



# Startup of a Continuous Stirred Tank Reactor

## Introduction

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The hydrolysis of propylene oxide into propylene glycol is an important chemical process with 400,000 metric tons produced worldwide each year. Propylene glycol finds wide application as a moisturizer in foods, pharmaceuticals, and cosmetics.

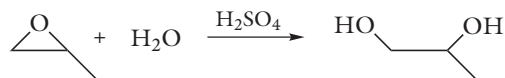
In this example, the startup phase of a continuous stirred tank reactor (CSTR), used to produce propylene glycol, is modeled. The nonisothermal process is described by a set of coupled mass and energy balances that are easily set up and solved in the Chemical Reaction Engineering Module. The model highlights the use of the predefined CSTR reactor type in the Reaction Engineering interface, and also shows how to enter the thermodynamic data needed for the energy balances.

This example reproduces results found in [Ref. 1](#).

## Model Description

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Propylene glycol ( $\text{C}_3\text{H}_8\text{O}_2$ ) is produced from the reaction of propylene oxide ( $\text{C}_3\text{H}_6\text{O}$ ) with water ( $\text{H}_2\text{O}$ ) in the presence of an acid catalyst:



The reaction rate (SI unit:  $\text{mol}/(\text{m}^3 \cdot \text{s})$ ) is first order with respect to the activity of propylene oxide:

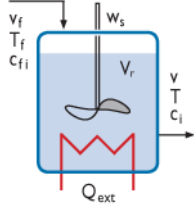
$$r_1 = -k_1 c_{\text{C}_3\text{H}_6\text{O}}$$

where the rate constant is temperature dependent according to the Arrhenius expression:

$$k_1 = A_1 \exp\left(-\frac{E_1}{R_g T}\right) \quad (1)$$

The Arrhenius parameters in [Equation 1](#) are  $A_1 = 4.71 \cdot 10^9 \text{ s}^{-1}$  and  $E_1 = 75.358 \text{ kJ/mol}$ .

The liquid phase reaction takes place in a continuous stirred tank reactor (CSTR) equipped with a heat-exchanger. Methanol ( $\text{CH}_3\text{OH}$ ) is also added to the mixture but does not react. It is further assumed that the reactor volume is constant over time.



*Figure 1: A perfectly mixed CSTR for the production of propylene glycol. The CSTR is a predefined reactor type in the Chemical Reaction Engineering Module.*

The time evolution of the nonisothermal reacting system is given by several coupled balance equations. The species mass balances are:

$$V_r \frac{dc_i}{dt} = v_f c_{f,i} - v c_i + R_i V_r \quad (2)$$

In Equation 2,  $c_i$  is the species molar concentration (SI unit:  $\text{mol}/\text{m}^3$ ),  $V_r$  denotes the reactor volume (SI unit:  $\text{m}^3$ ),  $R_i$  is the species rate expression (SI unit:  $\text{mol}/(\text{m}^3 \cdot \text{s})$ ), and  $v_f$  is the volumetric flow rate of the feed inlet (SI unit:  $\text{m}^3/\text{s}$ ).  $v$  is the volumetric flow of the species exiting the reactor and is defined as:

$$v = v_{f,i} + v_p = v_{f,i} + V_r \sum_i \frac{R_i M_i}{\rho_i}$$

$v_p$  is the volumetric production rate, arising due to differences in molar mass,  $M_i$ , and densities,  $\rho_i$ , of the species.

For an incompressible and ideally mixed reacting liquid, the energy balance is:

$$V_r \sum_i c_i C_{p,i} \frac{dT}{dt} = Q + Q_{\text{ext}} + \sum_i v_{f,i} c_{f,i} (h_{f,i} - h_i)$$

where  $C_{p,i}$  is the species molar heat capacity (SI unit:  $\text{J}/(\text{mol} \cdot \text{K})$ ), and  $T$  is the temperature (SI unit: K). On the right-hand side,  $Q$  represents the heat due to chemical reaction (SI unit: J/s), and  $Q_{\text{ext}}$  denotes heat added to the system (SI unit: J/s), for instance by a heat exchanger. The last term signifies heat added as species flow through the reactor. In this term,  $h_i$  is the species molar enthalpy (SI unit: J/mol).

