

Decorative Plating

This tutorial model of decorative electroplating models a secondary current distribution with full Butler-Volmer kinetics for both anode and cathode. The thickness of the deposited layer at the cathode is computed along with the surface thickness change on the anode caused by metal dissolution.

A more detailed description of how to build this model, including screenshots, can be found in the Introduction to the Electrodeposition Module book.

Model Definition

The model geometry is shown in Figure 1. The anode is a planar dissolving anode. The cathode represents a furniture fitting that is to be decorated by metal plating.

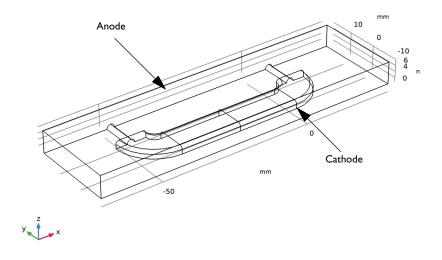


Figure 1: The model geometry.

The conductivity of the metal of the anode and cathode is very high compared to that of the electrolyte and it is thus assumed that the electric potential in the metal is constant. Variations in the activation overpotential are therefore caused by the potential in the electrolyte at the surface of the electrodes. Under these assumptions, the electrodes are treated as boundaries in the simulations.

Before beginning, one difficulty found in all current density distribution models needs to be discussed. The overpotential, η_m , for an electrode reaction of index m, is defined according to the following equation:

$$\eta = \phi_{s, 0} - \phi_l - E_{eq, m}$$

where $\phi_{s,0}$ denotes the electric potential of the metal, ϕ_l denotes the potential in the electrolyte, and $E_{\mathrm{eq},m}$ denotes the difference between the metal and electrolyte potentials at the electrode surface, measured at equilibrium using a common reference potential. The electric potential of one of the electrodes may be bootstrapped, so that all other potentials are measured with this reference (this bootstrap can actually be achieved by fixing the potential at any point in the cell). In this case, the electric potential of the metal is selected at the cathode as a bootstrap by setting this potential to 0 V. This implies that the electric potential of the metal at the anode is equal to the cell voltage. The potential of the electrolyte floats and adapts to satisfy the balance of current, so that an equal amount of current that leaves at the cathode also enters at the anode. This then determines the overpotential at the anode and the cathode.

ELECTROLYTE CHARGE TRANSPORT

Use the Secondary Current Distribution interface to solve for the electrolyte potential, ϕ_I (SI unit: V), according to

$$\mathbf{i}_l = -\sigma_l \nabla \phi_l$$
$$\nabla \cdot \mathbf{i}_l = 0$$

where \mathbf{i}_I (SI unit: A/m²) is the electrolyte current density vector and σ_I (SI unit: S/m) is the electrolyte conductivity, which is assumed to be a constant.

Use the default Insulation condition for all boundaries except the anode and cathode surfaces:

$$\mathbf{n} \cdot \mathbf{i}_I = 0$$

where \mathbf{n} is the normal vector, pointing out of the domain.

The main electrode reaction on both the anode and the cathode surfaces is the nickel deposition/dissolution reaction according to

$$Ni^{2+} + 2e^- \Leftrightarrow Ni(s)$$

Use a Butler-Volmer expression to model this reaction; this sets the local current density to

$$i_{\text{loc, Ni}} = i_{0, \text{Ni}} \left(\exp \left(\frac{\alpha_a F \eta_{\text{Ni}}}{RT} \right) - \exp \left(-\frac{\alpha_c F \eta_{\text{Ni}}}{RT} \right) \right)$$

The rate of deposition at the cathode boundary surfaces and the rate of dissolution at the anode boundary surface, with a velocity in the normal direction, v (m/s), is calculated according to

$$v = \frac{i_{\text{loc, Ni}} M}{nF} \frac{M}{\rho}$$

where M is the mean molar mass (59 g/mol) and ρ is the density (8900 kg/m³) of the nickel atoms and n is number of participating electrons. Note that the local current density is positive at the anode surface and negative at the cathode surfaces.

