties to domains.

#### MATERIALS

Material Link: Steel [Bead Wires]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl) right-click Materials and choose More Materials>Material Link.
- 2 In the Settings window for Material Link, type Material Link: Steel [Bead Wires] in the Label text field.
- 3 Locate the Geometric Entity Selection section. Click Clear Selection.
- 4 Select Domain 7 only.
- 5 Click **\( \)** Create Selection.
- 6 In the Create Selection dialog box, type Bead Wires in the Selection name text field.
- 7 Click OK.
- 8 In the Settings window for Material Link, click to expand the Appearance section.
- **9** From the Material type list, choose Steel.

Material Link: Rubber [Sidewall and Tread]

- I Right-click Materials and choose More Materials>Material Link.
- 2 In the Settings window for Material Link, locate the Link Settings section.
- 3 From the Material list, choose Rubber [Sidewall and Tread] (mat3).
- 4 In the Label text field, type Material Link: Rubber [Sidewall and Tread].
- **5** Select Domains 2, 3, and 5 only.
- 6 Locate the Geometric Entity Selection section. Click \( \bigcup\_{\text{a}} \) Create Selection.

- 7 In the Create Selection dialog box, type Sidewall and Tread in the Selection name text field.
- 8 Click OK.
- **9** In the **Settings** window for **Material Link**, click to expand the **Appearance** section.
- **10** From the Material type list, choose Rubber.
- II From the Color list, choose Black.

Material Link: Rubber [Bead]

- I Right-click Materials and choose More Materials>Material Link.
- 2 In the Settings window for Material Link, type Material Link: Rubber [Bead] in the Label text field.
- **3** Select Domain 6 only.
- 4 Locate the Link Settings section. From the Material list, choose Rubber [Bead] (mat4).
- 5 Locate the Geometric Entity Selection section. Click \(\bigcap\_{\text{a}}\) Create Selection.
- 6 In the Create Selection dialog box, type Bead Rubber in the Selection name text field.
- 7 Click OK.
- 8 In the Settings window for Material Link, click to expand the Appearance section.
- 9 From the Material type list, choose Rubber.
- 10 From the Color list, choose Black.

Material Link: Reinforced Rubber [Carcass]

- I Right-click Materials and choose More Materials>Material Link.
- 2 In the Settings window for Material Link, type Material Link: Reinforced Rubber [Carcass] in the **Label** text field.
- **3** Select Domain 4 only.
- 4 Locate the Link Settings section. From the Material list, choose Reinforced Rubber [Carcass] (mat5).
- 5 Locate the Geometric Entity Selection section. Click \(\bigs\_{\text{he}}\) Create Selection.
- 6 In the Create Selection dialog box, type Carcass in the Selection name text field.
- 7 Click OK.
- 8 In the Settings window for Material Link, click to expand the Appearance section.
- 9 From the Color list, choose Gray.

## **DEFINITIONS (COMPI)**

Hyperelastic Domains

- I In the **Definitions** toolbar, click **Union**.
- 2 In the Settings window for Union, type Hyperelastic Domains in the Label text field.
- 3 Locate the Input Entities section. Under Selections to add, click + Add.
- 4 In the Add dialog box, in the Selections to add list, choose Sidewall and Tread and Bead Rubber.
- 5 Click OK.

Exclude the rim from **Solid Mechanics**, since it is modeled as a rigid boundary.

## SOLID MECHANICS (SOLID)

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl) click Solid Mechanics (solid).
- 2 Select Domains 2–7 only.

Assign the hyperelastic material model to domains made of rubber.

Hyperelastic Material 1

- I In the Physics toolbar, click **Domains** and choose **Hyperelastic Material**.
- 2 In the Settings window for Hyperelastic Material, locate the Domain Selection section.
- 3 From the Selection list, choose Hyperelastic Domains.
- 4 Locate the Hyperelastic Material section. From the Material model list, choose Yeoh.
- **5** From the Compressibility list, choose Compressible, uncoupled.

Assign a transversely isotropic linear elastic material model to the tire carcass.

Linear Elastic Material [Carcass]

- I In the Physics toolbar, click **Domains** and choose **Linear Elastic Material**.
- 2 In the Settings window for Linear Elastic Material, type Linear Elastic Material [Carcass] in the **Label** text field.
- 3 Locate the Domain Selection section. From the Selection list, choose Carcass.
- 4 Locate the Linear Elastic Material section. From the Material symmetry list, choose Orthotropic.
- 5 Select the Transversely isotropic check box.

Linear Elastic Material [Bead Wires]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl)> Solid Mechanics (solid) click Linear Elastic Material 1.
- 2 In the Settings window for Linear Elastic Material, type Linear Elastic Material [Bead Wires] in the Label text field.

Add a Curvilinear Coordinates physics interface in order to compute principal directions of anisotropy for the reinforced rubber.

## ADD PHYSICS

- I In the Physics toolbar, click and Physics to open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Mathematics>Curvilinear Coordinates (cc).
- 4 Click Add to 2D Axisymmetric [Tire] in the window toolbar.
- 5 In the Physics toolbar, click and Physics to close the Add Physics window.

## CURVILINEAR COORDINATES (CC)

- I In the Settings window for Curvilinear Coordinates, locate the Domain Selection section.
- 2 From the Selection list, choose Carcass.
- 3 Locate the Settings section. Select the Create base vector system check box.

Diffusion Method I

Right-click 2D Axisymmetric [Tire] (comp1)>Curvilinear Coordinates (cc) and choose Diffusion Method.