This example assumes that the species heat capacities,  $C_{p,i}$ , represent an average over the temperature interval. The associated species' enthalpies are then given by:

$$h_i = C_{p,i}(T - T_{\text{ref}}) + h_i(T_{\text{ref}})$$

where  $h_i(T_{\text{ref}})$  is the standard heat of formation at the reference temperature  $T_{\text{ref}}$ .

The heat of reaction is given by:

$$Q = -V_r \sum_j H_j r_j$$

where  $H_j$  is the enthalpy of reaction (SI unit: J/mol), and  $r_j$  denotes the reaction rate (SI unit: mol/(m<sup>3</sup>·s)).

The heat added by the heat exchanger is given by:

$$Q_{\text{ext}} = F_x C_{p,x}(T_x - T) \cdot \left[ 1 - \exp\left(\frac{-UA}{F_x C_{p,x}}\right) \right]$$

where  $F$  is the molar flow rate (SI unit: mol/s),  $U$  is the overall heat transfer coefficient (SI unit: J/(K·m<sup>2</sup>·s)), and  $A$  represents the heat exchange area (SI unit: m<sup>2</sup>). The subscript  $x$  refers to the heat exchanger medium, which in this case is water.  $T_x$  is the inlet temperature of the heat exchanger medium.

The following table summarizes additional parameters describing the reactor setup and process conditions:

PARAMETER	VALUE	DESCRIPTION
$V_r$	1.89 m <sup>3</sup>	Reactor volume
$v_f$	3.47·10 <sup>-3</sup> m <sup>3</sup> /s	Volumetric flow rate
$c_{f,\text{C}_3\text{H}_6\text{O}}$	2903 mol/m <sup>3</sup>	Concentration of propylene oxide in feed stream
$c_{f,\text{H}_2\text{O}}$	36291 mol/m <sup>3</sup>	Concentration of water in feed stream
$c_{f,\text{CH}_3\text{OH}}$	3629 mol/m <sup>3</sup>	Concentration of methanol in feed stream
$c_{0,\text{H}_2\text{O}}$	55273 mol/m <sup>3</sup>	Initial concentration of water in the reactor
$\rho_{\text{C}_3\text{H}_6\text{O}}$	830 kg/m <sup>3</sup>	Density of propylene oxide
$\rho_{\text{H}_2\text{O}}$	1000 kg/m <sup>3</sup>	Density of water
$\rho_{\text{C}_3\text{H}_8\text{O}_2}$	1036 kg/m <sup>3</sup>	Density of propylene glycol
$\rho_{\text{CH}_3\text{OH}}$	792 kg/m <sup>3</sup>	Density of methanol

PARAMETER	VALUE	DESCRIPTION
$C_{p,C_3H_6O}$	146.5 J/(mol·K)	Heat capacity of propylene oxide
$C_{p,H_2O}$	75.4 J/(mol·K)	Heat capacity of water
$C_{p,C_3H_8O_2}$	192.6 J/(mol·K)	Heat capacity of propylene glycol
$C_{p,CH_3OH}$	81.6 J/(mol·K)	Heat capacity of methanol
$C_{px}$	75.4 J/(mol·K)	Heat capacity of heat exchanger medium
$h_{ref,C_3H_6O}$	$-153.5 \cdot 10^3$ J/mol	Enthalpy of formation of propylene oxide at $T_{ref}$
$h_{ref,H_2O}$	$-286.1 \cdot 10^3$ J/mol	Enthalpy of formation of water at $T_{ref}$
$h_{ref,C_3H_8O_2}$	$-525.6 \cdot 10^3$ J/mol	Enthalpy of formation of propylene glycol at $T_{ref}$
$h_{ref,CH_3OH}$	-238.6 J/mol	Enthalpy of formation of methanol at $T_{ref}$
$T_f$	297 K	Feed stream temperature
$T_0$	340 K	Initial reactor temperature
$T_{ref}$	293 K	Reference temperature
$T_x$	289 K	Temperature of heat exchanger medium at inlet
$F_x$	126 mol/s	Heat exchanger medium molar flow
$U_A$	8441 J/(s·K)	Heat exchange parameter

The model described here is readily set up and solved using the predefined CSTR reactor with constant volume in the Reaction Engineering interface available in the Chemical Reaction Engineering Module.

## Results and Discussion

Figure 2 shows the concentration of propylene oxide (SI unit:  $\text{mol/m}^3$ ) as a function of reaction time.

