

Scattered-Field Formulation for Elastic Waves

This model showcases how to solve for the scattered field when knowing the incident field for three different types of scatterer, that is, an infinitely rigid one, a cavity, and an elastic inclusion.

This formulation can be useful when the scatterer is in the far field of the source, such that the probing wave resembles a plane wave. In such case, including the source would require an unnecessarily huge computational domain to be meshed. Both P and S plane waves are thus used as incident fields in the model.

Moreover, the model shows how to numerically compute the field emitted by a point source, and to use then the obtained solution as the known incident field for a subsequent study, where the scattering problem is solved.

Model Definition

The model geometry consists of an obstacle shaped as an infinite cylinder embedded in a background infinite elastic material. Focusing the attention on P and S waves, the plane strain assumption holds, and you can simply model a plane perpendicular to the axis of the cylindrical object. The infinite extension of the background elastic material can be simulated by adopting a finite computational domain truncated with perfectly matched layers. The radius of the obstacle is arbitrarily selected to be unitary, and the frequency is selected such that the wavelength of the P waves is unitary too.

DOMAIN EQUATIONS

The field equation for the background field reads

$$\rho_b \frac{\partial^2 \mathbf{u}_b}{\partial t^2} = \nabla \cdot (C_b \nabla \mathbf{u}_b)$$

The field equation for the total field reads

$$\rho \frac{\partial^2 \mathbf{u}_t}{\partial t^2} = \nabla \cdot (C \nabla \mathbf{u}_t)$$

where the elasticity tensor and the density are equal to the those of the background outside the scatterer and equal to those of the obstacle inside it. Defining the scattered field as

$$\mathbf{u}_t = \mathbf{u}_b + \mathbf{u}_s$$

and subtracting the field equation for the background to that of the total gives

$$\rho_b \frac{\partial^2 \mathbf{u}_s}{\partial t^2} = \nabla \cdot (C_b \nabla \mathbf{u}_s)$$

outside the scatterer, while

$$\rho_b \frac{\partial^2 \mathbf{u}_s}{\partial t^2} = (\rho_b - \rho_o) \frac{\partial^2 \mathbf{u}_b}{\partial t^2} + \nabla \cdot (C_o \nabla (\mathbf{u}_s + \mathbf{u}_b)) - (\nabla \cdot (C_b \nabla \mathbf{u}_b))$$

inside it. This equation can be rewritten as

$$\rho_b \frac{\partial^2 \mathbf{u}_s}{\partial t^2} = \mathbf{f} + \nabla \cdot (C_o(\nabla \mathbf{u}_s - \varepsilon) + \sigma)$$

Thus, one can solve for the scattered field by including in the standard elastodynamic problem a body force, an initial strain, and an initial stress according to

$$\mathbf{f} = (\rho_b - \rho_o) \frac{\partial^2 \mathbf{u}_b}{\partial t^2}$$

$$\sigma = -C_b \nabla \mathbf{u}_b$$

$$\varepsilon = -\frac{1}{2}(\nabla \mathbf{u}_b + \nabla \mathbf{u}_b^{\mathrm{T}})$$

BOUNDARY CONDITIONS

An infinitely rigid obstacle is one for which no displacements can occur and it can therefore be simulated using a homogeneous Dirichlet (fixed) boundary condition:

$$\mathbf{u}_t = \mathbf{u}_b + \mathbf{u}_s = 0$$

Rewriting this equation in terms of the scattered field, one obtains

$$\mathbf{u}_s = -\mathbf{u}_b$$

A cavity is such that its boundaries are stress free, which corresponds to a homogeneous Neumann condition:

$$\sigma_t \cdot \mathbf{n} = (\sigma_b + \sigma_s) \cdot \mathbf{n} = 0$$

$$\sigma_s \cdot \mathbf{n} = -(\sigma_b \cdot \mathbf{n})$$

Results

Figure 1 shows the displacement magnitude of the scattered field as obtained when a unitary amplitude plane wave impinges on the three different types of obstacles.

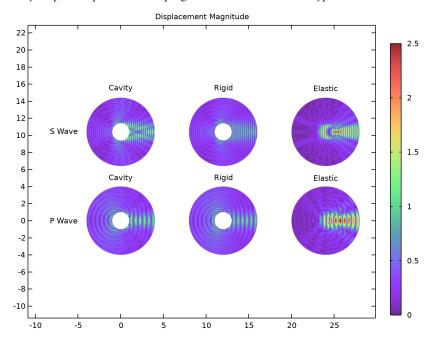


Figure 1: Displacement magnitude of scattered field for a unitary amplitude incident S (top row) and P (bottom row) plane wave for different types of obstacles.

The top row is the field obtained for an incident S wave, while the bottom row shows the scattered field for a P wave. Exploiting the fact that S waves are divergence free and P waves are curl free, the scattered field can be separated into a P and an S contribution for each analyzed case.

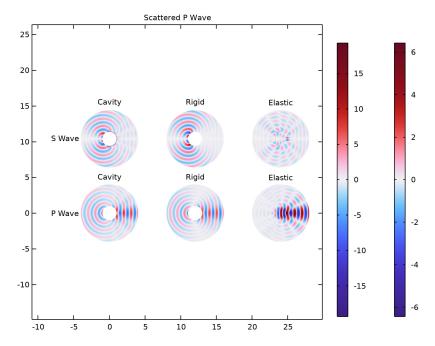


Figure 2: P wave scattered for an incident S (top row) and P (bottom row) plane wave for different types of obstacles.

Figure 2 shows the scattered P wave, while Figure 3 shows the scattered S wave.

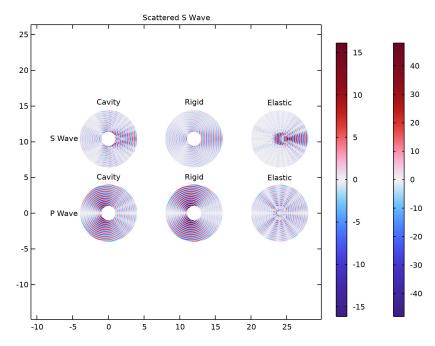


Figure 3: S wave scattered for an incident S (top row) and P (bottom row) plane wave for different types of obstacles.

Adding the known incident field to the solved scattered field gives the total field shown in Figure 4, Figure 5, and Figure 6 in terms of displacement magnitude, P wave, and S wave, respectively.

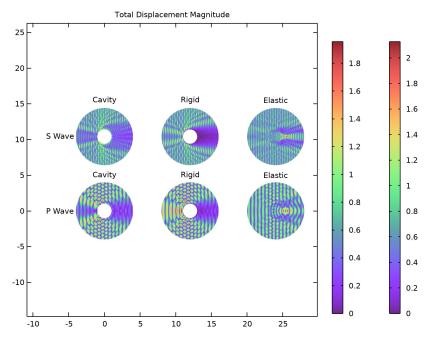


Figure 4: Total displacement magnitude for a unitary amplitude incident S (top row) and P (bottom row) plane wave for different types of obstacles.

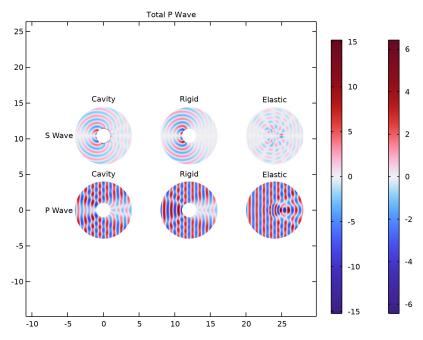


Figure 5: Total P wave field obtained for a unitary amplitude incident S (top row) and P (bottom row) plane wave for different types of obstacles.

