

Vibration in a Washing Machine Assembly

Vibration and noise, due to nonuniform distribution of clothes, is a common problem in washing machines.

This model simulates a simplified multibody dynamics model of a horizontal-axis portable washing machine. An eigenfrequency analysis is performed to compute the natural frequencies and mode shapes of the entire assembly. Transient analysis is performed to find out the vibrations induced in the housing during the spinning cycle. The housing is modeled as a flexible shell.

Note: This model requires the Multibody Dynamics Module and the Structural Mechanics Module.

Model Definition

The geometry of the washing machine assembly is shown in Figure 1.

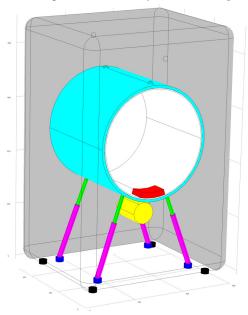


Figure 1: Model geometry (top, bottom, front, and left panels of the housing are hidden).

A key to the coloring of the parts constituting the washing machine is given below.

TABLE I: IDENTIFICATION OF VARIOUS PARTS OF WASHING MACHINE ASSEMBLY.

Part	Color in figure
Clothes	Red
Drum	White
Tub	Cyan
Motor	Yellow
Pistons	Green
Cylinders	Magenta
Mountings	Blue
Base supports	Black
Housing	Gray

The following assumptions are used:

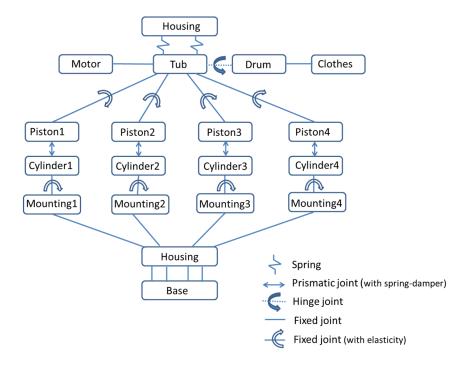
- The housing is modeled using flexible shell elements.
- The other parts are modeled by rigid solids.
- The clothes do not move relative to the drum.

CONNECTION DETAILS

The connections of the housing to the remaining parts are as follows:

- Connection with the base, at four locations on the bottom surface, using fixed joints.
- Connection with the mountings, at four locations on the bottom surface, using fixed joints.
- Connection with the tub, at front and back surfaces, using stabilizing springs. These springs are not shown in the geometry (Figure 1) or in the model.

The details of all the connections in the assembly are shown below:



Results and Discussion

The mode shapes of the washing machine assembly can be seen in Figure 2 and Figure 3. In these figures, one of the modes showing the translation of the tub whereas the other one shows the rotation of the tub about the vertical axis. The corresponding housing deformation can also be seen. The magnitude of deformation of housing is very small compared to the motion of the tub, so a different color table is used for better clarity.

Figure 4 and Figure 5 show the tub displacement magnitude with the drum rotation or the position of unbalanced clothes for the full time duration. The color of the trajectory has the time information representing red as the initial time and blue as final time.

Eigenfrequency=2.6539+0.66123i Hz Surface: Displacement magnitude (mm)

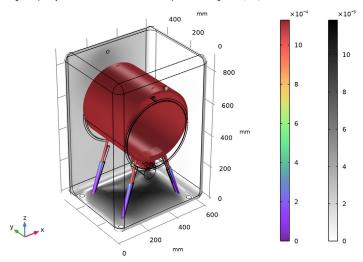


Figure 2: One of the eigenmodes of the washing machine assembly (with the tub translating along vertical axis).

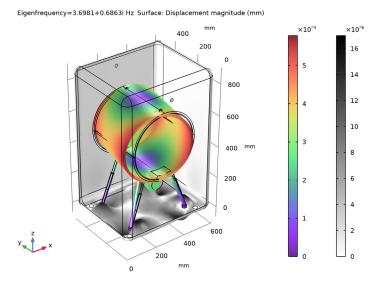


Figure 3: One of the eigenmodes of the washing machine assembly (with the tub rotating about vertical axis).

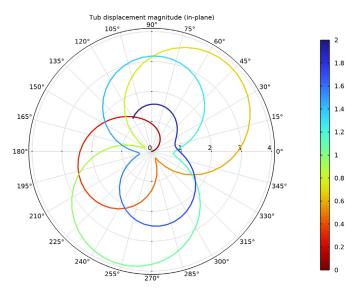


Figure 4: In-plane (x-z) displacement magnitude of the tub with the position of unbalanced clothes.

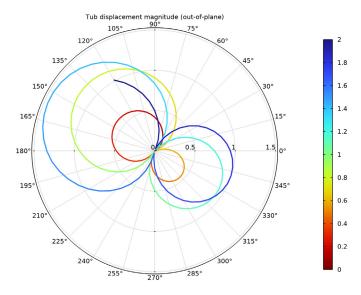


Figure 5: Out-of-plane (y) displacement magnitude of the tub with the position of unbalanced clothes.

Tub rotation about all three axes with the rotation of the drum is shown in Figure 6 below.

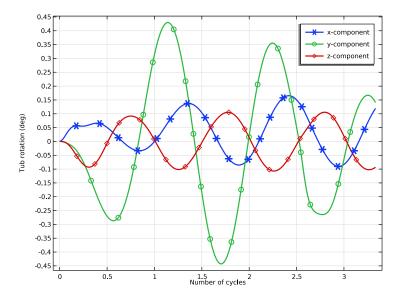


Figure 6: Tub rotation about all three axes.

Figure 7 shows the extension in the front and back stabilizing springs with the rotation of the drum.

The relative displacement between the piston and the cylinder for the different struts is shown in Figure 8. The energy dissipation in the struts with the rotation of the drum is plotted in Figure 9.