On the anode the electrolyte current density is set to the local current density of the nickel deposition reaction:

$$\mathbf{n} \cdot \mathbf{i}_l = i_{\text{loc. Ni}}$$

On the cathode, add a second electrode reaction to model the parasitic hydrogen evolution reaction:

$$2H^+ + 2e^- \Leftrightarrow H_2$$

Use a cathodic Tafel equation to model the kinetics of the hydrogen reaction on the cathode, this sets the local current density to

$$i_{\text{loc, H}} = -i_{0, H} 10^{-\eta_H/A_c}$$

The hydrogen reaction does not contribute to the rate of deposition of nickel, but it contributes to the total current density at the cathode surface:

$$\mathbf{n} \cdot \mathbf{i}_l = i_{\text{loc. Ni}} + i_{\text{loc. H}}$$

Solve the model in a time-dependent study, simulating the electroplating for 600 s.

Results and Discussion

Figure 2 shows the change in the total electrode thickness for the cathode surfaces indicating the deposition thickness after 600 s. It can be seen that the deposition thickness

is quite nonuniform. The lowest deposition thickness is found at the bottom end of the cathode geometry, farthest from the anode surface. The deposition thickness could be optimized further by changing design parameters such as plating cell geometry, distance between the anode and cathode surface, conductivity of the electrolyte and operational parameters such as applied current or potential.

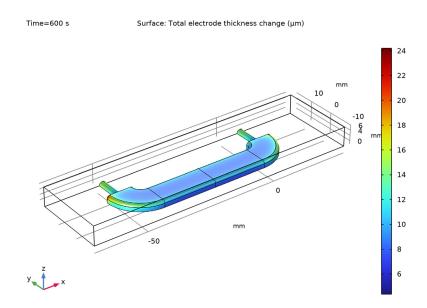


Figure 2: The simulated results of the change in the total electrode thickness.

Figure 3 shows the local current efficiency over the cathode surface. The efficiency is calculated as the nickel deposition current density divided by the total current density at the cathode. The efficiency is about 97%.



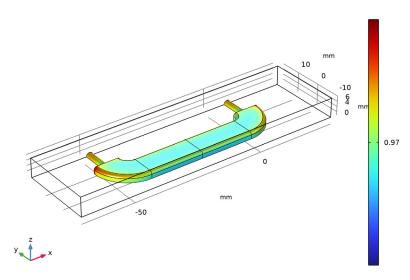


Figure 3: The current efficiency factor at the cathode.

Application Library path: Electrodeposition_Module/Tutorials/ decorative_plating

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

I In the Model Wizard window, click **1** 3D.

- 2 In the Select Physics tree, select Electrochemistry> Primary and Secondary Current Distribution > Secondary Current Distribution (cd).
- 3 Click Add.
- 4 Click Study.
- 5 In the Select Study tree, select Preset Studies for Selected Physics Interfaces> Time Dependent with Initialization.
- 6 Click M Done.

GLOBAL DEFINITIONS

Load the model parameters from a text file.

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file decorative plating parameters.txt.

GEOMETRY I

The model geometry is available as a parameterized geometry sequence in a separate MPH-file. If you want to build it from scratch, follow the instructions in the section Appendix — Geometry Modeling Instructions. Otherwise load it from file with the following steps.

- I In the Geometry toolbar, click Insert Sequence and choose Insert Sequence.
- **2** Browse to the model's Application Libraries folder and double-click the file decorative plating geom sequence.mph.
- 3 In the Geometry toolbar, click Build All.
- 4 Click the Wireframe Rendering button in the Graphics toolbar.
- 5 In the Model Builder window, under Component I (compl) right-click Geometry I and choose Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

SECONDARY CURRENT DISTRIBUTION (CD)

Now start setting up the current distribution model, beginning with the settings for the electrolyte.

Electrolyte I

- I In the Model Builder window, under Component I (compl)> Secondary Current Distribution (cd) click Electrolyte 1.
- 2 In the Settings window for Electrolyte, locate the Electrolyte section.
- **3** From the σ_l list, choose **User defined**. In the associated text field, type kappa.

