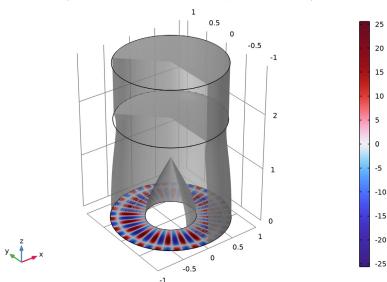


Flow Duct

The modeling of aircraft-engine noise attenuation is a central problem in the field of computational aeroacoustics (CAA). In this example you simulate the harmonically timevarying acoustic field from a turbofan engine, under various background flow conditions (a convected acoustic simulation), and analyze the modal sound transmission loss made possible by introducing a layer of lining inside the engine duct. The source is generated by a single mode excitation at a boundary, the source plane, see Figure 1. Sources and nonreflecting conditions are applied using port boundary conditions. The model analysis is performed in three steps, first computing the background mean flow (compressible irrotational potential flow), then analyzing the propagating modes with a boundary mode analysis, and finally solving the acoustic field in the flow duct with the linearized potential flow equations. Results are presented for situations with and without a background flow and for the cases of hard and lined duct walls.



M(2)=-0.5 Out-of-plane wave number=-0.89086 Source Plane: Acoustic Pressure, 3D (lpfbm)

Figure 1: Flow duct geometry and one of the propagating modes depicted at the so-called source plane.

The 2D axisymmetric duct geometry representation used in this model, shown in Figure 2, is taken from Ref. 1. It is an approximate model of the inlet section of a turbofan engine in the very common CFM56 series.

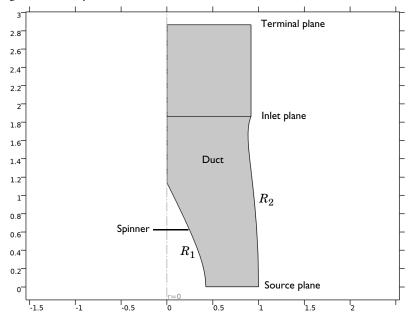


Figure 2: The duct geometry including reference planes used in the model.

The spinner and duct-wall profiles are given, respectively, by the equations

$$\begin{split} R_1(z') &= \max[0, 0.64212 - (0.04777 + 0.98234{z'}^2)^{1/2}] \\ R_2(z') &= 1 - 0.18453{z'}^2 + 0.10158 \frac{e^{-11(1-z')} - e^{-11}}{1 - e^{-11}} \end{split}$$

where $0 \le z' = z/L \le 1$, and L = 1.86393 is the duct length. A noise source is imposed at z' = 0, henceforth referred to as the *source plane*. This is where the fan would be located in the actual engine geometry. The plane z = L corresponds to the fore end of the engine and is referred to as the *inlet plane*. The attenuation of the liner for specific flow conditions is computed from the source plane to the inlet plane. A cylindrical domain, adjoined at the inlet plane and extending to the *terminal plane*, extends the modeling domain into a region where you can consider the mean flow as being uniform. This allows

you to impose the simple boundary condition of a constant velocity potential and a vanishing tangential velocity for the background flow. For the acoustic problem, port boundary conditions are used at the source plane and the terminal plane to set up ideal nonreflecting conditions as well as imposing the source.

The model will analyze so-called modal sound transmission, where a single propagating mode is used as source. In this particular example the first radial mode is used as the source, see Ref. 1 for details. All propagating modes are used when setting up the ports to ensure good nonreflecting performance. The sound transmission loss is computed from the source plane to the inlet plane. The power of the incident mode is defined through a predefined variable and the power of the transmitted sound at the inlet plane is computed as the integral of the axial intensity.

MODEL CONDITIONS

Assume that the flow in the axisymmetric duct is compressible, inviscid, perfectly isentropic, and irrotational. This is an assumption often used for the study of duct or engine acoustics. In this case the background mean flow is well described by the Compressible Potential Flow interface and the acoustic field is well described by the Linearized Potential Flow, Frequency Domain interface.

For more theory information on the governing equations, see the aeroacoustics theory chapter in the Acoustics Module User's Guide.

Compressible Potential Flow

This study examines two cases for the mean-flow normal velocity component at the source plane V_z , which (owing to the choice of reference speed) alternatively can be referred to as the source-plane axial Mach number M = -0.5, approximately representative of a passenger aircraft at cruising speed, and M = 0.

The governing equations are nondimensionalized in the present study. For the reference quantities in this model, choose the duct radius, the mean-flow speed of sound, and the mean-flow density at the source plane. Hence, all three of these quantities take the value 1.

The remaining boundary conditions for the mean flow consist of a natural boundary condition specifying the mass-flow rate through the source plane via the normal velocity and the density; slip conditions (vanishing tangential velocity) at the duct wall and at the spinner; and axial symmetry at r = 0.

Linearized Potential Flow

For the aeroacoustic field, the model considers two different boundary conditions at the duct wall:

- Sound hard the normal component of the acoustic particle velocity vanishes at the boundary.
- *Impedance* the normal component of the acoustic particle velocity is related to the particle displacement through the equation

$$i\omega(\mathbf{u}\cdot\mathbf{n}) = [i\omega + \mathbf{u}_0 \cdot \nabla - (\mathbf{n}\cdot(\mathbf{n}\cdot\nabla\mathbf{u}_0))]\frac{p}{Z}$$

where Z is the impedance, \mathbf{u}_0 is the mean background flow, p is the acoustic pressure, and \mathbf{u} is the acoustic velocity. This condition is often referred to as the *Ingard-Myers* impedance condition. This boundary condition, first derived by Myers (Ref. 2), was later recast in a weak form by Eversman (Ref. 3); it is this weak version, which is directly suitable for finite element modeling, that is implemented in the Acoustics Module's Linearized Potential Flow, Frequency Domain interface. The impedance boundary condition represents a lined duct wall. In this model, following Ref. 1, the impedance is taken to be Z = 2 - i.

The spinner, in contrast, is always assumed to be acoustically hard.

One of the configurations from Ref. 1 is studied in this model. This is the case where the dimensionless angular frequency (nondimensionalized through division by R_{∞}/c_{∞}) is $\omega=16$, and the azimuthal mode number is m=10. If you want to obtain a deeper understanding of the duct's aeroacoustic characteristics, you can, of course, perform a systematic exploration of parameter space by varying these quantities independently. Several more cases are examined in the reference paper.

Results and Discussion

THE MEAN-FLOW FIELD

For the nontrivial case of a source-plane axial Mach number of M = -0.5, the resulting mean-flow field appears in Figure 3. Note that the velocity potential is uniform well beyond the terminal plane, thus justifying the boundary condition imposed there. Furthermore, as could be expected, deviations from the mean density value appear primarily near the nonuniformities of the duct geometry, such as at the tip of the spinner.

As a complement, a more quantitative picture of the variations of the mean-flow velocity and density profiles along the axial direction (for r = 0.8) appear in the cross-section plots in Figure 4.

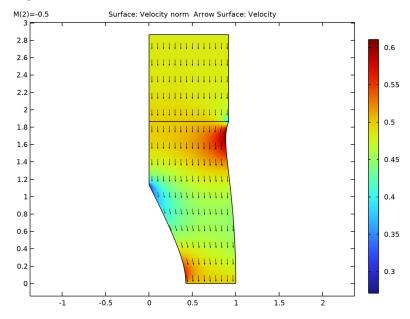


Figure 3: Mean-flow velocity potential and density for source-plane Mach number M = -0.5.

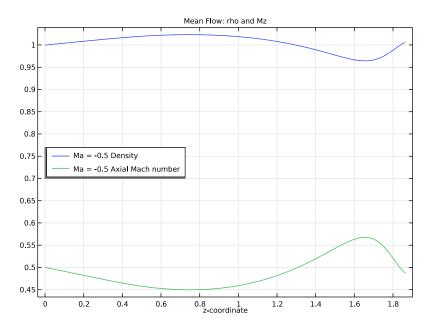


Figure 4: Mean-flow cross section plot at a sample radius of 0.8.

SOURCE PLANE MODES

With the solution for the mean-flow field at hand, it is possible to calculate the corresponding eigenmodes for the acoustic field at the ports. To use the modes at the ports it is necessary to know if they are incident or outgoing. In the no-flow case this is simply done by looking at the sign of the wave vector. The outgoing mode has a positive wave number and the incident is negative. However, in the flow case this is not the case, the presence of the mean background flow shifts the eigenvalues. Here it can be advantageous to look at the sign of the intensity vector at the port to identify the propagation direction.

A plot of the modes at the source plane (z=0) including the orientation of the axial intensity vector I_z is depicted in Figure 5 for the flow case (M=-0.5). The source plane is located below the duct, such that an incident mode has a positive intensity and vice versa.

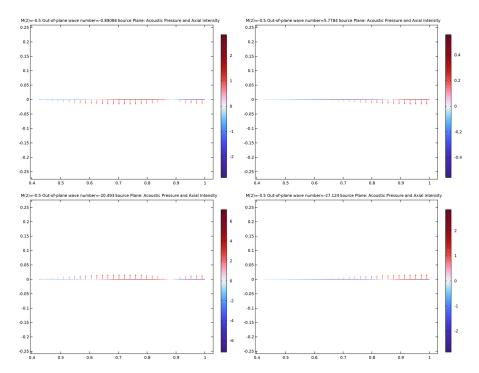


Figure 5: Mode pressures and axial intensity at the source plane (z = 0) for the case of a background flow with Mach number M = -0.5.

