

Transient Response of a Shallow Foundation on Unsaturated Soil

This example is an extension of the model Shallow Foundation on Unsaturated Soil. In the referred example, sudden changes in suction occur due to changes in the underground water level. In this example, the deformation of the clay stratum due to footing pressure and pore suction is analyzed after time-dependent changes in the boundary conditions. Two distinct natural events — a few days of rainfall and a few days of evaporation — are considered, after which the soil is subjected to a footing pressure.

The model is inspired by the example presented in Ref. 1. The Extended Barcelona Basic model (BBMx), which includes suction in its constitutive relationship, is used to demonstrate the behavior of a settlement on an unsaturated soil layer.

Model Definition

In this example, a 6 m wide and 3 m deep soil layer is studied. A 1 m wide footing is placed on top of the layer. The footing is modeled as a boundary load applied on the surface. The settlement analysis is carried out for an increasing footing pressure. Initially, in the first analysis, the ground water level is constant (3 m below the surface), and the footing pressure gradually increases to its final value. Once the final footing pressure is applied, a rainfall event with an infiltration rate of 10 cm/day is considered. The second scenario considers evaporation at a rate of 2 mm/day.

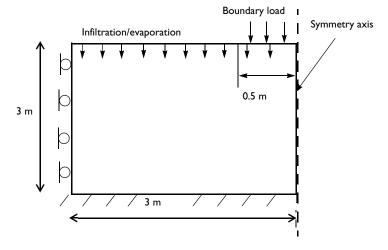


Figure 1: Dimensions, boundary conditions, pressure load, and flow rate for the unsaturated

SOIL PROPERTIES

The properties of the soil are given in Table 1.

TABLE I: MATERIAL PROPERTIES

Property	Variable	Value
Poisson's ratio	ν	0.2
Soil density	$ ho_{ m s}$	1743 kg/m ³
Water density	$\rho_{ m w}$	1000 kg/m ³
Dynamic viscosity of water	μ_{w}	0.001 Pa.s
Swelling index	κ	0.006
Swelling index for changes in suction	κ_{s}	0.008
Compression index at saturation	λ	0.22
Compression index for changes in suction	$\lambda_{ m s}$	0.123
Slope of critical state line	M	1.24
Weight parameter	w	0.4
Soil stiffness parameter	m	50 kPa
Plastic potential smoothing parameter	$b_{ m s}$	10
Tension to suction ratio	$k_{ m s}$	0.6
Initial yield value for suction	$s_{ m y}$	100 kPa
Initial void ratio	e_0	0.666
Reference pressure	$p_{ m ref}$	10 kPa
Initial consolidation pressure	p_{c0}	50 kPa
Initial porosity	ф	0.4
Saturated hydraulic conductivity	$k_{\rm sat}$	I m/day
Fitting parameter	α	2 I/m
Residual degree of saturation	$S_{ m res}$	0.23
Degree of saturation at full saturation	$S_{ m sat}$	I

The Richards' Equation interface requires additional material properties, which are derived from Table 1 and based on data from Ref. 1.

CONSTRAINTS AND LOADS

- The soil layer is supported by a rigid and perfectly rough base. Apply a fixed constraint on the lower horizontal boundary.
- Use a roller boundary condition on the left vertical boundary, symmetry on the right.

- A hydraulic head of 0 m is initially assigned to the lower horizontal boundary in the Richards' Equation interface.
- The infiltration and evaporation rates are applied in the Richards' Equation interface
 using the Precipitation node. Infiltration is represented by a positive quantity in the
 Precipitation node, and evaporation by a negative quantity.
- The gravity load is applied using the **Gravity** node. The pore pressure in the saturated region of the layer is applied using an **External Stress** node.
- A boundary load is applied on top of the soil layer to model the weight of the footing, see Figure 1.

Results and Discussion

Figure 2 shows the pressure head in the clay stratum after five days of rainfall (left) and five days of evaporation (right). The pressure head after five days of rainfall shows less variation across the layer due to the high infiltration rate. In contrast, with a low evaporation rate, the pressure head is almost linear with layer position and changes slightly at the top surface.

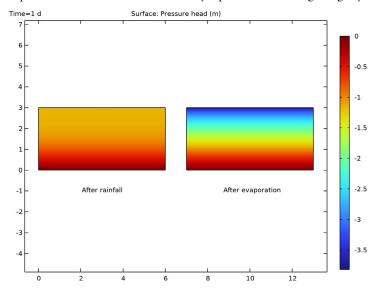


Figure 2: Pressure head after infiltration and evaporation.

The results presented in Figure 2 are emphasized in Figure 3 and Figure 4. With a high infiltration rate (Figure 3), the pressure head after 5 days of rainfall is within the range of 0–1 m instead of the initial range of 0–3 m. The pressure head after five days of rainfall

matches the Gardener steady state solution quite well. Figure 4 shows changes in the pressure head with a low evaporation rate, with the opposite trend as compared to Figure 3. Evaporation decreases the water content, which lowers the pressure head. Due to the low evaporation rate, changes in the pressure head are much smaller as compared to the changes due to the rainfall event, and mostly affect the region near the top surface. Again, the pressure head after five days of evaporation matches the Gardener steady state solution.

The distribution of the von Mises stress due to footing pressure is shown in Figure 5. Five days of rainfall reduces the suction and increases the pore pressure. The water in the pores can bear more load, which reduces the stresses in the soil skeleton, see Figure 6. Vice versa, after five days of evaporation, the stress in the soil skeleton increases slightly due to the reduced amount of water in the pores, see Figure 7.

