

Notch Filter Using a Split Ring Resonator

A split ring resonator (SRR) has a band-stop frequency response. In this example, a printed SRR on a dielectric substrate is coupled to a microstrip line. The entire circuit behaves as a notch (band-stop) filter, which can be used to block a specific signal frequency range.

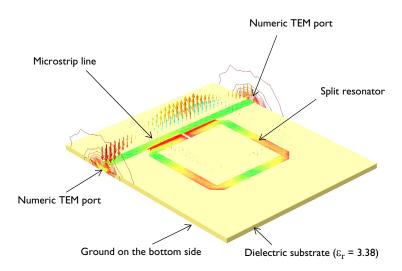


Figure 1: A split ring resonator coupled to a microstrip line.

Model Definition

Using the resonance characteristics of a split ring resonator, either a band-pass or bandstop filter can be realized on a microstrip line type structure. The band-pass or band-stop frequency response depends on the coupling configuration between a microstrip line and a split ring resonator.

In this example, to get a band-stop filter response, the split part of the resonator is adjacent and coupled to the straight microstrip line (Figure 1). On a ground plane, the printed split ring resonator, on a 1.524 mm thick dielectric ($\varepsilon_r = 3.38$) substrate, has multiple resonant modes. Although not included in this example, the resonant modes can be identified using an eigenfrequency analysis. Among those resonant modes, the frequency close to 2.4 GHz is of interest. The split ring resonator's frequency response is studied when it is coupled to the microstrip line.

All metal parts are modeled as perfect electric conductors (PEC). Scattering boundary conditions are assigned on all exterior boundaries of the simulation domain, except for the ground plane. The remaining part is characterized as a vacuum domain.

On the surfaces of each end of the microstrip line, including the air domain, a numeric port is added that calculates the electric mode field on the given structure, with an effective dielectric constant $\varepsilon_r = \operatorname{sqrt}(3.38)$. This is done through a Boundary Mode analysis. In the numeric port setting, "Analyzed as a TEM field" is selected. To compute the voltage and current of the port, this setting requires defined electric and magnetic field integration lines, respectively. The port characteristic impedance is calculated using the voltage and current extracted from these integration lines. The port mode field is scaled by the ratio of the calculated impedance and the reference impedance, defined in the settings window. The electric fields are guided between two conductors and the field component in the direction of propagation, the normal to the port boundary is negligible. Thus, it is reasonable to analyze the port mode as transverse electromagnetic (TEM) field.

Results and Discussion

The default electric field norm on the xy-plane is plotted in Figure 2. The electric fields are confined symmetrically along the split ring resonator at 2.4 GHz. Figure 3 shows the frequency response of the device. Around 2.4 GHz, its S_{11} is almost 0 dB, while its S_{21} is below -10 dB, so it behaves as band-stop (notch) filter.

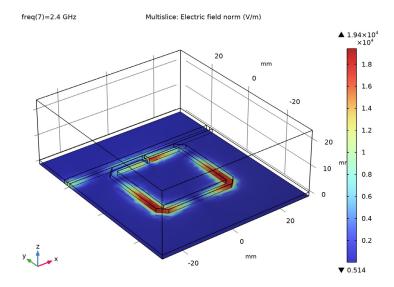


Figure 2: The electric field norm visualized on the xy-plane.

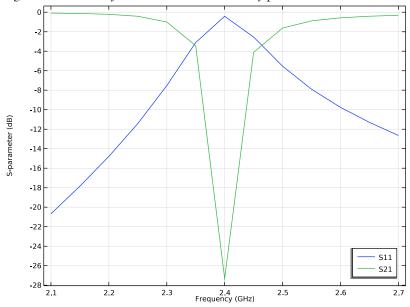


Figure 3: The S-parameter plot showing a band-stop frequency response.