Inlet I

- I In the Physics toolbar, click Attributes and choose Inlet.
- 2 Select Boundary 21 only.

Diffusion Method I

In the Model Builder window, click Diffusion Method I.

Outlet I

- I In the Physics toolbar, click \_ Attributes and choose Outlet.
- 2 Select Boundary 17 only.

## SOLID MECHANICS (SOLID)

Linear Elastic Material [Carcass]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (comp1)> Solid Mechanics (solid) click Linear Elastic Material [Carcass].
- 2 In the Settings window for Linear Elastic Material, locate the Coordinate System Selection section.
- 3 From the Coordinate system list, choose Curvilinear System (cc) (cc\_cs).

Define geometric parameters of the belts' cord reinforcements.

## **GLOBAL DEFINITIONS**

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
dcord_belts	0.5[mm]	5E-4 m	Diameter of belt cords
spcord_belts	1.16[mm]	0.00116 m	Spacing between belt cords
alpha_belt	70[deg]	1.2217 rad	Angle of belt cords

Add the belts.

## SOLID MECHANICS (SOLID)

Thin Layer I

- I In the Physics toolbar, click 

  Boundaries and choose Thin Layer.
- 2 Select Boundaries 57–59 only.
- 3 In the Settings window for Thin Layer, locate the Boundary Selection section.
- 4 Click **\( \)** Create Selection.
- 5 In the Create Selection dialog box, type Belts in the Selection name text field.
- 6 Click OK.
- 7 In the Settings window for Thin Layer, locate the Boundary Properties section.
- **8** In the  $L_{\rm th}$  text field, type dcord\_belts.

Hyperelastic Material I

- I In the Physics toolbar, click Attributes and choose Hyperelastic Material.
- 2 In the Settings window for Hyperelastic Material, locate the Boundary Selection section.
- 3 From the Selection list, choose Belts.
- 4 Locate the Hyperelastic Material section. From the Material model list, choose Yeoh.
- 5 From the Compressibility list, choose Compressible, uncoupled.

## MATERIALS

Material Link: Rubber [Sidewall and Tread] (matlnk2)

In the Model Builder window, under 2D Axisymmetric [Tire] (comp I)>Materials right-click Material Link: Rubber [Sidewall and Tread] (matlnk2) and choose Duplicate.

Material Link: Rubber [Belts]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl)>Materials click Material Link: Rubber [Sidewall and Tread] I (matlnk5).
- 2 In the Settings window for Material Link, type Material Link: Rubber [Belts] in the **Label** text field.
- 3 Locate the Geometric Entity Selection section. From the Geometric entity level list, choose **Boundary**.
- 4 From the Selection list, choose Belts.

## SOLID MECHANICS (SOLID)

Hyperelastic Material I

In the Model Builder window, under 2D Axisymmetric [Tire] (compl)> Solid Mechanics (solid)>Thin Layer I click Hyperelastic Material I.

Fiber [Cords, Belt 1]

- I In the Physics toolbar, click Attributes and choose Fiber.
- 2 In the Settings window for Fiber, type Fiber [Cords, Belt 1] in the Label text field.
- 3 Locate the Fiber Model section. From the Material model list, choose Linear elastic.
- 4 From the Material list, choose Steel [Cords] (mat2).
- 5 Locate the Orientation section. From the a list, choose User defined.
- **6** Specify the **Direction** vector as

<pre>cos(alpha_belt)</pre>	tl
sin(alpha_belt)	to

- **7** In the  $d_{\text{fiber}}$  text field, type dcord\_belts.
- **8** In the  $s_{\text{fiber}}$  text field, type spcord\_belts.
- 9 Locate the Boundary Selection section. Click Clear Selection.
- 10 Select Boundary 57 only.
- II Click **Create Selection**.
- 12 In the Create Selection dialog box, type Belt 1 in the Selection name text field.
- I3 Click OK.
- 14 Right-click Fiber [Cords, Belt 1] and choose Duplicate.

Fiber [Cords, Belt 2]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl)> Solid Mechanics (solid)>Thin Layer I>Hyperelastic Material I click Fiber [Cords, Belt 1] I.
- 2 In the Settings window for Fiber, type Fiber [Cords, Belt 2] in the Label text field.
- 3 Locate the Boundary Selection section. Click Clear Selection.
- 4 Select Boundary 58 only.
- 5 Click **Create Selection**.
- 6 In the Create Selection dialog box, type Belt 2 in the Selection name text field.
- 7 Click OK.
- 8 In the Settings window for Fiber, locate the Orientation section.
- **9** Specify the **Direction** vector as

```
-cos(alpha belt)
```

10 Right-click Fiber [Cords, Belt 2] and choose Duplicate.

Fiber [Cords, Belt 3]

- I In the Model Builder window, under 2D Axisymmetric [Tire] (compl)> Solid Mechanics (solid)>Thin Layer I>Hyperelastic Material I click Fiber [Cords, Belt 2] I.
- 2 In the Settings window for Fiber, type Fiber [Cords, Belt 3] in the Label text field.
- 3 Locate the Boundary Selection section. Click Clear Selection.
- 4 Select Boundary 59 only.
- 5 Click **Create Selection**.
- 6 In the Create Selection dialog box, type Belt 3 in the Selection name text field.
- 7 Click OK.
- 8 In the Settings window for Fiber, locate the Orientation section.

9 From the a list, choose Second axis.

Thin Layer 1

In the Model Builder window, under 2D Axisymmetric [Tire] (compl)>Solid Mechanics (solid) click Thin Layer 1.