Figure 6 shows the resulting velocity-potential profile for all propagating modes at the source plane in the no-flow case (M = 0); and Figure 7 shows all the propagating modes in the flow case (M = -0.5). Notice that the mode profiles are not identical for the incident and outgoing modes (zoom in the graph in the model to see this clearly), indicating that the mean background flow is not uniform at this boundary.

Combining the information from all the plots, at the source plane, the mode identification necessary for the ports conditions can be done. In all cases the source is the first radial mode as defined in Ref. 1. See also the last two Evaluation Groups in the model where the solution index is shown for the various modes and flow conditions.

• At the source plane in the no-flow case (M = 0), the outgoing mode has the wave number $k_n = 10.8$. This is the first eigenvalue in solution list and thus as index 1

- (necessary for referencing at the port). The incident mode (the source) has wave number $k_{\rm n}$ = -10.8 (index 2).
- At the source plane in the flow case (M = -0.5), the outgoing modes have wave numbers are $k_{\rm n} = -0.9$ (index 1) and $k_{\rm n} = 5.8$ (index 2). The first incident radial mode (the source) has wave number $k_{\rm n} = -27.1$ (index 4). In the port condition the modes corresponding to the same mode shape should be defined together. This means that the first radial modes (index 2 and 4) are referenced in one port, and the second radial mode (index 1) is referenced in the second port (where no source is added).

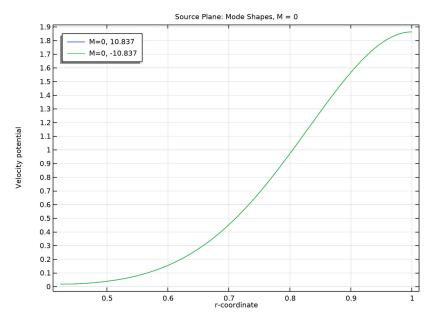


Figure 6: Propagating modes at the source plane for the no-flow case (M = 0).

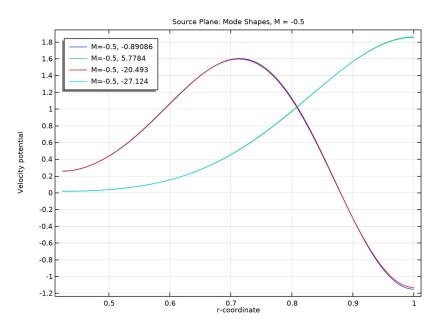


Figure 7: Propagating modes at the source plane for the flow case (M = -0.5).

TERMINAL PLANE MODES

A plot of the modes at the terminal plane (z = 1.86393) including the orientation of the axial intensity vector I_z is depicted in Figure 8 for the flow case (M = -0.5). The terminal plane is located above the duct, such that an incident mode has a negative intensity and vice versa.

Figure 9 shows the resulting velocity-potential profile for all propagating modes at the source plane in the no-flow case (M = 0); and Figure 10 shows all the propagating modes in the flow case (M = -0.5). Notice that the mode profiles are identical for the incident and outgoing mode, indicating that the mean background flow is uniform at this boundary (as expected).

Combining the information from all the plots, at the terminal plane, the mode identification necessary for the ports conditions can be done. See also the last two Evaluation Groups in the model where the solution index is shown for the various modes and flow conditions. No source is defined at the terminal plane.

• At the terminal plane in the no-flow case (M = 0), the outgoing mode has the wave number $k_n = 9.6$. This is the second eigenvalue in solution list and has solution index 2 (necessary for referencing at the port). No incident mode is necessary as no source is defined here.

• At the terminal plane in the flow case (M = -0.5), the outgoing modes have wave numbers $k_{\rm n}$ = 13.9 (index 3) and $k_{\rm n}$ = 24.9 (index 4). No incident mode is necessary as no source is defined here.

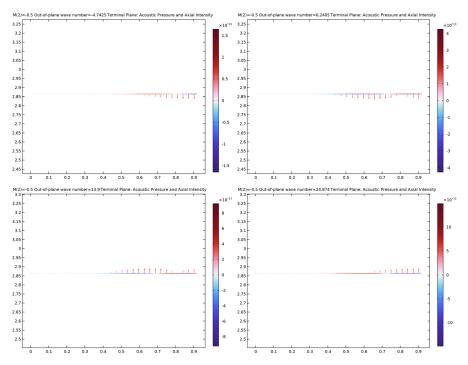


Figure 8: Mode pressures and axial intensity at the terminal plane for the case of a background flow with Mach number M=-0.5.

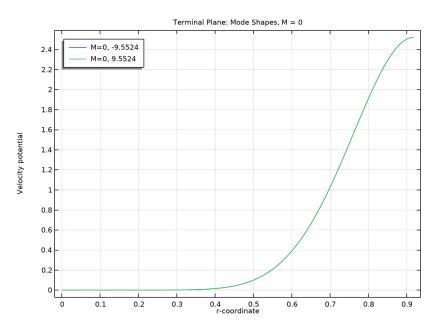


Figure 9: Propagating modes at the terminal plane for the no-flow case (M = 0).

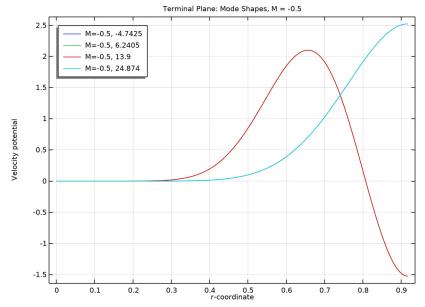


Figure 10: Propagating modes at the terminal plane for the flow case (M = -0.5).

THE AEROACOUSTIC FIELD

The normalized pressure fields for the case without a no background mean flow (M=0), shown in Figure 11, very closely match those for the corresponding finite element model (FEM) solutions presented in Figure 6 of Ref. 1. Similarly, the results for the attenuation between the source and inlet planes in the lined-wall case are in good agreement: 50.67 dB for the COMSOL Multiphysics solution versus 51.6 dB for the FEM solution, as shown in Table. 1 in Ref. 1.

Turning to the case with a mean flow (M = -0.5), the pressure field for the hard-wall as well as the lined wall (soft wall) cases in Figure 12 closely resembles the FEM solution obtained by Rienstra and Eversman in Ref. 1. This observation extends to the attenuation, for which the calculated value of 28.0 dB is in good agreement with the value of 27.2 dB obtained in Ref. 1.

Note that the source mode in the COMSOL Multiphysics calculation was derived for the case of a hard duct wall, whereas Rienstra and Eversman used a noise source adapted to the acoustic lining. However this fact does not seem to have a large influence on the solution for this particular problem. The propagating mode for the lined wall is actually a linear combination of the two hard-wall propagating modes.

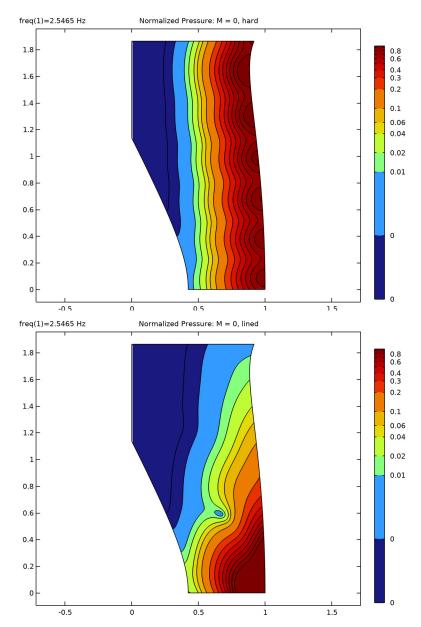


Figure 11: Acoustic pressure field for the cases of hard (top) and lined (bottom) duct wall with no mean flow (M=0); azimuthal mode number m=10 and angular frequency $\omega=16$.

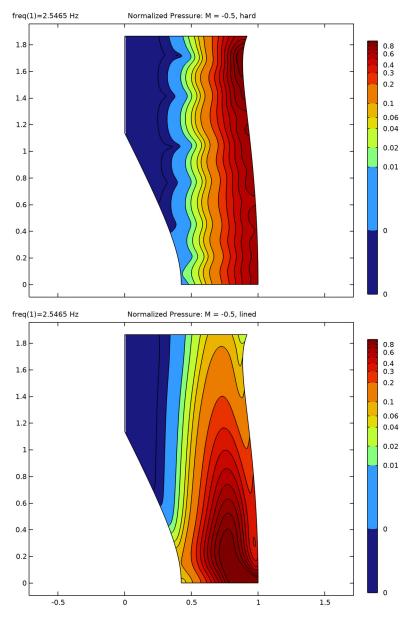


Figure 12: Acoustic pressure distribution for the cases of hard (top) and lined (bottom) duct wall with mean flow (M=-0.5); azimuthal mode number m=10 and angular frequency $\omega=16$.

PHYSICS INTERFACES

- Compressible Potential Flow (cpf) for modeling the background mean-flow velocity field as a potential flow (a lossless and irrotational flow).
- Linearized Potential Flow, Boundary Mode (lpfbm) for calculating the boundary eigenmode to be used by the port boundary conditions, defining outgoing and incident (the source) propagating acoustic field.
- Linearized Potential Flow, Frequency Domain (lpff) for modeling the timeharmonic acoustic field in the duct for the various excitation and flow condition.