Notes About the COMSOL Implementation

To learn more about how to define integration lines for calculating the voltage and the current of the numeric TEM port, review the following examples in the Application Libraries:

RF Module/Verification Models/coaxial cable impedance RF Module/Verification Models/parallel wires impedance

Application Library path: RF_Module/Filters/notch_filter_srr

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Radio Frequency>Electromagnetic Waves, Frequency Domain (emw).
- 3 Click Add.
- 4 Click M Done.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Boundary Mode Analysis.
- 4 Right-click and choose Add Study.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY I

Step 1: Boundary Mode Analysis

Define the study frequency ahead of performing any frequency-dependent operation such as building mesh. The physics-controlled mesh uses the highest frequency value in the specified range.

- I In the Settings window for Boundary Mode Analysis, locate the Study Settings section.
- 2 In the Mode analysis frequency text field, type 2.4[GHz].
- 3 Select the Search for modes around shift check box. In the associated text field, type sqrt(3.38).
- 4 Right-click Study I>Step I: Boundary Mode Analysis and choose Duplicate.

Step 3: Boundary Mode Analysis I

- I In the Model Builder window, right-click Step 3: Boundary Mode Analysis I and choose Move Up.
- 2 In the Settings window for Boundary Mode Analysis, locate the Study Settings section.
- 3 In the Port name text field, type 2.

Step 3: Frequency Domain

- I In the Model Builder window, click Step 3: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type range (2.1[GHz], 0.05[GHz], 2.7[GHz]).

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- **3** From the **Length unit** list, choose **mm**.

Work Plane I (wbl)

In the Geometry toolbar, click Work Plane.

Work Plane I (wp I)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wp I)>Rectangle I (r I)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 60.

- 4 In the Height text field, type 3.2.
- 5 Locate the Position section. From the Base list, choose Center.
- 6 In the yw text field, type 18.

Work Plane I (wp I)>Rectangle 2 (r2)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 60.
- 4 In the Height text field, type 70.
- 5 Locate the Position section. From the Base list, choose Center.
- 6 Click | Build Selected.
- 7 Click the **Zoom Extents** button in the **Graphics** toolbar.

Work Plane I (wp I)>Rectangle 3 (r3)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 32.
- 4 In the Height text field, type 32.
- **5** Locate the **Position** section. In the **xw** text field, type -16.
- 6 In the yw text field, type -15.7.

Work Plane I (wp I)>Rectangle 4 (r4)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 26.
- 4 In the Height text field, type 26.
- 5 Locate the **Position** section. In the xw text field, type -13.
- 6 In the yw text field, type -12.7.

Work Plane I (wb I)>Rectangle 5 (r5)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Height text field, type 6.
- 4 Locate the **Position** section. In the xw text field, type -0.5.
- 5 In the yw text field, type 12.

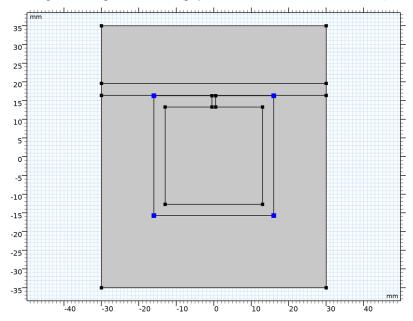
Work Plane I (wpl)>Difference I (difl)

- I In the Work Plane toolbar, click Booleans and Partitions and choose Difference.
- 2 Select the object **r3** only.
- 3 In the Settings window for Difference, locate the Difference section.
- 4 Click to select the **Activate Selection** toggle button for **Objects to subtract**.
- 5 Select the objects **r4** and **r5** only.

Work Plane I (wpl)>Chamfer I (chal)

- I In the Work Plane toolbar, click Chamfer.
- 2 In the Settings window for Chamfer, locate the Distance section.
- 3 In the Distance from vertex text field, type 3.
- **4** On the object **dif1**, select Points 1, 2, 11, and 12 only.

