



# Electrochemical Impedance Spectroscopy

## Introduction

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*Electrochemical impedance spectroscopy* is a common technique in electroanalysis. It is used to study the harmonic response of an electrochemical system. A small, sinusoidal variation is applied to the potential at the working electrode, and the resulting current is analyzed in the frequency domain.

The real and imaginary components of the impedance give information about the kinetic and mass transport properties of the cell, as well as its capacitive properties. By measuring impedance at a range of frequencies, the relative influence of the various constituent physics of the system can be interpreted as a function of time scale.

As in electrical analysis, the real component of impedance corresponds to a resistance in-phase with the applied voltage. The imaginary component corresponds to a reactance  $90^\circ$  out-of-phase with the applied voltage; the reactance is caused by capacitive charging in the cell.

Capacitive charging occurs at the *double layer* adjacent to the working electrode surface. Here, the net charge on the electrode causes accumulation or depletion of charged ions in the neighboring solution; as the potential on the electrode changes, so does its charge, and so the double layer charges and discharges with a characteristic capacitance.

In this example, the AC Impedance, Initial Values study type is used to perform a linearized perturbation study in the frequency domain around the provided initial values to resolve the magnitude and phase of the current response to the sinusoidal voltage. A Parametric Sweep is used to compare the response of the system with different electrode kinetics for the redox couple.

## Model Definition

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This model contains a single 1D domain. The length of the domain,  $L$  (m), is based on the diffusion coefficient,  $D$  ( $\text{m}^2/\text{s}$ ) and lowest frequency,  $f_{\min}$  (1/s), in order to be sufficiently large compared to the time scale of diffusion (the diffusion layer).

$$L = 10 \sqrt{\frac{D}{2\pi f_{\min}}} \quad (1)$$

### DOMAIN EQUATIONS

We assume the presence of a large quantity of supporting electrolyte. This is inert salt that is added in electroanalytical experiments to increase the conductivity of the electrolyte without otherwise interfering with the reaction chemistry. Under these conditions, the

resistance of the solution is sufficiently low that the electric field is negligible, and we can assume  $\phi_l = 0$ .

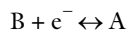
The Electroanalysis interface implements chemical transport equations for the reactant and product species of the redox couple subject to this assumption. The domain equation is the diffusion equation (also known as Fick's 2nd law) to describe the chemical transport of the electroactive species A and B:

$$\frac{\partial c_i}{\partial t} + \nabla \cdot (-D_i \nabla c_i) = 0$$

### BOUNDARY EQUATIONS

Both the oxidized and reduced species are equally concentrated at  $c_i = 1 \mu\text{M}$  in bulk ( $x = L$ ).

At the working electrode surface ( $x = 0$ ), the reactant species A oxidizes (loses one electron) to form the product B. By convention, electrochemical reactions are written in the reductive direction:



The stoichiometric coefficient is  $-1$  for B, the “reactant” in the reductive direction, and  $+1$  for A, the “product” in the reductive direction. The number of electrons transferred,  $n$ , equals one.

The current density for this reaction is given by the electroanalytical Butler-Volmer equation for an oxidation:

$$i_{\text{loc}} = nFk_0 \left( c_{\text{A}} \exp\left(\frac{(n - \alpha_c)F\eta}{RT}\right) - c_{\text{B}} \exp\left(\frac{-\alpha_c F\eta}{RT}\right) \right) \quad (2)$$

in which  $k_0$  is the *heterogeneous rate constant* of the reaction,  $\alpha_c$  is the cathodic *transfer coefficient*, and  $\eta$  is the overpotential at the working electrode. This overpotential is the difference between the applied potential and the *equilibrium potential* (formal reduction potential) of the redox couple of species A and B,  $E_{\text{eq}}$ :

$$\eta = \phi_{s, \text{ext}} - E_{\text{eq}}$$

According to Faraday's laws of electrolysis, the flux of the reactant and product species are proportional to the current density drawn:

$$-\mathbf{n} \cdot (-D_i \nabla c_i) = \frac{v_i i_{\text{loc}}}{nF} \quad (3)$$

This is expressed in the Electrode Surface boundary condition.

