

Piezoelectric Energy Harvester

The development of extremely low-power electronics and wireless systems has led to a strong interest in the field of energy harvesting — the development of miniature generators. Typically, these devices are used to power sensors and wireless communication systems, enabling standalone wireless sensors that are cheap to deploy. Wireless sensors frequently make measurements intermittently over an extended period, reporting via a wireless link to other sensors and ultimately to a base station that records readings from all the deployed sensors (creating a wireless sensor network). This model analyzes a simple "seismic" energy harvester, that is a device designed to generate electrical energy from local variations in acceleration that occur, for example, when a wireless sensor is mounted on a vibrating piece of machinery. The energy harvester analyzed in this model consists of a piezoelectric bimorph clamped at one end to the vibrating machinery with a proof mass mounted at its other end. It is loosely based on the mechanical system described in detail in Ref. 1.

Model Definition

Figure 1 shows the device geometry. The power harvester consists of a piezoelectric bimorph clamped at one end with a proof mass mounted on the other end. The bimorph has two output electrodes embedded within it and two ground electrodes on the exterior surfaces of the cantilever beam. This configuration ensures that same voltage is induced on the output electrodes, even though the stress above and below the neutral layer is of opposite sign. Since the clamp is mounted to a piece of vibrating machinery the device is analyzed in a vibrating reference frame (modeled in COMSOL by the application of a sinusoidal body load).

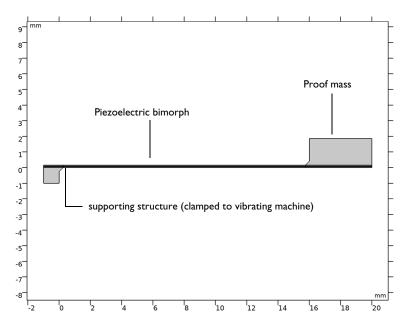


Figure 1: 2D model geometry, showing the major components of the energy harvester, including the piezoelectric bimorph, proof mass, and supporting structure.

The model performs three analyses of the mechanical part of the energy harvester system. First, the power output is analyzed as a function of vibration frequency with a fixed electrical load. Then, the power output as a function of electrical load is explored. Finally, the DC voltage output is shown to be a linear function of the acceleration.

Results and Discussion

Figure 2 shows the input mechanical power and the power harvested (in mW) as well as the peak voltage induced across the piezoelectric bimorph (in V) as a function of frequency when the energy harvester is excited by a sinusoidal acceleration. The electrical load is 12 k Ω . The response of the system shows a peak at 71 Hz, close to the computed resonant frequency of the cantilever at 72 Hz (from a separate eigenfrequency analysis of this device).

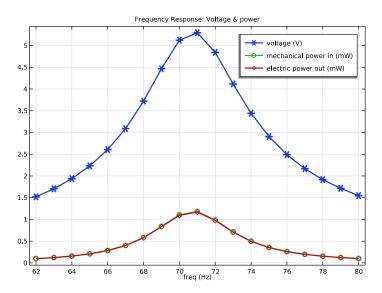


Figure 2: Energy harvester input mechanical power and the power harvested (in mW) as well as the peak voltage induced across the piezoelectric bimorph (in V) vs. excitation frequency. The load impedance is 12 k Ω and the acceleration magnitude is 1 g.

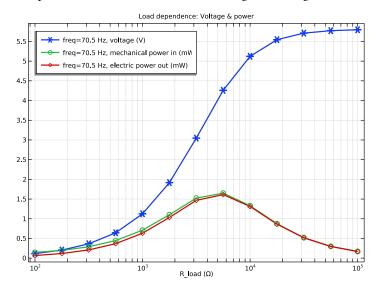


Figure 3: Power harvested from the device as a function of the electrical load resistance at an acceleration of 1 g oscillating at 70.5 Hz.

Figure 3 shows the harvested power from the device as a function of the electrical load resistance at an acceleration of 1 g oscillating at 70.5 Hz. The peak in energy harvested corresponds to an electrical load of 6 k Ω .

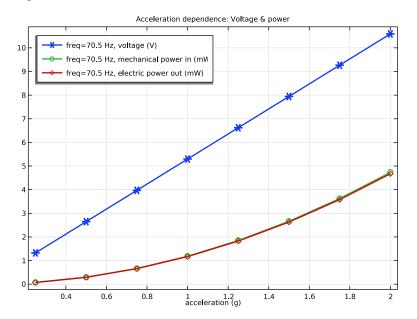


Figure 4: DC voltage and mechanical/electrical power output versus the magnitude of the mechanical acceleration at a fixed frequency of 70.5 Hz with a load impedance of $12 \, k\Omega$.