The deformation of the housing in the vertical direction with the drum rotation at the locations where mountings are attached is shown in Figure 10.

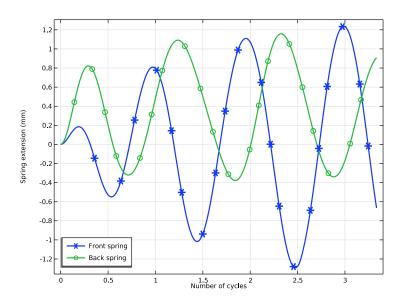


Figure 7: Extension of the stabilizing springs.

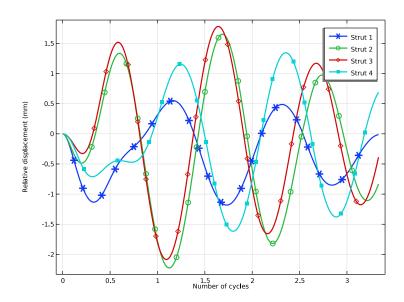


Figure 8: Relative displacement between the piston and the cylinder of different struts.

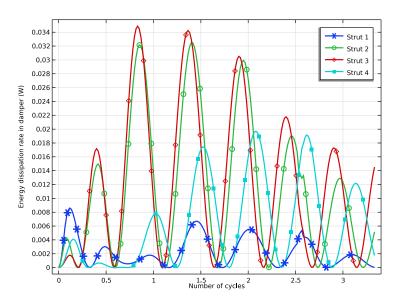


Figure 9: Energy dissipation rate in different struts.

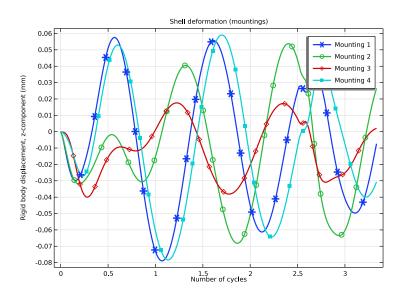


Figure 10: Vertical deformation of the housing at the mounting locations.

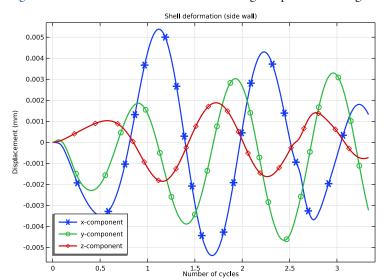


Figure 11 shows the deformation of the housing at a point on the right side wall.

Figure 11: Deformation of the housing in different directions at a point on the side wall.

Notes About the COMSOL Implementation

- Use the Mass and Moment of Inertia subnode of the Rigid Material node to enter the inertia properties given at a certain point.
- The connections set up in the model and the details of the system DOF and constraints can be seen in the Joints Summary and Rigid Body DOF Summary sections of the Multibody Dynamics node.
- Use the **Attachment** boundary condition in the Shell interface to establish the connection to the solid objects through joints and springs.
- The numbering used in the model for the piston, cylinder, mounting, and base is such that 1, 2, 3, and 4 corresponds to front-left, front-right, back-right, and back-left locations, respectively.

Application Library path: Multibody Dynamics Module/ Machinery and Robotics/washing machine vibration

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **3D**.
- 2 In the Select Physics tree, select Structural Mechanics>Multibody Dynamics (mbd).
- 3 Click Add.
- 4 In the Select Physics tree, select Structural Mechanics>Shell (shell).
- 5 Click Add.
- 6 Click 🗪 Study.
- 7 In the Select Study tree, select General Studies>Eigenfrequency.
- 8 Click Done.

GLOBAL DEFINITIONS

Start by importing the model parameters and geometry.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file washing_machine_vibration_parameters.txt.

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Import I (impl)

- I In the Home toolbar, click Import.
- 2 In the Settings window for Import, locate the Import section.
- 3 Click **Browse**.

- 4 Browse to the model's Application Libraries folder and double-click the file washing_machine_vibration.mphbin.
- 5 Click Import.

Form Union (fin)

- I In the Model Builder window, under Component I (compl)>Geometry I click Form Union (fin).
- 2 In the Settings window for Form Union/Assembly, locate the Form Union/Assembly section.
- 3 From the Action list, choose Form an assembly.
- 4 Clear the Create pairs check box.
- 5 In the Home toolbar, click **Build All**.

DEFINITIONS

Hiding the front panels of the geometry will make it more convenient to set up the model.

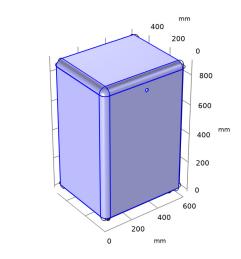
View 1

- I In the Model Builder window, expand the Component I (compl)>Definitions node, then click View 1.
- 2 In the Settings window for View, locate the View section.
- 3 Select the Wireframe rendering check box.

Hide for Geometry 1

- I Right-click View I and choose Hide for Geometry.
- 2 In the Settings window for Hide for Geometry, locate the Selection section.
- 3 From the Geometric entity level list, choose Boundary.

4 On the object fin, select Boundaries 1, 2, 5, 6, 10, 12, and 14 only.



Define some selections to be used later.

Housing

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, type Housing in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 36 only. It might be easier to select the correct boundary by using the **Selection List** window. To open this window, in the Home toolbar click Windows and choose Selection List. (If you are running the cross-platform desktop, you find Windows in the main menu.)
- 5 Select the Group by continuous tangent check box.

Strut axis I

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Edge.
- 4 Select Edge 228 only.
- 5 In the Label text field, type Strut axis 1.
- 6 Right-click Strut axis I and choose Duplicate.

Strut axis 2

- I In the Model Builder window, under Component I (compl)>Definitions>Selections click Strut axis I.I.
- 2 In the Settings window for Explicit, type Strut axis 2 in the Label text field.
- 3 Locate the Input Entities section. Click Clear Selection.
- 4 Select Edge 444 only.
- **5** Right-click **Strut axis 2** and choose **Duplicate**.

