

Heterogeneous Lithium-Ion Battery

Most lithium-ion battery models make use of a homogenized domain formulation of the porous electrodes, which solve simultaneously for the electrode phase and electrolyte phase potentials in the same domain, defining the electrode reactions by the use of source terms. In these models, the diffusion of lithium into the solid electrode particles is modeled by the use of an extra dimension, representing an average particle for a certain position in the electrode. This modeling approach has great advantages in terms of a relatively small computational load, allowing most models to be formulated in one dimension only, representing the electrode depth (plus the extra dimension for defining the particle diffusion dimension).

However, certain phenomena cannot be captured using the above approach. For instance, the above particle diffusion model inherently assumes either Cartesian, cylindrical, or spherical symmetry, thus not allowing modeling the impact of irregular particle shapes, nor the impact of micro- and macropore distributions.

The instead of homogenizing the porous electrode, you can instead include the structural details of the porous electrodes in the model geometry. Such models are referred to as heterogeneous models.

This tutorial describes the behavior of a lithium-ion battery unit cell modeled using a three-dimensional geometry, where a number of ellipses are used to define the electrode particles in the two electrodes. The model can be used as a starting point for modeling more realistic electrode geometries, for instance based on tomography data.

This tutorial also demonstrates how to couple the lithium concentration distribution in the particles to a corresponding volumetric expansion in the Solid Mechanics interface and the resulting von Mises stresses.

Model Definition

The model geometry is shown in Figure 1. The geometry consists of a rectangular block, forming a representative unit cell of the model geometry. The two electrodes are defined using a number of ellipses.

The battery chemistry is modeled using a **Lithium-Ion Battery** interface using the **Electrolyte** node to define the concentrated battery electrolyte charge and ion transport. Two **Electrode** nodes are used to define the ohmic drop due to the current conduction in each electrode phase. On the interior boundaries between the electrode and electrolyte phases, Internal Electrode Surface nodes are used to define the charge transfer reactions. Transport of solid lithium in the electrode phases is modeled using a separate Transport of Diluted Species interface, which defines the molecular flux of lithium according to Fick's law. **Electrode Surface Coupling** nodes define the molecular flux on the external boundaries to the electrode particles, stemming from the electrochemical reactions.

The concentration of solid lithium is coupled to the Lithium Insertion Reaction electrode kinetics, defined in the Electrode Reaction subnodes to the Internal Electrode Surface nodes.

As the lithium concentration increases in the negative graphite electrode material, the material expands. This is modeled using a Solid Mechanics interface, where expansion is defined as an initial strain in the Initial Stress and Strain node (subnode to the Linear-Elastic Material node). The expansion is defined as a function of the local solid lithium concentration using an interpolation function, based on experimental data (Ref. 1).

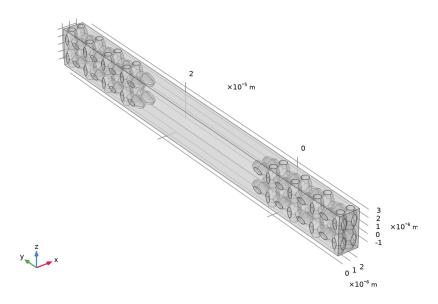


Figure 1: Model geometry. The negative graphite electrode located toward the upper left and the positive LCO electrode is located toward the lower right in the figure.

The model is solved using two different studies. The first, time-dependent study, simulates a high-rate discharge during 20 s, solving for the Lithium-Ion Battery and Transport of Diluted Species interfaces only. The second, stationary study, solves for the Solid

Mechanics interface only, using the results of Study 1 for the concentration distribution in the battery at 0 and 20 s as input.

Results and Discussion

Figure 2 shows the solid lithium concentration in the particles after 75 s of discharge. For the negative electrode, the solid lithium concentration is generally lower toward the electrolyte and higher toward the current collector — reflecting what parts of the electrode surface are more accessible for charge transfer. A similar trend is seen for the positive electrode.

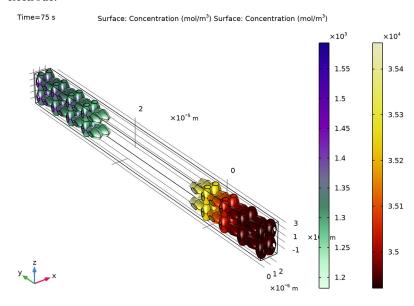


Figure 2: Surface concentration of solid lithium at the surface at the electrode particles at t = 75 s.

Figure 3 shows a slice plot of the solid lithium concentration at 75 s, demonstrating a significant concentration gradient from the center of the particles toward the surface.

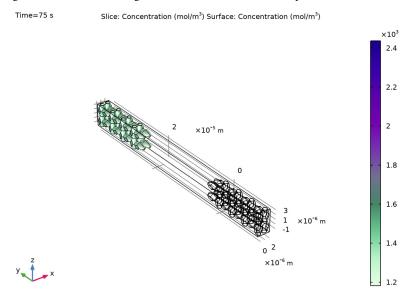


Figure 3: Slice plot of the solid lithium concentration in the negative electrode at t = 75 s.

