

Uncertainty Quantification of a Bracket — Fillet Version

This example demonstrates how to use the Uncertainty Quantification Module by running a series of uncertainty quantification studies for a steel bracket.

This type of bracket can be used to install an actuator that is mounted on a pin placed between the two holes in the bracket arms. The design objective is that the actuator's horizontal misalignment, φ , should not be too large.

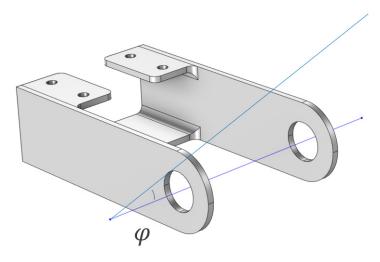


Figure 1: Bracket geometry with the quantity of interest, the misalignment angle, φ , indicated.

Note: The geometry is created using the 3D fillet functionality that is available in the Design Module. If you do not have access to the Design Module, a version without 3D fillets is also provided; see Uncertainty Quantification of a Bracket. A few of the model parameters are slightly changed for the version without fillets but otherwise the instructions are identical.

The geometry is fully parameterized with parameters according to the table shown in Figure 2.

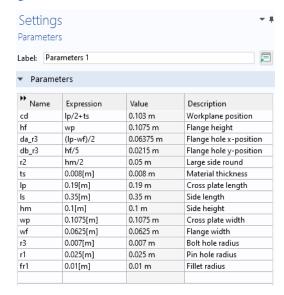


Figure 2: Geometry parameters.

The mesh is customized to have about two elements across the thickness of the material.

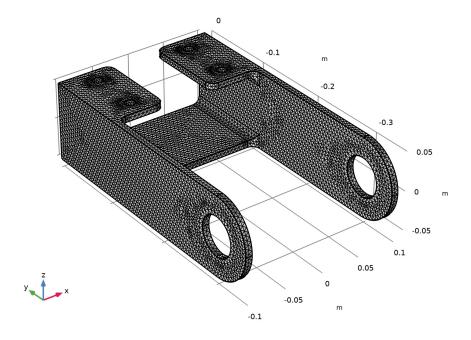


Figure 3: Meshed geometry.

In this analysis, the mounting bolts are assumed to be fixed and securely bonded to the bracket. One of the arms is loaded upward and the other downward. The loads are applied as a pressure on the inner surfaces of the holes, and their intensity is $P_0\cos(\alpha)$, where α is the angle from the direction of the load resultants.

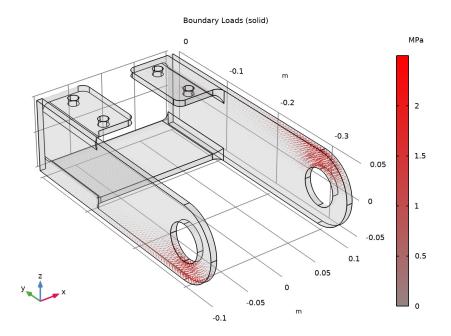


Figure 4: Applied loads.

This force is assumed not to vary in the uncertainty quantification studies. Similarly, the material properties for a generic structural steel are assumed not to vary.

The misalignment angle is chosen as the quantity of interest (QoI). The design objective is that the actuator's horizontal misalignment angle φ does not exceed 0.1 degree. The angle is defined as a global variable; for details, see the Modeling Instructions section.

The parameters to be varied are the geometric dimensions of the bracket.

The parameters that participate in the uncertainty quantification are all assumed to be normally distributed around their nominal values according to the table in Figure 5, which corresponds to the screening and sensitivity studies, as described later.