The footing pressure versus settlement after the rainfall and evaporation events is shown in Figure 8 and Figure 9, respectively. The collapse of the soil under the footing is expected with increasing infiltration. Collapse also occurs after evaporation (although barely visible in the figure). The vertical displacement of the top layer due to rainfall and evaporation is different (see Figure 10); with rainfall there is a large collapse under the footing, whereas the collapse due to evaporation is not that drastic.

The changes in pore suction due to rainfall and evaporation is shown in Figure 11. Pore suction decreases during rainfall event, which results in positive volumetric strains in the soil layer (expansion of pores). Pore suction increases when considering evaporation, which results in a negative volumetric strain in the soil (compression of pores).

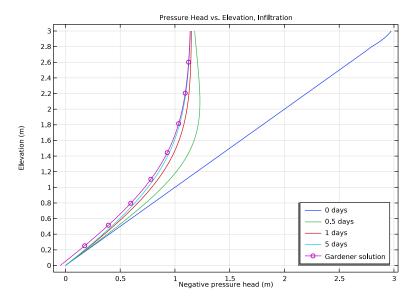


Figure 3: Pressure head versus elevation for rainfall event.

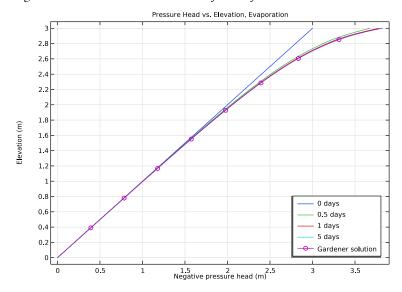


Figure 4: Pressure head versus elevation for evaporation event.

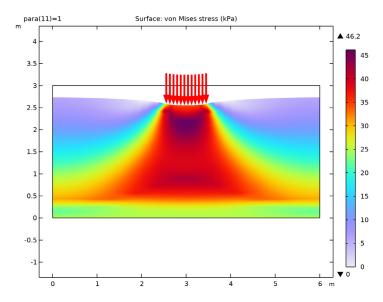


Figure 5: von Mises stress due to footing pressure.

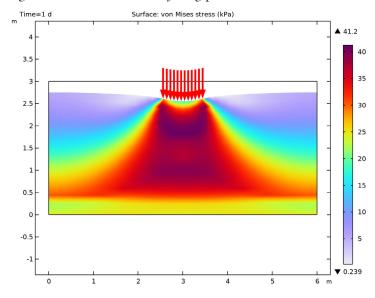


Figure 6: von Mises stress due to footing pressure after five days of rainfall.

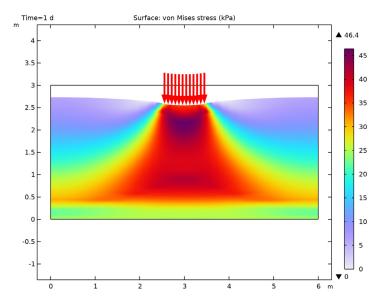


Figure 7: von Mises stress due to footing pressure after five days of evaporation.

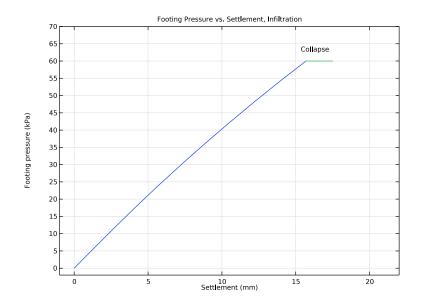


Figure 8: Footing pressure versus settlement after five days of rainfall.

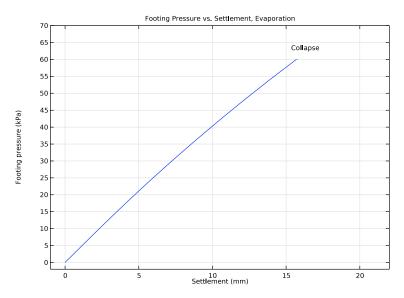


Figure 9: Footing pressure versus settlement after five days of evaporation.

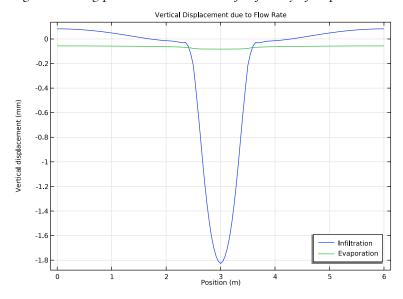


Figure 10: Vertical displacement of top layer of soil due to rainfall and evaporation.

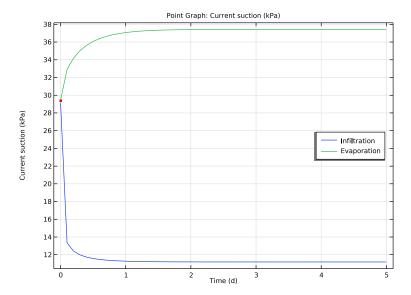


Figure 11: Changes in pore suction due to rainfall and evaporation.

Notes About the COMSOL Implementation

The model setup represents a unidirectional multiphysics coupling where changes in pore pressure affect the soil deformation, but changes in the deformation have no effect on the pore pressure.

The Cam-Clay family of soil models, like the MCC or BBMx models, do not define any stiffness at zero stress. To avoid numerical instabilities, prescribe an initial mean stress equal to the reference pressure at zero strain.

Reference

1. A.A. Abed and P.A. Vermeer, "Numerical Simulation of Unsaturated Soil Behavior," International Journal of Computer Applications in Technology, vol. 34, no. 1, 2009.