REFERENCING THE ACOUSTIC MODES AT THE PORTS

The modes computed at the source plane and the terminal plane with the boundary mode interfaces need to be referenced and used by the port conditions. This is achieved by using the withsol() operator. The operator is called with a solution tag, referencing which solution it should look at, here the tag used depends on if the model is solved at the source ('sol3') or the terminal planes ('sol7'). The input is the variable needed, for example, phi_sp for the source plane potential or lpfbm.kn for the source plane mode wavenumber. Finally, the operator is called with two arguments using setval() to reference if the Mach number M is 0 or -0.5; and using setind() to set the solution index of the mode (of the eigenvalue lambda). For the index it is the number of the eigenvalue in the solution object. Note that lambda is always used as the internal eigenvalue variable in COMSOL Multiphysics.

References

- 1. S.W. Rienstra and W. Eversman, "A Numerical Comparison Between the Multiple-Scales and Finite-Element Solution for Sound Propagation in Lined Flow Ducts," J. Fluid Mech., vol. 437, pp. 367-384, 2001.
- 2. M.K. Myers, "On the Acoustic Boundary Condition in the Presence of Flow," J. Sound Vib., vol. 71, pp. 429-434, 1980.
- 3. W. Eversman, "The Boundary Condition at an Impedance Wall in a Non-Uniform Duct with Potential Mean Flow," J. Sound Vib., vol. 246, pp. 63-69, 2001. Errata: ibid, vol. 258, pp. 791-792, 2002.

Application Library path: Acoustics_Module/Aeroacoustics_and_Noise/flow_duct

Modeling Instructions

From the File menu, choose New.

NEW

In the New window, click Model Wizard.

MODEL WIZARD

- I In the Model Wizard window, click 2D Axisymmetric.
- 2 In the Select Physics tree, select Acoustics>Aeroacoustics> Compressible Potential Flow (cpf).
- 3 Click Add.
- 4 In the Select Physics tree, select Acoustics>Aeroacoustics>Linearized Potential Flow, Boundary Mode (lpfbm).
- 5 Click Add.
- **6** In the **Velocity potential (m^2/s)** text field, type phi_sp.

Here sp stands for source plane.

- 7 In the Select Physics tree, select Acoustics>Aeroacoustics>Linearized Potential Flow, Boundary Mode (lpfbm).
- 8 Click Add.
- 9 In the Velocity potential (m²/s) text field, type phi_tp.
 Here _tp stands for terminal plane.
- 10 In the Select Physics tree, select Acoustics>Aeroacoustics>Linearized Potential Flow, Frequency Domain (lpff).
- II Click Add.
- 12 Click Study.
- 13 In the Select Study tree, select Preset Studies for Some Physics Interfaces>Stationary.
- 14 Click Done.

ROOT

- I In the Model Builder window, click the root node.
- 2 In the root node's **Settings** window, locate the **Unit System** section.
- **3** From the **Unit system** list, choose **None**.

This setting turns off all unit support in the model.

GLOBAL DEFINITIONS

Parameters 1

Load the parameters from a file. They define model, geometry, and physical properties including the liner impedance. Then proceed and create the geometry of the duct.

- I In the Model Builder window, under Global Definitions click Parameters I.
- 2 In the Settings window for Parameters, locate the Parameters section.
- 3 Click Load from File.
- **4** Browse to the model's Application Libraries folder and double-click the file flow duct parameters.txt.

Proceed and draw the geometry of the engine duct. Use the Parametric Curve features to draw the shapes defined by the functions described in the main document.

GEOMETRY I

Parametric Curve I (bcl)

- I In the Geometry toolbar, click * More Primitives and choose Parametric Curve.
- 2 In the Settings window for Parametric Curve, locate the Expressions section.
- 3 In the r text field, type $1-0.18453*s^2+0.10158*(exp(-11*(1-s))-exp(-11))/$ (1-exp(-11)).
- 4 In the z text field, type s*zi.

Parametric Curve 2 (bc2)

- I In the Geometry toolbar, click * More Primitives and choose Parametric Curve.
- 2 In the Settings window for Parametric Curve, locate the Parameter section.
- 3 In the Maximum text field, type 0.7.
- 4 Locate the Expressions section. In the r text field, type 0.64212-sqrt (0.04777+ 0.98234*s^2).
- 5 In the z text field, type s*zi.

Line Segment I (Is I)

- I In the Geometry toolbar, click * More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 From the Specify list, choose Coordinates.
- 4 Locate the **Endpoint** section. From the **Specify** list, choose **Coordinates**.
- 5 In the z text field, type zi.

Union I (uni I)

- I In the Geometry toolbar, click Booleans and Partitions and choose Union.
- 2 Select the objects IsI and pc2 only.

Line Segment 2 (Is2)

- I In the Geometry toolbar, click More Primitives and choose Line Segment.
- 2 In the Settings window for Line Segment, locate the Starting Point section.
- 3 Click to select the Activate Selection toggle button for Start vertex.
- **4** On the object **unil**, select Point 5 only.
- 5 Locate the **Endpoint** section. Click to select the **Activate Selection** toggle button for **End vertex**.
- 6 On the object pc1, select Point 1 only.

Line Segment 3 (Is3)

- I In the Geometry toolbar, click * More Primitives and choose Line Segment.
- 2 On the object unil, select Point 4 only.
- 3 In the Settings window for Line Segment, locate the Endpoint section.
- 4 Click to select the Activate Selection toggle button for End vertex.
- 5 On the object pc1, select Point 2 only.
- 6 In the Geometry toolbar, click | Build All.

Delete Entities I (del I)

- I In the Model Builder window, right-click Geometry I and choose Delete Entities.
- 2 On the object unil, select Boundaries 1 and 3 only.
- 3 In the Settings window for Delete Entities, click | Build Selected.

Convert to Solid I (csoll)

- I In the Geometry toolbar, click Conversions and choose Convert to Solid.
- 2 Click in the **Graphics** window and then press Ctrl+D to clear all objects.

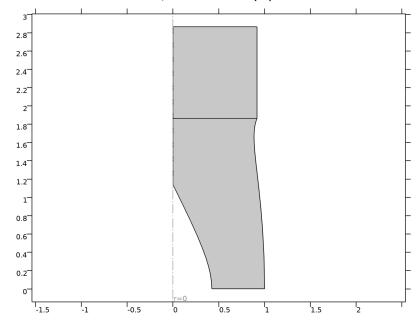
3 Click the Select All button in the Graphics toolbar.

Rectangle I (rI)

- I In the Geometry toolbar, click Rectangle.
- 2 In the Settings window for Rectangle, locate the Size and Shape section.
- 3 In the Width text field, type ri.
- 4 Locate the **Position** section. In the z text field, type zi.

Form Union (fin)

- I In the Geometry toolbar, click **Build All**.
- 2 Click the **Zoom Extents** button in the **Graphics** toolbar.
- 3 In the Model Builder window, click Form Union (fin).



Proceed and set up variables used for the results analysis. One is a normalized absolute pressure which uses a maximum operator over the domain. Define selections for the source, inlet and terminal planes. Finally, define an integration operator used to compute the power through the inlet plane.

DEFINITIONS

Variables 1

- I In the Model Builder window, under Component I (compl) right-click Definitions and choose Variables.
- 2 In the Settings window for Variables, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Domain.
- **4** Select Domain 1 only.
- **5** Locate the **Variables** section. In the table, enter the following settings:

Name	Expression	Unit	Description
Mz	-cpf.Vz		Axial Mach number
pabsn	<pre>abs(lpff.p)/ comp1.maxop1(lpff.p)</pre>		Normalized pressure

Source Plane

- I In the **Definitions** toolbar, click **\(\bigcap_{\bigcap} \) Explicit**.
- 2 In the Settings window for Explicit, type Source Plane in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 5 only.

Inlet Plane

- I In the **Definitions** toolbar, click 堶 **Explicit**.
- 2 In the Settings window for Explicit, type Inlet Plane in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 3 only.

Terminal Plane

- I In the **Definitions** toolbar, click **\(\) Explicit**.
- 2 In the Settings window for Explicit, type Terminal Plane in the Label text field.
- 3 Locate the Input Entities section. From the Geometric entity level list, choose Boundary.
- 4 Select Boundary 4 only.

Maximum I (maxop I)

- I In the **Definitions** toolbar, click Nonlocal Couplings and choose Maximum.
- 2 Select Domain 1 only.

Integration | (intob|)

- I In the Definitions toolbar, click Nonlocal Couplings and choose Integration.
- 2 In the Settings window for Integration, type intop ip in the Operator name text field.
- 3 Locate the Source Selection section. From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Inlet Plane.

Now proceed and set up the physics for the Compressible Potential Flow as well as the two Boundary Mode interfaces. The latter two are used to compute the propagating modes at the source and the terminal planes. The modes are used in the Port boundary conditions used for the frequency domain analysis.

COMPRESSIBLE POTENTIAL FLOW (CPF)

- I In the Model Builder window, under Component I (compl) click Compressible Potential Flow (cpf).
- 2 In the Settings window for Compressible Potential Flow, locate the Reference Values section.
- 3 In the p_{ref} text field, type cpf.rhoref^gamma/gamma.
- **4** In the ρ_{ref} text field, type rho0.
- **5** In the v_{ref} text field, type M.

Compressible Potential Flow Model 1

- I In the Model Builder window, under Component I (compl)> Compressible Potential Flow (cpf) click Compressible Potential Flow Model 1.
- 2 In the Settings window for Compressible Potential Flow Model, locate the **Compressible Potential Flow Model** section.
- **3** From the γ list, choose **User defined**. In the associated text field, type gamma.

Normal Flow 1

- I In the Physics toolbar, click Boundaries and choose Normal Flow.
- 2 In the Settings window for Normal Flow, locate the Boundary Selection section.
- 3 From the Selection list, choose Terminal Plane.

