



# Rotors Connected Through Helical Gears

## Introduction

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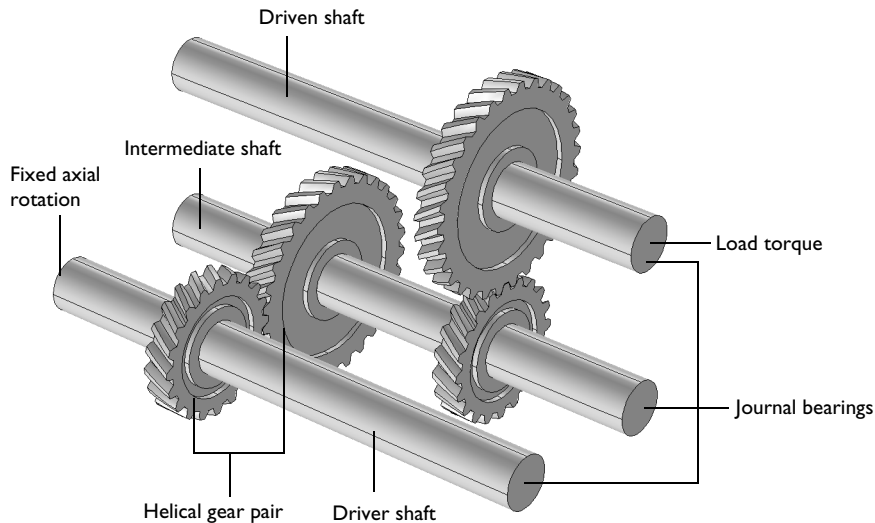
This example illustrates the modeling of multiple rotors connected through helical gears. The presence of gears in the system induces lateral as well as torsional vibration in the rotors. An eigenfrequency analysis is performed for different speeds of the driver shaft in order to compute the critical speeds. The frequency response of the system is also computed for a range of frequencies, assuming the speed of the driver shaft to be the same as the excitation frequency. A transient analysis is performed for the given speed and load to compute the orbit and the dynamic transmission error of the gears as well as the forces acting on the bearings.

## Model Definition

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The model consists of three shafts connected through two pairs of helical gears. The helical gear on the first (driver) shaft transfers rotation to the larger helical gear of the second (intermediate) shaft. The smaller helical gear of the second (intermediate) shaft transfers rotation to the helical gear of the third (driven) shaft. All three shafts are simply supported at both the ends using journal bearings.

The geared rotor geometry is shown in [Figure 1](#) below.



*Figure 1: Geared rotor geometry.*

**SHAFTS**

All the shafts are of the same dimensions and made of structural steel. The shafts’ diameter and length are 40 mm and 600 mm, respectively.

In the time-dependent analysis, the angular speed of the driver shaft is assumed to be 1500 rpm. In the eigenfrequency, it is varied from 0 to 9000 rpm whereas in the frequency domain analysis, it is assumed to be the same as the excitation frequency. The angular speed of the other two shafts is computed using the gear ratio.

**BEARINGS**

Each shaft is supported by journal bearings at both the ends. All the bearings are assumed to have constant isotropic stiffness with a value of  $10^7$  N/m.

**GEARS**

The properties of the helical gears are given in the [Table 1](#).

TABLE 1: GEAR PROPERTIES.

PROPERTY	VALUE
Number of teeth (Gear-1)	20
Pitch diameter (Gear-1)	100 mm
Number of teeth (Gear-2)	30
Pitch diameter (Gear-2)	150 mm
Pressure angle	25°
Helix angle	30°
Gear ratio	1.5
Gear mesh stiffness	$2 \cdot 10^6$ N/m

The density of the gears, used to compute the inertial properties, is same as the shaft density.

**CONSTRAINTS AND LOADS**

- The axial rotation is constrained at one end of the driver shaft.
- In the time dependent analysis, a resisting load torque of  $10^2$  Nm is applied at the opposite end of the driven shaft.

**CRITICAL SPEEDS OF A ROTOR**

The angular speeds of a rotor that match its natural frequencies are known as the critical speeds. Approximate values of the critical speeds of a rotor can be obtained as the rotor’s eigenfrequencies computed while neglecting rotating frame forces. However, to predict

the eigenfrequencies accurately, the rotating frame forces for a range of angular speeds must be included in the computations. The Campbell diagram, showing the variation of eigenfrequencies with angular speed, can be drawn and accurate critical speeds can be computed. A Campbell plot using the Solid Rotor interface plots the frequencies in the rotating frame. In such a plot critical speeds are obtained by the intersection of the backward whirl frequency curve with  $\omega = 2\Omega$  curve and intersection of the forward whirl curve with the  $x$ -axis. In the rotating frame, generally the backward whirl frequencies increase with the rotor speed and forward whirl frequencies decrease.

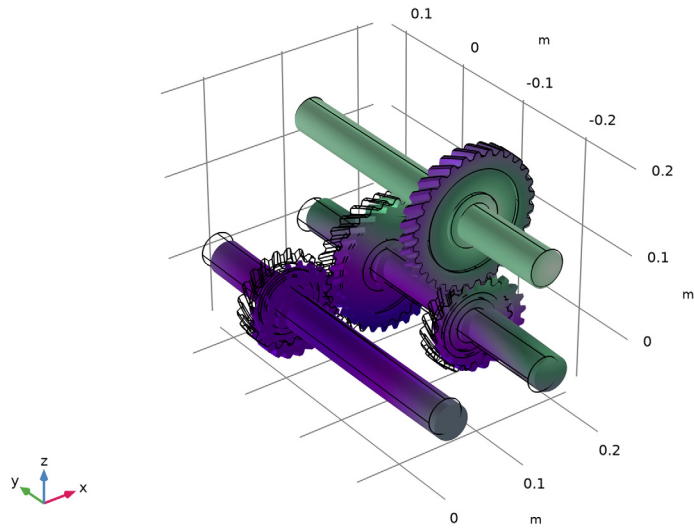
### Results and Discussion

There are five points where the  $\omega = 2\Omega$  curve intersects with the eigenfrequency curve. These are the critical speeds of the rotor system below 9000 rpm and they are listed in the [Table 2](#).

TABLE 2: CRITICAL SPEEDS OF THE ROTOR.