Strut axis 3

- I In the Model Builder window, under Component I (compl)>Definitions>Selections click Strut axis 2.1
- 2 In the Settings window for Explicit, type Strut axis 3 in the Label text field.
- 3 Locate the Input Entities section. Click Clear Selection.
- 4 Select Edge 484 only.
- 5 Right-click Strut axis 3 and choose Duplicate.

Strut axis 4

- I In the Model Builder window, under Component I (compl)>Definitions>Selections click Strut axis 3.1.
- 2 In the Settings window for Explicit, type Strut axis 4 in the Label text field.
- 3 Locate the Input Entities section. Click Clear Selection.
- 4 Select Edge 268 only.

Define various components of the washing machine assembly.

MULTIBODY DYNAMICS (MBD)

Clothes

- I In the Model Builder window, under Component I (compl) right-click Multibody Dynamics (mbd) and choose Material Models>Rigid Material.
- 2 In the Settings window for Rigid Material, type Clothes in the Label text field.
- 3 Select Domain 13 only.
 - Set the density of the selected domain to zero. Use Mass and Moment of Inertia subnode instead to specify the mass of the domain.
- **4** Locate the **Density** section. From the ρ list, choose **User defined**.

Mass and Moment of Inertia I

- I In the Physics toolbar, click 🖳 Attributes and choose Mass and Moment of Inertia.
- 2 In the Settings window for Mass and Moment of Inertia, locate the Mass and Moment of Inertia section.
- **3** In the *m* text field, type Mc.

Use the **Applied Force** subnode to account for the gravitational force.

Clothes

In the Model Builder window, click Clothes.

Applied Force 1

- I In the Physics toolbar, click 💂 Attributes and choose Applied Force.
- 2 In the Settings window for Applied Force, locate the Applied Force section.
- **3** Specify the \mathbf{F} vector as

0	х
0	у
-Mc*g_const	z

Drum

- I In the Physics toolbar, click **Domains** and choose Rigid Material.
- 2 In the Settings window for Rigid Material, type Drum in the Label text field.
- 3 Select Domain 8 only.
 - Select Force initial values in the Consistent initialization list, to enforce the parts, which are connected to the drum such as clothes, to rotate with the same angular speed.
- 4 Locate the Initial Values section. From the list, choose Locally defined.
- 5 From the Consistent initialization list, choose Force initial values.
- 6 Select the Translation along first axis check box.
- 7 Select the Translation along second axis check box.
- 8 Select the Translation along third axis check box.
- **9** Select the **Total rotation** check box.

Initial Values 1

- I In the Model Builder window, click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Center of Rotation section.
- 3 From the list, choose Centroid of selected entities.

- 4 From the Entity level list, choose Point.
- **5** Locate the **Initial Values: Rotational** section. Specify the ω vector as

0	x
omega	у
0	z

Center of Rotation: Point I

- I In the Model Builder window, click Center of Rotation: Point I.
- **2** Select Points 141 and 151 only.

Tub

- I In the Physics toolbar, click **Domains** and choose Rigid Material.
- 2 In the Settings window for Rigid Material, type Tub in the Label text field.
- **3** Select Domains 5, 15, and 16 only.

Motor

- I In the Physics toolbar, click **Domains** and choose Rigid Material.
- 2 In the Settings window for Rigid Material, type Motor in the Label text field.
- **3** Select Domain 14 only.
- **4** Locate the **Density** section. From the ρ list, choose **User defined**.

Mass and Moment of Inertia I

- I In the Physics toolbar, click 📃 Attributes and choose Mass and Moment of Inertia.
- 2 In the Settings window for Mass and Moment of Inertia, locate the Mass and Moment of Inertia section.
- 3 In the m text field, type Mm.
- 4 In the I text field, type Im.

Piston I

- I In the Physics toolbar, click **Domains** and choose Rigid Material.
- 2 In the Settings window for Rigid Material, type Piston 1 in the Label text field.
- 3 Select Domain 11 only.

Rigid Materials

Similarly create more components by duplicating **Piston I** and resetting the inputs using the information given in the table below.

Name	Selection
Piston 2	17
Piston 3	18
Piston 4	12
Cylinder I	9
Cylinder 2	19
Cylinder 3	20
Cylinder 4	10
Mounting I	6
Mounting 2	21
Mounting 3	22
Mounting 4	7
Base	1-4

Base

In the Model Builder window, click Base.

Fixed Constraint I

In the Physics toolbar, click 🕞 Attributes and choose Fixed Constraint.

MATERIALS

Material I (mat I)

- I In the Model Builder window, under Component I (compl) right-click Materials and choose Blank Material.
- 2 In the Settings window for Material, locate the Material Contents section.
- **3** In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	rho0	kg/m³	Basic

ADD MATERIAL

- I In the Home toolbar, click **4** Add Material to open the Add Material window.
- 2 Go to the Add Material window.

- 3 In the tree, select Built-in>Aluminum.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click 4 Add Material to close the Add Material window.

MATERIALS

Aluminum (mat2)

- I In the Settings window for Material, locate the Geometric Entity Selection section.
- 2 From the Geometric entity level list, choose Boundary.
- 3 From the Selection list, choose Housing.

SHELL [HOUSING]

- I In the Model Builder window, under Component I (compl) click Shell (shell).
- 2 In the Settings window for Shell, type Shell [Housing] in the Label text field.
- 3 Locate the Boundary Selection section. From the Selection list, choose Housing. Use linear elements for the shell to reduce the computation time.
- 4 Click to expand the Discretization section. From the Displacement field list, choose Linear.

As the amplitude of vibration is going to be small in the shell, select the Force linear strains option in the Linear Elastic Material I node. This will reduce the analysis time.