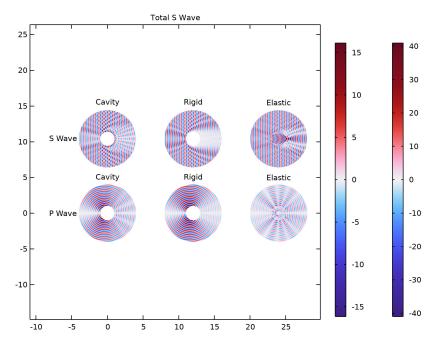


Figure 6: Total S wave field obtained for a unitary amplitude incident S (top row) and P (bottom row) plane wave for different types of obstacles.

Figure 7 shows instead the field produced by a point source in a homogeneous infinitely extended medium. This is used as an incident field to find the fields shown in Figure 8. In Figure 9, the total field obtained summing the scattered field and the incident field shown in Figure 7 is compared to the solution of the same problem solved without the scattered field formulation (SFF) using the point source along with the field equation and boundary conditions for the total field directly.

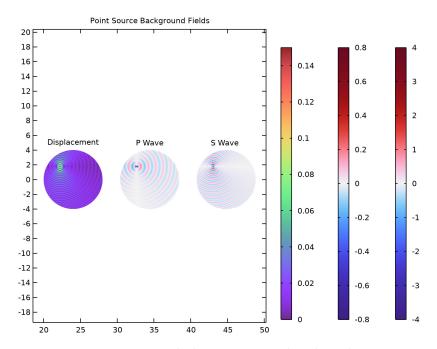


Figure 7: Point source in terms of displacement magnitude and P and S waves.

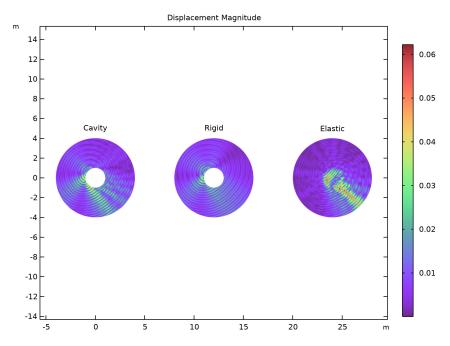


Figure 8: Scattered field produced by a point source for different types of obstacles.

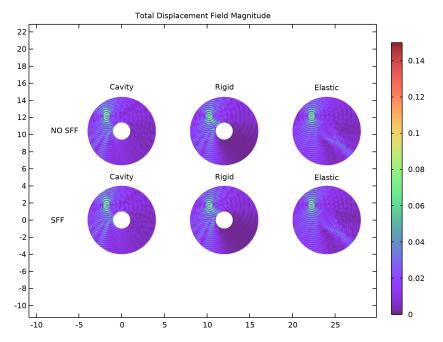


Figure 9: Total field obtained with a point source and different types of obstacles. The top row shows the results obtained without the scattered field formulation (SFF), while the bottom row shows the results obtained summing the incident field to the scattered solved with the SFF.

Application Library path: Structural_Mechanics_Module/Elastic_Waves/ scattered_field_elastic_waves

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

I In the Model Wizard window, click **2** 2D.

- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Frequency Domain.
- 6 Click M Done.

GLOBAL DEFINITIONS

Material Parameters

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the **Settings** window for **Parameters**, type Material Parameters in the **Label** text field.
- 3 Locate the Parameters section. In the table, enter the following settings:

Name	Expression	Value	Description
rho	1[kg/m^3]	I kg/m³	Density of background material
muLame	1[Pa]	l Pa	Shear modulus of background material
lambLame	2.3[Pa]	2.3 Pa	First Lamé parameter of background material
rho_o	2[kg/m^3]	2 kg/m³	Density of elastic obstacle
muLame_o	1.1[Pa]	I.I Pa	Shear modulus of elastic obstacle
lambLame_o	2.5[Pa]	2.5 Pa	First Lamé parameter elastic obstacle

P Wave Parameters

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, type P Wave Parameters in the Label text field.
- **3** Locate the **Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
сР	<pre>sqrt((lambLame+2* muLame)/rho)</pre>	2.0736 m/s	Speed of P waves
wlengthP	1 [m]	l m	Wavelength
kP	2*pi[rad]/wlengthP	6.2832 rad/m	Wave number
omega	kP*cP	13.029 rad/s	Angular frequency

- S Wave Parameters
- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, type S Wave Parameters in the Label text field.
- 3 Locate the Parameters section. In the table, enter the following settings:

Name	Expression	Value	Description
cS	sqrt(muLame/rho)	I m/s	Speed of S waves
kS	omega/cS	13.029 rad/m	Wave number
wlengthS	2*pi/kS	0.48224 m	Wavelength

Geometrical Parameters

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, type Geometrical Parameters in the Label text field.
- **3** Locate the **Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
R	5[m]	5 m	Radius of computational domain
r_o	1[m]	l m	Radius of inclusion
r_layer	1[m]	l m	Thickness of PML

GEOMETRY I

Circle I (c1)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type R.
- 4 Click to expand the Layers section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	r_layer
Layer 2	R-r_layer-r_o

5 Click | Build Selected.

Add more copies of the computational domain in order to solve for cavity inclusion, infinitely rigid obstacle, and elastic inclusion at the same time.

Array I (arr I)

- I In the Geometry toolbar, click \(\sum_{\text{in}} \) Transforms and choose Array.
- 2 Select the object cl only.
- 3 In the Settings window for Array, locate the Size section.
- 4 From the Array type list, choose Linear.
- 5 In the Size text field, type 3.
- **6** Locate the **Displacement** section. In the x text field, type $2*(R+r_0)$.
- 7 Click | Build Selected.
- 8 Click the Zoom Extents button in the Graphics toolbar.

Delete Entities I (del I)

- I In the Model Builder window, right-click Geometry I and choose Delete Entities.
- 2 In the Settings window for Delete Entities, locate the Entities or Objects to Delete section.
- 3 From the Geometric entity level list, choose Domain.
- 4 On the object arrI(I), select Domain 9 only.
- 5 On the object arr1(2), select Domain 9 only.
- 6 Click **Build All Objects**.

DEFINITIONS

Perfectly Matched Layer I (pml1)

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click Definitions and choose Perfectly Matched Layer.
- **3** Select Domains 1, 2, 5, and 8 only.
- 4 In the Settings window for Perfectly Matched Layer, locate the Geometry section.
- 5 From the Type list, choose Cylindrical.

ARTIFICIAL DOMAINS

Perfectly Matched Layer 2 (pml2)

- I In the Definitions toolbar, click M Perfectly Matched Layer.
- **2** Select Domains 9, 10, 13, and 16 only.
- 3 In the Settings window for Perfectly Matched Layer, locate the Geometry section.
- 4 From the Type list, choose Cylindrical.

Perfectly Matched Layer 3 (pml3)

- I In the Definitions toolbar, click M Perfectly Matched Layer.
- **2** Select Domains 17, 18, 21, and 24 only.
- 3 In the Settings window for Perfectly Matched Layer, locate the Geometry section.
- 4 From the Type list, choose Cylindrical.

First, set up the simulation for an incident P wave.

DEFINITIONS

Incident P Wave

- I In the Model Builder window, under Component I (compl) right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, type Incident P Wave in the Label text field.
- **3** Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
uP	exp(-1i*kP*x-1i*pi/2+ 1i*phase)[m]	m	Incident wave: u field
VΡ	O[m]	m	Incident wave: v field
eps11P	d(uP,x)		Incident wave: strain tensor, 11 component
eps22P	d(vP,y)		Incident wave: strain tensor, 22 component
eps12P	0.5*(d(uP,y)+d(vP,x))		Incident wave: strain tensor, 12 component
s11P	<pre>(lambLame+2*muLame)* eps11P+lambLame*eps22P</pre>	Pa	Incident wave: stress tensor, 11 component
s22P	lambLame*eps11P+ (lambLame+2*muLame)* eps22P	Pa	Incident wave: stress tensor, 22 component
s12P	2*muLame*eps12P	Pa	Incident wave: stress tensor, 12 component

The internal variable **phase** is used to synchronize the incident field with the solved scattered field in plots and animations over the dynamic data extension.