Figure 4 shows the current distribution in the electrolyte at the same time. The maximum values of the reaction current density at 75 s is located in the negative electrode at the parts of the surface with the highest solid lithium concentration values (see Figure 2).

Time=75 s Surface: abs(liion.iloc_er1) (A/m²) Surface: abs(liion.iloc_er1) (A/m²) Streamline: Electrolyte current density vector

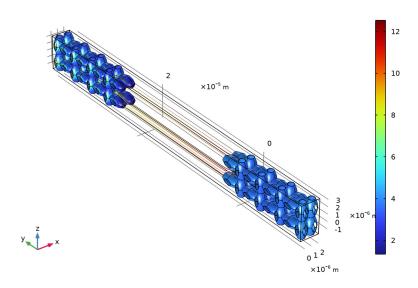


Figure 4: Electrolyte current density magnitude at t=75 s.

Finally, Figure 5 shows the resulting von Mises stresses, based on the graphite lithium concentration at t = 75 s, in combination with the experimental expansion function.

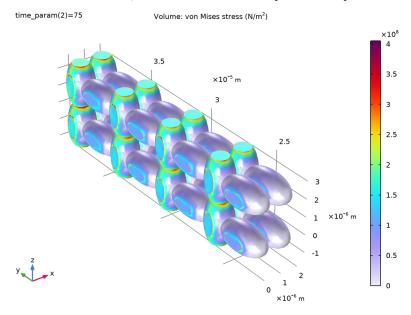


Figure 5: The von Mises stress at the surface of the negative graphite particles at t = 75s.

Reference

- 1. J.B. Siegel, A.G. Stefanopoulou, P. Hagans, Y. Ding, and D. Gorsich,
- J. Electrochemical Soc., vol. 160, p. A1031, 2013.

Application Library path: Battery Design Module/Batteries, Heterogeneous/ heterogeneous_li_battery

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Electrochemistry>Batteries>Lithium-Ion Battery (liion).
- Click Add.
- 4 In the Select Physics tree, select Chemical Species Transport> Transport of Diluted Species (tds).
- 5 Click Add.
- 6 In the Concentrations (mol/m³) table, enter the following settings:

cs

- 7 Click 🔁 Study.
- 8 In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Lithium-Ion Battery>Time Dependent with Initialization.
- 9 Click M Done.

GEOMETRY I

Insert a prepared geometry sequence from a file. You can follow the steps required to build the geometry in the section Appendix — Geometry Modeling Instructions.

- I In the Geometry toolbar, click Insert Sequence and choose Insert Sequence.
- 2 Browse to the model's Application Libraries folder and double-click the file heterogeneous_li_battery_geom_sequence.mph.
- 3 In the Geometry toolbar, click **Build All**.
- **4** Click the **Zoom Extents** button in the **Graphics** toolbar.

GEOMETRY I

In the Model Builder window, collapse the Component I (compl)>Geometry I node.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.

3 In the table, enter the following settings:

Name	Expression	Value	Description
csmax_neg	31507[mol/m^3]	31507 mol/m³	Maximum lithium concentration in graphite
iOref_neg	0.96[A/m^2]	0.96 A/m ²	Reference exchange current density negative
iOref_pos	1.72[A/m^2]	1.72 A/m ²	Reference exchange current density positive
exp_max	10[%]	0.1	
time_param	1	I	Time parameter for parametric sweep

DEFINITIONS

Variables 1

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click **Definitions** and choose **Variables**.
- 3 In the Settings window for Variables, locate the Variables section.
- 4 Click Load from File.
- **5** Browse to the model's Application Libraries folder and double-click the file heterogeneous_li_battery_variables.txt.

ADD MATERIAL

- I In the Home toolbar, click **‡** Add Material to open the Add Material window.
- 2 Go to the Add Material window.

Add the electrolyte first, then graphite, and finally LCO. The order is important since it will determine the tags (mat1, mat2, and mat3) the added material nodes get in the model tree. These tags will be used later in certain variable declarations.

- 3 In the tree, select Battery>Electrolytes>LiPF6 in 1:2 EC:DMC and p(VdF-HFP) (Polymer, Liion Battery).
- 4 Click Component I (compl) in the window toolbar.
- 5 In the tree, select Battery>Electrodes>Graphite, LixC6 MCMB (Negative, Li-ion Battery).
- **6** Click **Component I (compl)** in the window toolbar.
- 7 In the tree, select Battery>Electrodes>LCO, LiCoO2 (Positive, Li-ion Battery).

- **8** Click **Component I (compl)** in the window toolbar.
- 9 In the Home toolbar, click 👯 Add Material to close the Add Material window.

MATERIALS

LiPF6 in 1:2 EC:DMC and p(VdF-HFP) (Polymer, Li-ion Battery) (mat1)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Selection list, choose Electrolyte.

Graphite, LixC6 MCMB (Negative, Li-ion Battery) (mat2)

- I In the Model Builder window, click Graphite, LixC6 MCMB (Negative, Liion Battery) (mat2).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Negative electrode.

LCO, LiCoO2 (Positive, Li-ion Battery) (mat3)

- I In the Model Builder window, click LCO, LiCoO2 (Positive, Li-ion Battery) (mat3).
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- **3** From the **Selection** list, choose **Positive electrode**.

