

Flow Through a Uniform Inclined Screen

This example simulates the flow through a uniform inclined screen using the Screen feature in Single-Phase Flow physics and compares the results with an analytic solution due to Elder (Ref. 1). The Screen feature is a tool for modeling wire gauzes, perforated plates etc without resolving their geometric complexity (see the CFD Module User's Guide for further details).

Model Definition

The model geometry is shown in Figure 1.

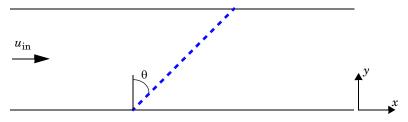


Figure 1: Model geometry showing flow direction and screen inclination.

Air at a temperature of T = 20 °C enters the channel on the left with a uniform inlet velocity of $u_{in} = 1$ m/s and exits on the right at uniform pressure, $p_0 = 0$ Pa. The flow through the channel is obstructed by a screen inclined at an angle θ . The combined effect of resistance and refraction (suppression of the tangential velocity component) creates a nonuniform velocity profile on the downstream side of the screen. An asymptotic solution valid for small inclinations is (Ref. 1),

$$\frac{(u/u_{\rm in} - 1)(1 + \eta + K\cos^2\theta)}{(1 - \eta)\tan\theta \cdot K\cos^2\theta} = \frac{2}{\pi}\log\left(\cot\left(\frac{\pi y}{2}\right)\right) \tag{1}$$

where K and η are the screen resistance and refraction coefficients. To facilitate comparison with the asymptotic solution, we assume that the flow is incompressible and apply free-slip boundary conditions on the channel walls. Then, we choose the userdefined option for both the screen type and refraction in order to set the resistance coefficient K to 2.2 and the refraction coefficient η to 0.78.

Results and Discussion

The study performs a Parametric Sweep with the angle θ taking the values,

$$\theta = \frac{\pi}{18}, \frac{\pi}{9}, \frac{\pi}{6}, \frac{2\pi}{9}, \frac{\pi}{4} \qquad (\theta = 10^{\circ}, 20^{\circ}, 30^{\circ}, 40^{\circ}, 45^{\circ})$$

Figure 2 shows the outlet velocity scaled according to the left-hand side of Equation 1 together with the asymptotic solution on the right-hand side.

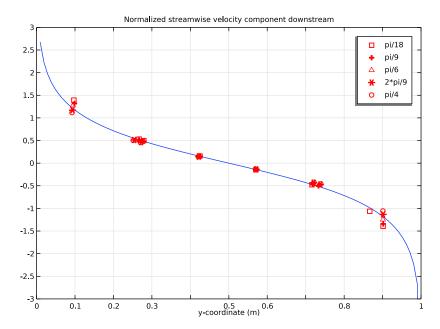


Figure 2: Comparison between the asymptotic solution (blue) and the simulations (red).

The agreement between the asymptotic solution and the simulations is good, surprisingly so even for $\theta = \pi/4$ (45°). Figure 3 shows a surface plot of the pressure field together with velocity vectors on the upstream and downstream side of the screen. The velocity vectors are displaced from the screen for clarity. You can easily distinguish the induced pressure jump, the flow distribution and deflection. See Ref. 1 for asymptotic solutions to other

related screen-flow problems if you are looking to extend the analysis to screens of varying shape and/or resistance.

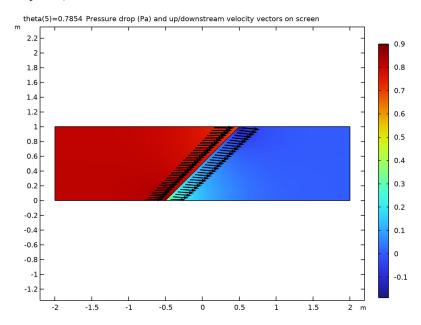


Figure 3: Pressure drop, flow distribution and deflection for a screen inclined at an angle of 45° to the incoming flow.