Mass Flow I

- I In the Physics toolbar, click Boundaries and choose Mass Flow.
- 2 In the Settings window for Mass Flow, locate the Boundary Selection section.
- 3 From the Selection list, choose Source Plane.

LINEARIZED POTENTIAL FLOW, BOUNDARY MODE (LPFBM)

- I In the Model Builder window, under Component I (compl) click Linearized Potential Flow, Boundary Mode (lpfbm).
- 2 In the Settings window for Linearized Potential Flow, Boundary Mode, locate the Boundary Selection section.
- 3 From the Selection list, choose Source Plane.
- **4** Locate the **Linearized Potential Flow Equation Settings** section. In the m text field, type m.

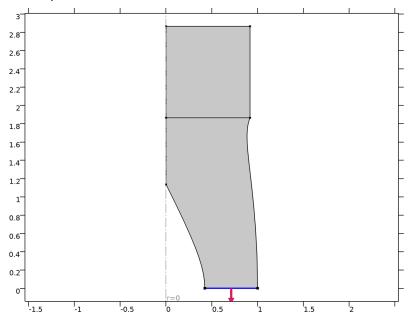
Linearized Potential Flow Model 1

- I In the Model Builder window, under Component I (compl)>Linearized Potential Flow, Boundary Mode (lpfbm) click Linearized Potential Flow Model I.
- 2 In the Settings window for Linearized Potential Flow Model, locate the Model Input section.
- **3** From the \mathbf{u}_0 list, choose **Velocity** (cpf/cpfl).
- **4** Locate the **Fluid Properties** section. From the ρ_0 list, choose **Density (cpf)**.
- 5 From the c_0 list, choose **Speed of sound (cpf/cpf1)**.

 Notice the orientation of the outward propagating normal, the surface of the outward propagating normal and the surface of the outward normal and the surface of the outward normal and the surface of the outward normal and the outward normal and the surface of the outward normal and the surface of the outward normal and the outward normal and the surface of the outward normal and the surface of the outward normal and the outward normal and the outward n

Notice the orientation of the outward propagating normal, the red arrow seen in the **Graphics** window. For consistency it should point out of the domains. It is possible to

reverse the orientation using the Reverse normal direction check box. This is not necessary here.



LINEARIZED POTENTIAL FLOW, BOUNDARY MODE 2 (LPFBM2)

- In the Model Builder window, under Component I (compl) click Linearized Potential Flow, Boundary Mode 2 (lpfbm2).
- 2 In the Settings window for Linearized Potential Flow, Boundary Mode, locate the Boundary Selection section.
- 3 From the Selection list, choose Terminal Plane.
- 4 Locate the Linearized Potential Flow Equation Settings section. In the m text field, type m.
- I In the Model Builder window, under Component I (compl)>Linearized Potential Flow, Boundary Mode 2 (Ipfbm2) click Linearized Potential Flow Model I.
- 2 In the Settings window for Linearized Potential Flow Model, locate the Model Input section.
- **3** From the \mathbf{u}_0 list, choose **Velocity** (cpf/cpfl).
- 4 Locate the Fluid Properties section. From the ρ_0 list, choose Density (cpf).
- **5** From the c_0 list, choose **Speed of sound (cpf/cpf1)**.

Set up a fully user defined mesh for the computational domain.

MESH I

Free Triangular 1

- I In the Mesh toolbar, click Free Triangular.
- 2 In the Settings window for Free Triangular, locate the Domain Selection section.
- 3 From the Geometric entity level list, choose Domain.
- 4 Select Domain 1 only.

Size 1

- I Right-click Free Triangular I and choose Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- **4** Locate the **Geometric Entity Selection** section. From the **Geometric entity level** list, choose **Point**.
- **5** Select Points 4 and 7 only.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type 0.005.

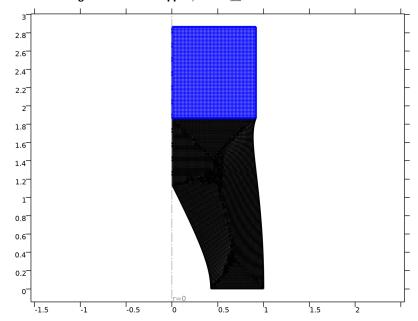
Size

- I In the Model Builder window, under Component I (compl)>Mesh I click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- **3** Click the **Custom** button.
- **4** Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type 0.015.
- 5 In the Minimum element size text field, type 0.001.

Mapped I

I In the Mesh toolbar, click Mapped.





Now, first solve the background flow and look at the results. The flow is solved for two Mach numbers using a Parametric Sweep.

STUDY I - BACKGROUND FLOW

- I In the Model Builder window, click Study I.
- 2 In the Settings window for Study, type Study 1 Background Flow in the Label text field.

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

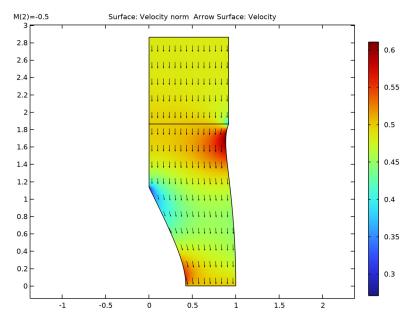
Parameter name	Parameter value list	Parameter unit
M (Mean flow Mach number)	0 -0.5	

5 In the Study toolbar, click **Compute**.

RESULTS

Arrow Surface 1

- I Right-click Mean Flow Velocity (cpf) and choose Arrow Surface.
- 2 In the Settings window for Arrow Surface, locate the Coloring and Style section.
- 3 From the Color list, choose Black.
- 4 In the Mean Flow Velocity (cpf) toolbar, click Plot.



Cut Line 2D I

- I In the Results toolbar, click Cut Line 2D.
- 2 In the Settings window for Cut Line 2D, locate the Line Data section.
- 3 In row Point I, set R to 0.8.
- 4 In row Point 2, set R to 0.8.
- 5 In row Point 2, set Z to zi.

Mean Flow: rho and Mz

- I In the Results toolbar, click \sim ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Mean Flow: rho and Mz in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Cut Line 2D 1.

- 4 From the Parameter selection (M) list, choose Last.
- 5 Click to expand the Title section. From the Title type list, choose Label.
- **6** Locate the **Legend** section. From the **Position** list, choose **Middle left**.

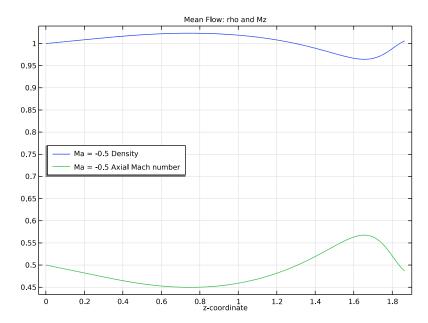
Line Graph 1

- I Right-click Mean Flow: rho and Mz and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- **3** In the **Expression** text field, type rho.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **5** In the **Expression** text field, type **z**.
- **6** Click to expand the **Legends** section. Select the **Show legends** check box.
- **7** Find the **Include** subsection. Select the **Description** check box.
- 8 Find the Prefix and suffix subsection. In the Prefix text field, type Ma = .
- 9 In the Mean Flow: rho and Mz toolbar, click Plot.

Line Graph 2

- I In the Model Builder window, right-click Mean Flow: rho and Mz and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the y-Axis Data section.
- 3 In the Expression text field, type Mz.
- 4 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 5 In the Expression text field, type z.
- **6** Locate the **Legends** section. Select the **Show legends** check box.
- **7** Find the **Include** subsection. Select the **Description** check box.
- 8 Find the Prefix and suffix subsection. In the Prefix text field, type Ma = .

9 In the Mean Flow: rho and Mz toolbar, click Plot.



Proceed to compute and analyze the mode shapes for the source plane. The **Rectangle** mode search method will be used as it can filter out all the evanescent modes by setting a small range for the imaginary part of the out-of-plane wave number. A parametric sweep is also performed solving for the two Mach numbers.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.
- 3 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode 2 (lpfbm2), and Linearized Potential Flow, Frequency Domain (lpff).
- 4 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Mode Analysis.
- 5 Click Add Study in the window toolbar.

STUDY 2 - SOURCE PLANE MODES

I In the Model Builder window, click Study 2.

2 In the Settings window for Study, type Study 2 - Source Plane Modes in the Label text field.

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- **4** In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
M (Mean flow Mach number)	0 -0.5	

Step 1: Mode Analysis

- I In the Model Builder window, click Step I: Mode Analysis.
- 2 In the Settings window for Mode Analysis, locate the Study Settings section.
- 3 In the Mode analysis frequency text field, type f.
- 4 From the Mode search method list, choose Rectangle.
- 5 In the Approximate number of modes text field, type 5.
- 6 In the Maximum number of modes text field, type 10.
- 7 Find the Rectangle search region subsection. In the Smallest real part (Out-ofplane wave number) text field, type -40.
- 8 In the Largest real part (Out-of-plane wave number) text field, type 40.
- 9 In the Smallest imaginary part (Out-of-plane wave number) text field, type -0.1.
- 10 In the Largest imaginary part (Out-of-plane wave number) text field, type 0.1.
- II Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 12 From the Method list, choose Solution.
- 13 From the Study list, choose Study I Background Flow, Stationary.
- **14** From the **Solution** list, choose **Solution 1** (soll).
- **15** In the **Study** toolbar, click **Compute**.