Mode	Critical speeds (rad/s)
First	281 . 8
Second	473 . 7
Third	549 . 0
Fourth	595 . 1
Fifth	668 . 7

omega(19)=9000 rpm Eigenfrequency=113.39 Hz Surface: Displacement magnitude (m)



*Figure 2: The second mode of the geared rotors at 9000 rpm.*

Figure 2 shows the second mode ( $f = 113.4$  Hz) of the geared rotors at 9000 rpm. The Campbell Plot, showing the variation of eigenfrequencies with the rotational speed, is shown in Figure 3. The three critical speeds of the rotor, where the straight line ( $\omega = 2\Omega$ ) intersects the eigenfrequency curves, can be seen.

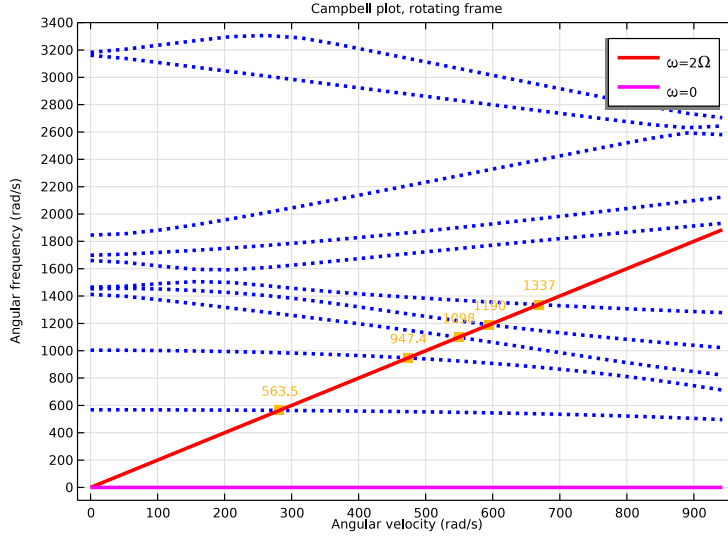


Figure 3: Campbell diagram.

The frequency response curves for the gear displacement and rotation are shown in Figure 4 and Figure 5. It can be seen that both the displacement and rotation of all gears have a peak around the critical speeds computed from the Campbell plot.

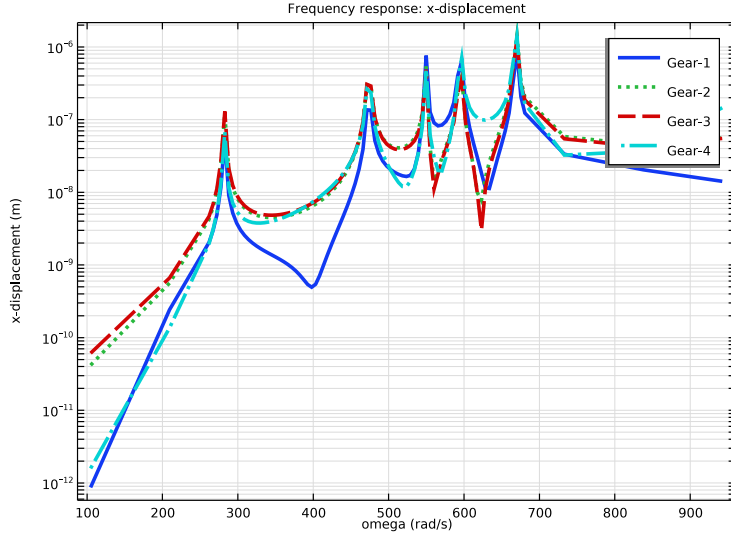


Figure 4: Frequency response of the  $x$ -direction displacement of all the gears.

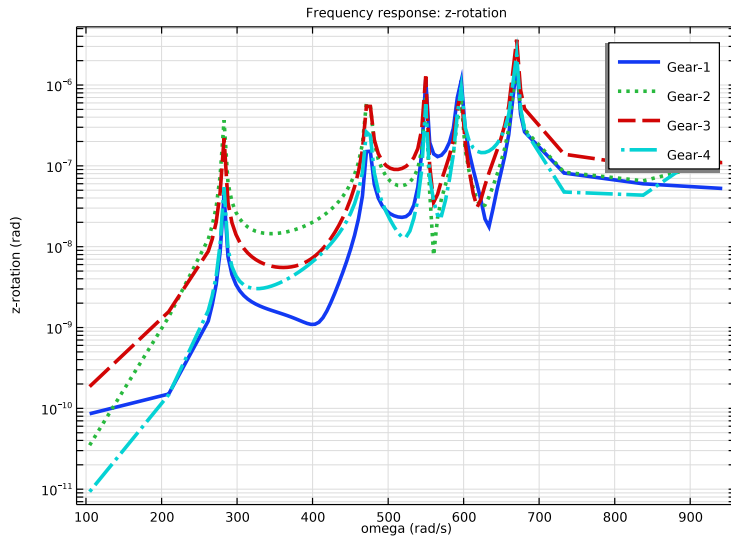


Figure 5: Frequency response of the  $z$ -direction rotation of all the gears.

Figure 6 shows the von Mises stress distribution in the shafts. It can be observed that state of stress in the shafts is combination of twisting and bending of the shafts. The effect of twisting is dominant in the driven shaft where the loading torque is applied. The remaining parts of the shafts experience mostly the bending load generated due to gearing action.

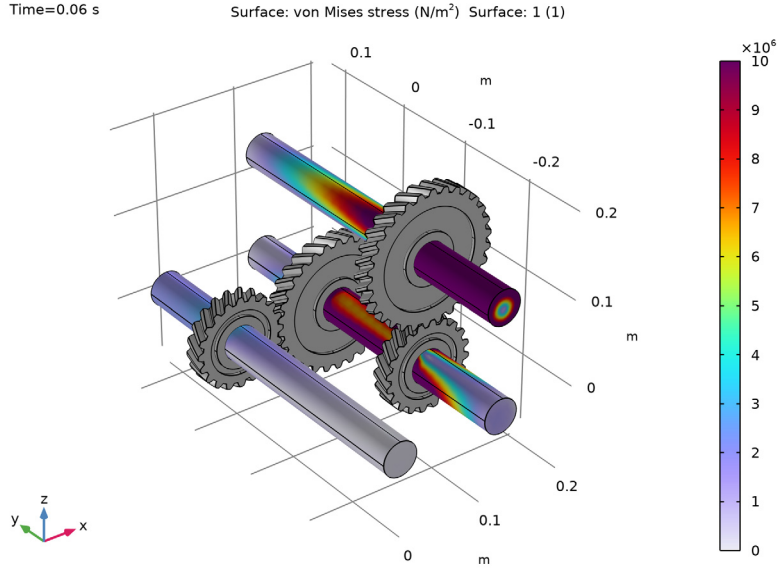


Figure 6: von Mises stress distribution in the shafts at a particular instance.