An additional capacitance is applied at the working electrode. It is set equal to  $20 \mu\text{F}/\text{cm}^2$  which is a typical value for a water-metal interface. The real value of this capacitance can be established by impedance spectroscopy of the blank solution containing only the supporting electrolyte, or by an alternative voltammetric method.

### AC IMPEDANCE STUDY

The AC Impedance study is used to model a harmonic perturbation applied to a fixed center electrode potential, which in this case is fixed to the equilibrium potential of the redox couple:

$$\phi_{s, \text{ext}} = E_{\text{eq}} + \Delta\phi e^{j\omega t}$$

where it is implied that only the real part of the complex term contributes.

The magnitude of this perturbation,  $\Delta\phi$ , is small with respect to  $RT/F$ , so that the Butler-Volmer equation (Equation 2) can be linearized. Therefore, the system responds linearly to the perturbation, and the flux (Equation 3), the concentration profiles, and the current density are all also subject to a sinusoidal perturbation at the same frequency.

The AC Impedance Study makes the approximation that the dependent variables  $c_i$  can be expressed as the sum of a stationary solution  $c_{i,0}$  due to the center voltage of the applied potential, and a sinusoidal perturbation  $c_{i,1}$  to the concentration resulting from the perturbation on the applied potential:

$$c_i(x, t) = c_{i,0}(x) + c_{i,1}(x) e^{j\omega t}$$

If  $c_{i,1}$  is complex, it implies that the response of the concentration profile is out-of-phase with the applied waveform.

The AC Impedance Initial Values study contains a Frequency Domain study step that solves for the perturbation around the provided initial values, for a range of applied frequencies from 1 Hz to 1 kHz. In each case the domain equation is the frequency domain form of Fick's 2nd Law:

$$j\omega c_{i,1} + \nabla \cdot (-D_i \nabla c_{i,1}) = 0$$

solved subject to  $c_{i,1} = 0$  in bulk and:

$$\phi_{s, \text{ext}} = \Delta\phi$$

at the surface.

A Parametric Sweep is used to investigate different values of the *heterogeneous rate constant* of the electrode reaction,  $k_0$ , from a value that is kinetically fast on the time scale of the study (0.1 cm/s) to one that it is slow on the same time scale (0.001 cm/s).

## Results and Discussion

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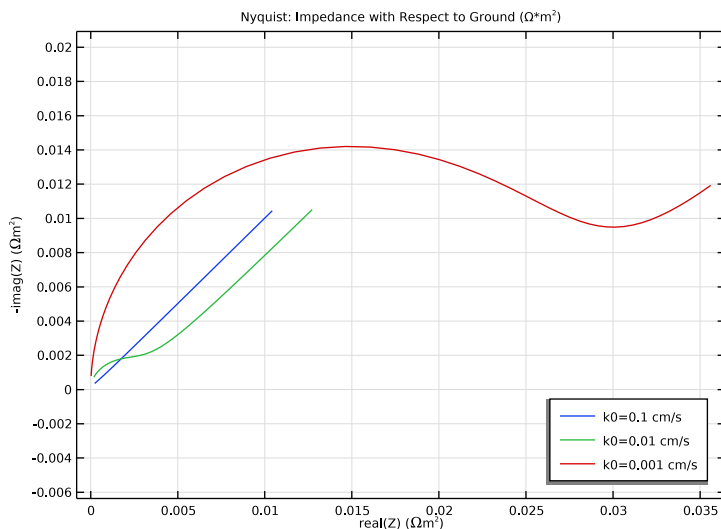
A Nyquist plot (Figure 1) is the most common means of plotting the results of an impedance experiment. It is an Argand diagram of the complex value of the impedance as a function of frequency; the real component of impedance (resistance) is plotted on the  $x$ -axis, and the imaginary component (reactance) is plotted on the  $y$ -axis.

For a fast electrochemical reaction with respect to the frequency of the electrochemical impedance study, the impedance always results from the limitation to the current due to the finite diffusivity of the redox species in the solution. It is known from theory that the real and imaginary impedances are linearly correlated in this “transport-controlled” regime (Figure 1).