SOLID MECHANICS (SOLID)

Background Material

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.
- 2 In the Settings window for Linear Elastic Material, type Background Material in the Label text field.
- 3 Locate the Linear Elastic Material section. From the Specify list, choose Pressurewave and shear-wave speeds.
- **4** From the $c_{\rm p}$ list, choose **User defined**. In the associated text field, type cP.
- **5** From the $c_{\rm s}$ list, choose **User defined**. In the associated text field, type cS.
- **6** From the ρ list, choose **User defined**. In the associated text field, type rho.

Add the boundary condition for a cavity inclusion.

Cavity Inclusion, P Wave

- I In the Physics toolbar, click Boundaries and choose Boundary Load.
- 2 In the Settings window for Boundary Load, type Cavity Inclusion, P Wave in the Label text field.
- 3 Select Boundaries 29, 30, 33, and 34 only.
- **4** Locate the **Force** section. Specify the $\mathbf{F}_{\mathbf{A}}$ vector as

```
-(s11P*solid.nx+s12P*solid.ny) x
-(s12P*solid.nx+s22P*solid.ny) y
```

Now add the boundary condition for an infinitely rigid inclusion.

Infinitely Rigid Inclusion, P Wave

- I In the Physics toolbar, click Boundaries and choose Prescribed Displacement.
- 2 In the Settings window for Prescribed Displacement, type Infinitely Rigid Inclusion, P Wave in the Label text field.
- 3 Select Boundaries 41, 42, 45, and 46 only.
- 4 Locate the Prescribed Displacement section. From the Displacement in x direction list, choose Prescribed.
- **5** In the u_{0x} text field, type -uP.
- 6 From the Displacement in y direction list, choose Prescribed.
- **7** In the u_{0v} text field, type -vP.

Finally, set up the domain equation for the elastic inclusion.

Elastic Inclusion, P Wave

- I In the Physics toolbar, click **Domains** and choose **Linear Elastic Material**.
- 2 In the Settings window for Linear Elastic Material, type Elastic Inclusion, P Wave in the Label text field.
- **3** Select Domain 25 only.
- 4 Locate the Linear Elastic Material section. From the Specify list, choose Lamé parameters.
- **5** From the λ list, choose **User defined**. In the associated text field, type lambLame 0.
- **6** From the μ list, choose **User defined**. In the associated text field, type muLame_o.
- **7** From the ρ list, choose **User defined**. In the associated text field, type rho_o.

Add the initial stress and strain computed from the background field.

Initial Stress and Strain I

- I In the Physics toolbar, click Attributes and choose Initial Stress and Strain.
- 2 In the Settings window for Initial Stress and Strain, locate the Initial Stress and Strain section.
- **3** In the S_0 table, enter the following settings:

-s11P	-s12P	0
-s I 2P	-s22P	0

4 In the ε_0 table, enter the following settings:

-eps11P	-eps12P	0
-eps12P	-eps22P	0

Add also the body force.

Body Load (Elastic Inclusion), P Wave

- I In the Physics toolbar, click **Domains** and choose **Body Load**.
- 2 In the Settings window for Body Load, type Body Load (Elastic Inclusion), P Wave in the Label text field.
- **3** Select Domain 25 only.
- **4** Locate the **Force** section. Specify the $\mathbf{F}_{\mathbf{V}}$ vector as

(rho-rho_o)*(-omega^2)*uP	x
(rho-rho_o)*(-omega^2)*vP	у

MESH I

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domains 1, 2, 5, 8–10, 13, 16–18, 21, and 24 only.

Free Triangular 1

In the Mesh toolbar, click Free Triangular.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 Click the **Custom** button.
- 4 Locate the Element Size Parameters section. In the Maximum element size text field, type wlengthS/6.
- 5 In the Minimum element size text field, type wlengthS/8.
- 6 Click Build All.

P WAVE

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type P Wave in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.

Step 1: Frequency Domain

- I In the Model Builder window, under P Wave click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type omega/2/pi[rad].

P WAVE

- I In the Model Builder window, expand the Results node.
- 2 Right-click P Wave and choose Compute.

RESULTS

Scattered u Field

I In the Home toolbar, click Add Plot Group and choose 2D Plot Group.

- 2 In the Settings window for 2D Plot Group, type Scattered u Field in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Manual.
- 4 In the Title text area, type Displacement Field, X-component.
- 5 Clear the Parameter indicator text field.
- 6 Locate the Plot Settings section. Clear the Plot dataset edges check box.

Surface I

- I Right-click Scattered u Field and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type u.
- 4 Locate the Coloring and Style section. From the Scale list, choose Linear symmetric.

Selection 1

- I Right-click Surface I and choose Selection.
- **2** Select Domains 3, 4, 6, 7, 11, 12, 14, 15, 19, 20, 22, 23, and 25 only.

Scattered u Field

In the Model Builder window, under Results click Scattered u Field.

Table Annotation I

- I In the Scattered u Field toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	5	Cavity
12	5	Rigid
24	5	Elastic

- 5 In the Scattered u Field toolbar, click Plot.
- **6** Locate the Coloring and Style section. From the Anchor point list, choose Center.
- 7 Clear the **Show point** check box.

Surface I

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, collapse the Surface I node.

RESULTS

Scattered u Field

- I In the Model Builder window, collapse the Results>Scattered u Field node.
- 2 In the Model Builder window, right-click Scattered u Field and choose Duplicate.

Scattered v Field

- I In the Model Builder window, expand the Results>Scattered u Field I node, then click Scattered u Field I.
- 2 In the Settings window for 2D Plot Group, type Scattered v Field in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type Displacement Field, Y-component.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type v.
- 4 In the Scattered v Field toolbar, click Plot.

RESULTS

Scattered v Field

- I In the Model Builder window, collapse the Results>Scattered v Field node.
- 2 In the Model Builder window, right-click Scattered v Field and choose Duplicate.

Scattered Displacement Field Magnitude

- I In the Model Builder window, expand the Results>Scattered v Field I node, then click Scattered v Field I.
- 2 In the **Settings** window for **2D Plot Group**, type **Scattered Displacement Field**Magnitude in the **Label** text field.
- 3 Locate the **Title** section. In the **Title** text area, type **Displacement** Magnitude.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type solid.disp.

- 5 Locate the Coloring and Style section. From the Scale list, choose Linear.
- 6 Click Change Color Table.
- 7 In the Color Table dialog box, select Rainbow>SpectrumLight in the tree.
- 8 Click OK.

Scattered Displacement Field Magnitude

- I In the Model Builder window, right-click Scattered Displacement Field Magnitude and choose **Duplicate**.
- 2 In the Model Builder window, collapse the Scattered Displacement Field Magnitude node.

Apply the divergence to the displacement field to highlight P waves only.

Scattered P Wave

- I In the Model Builder window, under Results click Scattered Displacement Field Magnitude I.
- 2 In the Settings window for 2D Plot Group, type Scattered P Wave in the Label text field.
- 3 Locate the Title section. In the Title text area, type Scattered P Wave.

Surface I

- I In the Model Builder window, expand the Scattered P Wave node, then click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type d(u,x)+d(v,y).
- 4 In the Scattered P Wave toolbar, click Plot.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Wave>Wave in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Coloring and Style section.
- 9 From the Scale list, choose Linear symmetric.
- **10** In the **Scattered P Wave** toolbar, click **Plot**.

Apply the curl to the displacement field to highlight S waves only.