Figure 7 and Figure 8 show the orbits of the gear centers in the rotating and the fixed frame of reference, respectively. It can be observed that in the rotating frame of reference, all the gears are settled in different directions except gear-2 and gear-3, as they are both mounted on the intermediate shaft.

The gear mesh is assumed to be elastic, which causes an error while transferring rotation from one shaft to another. This error, known as the dynamic transmission error (DTE), is shown in Figure 9.

Finally, Figure 10 shows the time variation of the bearing loads on one of the journal bearings.



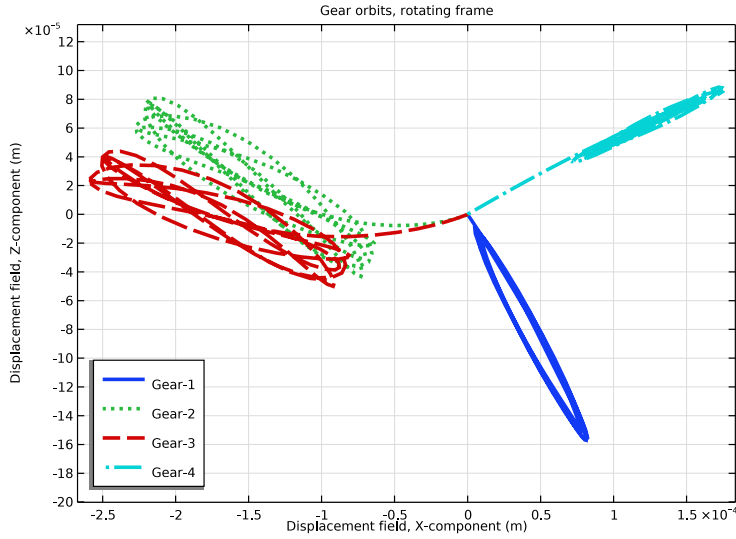


Figure 7: Orbits of gear center in the rotating frame of reference.

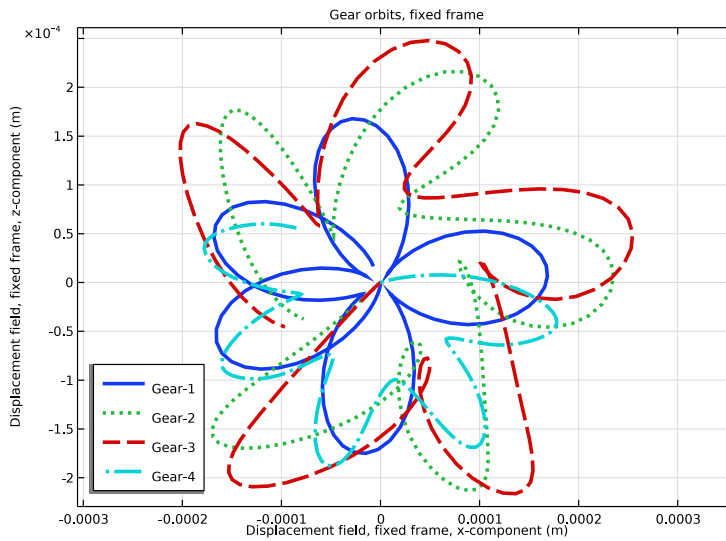


Figure 8: Orbits of gear center in the fixed frame of reference.

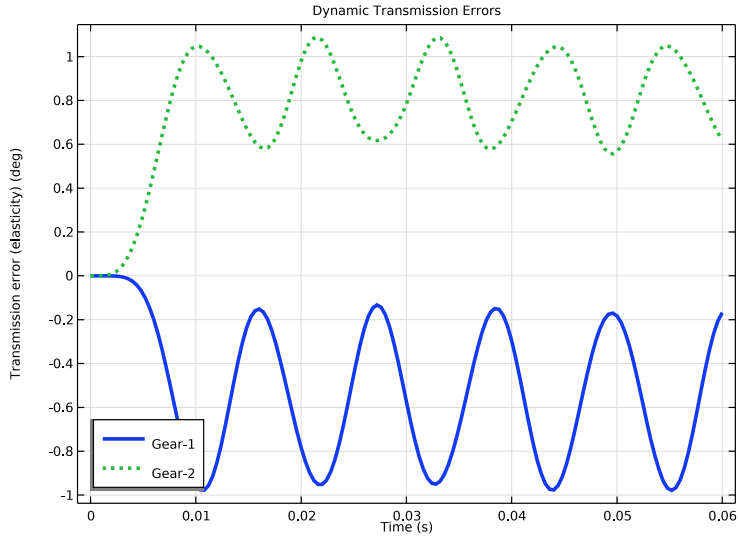


Figure 9: Time variation of the dynamic transmission error (DTE) of both gear pairs.

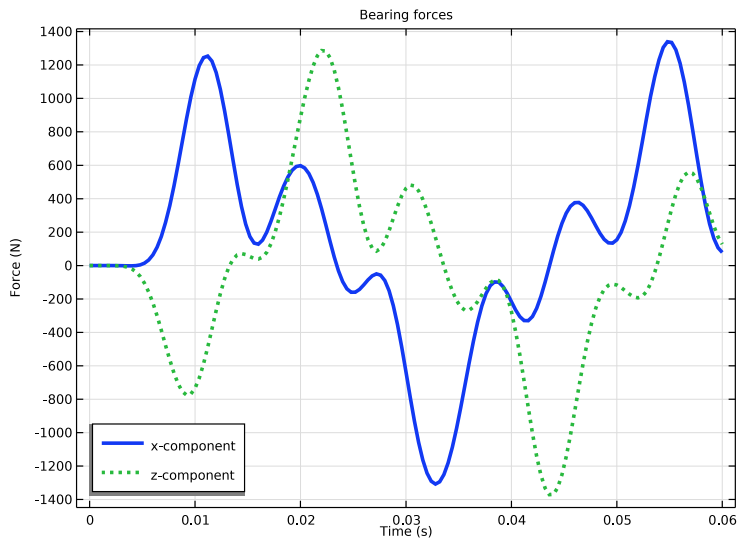


Figure 10: Time variation of the bearing forces.

## *Notes About the COMSOL Implementation*

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The **Solid Rotor** physics interface is used to model multiple rotors connected through gears.

To model multiple rotors, use **Rotor Axis** and **Change Rotor Speed** features to define the axis of rotation and speed of each rotor. In cases where two shafts are connected through gears, the shaft speeds are related through the gear ratio.