It might be easier to select the points by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)



Extrude I (ext I)

- I In the Model Builder window, right-click Geometry I and choose Extrude.
- 2 In the Settings window for Extrude, locate the Distances section.

3 In the table, enter the following settings:

Distances (mm) 1.524

- 4 Click Pauld Selected.
- 5 Click the Wireframe Rendering button in the Graphics toolbar.

Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 60.
- **4** In the **Depth** text field, type 70.
- 5 In the Height text field, type 25.
- 6 Locate the Position section. From the Base list, choose Center.
- 7 In the z text field, type 12.5.

Work Plane 2 (wp2)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose yz-plane.
- 4 In the x-coordinate text field, type -30.
- 5 Click A Go to Plane Geometry.

Work Plane 2 (wp2)>Polygon 1 (pol1)

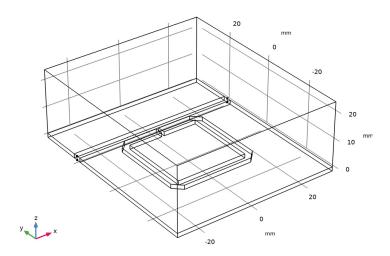
- I In the Work Plane toolbar, click / Polygon.
- 2 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 3 In the Settings window for Polygon, locate the Coordinates section.
- **4** In the table, enter the following settings:

xw (mm)	yw (mm)	
18	0	
18	1.524	

Mirror I (mirl)

- I Right-click Geometry I and choose Transforms>Mirror.
- 2 Select the object wp2 only.

- 3 In the Settings window for Mirror, locate the Input section.
- 4 Select the Keep input objects check box.
- 5 Locate the Normal Vector to Plane of Reflection section. In the x text field, type 1.
- 6 In the z text field, type 0.
- 7 Click **Build All Objects**.



ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

Perfect Electric Conductor 2

- I In the Model Builder window, under Component I (compl) right-click Electromagnetic Waves, Frequency Domain (emw) and choose the boundary condition Perfect Electric Conductor.
- 2 Select Boundaries 11 and 22 only.

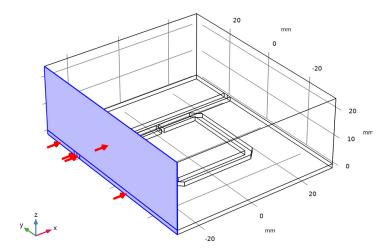
Scattering Boundary Condition 1

- I In the Physics toolbar, click **Boundaries** and choose Scattering Boundary Condition.
- **2** Select Boundaries 2, 5, 7, 17, and 18 only.

Port 1

I In the Physics toolbar, click **Boundaries** and choose Port.

2 Select Boundaries 1, 4, 8, 12, and 13 only.

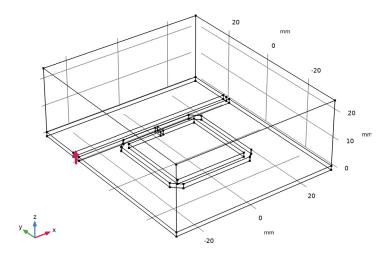


- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Numeric. For the first port, wave excitation is **on** by default.
- 5 Select the Analyze as a TEM field check box.

Integration Line for Voltage I

- I In the Physics toolbar, click 🕞 Attributes and choose Integration Line for Voltage.
- 2 In the Settings window for Integration Line for Voltage, locate the Edge Selection section.
- 3 Click Clear Selection.

4 Select Edge 14 only.



Port 2

- I In the Physics toolbar, click **Boundaries** and choose Port.
- 2 Select Boundaries 37–41 only.
- 3 In the Settings window for Port, locate the Port Properties section.
- 4 From the Type of port list, choose Numeric.
- 5 Select the Analyze as a TEM field check box.