When setting up the Port boundary conditions it is necessary to know which modes are outgoing and incident. Simply knowing the sign of the computed out-of-plane wave number is not enough when a background flow is present and when higher order azimuthal modes are analyzed. In this case it is advantageous to plot the axial intensity

vector to identify the propagation directions. This is done by modifying the next default plot, here at the source plane.

RESULTS

Source Plane: Acoustic Pressure and Axial Intensity

- I In the **Settings** window for **2D Plot Group**, type Source Plane: Acoustic Pressure and Axial Intensity in the **Label** text field.
- 2 Click to expand the Selection section. From the Geometric entity level list, choose **Boundary**.
- 3 From the Selection list, choose Source Plane.
- 4 Select the Apply to dataset edges check box.
- **5** Click to expand the **Title** section. From the **Title type** list, choose **Label**.

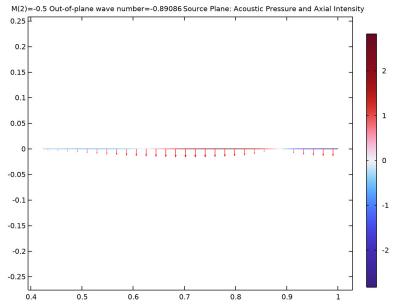
Arrow Line 1

- I Right-click Source Plane: Acoustic Pressure and Axial Intensity and choose Arrow Line.
- 2 In the Settings window for Arrow Line, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Linearized Potential Flow, Boundary Mode>Intensity>Ipfbm.Ir,Ipfbm.Iz Intensity.
- **3** Locate the **Expression** section. In the **R-component** text field, type **0**.
- 4 Locate the Arrow Positioning section. In the Number of arrows text field, type 30.
- 5 Locate the Coloring and Style section. From the Arrow length list, choose Logarithmic.

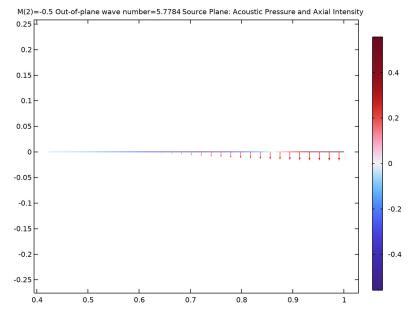
Source Plane: Acoustic Pressure and Axial Intensity

- I In the Model Builder window, click Source Plane: Acoustic Pressure and Axial Intensity.
- 2 In the Source Plane: Acoustic Pressure and Axial Intensity toolbar, click Plot.

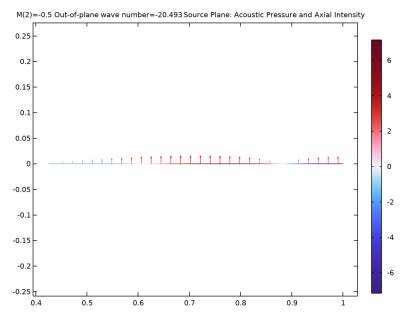
3 Click the **Zoom Extents** button in the **Graphics** toolbar.



- 4 In the Settings window for 2D Plot Group, locate the Data section.
- 5 From the Out-of-plane wave number list, choose 5.7784.

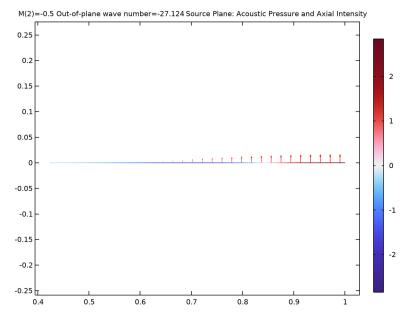


7 From the Out-of-plane wave number list, choose -20.493.



9 From the Out-of-plane wave number list, choose -27.124.

10 In the Source Plane: Acoustic Pressure and Axial Intensity toolbar, click Plot.



Looking at the four out-of-plane wave numbers (for the M = -0.5 case) it can be seen that the first two are inward propagating and the last two are outward propagating.

Revolution 2D I

- I In the Model Builder window, under Results>Datasets click Revolution 2D 1.
- 2 In the Settings window for Revolution 2D, click to expand the Advanced section.
- 3 In the Azimuthal mode number text field, type m.
- 4 Click to expand the **Revolution Layers** section. From the **Number of layers** list, choose **Fine**.

Source Plane: Acoustic Pressure, 3D (Ipfbm)

- I In the Model Builder window, under Results click Acoustic Pressure, 3D (lpfbm).
- 2 In the Settings window for 3D Plot Group, type Source Plane: Acoustic Pressure, 3D (lpfbm) in the Label text field.
- 3 Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Surface 2

- 1 Right-click Source Plane: Acoustic Pressure, 3D (Ipfbm) and choose Surface.
- 2 In the Settings window for Surface, locate the Data section.

- 3 From the Dataset list, choose Revolution 2D.
- **4** Locate the **Expression** section. In the **Expression** text field, type 1.
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Gray.

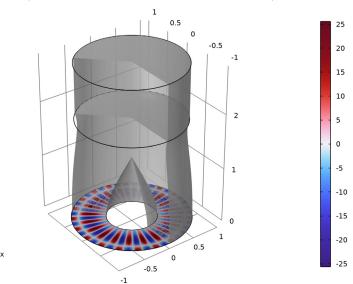
Selection I

- I Right-click Surface 2 and choose Selection.
- 2 Click in the **Graphics** window and then press Ctrl+A to select both domains.
- 3 In the Settings window for Selection, locate the Revolution Selection section.
- 4 Clear the **Evaluate the start cap** check box.
- 5 Clear the Evaluate the end cap check box.

Transparency I

- I In the Model Builder window, right-click Surface 2 and choose Transparency.
- 2 In the Settings window for Transparency, locate the Transparency section.
- 3 Set the Transparency value to 0.2.

M(2)=-0.5 Out-of-plane wave number=-0.89086 Source Plane: Acoustic Pressure, 3D (Ipfbm)



Next, set up a plot that shows the mode shapes at the source plane. Notice the small difference in the shape of the outgoing and incident modes. This is due to the fact that flow is not uniform at this boundary. In the frequency domain analysis the model will be excited by the first incident radial mode. For the M = -0.5 case, it can be seen to have the wave number -27.1 and it is number 4 in the list. See also the previous plot to verify the propagation direction.

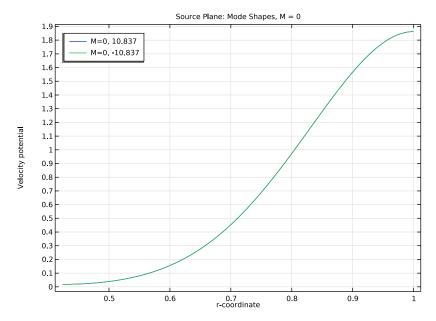
Source Plane: Mode Shapes, M = 0

- I In the Home toolbar, click Add Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Source Plane: Mode Shapes, M = 0 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2 Source Plane Modes/ Parametric Solutions 1 (sol3).
- 4 From the Parameter selection (M) list, choose First.
- **5** Click to expand the **Title** section. From the **Title type** list, choose **Label**.
- 6 Locate the Legend section. From the Position list, choose Upper left.

Line Graph 1

- I Right-click Source Plane: Mode Shapes, M = 0 and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Source Plane.
- 4 Locate the y-Axis Data section. In the Expression text field, type phi sp.
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- **6** In the **Expression** text field, type r.
- 7 Locate the **Legends** section. Select the **Show legends** check box.

8 In the Source Plane: Mode Shapes, M = 0 toolbar, click Plot.



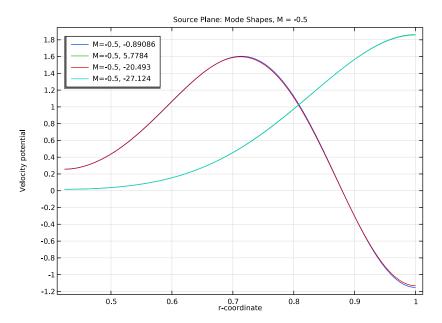
Source Plane: Mode Shapes, M = 0

In the Model Builder window, right-click Source Plane: Mode Shapes, M = 0 and choose Duplicate.

Source Plane: Mode Shapes, M = -0.5

- I In the Model Builder window, under Results click Source Plane: Mode Shapes, M = 0.1.
- 2 In the Settings window for ID Plot Group, type Source Plane: Mode Shapes, M = -0.5 in the Label text field.
- 3 Locate the Data section. From the Parameter selection (M) list, choose Last.

4 In the Source Plane: Mode Shapes, M = -0.5 toolbar, click Plot.



Now, proceed and set up the same analysis for the terminal plane, including study and results, as discussed above.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.
- 3 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode (lpfbm), and Linearized Potential Flow, Frequency Domain (lpff).
- 4 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Mode Analysis.
- 5 Click **Add Study** in the window toolbar.

STUDY 3 - TERMINAL PLANE MODES

- I In the Model Builder window, click Study 3.
- 2 In the Settings window for Study, type Study 3 Terminal Plane Modes in the Label text field.