Electrode Surface I

Now define the anode and the nickel dissolution-deposition electrode reaction on this surface. The combination of the properties of the surface and the reaction stoichiometry will determine how the magnitude and direction of the growth velocity of the deposited layer relates to the electrode reaction currents.

- I In the Physics toolbar, click **Boundaries** and choose **Electrode Surface**.
- 2 Select Boundary 4 only.

Keep the default boundary condition for this surface, setting the electric potential to zero (grounding the electrode).

- 3 In the Settings window for Electrode Surface, click to expand the Dissolving-**Depositing Species** section.
- 4 Click + Add.
- 5 In the table, enter the following settings:

Species	Density (kg/m^3)	Molar mass (kg/mol)
Ni	rho_Ni	M_Ni

Electrode Reaction 1

Set the first electrode reaction to be the nickel deposition reaction.

- I In the Model Builder window, click Electrode Reaction I.
- 2 In the Settings window for Electrode Reaction, locate the Stoichiometric Coefficients section.
- **3** In the n text field, type 2.
- 4 In the Stoichiometric coefficients for dissolving-depositing species: table, enter the following settings:

Species	Stoichiometric coefficient (I)
Ni	1

5 Locate the **Equilibrium Potential** section. In the E_{eq} text field, type Eeq_Ni.

- 6 Locate the Electrode Kinetics section. From the Kinetics expression type list, choose Butler-Volmer.
- **7** In the i_0 text field, type i0_Ni.

Electrode Surface 1

Now duplicate this node to define the cathode.

I In the Model Builder window, right-click Electrode Surface I and choose Duplicate.

Electrode Surface 2

- I In the Model Builder window, click Electrode Surface 2.
- 2 In the Settings window for Electrode Surface, locate the Boundary Selection section.
- 3 From the Selection list, choose Cathode.
- 4 Locate the Electrode Phase Potential Condition section. From the Electrode phase potential condition list, choose Average current density.
- **5** In the $i_{l,average}$ text field, type Iavg.

Electrode Reaction 1

- I In the Model Builder window, expand the Electrode Surface 2 node, then click Electrode Reaction 1.
- 2 In the Settings window for Electrode Reaction, locate the Stoichiometric Coefficients section.
- 3 In the Stoichiometric coefficients for dissolving-depositing species: table, enter the following settings:

Species	Stoichiometric coefficient (I)
Ni	1

Electrode Surface 2

Add the hydrogen evolution reaction.

In the Model Builder window, click Electrode Surface 2.

Electrode Reaction 2

- I In the Physics toolbar, click 🖳 Attributes and choose Electrode Reaction.
- 2 In the Settings window for Electrode Reaction, locate the Electrode Kinetics section.
- 3 From the Kinetics expression type list, choose Cathodic Tafel equation.
- **4** In the i_0 text field, type i0_H.

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Physics-Controlled Mesh section.
- **3** From the **Element size** list, choose **Finer**.
- 4 Click **Build All**.
- 5 Right-click Component I (compl)>Mesh I and choose Plot.
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.

STUDY I

Step 1: Current Distribution Initialization

- I In the Model Builder window, under Study I click
 - Step 1: Current Distribution Initialization.
- 2 In the Settings window for Current Distribution Initialization, locate the Study Settings section.
- 3 From the Current distribution type list, choose Secondary.

Step 2: Time Dependent

- I In the Model Builder window, click Step 2: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- 3 In the Output times text field, type range (0,60,600).
- 4 In the Home toolbar, click **Compute**.

RESULTS

Deposited Thickness, Cathode

Modify the default plot for the electrode thickness change to show the deposited thickness on the cathode only.

- I In the Model Builder window, under Results click Total Electrode Thickness Change (cd).
- 2 In the Settings window for 3D Plot Group, click to expand the Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Cathode.
- 5 In the Total Electrode Thickness Change (cd) toolbar, click In the Total Electrode Thickness Change (cd) toolbar, click
- 6 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 7 Right-click Results>Total Electrode Thickness Change (cd) and choose Rename.