Thickness and Offset I

- I In the Model Builder window, under Component I (compl)>Shell [Housing] (shell) click Thickness and Offset I.
- 2 In the Settings window for Thickness and Offset, locate the Thickness and Offset section.
- **3** In the d_0 text field, type 0.001[m].

Linear Elastic Material I

- I In the Model Builder window, click Linear Elastic Material I.
- 2 In the Settings window for Linear Elastic Material, locate the Geometric Nonlinearity section.
- 3 From the Formulation list, choose Geometrically linear.

Define the attachments in the Shell interface to couple it with the Multibody Dynamics interface.

Front spring

I In the Physics toolbar, click Edges and choose Attachment.

- 2 In the Settings window for Attachment, type Front spring in the Label text field.
- **3** Select Edges 45, 46, 49, and 50 only.

Shell Attachments

Similarly, create more attachments by duplicating Front Spring and resetting the inputs using the information given in the table below:

Name	Selection (edge)		
Back Spring	47, 48, 51, 52		
Mounting I	37, 38, 41, 42		
Mounting 2	53, 54, 57, 58		
Mounting 3	55, 56, 59, 60		
Mounting 4	39, 40, 43, 44		
Base I	29, 30, 33, 34		
Base 2	61, 62, 65, 66		
Base 3	63, 64, 67, 68		
Base 4	31, 32, 35, 36		

Use the **Spring-Damper** node to model the stabilizing springs.

MULTIBODY DYNAMICS (MBD)

In the Model Builder window, under Component I (compl) click Multibody Dynamics (mbd).

Housing-tub (front)

- I In the Physics toolbar, click Signature Global and choose Spring-Damper.
- 2 In the Settings window for Spring-Damper, type Housing-tub (front) in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Front spring (shell).
- 4 Locate the Spring-Damper section. In the k text field, type kt.

Destination Point I

- I In the Model Builder window, click Destination Point I.
- 2 Select Points 246 and 248 only.

Housing-tub (front)

In the Model Builder window, right-click Housing-tub (front) and choose Duplicate.

Housing-tub (back)

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd) click Housing-tub (front) 1.
- 2 In the Settings window for Spring-Damper, type Housing-tub (back) in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Back spring (shell).

Destination Point I

- I In the Model Builder window, expand the Housing-tub (back) node, then click **Destination Point 1.**
- 2 In the Settings window for Destination Point, locate the Point Selection section.
- 3 Click Clear Selection.
- 4 Select Points 258 and 260 only.

Define the connection between the drum and the tub using a **Hinge Joint**.

- I In the Physics toolbar, click Global and choose Hinge Joint.
- 2 In the Settings window for Hinge Joint, type Tub-drum in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Tub.
- 4 From the **Destination** list, choose **Drum**.
- 5 Locate the Center of Joint section. From the Entity level list, choose Point.
- **6** Locate the **Axis of Joint** section. Specify the e_0 vector as

0	x
1	у
0	z

Center of Joint: Point I

- I In the Model Builder window, click Center of Joint: Point I.
- 2 Select Points 141 and 151 only.

Tub-drum

In the Model Builder window, click Tub-drum.

Prescribed Motion 1

I In the Physics toolbar, click 💂 Attributes and choose Prescribed Motion.

- 2 In the Settings window for Prescribed Motion, locate the Prescribed Rotational Motion section.
- 3 From the Prescribed motion through list, choose Angular velocity.
- **4** In the ω_p text field, type omega.

Define **Fixed Joints** between motor-tub and drum-clothes.

Motor-tub

- I In the Physics toolbar, click Signature Global and choose Fixed Joint.
- 2 In the Settings window for Fixed Joint, type Motor-tub in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Motor.
- 4 From the **Destination** list, choose **Tub**.

Center of Joint: Boundary 1

- I In the Model Builder window, click Center of Joint: Boundary I.
- **2** Select Boundaries 168 and 171 only.

Motor-tub

In the Model Builder window, right-click Motor-tub and choose Duplicate.

Drum-clothes

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd) click Motor-tub 1.
- 2 In the Settings window for Fixed Joint, type Drum-clothes in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Drum.
- 4 From the **Destination** list, choose **Clothes**.

Center of Joint: Boundary I

- I In the Model Builder window, expand the Drum-clothes node, then click Center of Joint: Boundary I.
- 2 In the Settings window for Center of Joint: Boundary, locate the Boundary Selection section.
- 3 Click Clear Selection.
- 4 Select Boundary 157 only.

Model the struts using Prismatic Joints.

Cylinder I-piston I

I In the Physics toolbar, click A Global and choose Prismatic Joint.

- 2 In the Settings window for Prismatic Joint, type Cylinder 1-piston 1 in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Cylinder 1.
- 4 From the **Destination** list, choose **Piston I**.
- 5 Locate the Axis of Joint section. From the list, choose Select a parallel edge.

Center of Joint: Boundary 1

- I In the Model Builder window, click Center of Joint: Boundary I.
- 2 Select Boundary 144 only.

Joint Axis I

- I In the Model Builder window, click Joint Axis I.
- 2 In the Settings window for Joint Axis, locate the Edge Selection section.
- 3 From the Selection list, choose Strut axis 1.

Cylinder I-biston I

In the Model Builder window, click Cylinder 1-piston 1.

Spring and Damper I

- I In the Physics toolbar, click 🕞 Attributes and choose Spring and Damper.
- 2 In the Settings window for Spring and Damper, locate the Spring and Damper: Translational section.
- 3 In the k_{11} text field, type ks.
- **4** In the $c_{\rm u}$ text field, type cs.