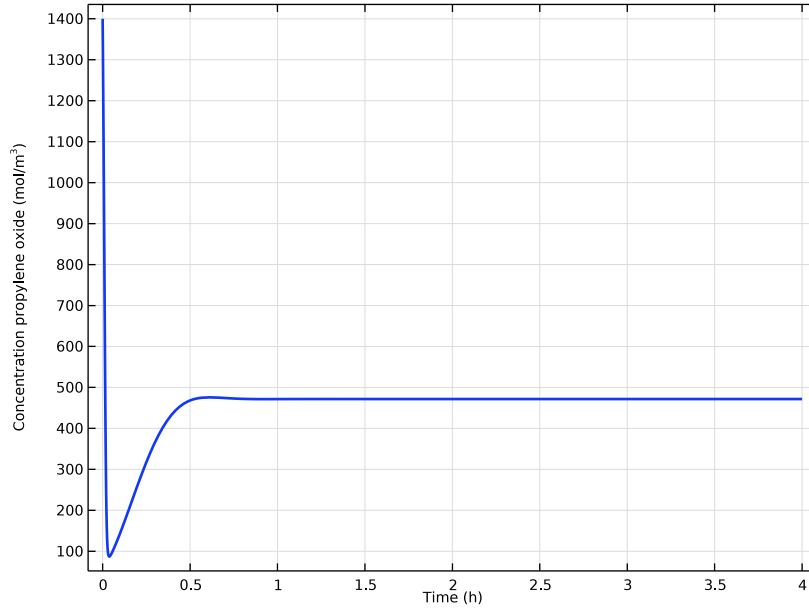
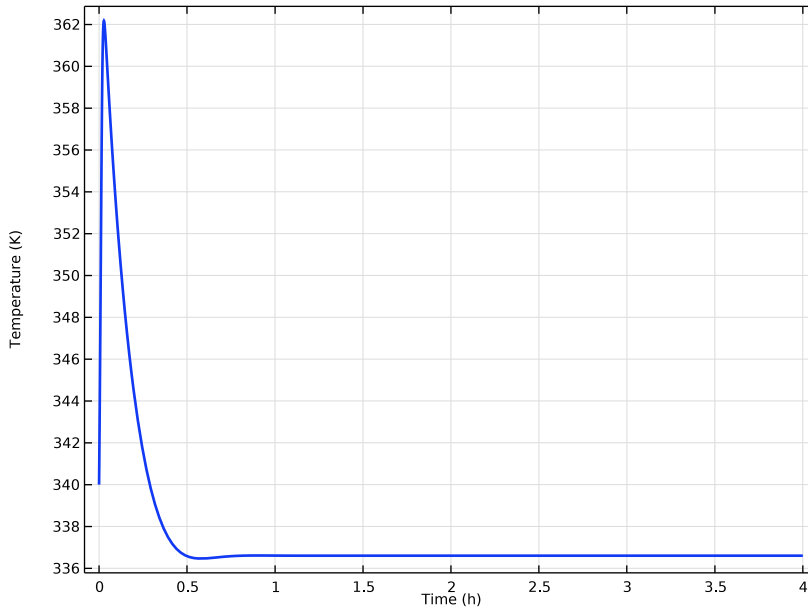


Figure 2: Concentrations of reactant propylene oxide ( $\text{mol/m}^3$ ) during the first 4 hours of operation.

The corresponding development of the reactor temperature is shown in Figure 3.



*Figure 3: Reactor temperature (K) during the first 4 hours of operation.*

Initially both the reactant concentration and the temperature oscillate around their respective steady-state values ( $472 \text{ mol/m}^3$  and  $337 \text{ K}$ , respectively). The model predicts that the reactor temperature passes a maximum value higher than the steady-state temperature. From a safety perspective it is therefore relevant to look closer at possible sets of initial conditions to see if process operation limits are violated. In the process modeled here, it is undesirable to exceed a reactor temperature of  $355 \text{ K}$  to avoid undesirable side reactions and not damage reactor equipment. [Figure 4](#) shows the concentration-

temperature phase plane for three initial condition scenarios: ( $c_{\text{C}_3\text{H}_6\text{O}} = 0$ ,  $T_0 = 297$  K), ( $c_{\text{C}_3\text{H}_6\text{O}} = 0$ ,  $T_0 = 340$  K), and ( $c_{\text{C}_3\text{H}_6\text{O}} = 1400$ ,  $T_0 = 340$  K).