Scattered P Wave

In the Model Builder window, right-click Scattered P Wave and choose Duplicate.

Scattered S Wave

- I In the Model Builder window, under Results click Scattered P Wave I.
- 2 In the Settings window for 2D Plot Group, type Scattered S Wave in the Label text field.

3 Locate the Title section. In the Title text area, type Scattered S Wave.

Scattered P Wave

In the Model Builder window, collapse the Results>Scattered P Wave node.

Surface 1

- In the Model Builder window, expand the Results>Scattered S Wave node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Solid Mechanics> Displacement>Curl of displacement (material and geometry frames)>solid.curlUZ Curl of displacement, Z-component.
- 3 In the Scattered S Wave toolbar, click Plot.

RESULTS

Scattered S Wave

In the Model Builder window, collapse the Results>Scattered S Wave node.

Scattered Displacement Field Magnitude

In the Model Builder window, right-click Scattered Displacement Field Magnitude and choose Duplicate.

Add the incident field to the scattered to obtain the total displacement.

Total Displacement Field Magnitude

- In the Model Builder window, expand the Results>
 Scattered Displacement Field Magnitude I node, then click
 Scattered Displacement Field Magnitude I.
- 2 In the **Settings** window for **2D Plot Group**, type Total Displacement Field Magnitude in the **Label** text field.
- 3 Locate the Title section. In the Title text area, type Total Displacement Magnitude.

Surface 1

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type sqrt((real(u+uP))^2+(real(v+vP))^2).
- 4 In the Total Displacement Field Magnitude toolbar, click Plot.

RESULTS

Total Displacement Field Magnitude

In the Model Builder window, collapse the Results>Total Displacement Field Magnitude node.

Scattered P Wave

In the Model Builder window, right-click Scattered P Wave and choose Duplicate.

Total P Wave

- I In the Model Builder window, expand the Results>Scattered P Wave I node, then click Scattered P Wave I.
- 2 In the Settings window for 2D Plot Group, type Total P Wave in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type **Total** P Wave.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type d(u+uP,x)+d(v+vP,y).

RESULTS

Total P Wave

In the Model Builder window, collapse the Results>Total P Wave node.

Scattered S Wave

In the Model Builder window, right-click Scattered S Wave and choose Duplicate.

Total S Wave

- I In the Model Builder window, expand the Results>Scattered S Wave I node, then click Scattered S Wave 1.
- 2 In the Settings window for 2D Plot Group, type Total S Wave in the Label text field.
- 3 Locate the **Title** section. In the **Title** text area, type **Total** S Wave.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type d(v+vP,x)-d(u+uP,y).
- 4 In the Total S Wave toolbar, click Plot.

Now analyze the case of impinging S wave.

DEFINITIONS

Incident P Wave

In the Model Builder window, under Component I (compl)>Definitions right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Component I (compl)>Definitions click Incident P Wave I.
- 2 In the Settings window for Variables, type Incident S Wave in the Label text field.
- 3 Locate the Variables section. In the table, enter the following settings:

Name	Expression	Unit	Description
uS	O[m]	m	Incident wave: u field
vS	exp(-1i*kS*x-1i*pi/2+ 1i*phase)[m]	m	Incident wave: v field
eps11S	d(uS,x)		Incident wave: strain tensor, 11 component
eps22S	d(vS,y)		Incident wave: strain tensor, 22 component
eps12S	0.5*(d(uS,y)+d(vS,x))		Incident wave: strain tensor, 12 component
s11S	<pre>(lambLame+2*muLame)* eps11S+lambLame*eps22S</pre>	Pa	Incident wave: stress tensor, 11 component
s22S	lambLame*eps11S+ (lambLame+2*muLame)* eps22S	Pa	Incident wave: stress tensor, 22 component
s12S	2*muLame*eps12S	Pa	Incident wave: stress tensor, 12 component

SOLID MECHANICS (SOLID)

In the Model Builder window, expand the Component I (compl)>Solid Mechanics (solid) node.

Body Load (Elastic Inclusion), P Wave, Cavity Inclusion, P Wave, Elastic Inclusion, P Wave, Infinitely Rigid Inclusion, P Wave

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid), Ctrlclick to select Cavity Inclusion, P Wave, Infinitely Rigid Inclusion, P Wave, Elastic Inclusion, P Wave, and Body Load (Elastic Inclusion), P Wave.
- 2 Right-click and choose Group.

P Wave

- I In the Settings window for Group, type P Wave in the Label text field.
- 2 Right-click P Wave and choose Duplicate.
- 3 In the Model Builder window, collapse the P Wave node.

S Wave

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click P Wave I.
- 2 In the Settings window for Group, type S Wave in the Label text field.

Cavity Inclusion, S Wave

- I In the Model Builder window, expand the S Wave node, then click Cavity Inclusion, P Wave I.
- 2 In the Settings window for Boundary Load, type Cavity Inclusion, S Wave in the **Label** text field.
- **3** Locate the **Force** section. Specify the $\mathbf{F}_{\mathbf{A}}$ vector as

-(s11S*solid.nx+s12S*solid.ny)	x
-(s12S*solid.nx+s22S*solid.ny)	у

Infinitely Rigid Inclusion, S Wave

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid)> S Wave click Infinitely Rigid Inclusion, P Wave I.
- 2 In the Settings window for Prescribed Displacement, type Infinitely Rigid Inclusion, S Wave in the Label text field.
- **3** Locate the **Prescribed Displacement** section. In the u_{0x} text field, type -uS.
- **4** In the u_{0v} text field, type -vS.

Elastic Inclusion, S Wave

- I In the Model Builder window, expand the Component I (compl)>Solid Mechanics (solid)> S Wave>Elastic Inclusion, P Wave I node, then click Elastic Inclusion, P Wave I.
- 2 In the Settings window for Linear Elastic Material, type Elastic Inclusion, S Wave in the Label text field.

Initial Stress and Strain

I In the Model Builder window, under Component I (compl) > Solid Mechanics (solid) > S Wave>Elastic Inclusion, S Wave click Initial Stress and Strain 1.

- 2 In the **Settings** window for **Initial Stress and Strain**, type Initial Stress and Strain in the **Label** text field.
- **3** Locate the **Initial Stress and Strain** section. In the S_0 table, enter the following settings:

-s11S	-s12S	0
-s12S	- \$22\$	0

4 In the ε_0 table, enter the following settings:

-eps11S	-eps12S	0
-eps12S	-eps22S	0

Body Load (Elastic Inclusion), S Wave

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid)> S Wave click Body Load (Elastic Inclusion), P Wave I.
- 2 In the Settings window for Body Load, type Body Load (Elastic Inclusion), S Wave in the Label text field.
- **3** Locate the **Force** section. Specify the \mathbf{F}_V vector as

Elastic Inclusion, S Wave

In the Model Builder window, collapse the Component I (compl)>Solid Mechanics (solid)> S Wave>Elastic Inclusion, S Wave node.

SOLID MECHANICS (SOLID)

S Wave

In the Model Builder window, collapse the Component I (compl)>Solid Mechanics (solid)> S Wave node.

Modify the previous study to include only the desired boundary conditions for future reruns.

P WAVE

Step 1: Frequency Domain

I In the Model Builder window, expand the P Wave node, then click Step I: Frequency Domain.

- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 Select the Modify model configuration for study step check box.
- 4 In the tree, select Component I (compl)>Solid Mechanics (solid)>S Wave.
- 5 Click O Disable.

P WAVE

In the **Model Builder** window, collapse the **P Wave** node.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 4 Click Add Study in the window toolbar.