Prismatic Joints

Create the other three prismatic joints by duplicating **Cylinder I-piston I** and resetting the inputs using the information given in the table below:

Name	Source	Destination	Center of Joint (boundary)	Joint axis selection (edge)
Cylinder 2- piston 2	Cylinder 2	Piston 2	195	Strut axis 2
Cylinder 3- piston 3	Cylinder 3	Piston 3	201	Strut axis 3
Cylinder 4- piston 4	Cylinder 4	Piston 4	150	Strut axis 4

Tub-biston I

- I In the Physics toolbar, click Signature Global and choose Fixed Joint.
- 2 In the Settings window for Fixed Joint, type Tub-piston 1 in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Tub.
- 4 From the **Destination** list, choose **Piston I**.
- 5 Locate the Axis of Joint section. From the list, choose Select a parallel edge.
- **6** Locate the **Joint Elasticity** section. From the list, choose **Elastic joint**.

Center of Joint: Boundary 1

- I In the Model Builder window, click Center of Joint: Boundary I.
- **2** Select Boundary 149 only.

Joint Axis I

- I In the Model Builder window, click Joint Axis I.
- 2 In the Settings window for Joint Axis, locate the Edge Selection section.
- 3 From the Selection list, choose Strut axis 1.

Joint Elasticity I

- I In the Model Builder window, click Joint Elasticity I.
- 2 In the Settings window for Joint Elasticity, locate the Elastic Degrees of Freedom section.
- 3 Clear the First axis check box.
- 4 Clear the **Second axis** check box.
- 5 Clear the Third axis check box.
- **6** Locate the **Spring** section. In the \mathbf{k}_{θ} text field, type kbr.
- **7** Locate the **Viscous Damping** section. In the \mathbf{c}_{θ} text field, type cbr.

Fixed Joints (with Elasticity)

Similarly create seven additional bushings by duplicating **Tub 1-piston 1** and resetting the inputs using the information given in the table below:

Name	Source	Destination	Center of Joint (boundary)	Joint axis selection (edge)
Tub-piston 2	Tub	Piston 2	190	Strut axis 2
Tub-piston 3	Tub	Piston 3	196	Strut axis 3
Tub-piston 4	Tub	Piston 4	155	Strut axis 4
Cylinder I- mounting I	Cylinder I	Mounting I	74	Strut axis I

Name	Source	Destination	Center of Joint (boundary)	Joint axis selection (edge)
Cylinder 2- mounting 2	Cylinder 2	Mounting 2	247	Strut axis 2
Cylinder 3- mounting 3	Cylinder 3	Mounting 3	257	Strut axis 3
Cylinder 4- mounting 4	Cylinder 4	Mounting 4	84	Strut axis 4

Cylinder 2-piston 2

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd) click Cylinder 2-piston 2.
- 2 In the Settings window for Prismatic Joint, locate the Axis of Joint section.
- 3 Select the Reverse direction check box.

Cylinder 3-biston 3

- I In the Model Builder window, click Cylinder 3-piston 3.
- 2 In the Settings window for Prismatic Joint, locate the Axis of Joint section.
- 3 Select the Reverse direction check box.

Tub-biston 2

- I In the Model Builder window, click Tub-piston 2.
- 2 In the Settings window for Fixed Joint, locate the Axis of Joint section.
- 3 Select the Reverse direction check box.

Tub-piston 3

- I In the Model Builder window, click Tub-piston 3.
- 2 In the Settings window for Fixed Joint, locate the Axis of Joint section.
- 3 Select the Reverse direction check box.

Cylinder 2-mounting 2

- I In the Model Builder window, click Cylinder 2-mounting 2.
- 2 In the Settings window for Fixed Joint, locate the Axis of Joint section.
- 3 Select the Reverse direction check box.

Cylinder 3-mounting 3

- I In the Model Builder window, click Cylinder 3-mounting 3.
- 2 In the Settings window for Fixed Joint, locate the Axis of Joint section.

3 Select the Reverse direction check box.

Cylinder 4-mounting 4

In the Model Builder window, right-click Cylinder 4-mounting 4 and choose Duplicate.

Mounting 1-housing

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd) click Cylinder 4-mounting 4.1.
- 2 In the Settings window for Fixed Joint, type Mounting 1-housing in the Label text field.
- 3 Locate the Attachment Selection section. From the Source list, choose Mounting 1.
- 4 From the Destination list, choose Mounting I (shell).
- 5 Locate the Axis of Joint section. From the list, choose Specify direction.
- 6 Locate the Joint Elasticity section. From the list, choose Rigid joint.
- 7 Locate the Center of Joint section. From the list, choose Centroid of destination.

Fixed Joints (Rigid)

Similarly, create seven additional connections by duplicating Mounting I-housing and resetting the inputs using the information given in the table below:

Name	Source	Destination
Mounting 2-housing	Mounting 2	Mounting 2(shell)
Mounting 3-housing	Mounting 3	Mounting 3(shell)
Mounting 4-housing	Mounting 4	Mounting 4(shell)
Housing-base I	Base I (shell)	Base
Housing-base 2	Base 2 (shell)	Base
Housing-base 3	Base 3 (shell)	Base
Housing-base 4	Base 4 (shell)	Base

To create node groups for the physics features, do the following:

Base, Clothes, Cylinder I, Cylinder 2, Cylinder 3, Cylinder 4, Drum, Motor, Mounting I, Mounting 2, Mounting 3, Mounting 4, Piston 1, Piston 2, Piston 3, Piston 4, Tub

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd), Ctrl-click to select Clothes, Drum, Tub, Motor, Piston 1, Piston 2, Piston 3, Piston 4, Cylinder 1, Cylinder 2, Cylinder 3, Cylinder 4, Mounting 1, Mounting 2, Mounting 3, Mounting 4, and Base.
- 2 Right-click and choose Group.

Rigid Materials

In the Settings window for Group, type Rigid Materials in the Label text field.