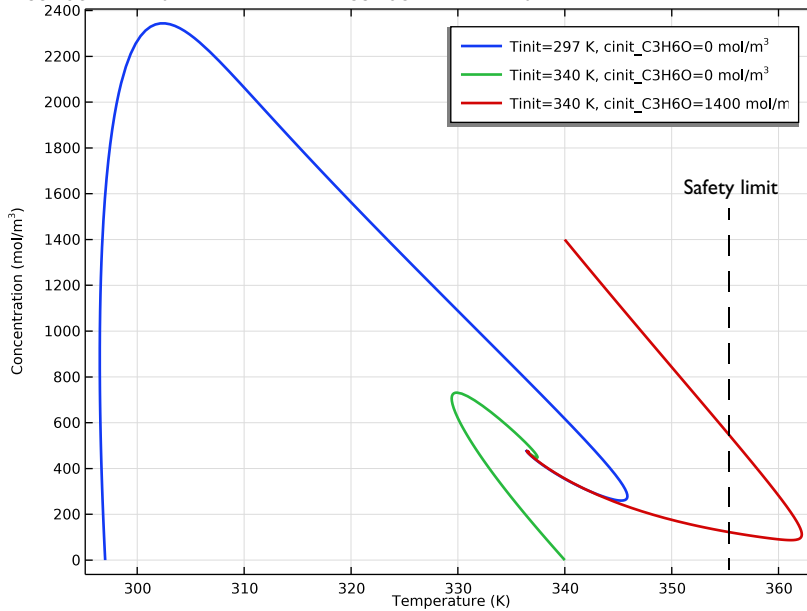


Figure 4: Trajectories in the concentration-temperature phase plane for three sets of initial conditions.

The plot shows that all investigated initial conditions converge to the same steady state. However, starting with  $c_{\text{C}_3\text{H}_6\text{O}} = 1400$  mol/m<sup>3</sup> and  $T_0 = 340$  K leads to violation of the temperature safety limits.

## Reference


1. H.S. Fogler, *Elements of Chemical Reaction Engineering*, 3rd ed., Prentice Hall PTR, Example 9-4, pp. 553–559, 1999.

**Application Library path:** Chemical\_Reaction\_Engineering\_Module/Tutorials/cstr\_startup




From the **File** menu, choose **New**.



## NEW

In the **New** window, click  **Model Wizard**.


## MODEL WIZARD

- 1 In the **Model Wizard** window, click  **OD**.
- 2 In the **Select Physics** tree, select **Chemical Species Transport>Reaction Engineering (re)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Time Dependent**.
- 6 Click  **Done**.

## GLOBAL DEFINITIONS

Add a set of model parameters by importing their definitions from a data text file provided with the **Application Library**.


### *Parameters*

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters** **1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `cstr_startup_parameters.txt`.

## DEFINITIONS

Similarly, variables for the concentration-dependent and temperature-dependent enthalpies are available in a text file.

### *Variables*


- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Definitions** and choose **Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `cstr_startup_variables.txt`.

Select the **Reactor Type**-CSTR, constant volume for a liquid mixture and include the **Energy Balance**. That is, nonisothermal conditions apply.


## REACTION ENGINEERING (RE)

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Reaction Engineering (re)**.
- 2 In the **Settings** window for **Reaction Engineering**, locate the **Reactor** section.
- 3 From the **Reactor type** list, choose **CSTR, constant volume**.
- 4 Locate the **Energy Balance** section. From the **Energy balance** list, choose **Include**.
- 5 In the  $Q_{\text{ext}}$  text field, type  $Q_{\text{xch}}$ .
- 6 Click to expand the **Mixture Properties** section. From the **Phase** list, choose **Liquid**.
- 7 Locate the **Reactor** section. Find the **Mass balance** subsection. In the  $V_r$  text field, type  $V_{r\_tank}$ .

### Reaction 1

- 1 In the **Reaction Engineering** toolbar, click  **Reaction**.  
Add the reaction. Note that the reaction in this example is of first order in regard to propylene oxide, not the default stoichiometric reaction order.
- 2 In the **Settings** window for **Reaction**, locate the **Reaction Formula** section.
- 3 In the **Formula** text field, type  $\text{C3H6O} + \text{H2O} \Rightarrow \text{C3H8O2}$ .
- 4 Locate the **Reaction Rate** section. From the list, choose **User defined**.
- 5 In the  $r_j$  text field, type  $\text{re.kf}_1 * \text{re.c}_{\text{C3H6O}}$ .
- 6 Locate the **Reaction Orders** section. Find the **Volumetric overall reaction order** subsection. In the **Forward** text field, type 1.
- 7 Locate the **Rate Constants** section. Select the **Use Arrhenius expressions** check box.
- 8 In the  $A^f$  text field, type  $Af_{\text{reaction}}$ .
- 9 In the  $E^f$  text field, type  $Ea_{\text{reaction}}$ .