LITHIUM-ION BATTERY (LIION)

Separator I

- I In the Model Builder window, under Component I (compl)>Lithium-lon Battery (liion) click **Separator 1**.
- 2 In the Settings window for Separator, locate the Electrolyte Properties section.
- 3 From the Electrolyte material list, choose LiPF6 in 1:2 EC:DMC and p(VdF-HFP) (Polymer, Li-ion Battery) (mat I).
- **4** Locate the **Porous Matrix Properties** section. In the ε_1 text field, type 1.

Initial Values - Negative and Electrolyte

- I In the Model Builder window, click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- **3** In the *phil* text field, type phil init.
- 4 In the Label text field, type Initial Values Negative and Electrolyte.

Initial Values - Positive

I In the Physics toolbar, click **Domains** and choose Initial Values.

- 2 In the Settings window for Initial Values, locate the Domain Selection section.
- 3 From the Selection list, choose Positive electrode.
- 4 In the Label text field, type Initial Values Positive.
- **5** Locate the **Initial Values** section. In the *phil* text field, type phil init.
- **6** In the *phis* text field, type E cell init.

Electrode - Negative

- I In the Physics toolbar, click **Domains** and choose Current Conductor.
- 2 In the Settings window for Current Conductor, type Electrode Negative in the Label text field.
- 3 Locate the Domain Selection section. From the Selection list, choose Negative electrode.
- 4 Right-click Electrode Negative and choose Duplicate.

Electrode - Positive

- I In the Model Builder window, click Electrode Negative I.
- 2 In the Settings window for Current Conductor, locate the Domain Selection section.
- 3 From the Selection list, choose Positive electrode.
- 4 In the Label text field, type Electrode Positive.

Internal Electrode Surface I

- I In the Physics toolbar, click **Boundaries** and choose **Internal Electrode Surface**.
- 2 In the Settings window for Internal Electrode Surface, locate the Boundary Selection section.
- 3 From the Selection list, choose Negative electrode surface.

Electrode Reaction 1

- I In the Model Builder window, click Electrode Reaction I.
- 2 In the Settings window for Electrode Reaction, locate the Model Input section.
- **3** From the c list, choose **Concentration (tds)**.
- 4 Locate the **Electrode Kinetics** section. From the **Kinetics expression type** list, choose Lithium insertion.
- 5 Locate the Material section. From the Material list, choose Graphite, LixC6 MCMB (Negative, Li-ion Battery) (mat2).
- **6** Locate the **Electrode Kinetics** section. In the $i_{0 \text{ ref}}(T)$ text field, type i0ref_neg.

Internal Electrode Surface 1

In the Model Builder window, click Internal Electrode Surface 1.

Double-Layer Capacitance I

In the Physics toolbar, click 🖳 Attributes and choose Double-Layer Capacitance.

Internal Electrode Surface - Negative

- I In the Model Builder window, under Component I (compl)>Lithium-lon Battery (liion) click Internal Electrode Surface I.
- 2 In the Settings window for Internal Electrode Surface, type Internal Electrode Surface - Negative in the Label text field.

Internal Electrode Surface - Positive

- In the Physics toolbar, click Boundaries and choose Internal Electrode Surface.
- 2 In the Settings window for Internal Electrode Surface, type Internal Electrode Surface - Positive in the Label text field.
- 3 Locate the Boundary Selection section. From the Selection list, choose Positive electrode surface.

Electrode Reaction 1

- I In the Model Builder window, click Electrode Reaction I.
- 2 In the Settings window for Electrode Reaction, locate the Model Input section.
- **3** From the c list, choose **Concentration (tds)**.
- 4 Locate the Electrode Kinetics section. From the Kinetics expression type list, choose Lithium insertion.
- 5 Locate the Material section. From the Material list, choose LCO, LiCoO2 (Positive, Liion Battery) (mat3).
- **6** Locate the **Electrode Kinetics** section. In the $i_{0,ref}(T)$ text field, type iOref_pos.

Internal Electrode Surface - Positive

In the Model Builder window, click Internal Electrode Surface - Positive.

Double-Layer Capacitance 1

In the Physics toolbar, click 🖳 Attributes and choose Double-Layer Capacitance.

Electric Ground 1

- I In the Physics toolbar, click **Boundaries** and choose **Electric Ground**.
- 2 In the Settings window for Electric Ground, locate the Boundary Selection section.
- 3 From the Selection list, choose Negative current collector.

Electrode Current I

I In the Physics toolbar, click **Boundaries** and choose **Electrode Current**.

- 2 In the Settings window for Electrode Current, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Positive current collector**.
- **4** Locate the **Electrode Current** section. In the $I_{s,total}$ text field, type -1e-9[A].
- **5** In the $\phi_{s.bnd.init}$ text field, type E_cell_init.

DEFINITIONS

phis

- I In the Definitions toolbar, click Probes and choose Boundary Probe.
- 2 In the Settings window for Boundary Probe, type phis in the Label text field.
- 3 Locate the Source Selection section. From the Selection list, choose Manual.
- 4 Click Clear Selection.
- 5 Click Paste Selection.
- 6 In the Paste Selection dialog box, type 210 in the Selection text field.
- 7 Click OK.
- 8 In the Settings window for Boundary Probe, locate the Expression section.
- **9** In the **Expression** text field, type phis.