Integration Line for Voltage I

- I In the Physics toolbar, click 🦳 Attributes and choose Integration Line for Voltage.
- 2 In the Settings window for Integration Line for Voltage, locate the Edge Selection section.
- 3 Click Clear Selection.
- **4** Select Edge 83 only.

MATERIALS

Material I (mat I)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	1	I	Basic
Relative permeability	mur_iso; murii = mur_iso, murij = 0	1	I	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

Material 2 (mat2)

- I Right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Geometric Entity Selection section.
- 3 Click Paste Selection.
- 4 In the Paste Selection dialog box, type 1, 3-5 in the Selection text field.
- 5 Click OK.
- 6 In the Settings window for Material, locate the Material Contents section.
- **7** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilonr_iso; epsilonrii = epsilonr_iso, epsilonrij = 0	3.38	I	Basic
Relative permeability	mur_iso; murii = mur_iso, murij = 0	1	I	Basic
Electrical conductivity	sigma_iso; sigmaii = sigma_iso, sigmaij = 0	0	S/m	Basic

MESH I

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click Component I (compl)>Mesh I and choose Build All.

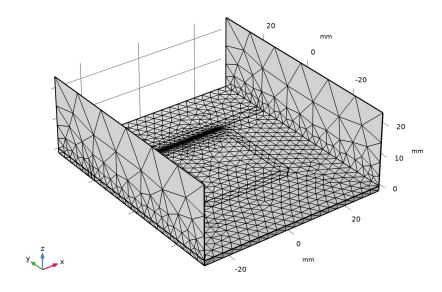
DEFINITIONS

Hide for Physics 1

- I In the Model Builder window, right-click View I and choose Hide for Physics.
- 2 In the Settings window for Hide for Physics, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select Boundaries 5, 7, and 18 only.

MESH I

- I Click the **Zoom Extents** button in the **Graphics** toolbar.
- 2 In the Model Builder window, under Component I (compl) click Mesh I.



STUDY I

Step 3: Frequency Domain

In the **Home** toolbar, click **Compute**.

RESULTS

Electric Field (emw)

- I In the Settings window for 3D Plot Group, locate the Data section.
- 2 From the Parameter value (freq (GHz)) list, choose 2.4.

Multislice

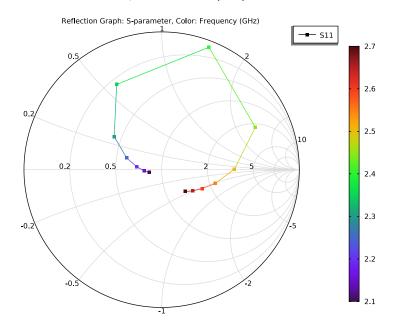
- I In the Model Builder window, expand the Electric Field (emw) node, then click Multislice.
- 2 In the Settings window for Multislice, locate the Multiplane Data section.
- 3 Find the X-planes subsection. In the Planes text field, type 0.
- 4 Find the Y-planes subsection. In the Planes text field, type 0.
- 5 Find the **Z-planes** subsection. From the **Entry method** list, choose **Coordinates**.
- 6 In the Coordinates text field, type 0.
- 7 In the Electric Field (emw) toolbar, click Plot. Reproduce Figure 2.

S-parameter (emw)

- I In the Model Builder window, under Results click S-parameter (emw).
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 From the Position list, choose Lower right.

Compare the reproduced plot with Figure 3.

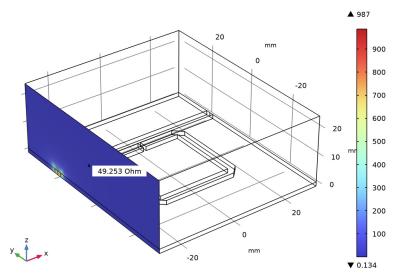
Smith Plot (emw) In the Model Builder window, click Smith Plot (emw).



Electric Mode Field, Port I (emw)

In the Model Builder window, click Electric Mode Field, Port I (emw).