Parameter		Distribution		Distribution parameter 1	Distribution parameter 2	CDF-Lower	CDF-Upper	Lower bound	Upper bound	Unit
	•	Normal(μ,σ)	•	ts	0.01*ts	Manual ▼	Manual ▼	0.99*ts	1.01*ts	m
lp (Cross plate length)	•	Normal(μ,σ)	•	lp	0.01*lp	Manual ▼	Manual ▼	0.95*lp	1.05*lp	m
Is (Side length)	•	Normal(μ,σ)	•	Is	0.01*Is	Manual ▼	Manual ▼	0.95*Is	1.05*Is	m
hm (Side height)	•	Normal(μ,σ)	•	hm	0.01*hm	Manual ▼	Manual ▼	0.95*hm	1.05*hm	m
wp (Cross plate width)	•	Normal(μ,σ)	•	wp	0.01*wp	Manual ▼	Manual ▼	0.95*wp	1.05*wp	m
wf (Flange width)	•	Normal(μ,σ)	•	wf	0.01*wf	Manual ▼	Manual ▼	0.95*wf	1.05*wf	m
fr1 (Fillet radius)	•	Normal(μ,σ)	•	fr1	0.01*fr1	Manual ▼	Manual ▼	0.95*fr1	1.05*fr1	m
r1 (Pin hole radius)		Normal(μ,σ)		r1	0.01*r1	Manual ▼	Manual ▼	0.95*r1	1.05*r1	m

Figure 5: Input-parameter distributions used in screening and sensitivity studies.

THE UNCERTAINTY QUANTIFICATION STUDIES

The Uncertainty Quantification Module provides four different study types:

- · Screening, MOAT
 - Identifies the most influential inputs, for each QoI
 - Is based on the Morris One-At-a-Time (MOAT) method
 - Outputs MOAT mean and MOAT standard deviation values
- · Sensitivity Analysis
 - Computes the fraction of impact for the inputs, for each QoI
 - Outputs first-order and total Sobol indices
- Uncertainty Propagation
 - Computes the statistical variation of the QoI
 - Outputs a kernel density estimation (KDE) plot representing an estimate of the probability distribution of the QoI
- Reliability Analysis
 - Computes the probability for the fulfillment of a condition based on the QoI
 - For example, what is the probability $P(\phi > 0.1)$

For more information, see the Uncertainty Quantification Module User's Guide.

SURROGATE MODELS

To get statistical data based on a physics model you need to run a lot of simulations, varying the parameters of the inputs according to their probability distributions. For a 3D model, this might be computationally unfeasible. To get around this problem, the Uncertainty Quantification Module first builds up a so-called surrogate model that is used

for sensitivity analysis, uncertainty propagation, and reliability analysis (but not for screening).

This process is typically adaptive and the surrogate model can approximate the original model to a high degree of accuracy (which can be modified by the user). The Uncertainty Quantification Module uses two different types of surrogate models:

- Sparse Polynomial Chaos Expansion (SPCE)
 - This surrogate model improves its accuracy by adaptively solving the full model and thereby adding new QoI data by using sequential Latin hypercube sampling.
- Gaussian Process (GP)
 - This surrogate model improves its accuracy by, using information from the current Gaussian Process surrogate model, adaptively solve the full model for new carefully selected sets of parameter values.

Results and Discussion

The uncertainty quantification study gives the kernel density estimation plot shown in Figure 6 with associated confidence interval information in the QOI confidence interval table, as shown in Figure 7.

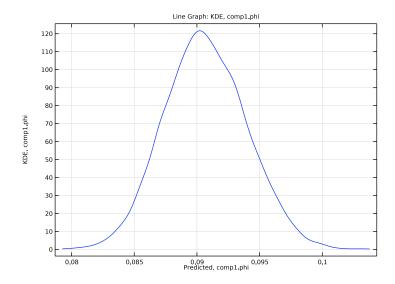


Figure 6: Kernel density estimation.

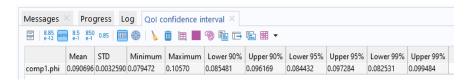


Figure 7: QoI confidence interval.

The reliability analysis study shows that the probability for the misalignment angle φ not to exceed 0.1 degree is about 0.003 or 0.3%. This result is made available in the **Probability** for conditions table, as shown in Figure 8.



Figure 8: Probability for conditions.

Note that this value is sensitive to minute changes in the mesh and may vary slightly depending on the COMSOL Multiphysics version you are running.

It is now up to the designer to decide whether this is an acceptable level or risk or if a redesign and/or further studies are needed.

To be more conservative about the uncertainty propagation and reliability analysis, we can choose to include all parameters in the analysis. Running the computationally much more demanding uncertainty propagation and reliability analysis for all parameters (not demonstrated here) shows that the probability for the misalignment angle φ not to exceed 0.1 degree is about 0.8%.