Parametric Sweep

- I In the Study toolbar, click Parametric Sweep.
- 2 In the Settings window for Parametric Sweep, locate the Study Settings section.
- 3 Click + Add.
- 4 In the table, enter the following settings:

Parameter name	Parameter value list	Parameter unit
M (Mean flow Mach number)	0 -0.5	

Step 1: Mode Analysis

- I In the Model Builder window, click Step I: Mode Analysis.
- 2 In the Settings window for Mode Analysis, locate the Study Settings section.
- 3 In the Mode analysis frequency text field, type f.
- 4 From the Mode search method list, choose Rectangle.
- 5 In the Approximate number of modes text field, type 5.
- 6 In the Maximum number of modes text field, type 10.
- 7 Find the Rectangle search region subsection. In the Smallest real part (Out-ofplane wave number) text field, type -40.
- 8 In the Largest real part (Out-of-plane wave number) text field, type 40.
- 9 In the Smallest imaginary part (Out-of-plane wave number) text field, type -0.1.
- 10 In the Largest imaginary part (Out-of-plane wave number) text field, type 0.1.
- II Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 12 From the Method list, choose Solution.
- 13 From the Study list, choose Study I Background Flow, Stationary.
- 14 From the Solution list, choose Solution I (soll).
- 15 In the Study toolbar, click **Compute**.

RESULTS

Terminal Plane: Acoustic Pressure and Axial Intensity

I In the Settings window for 2D Plot Group, type Terminal Plane: Acoustic Pressure and Axial Intensity in the Label text field.

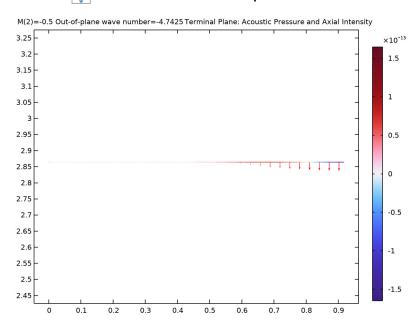
- 2 Click to expand the Selection section. From the Geometric entity level list, choose Boundary.
- 3 From the Selection list, choose Terminal Plane.
- 4 Select the Apply to dataset edges check box.
- **5** Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Arrow Line 1

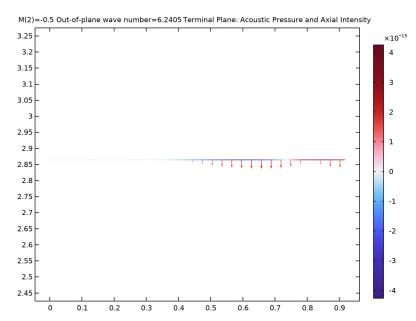
- I Right-click Terminal Plane: Acoustic Pressure and Axial Intensity and choose Arrow Line.
- 2 In the Settings window for Arrow Line, click Replace Expression in the upper-right corner of the Expression section. From the menu, choose Component I (compl)> Linearized Potential Flow, Boundary Mode 2>Intensity>lpfbm2.lr,lpfbm2.lz Intensity.
- **3** Locate the **Expression** section. In the **R-component** text field, type **0**.
- 4 Locate the Arrow Positioning section. In the Number of arrows text field, type 30.
- 5 Locate the Coloring and Style section. From the Arrow length list, choose Logarithmic.

Terminal Plane: Acoustic Pressure and Axial Intensity

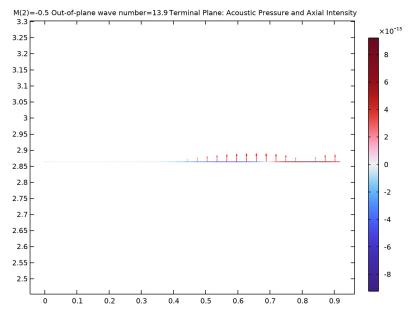
- I In the Model Builder window, click Terminal Plane: Acoustic Pressure and Axial Intensity.
- 2 In the Terminal Plane: Acoustic Pressure and Axial Intensity toolbar, click **Plot**.
- 3 Click the **Toom Extents** button in the **Graphics** toolbar.



- 4 In the Settings window for 2D Plot Group, locate the Data section.
- 5 From the Out-of-plane wave number list, choose 6.2405.
- 6 In the Terminal Plane: Acoustic Pressure and Axial Intensity toolbar, click Plot.

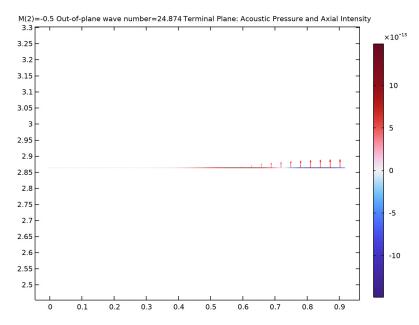


7 From the Out-of-plane wave number list, choose 13.9.



9 From the Out-of-plane wave number list, choose 24.874.

10 In the Terminal Plane: Acoustic Pressure and Axial Intensity toolbar, click Plot.



Revolution 2D 2

- I In the Model Builder window, under Results>Datasets click Revolution 2D 2.
- 2 In the Settings window for Revolution 2D, click to expand the Advanced section.
- 3 In the Azimuthal mode number text field, type m.
- 4 Click to expand the Revolution Layers section. From the Number of layers list, choose Fine.

Terminal Plane: Acoustic Pressure, 3D (lpfbm2)

- I In the Model Builder window, under Results click Acoustic Pressure, 3D (lpfbm2).
- 2 In the Settings window for 3D Plot Group, type Terminal Plane: Acoustic Pressure, 3D (1pfbm2) in the Label text field.
- 3 Click to expand the Title section. From the Title type list, choose Label.

Surface 2

- I Right-click Terminal Plane: Acoustic Pressure, 3D (lpfbm2) and choose Surface.
- 2 In the Settings window for Surface, locate the Data section.
- 3 From the Dataset list, choose Revolution 2D.
- **4** Locate the **Expression** section. In the **Expression** text field, type 1.

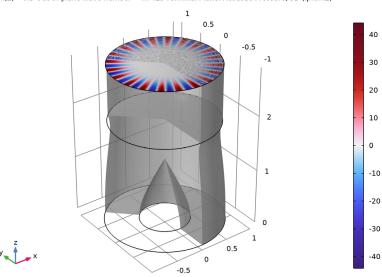
- 5 Locate the Coloring and Style section. From the Coloring list, choose Uniform.
- 6 From the Color list, choose Gray.

Selection 1

- I Right-click Surface 2 and choose Selection.
- 2 Click in the **Graphics** window and then press Ctrl+A to select both domains.
- 3 In the Settings window for Selection, locate the Revolution Selection section.
- 4 Clear the Evaluate the start cap check box.
- **5** Clear the **Evaluate the end cap** check box.

Transparency I

- I In the Model Builder window, right-click Surface 2 and choose Transparency.
- 2 In the Settings window for Transparency, locate the Transparency section.
- 3 Set the Transparency value to 0.2.



M(2)=-0.5 Out-of-plane wave number=-4.7425 Terminal Plane: Acoustic Pressure, 3D (lpfbm2)

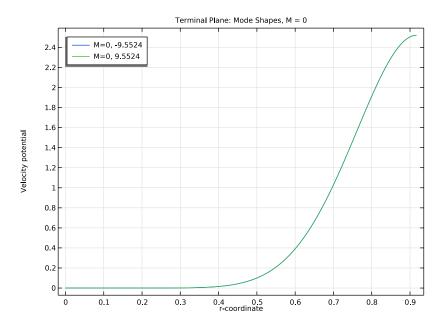
Terminal Plane: Mode Shapes, M = 0

- I In the Home toolbar, click <a>Plot Group and choose ID Plot Group.
- 2 In the Settings window for ID Plot Group, type Terminal Plane: Mode Shapes, M = 0 in the Label text field.

- 3 Locate the Data section. From the Dataset list, choose Study 3 Terminal Plane Modes/ Parametric Solutions 2 (sol7).
- 4 From the Parameter selection (M) list, choose First.
- **5** Click to expand the **Title** section. From the **Title type** list, choose **Label**.
- **6** Locate the **Legend** section. From the **Position** list, choose **Upper left**.

Line Graph 1

- I Right-click Terminal Plane: Mode Shapes, M = 0 and choose Line Graph.
- 2 In the Settings window for Line Graph, locate the Selection section.
- 3 From the Selection list, choose Terminal Plane.
- 4 Locate the y-Axis Data section. In the Expression text field, type phi_tp.
- 5 Locate the x-Axis Data section. From the Parameter list, choose Expression.
- 6 In the Expression text field, type r.
- 7 Locate the **Legends** section. Select the **Show legends** check box.
- 8 In the Terminal Plane: Mode Shapes, M = 0 toolbar, click Plot.

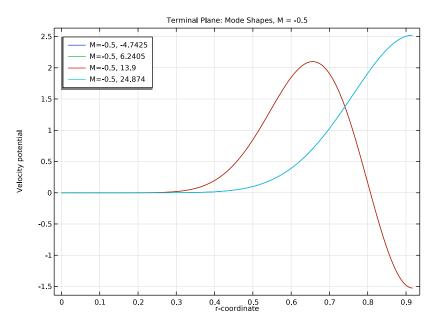


Terminal Plane: Mode Shapes, M = 0

In the Model Builder window, right-click Terminal Plane: Mode Shapes, M = 0 and choose Duplicate.

Terminal Plane: Mode Shapes, M = -0.5

- I In the Model Builder window, under Results click Terminal Plane: Mode Shapes, M = 0.1.
- 2 In the Settings window for ID Plot Group, type Terminal Plane: Mode Shapes, M = -0.5 in the Label text field.
- 3 Locate the Data section. From the Parameter selection (M) list, choose Last.
- 4 In the Terminal Plane: Mode Shapes, M = -0.5 toolbar, click Plot.



Finally, set up the physics and boundary conditions for the Linearized Potential Flow, Frequency Domain physics interface. Of particular importance is the set up of the Port conditions. The ports are divided into those applied at the source and inlet planes as well as their use in the flow and no flow cases. To reference the mode shapes and wave numbers the withsol() operator is used. Using the setval() and setind() statements it is possible to pick the desired mode.