- 8 In the Rename 3D Plot Group dialog box, type Deposited Thickness, Cathode in the New label text field.
- 9 Click OK.
- **10** Right-click **Results>Deposited Thickness**, **Cathode** and choose **Duplicate**.

Surface I

- In the Model Builder window, expand the Deposited Thickness, Cathode I node, then click Surface I.
- 2 In the Settings window for Surface, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Secondary Current Distribution>Electrode kinetics>cd.iloc_erl Local current density A/m².

Divide the current density of the nickel reaction with the total current density variable.

- 3 Locate the Expression section. In the Expression text field, type cd.iloc er1/cd.itot.
- 4 In the Deposited Thickness, Cathode I toolbar, click **Plot**.
- **5** Click the **Zoom Extents** button in the **Graphics** toolbar.

Current Efficiency, Cathode

- I In the Model Builder window, right-click Deposited Thickness, Cathode I and choose Rename.
- 2 In the Rename 3D Plot Group dialog box, type Current Efficiency, Cathode in the New label text field.
- 3 Click OK.

Appendix — Geometry Modeling Instructions

ADD COMPONENT

- I In the Model Builder window, expand the Results node.
- 2 Right-click the root node and choose Add Component>3D.

DEFINITIONS

In the Model Builder window, expand the Component I (compl)>Definitions node.

View 1

- I In the Model Builder window, expand the Component I (compl)>Definitions>View I node, then click View I.
- 2 In the Settings window for View, locate the View section.

3 Select the Wireframe rendering check box.

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Units section.
- 3 From the Length unit list, choose mm.

Block I (blk I)

- I In the Geometry toolbar, click Block.
- 2 In the Settings window for Block, locate the Size and Shape section.
- 3 In the Width text field, type 100.
- 4 In the Depth text field, type 28.
- 5 In the Height text field, type 7.25.
- 6 Locate the Position section. In the x text field, type -70.
- 7 In the y text field, type 10.
- 8 In the z text field, type -1.25.
- 9 Locate the Selections of Resulting Entities section. Select the Resulting objects selection check box.

Cylinder I (cyll)

- I In the Geometry toolbar, click (Cylinder.
- 2 In the Settings window for Cylinder, locate the Size and Shape section.
- 3 In the Radius text field, type 1.25.
- 4 In the **Height** text field, type 10.
- **5** Locate the **Position** section. In the **x** text field, type -48.
- 6 In the y text field, type 8.
- 7 In the z text field, type -1.25.
- 8 Locate the Axis section. From the Axis type list, choose y-axis.

Cumulative Selections

In the Geometry toolbar, click Selections and choose Cumulative Selections.

Objects to subtract

- I Right-click Cumulative Selections and choose Cumulative Selection.
- 2 In the Settings window for Selection, type Objects to subtract in the Label text field.

Cylinder I (cyll)

- I In the Model Builder window, under Component I (compl)>Geometry I click Cylinder I (cyll).
- 2 In the Settings window for Cylinder, locate the Selections of Resulting Entities section.
- **3** Find the **Cumulative selection** subsection. From the **Contribute to** list, choose **Objects to subtract**.

Work Plane I (wpl)

- I In the Geometry toolbar, click Work Plane.
- 2 In the Settings window for Work Plane, locate the Plane Definition section.
- 3 From the Plane list, choose zx-plane.
- 4 In the y-coordinate text field, type 8.

Work Plane I (wp I)>Plane Geometry

In the Model Builder window, click Plane Geometry.

Work Plane I (wp I)>Rectangle I (r I)

- I In the Work Plane toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 2.5.
- 4 In the Height text field, type 10.
- **5** Locate the **Position** section. In the **xw** text field, type -1.25.
- 6 In the yw text field, type -53.

Work Plane I (wbl)>Fillet I (fill)

- I In the Work Plane toolbar, click Fillet.
- 2 On the object r1, select Points 2 and 3 only.
- 3 In the Settings window for Fillet, locate the Radius section.
- 4 In the Radius text field, type 1.