Figure 4 shows the DC voltage and mechanical/electrical power output versus the magnitude of the mechanical acceleration at a fixed frequency of 70.5 Hz with a load impedance of 12 k Ω . The voltage increases linearly with the load, whilst the harvested power increases quadratically, as expected from equation 4 in Ref. 1.

Note that these results are in good qualitative agreement with those presented in Ref. 1. Completely quantitative agreement would not be expected from a two dimensional model.

Reference

1. E. Lefeuvre, D. Audiger, C. Richard, and D. Guyomar, "Buck-Boost Converter for Sensorless Power Optimization of Piezoelectric Energy Harvester," IEEE Transactions on Power Electronics, vol. 22, no. 5, pp. 2018-2025, 2007.

Application Library path: MEMS Module/Piezoelectric Devices/

piezoelectric_energy_harvester

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 9 2D.
- 2 In the Select Physics tree, select Structural Mechanics>Electromagnetics-Structure Interaction>Piezoelectricity>Piezoelectricity, Solid.
- 3 Click Add.
- 4 In the Select Physics tree, select AC/DC>Electrical Circuit (cir).
- 5 Click Add.
- 6 Click 🗪 Study.
- 7 In the Select Study tree, select General Studies>Frequency Domain.
- 8 Click M Done.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description	
acc	1	I	Acceleration (g)	
R_load	12[kohm]	12000 Ω	Load resistance	
w_plate	14[mm]	0.014 m	Out of plane dimension	

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Position section.
- 3 In the x text field, type -1.
- 4 In the y text field, type -1.

Rectangle 2 (r2)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 21.
- 4 In the Height text field, type 0.16.
- 5 Locate the **Position** section. In the **x** text field, type -1.
- **6** Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (mm)	
Layer 1	0.06	
Layer 2	0.04	

Rectangle 3 (r3)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 4.
- 4 In the Height text field, type 1.7.
- **5** Locate the **Position** section. In the **x** text field, type 16.
- 6 In the y text field, type 0.16.

Union I (uni I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects r1 and r2 only.
- 3 In the Model Builder window, click Union I (unil).
- 4 In the Settings window for Union, locate the Union section.

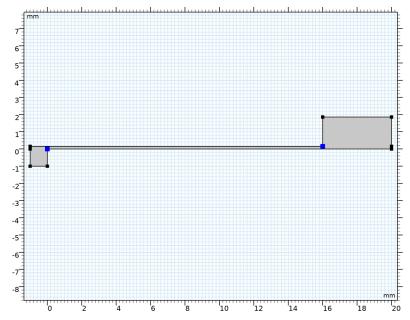
- 5 Click the **Zoom to Selection** button for **Input objects**.
- **6** Click in the **Graphics** window and then press Ctrl+A to select all objects.
- 7 Clear the Keep interior boundaries check box.

Add chamfers to the model to avoid stress singularities at the reentrant corners.

Chamfer I (chal)

- I In the Geometry toolbar, click Chamfer.
- 2 On the object unil, select Points 7 and 8 only.

It might be easier to select the correct points by using the **Selection List** window. To open this window, in the **Home** toolbar click **Windows** and choose **Selection List**. (If you are running the cross-platform desktop, you find **Windows** in the main menu.)



- 3 In the Settings window for Chamfer, locate the Distance section.
- 4 In the Distance from vertex text field, type 0.25.

Rectangle 2 (r2)

In the Model Builder window, right-click Rectangle 2 (r2) and choose Duplicate.

Line Segment I (Is I)

- I In the Geometry toolbar, click * More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.

- 3 From the Specify list, choose Coordinates.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- **5** Locate the **Starting Point** section. In the **x** text field, type **0.25**.
- 6 Locate the **Endpoint** section. In the x text field, type 0.25 and y to 0.16.

Line Segment 2 (Is2)

- I In the Geometry toolbar, click More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- **3** From the **Specify** list, choose **Coordinates**.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 Locate the Starting Point section. In the x text field, type 15.75 and y to 0.16.
- **6** Locate the **Endpoint** section. In the **x** text field, type 15.75.
- 7 In the Geometry toolbar, click **Build All**.

ADD MATERIAL

- I In the Home toolbar, click Radd Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Piezoelectric>Lead Zirconate Titanate (PZT-5A).
- 4 Click Add to Component in the window toolbar.
- 5 In the tree, select Built-in>Structural steel.
- 6 Click Add to Component in the window toolbar.
- 7 In the Home toolbar, click **Add Material** to close the Add Material window.

MATERIALS

Structural steel (mat2)

Select Domains 1, 3, 6, 9, and 11 only.

SOLID MECHANICS (SOLID)

Linear Elastic Material I

In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Linear Elastic Material I.