Application Library path: Geomechanics_Module/Soil/ settlement analysis transient

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click **2** 2D.
- 2 In the Select Physics tree, select Fluid Flow>Porous Media and Subsurface Flow> Richards' Equation (dl).
- 3 Right-click and choose Add Physics.
- 4 In the Select Physics tree, select Structural Mechanics>Solid Mechanics (solid).
- 5 Right-click and choose Add Physics.
- 6 Click \bigcirc Study.
- 7 In the Select Study tree, select General Studies>Stationary.
- 8 Click Done.

GEOMETRY I

Model parameters are available in the appended text file.

GLOBAL DEFINITIONS

Parameters 1

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- 4 Browse to the model's Application Libraries folder and double-click the file settlement_analysis_transient_parameters.txt.

Footing Pressure

- I In the Home toolbar, click f(x) Functions and choose Global>Interpolation.
- 2 In the Settings window for Interpolation, type Footing Pressure in the Label text field.
- 3 Locate the **Definition** section. In the **Function name** text field, type F P.

4 In the table, enter the following settings:

t	f(t)
0	0
1	60

5 Locate the **Units** section. In the **Argument** table, enter the following settings:

Argument	Unit
t	1

6 In the **Function** table, enter the following settings:

Function	Unit
F_P	kPa

DEFINITIONS

Variables 1

- I In the Model Builder window, expand the Component I (compl)>Definitions node.
- 2 Right-click **Definitions** and choose **Variables**. Model variables are available in the appended text file.
- 3 In the Settings window for Variables, locate the Variables section.
- 4 Click Load from File.
- 5 Browse to the model's Application Libraries folder and double-click the file settlement_analysis_transient_variables.txt.

Create half of the geometry by exploiting symmetry.

GEOMETRY I

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type 3.
- 4 In the **Height** text field, type 3.

Add a line segment to represent the foundation.

Line Segment I (Is I)

- I In the Geometry toolbar, click : More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 From the Specify list, choose Coordinates.
- 4 In the x text field, type 2.5.
- 5 In the y text field, type 3.
- **6** Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 7 In the x text field, type 3.
- 8 In the y text field, type 3.
- 9 Click | Build Selected.

MATERIALS

Add a **Porous Material** that contains information about the fluid and porous matrix properties together with the structural properties.

Porous Material I (pmat I)

In the Model Builder window, under Component I (compl) right-click Materials and choose More Materials>Porous Material.

Continue with setting up the physics. After that, the software automatically detects which material properties are required.

RICHARDS' EQUATION (DL)

Unsaturated Porous Medium 1

- In the Settings window for Unsaturated Porous Medium, locate the Porous Medium section.
- 2 From the Storage model list, choose User defined.

Porous Matrix I

- I In the Model Builder window, click Porous Matrix I.
- 2 In the Settings window for Porous Matrix, locate the Retention Model section.
- 3 From the Retention model list, choose User defined. In the $S_{\rm e}$ text field, type Se.
- 4 In the θ_l text field, type S_res*phi0+Se*(phi0-S_res*phi0).
- **5** In the C_{m} text field, type Cm.
- **6** In the κ_r text field, type k_rel.
- 7 In the θ_r text field, type S res*phi0.

Initial Values 1

- I In the Model Builder window, under Component I (compl)>Richards' Equation (dl) click Initial Values I.
- 2 In the Settings window for Initial Values, locate the Initial Values section.
- 3 Click the Hydraulic head button.

Hydraulic Head 1

- I In the Physics toolbar, click Boundaries and choose Hydraulic Head.
- 2 Select Boundary 2 only.

Symmetry I

- I In the Physics toolbar, click Boundaries and choose Symmetry.
- 2 Select Boundary 5 only.

Infiltration

- I In the Physics toolbar, click Boundaries and choose Precipitation.
- 2 In the Settings window for Precipitation, type Infiltration in the Label text field.
- **3** Select Boundaries 3 and 4 only.
- **4** Locate the **Precipitation** section. In the P_0 text field, type U_in.
- 5 Right-click Infiltration and choose Duplicate.

Evaporation

- I In the Model Builder window, under Component I (compl)>Richards' Equation (dl) click Infiltration 1.
- 2 In the Settings window for Precipitation, type Evaporation in the Label text field.
- **3** Locate the **Precipitation** section. In the P_0 text field, type -U_out.

Continue with setting up the Solid Mechanics interface.

SOLID MECHANICS (SOLID)

- I In the Model Builder window, under Component I (compl) click Solid Mechanics (solid).
- 2 In the Settings window for Solid Mechanics, locate the Structural Transient Behavior section.
- 3 From the list, choose Quasistatic.

Extended Barcelona Basic Model (BBMx)

I In the Physics toolbar, click **Domains** and choose **Elastoplastic Soil Material**.

- 2 In the Settings window for Elastoplastic Soil Material, type Extended Barcelona Basic Model (BBMx) in the Label text field.
- 3 Locate the Elastoplastic Soil Material section. From the Material model list, choose Extended Barcelona Basic.
- **4** From the *M* list, choose **From material**.
- **5** From the e_0 list, choose **From material**.
- **6** In the s_0 text field, type InitSuction.
- **7** In the *s* text field, type Suction.
- **8** In the p_{ref} text field, type pref.
- **9** In the p_{c0} text field, type pc0.
- **10** Select Domain 1 only.

External Stress 1

- I In the Physics toolbar, click Attributes and choose External Stress.
- 2 In the Settings window for External Stress, locate the External Stress section.
- 3 From the Stress input list, choose Pore pressure.
- **4** In the p_A text field, type PorePressure.
- **5** In the p_{ref} text field, type 0.
- 6 From the α_{B} list, choose User defined. In the associated text field, type 1.