The gear mesh stiffness is assumed constant. However, in general it is a function of gear rotation. The varying gear mesh stiffness causes additional sustained vibration in the system.

It is possible to visualize results in both the rotating as well as the fixed frame of reference. In this model, the fixed frame of reference is used when animating the results.

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**Application Library path:** Rotordynamics\_Module/Automotive\_and\_Aerospace/geared\_rotors


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## *Modeling Instructions*




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From the **File** menu, choose **New**.

### **NEW**

In the **New** window, click  **Model Wizard**.


### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Structural Mechanics>Rotordynamics>Solid Rotor (rotsld)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Eigenfrequency**.
- 6 Click  **Done**.

### **GLOBAL DEFINITIONS**

#### *Parameters* 1

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.

- 3 Click  **Load from File**.
- 4 Browse to the model's Application Libraries folder and double-click the file `geared_rotors_parameters.txt`.

## DEFINITIONS

### *Step 1 (step1)*


- 1 In the **Model Builder** window, expand the **Component 1 (comp1)>Definitions** node.
- 2 Right-click **Definitions** and choose **Functions>Step**.
- 3 In the **Settings** window for **Step**, locate the **Parameters** section.
- 4 In the **Location** text field, type `t_end/12`.
- 5 Click to expand the **Smoothing** section. In the **Size of transition zone** text field, type `t_end/6`.

## GEOMETRY 1


### *Import 1 (imp1)*


- 1 In the **Home** toolbar, click  **Import**.
- 2 In the **Settings** window for **Import**, locate the **Import** section.
- 3 Click  **Browse**.
- 4 Browse to the model's Application Libraries folder and double-click the file `geared_rotors.mphbin`.
- 5 Click  **Import**.

### *Form Union (fin)*

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Geometry 1** click **Form Union (fin)**.
- 2 In the **Settings** window for **Form Union/Assembly**, locate the **Form Union/Assembly** section.
- 3 From the **Action** list, choose **Form an assembly**.
- 4 Clear the **Create pairs** check box.
- 5 In the **Home** toolbar, click  **Build All**.

## ADD MATERIAL

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Built-in>Structural steel**.


- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.

### **SOLID ROTOR (ROTSLD)**


This model has multiple rotors having different axis of rotation as well as different speeds. So first set the axis of rotation and speed for all three rotors.

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Solid Rotor (rotsld)**.
- 2 In the **Settings** window for **Solid Rotor**, locate the **Rotor Speed** section.
- 3 In the text field, type omega.

#### *First Support 1*

- 1 In the **Model Builder** window, click **First Support 1**.
- 2 In the **Settings** window for **First Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 97-98 in the **Selection** text field.
- 5 Click **OK**.


#### *Second Support 1*

- 1 In the **Model Builder** window, click **Second Support 1**.
- 2 In the **Settings** window for **Second Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 119-120 in the **Selection** text field.
- 5 Click **OK**.

#### *Rotor Axis 2*


- 1 In the **Physics** toolbar, click  **Domains** and choose **Rotor Axis**.
- 2 Select Domains 5–7 only.

#### *First Support 1*

- 1 In the **Model Builder** window, click **First Support 1**.
- 2 In the **Settings** window for **First Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 744, 756 in the **Selection** text field.
- 5 Click **OK**.

#### *Second Support 1*


- 1 In the **Model Builder** window, click **Second Support 1**.

- 2 In the **Settings** window for **Second Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 749, 761 in the **Selection** text field.
- 5 Click **OK**.


#### *Rotor Axis 3*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Rotor Axis**.
- 2 Select Domains 3 and 4 only.


#### *First Support 1*

- 1 In the **Model Builder** window, click **First Support 1**.
- 2 In the **Settings** window for **First Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 355, 363 in the **Selection** text field.
- 5 Click **OK**.


#### *Second Support 1*

- 1 In the **Model Builder** window, click **Second Support 1**.
- 2 In the **Settings** window for **Second Support**, locate the **Point Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 358, 366 in the **Selection** text field.
- 5 Click **OK**.

#### *Change Rotor Speed 1*

- 1 In the **Physics** toolbar, click  **Domains** and choose **Change Rotor Speed**.
- 2 Select Domains 5–7 only.
- 3 In the **Settings** window for **Change Rotor Speed**, locate the **Rotor Speed** section.
- 4 In the text field, type  $-\omega/g_r$ .

#### *Change Rotor Speed 2*


- 1 In the **Physics** toolbar, click  **Domains** and choose **Change Rotor Speed**.
- 2 Select Domains 3 and 4 only.
- 3 In the **Settings** window for **Change Rotor Speed**, locate the **Rotor Speed** section.
- 4 In the text field, type  $\omega/g_r^2$ .

#### *Fixed Axial Rotation 1*

- 1 In the **Model Builder** window, click **Fixed Axial Rotation 1**.

2 Select Boundary 57 only.

Use the weak form of constraint to stabilize the solver. This is available as an advance physics option.

3 Click the  **Show More Options** button in the **Model Builder** toolbar.

4 In the **Show More Options** dialog box, select **Physics>Advanced Physics Options** in the tree.

5 In the tree, select the check box for the node **Physics>Advanced Physics Options**.

6 Click **OK**.

7 In the **Settings** window for **Fixed Axial Rotation**, click to expand the **Constraint Settings** section.

8 Select the **Use weak constraints** check box.

Now define helical gears to connect the three rotors.

#### *Helical Gear 1*

1 In the **Physics** toolbar, click  **Domains** and choose **Helical Gear**.

2 Select Domain 1 only.

3 In the **Settings** window for **Helical Gear**, locate the **Gear Properties** section.

4 In the  $n$  text field, type  $n1$ .

5 In the  $d_p$  text field, type  $d1$ .

6 In the  $\alpha$  text field, type  $\alpha$ .

7 In the  $\beta$  text field, type  $\beta$ .

8 Locate the **Center of Rotation** section. From the list, choose **Centroid of selected entities**.

9 From the **Entity level** list, choose **Point**.

#### *Center of Rotation: Point 1*

1 In the **Model Builder** window, expand the **Helical Gear 1** node, then click **Center of Rotation: Point 1**.

2 In the **Settings** window for **Center of Rotation: Point**, locate the **Point Selection** section.

3 Click  **Paste Selection**.


4 In the **Paste Selection** dialog box, type 101, 115 in the **Selection** text field.

5 Click **OK**.



#### *Helical Gear 1*

In the **Model Builder** window, right-click **Helical Gear 1** and choose **Duplicate**.