Application Library path: Uncertainty Quantification Module/Tutorials/ bracket_uncertainty_quantification_fillet

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 1 3D.
- 2 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 3 Click Add.
- 4 Click 🔵 Study.
- 5 In the Select Study tree, select General Studies>Stationary.
- 6 Click **Done**.

GEOMETRY I

- I In the Model Builder window, under Component I (compl) click Geometry I.
- 2 In the Settings window for Geometry, locate the Advanced section.
- **3** From the **Geometry representation** list, choose **CAD kernel**. This is necessary because the prepared geometry sequence contains a **Fillet** feature.
- 4 In the Geometry toolbar, click Insert Sequence and choose Insert Sequence.
- **5** Browse to the model's Application Libraries folder and double-click the file bracket_uncertainty_quantification_fillet_geom_sequence.mph.
- 6 In the Geometry toolbar, click **Build All**.

GLOBAL DEFINITIONS

The geometry sequence already provided a set of geometry dimension parameters. Now define this additional set of parameters for the boundary load and mesh density.

Parameters 2

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, locate the Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
Р0	2.5[MPa]	2.5E6 Pa	Force per area
dx	lp+ts	0.198 m	X-distance between pin holes
hmax	ts/1.5	0.0053333 m	Max element size
hmin	ts/2.5	0.0032 m	Min element size
YC	-ls+r2	-0.3 m	Y-coordinate of hole center

ADD MATERIAL

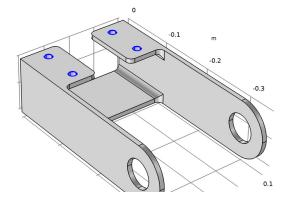
- I In the Home toolbar, click 👯 Add Material to open the Add Material window.
- 2 Go to the Add Material window.
- 3 In the tree, select Built-in>Structural steel.
- 4 Click Add to Component in the window toolbar.
- 5 In the Home toolbar, click **‡ Add Material** to close the **Add Material** window.

DEFINITIONS

Next, define a series of **Explicit** selections to be used for the constraints and loads.

Bolt Holes

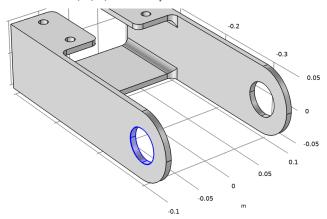
- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click Definitions and choose Selections>Explicit.
- 3 In the Settings window for Explicit, locate the Input Entities section.
- 4 From the Geometric entity level list, choose Boundary.
- 5 Select the **Group by continuous tangent** check box. This setting greatly facilitates the selection of curved surfaces. In this case use it to select the four bolt holes. It is sufficient to select one boundary per hole; the three other boundaries will be selected automatically.



6 In the Label text field, type Bolt Holes.

Left Pin Hole

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select the Group by continuous tangent check box.
- **5** Select Boundaries 4, 5, 7, and 8 only.

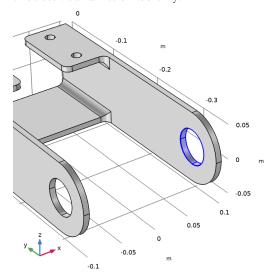


6 In the Label text field, type Left Pin Hole.

Right Pin Hole

- I In the **Definitions** toolbar, click **\(\frac{1}{2} \) Explicit**.
- 2 In the Settings window for Explicit, locate the Input Entities section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 Select the Group by continuous tangent check box.

5 Select Boundaries 52–55 only.



6 In the Label text field, type Right Pin Hole.

Pin Holes

- I In the **Definitions** toolbar, click **Union**.
- 2 In the Settings window for Union, locate the Geometric Entity Level section.
- 3 From the Level list, choose Boundary.
- **4** Locate the **Input Entities** section. Under **Selections to add**, click + **Add**.
- 5 In the Add dialog box, in the Selections to add list, choose Left Pin Hole and Right Pin Hole.
- 6 Click OK.
- 7 In the Settings window for Union, type Pin Holes in the Label text field.

Define average operators that will be used for computing the average z-directional displacement of the pin holes.

Average I (aveop I)

- I In the Definitions toolbar, click Monlocal Couplings and choose Average.
- 2 In the Settings window for Average, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Left Pin Hole.

Average 2 (aveop2)

- I In the **Definitions** toolbar, click **Monlocal Couplings** and choose **Average**.
- 2 In the Settings window for Average, locate the Source Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Right Pin Hole.