LINEARIZED POTENTIAL FLOW, FREQUENCY DOMAIN (LPFF)

- I In the Model Builder window, under Component I (compl) click Linearized Potential Flow, Frequency Domain (lpff).
- 2 In the Settings window for Linearized Potential Flow, Frequency Domain, locate the Linearized Potential Flow Equation Settings section.
- 3 In the m text field, type m.

4 Locate the Global Port Settings section. From the Mode shape normalization list, choose Power normalization

MULTIPHYSICS

Background Potential Flow Coupling I (pfc1)

In the Physics toolbar, click Multiphysics Couplings and choose Global> **Background Potential Flow Coupling.**

LINEARIZED POTENTIAL FLOW, FREQUENCY DOMAIN (LPFF)

Impedance I

- I In the Physics toolbar, click Boundaries and choose Impedance.
- 2 Select Boundaries 6 and 8 only.
- 3 In the Settings window for Impedance, locate the Impedance (Ingard-Myers) section.
- **4** In the Z_n text field, type Zw.

Source Plane

- I In the Model Builder window, right-click Linearized Potential Flow, Frequency Domain (lpff) and choose Node Group.
- 2 In the Settings window for Group, type Source Plane in the Label text field.

Port I (for M = 0)

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Source Plane.
- 4 In the Label text field, type Port 1 (for M = 0).
- **5** Locate the **Port Outgoing Mode Settings** section. In the $\phi_n^{\ out}$ text field, type withsol('sol3',phi sp,setval(M,0),setind(lambda,1)).
- **6** In the $k_{\rm n}^{\rm out}$ text field, type withsol('sol3',lpfbm.kn,setval(M,0), setind(lambda,1)).
- 7 Locate the Port Incident Mode Settings section. From the Incident wave excitation at this port list, choose On.
- 8 In the $\phi_n^{~in}$ text field, type withsol('sol3',phi_sp,setval(M,0),setind(lambda, 2)).
- **9** In the k_n^{in} text field, type withsol('sol3',lpfbm.kn,setval(M,0), setind(lambda,2)).

10 From the Define incident wave list, choose Mode scale.

II In the S^{in} text field, type 1.

Port 2 (for
$$M = -0.5$$
)

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Source Plane.
- 4 In the Label text field, type Port 2 (for M = -0.5).
- 5 Locate the **Port Outgoing Mode Settings** section. In the $\phi_n^{\ out}$ text field, type withsol('sol3',phi_sp,setval(M,-0.5),setind(lambda,2)).
- **6** In the $k_{\rm n}^{\rm out}$ text field, type withsol('sol3',lpfbm.kn,setval(M,-0.5), setind(lambda,2)).
- 7 Locate the Port Incident Mode Settings section. From the Incident wave excitation at this port list, choose On.
- 8 In the $\phi_n^{~in}$ text field, type withsol('sol3',phi_sp,setval(M,-0.5), setind(lambda,4)).
- **9** In the $k_{\rm n}^{\rm in}$ text field, type withsol('sol3',lpfbm.kn,setval(M,-0.5), setind(lambda,4)).
- 10 From the Define incident wave list, choose Mode scale.
- II In the S^{in} text field, type 1.

Port 3 (for
$$M = -0.5$$
)

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Source Plane.
- 4 In the Label text field, type Port 3 (for M = -0.5).
- 5 Locate the **Port Outgoing Mode Settings** section. In the ϕ_n^{out} text field, type withsol('sol3',phi sp,setval(M,-0.5),setind(lambda,1)).
- **6** In the $k_{\rm n}^{\rm out}$ text field, type withsol('sol3',lpfbm.kn,setval(M,-0.5), setind(lambda,1)).

Terminal Plane

- I Right-click Linearized Potential Flow, Frequency Domain (Ipff) and choose Node Group.
- 2 In the Settings window for Group, type Terminal Plane in the Label text field.

```
Port 4 (for M = 0)
```

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, type Port 4 (for M = 0) in the Label text field.
- 3 Locate the Boundary Selection section. From the Selection list, choose Terminal Plane.
- **4** Locate the **Port Outgoing Mode Settings** section. In the ϕ_n^{out} text field, type withsol('sol7',phi tp,setval(M,0),setind(lambda,2)).
- 5 In the k_n^{out} text field, type withsol('sol7',lpfbm2.kn,setval(M,0), setind(lambda,2)).

```
Port 5 (for M = -0.5)
```

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Terminal Plane.
- 4 In the Label text field, type Port 5 (for M = -0.5).
- **5** Locate the **Port Outgoing Mode Settings** section. In the $\phi_n^{\ out}$ text field, type withsol('sol7',phi tp,setval(M,-0.5),setind(lambda,3)).
- **6** In the $k_{\rm n}^{\rm out}$ text field, type withsol('sol7',lpfbm2.kn,setval(M,-0.5), setind(lambda,3)).

Port 6 (for
$$M = -0.5$$
)

- I In the Physics toolbar, click Boundaries and choose Port.
- 2 In the Settings window for Port, locate the Boundary Selection section.
- 3 From the Selection list, choose Terminal Plane.
- 4 In the Label text field, type Port 6 (for M = -0.5).
- **5** Locate the **Port Outgoing Mode Settings** section. In the ϕ_n^{out} text field, type withsol('sol7',phi tp,setval(M,-0.5),setind(lambda,4)).
- **6** In the k_n^{out} text field, type withsol('sol7',lpfbm2.kn,setval(M,-0.5), setind(lambda,4)).

Solve the frequency domain model for the no-flow (M = 0) and flow (M = -0.5) cases as well as having a liner (finite impedance) and a sound hard configuration. Then analyze the results.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.

- 3 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode (lpfbm), and Linearized Potential Flow, Boundary Mode 2 (lpfbm2).
- 4 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 5 Click Add Study in the window toolbar.

STUDY 4 - FREQUENCY DOMAIN (M = 0, LINED)

- I In the Model Builder window, click Study 4.
- 2 In the Settings window for Study, type Study 4 Frequency Domain (M = 0, lined) in the Label text field.

Step 1: Frequency Domain

- I In the Model Builder window, under Study 4 Frequency Domain (M = 0, lined) click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type f.
- 4 Locate the **Physics and Variables Selection** section. Select the **Modify model configuration for study step** check box.
- 5 In the tree, select Component I (compl)>Linearized Potential Flow,
 Frequency Domain (lpff)>Source Plane>Port 2 (for M = -0.5), Component I (compl)>
 Linearized Potential Flow, Frequency Domain (lpff)>Source Plane>Port 3 (for M = -0.5),
 Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)>
 Terminal Plane>Port 5 (for M = -0.5), and Component I (compl)>
 Linearized Potential Flow, Frequency Domain (lpff)>Terminal Plane>Port 6 (for M = -0.5).
- 6 Click Disable.
- 7 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 8 From the Method list, choose Solution.
- 9 From the Study list, choose Study I Background Flow, Stationary.
- 10 From the Parameter value (M) list, choose 0.
- II In the Model Builder window, click Study 4 Frequency Domain (M = 0, lined).
- 12 In the Settings window for Study, locate the Study Settings section.
- 13 Clear the Generate default plots check box.

14 In the Home toolbar, click **Compute**.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.
- **3** Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode (lpfbm), and Linearized Potential Flow, Boundary Mode 2 (lpfbm2).
- 4 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 5 Click Add Study in the window toolbar.

STUDY 5 - FREQUENCY DOMAIN (M = 0, HARD)

- I In the Model Builder window, click Study 5.
- 2 In the Settings window for Study, type Study 5 Frequency Domain (M = 0. hard) in the Label text field.
- I In the Model Builder window, under Study 5 Frequency Domain (M = 0, hard) click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- **3** In the **Frequencies** text field, type f.
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)>Impedance I, Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)>Source Plane>Port 2 (for M = -0.5), Component I (compl)> Linearized Potential Flow, Frequency Domain (lpff)>Source Plane>Port 3 (for M = -0.5), Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)> Terminal Plane>Port 5 (for M = -0.5), and Component I (compl)> Linearized Potential Flow, Frequency Domain (lpff)>Terminal Plane>Port 6 (for M = -0.5).
- 6 Click ODisable.
- 7 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 8 From the Method list, choose Solution.
- 9 From the Study list, choose Study I Background Flow, Stationary.

- 10 From the Parameter value (M) list, choose 0.
- II In the Model Builder window, click Study 5 Frequency Domain (M = 0, hard).
- 12 In the Settings window for Study, locate the Study Settings section.
- 13 Clear the Generate default plots check box.
- 14 In the Home toolbar, click **Compute**.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.
- 3 Find the Physics interfaces in study subsection. In the table, clear the Solve check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode (lpfbm), and Linearized Potential Flow, Boundary Mode 2 (lpfbm2).
- 4 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 5 Click Add Study in the window toolbar.

STUDY 6 - FREQUENCY DOMAIN (M = -0.5, LINED)

- I In the Model Builder window, click Study 6.
- 2 In the Settings window for Study, type Study 6 Frequency Domain (M = -0.5, lined) in the Label text field.
- I In the Model Builder window, under Study 6 Frequency Domain (M = -0.5, lined) click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type f.
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Linearized Potential Flow,
 Frequency Domain (lpff)>Source Plane>Port I (for M = 0) and Component I (compl)>
 Linearized Potential Flow, Frequency Domain (lpff)>Terminal Plane>Port 4 (for M = 0).
- 6 Click O Disable.
- 7 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled
- 8 From the Method list, choose Solution.