## Roller I

- I In the Physics toolbar, click Attributes and choose Roller.
- 2 Select Points 46, 48, and 49 only. Because of the orientation of the fibers, the circumferential displacement will not be zero.
- 3 In the Model Builder window, click Solid Mechanics (solid).
- 4 In the Settings window for Solid Mechanics, locate the Axial Symmetry Approximation section.
- 5 Select the Include circumferential displacement check box.

Set the prestress in the bead wires.

Linear Elastic Material [Bead Wires]

In the Model Builder window, under 2D Axisymmetric [Tire] (comp I) > Solid Mechanics (solid) click Linear Elastic Material [Bead Wires].

Initial Stress and Strain I

- I In the Physics toolbar, click Attributes and choose Initial Stress and Strain.
- 2 In the Settings window for Initial Stress and Strain, locate the Initial Stress and Strain section.
- **3** In the  $S_0$  table, enter the following settings:

0	300[MPa]	0

## Contact I

- I In the Model Builder window, under 2D Axisymmetric [Tire] (comp1)> Solid Mechanics (solid) click Contact 1.
- 2 In the Settings window for Contact, locate the Contact Pressure Penalty Factor section.
- 3 From the Penalty factor control list, choose Manual tuning.
- 4 In the  $f_{\rm p}$  text field, type 2.

Set up the inner pressure.

#### **GLOBAL DEFINITIONS**

## Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
p0	200[kPa]	2E5 Pa	Inflation pressure
para	0	0	Continuation parameter for inflation

## SOLID MECHANICS (SOLID)

## Inner Pressure

- I In the Physics toolbar, click Boundaries and choose Boundary Load.
- 2 In the Settings window for Boundary Load, type Inner Pressure in the Label text field.
- **3** Select Boundaries 30, 45, and 48 only.
- 4 Locate the Force section. From the Load type list, choose Pressure.
- **5** In the *p* text field, type p0\*para.

Set up the symmetry plane.

## Symmetry Plane I

- I In the Physics toolbar, click Boundaries and choose Symmetry Plane.
- 2 Click the Select Box button in the Graphics toolbar.
- **3** Select Boundaries 20–23, 25, and 26 only.
- 4 In the Settings window for Symmetry Plane, locate the Circumferential Condition section.
- **5** From the list, choose **Antisymmetry**.

Set up the mesh.

#### MESH I

## Free Ouad I

- I In the Mesh toolbar, click Free Quad.
- 2 In the Settings window for Free Quad, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domains 2–4, 8, and 19 only.

**5** Click to expand the **Control Entities** section. Clear the Smooth across removed control entities check box.

## Distribution I

- I Right-click Free Quad I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 In the Number of elements text field, type 1.
- **4** Select Boundaries 15, 95, and 96 only.

### Distribution 2

- I In the Model Builder window, right-click Free Quad I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 From the Distribution type list, choose Predefined.
- **4** Select Boundaries 55, 56, and 70 only.
- 5 In the Number of elements text field, type 6.
- 6 In the Element ratio text field, type 1.2.
- 7 From the Growth rate list, choose Exponential.

#### Distribution 3

- I Right-click Free Quad I and choose Distribution.
- 2 Select Boundary 45 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 15.
- 6 In the Element ratio text field, type 1.4.
- 7 From the Growth rate list, choose Exponential.
- 8 Select the Reverse direction check box.
- **9** Right-click **Distribution 3** and choose **Duplicate**.

## Distribution 4

- I In the Model Builder window, click Distribution 4.
- **2** Select Boundary 71 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Element ratio text field, type 1.6.
- 5 Clear the Reverse direction check box.

6 Right-click Distribution 4 and choose Duplicate.

#### Distribution 5

- I In the Model Builder window, click Distribution 5.
- 2 Select Boundary 72 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Element ratio text field, type 1.8.

## Distribution 6

- I In the Model Builder window, right-click Free Quad I and choose Distribution.
- **2** Select Boundary 63 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 6.
- **5** Select Boundaries 42–44, 51, 52, and 63 only.

## Distribution 7

- I Right-click Free Quad I and choose Distribution.
- 2 Select Boundaries 34 and 37 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 2.

## Distribution 8

- I Right-click Free Quad I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 From the Distribution type list, choose Predefined.
- 4 In the Element ratio text field, type 1.5.
- **5** Select Boundary 30 only.

## Distribution 9

- I Right-click Free Quad I and choose Distribution.
- **2** Select Boundaries 32 and 35 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 3.

## Distribution 10

- I Right-click Free Quad I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.

- 3 From the Distribution type list, choose Predefined.
- 4 In the Number of elements text field, type 10.
- **5** In the **Element ratio** text field, type 1.5.
- 6 From the Growth rate list, choose Exponential.
- 7 Select the Symmetric distribution check box.
- 8 Select Boundaries 31, 33, and 36 only.

## Distribution 11

- I Right-click Free Quad I and choose Distribution.
- **2** Select Boundaries 46, 53, and 54 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 10.
- 6 In the Element ratio text field, type 5.
- 7 From the Growth rate list, choose Exponential.
- 8 Click **Build All**.

## Refine I

- I In the Mesh toolbar, click **Modify** and choose Refine.
- 2 In the Settings window for Refine, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 2–4 only.
- 5 Click | Build Selected.

## Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 5, 9-18, 21-37, 39-45 in the Selection text field.
- 6 Click OK.
- 7 In the Settings window for Mapped, click to expand the Control Entities section.
- 8 Clear the Smooth across removed control entities check box.