TRANSPORT OF DILUTED SPECIES (TDS)

- I In the Model Builder window, under Component I (compl) click Transport of Diluted Species (tds).
- **2** Select Domains 2 and 3 only.
- 3 In the Settings window for Transport of Diluted Species, locate the Transport Mechanisms section.
- 4 Clear the **Convection** check box.
- 5 Click to expand the **Discretization** section. From the **Concentration** list, choose **Quadratic**.

Transport Properties - Negative

- I In the Model Builder window, under Component I (compl)> Transport of Diluted Species (tds) click Transport Properties 1.
- 2 In the Settings window for Transport Properties, type Transport Properties -Negative in the Label text field.
- 3 Locate the Diffusion section. From the Material list, choose Graphite, LixC6 MCMB (Negative, Li-ion Battery) (mat2).
- **4** From the D_{cs} list, choose **Basic** (def).

Initial Values - Negative

- I In the Model Builder window, under Component I (compl)> Transport of Diluted Species (tds) click Initial Values 1.
- 2 In the Settings window for Initial Values, type Initial Values Negative in the Label text field.
- 3 Locate the **Initial Values** section. In the cs text field, type csinit neg.

Transport Properties - Positive

- I In the Physics toolbar, click **Domains** and choose **Transport Properties**.
- 2 In the Settings window for Transport Properties, type Transport Properties -Positive in the Label text field.
- 3 Locate the Domain Selection section. From the Selection list, choose Positive electrode.
- 4 Locate the Diffusion section. From the Material list, choose LCO, LiCoO2 (Positive, Liion Battery) (mat3).
- **5** From the D_{cs} list, choose **Basic** (def).

Initial Values - Positive

- I In the Physics toolbar, click **Domains** and choose Initial Values.
- 2 In the Settings window for Initial Values, type Initial Values Positive in the Label text field.
- 3 Locate the Domain Selection section. From the Selection list, choose Positive electrode.
- **4** Locate the **Initial Values** section. In the *cs* text field, type csinit_pos.

Electrode Surface Coupling I

- I In the Physics toolbar, click **Boundaries** and choose **Electrode Surface Coupling**.
- 2 In the Settings window for Electrode Surface Coupling, locate the Boundary Selection section.
- 3 From the Selection list, choose Negative electrode surface.

Reaction Coefficients I

- I In the Model Builder window, expand the Electrode Surface Coupling I node, then click Reaction Coefficients 1.
- 2 In the Settings window for Reaction Coefficients, locate the Model Inputs section.
- 3 From the i_{loc} list, choose Local current density, Electrode Reaction I (liion/beil/erl).
- **4** Locate the **Stoichiometric Coefficients** section. In the v_{cs} text field, type 1.

Electrode Surface Coupling 2

- In the Physics toolbar, click Boundaries and choose Electrode Surface Coupling.
- 2 In the Settings window for Electrode Surface Coupling, locate the Boundary Selection section.
- 3 From the Selection list, choose Positive electrode surface.

Reaction Coefficients I

- I In the Model Builder window, expand the Electrode Surface Coupling 2 node, then click Reaction Coefficients I.
- 2 In the Settings window for Reaction Coefficients, locate the Model Inputs section.
- 3 From the i_{loc} list, choose Local current density, Electrode Reaction I (liion/bei2/er1).
- **4** Locate the **Stoichiometric Coefficients** section. In the v_{cs} text field, type 1.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- 3 From the Element size list, choose Coarse.

Free Tetrahedral I

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Settings window for Free Tetrahedral, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Click Paste Selection.
- 5 In the Paste Selection dialog box, type 2 3 in the Selection text field.
- 6 Click OK.

Size 1

- I Right-click Free Tetrahedral I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Selection list, choose Negative electrode.
- 4 Locate the Element Size section. From the Predefined list, choose Fine.

Size 2

- I In the Model Builder window, right-click Free Tetrahedral I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- **3** From the **Selection** list, choose **Positive electrode**.

4 Locate the Element Size section. From the Predefined list, choose Fine.

Free Tetrahedral 2

In the Mesh toolbar, click A Free Tetrahedral.



Size 1

- I Right-click Free Tetrahedral 2 and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Finer.
- 4 Click Build All.

STUDY I - DISCHARGE

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study 1 Discharge in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.

Solution I (soll)

In the Study toolbar, click Show Default Solver.

Step 1: Current Distribution Initialization

- I In the Model Builder window, under Study I Discharge click Step 1: Current Distribution Initialization.
- 2 In the Settings window for Current Distribution Initialization, locate the Study Settings section.
- 3 From the Current distribution type list, choose Secondary.
- 4 Locate the Physics and Variables Selection section. In the table, clear the Solve for check box for Transport of Diluted Species (tds).

Step 2: Time Dependent

- I In the Model Builder window, click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0,5,75).
- **4** From the **Tolerance** list, choose **User controlled**.
- 5 In the Relative tolerance text field, type 1e-4.

Solution I (soll)

I In the Model Builder window, expand the Solution I (soll) node.

