

# Stresses and Heat Generation in Landing Gear

This model simulates the dynamics of the shock absorber used in a landing gear mechanism using the Multibody Dynamics interface present in COMSOL Multiphysics. It analyzes the stresses in the landing gear components and the energy dissipated in the absorber during the landing of an aircraft. The heat transfer analysis is also performed, in which the rise of temperature in the components due to heat generated in the shock absorber is calculated by coupling the Multibody Dynamics interface with the Heat Transfer in Solids interface.

# Model Definition

The landing gear assembly, shown in Figure 1, consists of two tires, a shock-absorber piston, and a shock-absorber cylinder. Other components in the landing gear, which are not relevant in this analysis, are not modeled.

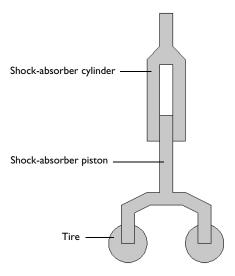


Figure 1: Geometry of the landing gear.

The shock-absorber piston and cylinder are connected through a prismatic joint that has only one translational degree of freedom. The joint is loaded with a spring and a damper to absorb the shock during the landing. This is modeled using the spring and damper subnode of the prismatic joint.

To model the effect of the tires, the bottom surfaces of the shock-absorber piston are loaded with equivalent spring and damper. The energy dissipated in the damper is used as a heat source on the common boundaries of the shock-absorber piston and cylinder. Remaining boundaries are considered to be insulated. The heat generated on the boundaries is conducted into the landing gear components during the landing, which increases their temperature.

# Results and Discussion

Figure 2 displays the stress generated in the landing gear components at the time when the displacement reaches its maximum.

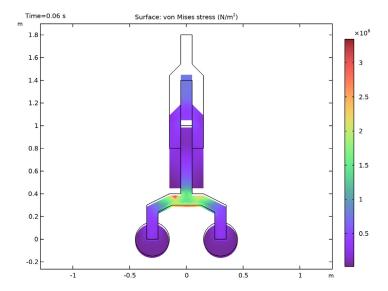


Figure 2: von Mises stress distribution in the deformed landing gear.

Figure 3 shows the relative displacement between the shock-absorber piston and cylinder during landing. The amplitude of the relative displacement is very high initially, but it decays rapidly due to the energy loss in the shock absorber and tires.

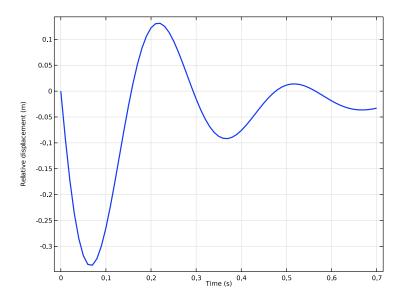


Figure 3: Relative displacement between the shock-absorber piston and cylinder.

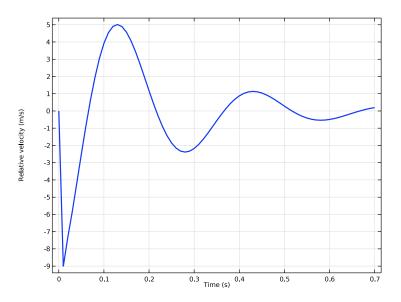


Figure 4: Relative velocity between the shock-absorber piston and cylinder.

Figure 4 shows the relative velocity variation between the shock-absorber piston and cylinder during landing. The relative velocity is also very high initially, and it decays to zero due to the energy loss in the shock absorber and tires during the course of the landing.

The force component in y direction in the prismatic joint is shown in Figure 5. The force also decays with time and subsequently acquires a steady state value equivalent to the weight of the whole supported system.

Figure 6 shows the variation in the energy components during the landing. Initially, the kinetic energy is very high. But due to the dissipation in the subsequent cycles, it decays to zero. The other forms of energies, such as strain energy and potential energy, are very small as compared to the kinetic energy. This happens because most of the kinetic energy is stored in the shock absorber initially and then dissipated before getting converted to any other forms of energy.