Variables 1

I Right-click **Definitions** and choose **Variables**.

Define the quantity of interest (QoI), the misalignment angle, as well as auxiliary variables for the pin hole z-coordinates.

- 2 In the Settings window for Variables, locate the Variables section.
- **3** In the table, enter the following settings:

Name	Expression	Unit	Description
z1	aveop1(w)	m	Left pin hole center
z2	aveop2(w)	m	Right pin hole center
phi	atan((z2-z1)/dx)[1/deg]		Misalignment angle

The output from the atan() function has the unit radian, which is unitless. The conversion factor [1/deg] corresponds to multiplication by 180/pi for converting to degrees.

Now, define an analytic function load used to apply the spatially varying load on the pin holes.

Analytic I (an I)

- I In the **Definitions** toolbar, click $\bigcap_{n=0}^{\infty}$ **Analytic**.
- 2 In the Settings window for Analytic, type load in the Function name text field.
- 3 Locate the **Definition** section. In the **Expression** text field, type F*cos(atan2(py, abs(px))).
- 4 In the Arguments text field, type F, py, px.
- 5 Locate the Units section. In the Function text field, type Pa.
- **6** In the table, enter the following settings:

Argument	Unit
F	Ра

Argument	Unit
ру	m
рх	m

MESH I

- I In the Model Builder window, under Component I (compl) click Mesh I.
- 2 In the Settings window for Mesh, locate the Sequence Type section.
- **3** From the list, choose **User-controlled mesh**.

Ensure that the mesh density is fine enough to resolve all the stress gradients reasonably well.

Size

- I In the Model Builder window, under Component I (compl)>Mesh I click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- 4 Locate the Element Size Parameters section. In the Maximum element size text field, type hmax.
- 5 In the Minimum element size text field, type hmin.
- 6 Click **Build All**.

SOLID MECHANICS (SOLID)

Apply fixed constraint boundary conditions on the bolt holes.

Fixed Constraint I

- I In the Model Builder window, under Component I (compl) right-click Solid Mechanics (solid) and choose Fixed Constraint.
- 2 In the Settings window for Fixed Constraint, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Bolt Holes**.

Next, apply the spatially varying load.

Boundary Load 1

- I In the Physics toolbar, click **Boundaries** and choose **Boundary Load**.
- 2 In the Settings window for Boundary Load, locate the Coordinate System Selection section.
- 3 From the Coordinate system list, choose Boundary System I (sysI).

4 Locate the **Force** section. Specify the \mathbf{F}_A vector as

0	tl
0	t2
load(-P0,Y-YC,Z)*(sign(X)*Z>0)	n

5 Locate the Boundary Selection section. From the Selection list, choose Pin Holes.

STUDY I, STATIC

First, run a static analysis with no uncertainty quantification analysis.

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study 1, Static in the Label text field.
- 3 In the Home toolbar, click **Compute**.

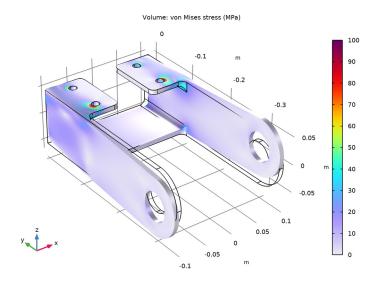
RESULTS

Volume I

Now, let us assume that we are only interested in values up to 100 MPa.

- I In the Model Builder window, expand the Stress (solid) node, then click Volume I.
- 2 In the Settings window for Volume, click to expand the Range section.
- 3 Locate the Expression section. From the Unit list, choose MPa.
- 4 In the Stress (solid) toolbar, click Plot.
- 5 Locate the Range section. Select the Manual color range check box.
- **6** In the **Minimum** text field, type **0**.
- 7 In the Maximum text field, type 100.

8 In the Stress (solid) toolbar, click Plot.



STUDY I, STATIC

In the Model Builder window, right-click Study I, Static and choose Uncertainty Quantification>Add Uncertainty Quantification Study Using Study Reference.

STUDY 2, SCREENING

In the Settings window for Study, type Study 2, Screening in the Label text field.

Next, add a screening analysis to see which input parameters are most significantly impacting the misalignment angle (QoI). The screening study is added as a study reference which means it refers back to the already defined static study.