Dambing 1

- I In the Physics toolbar, click Attributes and choose Damping.
- 2 In the Settings window for Damping, locate the Damping Settings section.

- 3 From the Damping type list, choose Isotropic loss factor.
- **4** From the η_s list, choose **User defined**. In the associated text field, type 0.001.

Piezoelectric Material I

- I In the Model Builder window, under Component I (compl)>Solid Mechanics (solid) click Piezoelectric Material I.
- 2 In the Settings window for Piezoelectric Material, locate the Domain Selection section.
- 3 From the Selection list, choose Manual.
- **4** Select Domains 2, 4, 5, 7, 8, and 10 only.

Mechanical Damping I

- I In the Physics toolbar, click ___ Attributes and choose Mechanical Damping.
- 2 In the Settings window for Mechanical Damping, locate the Damping Settings section.
- 3 From the Damping type list, choose Isotropic loss factor.
- 4 From the $\eta_{\rm s}$ list, choose User defined. In the associated text field, type 0.001.

Body Load I

- I In the Physics toolbar, click **Domains** and choose **Body Load**.
- 2 In the Settings window for Body Load, locate the Domain Selection section.
- 3 From the Selection list, choose All domains.
- **4** Locate the **Force** section. Specify the $\mathbf{F}_{\mathbf{V}}$ vector as

0	x
-solid.rho*g_const*acc	у

Fixed Constraint I

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- 2 Select Boundary 2 only.

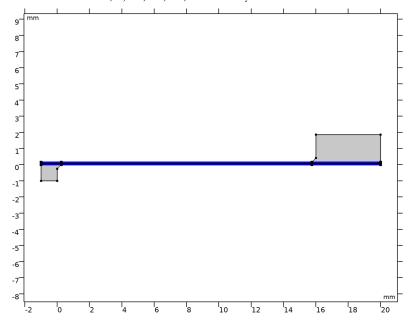
ELECTROSTATICS (ES)

- I In the Model Builder window, under Component I (compl) click Electrostatics (es).
- **2** Select Domains 2, 4, 5, 7, 8, and 10 only.
- 3 In the Settings window for Electrostatics, locate the Thickness section.
- **4** In the *d* text field, type w plate.

Ground I

I In the Physics toolbar, click — Boundaries and choose Ground.

2 Select Boundaries 4, 9, 13, 18, 20, and 26 only.



Terminal I

- I In the Physics toolbar, click Boundaries and choose Terminal.
- **2** Select Boundaries 6, 8, 15, 17, 22, and 24 only.
- 3 In the Settings window for Terminal, locate the Terminal section.
- 4 From the Terminal type list, choose Circuit.

ELECTRICAL CIRCUIT (CIR)

In the Model Builder window, under Component I (compl) click Electrical Circuit (cir).

Resistor I (RI)

- I In the Electrical Circuit toolbar, click Resistor.
- 2 In the Settings window for Resistor, locate the Node Connections section.
- **3** In the table, enter the following settings:

Label	Node names	
n	0	

4 Locate the **Device Parameters** section. In the R text field, type R_load.

External I-Terminal I (termII)

- I In the Electrical Circuit toolbar, click Faternal I-Terminal.
- 2 In the Settings window for External I-Terminal, locate the Node Connections section.
- 3 In the Node name text field, type 1.
- 4 Locate the External Terminal section. From the V list, choose Terminal voltage (es/ term I).

The high aspect ratio of the modeled geometry makes this problem numerically challenging. There is only a moderate range of mesh sizes where the result is reliable within a few percent. Outside of this range, with the mesh either too coarse or too fine, the result is not reliable.

MESH I

Free Triangular 1

In the Mesh toolbar, click Free Triangular.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the Element Size Parameters section. In the Maximum element size text field, type 0.02.
- 5 In the Minimum element size text field, type 0.002.

FREQUENCY RESPONSE

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Frequency Response in the Label text field.

Step 1: Frequency Domain

- I In the Model Builder window, under Frequency Response click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type range (62, 1, 80). Disable direct solver error checking which is too stringent in this case.

Solution I (soll)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution I (soll) node.

DEFINITIONS

Define a nonlocal integration coupling to calculate mechanical power input later when plotting results.

Integration | (intob |)

- I In the Model Builder window, expand the Frequency Response>Solver Configurations> Solution I (soll)>Stationary Solver I node.
- 2 Right-click Component I (compl)>Definitions and choose Nonlocal Couplings> Integration.
- 3 In the Settings window for Integration, locate the Source Selection section.
- 4 From the Selection list, choose All domains.

FREQUENCY RESPONSE

Solution I (soll)

- I In the Model Builder window, under Frequency Response>Solver Configurations> Solution I (soll)>Stationary Solver I click Direct.
- 2 In the Settings window for Direct, click to expand the Error section.
- 3 From the Check error estimate list, choose No.
- 4 In the Home toolbar, click **Compute**.