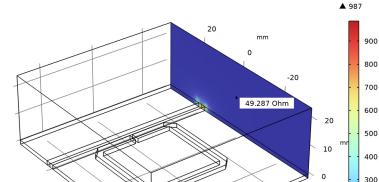




Electric Mode Field, Port 2 (emw)

freq(13)=2.7 GHz

In the Model Builder window, click Electric Mode Field, Port 2 (emw).



-20

Surface: Tangential boundary mode electric field norm (V/m)

Analyze the same model with a much finer frequency resolution using **Adaptive Frequency Sweep** based on asymptotic waveform evaluation (AWE). When a device presents a slowly varying frequency response, the AWE provides a faster solution time when running the simulation on many frequency points. The following example with the AWE can be computed 25 times faster than regular Frequency Domain sweeps with a same finer frequency resolution.

mm

200 100

▼ 0.133

ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

Port 1

- I In the Model Builder window, under Component I (compl)>Electromagnetic Waves, Frequency Domain (emw) click Port 1.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 Click **Create Selection**.
- 4 In the Create Selection dialog box, type Port 1 in the Selection name text field.
- 5 Click OK.

Port 2

- I In the Model Builder window, click Port 2.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 Click **\(\bigcup_{\text{a}} \) Create Selection.**
- 4 In the Create Selection dialog box, type Port 2 in the Selection name text field.
- 5 Click OK.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Empty Study.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY I

Step 1: Boundary Mode Analysis, Step 2: Boundary Mode Analysis I

- I In the Model Builder window, under Study I, Ctrl-click to select Step 1: Boundary Mode Analysis and Step 2: Boundary Mode Analysis 1.
- 2 Right-click and choose Copy.

STUDY 2

In the Model Builder window, right-click Study 2 and choose Paste Multiple Items.

Step 3: Adaptive Frequency Sweep

- I In the Study toolbar, click Study Steps and choose Frequency Domain> Adaptive Frequency Sweep.
- 2 In the Settings window for Adaptive Frequency Sweep, locate the Study Settings section.
- 3 In the Frequencies text field, type range (2.1[GHz], 1[MHz], 2.7[GHz]). Use a 50 times finer frequency resolution.
- 4 From the AWE expression type list, choose User controlled.

5 In the table, enter the following settings:

Asymptotic waveform evaluation (AWE) expressions abs(comp1.emw.S11)

A slowly varying scalar value curve works well for AWE expressions. For two-port bandstop-type devices, use abs(comp1.emw.S11).

Because such a fine frequency step generates a memory-intensive solution, the model file size will increase tremendously when it is saved. When only the frequency response of port related variables are of interest, it is not necessary to store all of the field solutions. By selecting the Store in Output check box in the Values of Dependent Variables section, we can control the part of the model on which the computed solution is saved. We only add the selection containing these boundaries where the port variables are calculated. The port size is relatively small compared to the entire modeling domain, and the saved file size with the fine frequency step is more or less that of the regular discrete frequency sweep model when only the solutions on the port boundaries are stored.

6 Click to expand the **Store in Output** section. In the table, enter the following settings:

Interface	Output
Electromagnetic Waves, Frequency Domain (emw)	Selection

- **7** Click to select row number 1 in the table.
- 8 Under Selections, click Add.
- 9 In the Add dialog box, in the Selections list, choose Port I and Port 2.
- 10 Click OK.

It is necessary to include the port boundaries to calculate S-parameters. By choosing only the port boundaries for **Store in Output** settings, it is possible to reduce the size of a model file a lot.

II In the **Study** toolbar, click **Compute**.

RESULTS

Multislice

- I In the Model Builder window, expand the Electric Field (emw) I node.
- 2 Right-click Multislice and choose Delete.

Surface 1

I In the Model Builder window, right-click Electric Field (emw) I and choose Surface.