View 2

- I In the Model Builder window, expand the Component I (compl)>Geometry I> Work Plane I (wpl)>View 2 node, then click View 2.
- 2 On the object r1, select Point 3 only.

Work Plane I (wpl)>Fillet I (fill)

I In the Model Builder window, under Component I (compl)>Geometry I> Work Plane I (wpl)>Plane Geometry click Fillet I (fill).

2 In the Settings window for Fillet, click | Build Selected.

Revolve I (rev I)

- I In the **Geometry** toolbar, click **Revolve**.
- 2 In the Settings window for Revolve, locate the Revolution Angles section.
- 3 Clear the **Keep original faces** check box.
- 4 Click the Angles button.
- 5 In the End angle text field, type 90.
- 6 Locate the Revolution Axis section. From the Axis type list, choose 3D.
- 7 Find the Point on the revolution axis subsection. In the x text field, type -40.
- **8** In the **y** text field, type **8**.
- 9 In the z text field, type -1.25.
- 10 Find the Direction of revolution axis subsection. In the y text field, type 0.
- II In the z text field, type 1.
- 12 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Objects to subtract.

Extrude | (ext|)

- I In the Geometry toolbar, click Extrude.
- 2 In the Settings window for Extrude, locate the General section.
- 3 From the Input objects list, choose Objects to subtract.
- 4 From the Extrude from list, choose Faces.
- 5 From the Input faces list, choose Objects to subtract.
- 6 In the tree, select cyll.
- 7 Click the Remove from Selection button for Input faces.
- **8** On the object **cyll**, select Boundaries 1–6 only.
- **9** On the object **rev1**, select Boundaries 1–8 only.
- **10** Click the **Remove from Selection** button for **Input faces**.
- II On the object cyll, select Boundaries 1–6 only.
- 12 On the object rev1, select Boundaries 1–8 only.
- 13 In the tree, select cyll>1 (not applicable), cyll>2 (not applicable), cyll>3, cyll>4, cyll> 5 (not applicable), and cyll>6 (not applicable).
- **14** Click the Remove from Selection button for Input faces.

- **15** On the object **rev1**, select Boundaries 1–8 only.
- 16 In the tree, select revi>1, revi>2 (not applicable), revi>3, revi>4 (not applicable), revi> 5, rev1>6 (not applicable), and rev1>7 (not applicable).
- 17 Click the Remove from Selection button for Input faces.
- **18** On the object **rev1**, select Boundary 8 only.
- 19 In the tree, select rev1>8.
- **20** Locate the **Distances** section. In the table, enter the following settings:

Distances (mm) 20

- 21 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Objects to subtract.
- **22** Click **P** Build Selected.

Mirror I (mir I)

- I In the Model Builder window, right-click Geometry I and choose Transforms>Mirror.
- 2 In the Settings window for Mirror, locate the Input section.
- 3 From the Input objects list, choose Objects to subtract.
- 4 Select the **Keep input objects** check box.
- 5 Locate the Point on Plane of Reflection section. In the x text field, type -20.
- 6 Locate the Normal Vector to Plane of Reflection section. In the x text field, type 1.
- 7 In the z text field, type 0.
- 8 Locate the Selections of Resulting Entities section. Find the Cumulative selection subsection. From the Contribute to list, choose Objects to subtract.

Difference I (dif1)

- I In the Geometry toolbar, click Booleans and Partitions and choose Difference.
- 2 In the Settings window for Difference, locate the Difference section.
- 3 From the Objects to add list, choose Block 1.
- 4 From the Objects to subtract list, choose Objects to subtract.

Cathode

- I In the Geometry toolbar, click \(\frac{1}{2} \) Selections and choose Box Selection.
- 2 In the Settings window for Box Selection, type Cathode in the Label text field.
- 3 Locate the Geometric Entity Level section. From the Level list, choose Boundary.

- 4 Locate the **Box Limits** section. In the **x minimum** text field, type -55.
- 5 In the x maximum text field, type 15.
- 6 In the y minimum text field, type -8.
- 7 In the y maximum text field, type 15.
- **8** In the **z minimum** text field, type 0.
- 9 In the z maximum text field, type 4.