Go to the material node and assign the required material properties.

MATERIALS

Porous Material I (pmat I)

- I In the Model Builder window, under Component I (compl)>Materials click Porous Material I (pmatl).
- 2 In the Settings window for Porous Material, locate the Porosity section.
- **3** In the $\varepsilon_{\rm p}$ text field, type phi0.
- 4 Locate the **Homogenized Properties** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Plastic potential smoothing parameter	bB	bb	I	Barcelona Basic
Density	rho	rhos	kg/m³	Basic

Property	Variable	Value	Unit	Property group
Compression index at saturation	lambdaComp0	lambda	I	Barcelona Basic
Poisson's ratio	nu	Nu	I	Young's modulus and Poisson's ratio
Weight parameter	wB	wb	I	Barcelona Basic
Initial yield value for suction	sy0	sy	Pa	Barcelona Basic
Slope of critical state line	М	Mb	1	Barcelona Basic
Compression index for changes in suction	lambdaCompss	lambda_s	I	Barcelona Basic
Swelling index for changes in suction	kappaSwellings	kappa_s	1	Barcelona Basic
Soil stiffness parameter	mB	mb	Pa	Barcelona Basic
Tension to suction ratio	kB	kb	1	Barcelona Basic
Swelling index	kappaSwelling	kappa	I	Barcelona Basic
Initial void ratio	evoid0	e0	1	Barcelona Basic
Permeability	kappa_iso ; kappaii = kappa_iso, kappaij = 0	k	m²	Basic

⁵ Locate the Phase-Specific Properties section. Click 🙀 Add Required Phase Nodes.

Fluid I (pmat1.fluid1)

I In the Model Builder window, click Fluid I (pmat1.fluidI).

² In the Settings window for Fluid, locate the Material Contents section.

3 In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Density	rho	rhow	kg/m³	Basic
Dynamic viscosity	mu	muw	Pa·s	Basic
Porosity	epsilon	phi0	I	Porous model

SOLID MECHANICS (SOLID)

Gravity I

In the Physics toolbar, click A Global and choose Gravity.

Fixed Constraint I

- I In the Physics toolbar, click Boundaries and choose Fixed Constraint.
- 2 Select Boundary 2 only.

Roller I

- I In the Physics toolbar, click Boundaries and choose Roller.
- 2 Select Boundary 1 only.

Symmetry I

- I In the Physics toolbar, click Boundaries and choose Symmetry.
- 2 Select Boundary 5 only.

Boundary Load 1

- I In the Physics toolbar, click Boundaries and choose Boundary Load.
- 2 Select Boundary 4 only.
- 3 In the Settings window for Boundary Load, locate the Force section.
- **4** Specify the \mathbf{F}_{A} vector as



MESH I

Mapped I

- I In the Mesh toolbar, click Mapped.
- 2 In the Settings window for Mapped, click Build All.

STUDY: FOOTING PRESSURE

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study: Footing Pressure in the Label text field.

Step 1: Stationary

- I In the Model Builder window, under Study: Footing Pressure click Step 1: Stationary.
- 2 In the Settings window for Stationary, locate the Physics and Variables Selection section.
- 3 Select the Modify model configuration for study step check box.
- 4 In the tree, select Component I (compl)>Richards' Equation (dl)>Infiltration and Component I (compl)>Richards' Equation (dl)>Evaporation.
- **5** Right-click and choose **Disable**.
- 6 Click to expand the Study Extensions section. Select the Auxiliary sweep check box.
- 7 Click + Add.
- **8** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
para (Parameter)	range(0,0.1,1)	

9 In the Home toolbar, click **Compute**.

ADD PREDEFINED PLOT

- I In the Home toolbar, click Windows and choose Add Predefined Plot.
- 2 Go to the Add Predefined Plot window.
- 3 In the tree, select Study: Footing Pressure/Solution I (soll)>Solid Mechanics> Volumetric Plastic Strain (solid), Study: Footing Pressure/Solution I (soll)> Solid Mechanics>Void Ratio (solid), and Study: Footing Pressure/Solution I (soll)> Solid Mechanics>Applied Loads (solid).
- 4 Click Add Plot in the window toolbar.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Right-click and choose Add Study.

5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY: INFILTRATION

- I In the Settings window for Study, type Study: Infiltration in the Label text field.
- 2 Locate the Study Settings section. Clear the Generate default plots check box.

Step 1: Time Dependent

- I In the Model Builder window, under Study: Infiltration click Step 1: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** From the **Time unit** list, choose **d**.
- 4 In the Output times text field, type range (0,0.1,5).
- 5 From the Tolerance list, choose User controlled.
- 6 In the Relative tolerance text field, type 0.0001.
- 7 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 8 In the tree, select Component I (compl)>Richards' Equation (dl)>Evaporation.
- 9 Right-click and choose Disable.
- 10 Click to expand the Values of Dependent Variables section. Find the **Initial values of variables solved for subsection.** From the **Settings** list, choose User controlled.
- II From the Method list, choose Solution.
- 12 From the Study list, choose Study: Footing Pressure, Stationary.
- 13 From the Parameter value (para) list, choose Last.

Solution 2 (sol2)

- 2 In the Model Builder window, expand the Solution 2 (sol2) node.
- 3 In the Model Builder window, expand the Study: Infiltration>Solver Configurations> Solution 2 (sol2)>Time-Dependent Solver I node, then click Fully Coupled I.
- 4 In the Settings window for Fully Coupled, click to expand the Method and Termination section.
- 5 From the Nonlinear method list, choose Automatic (Newton).
- 6 In the Study toolbar, click **Compute**.