## Distribution I

- I Right-click Mapped I and choose Distribution.
- **2** Select Boundaries 24, 26, 27, 50, and 59–62 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 2.

#### Distribution 2

- I In the Model Builder window, right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- **3** In the **Number of elements** text field, type **3**.
- **4** Select Boundary 49 only.

## Distribution 3

- I Right-click Mapped I and choose Distribution.
- 2 Select Boundary 47 only.

#### Distribution 4

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- **3** In the **Number of elements** text field, type 1.
- **4** Select Boundaries 101–103 only.

## Distribution 5

- I Right-click Mapped I and choose Distribution.
- 2 In the Settings window for Distribution, locate the Distribution section.
- 3 In the Number of elements text field, type 12.
- 4 Select Boundary 131 only.

## Distribution 6

- I Right-click Mapped I and choose Distribution.
- **2** Select Boundary 130 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 From the Distribution type list, choose Predefined.
- 5 In the Number of elements text field, type 12.
- 6 In the Element ratio text field, type 1.2.
- 7 From the Growth rate list, choose Exponential.

- 8 Select the Reverse direction check box.
- 9 Click **Build Selected**.

## Mapped 2

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 38 only.
- 5 Locate the Control Entities section. Clear the Smooth across removed control entities check box.

## Free Triangular 1

- I In the Mesh toolbar, click Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 7 and 20 only.
- **5** Click to expand the **Control Entities** section. Clear the Smooth across removed control entities check box.

### Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra coarse.

#### Size 1

- I In the Model Builder window, right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Coarser.
- 4 Click Build Selected.

# Free Triangular 2

- I In the Mesh toolbar, click Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domain 6 only.

## Edge 1

- I In the Mesh toolbar, click \triangle More Generators and choose Edge.
- **2** Select Boundaries 8, 10, and 31 only.
- 3 In the Settings window for Edge, locate the Boundary Selection section.
- 4 In the list, select 31.
- 5 Click Remove from Selection.
- 6 Select Boundaries 8, 10, and 30 only.
- 7 In the list, select 30.
- 8 Click Remove from Selection.
- **9** Select Boundaries 7, 8, and 10 only.

#### Size 1

- I Right-click **Edge** I and choose **Size**.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extremely fine.
- 4 Click the **Custom** button.
- 5 Locate the Element Size Parameters section.
- 6 Select the Maximum element size check box. In the associated text field, type 0.05.
- 7 Click | Build Selected.

## Free Triangular 3

In the Mesh toolbar, click Free Triangular.

## Size 1

- I Right-click Free Triangular 3 and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extremely coarse.
- 4 Click Build All.

Refine the mesh for the 3D rim to improve visualization.

## **GEOMETRY 2**

In the Model Builder window, under 3D [Rim] (comp2) click Geometry 2.

Remove Details I (rmd1)

- I In the Geometry toolbar, click \* Remove Details.
- 2 Right-click Remove Details I (rmdI) and choose Build All.

#### MESH 2

- I In the Model Builder window, under 3D [Rim] (comp2) click Mesh 2.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Fine**.

#### STUDY: FIBER DIRECTION

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study: Fiber Direction in the Label text field.

## Step 1: Stationary

- I In the Model Builder window, under Study: Fiber Direction click Step I: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 3 Select the Modify model configuration for study step check box.
- 4 In the tree, select 2D Axisymmetric [Tire] (comp1)>Definitions>Contact Pair I (p1).
- 5 Click // Disable.
- 6 In the tree, select 2D Axisymmetric [Tire] (comp1)>Solid Mechanics (solid), Controls spatial frame.
- 7 Click Disable in Model.
- 8 In the Home toolbar, click **Compute**.

#### RESULTS

Coordinate System Surface 1

- I In the Model Builder window, expand the Coordinate system (cc) node, then click Coordinate System Surface 1.
- 2 In the Settings window for Coordinate System Surface, locate the Positioning section.
- 3 From the Placement list, choose Element centers.
- 4 In the Coordinate system (cc) toolbar, click Plot.

## ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- **2** Go to the **Add Study** window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

### STUDY: INFLATION

- I In the Model Builder window, click Study 2.
- 2 In the Settings window for Study, type Study: Inflation in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.

## Steb 1: Stationary

- I In the Model Builder window, under Study: Inflation click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check box for Curvilinear Coordinates (cc).
- 4 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 5 From the Method list, choose Solution.
- 6 From the Study list, choose Study: Fiber Direction, Stationary.
- 7 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 8 Click + Add.
- **9** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Continuation parameter for inflation)	range(0, 0.1, 1)	

10 In the Home toolbar, click **Compute**.

Use Add Predefined Plot to generate plots of the von Mises stress and the circumferential displacement.

## ADD PREDEFINED PLOT

- I In the Home toolbar, click Add Predefined Plot to open the Add Predefined Plot window.
- 2 Go to the Add Predefined Plot window.
- 3 In the tree, select Study: Inflation/Solution 2 (sol2)>Solid Mechanics>Stress (solid).
- 4 Click Add Plot in the window toolbar.
- 5 In the tree, select Study: Inflation/Solution 2 (sol2)>Solid Mechanics>Displacement (solid).
- 6 Click Add Plot in the window toolbar.

7 In the Home toolbar, click Add Predefined Plot to close the Add Predefined Plot window.

#### RESULTS

## Stress (solid)

- I In the Model Builder window, under Results click Stress (solid).
- 2 In the Settings window for 2D Plot Group, locate the Color Legend section.
- 3 Select the Show maximum and minimum values check box.