Notes About the COMSOL Implementation

The model uses the Screen feature together with a Parametric Sweep to vary the inclination angle of the screen.

Reference

1. J.W. Elder, "Steady Flow Through Non-Uniform Gauzes of Arbitrary Shape," J. Fluid Mech., vol 5, pp 355-363, 1959.

Application Library path: CFD_Module/Verification_Examples/inclined_screen

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Fluid Flow>Single-Phase Flow>Laminar Flow (spf).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
theta	pi/18	0.17453	Angle of inclination
u_in	1[m/s]	I m/s	Inlet velocity

GEOMETRY I

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 4.
- 4 Locate the **Position** section. In the x text field, type -2.

Polygon I (boll)

- I In the Geometry toolbar, click / Polygon.
- 2 In the Settings window for Polygon, locate the Coordinates section.
- 3 From the Data source list, choose Vectors.

- 4 In the x text field, type -0.5*tan(theta) 0.5*tan(theta).
- 5 In the y text field, type 0 1.
- 6 In the Geometry toolbar, click **Build All**.

ADD MATERIAL

- I In the Home toolbar, click **Add Material** to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Air.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click **‡ Add Material** to close the **Add Material** window.

LAMINAR FLOW (SPF)

Wall I

- I In the Model Builder window, under Component I (compl)>Laminar Flow (spf) click Wall I.
- 2 In the Settings window for Wall, locate the Boundary Condition section.
- 3 From the Wall condition list, choose Slip.

Inlet I

- I In the Physics toolbar, click Boundaries and choose Inlet.
- 2 Select Boundary 1 only.
- 3 In the Settings window for Inlet, locate the Velocity section.
- **4** In the U_0 text field, type u_in.

Outlet I

- I In the Physics toolbar, click Boundaries and choose Outlet.
- **2** Select Boundary 7 only.
- 3 In the Settings window for Outlet, locate the Pressure Conditions section.
- 4 Select the Normal flow check box.

Screen I

- I In the Physics toolbar, click Boundaries and choose Screen.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Screen, locate the Screen Type section.

- 4 From the Screen type list, choose User defined. Locate the Parameters section. In the Ktext field, type 2.2.
- **5** From the **Refraction** list, choose **User defined**. In the η text field, type 0.78.

STUDY I

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
theta (Angle of inclination)	pi/18, pi/9, pi/6, 2* pi/9, pi/4	

5 In the Study toolbar, click **Compute**.

RESULTS

Create a new plot group to reproduce Figure 2.

ID Plot Group 3

In the Home toolbar, click Add Plot Group and choose ID Plot Group.

Line Graph 1

- I Right-click ID Plot Group 3 and choose Line Graph.
- **2** Select Boundary 7 only.

Type in the analytic solution.

- 3 In the Settings window for Line Graph, locate the y-Axis Data section.
- 4 In the Expression text field, type 2/pi*log(cot(pi*y/2)).
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 6 In the Expression text field, type y.
- 7 In the ID Plot Group 3 toolbar, click Plot.

ID Plot Group 3

- I In the Model Builder window, click ID Plot Group 3.
- 2 In the Settings window for ID Plot Group, locate the Axis section.
- 3 Select the Manual axis limits check box.

- 4 In the x minimum text field, type 0.
- 5 In the x maximum text field, type 1.
- **6** In the **y minimum** text field, type -3.
- 7 In the y maximum text field, type 3.

Line Grabh I

In the Model Builder window, right-click Line Graph I and choose Duplicate.

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study I/Parametric Solutions I (sol2).
- 4 From the Parameter selection (theta) list, choose From list.
- 5 In the Parameter values (theta) list, select 0.17453. Scale the solutions for comparison with the analytic solution.
- 6 Locate the y-Axis Data section. In the Expression text field, type (u/u in-1)/(1-0.78)/2.2/cos(theta)^2*(1+0.78+2.2*cos(theta)^2)/tan(theta).
- 7 Click to expand the Coloring and Style section. Find the Line style subsection. From the Line list, choose None.
- 8 From the Color list, choose Red.
- 9 Find the Line markers subsection. From the Marker list, choose Square.
- 10 From the Positioning list, choose Interpolated.
- II Click to expand the **Legends** section. Select the **Show legends** check box.
- 12 From the Legends list, choose Manual.
- **I3** In the table, enter the following settings:

Legends pi/18

14 Right-click Line Graph 2 and choose Duplicate.

Line Graph 3

- I In the Model Builder window, click Line Graph 3.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Parameter values (theta) list, select 0.34907.