The temperature rise in the components due to heat dissipated in shock-absorber is shown in Figure 7. The maximum temperature rise occurs near the piston-cylinder boundaries.

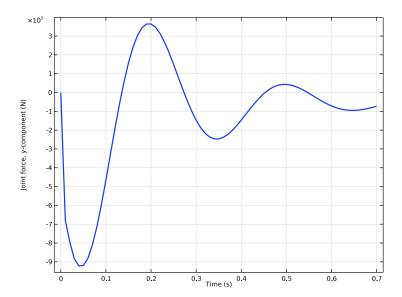


Figure 5: The y component of force in the shock-absorber.

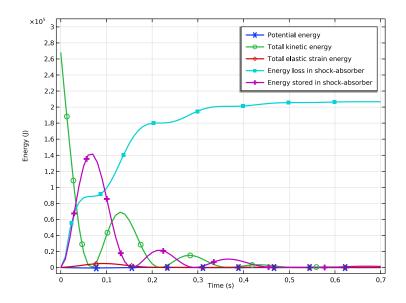


Figure 6: Variation of different types of energy in the gear during landing.

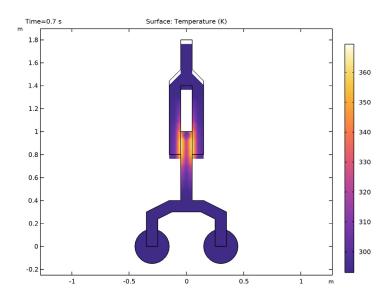


Figure 7: Temperature profile in the landing gear.

# Application Library path: Multibody Dynamics Module/

Automotive\_and\_Aerospace/landing\_gear

# Modeling Instructions

From the File menu, choose New.

#### NEW

In the New window, click Model Wizard.

## MODEL WIZARD

- I In the Model Wizard window, click 9 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Multibody Dynamics (mbd).
- 3 Click Add.
- 4 In the Select Physics tree, select Heat Transfer>Heat Transfer in Solids (ht).
- 5 Click Add.
- 6 Click Study.
- 7 In the Select Study tree, select General Studies>Time Dependent.
- 8 Click **Done**.

## **GLOBAL DEFINITIONS**

## Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
m	5000[kg]	5000 kg	Mass of the aircraft
vi	10[m/s]	10 m/s	Downward velocity of the aircraft
k_sa	2.5e6[N/m]	2.5E6 N/m	Spring constant of shock absorber
c_sa	5e4[N*s/m]	50000 N·s/m	Damping coefficient of shock absorber

Name	Expression	Value	Description
k_t	2.5e7[N/m]	2.5E7 N/m	Stiffness of tire
c_t	2.5e6[N*s/m]	2.5E6 N·s/m	Damping coefficient of tire
d	0.1[m]	0.1 m	Out of plane dimension

If you do not want to build all the geometry, you can load the geometry sequence from the stored model. In the Model Builder window, under Component I (comp I) right-click Geometry I and choose Insert Sequence. Browse to the model's Application Libraries folder and double-click the file landing gear.mph. You can then continue to the Add Material section below.

To build the geometry from scratch, continue here.

#### GEOMETRY I

Circle I (c1)

- I In the Geometry toolbar, click Circle.
- 2 In the Settings window for Circle, locate the Size and Shape section.
- 3 In the Radius text field, type 0.15.
- 4 Locate the **Position** section. In the **x** text field, type -0.3.

Polygon I (poll)

- I In the **Geometry** toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.
- 4 In the x text field, type -0.35 -0.35 -0.35 -0.15 -0.15 -0.05 -0.05 -0.05 -0.05 0 0 0 0 -0.15+0.1\*(sqrt(5)-2) -0.15+0.1\*(sqrt(5)-2) -0.25 -0.25 -0.25.
- 5 In the y text field, type 0 0.3 0.3 0.4 0.4 0.4 0.4 1 1 1 1 0.3 0.3 0.3 0.3 0.3-0.05\*(sqrt(5)-1) 0.3-0.05\*(sqrt(5)-1) 0.