The parameters that participate in the uncertainty quantification are all assumed to be normally distributed around their nominal values, according to the instructions below. The mean and standard deviation, as well as the max and min limits are all defined in terms of their nominal parameters (from Global Definitions>Parameters).

Uncertainty Quantification

- I In the Model Builder window, under Study 2, Screening click Uncertainty Quantification.
- 2 In the Settings window for Uncertainty Quantification, locate the Quantities of Interest section.
- 3 Click + Add.

4 In the table, enter the following settings:

Expression	Description	Individual solution to use
comp1.phi	Misalignment angle	From "Solution to use"

- **5** Locate the **Input Parameters** section. Click + **Add** eight times.
- **6** In the table, enter the following settings:

Parameter	Source type	Parameter description
ts (Material thickness)	Analytic	Uniform
lp (Cross-plate length)	Analytic	Uniform
Is (Side length)	Analytic	Uniform
hm (Side height)	Analytic	Uniform
wp (Cross-plate width)	Analytic	Uniform
wf (Flange width)	Analytic	Uniform
fr I (Fillet radius)	Analytic	Uniform
r1 (Pin-hole radius)	Analytic	Uniform

- 7 In the table, click to select the cell at row number 1 and column number 1.
- **8** From the **Distribution** list, choose **Normal**(μ , σ).
- 9 In the Mean text field, type ts.
- 10 In the Standard deviation text field, type 0.01*ts.
- II From the CDF-Lower list, choose Manual.
- 12 From the CDF-Upper list, choose Manual.
- **I3** In the **Lower bound** text field, type 0.99*ts.
- **14** In the **Upper bound** text field, type 1.01*ts.
- **I5** In the **Unit** text field, type m.
- **16** In the table, click to select the cell at row number 2 and column number 1.
- 17 From the Distribution list, choose Normal(μ , σ).
- 18 In the Mean text field, type 1p.
- 19 In the Standard deviation text field, type 0.01*1p.
- 20 From the CDF-Lower list, choose Manual.
- 21 From the CDF-Upper list, choose Manual.
- **22** In the **Lower bound** text field, type 0.95*lp.

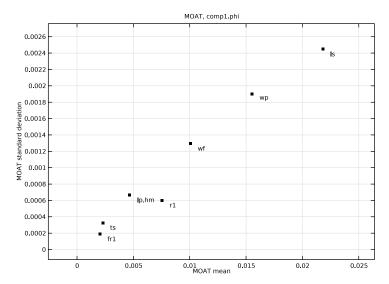
- **23** In the **Upper bound** text field, type 1.05*1p.
- **24** In the **Unit** text field, type m.
- **25** In the table, click to select the cell at row number 3 and column number 1.
- **26** From the **Distribution** list, choose **Normal**(μ , σ).
- **27** In the **Mean** text field, type 1s.
- 28 In the Standard deviation text field, type 0.01*1s.
- 29 From the CDF-Lower list, choose Manual.
- 30 From the CDF-Upper list, choose Manual.
- **3I** In the **Lower bound** text field, type 0.95*1s.
- **32** In the **Upper bound** text field, type 1.05*ls.
- **33** In the **Unit** text field, type m.
- **34** In the table, click to select the cell at row number 4 and column number 1.
- **35** From the **Distribution** list, choose **Normal**(μ , σ).
- 36 In the Mean text field, type hm.
- 37 In the Standard deviation text field, type 0.01*hm.
- **38** From the **CDF-Lower** list, choose **Manual**.
- 39 From the CDF-Upper list, choose Manual.
- **40** In the **Lower bound** text field, type 0.95*hm.
- **4I** In the **Upper bound** text field, type 1.05*hm.
- **42** In the **Unit** text field, type m.
- **4** In the table, click to select the cell at row number 5 and column number 1.
- **44** From the **Distribution** list, choose **Normal**(μ , σ).
- **45** In the **Mean** text field, type wp.
- **46** In the **Standard deviation** text field, type 0.01*wp.
- 47 From the CDF-Lower list, choose Manual.
- **48** From the **CDF-Upper** list, choose **Manual**.
- 49 In the Lower bound text field, type 0.95*wp.
- 50 In the Upper bound text field, type 1.05*wp.
- **5I** In the **Unit** text field, type m.
- **52** In the table, click to select the cell at row number 6 and column number 1.
- **53** From the **Distribution** list, choose **Normal**(μ , σ).