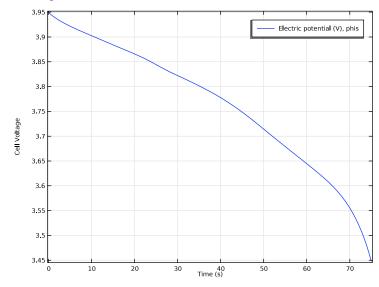
- 2 In the Model Builder window, under Study I Discharge>Solver Configurations> Solution I (soll) click Time-Dependent Solver I.
- 3 In the Settings window for Time-Dependent Solver, click to expand the Time Stepping section.
- 4 Find the Algebraic variable settings subsection. From the Consistent initialization list, choose Off.
- 5 Right-click Study I Discharge>Solver Configurations>Solution I (sol1)>Time-**Dependent Solver I** and choose **Fully Coupled**.
- 6 In the Study toolbar, click **Compute**.

RESULTS

Cell Voltage

- I In the Settings window for ID Plot Group, type Cell Voltage in the Label text field.
- 2 Locate the Plot Settings section.
- 3 Select the y-axis label check box. In the associated text field, type Cell Voltage.
- 4 In the Cell Voltage toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

The plot should look as shown below:



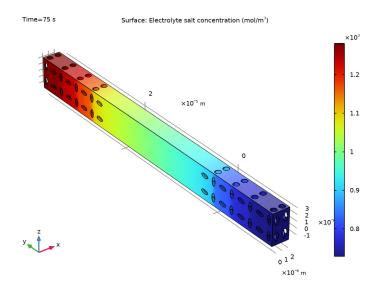
Electrolyte Salt Concentration (liion)

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Electrolyte Salt Concentration (liion) in the Label text field.

Surface I

- I Right-click Electrolyte Salt Concentration (liion) and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type cl.
- 4 In the Electrolyte Salt Concentration (liion) toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

The plot should look as shown below:



Electrolyte Potential (liion)

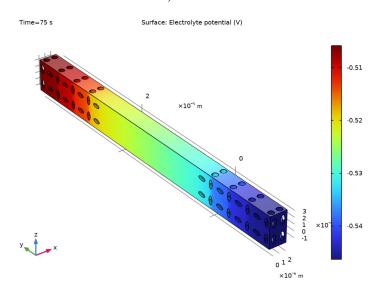
- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Electrolyte Potential (liion) in the Label text field.

Surface I

- I Right-click Electrolyte Potential (liion) and choose Surface.
- 2 In the Electrolyte Potential (liion) toolbar, click Plot.

3 Click the **Zoom Extents** button in the **Graphics** toolbar. The plot should look as shown below:

4 In the Model Builder window, click Surface 1.



Lithium Concentration Surface (tds)

The following steps reproduce the figures in the Results and Discussion section.

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Lithium Concentration Surface (tds) in the Label text field.

Negative Electrode

- I Right-click Lithium Concentration Surface (tds) and choose Surface.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Aurora Aurora Borealis in the tree.
- 5 Click OK.
- 6 In the Settings window for Surface, type Negative Electrode in the Label text field.
- 7 Locate the Expression section. In the Expression text field, type cs.

Selection I

I Right-click Negative Electrode and choose Selection.

- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Negative electrode surface.
- 4 In the Lithium Concentration Surface (tds) toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Negative Electrode

In the Model Builder window, right-click Negative Electrode and choose Duplicate.

Positive Electrode

- I In the Model Builder window, click Negative Electrode I.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Thermal>ThermalDark in the tree.
- 5 Click OK.
- 6 In the Settings window for Surface, type Positive Electrode in the Label text field.

Selection 1

- I In the Model Builder window, expand the Positive Electrode node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Positive electrode surface.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Current Distribution

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Current Distribution in the Label text field.

Negative Electrode

- I Right-click Current Distribution and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type abs(liion.iloc er1).
- 4 In the Label text field, type Negative Electrode.

Selection 1

- I Right-click Negative Electrode and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.

- 3 From the Selection list, choose Negative electrode surface.
- 4 In the Current Distribution toolbar, click Plot.

Negative Electrode

In the Model Builder window, right-click Negative Electrode and choose Duplicate.

Positive Electrode

- I In the Model Builder window, under Results>Current Distribution click Negative Electrode 1.
- 2 In the Settings window for Surface, type Positive Electrode in the Label text field.
- 3 Click to expand the Inherit Style section. From the Plot list, choose Negative Electrode.

Selection 1

- I In the Model Builder window, expand the Positive Electrode node, then click Selection I.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Positive electrode surface.

Streamline 1

- I In the Model Builder window, right-click Current Distribution and choose Streamline.
- 2 In the Settings window for Streamline, locate the Selection section.
- 3 From the Selection list, choose Negative electrode surface.
- 4 Locate the Coloring and Style section. Find the Line style subsection. From the Type list, choose Ribbon.
- 5 In the Width expression text field, type liion. IlMag.
- 6 Select the Width scale factor check box. In the associated text field, type 4e-10.
- 7 Click to expand the Quality section. From the Recover list, choose Within domains.