ADD STUDY

- I In the Study toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select General Studies> Time Dependent.
- 4 Right-click and choose Add Study.
- 5 In the Study toolbar, click Add Study to close the Add Study window.

STUDY: EVAPORATION

- I In the Settings window for Study, type Study: Evaporation in the Label text field.
- 2 Locate the Study Settings section. Clear the Generate default plots check box.

Step 1: Time Dependent

- I In the Model Builder window, under Study: Evaporation click Step 1: Time Dependent.
- 2 In the Settings window for Time Dependent, locate the Study Settings section.
- **3** From the **Time unit** list, choose **d**.
- 4 In the Output times text field, type range (0,0.1,5).
- **5** From the **Tolerance** list, choose **User controlled**.
- **6** In the **Relative tolerance** text field, type 0.0001.
- 7 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 8 In the tree, select Component I (compl)>Richards' Equation (dl)>Infiltration.
- 9 Right-click and choose Disable.
- 10 Locate the Values of Dependent Variables section. Find the **Initial values of variables solved for** subsection. From the **Settings** list, choose User controlled.
- II From the Method list, choose Solution.
- 12 From the Study list, choose Study: Footing Pressure, Stationary.
- 13 From the Parameter value (para) list, choose Last.

Solution 3 (sol3)

- I In the Study toolbar, click Show Default Solver.
- 2 In the Model Builder window, expand the Solution 3 (sol3) node.
- 3 In the Model Builder window, expand the Study: Evaporation>Solver Configurations> Solution 3 (sol3)>Time-Dependent Solver I node, then click Fully Coupled I.

- 4 In the Settings window for Fully Coupled, locate the Method and Termination section.
- 5 From the Nonlinear method list, choose Automatic (Newton).
- 6 In the Study toolbar, click **Compute**.

RESULTS

Mirror 2D I

- I In the Results toolbar, click More Datasets and choose Mirror 2D.
- 2 In the Settings window for Mirror 2D, locate the Axis Data section.
- 3 In row Point 1, set X to 3.
- 4 In row Point 2, set X to 3.
- 5 Click to expand the Advanced section. Select the Remove elements on the symmetry axis check box.
- 6 Right-click Mirror 2D I and choose Duplicate.

Mirror 2D 2

- I In the Model Builder window, click Mirror 2D 2.
- 2 In the Settings window for Mirror 2D, locate the Data section.
- 3 From the Dataset list, choose Study: Infiltration/Solution 2 (sol2).
- 4 Right-click Mirror 2D 2 and choose Duplicate.

Mirror 2D 3

- I In the Model Builder window, click Mirror 2D 3.
- 2 In the Settings window for Mirror 2D, locate the Data section.
- 3 From the Dataset list, choose Study: Evaporation/Solution 3 (sol3).

Pressure Head

- I In the Model Builder window, under Results click Pressure (dl).
- 2 In the Settings window for 2D Plot Group, type Pressure Head in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 2D 2.

Streamline 1

- I In the Model Builder window, expand the Pressure Head node.
- 2 Right-click Streamline I and choose Delete.

Surface

I In the Model Builder window, under Results>Pressure Head click Surface.

- 2 In the Settings window for Surface, locate the Expression section.
- **3** In the **Expression** text field, type dl. Hp.
- 4 Right-click Results>Pressure Head>Surface and choose Duplicate.

Surface 2

- I In the Model Builder window, click Surface 2.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 3.
- **4** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 5 Click to expand the Inherit Style section. From the Plot list, choose Surface.

Translation 1

- I Right-click Surface 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 7.
- 4 In the Pressure Head toolbar, click Plot.

Pressure Head

In the Model Builder window, under Results click Pressure Head.

Table Annotation I

- I In the Pressure Head toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- 4 Locate the Coloring and Style section. Clear the Show point check box.
- 5 Locate the Data section. Select the LaTeX markup check box.
- **6** In the table, enter the following settings:

x-coordinate y-coordinate		Annotation
1.8	-0.7	After rainfall
8.5	-0.7	After evaporation

Degree of Saturation, Infiltration

- I In the Model Builder window, under Results click Flownet (dl).
- 2 In the Settings window for 2D Plot Group, type Degree of Saturation, Infiltration in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 2D 2.

- 4 Click to expand the **Title** section. From the **Title type** list, choose **Manual**.
- 5 In the **Title** text area, type Degree of Saturation.
- 6 In the Model Builder window, expand the Degree of Saturation, Infiltration node.

Contour I, Streamline I

- I In the Model Builder window, under Results>Degree of Saturation, Infiltration, Ctrl-click to select Contour I and Streamline I.
- 2 Right-click and choose **Delete**.

Surface I

- I In the Model Builder window, right-click Degree of Saturation, Infiltration and choose Surface.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 2.
- 4 From the Time (d) list, choose 0.
- 5 Click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)>Richards' Equation>Retention model>dl.Se -Effective saturation - I.
- 6 Right-click Surface I and choose Duplicate.

Surface 2

- I In the Model Builder window, click Surface 2.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose From parent.
- 4 Locate the Inherit Style section. From the Plot list, choose Surface 1.

Translation 1

- I Right-click Surface 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 7.
- 4 In the Degree of Saturation, Infiltration toolbar, click Plot.

Degree of Saturation, Infiltration

In the Model Builder window, under Results click Degree of Saturation, Infiltration.