- 54 In the Mean text field, type wf.
- 55 In the Standard deviation text field, type 0.01*wf.
- **56** From the **CDF-Lower** list, choose **Manual**.
- 57 From the CDF-Upper list, choose Manual.
- **58** In the **Lower bound** text field, type 0.95*wf.
- **59** In the **Upper bound** text field, type 1.05*wf.
- **60** In the **Unit** text field, type m.
- **6I** In the table, click to select the cell at row number 7 and column number 1.
- **62** From the **Distribution** list, choose **Normal**(μ , σ).
- **63** In the **Mean** text field, type fr1.
- **64** In the **Standard deviation** text field, type 0.01*fr1.
- 65 From the CDF-Lower list, choose Manual.
- **66** From the **CDF-Upper** list, choose **Manual**.
- 67 In the Lower bound text field, type 0.95*fr1.
- **68** In the **Upper bound** text field, type 1.05*fr1.
- **69** In the **Unit** text field, type m.
- **70** In the table, click to select the cell at row number 8 and column number 1.
- 71 From the **Distribution** list, choose **Normal**(μ , σ).
- 72 In the Mean text field, type r1.
- 73 In the Standard deviation text field, type 0.01*r1.
- 74 From the CDF-Lower list, choose Manual.
- 75 From the CDF-Upper list, choose Manual.
- **76** In the **Lower bound** text field, type 0.95*r1.
- **77** In the **Upper bound** text field, type 1.05*r1.
- **78** In the **Unit** text field, type m.
- **79** In the **Home** toolbar, click **Compute**.

RESULTS

MOAT, compl.phi

I Click the Zoom Extents button in the Graphics toolbar.



The screening results indicate that the Side length (1s) and the Cross plate width (wp) parameters are the most influential on the quantity of interest. However, several of the other parameters also appear to be significant. A high value of the MOAT mean means that the parameter is significantly influencing the quantity of interest. A high value of the MOAT standard deviation means that the parameter is influential and that it is either interacting with other parameters and/or that it has a nonlinear influence.

STUDY 2, SCREENING

The next step is a sensitivity analysis. Use the results from the screening to decide which parameters to include in the sensitivity analysis. Sensitivity is more computationally demanding than screening and for this reason we would prefer to pick a subset of the parameters used for the screening study. However, in this example, we would like to learn as much as possible about the model and we pick all the available design parameters. We do not need to type all of the uncertainty quantification parameters again but we can define the new Uncertainty Quantification study for the sensitivity analysis by reusing the information in the screening study.

Uncertainty Quantification

Right-click Uncertainty Quantification and choose

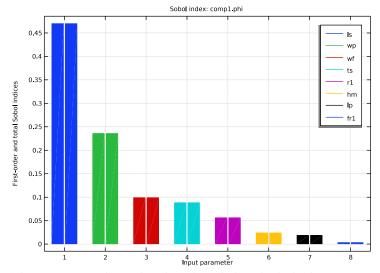
Add New Uncertainty Quantification Study For>Sensitivity Analysis.

STUDY 3, SENSITIVITY

- I In the Model Builder window, click Study 3.
- 2 In the Settings window for Study, type Study 3, Sensitivity in the Label text field.
- I In the Model Builder window, under Study 3, Sensitivity click Uncertainty Quantification.
- 2 In the Settings window for Uncertainty Quantification, locate the **Uncertainty Quantification Settings** section.
- 3 From the Compute action list, choose Compute and analyze.
- 4 In the Home toolbar, click **Compute**.

RESULTS

Sobol Index, compl.phi



The sensitivity analysis is based on the Sobol method, also known as variance-based sensitivity analysis. The result of the sensitivity analysis is a set of Sobol indices and an associated Sobol table and Sobol plot. There are two different types of Sobol indices: firstorder index and total index. The first-order index of a parameter shows the sensitivity by varying this parameter alone. The total index shows how much a parameter contributes to the overall sensitivity.

In this case, the first and total indices are equal, up to the computed accuracy, for all parameters which indicates very little or no interaction between the parameters. The Sobol plot indicates that the misalignment angle is most sensitive to the parameters Side length (1s) and Cross plate width (wp). This is consistent with the screening results.