Color Expression 1

- I Right-click Streamline I and choose Color Expression.
- 2 In the Settings window for Color Expression, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Thermal>ThermalDark in the tree.
- 5 Click OK.
- 6 In the Settings window for Color Expression, locate the Coloring and Style section.
- 7 Clear the Color legend check box.
- **8** In the Current Distribution toolbar, click **Plot**.

9 Click the **Zoom Extents** button in the **Graphics** toolbar.

Lithium Concentration in Negative Electrode

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Lithium Concentration in Negative Electrode in the Label text field.

Slice 1

- I Right-click Lithium Concentration in Negative Electrode and choose Slice.
- 2 In the Settings window for Slice, click Replace Expression in the upper-right corner of the **Expression** section. From the menu, choose **Component I (compl)>** Transport of Diluted Species>Species cs>cs - Concentration - mol/m3.
- 3 Locate the Plane Data section. From the Plane list, choose XY-planes.
- 4 In the Planes text field, type 2.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Aurora Aurora Borealis in the tree.
- 7 Click OK.

Selection 1

- I Right-click Slice I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Negative electrode.

Surface 1

- I In the Model Builder window, right-click Lithium Concentration in Negative Electrode and choose Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Transport of Diluted Species>Species cs>cs - Concentration - mol/m3.
- 3 Locate the Inherit Style section. From the Plot list, choose Slice 1.

Selection 1

- I Right-click Surface I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Negative electrode surface.

Setting up and solving for the heterogeneous battery is now complete. Next, extend the model to analyze the stresses and strains using the **Structural Mechanics** interface.

ADD PHYSICS

- I In the Home toolbar, click open the Add Physics window.
- 2 Go to the Add Physics window.
- 3 In the tree, select Structural Mechanics>Solid Mechanics (solid).
- **4** Click **Add to Component I** in the window toolbar.
- 5 In the Home toolbar, click and Physics to close the Add Physics window.

SOLID MECHANICS (SOLID)

- I In the Settings window for Solid Mechanics, click to expand the Dependent Variables section.
- 2 Locate the **Domain Selection** section. From the **Selection** list, choose **Negative electrode**.

Linear Elastic Material I

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.
- 2 In the Settings window for Linear Elastic Material, locate the Model Input section.
- **3** From the c list, choose Concentration (tds).

Intercalation Strain I

- I In the Physics toolbar, click 🕞 Attributes and choose Intercalation Strain. The volumetric strain is taken **From material** by default. Couple the strain to the concentration solved for by the **Transport of Diluted Species** interface as follows:
- 2 In the Settings window for Intercalation Strain, locate the Model Input section.
- **3** From the c list, choose **Concentration (tds)**.

Roller I

- I In the Physics toolbar, click **Boundaries** and choose Roller.
- 2 In the Settings window for Roller, locate the Boundary Selection section.
- 3 From the Selection list, choose Roller condition boundaries.

Prescribed Displacement I

In the Physics toolbar, click **Boundaries** and choose **Prescribed Displacement**.

- 2 In the Settings window for Prescribed Displacement, locate the Boundary Selection section.
- 3 From the Selection list, choose Negative current collector.
- 4 Locate the Prescribed Displacement section. From the Displacement in x direction list, choose Prescribed.
- 5 From the Displacement in y direction list, choose Prescribed.
- 6 From the Displacement in z direction list, choose Prescribed.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies>Stationary.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2 - EXPANSION AND STRESS

- I In the Model Builder window, click Study 2.
- 2 In the Settings window for Study, type Study 2 Expansion and Stress in the Label text field.

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
time_param (Time parameter for parametric sweep)	0 75	

5 Locate the **Output While Solving** section. From the **Probes** list, choose **None**.

Steb 1: Stationary

- I In the Model Builder window, click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 3 In the table, clear the Solve for check boxes for Lithium-Ion Battery (liion) and Transport of Diluted Species (tds).

- 4 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- **5** From the **Method** list, choose **Solution**.
- 6 From the Study list, choose Study I Discharge, Time Dependent.
- 7 From the Solution list, choose Solution I (soll).
- 8 From the Time (s) list, choose Interpolated.
- 9 In the **Time** text field, type time param.
- 10 In the Study toolbar, click **Compute**.

RESULTS

Stress (solid)

The Stress (solid) plot group shows the result for the von Mises stress on the particles experienced during the intercalation reaction at t = 75 s.

Appendix — Geometry Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click \ Clear Table.
- 4 Click Load from File.
- 5 Browse to the model's Application Libraries folder and double-click the file heterogeneous_li_battery_parameters.txt.
- **6** Click the **Transparency** button in the **Graphics** toolbar.

GEOMETRY I

Ellibsoid I (elb I)

- I In the Geometry toolbar, click \bigcirc More Primitives and choose Ellipsoid.
- 2 In the Settings window for Ellipsoid, locate the Size and Shape section.
- 3 In the a-semiaxis text field, type Rp*1.5/3*pr pos+Rp*(1-pr pos).
- 4 In the b-semiaxis text field, type Rp*1.5/3.
- 5 In the c-semiaxis text field, type Rp*pr_pos+Rp*1.5/3*(1-pr_pos).
- 6 Locate the Position section. In the y text field, type 6.5e-7*pr pos.
- 7 Locate the Axis section. From the Axis type list, choose y-axis.
- **8** Right-click **Ellipsoid I (elp I)** and choose **Copy**.