### *Helical Gear 2*

- 1 In the **Model Builder** window, click **Helical Gear 2**.
- 2 In the **Settings** window for **Helical Gear**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Domain 5 only.
- 5 Locate the **Gear Properties** section. In the  $n$  text field, type  $n2$ .
- 6 In the  $d_p$  text field, type  $d2$ .
- 7 In the  $\beta$  text field, type  $-\beta$ .


### *Center of Rotation: Point 1*

- 1 In the **Model Builder** window, expand the **Helical Gear 2** node, then click **Center of Rotation: Point 1**.
- 2 In the **Settings** window for **Center of Rotation: Point**, locate the **Point Selection** section.
- 3 Click  **Clear Selection**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 747, 760 in the **Selection** text field.
- 6 Click **OK**.



### *Helical Gear 1*

In the **Model Builder** window, under **Component 1 (comp1)>Solid Rotor (rotsld)** right-click **Helical Gear 1** and choose **Duplicate**.

### *Helical Gear 3*

- 1 In the **Model Builder** window, click **Helical Gear 3**.
- 2 In the **Settings** window for **Helical Gear**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Domain 6 only.

### *Center of Rotation: Point 1*


- 1 In the **Model Builder** window, expand the **Helical Gear 3** node, then click **Center of Rotation: Point 1**.
- 2 In the **Settings** window for **Center of Rotation: Point**, locate the **Point Selection** section.
- 3 Click  **Clear Selection**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 745, 758 in the **Selection** text field.
- 6 Click **OK**.





### *Helical Gear 2*

In the **Model Builder** window, under **Component 1 (comp1)>Solid Rotor (rotsld)** right-click **Helical Gear 2** and choose **Duplicate**.


### *Helical Gear 4*

- 1 In the **Model Builder** window, click **Helical Gear 4**.
- 2 In the **Settings** window for **Helical Gear**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Domain 3 only.

### *Center of Rotation: Point 1*

- 1 In the **Model Builder** window, expand the **Helical Gear 4** node, then click **Center of Rotation: Point 1**.
- 2 In the **Settings** window for **Center of Rotation: Point**, locate the **Point Selection** section.
- 3 Click  **Clear Selection**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 357, 364 in the **Selection** text field.
- 6 Click **OK**.

### *Gear Pair 1*

- 1 In the **Physics** toolbar, click  **Global** and choose **Gear Pair**.
- 2 In the **Settings** window for **Gear Pair**, locate the **Gear Selection** section.
- 3 From the **Wheel** list, choose **Helical Gear 1**.
- 4 From the **Pinion** list, choose **Helical Gear 2**.
- 5 Locate the **Gear Pair Properties** section. Select the **Include gear elasticity** check box.

### *Gear Elasticity 1*

- 1 In the **Model Builder** window, expand the **Gear Pair 1** node, then click **Gear Elasticity 1**.
- 2 In the **Settings** window for **Gear Elasticity**, locate the **Mesh Stiffness** section.
- 3 From the **Specify** list, choose **Total stiffness of gear pair**.
- 4 In the  $k_g$  text field, type kg.

### *Gear Pair 2*

- 1 In the **Physics** toolbar, click  **Global** and choose **Gear Pair**.
- 2 In the **Settings** window for **Gear Pair**, locate the **Gear Selection** section.
- 3 From the **Wheel** list, choose **Helical Gear 3**.


- 4 From the **Pinion** list, choose **Helical Gear 4**.
- 5 Locate the **Gear Pair Properties** section. Select the **Include gear elasticity** check box.

#### *Gear Elasticity 1*

- 1 In the **Model Builder** window, expand the **Gear Pair 2** node, then click **Gear Elasticity 1**.
- 2 In the **Settings** window for **Gear Elasticity**, locate the **Mesh Stiffness** section.
- 3 From the **Specify** list, choose **Total stiffness of gear pair**.
- 4 In the  $k_g$  text field, type kg.

Now define journal bearings to provide the support for the rotors on both ends.

#### *Journal Bearing 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Journal Bearing**.
- 2 Select Boundary 52 only.
- 3 In the **Settings** window for **Journal Bearing**, locate the **Bearing Orientation** section.
- 4 Specify the **Orientation vector defining local y direction** vector as


1	x
0	y
0	z

- 5 Locate the **Bearing Properties** section. From the **Bearing model** list, choose **Total spring and damping constant**.
- 6 In the  $k_u$  table, enter the following settings:


kb	0
0	kb

- 7 Right-click **Journal Bearing 1** and choose **Duplicate**.


#### *Journal Bearing 2*

- 1 In the **Model Builder** window, click **Journal Bearing 2**.
- 2 In the **Settings** window for **Journal Bearing**, locate the **Boundary Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Boundary 57 only.
- 5 Locate the **Bearing Properties** section. Clear the **Constrain axial motion** check box.
- 6 Right-click **Journal Bearing 2** and choose **Duplicate**.


### *Journal Bearing 3*

- 1 In the **Model Builder** window, click **Journal Bearing 3**.
- 2 In the **Settings** window for **Journal Bearing**, locate the **Boundary Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Boundary 397 only.
- 5 Locate the **Bearing Properties** section. Select the **Constrain axial motion** check box.
- 6 Right-click **Journal Bearing 3** and choose **Duplicate**.


### *Journal Bearing 4*

- 1 In the **Model Builder** window, click **Journal Bearing 4**.
- 2 In the **Settings** window for **Journal Bearing**, locate the **Boundary Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Boundary 406 only.
- 5 Locate the **Bearing Properties** section. Clear the **Constrain axial motion** check box.
- 6 Right-click **Journal Bearing 4** and choose **Duplicate**.


### *Journal Bearing 5*

- 1 In the **Model Builder** window, click **Journal Bearing 5**.
- 2 In the **Settings** window for **Journal Bearing**, locate the **Boundary Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Boundary 191 only.
- 5 Right-click **Journal Bearing 5** and choose **Duplicate**.


### *Journal Bearing 6*

- 1 In the **Model Builder** window, click **Journal Bearing 6**.
- 2 In the **Settings** window for **Journal Bearing**, locate the **Boundary Selection** section.
- 3 Click  **Clear Selection**.
- 4 Select Boundary 196 only.
- 5 Locate the **Bearing Properties** section. Select the **Constrain axial motion** check box.

### *Applied Torque 1*

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Applied Torque**.
- 2 Select Boundary 191 only.
- 3 In the **Settings** window for **Applied Torque**, locate the **Torque** section.
- 4 In the  $T_{ax}$  text field, type `Text*step1(t)`.