## Surface I

- I In the Model Builder window, expand the Stress (solid) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose MPa. Change the range of the plot to highlight the stress in the carcass.
- 4 Click to expand the Range section. Select the Manual color range check box.
- 5 In the Maximum text field, type 15.
- 6 In the Stress (solid) toolbar, click Plot.

Modify the plot of displacements in order to show the circumferential component.

## Out-of-Plane Displacement (solid)

- I In the Model Builder window, under Results click Displacement (solid).
- 2 In the Settings window for 2D Plot Group, type Out-of-Plane Displacement (solid) in the Label text field.

## Surface 1

- I In the Model Builder window, expand the Out-of-Plane Displacement (solid) node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type v.
- 4 From the Unit list, choose mm.
- 5 In the Out-of-Plane Displacement (solid) toolbar, click Plot. Add revolution datasets to plot the stress in 3D.
- 6 In the Model Builder window, click Results.
- 7 In the Settings window for Results, locate the Update of Results section.
- 8 Select the Only plot when requested check box.

## Revolution 2D: Tire

- I In the Results toolbar, click More Datasets and choose Revolution 2D.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Tire in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study: Inflation/Solution 2 (sol2).
- 4 Click to expand the Revolution Layers section. In the Start angle text field, type -90.
- 5 In the Revolution angle text field, type 225.

## Selection

- I In the Results toolbar, click has a Attributes and choose Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 2–6 only.

## Mirror 3D: Tire

- I In the Results toolbar, click More Datasets and choose Mirror 3D.
- 2 In the Settings window for Mirror 3D, type Mirror 3D: Tire in the Label text field.
- 3 Locate the Plane Data section. From the Plane list, choose xy-planes.
- 4 In the z-coordinate text field, type -7E-2.

## Stress, 3D (solid)

- I In the Results toolbar, click **3D Plot Group**.
- 2 In the Settings window for 3D Plot Group, type Stress, 3D (solid) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 3D: Tire.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 5 In the **Title** text area, type von Mises stress (MPa).
- **6** In the **Parameter indicator** text field, type para=eval(para).
- 7 Locate the Plot Settings section. Clear the Plot dataset edges check box.
- 8 Locate the Color Legend section. Select the Show maximum and minimum values check box.

#### Tire

- I Right-click Stress, 3D (solid) and choose Volume.
- 2 In the Settings window for Volume, locate the Expression section.
- 3 In the Expression text field, type solid.misesGp.

- 4 From the Unit list, choose MPa.
- **5** Click to expand the **Range** section. Select the **Manual color range** check box.
- 6 In the Maximum text field, type 180.
- 7 Locate the Coloring and Style section. Click Change Color Table.
- 8 In the Color Table dialog box, select Rainbow>Prism in the tree.
- 9 Click OK.
- 10 In the Settings window for Volume, type Tire in the Label text field.

## Deformation I

- I Right-click Tire and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box.

Add a dedicated dataset for the bead wires.

## Revolution 2D: Tire

In the Model Builder window, under Results>Datasets right-click Revolution 2D: Tire and choose **Duplicate**.

#### Revolution 2D: Bead Wires

- I In the Model Builder window, under Results>Datasets click Revolution 2D: Tire I.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Bead Wires in the **Label** text field.
- 3 Locate the Revolution Layers section. In the Revolution angle text field, type 275.

#### Selection

- I In the Model Builder window, expand the Revolution 2D: Bead Wires node, then click Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Bead Wires.

## Mirror 3D: Tire

In the Model Builder window, under Results>Datasets right-click Mirror 3D: Tire and choose Duplicate.

## Mirror 3D: Bead Wires

- I In the Model Builder window, under Results>Datasets click Mirror 3D: Tire I.
- 2 In the Settings window for Mirror 3D, type Mirror 3D: Bead Wires in the Label text field.

3 Locate the Data section. From the Dataset list, choose Revolution 2D: Bead Wires.

Tire

In the Model Builder window, under Results>Stress, 3D (solid) right-click Tire and choose Duplicate.

Bead Wires

- I In the Model Builder window, under Results>Stress, 3D (solid) click Tire I.
- 2 In the Settings window for Volume, type Bead Wires in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 3D: Bead Wires.
- 4 From the Solution parameters list, choose From parent.
- 5 Click to expand the Inherit Style section. From the Plot list, choose Tire.

Generate dedicated revolution datasets also for the belts.

Revolution 2D: Bead Wires

In the Model Builder window, under Results>Datasets right-click Revolution 2D: Bead Wires and choose **Duplicate**.

Revolution 2D: Belt I

- I In the Model Builder window, under Results>Datasets click Revolution 2D: Bead Wires I.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Belt 1 in the Label text field.
- 3 Locate the Revolution Layers section. In the Start angle text field, type 135.
- 4 In the Revolution angle text field, type 40.
- 5 From the Number of layers list, choose Fine.

Selection

- I In the Model Builder window, expand the Revolution 2D: Belt I node, then click Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Belt 1.

Mirror 3D: Bead Wires

In the Model Builder window, under Results>Datasets right-click Mirror 3D: Bead Wires and choose **Duplicate**.

Mirror 3D: Belt 1

I In the Model Builder window, under Results>Datasets click Mirror 3D: Bead Wires I.

- 2 In the Settings window for Mirror 3D, type Mirror 3D: Belt 1 in the Label text field.
- **3** Click to expand the **Advanced** section. Select the **Define variables** check box.
- 4 Locate the Data section. From the Dataset list, choose Revolution 2D: Belt 1.