RESULTS

Frequency Response: Voltage & Power

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Frequency Response: Voltage & Power in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Frequency Response: Voltage & power.

Global I

- I Right-click Frequency Response: Voltage & Power and choose Global.
- 2 In the Settings window for Global, locate the y-Axis Data section.

3 In the table, enter the following settings:

Expression	Unit	Description
abs(cir.R1_v)	V	voltage (V)
0.5*intop1(realdot(-solid.rho* g_const*acc,solid.u_tY))*w_plate	mW	mechanical power in (mW)
0.5*realdot(cir.R1_i,cir.R1_v)	mW	electric power out (mW)

- 4 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 5 Find the Line markers subsection. From the Marker list, choose Cycle.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- **2** Go to the **Add Study** window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2

Step 1: Frequency Domain

- I In the Settings window for Frequency Domain, locate the Study Settings section.
- 2 In the Frequencies text field, type 70.5.
- 3 Click to expand the **Study Extensions** section. Select the **Auxiliary sweep** check box.
- 4 Click + Add.
- 5 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
R_load (Load resistance)	10^range(2,0.25,5)	Ω

- 6 In the Model Builder window, click Study 2.
- 7 In the Settings window for Study, type Load Dependence in the Label text field.
- **8** Locate the **Study Settings** section. Clear the **Generate default plots** check box.

Solution 2 (sol2)

I In the Study toolbar, click Show Default Solver.

- 2 In the Model Builder window, expand the Solution 2 (sol2) node.
- 3 In the Model Builder window, expand the Load Dependence>Solver Configurations> Solution 2 (sol2)>Stationary Solver I node, then click Direct.
- 4 In the Settings window for Direct, locate the Error section.
- 5 From the Check error estimate list, choose No.
- 6 In the Study toolbar, click **Compute**.

RESULTS

Frequency Response: Voltage & Power

In the Model Builder window, under Results right-click Frequency Response: Voltage & Power and choose **Duplicate**.

Load Dependence: Voltage & Power

- I In the Model Builder window, under Results click Frequency Response: Voltage & Power I.
- 2 In the Settings window for ID Plot Group, type Load Dependence: Voltage & Power in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Load Dependence/Solution 2 (sol2).
- 4 Locate the Title section. In the Title text area, type Load dependence: Voltage & power.
- 5 Locate the Legend section. From the Position list, choose Upper left.
- 6 Click the **x-Axis Log Scale** button in the **Graphics** toolbar.
- 7 In the Load Dependence: Voltage & Power toolbar, click Plot.

ROOT

From the Home menu, choose Add Study.

ADD STUDY

- I Go to the Add Study window.
- 2 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- **3** Click **Add Study** in the window toolbar.
- **4** From the **Home** menu, choose **Add Study**.

STUDY 3

Step 1: Frequency Domain

- I In the Settings window for Frequency Domain, locate the Study Settings section.
- 2 In the Frequencies text field, type 70.5.
- 3 Locate the Study Extensions section. Select the Auxiliary sweep check box.
- 4 Click + Add.
- 5 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
acc (Acceleration (g))	range(0.25,0.25,2)	

- 6 In the Model Builder window, expand the Load Dependence: Voltage & Power node, then click Study 3.
- 7 In the Settings window for Study, type Acceleration Dependence in the Label text field.
- 8 Locate the Study Settings section. Clear the Generate default plots check box.

Solution 3 (sol3)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution 3 (sol3) node.
- 3 In the Model Builder window, expand the Acceleration Dependence> Solver Configurations>Solution 3 (sol3)>Stationary Solver I node, then click Direct.
- 4 In the Settings window for Direct, locate the Error section.
- **5** From the **Check error estimate** list, choose **No**.
- 6 In the Study toolbar, click **Compute**.

RESULTS

Load Dependence: Voltage & Power

In the Model Builder window, under Results right-click Load Dependence: Voltage & Power and choose **Duplicate**.

Acceleration Dependence: Voltage & Power

- I In the Model Builder window, under Results click Load Dependence: Voltage & Power I.
- 2 In the Settings window for ID Plot Group, type Acceleration Dependence: Voltage & Power in the Label text field.

- 3 Locate the Data section. From the Dataset list, choose Acceleration Dependence/ Solution 3 (sol3).
- 4 Locate the Plot Settings section.
- **5** Select the **x-axis label** check box. In the associated text field, type acceleration (g).
- 6 Locate the Axis section. Clear the x-axis log scale check box.
- 7 Locate the Title section. In the Title text area, type Acceleration dependence: Voltage & power.