- 4 Locate the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Plus sign.
- 5 From the Positioning list, choose Interpolated.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends pi/9

7 Right-click Line Graph 3 and choose Duplicate.

Line Graph 4

- I In the Model Builder window, click Line Graph 4.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Parameter values (theta) list, select 0.5236.
- 4 Locate the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Triangle.
- 5 From the Positioning list, choose Interpolated.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends pi/6

7 Right-click Line Graph 4 and choose Duplicate.

Line Graph 5

- I In the Model Builder window, click Line Graph 5.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Parameter values (theta) list, select 0.69813.
- 4 Locate the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Asterisk.
- 5 From the Positioning list, choose Interpolated.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends 2*pi/9

7 Right-click Line Graph 5 and choose Duplicate.

Line Graph 6

- I In the Model Builder window, click Line Graph 6.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 In the Parameter values (theta) list, select 0.7854.
- 4 Locate the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Circle.
- **5** From the **Positioning** list, choose **Interpolated**.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends pi/4

ID Plot Group 3

- I In the Model Builder window, click ID Plot Group 3.
- 2 In the Settings window for ID Plot Group, click to expand the Title section.
- **3** From the **Title type** list, choose **Manual**.
- 4 In the ID Plot Group 3 toolbar, click **Plot**.
- 5 In the Title text area, type Normalized streamwise velocity component downstream.

To generate Figure 3, continue with the steps below.

Surface

- I In the Model Builder window, expand the Results>Velocity (spf) node, then click Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type p.

Arrow Line 1

- I In the Model Builder window, right-click Velocity (spf) and choose Arrow Line.
- 2 In the Settings window for Arrow Line, locate the Expression section.
- 3 In the x-component text field, type up(u).
- 4 In the y-component text field, type up (v).
- 5 Locate the Coloring and Style section. From the Arrow base list, choose Head.
- 6 Select the Scale factor check box. In the associated text field, type 0.25.
- 7 Locate the Arrow Positioning section. In the Number of arrows text field, type 30.
- 8 Locate the Coloring and Style section. From the Color list, choose Black.

Selection 1

- I Right-click Arrow Line I and choose Selection.
- **2** Select Boundary 4 only.

Deformation I

- I In the Model Builder window, right-click Arrow Line I and choose Deformation.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x-component text field, type -0.05.
- **4** In the **y-component** text field, type **0**.
- **5** Locate the **Scale** section.
- 6 Select the Scale factor check box. In the associated text field, type 1.

Arrow Line 1

Right-click Arrow Line I and choose Duplicate.

Arrow Line 2

- I In the Model Builder window, click Arrow Line 2.
- 2 In the Settings window for Arrow Line, locate the Expression section.
- 3 In the x-component text field, type down(u).
- 4 In the y-component text field, type down(v).
- 5 Locate the Coloring and Style section. From the Arrow base list, choose Tail.

Deformation I

- I In the Model Builder window, expand the Arrow Line 2 node, then click Deformation I.
- 2 In the Settings window for Deformation, locate the Expression section.
- **3** In the **x-component** text field, type 0.05.

Velocity (spf)

- I In the Model Builder window, under Results click Velocity (spf).
- 2 In the Settings window for 2D Plot Group, click to expand the Title section.
- 3 From the Title type list, choose Manual.
- 4 In the Title text area, type Pressure drop (Pa) and up/downstream velocity vectors on screen.
- 5 In the **Velocity (spf)** toolbar, click **Plot**.