Use a Streamline Surface plot to show the cords in the belt.

Stress, 3D (solid)

In the Model Builder window, under Results click Stress, 3D (solid).

#### Belt I

- I In the Stress, 3D (solid) toolbar, click More Plots and choose Streamline Surface.
- 2 In the Settings window for Streamline Surface, type Belt 1 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 3D: Belt 1.
- 4 From the Solution parameters list, choose From parent.
- **5** Locate the **Expression** section. In the **r-component** text field, type solid.tl1.hmm1.fibt1.aOR\*((mir1side\*2)-1).
- **6** In the **phi-component** text field, type solid.tl1.hmm1.fibt1.aOPHI.
- 7 In the **z-component** text field, type solid.tl1.hmm1.fibt1.a0Z\*((mir1side\*2)-1).
- **8** Select Domain 5 only.
- **9** Locate the **Streamline Positioning** section. From the **Positioning** list, choose Uniform density.
- 10 In the Separating distance text field, type 0.02.
- II Locate the Coloring and Style section. Find the Line style subsection. From the Type list, choose Tube.
- 12 In the Tube radius expression text field, type solid.tl1.hmm1.fibt1.d/2.
- 13 Select the Radius scale factor check box. In the associated text field, type 2.
- 14 Click to expand the Inherit Style section. From the Plot list, choose Tire.

## Color Expression 1

- I Right-click Belt I and choose Color Expression.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type solid.tl1.hmm1.fibt1.mises.
- 4 From the Unit list, choose MPa.

## Deformation I

In the Model Builder window, right-click Belt I and choose Deformation.

Revolution 2D: Belt I

In the Model Builder window, under Results>Datasets right-click Revolution 2D: Belt I and choose **Duplicate**.

Revolution 2D: Belt 2

- I In the Model Builder window, under Results>Datasets click Revolution 2D: Belt 1.1.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Belt 2 in the Label text field.
- 3 Locate the Revolution Layers section. In the Revolution angle text field, type 30.

Selection

- I In the Model Builder window, expand the Revolution 2D: Belt 2 node, then click Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- **3** From the **Selection** list, choose **Belt 2**.

Mirror 3D: Belt 1

In the Model Builder window, under Results>Datasets right-click Mirror 3D: Belt I and choose **Duplicate**.

Mirror 3D: Belt 2

- I In the Model Builder window, under Results>Datasets click Mirror 3D: Belt 1.1.
- 2 In the Settings window for Mirror 3D, type Mirror 3D: Belt 2 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Revolution 2D: Belt 2.

Relt 1

In the Model Builder window, under Results>Stress, 3D (solid) right-click Belt I and choose Duplicate.

Belt 2

- I In the Model Builder window, under Results>Stress, 3D (solid) click Belt 1.1.
- 2 In the Settings window for Streamline Surface, type Belt 2 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 3D: Belt 2.
- **4** Locate the **Expression** section. In the **r-component** text field, type solid.tl1.hmm1.fibt2.aOR\*((mir1side\*2)-1).
- **5** In the **phi-component** text field, type solid.tl1.hmm1.fibt2.aOPHI.
- 6 In the z-component text field, type solid.tl1.hmm1.fibt2.a0Z\*((mir1side\*2)-1).
- 7 Locate the Coloring and Style section. Find the Line style subsection. In the **Tube radius expression** text field, type solid.tl1.hmm1.fibt2.d/2.

Color Expression 1

- I In the Model Builder window, expand the Belt 2 node, then click Color Expression I.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type solid.tl1.hmm1.fibt2.mises.
- 4 In the Stress, 3D (solid) toolbar, click Plot.

Revolution 2D: Belt 2

In the Model Builder window, under Results>Datasets right-click Revolution 2D: Belt 2 and choose **Duplicate**.

Revolution 2D: Belt 3

- I In the Model Builder window, expand the Results>Datasets>Revolution 2D: Belt 2.I node, then click Revolution 2D: Belt 2.1.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Belt 3 in the Label text field.
- 3 Locate the Revolution Layers section. In the Revolution angle text field, type 20.

Selection

- I In the Model Builder window, click Selection.
- 2 In the Settings window for Selection, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Belt 3.

Mirror 3D: Belt 2

In the Model Builder window, under Results>Datasets right-click Mirror 3D: Belt 2 and choose **Duplicate**.

Mirror 2D: Belt 3

- I In the Model Builder window, click Mirror 3D: Belt 2.1.
- 2 In the Settings window for Mirror 3D, locate the Data section.
- 3 From the Dataset list, choose Revolution 2D: Belt 3.
- 4 In the Label text field, type Mirror 2D: Belt 3.

In the Model Builder window, under Results>Stress, 3D (solid) right-click Belt 2 and choose Duplicate.

Belt 3

- I In the Model Builder window, under Results>Stress, 3D (solid) click Belt 2.1.
- 2 In the Settings window for Streamline Surface, type Belt 3 in the Label text field.

- 3 Locate the Data section. From the Dataset list, choose Mirror 2D: Belt 3.
- **4** Locate the **Expression** section. In the **r-component** text field, type solid.tl1.hmm1.fibt3.aOR.
- **5** In the **phi-component** text field, type solid.tl1.hmm1.fibt3.aOPHI.
- **6** In the **z-component** text field, type solid.tl1.hmm1.fibt3.a0Z.
- 7 Locate the Streamline Positioning section. In the Separating distance text field, type 0.008.
- 8 From the Advanced parameters list, choose Manual.
- 9 In the Terminating distance factor text field, type 0.1.
- 10 Locate the Coloring and Style section. Find the Line style subsection. In the **Tube radius expression** text field, type solid.tl1.hmm1.fibt3.d/2.