**MESH 1**

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Mesh 1**.
- 2 In the **Settings** window for **Mesh**, locate the **Physics-Controlled Mesh** section.
- 3 From the **Element size** list, choose **Coarse**.
- 4 Click  **Build All**.

**STUDY 1: EIGENFREQUENCY**


- 1 In the **Model Builder** window, click **Study 1**.
- 2 In the **Settings** window for **Study**, type Study 1: Eigenfrequency in the **Label** text field.

*Parametric Sweep*

- 1 In the **Study** toolbar, click  **Parametric Sweep**.
- 2 In the **Settings** window for **Parametric Sweep**, locate the **Study Settings** section.
- 3 Click  **Add**.
- 4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
omega (Angular speed of driver shaft)	range (0,500,9000)	rpm



*Step 1: Eigenfrequency*

- 1 In the **Model Builder** window, click **Step 1: Eigenfrequency**.
- 2 In the **Settings** window for **Eigenfrequency**, locate the **Study Settings** section.
- 3 Select the **Desired number of eigenfrequencies** check box. In the associated text field, type 10.
- 4 In the **Study** toolbar, click  **Compute**.



**RESULTS**

*Mode Shape (rotsld)*

Use the following instructions to plot the mode shape and Campbell diagram as shown in [Figure 2](#) and [Figure 3](#) respectively.

- 1 In the **Settings** window for **3D Plot Group**, locate the **Data** section.
- 2 From the **Eigenfrequency (Hz)** list, choose **113.39**.
- 3 In the **Mode Shape (rotsld)** toolbar, click  **Plot**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.

## ADD PREDEFINED PLOT

- 1 In the **Home** toolbar, click  **Add Predefined Plot** to open the **Add Predefined Plot** window.
- 2 Go to the **Add Predefined Plot** window.
- 3 In the tree, select **Study 1: Eigenfrequency/Parametric Solutions 1 (sol2)>Solid Rotor>Campbell Plot, Rotating Frame (rotsld)**.
- 4 Click **Add Plot** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Predefined Plot** to close the **Add Predefined Plot** window.

## RESULTS

### *Backward Whirl Mode*

The default **Campbell Plot, Rotating Frame** segregates the whirl modes, namely, forward and backward. Because of the multiple rotors rotating at different speeds, whirl modes in all the rotors will not be identical. Therefore, automatic identification of the whirl mode is not correct in this case. Delete the **Backward Whirl Mode** node in this plot group.

- 1 In the **Model Builder** window, expand the **Campbell Plot, Rotating Frame (rotsld)** node.
- 2 Right-click **Backward Whirl Mode** and choose **Delete**.

### *Whirl Mode*



- 1 In the **Model Builder** window, under **Results>Campbell Plot, Rotating Frame (rotsld)** click **Forward Whirl Mode**.
- 2 In the **Settings** window for **Global**, type **Whirl Mode** in the **Label** text field.

### *Graph Marker 1*



- 1 In the **Model Builder** window, expand the **Whirl Mode** node, then click **Graph Marker 1**.
- 2 In the **Settings** window for **Graph Marker**, locate the **Display** section.
- 3 From the **Line type** list, choose **General**.
- 4 In the **A** text field, type 2.
- 5 In the **B** text field, type -1.
- 6 In the **C** text field, type 0.
- 7 Locate the **Text Format** section. Clear the **Show x-coordinate** check box.
- 8 Clear the **Prefix** text field.
- 9 Click to expand the **Coloring and Style** section. From the **Color** list, choose **Custom**.

- 10 On Windows, click the colored bar underneath, or — if you are running the cross-platform desktop — the **Color** button.
- 11 Click **Define custom colors**.
- 12 Set the RGB values to 253, 185, and 19, respectively.
- 13 Click **Add to custom colors**.
- 14 Click **Show color palette only** or **OK** on the cross-platform desktop.

*Campbell Plot, Rotating Frame (rotsld)*

- 1 In the **Model Builder** window, under **Results** click **Campbell Plot, Rotating Frame (rotsld)**.
- 2 In the **Campbell Plot, Rotating Frame (rotsld)** toolbar, click  **Plot**.
- 3 Click the  **Zoom Extents** button in the **Graphics** toolbar.



**ADD STUDY**

- 1 In the **Home** toolbar, click  **Add Study** to open the **Add Study** window.
- 2 Go to the **Add Study** window.
- 3 Find the **Studies** subsection. In the **Select Study** tree, select **General Studies> Frequency Domain**.
- 4 Click **Add Study** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Study** to close the **Add Study** window.

**STUDY 2: FREQUENCY DOMAIN**



- 1 In the **Model Builder** window, click **Study 2**.
- 2 In the **Settings** window for **Study**, type Study 2: Frequency Domain in the **Label** text field.
- 3 Locate the **Study Settings** section. Clear the **Generate default plots** check box.

*Parametric Sweep*

- 1 In the **Study** toolbar, click  **Parametric Sweep**.
- 2 In the **Settings** window for **Parametric Sweep**, locate the **Study Settings** section.
- 3 Click  **Add**.
- 4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
omega (Angular speed of driver shaft)	range ( 1000 , 1000 , 2000 ) range ( 2500 , 50 , 6500 ) range ( 7000 , 1000 , 9000 )	rpm


### Step 1: Frequency Domain

- 1 In the **Model Builder** window, click **Step 1: Frequency Domain**.
- 2 In the **Settings** window for **Frequency Domain**, locate the **Study Settings** section.
- 3 In the **Frequencies** text field, type  $2*\omega$ .
- 4 Locate the **Physics and Variables Selection** section. Select the **Modify model configuration for study step** check box.
- 5 In the tree, select **Component 1 (comp1)>Solid Rotor (rotsld)>Applied Torque 1**.
- 6 Click  **Disable**.
- 7 In the **Study** toolbar, click  **Compute**.

### RESULTS

Use the following instructions to plot the frequency response curves as shown in [Figure 4](#) and [Figure 5](#) respectively.

#### 1D Plot Group 4

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **1D Plot Group**.
- 2 In the **Settings** window for **1D Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 2: Frequency Domain/Parametric Solutions 2 (sol23)**.