Cylinder 1-mounting 1, Cylinder 2-mounting 2, Cylinder 3-mounting 3, Cylinder 4mounting 4, Drum-clothes, Housing-base 1, Housing-base 2, Housing-base 3, Housingbase 4, Motor-tub, Mounting 1-housing, Mounting 2-housing, Mounting 3-housing, Mounting 4-housing, Tub-piston 1, Tub-piston 2, Tub-piston 3, Tub-piston 4

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd), Ctrl-click to select Motor-tub, Drum-clothes, Tub-piston 1, Tub-piston 2, Tub-piston 3, Tub-piston 4, Cylinder 1-mounting 1, Cylinder 2-mounting 2, Cylinder 3-mounting 3, Cylinder 4-mounting 4, Mounting 1-housing, Mounting 2-housing, Mounting 3-housing, Mounting 4-housing, Housing-base 1, Housing-base 2, Housing-base 3, and Housing-base 4.
- 2 Right-click and choose **Group**.

Fixed Joints

In the Settings window for Group, type Fixed Joints in the Label text field.

Cylinder 1-piston 1, Cylinder 2-piston 2, Cylinder 3-piston 3, Cylinder 4-piston 4

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd), Ctrl-click to select Cylinder 1-piston 1, Cylinder 2-piston 2, Cylinder 3-piston 3, and Cylinder 4-piston 4.
- 2 Right-click and choose **Group**.

Prismatic Joints

In the Settings window for Group, type Prismatic Joints in the Label text field.

Housing-tub (back), Housing-tub (front)

- I In the Model Builder window, under Component I (compl)>Multibody Dynamics (mbd), Ctrl-click to select Housing-tub (front) and Housing-tub (back).
- **2** Right-click and choose **Group**.

Spring-Dambers

In the Settings window for Group, type Spring-Dampers in the Label text field.

SHELL [HOUSING] (SHELL)

Back spring, Base 1, Base 2, Base 3, Base 4, Front spring, Mounting 1, Mounting 2, Mounting 3, Mounting 4

I In the Model Builder window, under Component I (compl)>Shell [Housing] (shell), Ctrlclick to select Front spring, Back spring, Mounting 1, Mounting 2, Mounting 3, Mounting 4, Base 1, Base 2, Base 3, and Base 4.

2 Right-click and choose **Group**.

Attachments

In the **Settings** window for **Group**, type Attachments in the **Label** text field.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Fine**.
- 4 Click Build All.

STUDY I

Step 1: Eigenfrequency

- I In the Settings window for Eigenfrequency, locate the Study Settings section.
- 2 In the Search for eigenfrequencies around shift text field, type 2.
- 3 In the Model Builder window, click Study 1.
- 4 In the Settings window for Study, locate the Study Settings section.
- 5 Clear the Generate default plots check box.
- **6** In the **Home** toolbar, click **Compute**.

Use the instructions below to reproduce the mode shape shown in Figure 2.

RESULTS

Mode Shape

- I In the Home toolbar, click Add Plot Group and choose 3D Plot Group.
- 2 In the Settings window for 3D Plot Group, type Mode Shape in the Label text field.

Surface 1

- I Right-click Mode Shape and choose Surface.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Rainbow>SpectrumLight in the tree.
- 5 Click OK.

Deformation I

Right-click Surface I and choose Deformation.

Surface 2

- I In the Model Builder window, right-click Mode Shape and choose Surface.
- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type shell.disp.
- **4** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Coloring and Style section. Click | Change Color Table.
- 6 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Coloring and Style section.
- 9 From the Color table transformation list, choose Reverse.

Deformation I

- I Right-click Surface 2 and choose Deformation.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the X-component text field, type u2.
- 4 In the Y-component text field, type v2.
- **5** In the **Z-component** text field, type w2.

Mode Shape

- I In the Model Builder window, under Results click Mode Shape.
- 2 In the Settings window for 3D Plot Group, locate the Data section.
- 3 From the Eigenfrequency (Hz) list, choose 2.6539+0.66123i.
- 4 In the Mode Shape toolbar, click Plot.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar. Change the eigenfrequency to obtain the eigenmode as shown in Figure 3.
- 6 From the Eigenfrequency (Hz) list, choose 3.6981+0.6863i.
- 7 In the Mode Shape toolbar, click Plot.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Before performing a transient analysis, define additional variables to use them in postprocessing.

DEFINITIONS

Variables 1

- I In the Model Builder window, under Component I (compl) right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
uin_tub	sqrt(mbd.rd3.u^2+ mbd.rd3.w^2)	m	Tub displacement magnitude (in-plane)
uout_tub	abs(mbd.rd3.v)	m	Tub displacement magnitude (out-of-plane)
th_drum	mbd.hgj1.th	rad	Drum rotation
n_cycle	th_drum/360[deg]		Number of cycles

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2

Step 1: Time Dependent

- I In the Settings window for Time Dependent, locate the Study Settings section.
- 2 In the Output times text field, type range (0,0.01,2).
- 3 In the Model Builder window, click Study 2.
- 4 In the Settings window for Study, locate the Study Settings section.
- 5 Clear the Generate default plots check box.

Solution 2 (sol2)

I In the Study toolbar, click Show Default Solver.

Modify the default solver settings in such a way that both physics are solved together.

- 2 In the Model Builder window, expand the Solution 2 (sol2) node, then click Time-Dependent Solver I.
- 3 In the Settings window for Time-Dependent Solver, click to expand the Absolute Tolerance section.
- 4 From the Tolerance method list, choose Manual.
- 5 Click to expand the Time Stepping section. From the Steps taken by solver list, choose Intermediate.
- 6 Right-click Study 2>Solver Configurations>Solution 2 (sol2)>Time-Dependent Solver I and choose Fully Coupled.
- 7 In the Settings window for Fully Coupled, click to expand the Method and Termination section.
- 8 From the Jacobian update list, choose On every iteration.
- 9 In the Maximum number of iterations text field, type 15.
- 10 In the Model Builder window, under Study 2>Solver Configurations>Solution 2 (sol2)> Time-Dependent Solver I click Advanced.
- II In the Settings window for Advanced, locate the General section.
- 12 From the Null-space function list, choose Orthonormal.
- 13 In the Study toolbar, click **Compute**.