Polygon 2 (pol2)

- I In the Geometry toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.
- 4 In the x text field, type -0.15 -0.15 -0.15 -0.05 -0.05 -0.05 -0.05 0 0 0 -0.05 -0.05 -0.05.

- 5 In the y text field, type 0.8 1.3+0.1\*sqrt(2) 1.3+0.1\*sqrt(2) 1.4+0.1\*sqrt(2) 1.4+0.1\*sqrt(2) 1.8 1.8 1.8 1.8 1.4 1.4 1.4 0.8.
- 6 Click Pauld Selected.
- 7 Click the **Zoom Extents** button in the **Graphics** toolbar.

Copy I (copy I)

- I In the Geometry toolbar, click Transforms and choose Copy.
- **2** Select the object **poll** only.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- 2 Select the object cl only.
- 3 In the Settings window for Difference, locate the Difference section.
- 4 Click to select the Activate Selection toggle button for Objects to subtract.
- **5** Select the object **copy1** only.

Mirror I (mirl)

- I In the Geometry toolbar, click \( \sum\_{i} \) Transforms and choose Mirror.
- 2 Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 3 In the Settings window for Mirror, locate the Input section.
- 4 Select the **Keep input objects** check box.

Union I (uni I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects mirl(2) and poll only.
- 3 In the Settings window for Union, locate the Union section.
- 4 Clear the Keep interior boundaries check box.

Union 2 (uni2)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects mir1(3) and pol2 only.
- 3 In the Settings window for Union, locate the Union section.
- 4 Clear the **Keep interior boundaries** check box.

Union 3 (uni3)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects difl, mirl(1), and unil only.

## Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Click | Build Selected.
- 5 Click the Go to Default View button in the Graphics toolbar.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

#### ADD MATERIAL

- I In the Home toolbar, click Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Structural steel.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click **‡** Add Material to close the Add Material window.

## MULTIBODY DYNAMICS (MBD)

- I In the Model Builder window, under Component I (compl) click Multibody Dynamics (mbd).
- 2 In the Settings window for Multibody Dynamics, locate the Thickness section.
- **3** In the d text field, type d.

## Initial Values 1

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd) click Initial Values 1.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- 3 From the list, choose Locally defined.
- **4** Specify the du/dt vector as
- **5** In the table, enter the following settings:



## Attachment I

- I In the Physics toolbar, click Boundaries and choose Attachment.
- **2** Select Boundaries 34 and 40 only.

- 3 In the Settings window for Attachment, locate the Connection Type section.
- 4 From the list, choose Flexible.

#### Attachment 2

- I In the Physics toolbar, click Boundaries and choose Attachment.
- 2 Select Boundaries 10 and 14 only.
- 3 In the Settings window for Attachment, locate the Connection Type section.
- 4 From the list, choose Flexible.

# Prismatic Joint 1

- I In the Physics toolbar, click A Global and choose Prismatic Joint.
- 2 In the Settings window for Prismatic Joint, locate the Attachment Selection section.
- 3 From the Source list, choose Attachment 1.
- 4 From the Destination list, choose Attachment 2.
- **5** Locate the **Axis of Joint** section. Specify the  $e_0$  vector as

0	x
- 1	у

# Spring and Damper 1

- I In the Physics toolbar, click Rattributes and choose Spring and Damper.
- 2 In the Settings window for Spring and Damper, locate the Spring and Damper: Translational section.
- **3** In the  $k_{\rm u}$  text field, type k\_sa.
- **4** In the  $c_{\rm u}$  text field, type c\_sa.

Use the **Added Mass** node to account for the mass of the aircraft.