#### Global 1

- 1 Right-click **1D Plot Group 4** and choose **Global**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:



Expression	Unit	Description
$\text{abs}(\text{rotsld.hlg1.u})$	m	
$\text{abs}(\text{rotsld.hlg2.u})$	m	
$\text{abs}(\text{rotsld.hlg3.u})$	m	
$\text{abs}(\text{rotsld.hlg4.u})$	m	

- 4 Locate the **x-Axis Data** section. From the **Axis source data** list, choose **Outer solutions**.
- 5 From the **Parameter** list, choose **Expression**.
- 6 In the **Expression** text field, type  $2*\pi[\text{rad}]*\omega$ .
- 7 Select the **Description** check box. In the associated text field, type  $\omega$ .
- 8 Click to expand the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **Cycle**.

- 9 From the **Width** list, choose **3**.
- 10 Click to expand the **Legends** section. From the **Legends** list, choose **Manual**.
- 11 In the table, enter the following settings:

Legends
Gear - 1
Gear - 2
Gear - 3
Gear - 4

*Frequency response: x-displacement*

- 1 In the **Model Builder** window, under **Results** click **ID Plot Group 4**.
- 2 In the **Settings** window for **ID Plot Group**, type **Frequency response: x-displacement** in the **Label** text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **Label**.
- 4 Locate the **Plot Settings** section.
- 5 Select the **y-axis label** check box. In the associated text field, type **x-displacement (m)**.
- 6 Locate the **Axis** section. Select the **y-axis log scale** check box.
- 7 In the **Frequency response: x-displacement** toolbar, click  **Plot**.
- 8 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 9 Right-click **Frequency response: x-displacement** and choose **Duplicate**.

*Global 1*



- 1 In the **Model Builder** window, expand the **Frequency response: x-displacement 1** node, then click **Global 1**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:

Expression	Unit	Description
abs(rots1d.hlg1.thz)	rad	
abs(rots1d.hlg2.thz)	rad	
abs(rots1d.hlg3.thz)	rad	
abs(rots1d.hlg4.thz)	rad	



*Frequency response: z-rotation*

- 1 In the **Model Builder** window, under **Results** click **Frequency response: x-displacement 1**.



- 2 In the **Settings** window for **ID Plot Group**, type Frequency response: z-rotation in the **Label** text field.
- 3 Locate the **Plot Settings** section. In the **y-axis label** text field, type z-rotation (rad).
- 4 In the **Frequency response: z-rotation** toolbar, click  **Plot**.
- 5 Click the  **Zoom Extents** button in the **Graphics** toolbar.

#### ADD STUDY

- 1 In the **Home** toolbar, click  **Add Study** to open the **Add Study** window.
- 2 Go to the **Add Study** window.
- 3 Find the **Studies** subsection. In the **Select Study** tree, select **General Studies>Time Dependent**.
- 4 Click **Add Study** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Study** to close the **Add Study** window.

#### STUDY 3: TIME DEPENDENT



- 1 In the **Model Builder** window, click **Study 3**.
- 2 In the **Settings** window for **Study**, type Study 3: Time Dependent in the **Label** text field.

##### *Step 1: Time Dependent*

- 1 In the **Model Builder** window, under **Study 3: Time Dependent** click **Step 1: Time Dependent**.
- 2 In the **Settings** window for **Time Dependent**, locate the **Study Settings** section.
- 3 In the **Output times** text field, type range(0, t\_end/150, t\_end).

Change some solver settings for better convergence.

##### *Solution 110 (sol110)*

- 1 In the **Study** toolbar, click  **Show Default Solver**.
- 2 In the **Model Builder** window, expand the **Solution 110 (sol110)** node.
- 3 In the **Model Builder** window, expand the **Study 3: Time Dependent>Solver Configurations>Solution 110 (sol110)>Time-Dependent Solver 1** node, then click **Fully Coupled 1**.
- 4 In the **Settings** window for **Fully Coupled**, click to expand the **Method and Termination** section.
- 5 From the **Jacobian update** list, choose **On every iteration**.
- 6 In the **Study** toolbar, click  **Compute**.

## RESULTS

### *Study 3: Time Dependent/Solution 110 (sol110)*

Use the following instructions to plot the von-Mises stress and gear orbits as shown in [Figure 6](#), [Figure 7](#), and [Figure 8](#) respectively.

- 1 In the **Model Builder** window, expand the **Results>Datasets** node.
- 2 Right-click **Results>Datasets>Study 3: Time Dependent/Solution 110 (sol110)** and choose **Duplicate**.

### *Selection*

- 1 In the **Model Builder** window, right-click **Study 3: Time Dependent/Solution 110 (6) (sol110)** and choose **Selection**.
- 2 In the **Settings** window for **Selection**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Domain**.
- 4 Select Domains 1, 3, 5, and 6 only.

### *Surface*

In the **Model Builder** window, expand the **Results>Stress (rotsld)** node.

### *Deformation*

- 1 In the **Model Builder** window, expand the **Surface** node, then click **Deformation**.
- 2 In the **Settings** window for **Deformation**, click **Replace Expression** in the upper-right corner of the **Expression** section. From the menu, choose **Component 1 (comp1)>Solid Rotor>Displacement>rotsld.us\_fix,...,rotsld.ws\_fix - Displacement field, fixed frame**.
- 3 Locate the **Scale** section.
- 4 Select the **Scale factor** check box. In the associated text field, type 1.



### *Surface*

In the **Model Builder** window, right-click **Surface** and choose **Duplicate**.


### *Surface 2*

- 1 In the **Model Builder** window, click **Surface 2**.
- 2 In the **Settings** window for **Surface**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 3: Time Dependent/Solution 110 (6) (sol110)**.
- 4 Locate the **Expression** section. In the **Expression** text field, type 1.
- 5 Locate the **Coloring and Style** section. From the **Coloring** list, choose **Uniform**.
- 6 From the **Color** list, choose **Gray**.


### *Surface*

- 1 In the **Model Builder** window, click **Surface**.
- 2 In the **Settings** window for **Surface**, click to expand the **Range** section.
- 3 Select the **Manual color range** check box.
- 4 In the **Maximum** text field, type  $1e7$ .
- 5 In the **Stress (rotsld)** toolbar, click  **Plot**.
- 6 Click the  **Zoom Extents** button in the **Graphics** toolbar.

### *Cut Point 3D 1*

- 1 In the **Results** toolbar, click  **Cut Point 3D**.
- 2 In the **Settings** window for **Cut Point 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 3: Time Dependent/Solution 110 (5) (sol110)**.
- 4 Locate the **Point Data** section. In the **X** text field, type `rotsld.hlg1.xcx`, `rotsld.hlg2.xcx`, `rotsld.hlg3.xcx`, `rotsld.hlg4.xcx`.
- 5 In the **Y** text field, type `rotsld.hlg1.xcy`, `rotsld.hlg2.xcy`, `rotsld.hlg3.xcy`, `rotsld.hlg4.xcy`.
- 6 In the **Z** text field, type `rotsld.hlg1.xcz`, `rotsld.hlg2.xcz`, `rotsld.hlg3.xcz`, `rotsld.hlg4.xcz`.