Coby I (coby I)

- I In the Geometry toolbar, click Transforms and choose Copy.
- **2** Select the object **elp1** only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type Rp*0.9.

Ellipsoid 2 (elp2)

- I In the Geometry toolbar, click \bigcirc More Primitives and choose Ellipsoid.
- 2 In the Settings window for Ellipsoid, locate the Size and Shape section.
- 3 In the a-semiaxis text field, type Rp*1.5/3.
- 4 In the b-semiaxis text field, type Rp*1.5/3*pr pos+Rp*(1-pr pos).
- 5 In the c-semiaxis text field, type Rp*pr pos+Rp*1.5/3*(1-pr pos).
- 6 Locate the Position section. In the y text field, type Rp*1.2+6.5e-7*pr pos.

Copy 2 (copy2)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the object elp2 only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type Rp*0.9.

Copy 3 (copy3)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 3 In the Settings window for Copy, locate the Displacement section.

- 4 In the z text field, type Rp*1.6.
- 5 Click **Build Selected**.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Coby 4 (coby4)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the y text field, type -Rp*1.23*2.

Сору 5 (сору5)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the objects copy1, copy2, copy3(1), copy3(2), copy3(3), copy3(4), copy4(2), copy4(5), copy4(6), copy4(7), copy4(8), elp1, and elp2 only.
- 3 Click the Loom to Selection button in the Graphics toolbar.
- 4 Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 5 In the Settings window for Copy, locate the Displacement section.
- 6 In the y text field, type -Rp*1.23*4.
- 7 Click | Build Selected.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Ellipsoid 3 (elp3)

- I In the Geometry toolbar, click \bigcirc More Primitives and choose Ellipsoid.
- 2 In the Settings window for Ellipsoid, locate the Size and Shape section.
- 3 In the a-semiaxis text field, type Rp*1.5/3*pr neg+Rp*(1-pr neg).
- 4 In the b-semiaxis text field, type Rp*1.5/3.
- 5 In the c-semiaxis text field, type Rp*pr neg+Rp*1.5/3*(1-pr neg).
- 6 Locate the Position section. In the y text field, type L sep-5e-7*(1-pr neg).
- 7 Locate the Axis section. From the Axis type list, choose y-axis.
- 8 Click | Build Selected.
- **9** Click the **Zoom Extents** button in the **Graphics** toolbar.

Copy 6 (copy6)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the object elp3 only.

- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type Rp*0.9.
- 5 Click **Build Selected**.

Ellipsoid 4 (elp4)

- I In the Geometry toolbar, click \bigoplus More Primitives and choose Ellipsoid.
- 2 In the Settings window for Ellipsoid, locate the Size and Shape section.
- 3 In the a-semiaxis text field, type Rp*1.5/3.
- 4 In the b-semiaxis text field, type Rp*1.5/3*pr neg+Rp*(1-pr neg).
- 5 In the c-semiaxis text field, type Rp*pr neg+Rp*1.5/3*(1-pr neg).
- 6 Locate the **Position** section. In the **y** text field, type Rp*1.2+L_sep-5e-7*(1-pr_neg).
- 7 Click | Build Selected.

Сору 7 (сору7)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the object **elp4** only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the x text field, type Rp*0.9.
- 5 Click | Build Selected.

Сору 8 (сору8)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the objects copy6, copy7, elp3, and elp4 only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the z text field, type Rp*1.6.

Copy 9 (copy9)

- I In the Geometry toolbar, click Transforms and choose Copy.
- 2 Select the objects copy6, copy7, copy8(1), copy8(2), copy8(3), copy8(4), elp3, and elp4 only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the y text field, type Rp*1.23*2.
- 5 Click | Build Selected.

Coby 10 (coby10)

I In the Geometry toolbar, click Transforms and choose Copy.

- 2 Select the objects copy6, copy7, copy8(1), copy8(2), copy8(3), copy8(4), copy9(1), copy9(2), copy9(3), copy9(4), copy9(5), copy9(6), copy9(7), copy9(8), elp3, and elp4 only.
- 3 In the Settings window for Copy, locate the Displacement section.
- 4 In the y text field, type Rp*1.23*4.
- 5 Click | Build Selected.

Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type Rp*1.8.
- 4 In the **Depth** text field, type Rp*2.0889+L sep+Rp*14.76.
- 5 In the **Height** text field, type Rp*3.2.
- 6 Locate the **Position** section. In the x text field, type -Rp*0.45.
- 7 In the y text field, type -Rp*4/9-Rp*7.38.
- 8 In the z text field, type -Rp*0.8.
- 9 Click Pauld Selected.