For a slow electrochemical reaction with respect to the frequency, the mass transport is unimportant as the rate of electron transfer is limited by the rate of reaction at the surface: this is the “kinetically controlled” regime. This regime is characterized by a semi-circular Nyquist plot.

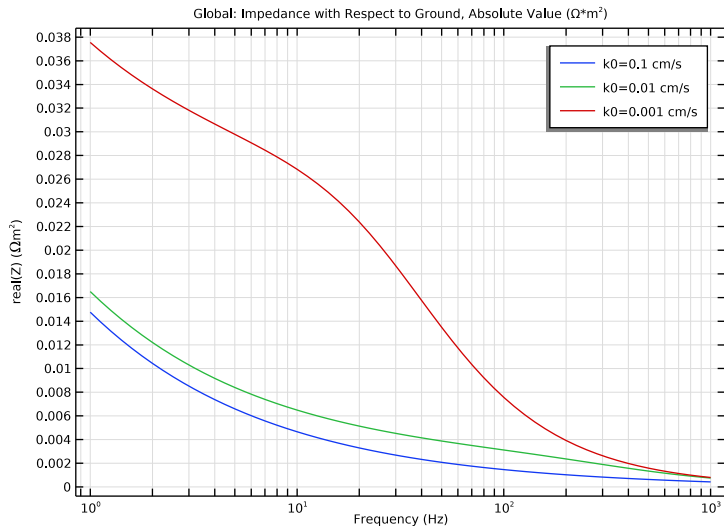
It is common to observe both regimes in a single plot, since the relevant time scale of the experiment changes with the frequency of the harmonic perturbation. At low frequency, mass transport dominates, but at high frequency (toward the lower-left of the plot), there

is a transition to kinetic control. This transition is most marked for the slowest electrochemical reaction studied, where  $k_0 = 0.001$  cm/s.

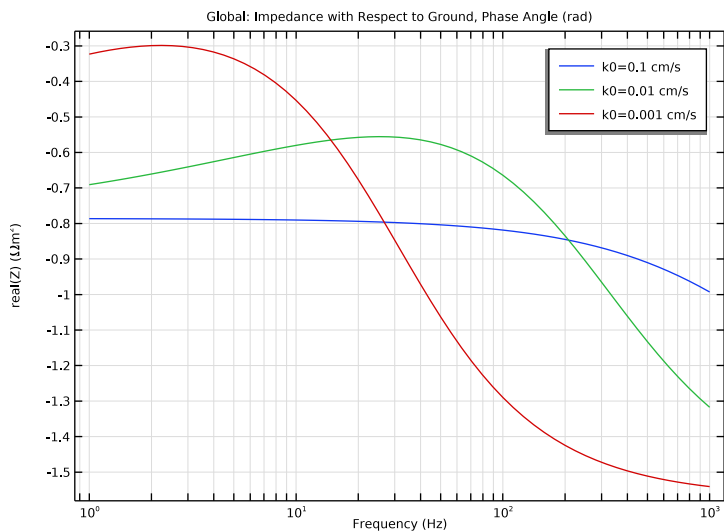


*Figure 1: Nyquist plot showing the relation of real to imaginary impedance for a range of frequencies and a range of electrode kinetic heterogeneous rate constants.*

In a Bode plot, either the magnitude (Figure 2) or the phase (Figure 3) of the complex impedance is plotted against frequency on the  $x$ -axis.



*Figure 2: Bode plot showing the magnitude of impedance as a function of frequency for a range of electrode kinetic heterogeneous rate constants.*



*Figure 3: Bode plot showing the phase of the impedance as a function of frequency for a range of electrode kinetic heterogeneous rate constants.*

Depending on whether a reaction proceeds under kinetic or transport control at a certain frequency, the Bode plots have different characteristic appearances. [Ref. 1.](#) gives a comprehensive discussion and references to further literature concerning the analysis of electrochemical impedance spectra.