### Species 1

- 1 In the **Reaction Engineering** toolbar, click  **Species**.
- 2 In the **Settings** window for **Species**, locate the **Name** section.
- 3 In the text field, type  $\text{CH3OH}$ .

### Species: C3H6O

- 1 In the **Model Builder** window, click **Species: C3H6O**.
- 2 In the **Settings** window for **Species**, locate the **Chemical Formula** section.
- 3 In the  $\rho$  text field, type  $\rho_{\text{C3H6O}}$ .

### Species: H2O

- 1 In the **Model Builder** window, click **Species: H2O**.

- 2 In the **Settings** window for **Species**, locate the **Chemical Formula** section.
- 3 In the  $\rho$  text field, type rho\_H2O.


*Species: C3H8O2*

- 1 In the **Model Builder** window, click **Species: C3H8O2**.
- 2 In the **Settings** window for **Species**, locate the **Chemical Formula** section.
- 3 In the  $\rho$  text field, type rho\_C3H8O2.

*Species: CH3OH*

- 1 In the **Model Builder** window, click **Species: CH3OH**.
- 2 In the **Settings** window for **Species**, locate the **Chemical Formula** section.
- 3 In the  $\rho$  text field, type rho\_CH3OH.

*Feed Inlet 1*

- 1 In the **Reaction Engineering** toolbar, click  **Feed Inlet**.  
Define the inlet feed stream of the CSTR.
- 2 In the **Settings** window for **Feed Inlet**, locate the **Feed Inlet Properties** section.
- 3 In the  $v_f$  text field, type v\_feed.
- 4 In the  $T_f$  text field, type Tfeed.
- 5 Locate the **Feed Inlet Concentration and Enthalpy** section. In the table, enter the following settings (clear all the check boxes in the rightmost column):

Species	Concentration (mol/m <sup>3</sup> )	Enthalpy (J/mol)	Enthalpy (true--species feature, false--User defined )
C3H6O	cfeed_C3H6O	hf_C3H6O	
C3H8O2	0	0	
CH3OH	cfeed_CH3OH	hf_CH3OH	
H2O	cfeed_H2O	hf_H2O	

*Initial Values 1*

- 1 In the **Model Builder** window, click **Initial Values 1**.
- 2 In the **Settings** window for **Initial Values**, locate the **General Parameters** section.
- 3 In the  $T_0$  text field, type Tinit.

- 4 Locate the **Volumetric Species Initial Values** section. In the table, enter the following settings:

Species	Concentration (mol/m <sup>3</sup> )
C3H6O	cinit_C3H6O
H2O	cinit_H2O

*Species: C3H6O*

- 1 In the **Model Builder** window, click **Species: C3H6O**.
- 2 In the **Settings** window for **Species**, click to expand the **Thermodynamic Expressions** section.
- 3 From the list, choose **User defined**.
- 4 In the  $C_p$  text field, type cp\_C3H6O.
- 5 In the  $h$  text field, type h\_C3H6O.

*Species: H2O*

- 1 In the **Model Builder** window, click **Species: H2O**.
- 2 In the **Settings** window for **Species**, locate the **Thermodynamic Expressions** section.
- 3 From the list, choose **User defined**.
- 4 In the  $C_p$  text field, type cp\_H2O.
- 5 In the  $h$  text field, type h\_H2O.

*Species: C3H8O2*


- 1 In the **Model Builder** window, click **Species: C3H8O2**.
- 2 In the **Settings** window for **Species**, locate the **Thermodynamic Expressions** section.
- 3 From the list, choose **User defined**.
- 4 In the  $C_p$  text field, type cp\_C3H8O2.
- 5 In the  $h$  text field, type h\_C3H8O2.

*Species: CH3OH*

- 1 In the **Model Builder** window, click **Species: CH3OH**.
- 2 In the **Settings** window for **Species**, locate the **Thermodynamic Expressions** section.
- 3 From the list, choose **User defined**.
- 4 In the  $C_p$  text field, type cp\_CH3OH.
- 5 In the  $h$  text field, type h\_CH3OH.