S WAVE

- I In the Model Builder window, click Study 2.
- 2 In the Settings window for Study, type S Wave in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.
- I In the Model Builder window, under S Wave click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type omega/2/pi[rad].
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Solid Mechanics (solid)>P Wave.
- 6 Click / Disable.
- 7 In the Home toolbar, click **Compute**.
- 8 In the Home toolbar, click Add Study to close the Add Study window.

RESULTS

Add the results for the incident S wave near those obtained for the P wave.

Scattered u Field

I In the Model Builder window, under Results click Scattered u Field.

- 2 In the Settings window for 2D Plot Group, click to expand the Plot Array section.
- **3** Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, expand the Scattered u Field node, then click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Scattered u Field click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).
- 4 In the Scattered u Field toolbar, click Plot.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Scattered u Field

In the Model Builder window, click Scattered u Field.

Table Annotation 2

- I In the Scattered u Field toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- 6 Clear the **Show point** check box.
- 7 In the Scattered u Field toolbar, click Plot.
- 8 Click the Zoom Extents button in the Graphics toolbar.

Incident P Wave

- I In the Model Builder window, click Incident P Wave.
- 2 In the Settings window for Surface, click to expand the Range section.
- **3** Select the Manual color range check box.
- 4 In the Minimum text field, type -1.5.
- 5 In the Maximum text field, type 1.5.

Incident S Wave

- I In the Model Builder window, click Incident S Wave.
- 2 In the Settings window for Surface, click to expand the Inherit Style section.
- 3 From the Plot list, choose Incident P Wave.
- 4 In the Scattered u Field toolbar, click Plot.

Scattered u Field

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, click Scattered u Field.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose New view.
- 5 In the Scattered u Field toolbar, click **Plot**.

Scattered v Field

- I In the Model Builder window, click Scattered v Field.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- 3 Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, expand the Scattered v Field node, then click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Scattered v Field click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).

Incident P Wave

- I In the Model Builder window, click Incident P Wave.
- 2 In the Settings window for Surface, locate the Range section.
- 3 Select the Manual color range check box.
- 4 In the Minimum text field, type -1.5.
- 5 In the Maximum text field, type 1.5.

Incident S Wave

- I In the Model Builder window, click Incident S Wave.
- 2 In the Settings window for Surface, locate the Inherit Style section.
- 3 From the Plot list, choose Incident P Wave.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Scattered v Field

In the Model Builder window, click Scattered v Field.

Table Annotation 2

- I In the Scattered v Field toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.

4 In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Scattered v Field toolbar, click **Plot**.

Scattered v Field

- I In the Model Builder window, click Scattered v Field.
- 2 Click Plot.
- 3 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 4 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 5 From the View list, choose View 2D 2.

Scattered Displacement Field Magnitude

- I In the Model Builder window, click Scattered Displacement Field Magnitude.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- 3 Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, expand the Scattered Displacement Field Magnitude node, then click Surface 1.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- In the Model Builder window, under Results>Scattered Displacement Field Magnitude click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).

Incident P Wave

- I In the Model Builder window, click Incident P Wave.
- 2 In the Settings window for Surface, locate the Range section.

- 3 Select the Manual color range check box.
- 4 In the Minimum text field, type 0.
- 5 In the Maximum text field, type 2.5.

Incident S Wave

- I In the Model Builder window, click Incident S Wave.
- 2 In the Settings window for Surface, click to collapse the Inherit Style section.
- 3 Click to expand the Inherit Style section. From the Plot list, choose Incident P Wave.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Scattered Displacement Field Magnitude

In the Model Builder window, click Scattered Displacement Field Magnitude.

Table Annotation 2

- I In the Scattered Displacement Field Magnitude toolbar, click More Plots and choose **Table Annotation.**
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Scattered Displacement Field Magnitude toolbar, click **Plot**.

Scattered Displacement Field Magnitude

I Click the Toom Extents button in the Graphics toolbar.

- 2 In the Model Builder window, click Scattered Displacement Field Magnitude.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 1.

Scattered P Wave

- I In the Model Builder window, expand the Results>Scattered P Wave node, then click Scattered P Wave.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- 3 Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, under Results>Scattered P Wave click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Scattered P Wave click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).

Table Annotation 1

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Scattered P Wave

In the Model Builder window, click Scattered P Wave.

Table Annotation 2

- I In the Scattered P Wave toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.

- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Scattered P Wave toolbar, click Plot.

Scattered P Wave

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, click Scattered P Wave.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 2.

Scattered S Wave

- I In the Model Builder window, click Scattered S Wave.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- **3** Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, expand the Scattered S Wave node, then click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Scattered S Wave click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).
- 4 In the Scattered S Wave toolbar, click **Plot**.

Table Annotation 1

I In the Model Builder window, click Table Annotation I.

- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Scattered S Wave

In the Model Builder window, click Scattered S Wave.

Table Annotation 2

- I In the Scattered S Wave toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Scattered S Wave toolbar, click Plot.

Scattered S Wave

- I Click the Zoom Extents button in the Graphics toolbar.
- 2 In the Model Builder window, click Scattered S Wave.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 3.

Total Displacement Field Magnitude

- I In the Model Builder window, expand the Results>Total Displacement Field Magnitude node, then click Total Displacement Field Magnitude.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- **3** Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, under Results>Total Displacement Field Magnitude click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Total Displacement Field Magnitude click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).
- 4 Locate the Expression section. In the Expression text field, type sqrt((real(u+uS))^2+ (real(v+vS))^2).

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Total Displacement Field Magnitude

In the Model Builder window, click Total Displacement Field Magnitude.

Table Annotation 2

- I In the Total Displacement Field Magnitude toolbar, click More Plots and choose **Table Annotation.**
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Total Displacement Field Magnitude toolbar, click **Displacement** Plot.

Total Displacement Field Magnitude

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, click Total Displacement Field Magnitude.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 4.

Total P Wave

- I In the Model Builder window, expand the Results>Total P Wave node, then click Total P Wave
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- 3 Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, under Results>Total P Wave click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Total P Wave click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose S Wave/Solution 2 (sol2).
- **4** Locate the **Expression** section. In the **Expression** text field, type d(u+uS,x)+d(v+vS,y).
- 5 In the Total P Wave toolbar, click Plot.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.

3 In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Total P Wave

In the Model Builder window, click Total P Wave.

Table Annotation 2

- I In the Total P Wave toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Total P Wave toolbar, click Plot.

Total P Wave

- I Click the Zoom Extents button in the Graphics toolbar.
- 2 In the Model Builder window, click Total P Wave.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 5.

Total S Wave

- I In the Model Builder window, expand the Results>Total S Wave node, then click Total S Wave.
- 2 In the Settings window for 2D Plot Group, locate the Plot Array section.
- **3** Select the **Enable** check box.
- 4 From the Array axis list, choose y.

Incident P Wave

- I In the Model Builder window, under Results>Total S Wave click Surface I.
- 2 In the Settings window for Surface, type Incident P Wave in the Label text field.
- 3 Right-click Incident P Wave and choose Duplicate.

Incident S Wave

- I In the Model Builder window, under Results>Total S Wave click Incident P Wave I.
- 2 In the Settings window for Surface, type Incident S Wave in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose \$ Wave/Solution 2 (sol2).
- **4** Locate the **Expression** section. In the **Expression** text field, type d(v+vS,x)-d(u+uS,y).

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Total S Wave

In the Model Builder window, click Total S Wave.

Table Annotation 2

- I In the Total S Wave toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	P Wave
-9	10.5	S Wave

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- 6 Clear the **Show point** check box.
- 7 In the Total S Wave toolbar, click Plot.

Total S Wave

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, click Total S Wave.
- 3 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 4 From the View list, choose View 2D 2.

The resulting plot is shown in Figure 6.

5 In the Model Builder window, collapse the Total S Wave node.

Total P Wave

In the Model Builder window, collapse the Results>Total P Wave node.