Table Annotation 1

I In the Degree of Saturation, Infiltration toolbar, click More Plots and choose Table Annotation.

- 2 In the Settings window for Table Annotation, locate the Coloring and Style section.
- **3** Clear the **Show point** check box.
- 4 Locate the Data section. Select the LaTeX markup check box.
- 5 From the Source list, choose Local table.
- **6** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
1.2	-0.7	Before rainfall
8.5	-0.7	After 5 days of \newline \$\qquad\$ rainfall

Degree of Saturation, Infiltration

- I In the Model Builder window, click Degree of Saturation, Infiltration.
- 3 Right-click Degree of Saturation, Infiltration and choose Duplicate.

Degree of Saturation, Evaporation

- I In the Model Builder window, click Degree of Saturation, Infiltration 1.
- 2 Drag and drop below Degree of Saturation, Infiltration.
- 3 In the Settings window for 2D Plot Group, type Degree of Saturation, Evaporation in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Mirror 2D 3.

Surface I

- I In the Model Builder window, expand the Degree of Saturation, Evaporation node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 3.

Table Annotation I

- I In the Model Builder window, click Table Annotation I.
- 2 In the Settings window for Table Annotation, locate the Data section.

3 In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
1.2	-0.7	Before evaporation
8.5	-0.7	After 5 days of \newline \$\;\;\$ evaporation

4 In the Degree of Saturation, Evaporation toolbar, click Plot.

Stress, Footing Pressure

- I In the Model Builder window, under Results click Stress (solid).
- 2 In the Settings window for 2D Plot Group, type Stress, Footing Pressure in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Mirror 2D 1.
- 4 Locate the Color Legend section. Select the Show maximum and minimum values check box.

Surface I

- I In the Model Builder window, expand the Stress, Footing Pressure node, then click Surface 1.
- 2 In the Settings window for Surface, locate the Expression section.
- 3 From the Unit list, choose kPa.
- 4 Click to expand the Quality section. From the Smoothing threshold list, choose None.

Arrow Line 1

- I In the Model Builder window, right-click Stress, Footing Pressure and choose Arrow Line.
- 2 In the Settings window for Arrow Line, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Solid Mechanics>Load>solid.F_Ax,solid.F_Ay - Load (spatial frame).
- **3** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- 4 Locate the Coloring and Style section. From the Arrow base list, choose Head.
- 5 Click to expand the Inherit Style section. From the Plot list, choose Surface 1.
- 6 Clear the Color check box.
- 7 Clear the Arrow scale factor check box.
- 8 Clear the Color and data range check box.

Deformation I

Right-click Arrow Line I and choose Deformation.

Stress, Footing Pressure

- I In the Stress, Footing Pressure toolbar, click **Plot**.
- 2 In the Model Builder window, under Results right-click Stress, Footing Pressure and choose **Duplicate**.

Stress. Infiltration

- I In the Model Builder window, click Stress, Footing Pressure I.
- 2 Drag and drop below Stress, Footing Pressure.
- 3 In the Settings window for 2D Plot Group, type Stress, Infiltration in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Mirror 2D 2.
- 5 In the Stress, Infiltration toolbar, click Plot.
- 6 Right-click Stress, Infiltration and choose Duplicate.

Stress, Evaporation

- I In the Model Builder window, click Stress, Infiltration 1.
- **2** Drag and drop below **Stress**, **Infiltration**.
- 3 In the Settings window for 2D Plot Group, type Stress, Evaporation in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Mirror 2D 3.
- 5 In the Stress, Evaporation toolbar, click **Plot**.

Volumetric Plastic Strain (solid)

- I In the Model Builder window, click Volumetric Plastic Strain (solid).
- 2 In the Settings window for 2D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 2.

Surface I

- I In the Model Builder window, expand the Volumetric Plastic Strain (solid) node.
- **2** Right-click **Surface I** and choose **Duplicate**.

Surface 2

- I In the Model Builder window, click Surface 2.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 3.
- **4** Locate the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Inherit Style section. From the Plot list, choose Surface 1.

Translation 1

- I Right-click Surface 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 7.

Volumetric Plastic Strain (solid)

- I In the Model Builder window, under Results click Volumetric Plastic Strain (solid).
- 2 In the Volumetric Plastic Strain (solid) toolbar, click Plot.

Table Annotation I

- I In the Volumetric Plastic Strain (solid) toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- 4 Locate the Coloring and Style section. Clear the Show point check box.
- **5** Locate the **Data** section. Select the **LaTeX markup** check box.
- **6** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
1.8	-0.7	After rainfall
8.5	-0.7	After evaporation

Void Ratio (solid)

- I In the Model Builder window, under Results click Void Ratio (solid).
- 2 In the Settings window for 2D Plot Group, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 2.

Surface I

- I In the Model Builder window, expand the Void Ratio (solid) node, then click Surface I.
- 2 In the Settings window for Surface, locate the Coloring and Style section.
- 3 Click Change Color Table.
- 4 In the Color Table dialog box, select Traffic>Traffic in the tree.
- 5 Click OK.
- 6 Right-click Surface I and choose Duplicate.

Surface 2

I In the Model Builder window, click Surface 2.

- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 3.
- **4** Locate the **Title** section. From the **Title type** list, choose **None**.
- 5 Locate the Inherit Style section. From the Plot list, choose Surface 1.

Translation 1

- I Right-click Surface 2 and choose Translation.
- 2 In the Settings window for Translation, locate the Translation section.
- 3 In the x text field, type 7.
- 4 In the Void Ratio (solid) toolbar, click Plot.