## Color Expression 1

- I In the Model Builder window, expand the Belt 3 node, then click Color Expression I.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type solid.tl1.hmm1.fibt3.mises.
- 4 In the Stress, 3D (solid) toolbar, click Plot.

Study: Inflation/Solution 2 (sol2)

In the Model Builder window, under Results > Datasets right-click Study: Inflation/ Solution 2 (sol2) and choose Duplicate.

## Rim geometry

- I In the Model Builder window, under Results>Datasets click Study: Inflation/ Solution 2 (3) (sol2).
- 2 In the Settings window for Solution, type Rim geometry in the Label text field.
- 3 Locate the Solution section. From the Component list, choose 3D [Rim] (comp2).

## Rim

- I In the Model Builder window, right-click Stress, 3D (solid) and choose Surface.
- 2 In the Settings window for Surface, type Rim in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Rim geometry (sol2).
- **4** Locate the **Expression** section. In the **Expression** text field, type 1.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 Click to expand the Quality section. From the Resolution list, choose Fine.

Material Appearance 1

- I Right-click Rim and choose Material Appearance.
- 2 In the Stress, 3D (solid) toolbar, click Plot.

Stress, 3D (solid)

In the Model Builder window, under Results right-click Stress, 3D (solid) and choose Duplicate.

Material and Fiber Direction

- I In the Model Builder window, expand the Results>Stress, 3D (solid) I node, then click Stress, 3D (solid) I.
- 2 In the Settings window for 3D Plot Group, type Material and Fiber Direction in the Label text field.
- 3 Locate the Title section. From the Title type list, choose None.

Tire

- I In the Model Builder window, click Tire.
- 2 In the Settings window for Volume, locate the Expression section.
- **3** In the **Expression** text field, type 1.

Material Appearance 1

- I Right-click Tire and choose Material Appearance.
- 2 In the Settings window for Material Appearance, locate the Appearance section.
- 3 From the Material list, choose Material Link: Rubber [Sidewall and Tread] (matlnk2).
- 4 In the Material and Fiber Direction toolbar, click Plot.

Material Appearance 1

- I In the Model Builder window, right-click Bead Wires and choose Material Appearance.

Color Expression 1

- I In the Model Builder window, expand the Results>Material and Fiber Direction>Belt I
- 2 Right-click Color Expression I and choose Delete.

Belt I

- I In the Model Builder window, under Results>Material and Fiber Direction click Belt I.
- 2 In the Settings window for Streamline Surface, locate the Inherit Style section.
- 3 From the Plot list, choose None.

- 4 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose **Custom**.
- 5 On Windows, click the colored bar underneath, or if you are running the crossplatform desktop — the **Color** button.
- 6 Click Define custom colors.
- **7** Set the RGB values to 253, 185, and 19, respectively.
- 8 Click Add to custom colors.
- **9** Click **Show color palette only** or **OK** on the cross-platform desktop.

## Deformation I

- I In the Model Builder window, click Deformation I.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box. In the associated text field, type 1.

## Color Expression 1

- I In the Model Builder window, expand the Results>Material and Fiber Direction>Belt 2
- 2 Right-click Color Expression I and choose Delete.

#### Belt 2

- I In the Model Builder window, under Results>Material and Fiber Direction click Belt 2.
- 2 In the Settings window for Streamline Surface, locate the Inherit Style section.
- **3** From the **Plot** list, choose **None**.
- 4 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose Custom.
- 5 On Windows, click the colored bar underneath, or if you are running the crossplatform desktop — the **Color** button.
- 6 Click Define custom colors.
- **7** Set the RGB values to 54, 140, and 203, respectively.
- 8 Click Add to custom colors.
- **9** Click **Show color palette only** or **OK** on the cross-platform desktop.

#### Deformation I

- I In the Model Builder window, click Deformation I.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box. In the associated text field, type 1.

## Color Expression 1

- I In the Model Builder window, expand the Belt 3 node.
- 2 Right-click Color Expression I and choose Delete.

#### Belt 3

- I In the Model Builder window, under Results>Material and Fiber Direction click Belt 3.
- 2 In the Settings window for Streamline Surface, locate the Inherit Style section.
- **3** From the **Plot** list, choose **None**.
- 4 Locate the Coloring and Style section. Find the Point style subsection. From the Color list, choose **Custom**.
- 5 On Windows, click the colored bar underneath, or if you are running the crossplatform desktop — the **Color** button.
- 6 Click Define custom colors.
- 7 Set the RGB values to 166, 214, and 208, respectively.
- 8 Click Add to custom colors.
- **9** Click **Show color palette only** or **OK** on the cross-platform desktop.

## Deformation I

- I In the Model Builder window, click Deformation I.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box. In the associated text field, type 1.
- 4 In the Material and Fiber Direction toolbar, click Plot.

### Revolution 2D: Belt 1

In the Model Builder window, under Results>Datasets right-click Revolution 2D: Belt I and choose **Duplicate**.

## Revolution 2D: Carcass

- I In the Model Builder window, expand the Results>Datasets>Revolution 2D: Belt 1.1 node, then click Revolution 2D: Belt I.I.
- 2 In the Settings window for Revolution 2D, type Revolution 2D: Carcass in the Label text field.
- 3 Locate the Revolution Layers section. In the Revolution angle text field, type 50.