Total Displacement Field Magnitude

In the Model Builder window, collapse the Results>Total Displacement Field Magnitude node.

Scattered S Wave

In the Model Builder window, collapse the Results>Scattered S Wave node.

Scattered P Wave

In the Model Builder window, collapse the Results>Scattered P Wave node.

Scattered Displacement Field Magnitude

In the Model Builder window, collapse the Results>Scattered Displacement Field Magnitude node.

Scattered v Field

In the Model Builder window, collapse the Results>Scattered v Field node.

Scattered u Field

In the Model Builder window, collapse the Results>Scattered u Field node.

Scattered Displacement Field Magnitude, Scattered P Wave, Scattered S Wave, Scattered u Field, Scattered v Field, Total Displacement Field Magnitude, Total P Wave, Total S Wave

- I In the Model Builder window, under Results, Ctrl-click to select Scattered u Field,
 Scattered v Field, Scattered Displacement Field Magnitude, Scattered P Wave,
 Scattered S Wave, Total Displacement Field Magnitude, Total P Wave, and Total S Wave.
- 2 Right-click and choose Group.

Plane Wave

In the Settings window for Group, type Plane Wave in the Label text field.

Add a point where to apply the point source.

GEOMETRY I

Point I (ptl)

- I In the **Geometry** toolbar, click **Point**.
- 2 In the Settings window for Point, locate the Point section.
- 3 In the x text field, type ((R-r layer-r o)/2+r o)*cos(pi/4).
- 4 In the y text field, type $((R-r_1ayer-r_0)/2+r_0)*sin(pi/4)$.
- 5 Click **Pauld Selected**.
- 6 Drag and drop below Circle I (c1).
- 7 Click | Build Selected.

Array I (arrI)

- I In the Model Builder window, click Array I (arrI).
- 2 Click the Select All button in the Graphics toolbar.
- 3 In the Settings window for Array, click | Build All Objects.

SOLID MECHANICS (SOLID)

Point Load 1

- I In the Physics toolbar, click Points and choose Point Load.
- **2** Select Point 29 only.
- 3 In the Settings window for Point Load, locate the Force section.
- **4** Specify the $\mathbf{F}_{\mathbf{P}}$ vector as

1 x

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

POINT SOURCE INCIDENT FIELD

I In the Model Builder window, click Study 3.

- 2 In the Settings window for Study, locate the Study Settings section.
- 3 Clear the Generate default plots check box.
- 4 In the Label text field, type Point Source Incident Field.

P WAVE

Step 1: Frequency Domain

- I In the Model Builder window, expand the P Wave node, then click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Load I.
- 4 Click O Disable.

P WAVE

In the Model Builder window, collapse the P Wave node.

S WAVE

- I In the Model Builder window, expand the S Wave node, then click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 Click O Disable.

S WAVE

In the Model Builder window, collapse the S Wave node.

POINT SOURCE INCIDENT FIELD

- I In the Model Builder window, expand the Point Source Incident Field node, then click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type omega/2/pi[rad].
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Solid Mechanics (solid)>P Wave.
- 6 Click O Disable.

- 7 In the tree, select Component I (compl)>Solid Mechanics (solid)>S Wave.
- 8 Click O Disable.
- **9** In the **Home** toolbar, click **Compute**.

Plot the field generated by the point source, that will be used as incident field.

RESULTS

Point Source Background Fields

- I In the Home toolbar, click Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Point Source Background Fields in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Point Source Incident Field/ Solution 3 (sol3).
- 4 Locate the Plot Settings section. Clear the Plot dataset edges check box.
- **5** Locate the **Plot Array** section. Select the **Enable** check box.

Displacement Magnitude

- I Right-click Point Source Background Fields and choose Surface.
- 2 In the Settings window for Surface, type Displacement Magnitude in the Label text field.
- 3 Locate the Coloring and Style section. Click Change Color Table.
- 4 In the Color Table dialog box, select Rainbow>SpectrumLight in the tree.
- 5 Click OK.

Selection 1

- I Right-click Displacement Magnitude and choose Selection.
- **2** Select Domains 19, 20, 22, 23, and 25 only.

Displacement Magnitude

- I In the Model Builder window, click Displacement Magnitude.
- 2 In the Settings window for Surface, locate the Range section.
- 3 Select the Manual color range check box.
- **4** In the **Minimum** text field, type 0.
- 5 In the Maximum text field, type 0.15.
- 6 In the Point Source Background Fields toolbar, click **Plot**.

7 Right-click Displacement Magnitude and choose Duplicate.

P Wave

- I In the Model Builder window, under Results>Point Source Background Fields click
 Displacement Magnitude 1.
- 2 In the Settings window for Surface, type P Wave in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type d(u,x)+d(v,y).
- 4 Locate the Range section. Clear the Manual color range check box.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Wave>Wave in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Range section.
- 9 Select the Manual color range check box.
- 10 In the Minimum text field, type -0.8.
- II In the Maximum text field, type 0.8.
- 12 In the Point Source Background Fields toolbar, click Plot.
- **I3** Right-click **P Wave** and choose **Duplicate**.

S Wave

- I In the Model Builder window, expand the P Wave node, then click Results> Point Source Background Fields>P Wave I.
- 2 In the Settings window for Surface, type S Wave in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type d(v,x) d(u,y).
- 4 In the Point Source Background Fields toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 6 Locate the Range section. In the Minimum text field, type -4.
- 7 In the Maximum text field, type 4.
- 8 In the Point Source Background Fields toolbar, click Plot.
- **9** Click the **Zoom Extents** button in the **Graphics** toolbar.

Point Source Background Fields

In the Model Builder window, click Point Source Background Fields.

Table Annotation I

I In the Point Source Background Fields toolbar, click More Plots and choose Table Annotation.

- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
24	5	Displacement
34.4	5	P Wave
44.6	5	S Wave

- 5 Locate the Coloring and Style section. Clear the Show point check box.
- **6** From the **Anchor point** list, choose **Center**.
- 7 In the Point Source Background Fields toolbar, click Plot.

The resulting plot is shown in Figure 7.

Point Source Background Fields

- I In the Model Builder window, click Point Source Background Fields.
- 2 In the Settings window for 2D Plot Group, locate the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Point Source Background Fields.
- 5 Clear the Parameter indicator text field.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

View 2D 3

In the Model Builder window, under Results right-click Views and choose View 2D.

Point Source Background Fields

- I In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 2 From the View list, choose View 2D 3.

P Wave

In the Model Builder window, collapse the Results>Point Source Background Fields>P Wave node.

Displacement Magnitude

In the Model Builder window, collapse the Results>Point Source Background Fields> Displacement Magnitude node.

Point Source Background Fields

In the Model Builder window, collapse the Results>Point Source Background Fields node.

Set the results of the previous study to be the new incident field.

DEFINITIONS

Incident S Wave

In the Model Builder window, under Component I (compl)>Definitions right-click **Incident S Wave** and choose **Duplicate**.

Point Source

- I In the Model Builder window, under Component I (compl)>Definitions click Incident S Wave I.
- 2 In the Settings window for Variables, type Point Source in the Label text field.
- **3** Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
uPS	<pre>withsol('sol3',u)* exp(1i*phase)</pre>	m	Incident wave: u field
vPS	<pre>withsol('sol3',v)* exp(1i*phase)</pre>	m	Incident wave: v field
eps11PS	<pre>withsol('sol3', solid.el11)*exp(1i* phase)</pre>		Incident wave: strain tensor, 11 component
eps22PS	<pre>withsol('sol3', solid.el22)*exp(1i* phase)</pre>		Incident wave: strain tensor, 22 component
eps12PS	<pre>withsol('sol3', solid.el12)*exp(1i* phase)</pre>		Incident wave: strain tensor, 12 component
s11PS	<pre>withsol('sol3', solid.sl11)*exp(1i* phase)</pre>	N/m²	Incident wave: stress tensor, 11 component
s22PS	<pre>withsol('sol3', solid.sl22)*exp(1i* phase)</pre>	N/m²	Incident wave: stress tensor, 22 component
s12PS	<pre>withsol('sol3', solid.sl12)*exp(1i* phase)</pre>	N/m²	Incident wave: stress tensor, 12 component

Note that the point source background field is only defined on the third computational domain. Add two General Extrusion operators in order to make the point source background field available also for the other two computational domains.