## STUDY I

### Step 1: Time Dependent

- 1 In the **Model Builder** window, under **Study I** click **Step 1: Time Dependent**.
- 2 In the **Settings** window for **Time Dependent**, locate the **Study Settings** section.
- 3 From the **Time unit** list, choose **h**.
- 4 In the **Output times** text field, type 4.  
First, compute the temperature and concentrations.
- 5 In the **Home** toolbar, click  **Compute**.


The following instructions generate [Figure 2](#) and [Figure 3](#).

## RESULTS

### Concentration (re)

- 1 In the **Settings** window for **ID Plot Group**, click to expand the **Title** section.
- 2 From the **Title type** list, choose **None**.
- 3 Locate the **Plot Settings** section.
- 4 Select the **y-axis label** check box. In the associated text field, type Concentration propylene oxide ( $\text{mol/m}^3$ ).

### Global I

- 1 In the **Model Builder** window, expand the **Concentration (re)** node, then click **Global I**.
- 2 In the **Settings** window for **Global**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1)>Reaction Engineering>re.c\_C3H6O - Concentration - mol/m<sup>3</sup>**.
- 3 Click to expand the **Coloring and Style** section. From the **Width** list, choose **2**.
- 4 Click to expand the **Legends** section. Clear the **Show legends** check box.
- 5 In the **Concentration (re)** toolbar, click  **Plot**.

### Temperature (re)

- 1 In the **Model Builder** window, under **Results** click **Temperature (re)**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Title** section.
- 3 From the **Title type** list, choose **None**.

### Global I



- 1 In the **Model Builder** window, expand the **Temperature (re)** node, then click **Global I**.
- 2 In the **Settings** window for **Global**, locate the **Coloring and Style** section.

- 3 From the **Width** list, choose **2**.
- 4 Locate the **Legends** section. Clear the **Show legends** check box.


## STUDY I

Next, compute the corresponding solutions for a set of initial temperatures and propylene-oxide concentrations.

### Parametric Sweep

- 1 In the **Study** toolbar, click  **Parametric Sweep**.
- 2 In the **Settings** window for **Parametric Sweep**, locate the **Study Settings** section.
- 3 Click  **Add**.
- 4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
Tinit (Initial reactor temperature)	297[K] 340[K] 340[K]	K

- 5 Click  **Add**.
- 6 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
cinit_C3H6O (Initial concentration, propylene oxide)	0 0 1400[mol/m^3]	mol/m^3

- 7 In the **Study** toolbar, click  **Compute**.

The following instructions generate [Figure 4](#).



## RESULTS

### Concentration vs. Temperature (re)

- 1 In the **Settings** window for **ID Plot Group**, type Concentration vs. Temperature (re) in the **Label** text field.
- 2 Locate the **Title** section. From the **Title type** list, choose **None**.

### Global I


- 1 In the **Model Builder** window, expand the **Concentration vs. Temperature (re)** node, then click **Global I**.
- 2 In the **Settings** window for **Global**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component I (comp I)> Reaction Engineering>re.c\_C3H6O - Concentration - mol/m^3**.

- 3 Click **Replace Expression** in the upper-right corner of the **x-Axis Data** section. From the menu, choose **Component 1 (comp1)>Reaction Engineering>re.T - Temperature - K**.
- 4 Locate the **Coloring and Style** section. From the **Width** list, choose **2**.
- 5 Locate the **Legends** section. Find the **Include** subsection. Clear the **Expression** check box.
- 6 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 7 In the **Concentration vs. Temperature (re)** toolbar, click  **Plot**.

#### *Temperature vs. Time (re)*

- 1 In the **Settings** window for **ID Plot Group**, type **Temperature vs. Time (re)** in the **Label** text field.
- 2 Click to expand the **Title** section. From the **Title type** list, choose **None**.

#### *Global 1*

- 1 In the **Model Builder** window, expand the **Temperature (re) 1** node, then click **Results>Temperature vs. Time (re)>Global 1**.
- 2 In the **Settings** window for **Global**, locate the **Coloring and Style** section.
- 3 From the **Width** list, choose **2**.
- 4 Locate the **Legends** section. Find the **Include** subsection. Clear the **Expression** check box.
- 5 In the **Temperature vs. Time (re)** toolbar, click  **Plot**.