For the final two studies, Uncertainty Propagation and Reliability Analysis, we will, for the purpose of faster demonstration, delete all parameters except for the dominant two: 1s and wp. However, to get a conservative estimate of the uncertainties we should in principle include all parameters (see earlier comment).

STUDY 3. SENSITIVITY

Uncertainty Quantification

Right-click Uncertainty Quantification and choose

Add New Uncertainty Quantification Study For>Uncertainty Propagation.

STUDY 4, PROPAGATION

- I In the Model Builder window, click Study 4.
- 2 In the Settings window for Study, type Study 4, Propagation in the Label text field.
- I In the Model Builder window, under Study 4, Propagation click Uncertainty Quantification.
- 2 In the Settings window for Uncertainty Quantification, locate the Input Parameters section.
- 3 Ctrl-click to select table rows 1, 2, 4, and 6–8. This is most easily done by first clicking in the table's upper-left corner and then dragging the bottom border of the pop-out table downward until you see all rows at once. The rows to select are those for the parameters ts, lp, hm, wf, fr1, and r1.
- 4 Click Delete.
- 5 Locate the Uncertainty Quantification Settings section. From the Compute action list, choose Compute and analyze. The default Compute action is Improve and analyze. This will reuse the previously computed uncertainty quantification results in order to speed up the computation. However, we are changing to Compute and analyze, which is slower, but gives a higher-fidelity result.

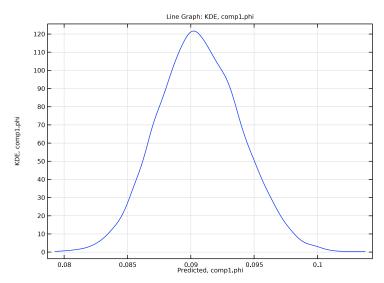
Uncertainty Quantification 3

In the **Home** toolbar, click **Compute**.

RESULTS

Kernel Density Estimation, compl.phi

I In the Model Builder window, under Results>Uncertainty Quantification Graph 2 click Kernel Density Estimation, compl.phi.



The uncertainty propagation study computes a so called kernel density estimation or KDE. You can think of the KDE as a smooth form of a histogram showing an estimate of the probability density function of the quantity of interest, given the input parameters and their distributions. We can see from the QoI confidence interval table, shown earlier in the Results and Discussion section, that the mean is about 0.09 degree with a standard deviation of 0.003 degree. The KDE plot gives us this information graphically. From the values in the table we can also see that there appears to be some risk that the angle exceeds 0.1 degree.

To get a more accurate estimate of the risk for exceeding 0.1 degree, we will next run a reliability analysis.

STUDY 4, PROPAGATION

Uncertainty Quantification

In the Model Builder window, under Study 4, Propagation right-click Uncertainty Quantification and choose Add New Uncertainty Quantification Study For> Reliability Analysis.

STUDY 5, RELIABILITY

- I In the Model Builder window, click Study 5.
- 2 In the Settings window for Study, type Study 5, Reliability in the Label text field.
- I In the Model Builder window, under Study 5, Reliability click Uncertainty Quantification.
- 2 In the Settings window for Uncertainty Quantification, locate the Quantities of Interest section.
- **3** In the table, enter the following settings:

Expression	Individual solution to use	True if	Threshold
comp1.phi	From "Solution to use"	Larger than threshold	0.1

Uncertainty Quantification 4

I In the **Home** toolbar, click **Compute**.

The reliability analysis performs a so-called importance sampling that refines the full model results near the threshold that we give for our quantity of interest. Recall that we are here asking for the probability that this angle exceeds 0.1 degree. The reliability analysis study gives us a table named **Probability for condition** having the value ~ 0.003 . This means that with the given conditions, there is a ~0.3% risk of the misalignment angle to exceed 0.1 degree.

As a final step, we can also produce a response surface of pairs of input parameters, in this case the Side length (1s) and the Cross plate width (wp).

Uncertainty Quantification

- I In the Model Builder window, under Study 5, Reliability click Uncertainty Quantification.
- 2 Locate the Surrogate-Based Response Surface section. Click Response Surface in the upper-right corner of the section.

RESULTS

Response surface

I Click the **Zoom Extents** button in the **Graphics** toolbar.

2 In the Model Builder window, under Results click Response surface.