General Extrusion I (genext1)

- I In the Definitions toolbar, click Nonlocal Couplings and choose General Extrusion.
- 2 Select Domains 17–25 only.
- 3 In the Settings window for General Extrusion, locate the Destination Map section.
- 4 In the x-expression text field, type x+24.
- 5 Right-click General Extrusion I (genext1) and choose Duplicate.

General Extrusion 2 (genext2)

- I In the Model Builder window, click General Extrusion 2 (genext2).
- 2 In the Settings window for General Extrusion, locate the Destination Map section.
- 3 In the x-expression text field, type x+12.

SOLID MECHANICS (SOLID)

S Wave

- I In the Model Builder window, expand the Component I (compl)>Solid Mechanics (solid)> P Wave>Cavity Inclusion, P Wave node.
- 2 Right-click Component I (compl)>Solid Mechanics (solid)>S Wave and choose Duplicate.

Point Source

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click S Wave I.
- 2 In the Settings window for Group, type Point Source in the Label text field.

Cavity Inclusion, Point Source

- I In the Model Builder window, expand the Point Source node, then click Cavity Inclusion,
- 2 In the Settings window for Boundary Load, type Cavity Inclusion, Point Source in the Label text field.
- $\boldsymbol{3}$. Locate the \boldsymbol{Force} section. Specify the \boldsymbol{F}_A vector as

-(genext1(s11PS)*solid.nx+genext1(s12PS)*solid.ny)	x
-(genext1(s12PS)*solid.nx+genext1(s22PS)*solid.ny)	у

Infinitely Rigid Inclusion, Point Source

I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid)> Point Source click Infinitely Rigid Inclusion, S Wave I.

- 2 In the Settings window for Prescribed Displacement, type Infinitely Rigid Inclusion, Point Source in the Label text field.
- **3** Locate the **Prescribed Displacement** section. In the u_{0x} text field, type -genext2(uPS).
- **4** In the u_{0v} text field, type -genext2(vPS).

Elastic Inclusion, Point Source

- I In the Model Builder window, click Elastic Inclusion, S Wave I.
- 2 In the Settings window for Linear Elastic Material, type Elastic Inclusion, Point Source in the Label text field.

Initial Stress and Strain

- I In the Model Builder window, click Initial Stress and Strain.
- 2 In the Settings window for Initial Stress and Strain, type Initial Stress and Strain in the Label text field.
- 3 Locate the Initial Stress and Strain section. In the S_0 table, enter the following settings:

-s11PS	-s12PS	0
-s12PS	-s22PS	0

4 In the ε_0 table, enter the following settings:

-eps11PS	-eps12PS	0
-eps12PS	-eps22PS	0

Body load (Elastic Inclusion), Point Source

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid)> Point Source click Body Load (Elastic Inclusion), S Wave I.
- 2 In the Settings window for Body Load, type Body load (Elastic Inclusion), Point Source in the Label text field.
- **3** Locate the **Force** section. Specify the $\mathbf{F}_{\mathbf{V}}$ vector as

(rho-rho_o)*(-omega^2)*uPS	x
(rho-rho_o)*(-omega^2)*vPS	у

Elastic Inclusion, Point Source

In the Model Builder window, collapse the Component I (compl)>Solid Mechanics (solid)> Point Source>Elastic Inclusion, Point Source node.

SOLID MECHANICS (SOLID)

Point Source

In the Model Builder window, collapse the Component I (comp I)>Solid Mechanics (solid)> Point Source node.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

POINT SOURCE SCATTERED FIELD

- I In the Model Builder window, click Study 4.
- 2 In the Settings window for Study, type Point Source Scattered Field in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.

P WAVE

Step 1: Frequency Domain

- I In the Model Builder window, expand the P Wave node, then click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source.
- 4 Click Disable.

S WAVE

- I In the Model Builder window, expand the S Wave node, then click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source.
- 4 Click O Disable.

POINT SOURCE INCIDENT FIELD

- I In the Model Builder window, expand the Point Source Incident Field node, then click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source.
- 4 Click O Disable.

POINT SOURCE SCATTERED FIELD

- I In the Model Builder window, under Point Source Scattered Field click
 Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type omega/2/pi[rad].
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Solid Mechanics (solid)>P Wave.
- 6 Click O Disable.
- 7 In the tree, select Component I (compl)>Solid Mechanics (solid)>S Wave.
- 8 Click O Disable.
- 9 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Load I.
- 10 Click O Disable.
- II In the Home toolbar, click **Compute**.

RESULTS

Point Source Scattered Displacement Field Magnitude

- I In the Home toolbar, click Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Point Source Scattered Displacement Field Magnitude in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Manual.
- 4 In the **Title** text area, type Displacement Magnitude.
- 5 Clear the Parameter indicator text field.
- 6 Locate the Data section. From the Dataset list, choose Point Source Scattered Field/ Solution 4 (sol4).

Surface I

Right-click Point Source Scattered Displacement Field Magnitude and choose Surface.

Selection 1

- I In the Model Builder window, right-click Surface I and choose Selection.
- **2** Select Domains 3, 4, 6, 7, 11, 12, 14, 15, 19, 20, 22, 23, and 25 only.

Surface I

- I In the Model Builder window, click Surface I.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Rainbow>SpectrumLight in the tree.
- 5 Click OK.

Point Source Scattered Displacement Field Magnitude

- I In the Model Builder window, click Point Source Scattered Displacement Field Magnitude.
- 2 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 3 Clear the Plot dataset edges check box.

Table Annotation I

- I In the Point Source Scattered Displacement Field Magnitude toolbar, click **More Plots** and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- **4** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	5	Cavity
12	5	Rigid
24	5	Elastic

- 5 Locate the Coloring and Style section. Clear the Show point check box.
- 6 From the Anchor point list, choose Center.

The resulting plot is shown in Figure 8.

View 2D 4

In the Model Builder window, under Results right-click Views and choose View 2D.

Point Source Scattered Displacement Field Magnitude

- I In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 2 From the View list, choose View 2D 4.
- 3 Click the Zoom Extents button in the Graphics toolbar.

Surface I

In the Model Builder window, collapse the Results>
Point Source Scattered Displacement Field Magnitude>Surface I node.

Point Source Scattered Displacement Field Magnitude

- I In the Model Builder window, right-click
 Point Source Scattered Displacement Field Magnitude and choose Duplicate.
- 2 In the Model Builder window, collapse the Point Source Scattered Displacement Field Magnitude node.

Point Source Total Displacement Field Magnitude

- In the Model Builder window, under Results click
 Point Source Scattered Displacement Field Magnitude 1.
- 2 In the Settings window for 2D Plot Group, type Point Source Total Displacement Field Magnitude in the Label text field.
- 3 In the Model Builder window, expand the Point Source Total Displacement Field Magnitude node.