## Reference

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1. A.J. Bard and L.R. Faulkner, *Electrochemical Methods, Fundamentals and Applications*, 2nd ed., Wiley, New York, 2001.

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**Application Library path:** Corrosion\_Module/General\_Electrochemistry/  
impedance\_spectroscopy


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## Modeling Instructions


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From the **File** menu, choose **New**.

### NEW

In the **New** window, click  **Model Wizard**.

### MODEL WIZARD

**1** In the **Model Wizard** window, click  **ID**.

**2** In the **Select Physics** tree, select **Electrochemistry>Electroanalysis (tcd)**.

**3** Click **Add**.

**4** In the **Concentrations** table, enter the following settings:

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cRed

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cOx

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**5** Click  **Study**.

Use an AC Impedance, Initial Values study type in this model. This study will set up a suitable solver sequence for your problem.

**6** In the **Select Study** tree, select **Preset Studies for Selected Physics Interfaces>AC Impedance, Initial Values**.


**7** Click  **Done**.



## GLOBAL DEFINITIONS

### *Parameters I*

Load the model parameters from a text file.

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters I**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `impedance_spectroscopy_parameters.txt`.



## GEOMETRY I

Build the model geometry as a single interval of length  $L_{e1}$ . (The parameter was included in the list of parameters that was loaded from the text file.)

### *Interval I (il)*

- 1 In the **Model Builder** window, under **Component I (comp1)** right-click **Geometry I** and choose **Interval**.
- 2 In the **Settings** window for **Interval**, locate the **Interval** section.
- 3 In the table, enter the following settings:

Coordinates (m)
0
$L_{e1}$

- 4 Click  **Build All Objects**.
- 5 Click the  **Zoom Extents** button in the **Graphics** toolbar.

## ELECTROANALYSIS (TCD)

### *Electrolyte I*


Now set up the physics. Start with the diffusion coefficients for  $c_{Ox}$  and  $c_{Red}$ .

- 1 In the **Model Builder** window, under **Component I (comp1)>Electroanalysis (tcd)** click **Electrolyte I**.
- 2 In the **Settings** window for **Electrolyte**, locate the **Diffusion** section.
- 3 In the  $D_{cRed}$  text field, type  $D$ .
- 4 In the  $D_{cOx}$  text field, type  $D$ .

### *Initial Values I*


- 1 In the **Model Builder** window, click **Initial Values I**.
- 2 In the **Settings** window for **Initial Values**, locate the **Initial Values** section.
- 3 In the  $c_{\text{Red}}$  text field, type  $c_{\text{bulk}}$ .
- 4 In the  $c_{\text{Ox}}$  text field, type  $c_{\text{bulk}}$ .

### *Concentration I*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Concentration**.
- 2 Select Boundary 2 only.
- 3 In the **Settings** window for **Concentration**, locate the **Concentration** section.
- 4 Select the **Species cRed** check box.
- 5 In the  $c_{0,\text{cRed}}$  text field, type  $c_{\text{bulk}}$ .
- 6 Select the **Species cOx** check box.
- 7 In the  $c_{0,\text{cOx}}$  text field, type  $c_{\text{bulk}}$ .

Add an Electrode Surface boundary node and specify the voltage perturbation, the electrode reaction, and the double layer capacitance.

### *Electrode Surface I*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Electrode Surface**.
- 2 Select Boundary 1 only.
- 3 In the **Settings** window for **Electrode Surface**, click to expand the **Harmonic Perturbation** section.
- 4 In the  $\Delta\phi_{\text{s,ext}}$  text field, type  $V_{\text{app}}$ .

### *Electrode Reaction I*

- 1 In the **Model Builder** window, click **Electrode Reaction I**.
- 2 In the **Settings** window for **Electrode Reaction**, locate the **Stoichiometric Coefficients** section.
- 3 In the  $v_{\text{cRed}}$  text field, type 1.
- 4 In the  $v_{\text{cOx}}$  text field, type -1.
- 5 Locate the **Electrode Kinetics** section. In the  $i_{0,\text{ref}}(T)$  text field, type  $i_{0\text{ref}}$ .