#### Added Mass 1

- I In the Physics toolbar, click Boundaries and choose Added Mass.
- **2** Select Boundaries 37 and 39 only.
- 3 In the Settings window for Added Mass, locate the Added Mass section.
- 4 From the Mass type list, choose Total mass.
- 5 From the list, choose Diagonal.

**6** In the **m** table, enter the following settings:

0	0
0	m

# Gravity I

In the Physics toolbar, click A Global and choose Gravity.

The Spring Foundation node is used to account for the elastic and damping effects of the tires.

# Spring Foundation I

- I In the Physics toolbar, click Boundaries and choose Spring Foundation.
- 2 Select Boundaries 2 and 19 only.
- 3 In the Settings window for Spring Foundation, locate the Spring section.
- 4 From the Spring type list, choose Total spring constant.
- 5 From the list, choose Diagonal.
- **6** In the  $\mathbf{k}_{\text{tot}}$  table, enter the following settings:



- 7 Click to expand the Viscous Damping section. From the Damping type list, choose Total damping constant.
- 8 From the list, choose Diagonal.
- **9** In the  $\mathbf{d}_{tot}$  table, enter the following settings:



## DEFINITIONS

Integration I (intopl)

- I In the Definitions toolbar, click / Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, locate the Source Selection section.
- 3 From the Selection list, choose All domains.

## Variables 1

I In the **Definitions** toolbar, click **a= Local Variables**.

The heat generated due to the energy dissipation in the absorber is modeled as a heat source. This heat source is distributed on the common boundaries of the shockabsorber piston and cylinder.

- 2 In the Settings window for Variables, locate the Variables section.
- 3 In the table, enter the following settings:

Name	Expression	Unit	Description
Q	mbd.prj1.Qdamper	W	Heat generated per second
Wp	<pre>intop1(mbd.rho*g_const* v*mbd.d)</pre>	J	Potential energy
h_sa	<pre>timeint(0,t,Q)</pre>	J	Energy loss in shock- absorber
Ws_sa	mbd.prj1.Wspring	J	Energy stored in shock- absorber

## **HEAT TRANSFER IN SOLIDS (HT)**

- I In the Model Builder window, under Component I (compl) click Heat Transfer in Solids (ht).
- 2 In the Settings window for Heat Transfer in Solids, locate the Physical Model section.
- **3** In the  $d_z$  text field, type d.

# Boundary Heat Source I

- I In the Physics toolbar, click Pairs and choose Boundary Heat Source.
- 2 In the Settings window for Boundary Heat Source, locate the Pair Selection section.
- 3 Under Pairs, click Add.
- 4 In the Add dialog box, select Identity Boundary Pair I (ap I) in the Pairs list.
- 5 Click OK.
- 6 In the Settings window for Boundary Heat Source, locate the Boundary Heat Source section.
- 7 From the Heat source list, choose Heat rate.
- **8** In the  $P_{\rm b}$  text field, type Q.

## MESH I

I In the Model Builder window, under Component I (compl) click Mesh I.

- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Finer**.
- 4 Click III Build All.

#### STUDY I

## Step 1: Time Dependent

- I In the Model Builder window, under Study I click Step I: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0,0.01,0.7).
- 4 In the Home toolbar, click **Compute**.

#### RESULTS

Follow these instructions to generate a plot similar to the one shown in Figure 2:

## Stress

- I In the Model Builder window, under Results click Displacement (mbd).
- 2 In the Settings window for 2D Plot Group, type Stress in the Label text field.
- 3 Locate the Plot Settings section. From the Frame list, choose Material (X, Y, Z).
- 4 Locate the Data section. From the Time (s) list, choose 0.06.

#### Surface

- I In the Model Builder window, expand the Stress node, then click Surface.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Multibody Dynamics>Stress>mbd.misesGp - von Mises stress - N/m2.
- 3 Click to expand the Quality section. From the Resolution list, choose No refinement.
- 4 In the Stress toolbar, click Plot.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Follow these instructions to generate a plot similar to the one shown in Figure 7:

## Surface I

- I In the Model Builder window, expand the Results>Temperature (ht) node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Quality section.
- 3 From the Resolution list, choose No refinement.