Scattered Field Formulation

- I In the Model Builder window, expand the Results>
 Point Source Total Displacement Field Magnitude>Surface I node, then click Surface I.
- 2 In the Settings window for Surface, type Scattered Field Formulation in the Label text field.
- 3 Locate the Expression section. In the Expression text field, type if(x>20,
 sqrt((real(u+uPS))^2+(real(v+vPS))^2),if(x<5,sqrt((real(u+
 genext1(uPS)))^2+(real(v+genext1(vPS)))^2),sqrt((real(u+
 genext2(uPS)))^2+(real(v+genext2(vPS)))^2))).</pre>
- 4 Locate the Range section. Select the Manual color range check box.
- **5** In the **Minimum** text field, type 0.
- **6** In the **Maximum** text field, type **0.15**.
- 7 In the Point Source Total Displacement Field Magnitude toolbar, click Plot.

RESULTS

Point Source Total Displacement Field Magnitude

- I In the Model Builder window, collapse the Results> Point Source Total Displacement Field Magnitude node.
- 2 In the Model Builder window, click Point Source Total Displacement Field Magnitude.
- 3 In the Settings window for 2D Plot Group, locate the Title section.
- 4 In the Title text area, type Total Displacement Field Magnitude.

Compute the total field without using the scattered field formulation, that is, adopting the actual boundary conditions and field equation for the total field.

SOLID MECHANICS (SOLID)

Point Load 1

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Point Load 1.
- 2 Select Points 3, 16, and 29 only.

Fixed Constraint 1

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- 2 Select Boundaries 41, 42, 45, and 46 only.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 4 Click Add Study in the window toolbar.

POINT SOURCE TOTAL FIELD (NO SCATTERED FIELD FORMULATION)

- I In the Model Builder window, click Study 5.
- 2 In the Settings window for Study, type Point Source Total Field (NO Scattered Field Formulation) in the Label text field.
- 3 Locate the Study Settings section. Clear the Generate default plots check box.

P WAVE

Step 1: Frequency Domain

- I In the Model Builder window, expand the P Wave node, then click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Fixed Constraint I.
- 4 Click Disable.

S WAVE

- I In the Model Builder window, expand the S Wave node, then click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Fixed Constraint I.
- 4 Click Disable.

POINT SOURCE INCIDENT FIELD

- I In the Model Builder window, expand the Point Source Incident Field node, then click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Solid Mechanics (solid)>Fixed Constraint I.
- 4 Click O Disable.

POINT SOURCE SCATTERED FIELD

- I In the Model Builder window, expand the Point Source Scattered Field node, then click Step I: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Physics and Variables Selection section.
- 3 Click O Disable.

POINT SOURCE TOTAL FIELD (NO SCATTERED FIELD FORMULATION)

I In the Model Builder window, expand the
Point Source Total Field (NO Scattered Field Formulation) node, then click
Step I: Frequency Domain.

- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type omega/2/pi[rad].
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Solid Mechanics (solid)>P Wave.
- 6 Click Disable.
- 7 In the tree, select Component I (compl)>Solid Mechanics (solid)>S Wave.
- 8 Click (/) Disable.
- 9 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source> Cavity Inclusion, Point Source.
- 10 Click / Disable.
- II In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source> Infinitely Rigid Inclusion, Point Source.
- 12 Click / Disable.
- 13 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source> Elastic Inclusion, Point Source>Initial Stress and Strain.
- 14 Click / Disable.
- 15 In the tree, select Component I (compl)>Solid Mechanics (solid)>Point Source> Body load (Elastic Inclusion), Point Source.
- 16 Click Disable.
- 17 In the Home toolbar, click **Compute**.
- 18 In the Home toolbar, click Add Study to close the Add Study window.
- 19 In the Model Builder window, collapse the

Point Source Total Field (NO Scattered Field Formulation) node.

Plot the results obtained next to those obtained with the scattered field formulation for comparison.

RESULTS

Point Source Total Displacement Field Magnitude

- I In the Model Builder window, under Results click Point Source Total Displacement Field Magnitude.
- 2 In the Settings window for 2D Plot Group, click to expand the Plot Array section.
- 3 Select the **Enable** check box.

4 From the Array axis list, choose y.

Scattered Field Formulation

- In the Model Builder window, expand the Point Source Total Displacement Field Magnitude node.
- 2 Right-click Scattered Field Formulation and choose Duplicate.

NO Scattered Field Formulation

- I In the Model Builder window, click Scattered Field Formulation I.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Point Source Total Field (NO Scattered Field Formulation)/ Solution 5 (sol5).
- **4** Locate the **Expression** section. In the **Expression** text field, type solid.disp.
- 5 In the Point Source Total Displacement Field Magnitude toolbar, click **Plot**.
- 6 Click to expand the Inherit Style section. From the Plot list, choose Scattered Field Formulation.
- 7 In the Label text field, type NO Scattered Field Formulation.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.
- **3** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
0	15.5	Cavity
12	15.5	Rigid
24	15.5	Elastic

Point Source Total Displacement Field Magnitude

In the Model Builder window, click Point Source Total Displacement Field Magnitude.

Table Annotation 2

- I In the Point Source Total Displacement Field Magnitude toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.

4 In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
-9	0	SFF
-9	10.5	NO SFF

- 5 Locate the Coloring and Style section. From the Anchor point list, choose Middle left.
- **6** Clear the **Show point** check box.
- 7 In the Point Source Total Displacement Field Magnitude toolbar, click Plot.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Point Source Total Displacement Field Magnitude

- I In the Model Builder window, click Point Source Total Displacement Field Magnitude.
- 2 In the Settings window for 2D Plot Group, locate the Plot Settings section.
- 3 From the View list, choose New view.
- The resulting plot is shown in Figure 9.
- 5 In the Model Builder window, right-click Point Source Total Displacement Field Magnitude and choose **Duplicate**.

Point Source Total P Wave

- I In the Model Builder window, expand the Results> Point Source Total Displacement Field Magnitude I node, then click Point Source Total Displacement Field Magnitude 1.
- 2 In the Settings window for 2D Plot Group, type Point Source Total P Wave in the **Label** text field.

Scattered Field Formulation

- I In the Model Builder window, click Scattered Field Formulation.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type if (x>20,d(u+uPS,x)+d(v+vPS,y),if(x<5,d(u+uPS,x))genext1(uPS),x)+d(v+genext1(vPS),y),d(u+genext2(uPS),x)+d(v+genegenext2(vPS),y))).
- 4 In the Point Source Total P Wave toolbar, click Plot.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Wave>Wave in the tree.
- 7 Click OK.

- 8 In the Settings window for Surface, click to expand the Range section.
- **9** Select the Manual color range check box.
- 10 In the Minimum text field, type -0.5.
- II In the Maximum text field, type 0.5.
- 12 In the Point Source Total P Wave toolbar, click **12** Plot.

NO Scattered Field Formulation

- I In the Model Builder window, click NO Scattered Field Formulation.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type d(u,x)+d(v,y).
- 4 In the Point Source Total P Wave toolbar, click Plot.

Point Source Total P Wave

In the Model Builder window, right-click Point Source Total P Wave and choose Duplicate.

Point Source Total S Wave

- I In the Model Builder window, expand the Results>Point Source Total P Wave I node, then click Point Source Total P Wave I.
- 2 In the Settings window for 2D Plot Group, type Point Source Total S Wave in the Label text field

Scattered Field Formulation

- I In the Model Builder window, click Scattered Field Formulation.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type if(x>20,-d(u+uPS,y)+d(v+vPS,x),if(x<5,-d(u+genext1(uPS),y)+d(v+genext1(vPS),x),-d(u+genext2(uPS),y)+d(v+genext2(vPS),x))).</p>
- 4 Click to expand the Range section. Select the Manual color range check box.
- 5 In the Minimum text field, type -1.
- 6 In the Maximum text field, type 1.
- 7 In the Point Source Total S Wave toolbar, click **Plot**.

NO Scattered Field Formulation

- I In the Model Builder window, click NO Scattered Field Formulation.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 In the Expression text field, type -d(u,y)+d(v,x).
- 4 In the Point Source Total S Wave toolbar, click Plot.