Duplicate the mode shape plot and change the dataset to plot the displacement obtained in the transient analysis.

RESULTS

Mode Shape

In the Model Builder window, under Results right-click Mode Shape and choose Duplicate.

Displacement

- I In the Model Builder window, under Results click Mode Shape I.
- 2 In the Settings window for 3D Plot Group, type Displacement in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).
- **4** From the **Time (s)** list, choose **I**.
- 5 Locate the Plot Settings section. From the Frame list, choose Spatial (x, y, z).
- 6 In the Model Builder window, expand the Displacement node.

Deformation I

- I In the Model Builder window, expand the Results>Displacement>Surface I node, then click **Deformation 1**.
- 2 In the Settings window for Deformation, locate the Scale section.
- 3 Select the Scale factor check box. In the associated text field, type 1.

Deformation I

- I In the Model Builder window, expand the Results>Displacement>Surface 2 node, then click Deformation I.
- 2 In the Settings window for Deformation, locate the Scale section.
- **3** Select the **Scale factor** check box. In the associated text field, type 1.
- 4 In the **Displacement** toolbar, click **| Old Plot**.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Follow the instructions below to get the polar plots of the tub displacement shown in Figure 4 and Figure 5.

Tub displacement magnitude (in-plane)

- I In the Home toolbar, click **Add Plot Group** and choose Polar Plot Group.
- 2 In the Settings window for Polar Plot Group, type Tub displacement magnitude (inplane) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Global I

- I Right-click Tub displacement magnitude (in-plane) and choose Global.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the r-Axis Data section. From the menu, choose Component I (compl)>Definitions> Variables>uin_tub - Tub displacement magnitude (in-plane) - m.
- **3** Locate the θ Angle Data section. From the Parameter list, choose Expression.
- 4 Click Replace Expression in the upper-right corner of the θ Angle Data section. From the menu, choose Component I (compl)>Definitions>Variables>th_drum - Drum rotation rad.
- 5 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 6 Click to expand the **Legends** section. Clear the **Show legends** check box.

Color Expression 1

- I Right-click Global I and choose Color Expression.
- 2 In the Settings window for Color Expression, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Solver>t - Time - s.
- 3 Locate the Coloring and Style section. From the Color table transformation list, choose Reverse.
- 5 Click the **Zoom Extents** button in the **Graphics** toolbar.

Tub displacement magnitude (in-plane)

In the Model Builder window, under Results right-click Tub displacement magnitude (inplane) and choose Duplicate.

Tub displacement magnitude (out-of-plane)

- I In the Model Builder window, under Results click Tub displacement magnitude (inplane) I.
- 2 In the Settings window for Polar Plot Group, type Tub displacement magnitude (out-of-plane) in the **Label** text field.

Global I

- I In the Model Builder window, expand the Tub displacement magnitude (out-of-plane) node, then click Global 1.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the r-Axis Data section. From the menu, choose Component I (compl)>Definitions> Variables>uout_tub - Tub displacement magnitude (out-of-plane) - m.
- 4 Click the **Zoom Extents** button in the **Graphics** toolbar.

Use the instructions below to generate the plot of the tub rotation and stabilizing springs extension shown in Figure 6 and Figure 7 respectively.

Tub rotation

- I In the Home toolbar, click <a> Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Tub rotation in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the **Plot Settings** section.
- 6 Select the x-axis label check box. In the associated text field, type Number of cycles.

7 Select the y-axis label check box. In the associated text field, type Tub rotation (deg).

Global I

- I Right-click **Tub rotation** and choose **Global**.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Rigid domains>Tub>Rigid body rotation (spatial frame) - rad> mbd.rd3.thx - Rigid body rotation, x-component.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Rigid domains>Tub> Rigid body rotation (spatial frame) - rad>mbd.rd3.thy - Rigid body rotation, y-component.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Rigid domains>Tub> Rigid body rotation (spatial frame) - rad>mbd.rd3.thz - Rigid body rotation, z-component. Change the units to degrees from radians.
- **5** Locate the **y-Axis Data** section. In the table, enter the following settings:

Expression	Unit	Description
mbd.rd3.thx	deg	Rigid body rotation, x-component
mbd.rd3.thy	deg	Rigid body rotation, y-component
mbd.rd3.thz	deg	Rigid body rotation, z-component

- 6 Click Replace Expression in the upper-right corner of the x-Axis Data section. From the menu, choose Component I (compl)>Definitions>Variables>n_cycle - Number of cycles -Ι.
- 7 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 8 Find the Line markers subsection. From the Marker list, choose Cycle.
- **9** From the **Positioning** list, choose **Interpolated**.
- 10 In the Number text field, type 20.
- II Click to expand the Legends section. From the Legends list, choose Manual.
- **12** In the table, enter the following settings:

Legends		
x-component		
y-component		
z-component		

13 In the **Tub rotation** toolbar, click **Plot**.

To plot the strut displacement and the energy dissipation rate in the struts as shown in Figure 8 and Figure 9 respectively, follow the instructions below.

14 Click the Zoom Extents button in the Graphics toolbar.

Tub rotation

In the Model Builder window, right-click Tub rotation and choose Duplicate.

Stabilizing spring extension

- I In the Model Builder window, under Results click Tub rotation I.
- 2 In the Settings window for ID Plot Group, type Stabilizing spring extension in the **Label** text field.
- 3 Locate the Plot Settings section. Clear the y-axis label check box.
- 4 Locate the Legend section. From the Position list, choose Lower left.