## Deformation I

- I Right-click Surface I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Scale section.
- **3** Select the **Scale factor** check box. In the associated text field, type 1.
- 4 In the Temperature (ht) toolbar, click Plot.

Follow these instructions to generate a relative displacement plot similar to the one shown in Figure 3:

## Relative Displacement

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Relative Displacement in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **None**.

#### Global I

- I Right-click Relative Displacement and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Prismatic joints>Prismatic Joint I>mbd.prjI.u -Relative displacement - m.
- 3 Click to expand the **Legends** section. Clear the **Show legends** check box.
- 4 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 5 In the Relative Displacement toolbar, click **Plot**.

## Relative Displacement

Follow these instructions to generate a relative velocity plot similar to the one shown in Figure 4:

I In the Model Builder window, right-click Relative Displacement and choose Duplicate.

## Relative Velocity

- I In the Model Builder window, under Results click Relative Displacement I.
- 2 In the Settings window for ID Plot Group, type Relative Velocity in the Label text field.

## Global I

I In the Model Builder window, expand the Relative Velocity node, then click Global I.

- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Prismatic joints>Prismatic Joint I>mbd.prj I.u\_t - Relative velocity m/s.
- 3 In the Relative Velocity toolbar, click Plot.

## Relative Velocity

Follow these instructions to generate a joint force plot similar to the one shown in Figure 5:

I In the Model Builder window, right-click Relative Velocity and choose Duplicate.

## Joint Force

- I In the Model Builder window, under Results click Relative Velocity I.
- 2 In the Settings window for ID Plot Group, type Joint Force in the Label text field.

#### Global I

- I In the Model Builder window, expand the Joint Force node, then click Global I.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Prismatic joints>Prismatic Joint 1>Joint force - N>mbd.prj1.Fy -Joint force, y-component.
- 3 In the **Joint Force** toolbar, click **Plot**.

To generate the energy plot shown in Figure 6, follow the instructions below.

#### Energy

- I In the Home toolbar, click <a> Add Plot Group</a> and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Energy in the Label text field.
- 3 Locate the Title section. From the Title type list, choose None.

#### Global I

- I Right-click Energy and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Definitions> Variables>Wp - Potential energy - J.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Global>mbd.Wk tot -Total kinetic energy - J.

- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Global>mbd.Ws\_tot Total elastic strain energy J.
- 5 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Definitions>Variables>h\_sa Energy loss in shockabsorber I.
- 6 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Definitions>Variables>Ws\_sa Energy stored in shock-absorber J.
- 7 Locate the Coloring and Style section. From the Width list, choose 2.
- 8 Find the Line markers subsection. From the Marker list, choose Cycle.
- **9** From the **Positioning** list, choose **Interpolated**.
- 10 In the Energy toolbar, click Plot.

## Energy

- I In the Model Builder window, click Energy.
- 2 In the Settings window for ID Plot Group, locate the Plot Settings section.
- 3 Select the y-axis label check box. In the associated text field, type Energy (J).
- 4 Locate the Axis section. Select the Manual axis limits check box.
- 5 In the y maximum text field, type 3.1e5.
- 6 In the Energy toolbar, click  **Plot**.

Use the instructions below to generate an animation of the stress distribution in the landing gear components.

## Animation I

- I In the Results toolbar, click Animation and choose File.
- 2 In the Settings window for Animation, locate the Target section.
- 3 From the Target list, choose Player.
- 4 Locate the Frames section. In the Number of frames text field, type 100.

Finally, follow these instructions to generate an animation of the temperature distribution in the components.

## Animation 2

- I In the **Results** toolbar, click **Animation** and choose **File**.
- 2 In the Settings window for Animation, locate the Target section.

- 3 From the Target list, choose Player.
- 4 Locate the Scene section. From the Subject list, choose Temperature (ht).
- 5 Locate the Frames section. In the Number of frames text field, type 100.