Union I (uni I)

- I In the Geometry toolbar, click | Booleans and Partitions and choose Union.
- 2 Select the object **blk1** only.
- 3 In the Settings window for Union, locate the Union section.
- 4 From the Repair tolerance list, choose Relative.
- 5 Click **Build Selected**.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- 2 Select the object unil only.
- 3 In the Settings window for Difference, locate the Difference section.
- 4 Click the Paste Selection button for Objects to subtract.
- 5 In the Paste Selection dialog box, type copy1 copy10(1) copy10(2) copy10(3) copy10(4) copy10(5) copy10(6) copy10(7) copy10(8) copy10(9) copy10(10)copy10(11) copy10(12) copy10(13) copy10(14) copy10(15) copy10(16) copy2 copy3(1) copy3(2) copy3(3) copy3(4) copy4(1) copy4(2) copy4(3) copy4(4) copy4(5) copy4(6) copy4(7) copy4(8) copy5(1) copy5(2)copy5(3) copy5(4) copy5(5) copy5(6) copy5(7) copy5(8) copy5(9)

- copy5(10) copy5(11) copy5(12) copy5(13) copy5(14) copy5(15) copy5(16) copy6 copy7 copy8(1) copy8(2) copy8(3) copy8(4) copy9(1) copy9(2)copy9(3) copy9(4) copy9(5) copy9(6) copy9(7) copy9(8) elp1 elp2 elp3 elp4 in the Selection text field.
- 6 Click OK.
- 7 Select the objects copy1, copy10(1), copy10(10), copy10(11), copy10(12), copy10(13), copy10(14), copy10(15), copy10(16), copy10(2), copy10(3), copy10(4), copy10(5), copy10(6), copy10(7), copy10(8), copy10(9), copy2, copy3(1), copy3(2), copy3(3), copy3(4), copy4(1), copy4(2), copy4(3), copy4(4), copy4(5), copy4(6), copy4(7), copy4(8), copy5(1), copy5(10), copy5(11), copy5(12), copy5(13), copy5(14), copy5(15), copy5(16), copy5(2), copy5(3), copy5(4), copy5(5), copy5(6), copy5(7), copy5(8), copy5(9), copy6, copy7, copy8(1), copy8(2), copy8(3), copy8(4), copy9(1), copy9(2), copy9(3), copy9(4), copy9(5), copy9(6), copy9(7), copy9(8), elp1, elp2, elp3, and elp4 only.
- 8 In the Settings window for Difference, locate the Difference section.
- **9** From the Repair tolerance list, choose Relative.
- 10 Click | Build Selected.
- II Click the **Zoom Extents** button in the **Graphics** toolbar.

Block 2 (blk2)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type Rp*1.8.
- 4 In the Depth text field, type Rp*2.0889+L sep+Rp*14.76.
- 5 In the **Height** text field, type Rp*3.2.
- 6 Locate the **Position** section. In the x text field, type -Rp*0.45.
- 7 In the y text field, type -Rp*4/9-Rp*7.38.
- 8 In the z text field, type -Rp*0.8.
- 9 Click | Build Selected.

Form Union (fin)

- I In the Model Builder window, click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Repair tolerance list, choose Relative.
- 4 Click | Build Selected.

Electrolyte

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Electrolyte in the Label text field.
- **3** On the object fin, select Domain 1 only.

Negative electrode

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Negative electrode in the Label text field.
- **3** On the object **fin**, select Domain 3 only.
- 4 Click | Build Selected.

Positive electrode

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Positive electrode in the Label text field.
- **3** On the object fin, select Domain 2 only.

Negative electrode surface

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Negative electrode surface in the **Label** text field.
- 3 Locate the Entities to Select section. From the Geometric entity level list, choose Boundary.
- 4 On the object fin, select Boundaries 86, 87, 89–94, 96, 97, 99–104, 106, 107, 109– 114, 116, 117, 119–124, 126, 127, 129–134, 136, 137, 139–144, 146, 147, 149–154, 156, 157, 159–164, 250–313, 378–441, and 526–589 only.
- 5 Click | Build Selected.

Positive electrode surface

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Positive electrode surface in the Label text field.
- 3 Locate the Entities to Select section. From the Geometric entity level list, choose Boundary.

- 4 On the object fin, select Boundaries 6, 7, 9–14, 16, 17, 19–24, 26, 27, 29–34, 36, 37, 39-44, 46, 47, 49-54, 56, 57, 59-64, 66, 67, 69-74, 76, 77, 79-84, 186-249, 314-377, and 462-525 only.
- 5 Click | Build Selected.

Negative current collector

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Negative current collector in the Label text field.
- 3 Locate the Entities to Select section. From the Geometric entity level list, choose
- 4 On the object fin, select Boundaries 184, 185, 460, and 461 only.
- 5 Click | Build Selected.

Positive current collector

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Positive current collector in the Label text field.
- 3 Locate the Entities to Select section. From the Geometric entity level list, choose Boundary.
- 4 On the object fin, select Boundaries 182, 183, 458, and 459 only.
- 5 Click | Build Selected.
- 6 In the Geometry toolbar, click **Build All**.
- 7 Click the **Zoom Extents** button in the **Graphics** toolbar.

Roller condition boundaries

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Explicit Selection.
- 2 In the Settings window for Explicit Selection, type Roller condition boundaries in the Label text field.
- 3 Locate the Entities to Select section. From the Geometric entity level list, choose Boundary.
- 4 On the object fin, select Boundaries 85, 88, 95, 98, 105, 108, 115, 118, 125, 128, 135, 138, 145, 148, 155, 158, 174–181, 450–457, and 607–622 only.