Global I

- I In the Model Builder window, expand the Stabilizing spring extension node, then click
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Spring-Dampers>Housing-tub (front)>mbd.spd1.dl -Spring extension - m.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Spring-Dampers>Housingtub (back)>mbd.spd2.dl - Spring extension - m.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends			
Front spring			
Back spring			

- 5 In the Stabilizing spring extension toolbar, click Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Stabilizing spring extension

In the Model Builder window, right-click Stabilizing spring extension and choose Duplicate.

Strut displacement

- I In the Model Builder window, under Results click Stabilizing spring extension I.
- 2 In the Settings window for ID Plot Group, type Strut displacement in the Label text field.
- 3 Locate the Legend section. From the Position list, choose Upper right.

Global I

- I In the Model Builder window, expand the Strut displacement node, then click Global I.
- 2 In the Settings window for Global, click Replace Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)> Multibody Dynamics>Prismatic joints>Cylinder I-piston I>mbd.prjI.u -Relative displacement - m.
- 3 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Prismatic joints>Cylinder 2piston 2>mbd.prj2.u - Relative displacement - m.
- 4 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Prismatic joints>Cylinder 3piston 3>mbd.prj3.u - Relative displacement - m.
- 5 Click Add Expression in the upper-right corner of the y-Axis Data section. From the menu, choose Component I (compl)>Multibody Dynamics>Prismatic joints>Cylinder 4piston 4>mbd.prj4.u - Relative displacement - m.
- **6** Locate the **Legends** section. In the table, enter the following settings:

Legends				
Strut	1			
Strut	2			
Strut	3			
Strut	4			

- 7 In the Strut displacement toolbar, click **Plot**.
- 8 Click the **Zoom Extents** button in the **Graphics** toolbar.

Strut displacement

In the Model Builder window, right-click Strut displacement and choose Duplicate.

Energy dissipation rate

I In the Model Builder window, under Results click Strut displacement I.

2 In the Settings window for ID Plot Group, type Energy dissipation rate in the Label text field.

Global I

- I In the Model Builder window, expand the Energy dissipation rate node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
mbd.prj1.Qdamper	W	Energy dissipation rate in damper
mbd.prj2.Qdamper	W	Energy dissipation rate in damper
mbd.prj3.Qdamper	W	Energy dissipation rate in damper
mbd.prj4.Qdamper	W	Energy dissipation rate in damper

- 4 In the Energy dissipation rate toolbar, click **Plot**.
- 5 Click the Zoom Extents button in the Graphics toolbar.

Use the instructions below to plot the shell deformation components at the mountings and the side wall as shown in Figure 10 and Figure 11 respectively.

Energy dissipation rate

In the Model Builder window, right-click Energy dissipation rate and choose Duplicate.

Shell deformation (mountings)

- I In the Model Builder window, under Results click Energy dissipation rate I.
- 2 In the Settings window for ID Plot Group, type Shell deformation (mountings) in the Label text field.
- 3 Locate the Title section. From the Title type list, choose Label.

Global I

- I In the Model Builder window, expand the Shell deformation (mountings) node, then click Global I.
- 2 In the Settings window for Global, locate the y-Axis Data section.
- **3** In the table, enter the following settings:

Expression	Unit	Description	
shell.att3.w	mm	Rigid body displacement, z-component	
shell.att4.w	mm	Rigid body displacement, z-component	

Expression	Unit	Description
shell.att5.w	mm	Rigid body displacement, z-component
shell.att6.w	mm	Rigid body displacement, z-component

4 Locate the **Legends** section. In the table, enter the following settings:

Legends Mounting 1 Mounting 2 Mounting 3 Mounting 4

- 5 In the Shell deformation (mountings) toolbar, click Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

Cut Point 3D I

- I In the Results toolbar, click Cut Point 3D.
- 2 In the Settings window for Cut Point 3D, locate the Data section.
- 3 From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Locate the **Point Data** section. In the **X** text field, type 600.
- 5 In the Y text field, type 250.
- 6 In the **Z** text field, type 450.
- 7 From the Snapping list, choose Snap to closest boundary.
- 8 Click Plot.

Shell deformation (side wall)

- I In the Results toolbar, click \(\subseteq ID Plot Group. \)
- 2 In the Settings window for ID Plot Group, type Shell deformation (side wall) in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Cut Point 3D 1.
- 4 Locate the Title section. From the Title type list, choose Label.
- 5 Locate the Plot Settings section.
- 6 Select the x-axis label check box. In the associated text field, type Number of cycles.
- 7 Select the y-axis label check box. In the associated text field, type Displacement (mm).
- **8** Locate the **Legend** section. From the **Position** list, choose **Lower left**.

Point Graph 1

- I Right-click Shell deformation (side wall) and choose Point Graph.
- 2 In the Settings window for Point Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type u2.
- 4 Click Replace Expression in the upper-right corner of the x-Axis Data section. From the menu, choose Component I (compl)>Definitions>Variables>n_cycle - Number of cycles -1.
- 5 Click to expand the Coloring and Style section. From the Width list, choose 2.
- 6 Find the Line markers subsection. From the Marker list, choose Cycle.
- 7 From the Positioning list, choose Interpolated.
- 8 In the Number text field, type 20.
- **9** Click to expand the **Legends** section. Select the **Show legends** check box.
- 10 From the Legends list, choose Manual.
- II In the table, enter the following settings:

Legends x-component

12 Right-click Point Graph I and choose Duplicate.

Point Graph 2

- I In the Model Builder window, click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type v2.
- **4** Locate the **Legends** section. In the table, enter the following settings:

Legends y-component

5 Right-click Point Graph 2 and choose Duplicate.

Point Graph 3

- I In the Model Builder window, click Point Graph 3.
- 2 In the Settings window for Point Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type w2.

4 Locate the **Legends** section. In the table, enter the following settings:

Legends z-component

- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.