Void Ratio (solid)

- I In the Model Builder window, under Results click Void Ratio (solid).
- 2 Click Plot.

Table Annotation I

- I In the Void Ratio (solid) toolbar, click More Plots and choose Table Annotation.
- 2 In the Settings window for Table Annotation, locate the Data section.
- 3 From the Source list, choose Local table.
- 4 Locate the Coloring and Style section. Clear the Show point check box.
- **5** Locate the **Data** section. Select the **LaTeX markup** check box.
- **6** In the table, enter the following settings:

x-coordinate	y-coordinate	Annotation
1.8	-0.7	After rainfall
8.5	-0.7	After evaporation

Suction Changes

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 Drag and drop below Void Ratio (solid).
- 3 In the Settings window for ID Plot Group, type Suction Changes in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Study: Infiltration/ Solution 2 (sol2).
- 5 Locate the Legend section. From the Position list, choose Middle right.

Point Graph 1

I Right-click Suction Changes and choose Point Graph.

- **2** Select Point 5 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.
- **4** In the **Expression** text field, type Suction.
- 5 From the Unit list, choose kPa.
- **6** Click to expand the **Legends** section. Select the **Show legends** check box.
- 7 From the Legends list, choose Manual.
- **8** In the table, enter the following settings:

Legends	
Infiltration	

9 Right-click Point Graph I and choose Duplicate.

Point Graph 2

- I In the Model Builder window, click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Study: Evaporation/Solution 3 (sol3).
- **4** Click to expand the **Title** section. From the **Title type** list, choose **None**.
- **5** Locate the **Legends** section. In the table, enter the following settings:

Legends Evaporation

Annotation I

- I In the Model Builder window, right-click Suction Changes and choose Annotation.
- 2 In the Settings window for Annotation, locate the Position section.
- 3 In the Y text field, type 29.4.
- 4 Locate the Coloring and Style section. From the Color list, choose Red.
- 5 In the Suction Changes toolbar, click Plot.

Suction Changes

Right-click Suction Changes and choose Duplicate.

Volume Changes

- I In the Model Builder window, click Suction Changes I.
- 2 Drag and drop below Suction Changes.
- 3 In the Settings window for ID Plot Group, type Volume Changes in the Label text field.

Point Graph 1

- I In the Model Builder window, expand the Volume Changes node, then click Point Graph I.
- 2 In the Settings window for Point Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type solid.epsm1.evols.

Point Graph 2

- I In the Model Builder window, click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type solid.epsm1.evols.

Annotation I

- I In the Model Builder window, click Annotation I.
- 2 In the Settings window for Annotation, locate the Position section.
- **3** In the **Y** text field, type **0**.
- 4 In the Volume Changes toolbar, click **Plot**.

Footing Pressure vs. Settlement, Infiltration

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 Drag and drop below Volume Changes.
- 3 In the Settings window for ID Plot Group, type Footing Pressure vs. Settlement, Infiltration in the Label text field.
- 4 Click to expand the **Title** section. From the **Title type** list, choose **Label**.
- 5 Locate the Plot Settings section.
- **6** Select the **x-axis label** check box. In the associated text field, type **Settlement** (mm).
- 7 Select the y-axis label check box. In the associated text field, type Footing pressure (kPa).
- 8 Locate the Axis section. Select the Manual axis limits check box.
- 9 In the x maximum text field, type 22.
- 10 In the y minimum text field, type -2.
- II In the y maximum text field, type 70.
- 12 Locate the Legend section. Clear the Show legends check box.

Point Graph 1

- I Right-click Footing Pressure vs. Settlement, Infiltration and choose Point Graph.
- **2** Select Point 5 only.
- 3 In the Settings window for Point Graph, locate the y-Axis Data section.

- **4** In the **Expression** text field, type F_P(para).
- 5 From the Unit list, choose kPa.
- 6 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 7 In the Expression text field, type abs(v-withsol('sol1',v,setval(para,0))).
- 8 From the Unit list, choose mm.
- **9** Click to expand the **Coloring and Style** section. From the **Width** list, choose **I**.
- 10 Right-click Point Graph I and choose Duplicate.

Point Graph 2

- I In the Model Builder window, click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the Data section.
- 3 From the Dataset list, choose Study: Infiltration/Solution 2 (sol2).

Annotation I

- I In the Model Builder window, right-click Footing Pressure vs. Settlement, Infiltration and choose Annotation.
- 2 In the Settings window for Annotation, locate the Annotation section.
- 3 In the **Text** text field, type Collapse.
- 4 Locate the **Position** section. In the **X** text field, type 15.
- **5** In the **Y** text field, type 65.
- 6 Locate the Coloring and Style section. Clear the Show point check box.
- 7 In the Footing Pressure vs. Settlement, Infiltration toolbar, click Plot.

Footing Pressure vs. Settlement, Infiltration

Right-click Footing Pressure vs. Settlement, Infiltration and choose Duplicate.

Footing Pressure vs. Settlement, Evaporation

- I In the Model Builder window, click Footing Pressure vs. Settlement, Infiltration I.
- 2 Drag and drop below Footing Pressure vs. Settlement, Infiltration.
- 3 In the Settings window for ID Plot Group, type Footing Pressure vs. Settlement, Evaporation in the Label text field.

Point Grabh 2

- I In the Model Builder window, expand the Footing Pressure vs. Settlement, Evaporation node, then click Point Graph 2.
- 2 In the Settings window for Point Graph, locate the Data section.

- 3 From the Dataset list, choose Study: Evaporation/Solution 3 (sol3).
- 4 In the Footing Pressure vs. Settlement, Evaporation toolbar, click Plot.