### *ID Plot Group 7*

- 1 In the **Results** toolbar, click  **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Cut Point 3D 1**.



### *Point Graph 1*

- 1 Right-click **ID Plot Group 7** and choose **Point Graph**.
- 2 In the **Settings** window for **Point Graph**, locate the **y-Axis Data** section.
- 3 In the **Expression** text field, type `w`.
- 4 Locate the **x-Axis Data** section. From the **Parameter** list, choose **Expression**.
- 5 In the **Expression** text field, type `u`.
- 6 Click to expand the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **Cycle**.
- 7 From the **Width** list, choose **3**.
- 8 Click to expand the **Legends** section. Select the **Show legends** check box.
- 9 From the **Legends** list, choose **Manual**.

10 In the table, enter the following settings:

Legends
Gear - 1
Gear - 2
Gear - 3
Gear - 4



*Gear orbits, rotating frame*

- 1 In the **Model Builder** window, under **Results** click **ID Plot Group 7**.
- 2 In the **Settings** window for **ID Plot Group**, type Gear orbits, rotating frame in the **Label** text field.
- 3 Locate the **Title** section. From the **Title type** list, choose **Label**.
- 4 Locate the **Axis** section. Select the **Preserve aspect ratio** check box.
- 5 Locate the **Legend** section. From the **Position** list, choose **Lower left**.
- 6 In the **Gear orbits, rotating frame** toolbar, click  **Plot**.
- 7 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 8 Right-click **Gear orbits, rotating frame** and choose **Duplicate**.

*Point Graph 1*

- 1 In the **Model Builder** window, expand the **Gear orbits, rotating frame 1** node, then click **Point Graph 1**.
- 2 In the **Settings** window for **Point Graph**, locate the **y-Axis Data** section.
- 3 In the **Expression** text field, type `rotsld.ws_fix`.
- 4 Locate the **x-Axis Data** section. In the **Expression** text field, type `rotsld.us_fix`.

*Gear orbits, fixed frame*

- 1 In the **Model Builder** window, under **Results** click **Gear orbits, rotating frame 1**.
- 2 In the **Settings** window for **ID Plot Group**, type Gear orbits, fixed frame in the **Label** text field.
- 3 In the **Gear orbits, fixed frame** toolbar, click  **Plot**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.

*ID Plot Group 9*

Use the following instructions to plot the gear transmission errors and bearing forces as shown in [Figure 9](#) and [Figure 10](#) respectively.

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.

- 2 In the **Settings** window for **ID Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 3: Time Dependent/Solution 110 (5) (sol110)**.

*Global 1*



- 1 Right-click **ID Plot Group 9** and choose **Global**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:

Expression	Unit	Description
rotsld.grp1.th_el	deg	Transmission error (elasticity)
rotsld.grp2.th_el	deg	Transmission error (elasticity)


- 4 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **Cycle**.
- 5 From the **Width** list, choose **3**.
- 6 Locate the **Legends** section. From the **Legends** list, choose **Manual**.
- 7 In the table, enter the following settings:

Legends
Gear-1
Gear-2

*Gear DTEs*


- 1 In the **Model Builder** window, under **Results** click **ID Plot Group 9**.
- 2 In the **Settings** window for **ID Plot Group**, type Gear DTEs in the **Label** text field.
- 3 Locate the **Title** section. From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Dynamic Transmission Errors.
- 5 Locate the **Legend** section. From the **Position** list, choose **Lower left**.
- 6 In the **Gear DTEs** toolbar, click  **Plot**.
- 7 Click the  **Zoom Extents** button in the **Graphics** toolbar.

*Cut Point 3D 2*

- 1 In the **Results** toolbar, click  **Cut Point 3D**.
- 2 In the **Settings** window for **Cut Point 3D**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 3: Time Dependent/Solution 110 (5) (sol110)**.
- 4 Locate the **Point Data** section. In the **X** text field, type 0.
- 5 In the **Y** text field, type  $1.25 \cdot d1$ .

- 6 In the **Z** text field, type 0.
- 7 From the **Snapping** list, choose **Snap to closest boundary**.

#### *ID Plot Group 10*

- 1 In the **Results** toolbar, click  **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Cut Point 3D 2**.

#### *Point Graph 1*

- 1 Right-click **ID Plot Group 10** and choose **Point Graph**.
- 2 In the **Settings** window for **Point Graph**, locate the **y-Axis Data** section.
- 3 In the **Expression** text field, type `rots1d.jrb2.f2`.
- 4 Locate the **Coloring and Style** section. Find the **Line style** subsection. From the **Line** list, choose **Cycle**.
- 5 From the **Width** list, choose **3**.
- 6 Locate the **Legends** section. From the **Legends** list, choose **Manual**.
- 7 Select the **Show legends** check box.
- 8 In the table, enter the following settings:

Legends
x-component

- 9 Right-click **Point Graph 1** and choose **Duplicate**.



#### *Point Graph 2*

- 1 In the **Model Builder** window, click **Point Graph 2**.
- 2 In the **Settings** window for **Point Graph**, locate the **y-Axis Data** section.
- 3 In the **Expression** text field, type `rots1d.jrb2.f3`.
- 4 Locate the **Legends** section. In the table, enter the following settings:


Legends
z-component

#### *Bearing forces*

- 1 In the **Model Builder** window, under **Results** click **ID Plot Group 10**.
- 2 In the **Settings** window for **ID Plot Group**, type **Bearing forces** in the **Label** text field.
- 3 Locate the **Title** section. From the **Title type** list, choose **Label**.

- 4 Locate the **Plot Settings** section.
- 5 Select the **y-axis label** check box. In the associated text field, type Force (N).
- 6 Locate the **Legend** section. From the **Position** list, choose **Lower left**.
- 7 In the **Bearing forces** toolbar, click  **Plot**.
- 8 Click the  **Zoom Extents** button in the **Graphics** toolbar.

#### *Animation 1*

- 1 In the **Results** toolbar, click  **Animation** and choose **Player**.
- 2 In the **Settings** window for **Animation**, locate the **Scene** section.
- 3 From the **Subject** list, choose **Stress (rotsld)**.
- 4 Locate the **Frames** section. In the **Number of frames** text field, type 50.