2 In the Electric Field (emw) I toolbar, click Plot.

Selection 1

- I In the Model Builder window, right-click Surface I and choose Selection.
- 2 In the Settings window for Selection, locate the Selection section.
- 3 From the Selection list, choose Port 1.
- 4 In the Electric Field (emw) I toolbar, click Plot.

S-parameter (emw) I

- I In the Model Builder window, under Results click S-parameter (emw) I.
- 2 In the Settings window for ID Plot Group, locate the Legend section.
- 3 From the Position list, choose Lower right.

Global I

- I In the Model Builder window, expand the S-parameter (emw) I node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

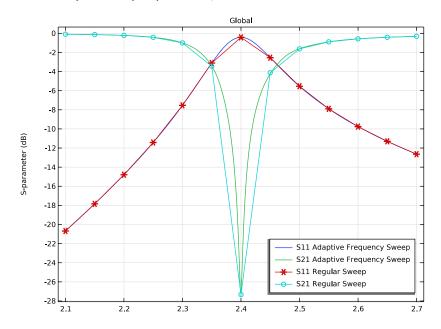
Expression	Unit	Description
emw.S11dB	1	S11 Adaptive Frequency Sweep
emw.S21dB	1	S21 Adaptive Frequency Sweep

Global 2

- I In the Model Builder window, right-click S-parameter (emw) I and choose Global.
- 2 In the Settings window for Global, locate the Data section.
- 3 From the Dataset list, choose Study I/Solution I (soll).
- 4 Locate the y-Axis Data section. In the table, enter the following settings:

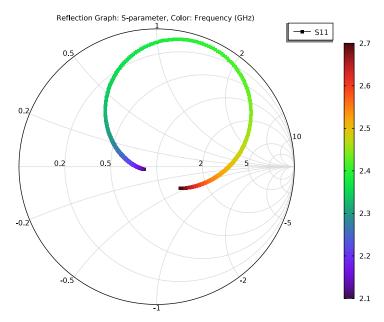
Expression	Unit	Description
emw.S11dB	dB	S11 Regular Sweep
emw.S21dB	dB	S21 Regular Sweep

5 Click to expand the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Cycle.



Smith Plot (emw) I

In the Model Builder window, under Results click Smith Plot (emw) 1.



The following instruction shows how to use the Graph Marker subfeature to analyze 1D plots. When plotting S21 of a bandstop filter, the -10dB attenuation bandwidth of the stopband can be computed with a graph marker. Use an additional graph marker on the S11 plot to check the maximum reflection level.

S-parameter with Graph Markers

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type S-parameter with Graph Markers in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 4 (sol4).

Global I

- I Right-click S-parameter with Graph Markers and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Ports>S-parameter, dB>emw.SIIdB - SII.

3 Locate the y-Axis Data section. In the table, enter the following settings:

Expression	Unit	Description
emw.S11dB	dB	S11

Graph Marker I

- I Right-click Global I and choose Graph Marker.
- 2 In the Settings window for Graph Marker, locate the Display section.
- 3 From the Display list, choose Max.
- 4 Locate the **Text Format** section. In the **Display precision** text field, type 2.
- **5** Select the **Show x-coordinate** check box.
- 6 Select the **Include unit** check box.

Global 2

- I In the Model Builder window, right-click S-parameter with Graph Markers and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Electromagnetic Waves, Frequency Domain>Ports>S-parameter, dB>emw.S21dB - S21.

Graph Marker I

- I Right-click Global 2 and choose Graph Marker.
- 2 In the Settings window for Graph Marker, locate the Display section.
- 3 From the Display mode list, choose Bandwidth.
- 4 From the Range type list, choose Stopband.
- 5 In the Cutoff value text field, type -10.
- 6 Locate the Text Format section. In the Display precision text field, type 3.
- **7** Select the **Include unit** check box.
- 8 Click to expand the Coloring and Style section. From the Orientation list, choose Vertical.
- **9** Select the **Show frame** check box.