### *Electrode Surface I*

In the **Model Builder** window, click **Electrode Surface I**.

### *Double Layer Capacitance I*

- 1 In the **Physics** toolbar, click  **Attributes** and choose **Double Layer Capacitance**.

- 2 In the **Settings** window for **Double Layer Capacitance**, locate the **Double Layer Capacitance** section.
- 3 In the  $C_{dl}$  text field, type Cd1.

### MESH I

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.
- 2 In the **Settings** window for **Mesh**, locate the **Physics-Controlled Mesh** section.
- 3 From the **Element size** list, choose **Extremely fine**.

Modify the default mesh by specifying the maximum element size on the electrode surface as a multiple of the shortest diffusion length (highest frequency).

#### Size

Right-click **Component 1 (comp1)>Mesh 1** and choose **Edit Physics-Induced Sequence**.



#### Size 1

- 1 Select Boundary 1 only.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 Click the **Custom** button.
- 4 Locate the **Element Size Parameters** section.
- 5 Select the **Maximum element size** check box. In the associated text field, type  $x_{diff\_min}/25$ .

### STUDY I

The model is now ready for solving. Add a parametric sweep to study the effect when varying the k0 parameter value for a range of frequencies.


#### Parametric Sweep

- 1 In the **Study** toolbar, click  **Parametric Sweep**.
- 2 In the **Settings** window for **Parametric Sweep**, locate the **Study Settings** section.
- 3 Click  **Add**.
- 4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
k0 (Heterogeneous rate constant)	$10^{\text{range}(-1, -1, -3)}$	cm/s

#### Step 1: Frequency Domain Perturbation



- 1 In the **Model Builder** window, click **Step 1: Frequency Domain Perturbation**.

- 2 In the **Settings** window for **Frequency Domain Perturbation**, locate the **Study Settings** section.
- 3 In the **Frequencies** text field, type `10^range(log_freq_min,0.05,log_freq_max)`.
- 4 In the **Study** toolbar, click  **Compute**.

## RESULTS

### *Impedance with Respect to Ground, Nyquist (tcd)*

A Nyquist plot, and plots of the real and imaginary parts of the impedance, are created by default.

- 1 In the **Settings** window for **ID Plot Group**, locate the **Legend** section.
- 2 From the **Position** list, choose **Lower right**.
- 3 In the **Impedance with Respect to Ground, Nyquist (tcd)** toolbar, click  **Plot**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.

### *Impedance with Respect to Ground, Real Part (tcd)*

Create plots of the magnitude (absolute value) and the phase angle as follows:

#### *Impedance with Respect to Ground, Absolute Value*

- 1 In the **Model Builder** window, right-click **Impedance with Respect to Ground, Real Part (tcd)** and choose **Duplicate**.
- 2 In the **Settings** window for **ID Plot Group**, type **Impedance with Respect to Ground, Absolute Value** in the **Label** text field.

#### *Global I*

- 1 In the **Model Builder** window, expand the **Impedance with Respect to Ground, Absolute Value** node, then click **Global I**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:

Expression	Unit	Description
<code>abs(conj(tcd.Zvsgrnd_es1))</code>	$\Omega \cdot \text{m}^2$	Impedance with Respect to Ground, Absolute Value

- 4 In the **Impedance with Respect to Ground, Absolute Value** toolbar, click  **Plot**.

### *Impedance with Respect to Ground, Phase Angle*

- 1 In the **Model Builder** window, right-click **Impedance with Respect to Ground, Absolute Value** and choose **Duplicate**.

- 2 In the **Settings** window for **ID Plot Group**, type Impedance with Respect to Ground, Phase Angle in the **Label** text field.

*Global I*

- 1 In the **Model Builder** window, expand the **Impedance with Respect to Ground, Phase Angle** node, then click **Global I**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:

Expression	Unit	Description
<code>arg(tcd.Zvsgrnd_es1)</code>	rad	Impedance with Respect to Ground, Phase Angle

- 4 In the **Impedance with Respect to Ground, Phase Angle** toolbar, click  **Plot**.