Cut Line 2D I

- I In the **Results** toolbar, click **Cut Line 2D**.
- 2 In the Settings window for Cut Line 2D, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 2.
- 4 Locate the Line Data section. In row Point 2, set x to 6.
- 5 In row Point 1, set y to 3.
- 6 In row Point 2, set y to 3.
- 7 Right-click Cut Line 2D I and choose Duplicate.

Cut Line 2D 2

- I In the Model Builder window, click Cut Line 2D 2.
- 2 In the Settings window for Cut Line 2D, locate the Data section.
- 3 From the Dataset list, choose Mirror 2D 3.

Vertical Disblacement

- I In the Results toolbar, click \to ID Plot Group.
- 2 Drag and drop below Footing Pressure vs. Settlement, Evaporation.
- 3 In the Settings window for ID Plot Group, type Vertical Displacement in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Cut Line 2D 1.
- **5** From the **Time selection** list, choose **Last**.
- 6 Locate the Title section. From the Title type list, choose Manual.
- 7 In the Title text area, type Vertical Displacement due to Flow Rate.
- 8 Locate the Plot Settings section.
- **9** Select the **x-axis label** check box. In the associated text field, type **Position** (m).
- 10 Select the y-axis label check box. In the associated text field, type Vertical displacement (mm).
- II Locate the Legend section. From the Position list, choose Lower right.

Line Grabh I

- I Right-click Vertical Displacement and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.

- 3 In the Expression text field, type v-withsol('sol1', v, setval(para, 1)).
- 4 From the **Unit** list, choose **mm**.
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 6 In the Expression text field, type cln1x.
- 7 Click to expand the **Legends** section. Select the **Show legends** check box.
- 8 From the Legends list, choose Manual.
- **9** In the table, enter the following settings:

Legends	
Infiltration	

10 Right-click Line Graph I and choose Duplicate.

Line Graph 2

- I In the Model Builder window, click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Cut Line 2D 2.
- **4** From the **Time selection** list, choose **Last**.
- **5** Locate the **Legends** section. In the table, enter the following settings:

Legends Evaporation

6 In the Vertical Displacement toolbar, click Plot.

Pressure Head vs. Elevation, Infiltration

- I In the Home toolbar, click **Add Plot Group** and choose ID Plot Group.
- 2 Drag and drop below Vertical Displacement.
- 3 In the Settings window for ID Plot Group, type Pressure Head vs. Elevation, Infiltration in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Study: Infiltration/ Solution 2 (sol2).
- 5 From the Time selection list, choose From list.
- **6** In the **Times (d)** list, choose **0**, **0.5**, **1**, and **5**.
- 7 Locate the Title section. From the Title type list, choose Label.
- 8 Locate the Plot Settings section.

- 9 Select the x-axis label check box. In the associated text field, type Negative pressure head (m).
- **10** Select the **y-axis label** check box. In the associated text field, type Elevation (m).
- II Locate the Legend section. From the Position list, choose Lower right.

Line Graph 1

- I Right-click Pressure Head vs. Elevation, Infiltration and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- **3** Click to select the **Activate Selection** toggle button.
- **4** Select Boundary 1 only.
- **5** Locate the **y-Axis Data** section. In the **Expression** text field, type Y.
- 6 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 7 In the Expression text field, type -dl.Hp.
- 8 In the Pressure Head vs. Elevation, Infiltration toolbar, click **Tool** Plot.
- **9** Locate the **Legends** section. Select the **Show legends** check box.
- 10 From the Legends list, choose Evaluated.
- II In the **Legend** text field, type eval(t, day) days.

Line Graph 2

- I In the Model Builder window, right-click Pressure Head vs. Elevation, Infiltration and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study: Infiltration/Solution 2 (sol2).
- 4 From the Time selection list, choose Last.
- **5** Select Boundary 1 only.
- 6 Locate the y-Axis Data section. In the Expression text field, type Y.
- 7 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 8 In the Expression text field, type -Hp_in.
- 9 Click to expand the Coloring and Style section. Find the Line markers subsection. From the Marker list, choose Circle.
- 10 From the Positioning list, choose Interpolated.
- II Locate the Legends section. Select the Show legends check box.
- 12 From the Legends list, choose Manual.

13 In the table, enter the following settings:

Legends Gardener solution

14 In the Pressure Head vs. Elevation, Infiltration toolbar, click Plot.

Pressure Head vs. Elevation, Infiltration

- I In the Model Builder window, click Pressure Head vs. Elevation, Infiltration.
- 2 Click Plot.
- 3 Right-click Pressure Head vs. Elevation, Infiltration and choose Duplicate.

Pressure Head vs. Elevation, Evaporation

- I In the Model Builder window, click Pressure Head vs. Elevation, Infiltration I.
- 2 Drag and drop below Pressure Head vs. Elevation, Infiltration.
- 3 In the Settings window for ID Plot Group, type Pressure Head vs. Elevation, Evaporation in the Label text field.
- 4 Locate the Data section. From the Dataset list, choose Study: Evaporation/ Solution 3 (sol3).

Line Graph 2

- I In the Model Builder window, expand the Pressure Head vs. Elevation, Evaporation node, then click Line Graph 2.
- 2 In the Settings window for Line Graph, locate the Data section.
- 3 From the Dataset list, choose Study: Evaporation/Solution 3 (sol3).
- 4 Locate the x-Axis Data section. In the Expression text field, type -Hp out.
- 5 In the Pressure Head vs. Elevation, Evaporation toolbar, click **Plot**.