## Selection

- I In the Model Builder window, click Selection.
- **2** Select Boundaries 35–37, 42, 52, 53, and 56 only.

## Mirror 3D: Belt 1

In the Model Builder window, under Results>Datasets right-click Mirror 3D: Belt I and choose **Duplicate**.

## Mirror 3D: Carcass

- I In the Model Builder window, under Results>Datasets click Mirror 3D: Belt 1.1.
- 2 In the Settings window for Mirror 3D, type Mirror 3D: Carcass in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Revolution 2D: Carcass.

#### Belt I

In the Model Builder window, under Results>Material and Fiber Direction right-click Belt I and choose **Duplicate**.

#### Carcass

- I In the Model Builder window, under Results>Material and Fiber Direction click Belt 1.1.
- 2 In the Settings window for Streamline Surface, type Carcass in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 3D: Carcass.
- 4 Click Replace Expression in the upper-right corner of the Expression section. From the menu, choose 2D Axisymmetric [Tire] (compl)>Curvilinear Coordinates>cc.elR,cc.elPHI, cc.e1Z - First basis vector.
- 5 Locate the Expression section. In the r-component text field, type cc.e1R\*((mir1side\* 2)-1).
- 6 In the **z-component** text field, type cc.e1Z\*((mir1side\*2)-1).
- 7 Locate the Surface Selection section. Click to select the Activate Selection toggle button.
- **8** Select Domain 4 only.
- 9 Locate the Streamline Positioning section. In the Separating distance text field, type 0.01.
- 10 Locate the Coloring and Style section. Find the Line style subsection. In the Tube radius expression text field, type dcord\_belts/2.
- II Find the Point style subsection. From the Color list, choose Red.
- 12 In the Material and Fiber Direction toolbar, click Plot.
- 13 Click Plot.
- 14 In the Model Builder window, click Results.
- 15 In the Settings window for Results, locate the Update of Results section.
- **16** Clear the **Only plot when requested** check box.

Generate a dedicated view for the 3D plots.

### View 3D 8

In the Model Builder window, under Results right-click Views and choose View 3D.

#### Camera

- I Click the **Show Grid** button in the **Graphics** toolbar.
- 2 Click the Show Axis Orientation button in the Graphics toolbar.
- 3 In the Model Builder window, expand the View 3D 8 node, then click Camera.
- 4 In the Settings window for Camera, in the Graphics window toolbar, click ▼ next to Scene Light, then choose Ambient Occlusion.
- 5 In the **Graphics** window toolbar, click ▼ next to **Scene Light**, then choose Direct Shadows.
- 6 In the Graphics window toolbar, click ▼ next to Scene Light, then choose **Outdoor Environment.**
- 7 In the Graphics window toolbar, click rext to Scene Light, then choose Floor Shadows.
- 8 Locate the Camera section. In the Zoom angle text field, type 5.
- **9** Locate the **Position** section. In the **x** text field, type -263.
- 10 In the y text field, type 195.
- II In the **z** text field, type 373.
- 12 Locate the **Target** section. In the **x** text field, type 0.78.
- **I3** In the y text field, type 0.
- 14 In the z text field, type -0.04.
- **I5** Locate the **Up Vector** section. In the **x** text field, type -0.7.
- **16** In the **y** text field, type 0.71.
- 17 In the z text field, type -0.12.
- **18** Locate the **Center of Rotation** section. In the **x** text field, type 0.78.
- **19** In the **y** text field, type -0.005.
- 20 In the z text field, type 0.044.

#### Material and Fiber Direction

- I In the Model Builder window, under Results click Material and Fiber Direction.
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- 3 From the View list, choose View 3D 8.

- 4 In the Material and Fiber Direction toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Make the cords unaffected by lighting such that results remain clear to be read.

## Visual Effects 1

- I In the Model Builder window, right-click Belt I and choose Visual Effects.
- 2 In the Settings window for Visual Effects, locate the Visual Effects section.
- 3 Clear the Affected by lighting check box.
- 4 Find the Ambient occlusion subsection. From the Mode list, choose Manual.
- 5 Clear the Casts shadows check box.
- 6 Clear the Receives shadows check box.
- 7 Find the Direct shadows subsection. From the Mode list, choose Manual.
- 8 Clear the Casts shadows check box.
- **9** Clear the **Receives shadows** check box.
- 10 Right-click Visual Effects I and choose Copy.

## Belt 2

In the Model Builder window, under Results>Material and Fiber Direction right-click Belt 2 and choose Paste Visual Effects.

#### Belt 3

In the Model Builder window, right-click Belt 3 and choose Paste Visual Effects.

#### Carcass

In the Model Builder window, right-click Carcass and choose Paste Visual Effects.

## Visual Effects 1

- I In the Model Builder window, click Visual Effects I.
- 2 In the Material and Fiber Direction toolbar, click Plot.

## Stress, 3D (solid)

- I In the Model Builder window, under Results click Stress, 3D (solid).
- 2 In the Settings window for 3D Plot Group, locate the Plot Settings section.
- 3 From the View list, choose View 3D 8.
- 4 In the Stress, 3D (solid) toolbar, click **Plot**.

## Belt I

In the Model Builder window, right-click Belt I and choose Paste Visual Effects.

# Belt 2

In the Model Builder window, right-click Belt 2 and choose Paste Visual Effects.

## Belt 3

In the Model Builder window, right-click Belt 3 and choose Paste Visual Effects.