- 9 From the Study list, choose Study I Background Flow, Stationary.
- 10 From the Parameter value (M) list, choose -0.5.
- II In the Model Builder window, click Study 6 Frequency Domain (M = -0.5, lined).
- 12 In the Settings window for Study, locate the Study Settings section.
- **13** Clear the **Generate default plots** check box.
- 14 In the Home toolbar, click **Compute**.

ADD STUDY

- I In the Home toolbar, click Windows and choose Add Study.
- 2 Go to the Add Study window.
- **3** Find the **Physics interfaces in study** subsection. In the table, clear the **Solve** check boxes for Compressible Potential Flow (cpf), Linearized Potential Flow, Boundary Mode (lpfbm), and Linearized Potential Flow, Boundary Mode 2 (lpfbm2).
- 4 Find the Studies subsection. In the Select Study tree, select General Studies> Frequency Domain.
- 5 Click Add Study in the window toolbar.

STUDY 7 - FREQUENCY DOMAIN (M = -0.5, HARD)

- I In the Model Builder window, click Study 7.
- 2 In the Settings window for Study, type Study 7 Frequency Domain (M = -0.5, hard) in the Label text field.
- I In the Model Builder window, under Study 7 Frequency Domain (M = -0.5, hard) click Step 1: Frequency Domain.
- 2 In the Settings window for Frequency Domain, locate the Study Settings section.
- 3 In the Frequencies text field, type f.
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)>Impedance I, Component I (compl)>Linearized Potential Flow, Frequency Domain (lpff)>Source Plane>Port I (for M = 0), and Component I (compl)> Linearized Potential Flow, Frequency Domain (lpff)>Terminal Plane>Port 4 (for M = 0).
- 6 Click ODisable.

- 7 Click to expand the Values of Dependent Variables section. Find the Values of variables not solved for subsection. From the Settings list, choose User controlled.
- 8 From the Method list, choose Solution.
- 9 From the Study list, choose Study I Background Flow, Stationary.
- 10 From the Parameter value (M) list, choose -0.5.
- II In the Model Builder window, click Study 7 Frequency Domain (M = -0.5, hard).
- 12 In the Settings window for Study, locate the Study Settings section.
- 13 Clear the Generate default plots check box.
- 14 In the Home toolbar, click **Compute**.

RESULTS

Normalized Pressure: M = 0, lined

- I In the Home toolbar, click Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Normalized Pressure: M = 0, lined in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 4 Frequency Domain (M = 0, lined)/Solution 10 (sol10).
- 4 Click to expand the Selection section. From the Geometric entity level list, choose Domain.
- **5** Select Domain 1 only.
- 6 Select the Apply to dataset edges check box.
- 7 Click to expand the **Title** section. From the **Title type** list, choose **Label**.

Contour I

- I Right-click Normalized Pressure: M = 0, lined and choose Contour.
- 2 In the Settings window for Contour, locate the Expression section.
- 3 In the Expression text field, type pabsn.
- 4 Locate the Levels section. From the Entry method list, choose Levels.
- **5** In the **Levels** text field, type 0.0001 0.001 0.01 0.02 0.04 0.06 0.1 0.2 0.3 0.4 0.5 0.6 0.7 0.8 0.9.
- 6 Locate the Coloring and Style section. From the Contour type list, choose Filled.
- 7 From the Scale list, choose Logarithmic.
- 8 In the Normalized Pressure: M = 0, lined toolbar, click Plot.

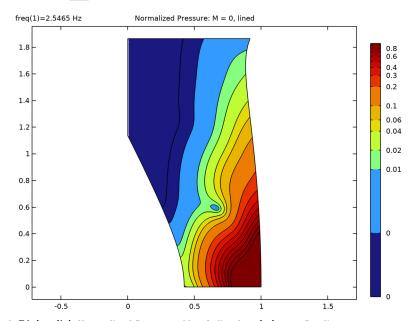
9 Right-click Contour I and choose Duplicate.

Contour 2

- I In the Model Builder window, click Contour 2.
- 2 In the Settings window for Contour, locate the Coloring and Style section.
- 3 From the Contour type list, choose Line.
- **4** From the **Coloring** list, choose **Uniform**.
- 5 From the Color list, choose Black.
- 6 Clear the Color legend check box.

Normalized Pressure: M = 0, lined

- I In the Model Builder window, click Normalized Pressure: M = 0, lined.
- 2 In the Normalized Pressure: M = 0, lined toolbar, click Plot.
- 3 Click the **Toom Extents** button in the **Graphics** toolbar.

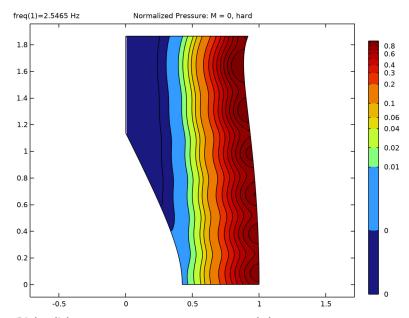


4 Right-click Normalized Pressure: M = 0, lined and choose Duplicate.

Normalized Pressure: M = 0, hard

- I In the Model Builder window, under Results click Normalized Pressure: M = 0, lined 1.
- 2 In the Settings window for 2D Plot Group, type Normalized Pressure: M = 0, hard in the Label text field.

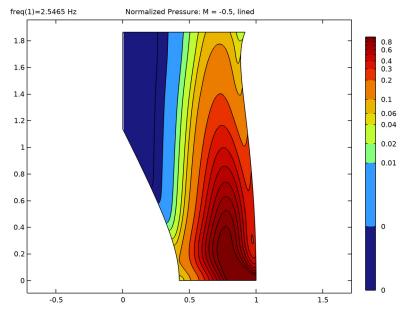
- 3 Locate the Data section. From the Dataset list, choose Study 5 Frequency Domain (M = 0, hard)/Solution 11 (sol11).
- 4 In the Normalized Pressure: M = 0, hard toolbar, click Plot.



5 Right-click Normalized Pressure: M = 0, hard and choose Duplicate.

Normalized Pressure: M = -0.5, lined

- I In the Model Builder window, under Results click Normalized Pressure: M = 0, hard I.
- 2 In the Settings window for 2D Plot Group, type Normalized Pressure: M = -0.5, lined in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 6 Frequency Domain (M = 0.5, lined)/Solution 12 (sol12).

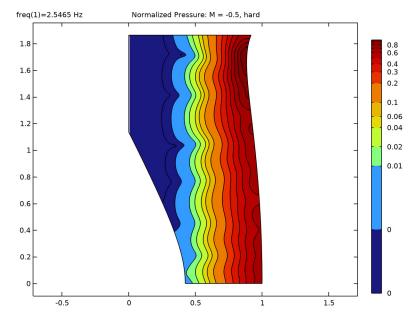


5 Right-click Normalized Pressure: M = -0.5, lined and choose Duplicate.

Normalized Pressure: M = -0.5, hard

- I In the Model Builder window, under Results click Normalized Pressure: M = -0.5, lined I.
- 2 In the Settings window for 2D Plot Group, type Normalized Pressure: M = -0.5, hard in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 7 Frequency Domain (M = -0.5, hard)/Solution 13 (sol13).

4 In the Normalized Pressure: M = -0.5, hard toolbar, click Plot.



Create an evaluation group for computing the attenuation of the propagating mode when the liner is present in the model.

Evaluation Group: Attenuation

- I In the Results toolbar, click Evaluation Group.
- 2 In the **Settings** window for **Evaluation Group**, type Evaluation Group: Attenuation in the **Label** text field.
- 3 Locate the Data section. From the Dataset list, choose None.

Global Evaluation 1

- I Right-click Evaluation Group: Attenuation and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- 3 From the Dataset list, choose Study 4 Frequency Domain (M = 0, lined)/ Solution 10 (sol10).
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
10*log10(lpff.port1.P_in/intop_ip(lpff.Iz))		M = 0, lined

Global Evaluation 2

- I In the Model Builder window, right-click Evaluation Group: Attenuation and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- 3 From the Dataset list, choose Study 6 Frequency Domain (M = -0.5, lined)/ Solution 12 (sol12).
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
10*log10(lpff.port2.P_in/		M = -0.5, lined
<pre>intop_ip(lpff.Iz))</pre>		

5 In the Evaluation Group: Attenuation toolbar, click **= Evaluate**.

Finally, create evaluation groups that help to identify the mode solution index related to a specific mode wave number and flow condition.

Source Plane: Mode Solution Index

- I In the Results toolbar, click Evaluation Group.
- 2 In the Settings window for Evaluation Group, type Source Plane: Mode Solution Index in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2 Source Plane Modes/ Parametric Solutions I (sol3).
- **4** Locate the **Transformation** section. Select the **Transpose** check box.

Global Evaluation 1

- I Right-click Source Plane: Mode Solution Index and choose Global Evaluation.
- 2 In the Settings window for Global Evaluation, locate the Data section.
- 3 From the Table columns list, choose Inner solutions.
- **4** Locate the **Expressions** section. In the table, enter the following settings:

Expression	Unit	Description
lpfbm.kn		kn

5 In the Source Plane: Mode Solution Index toolbar, click **Evaluate**.

Source Plane: Mode Solution Index

In the Model Builder window, right-click Source Plane: Mode Solution Index and choose Duplicate.

Terminal Plane: Mode Solution Index

- I In the Model Builder window, under Results click Source Plane: Mode Solution Index I.
- 2 In the Settings window for Evaluation Group, type Terminal Plane: Mode Solution Index in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 3 Terminal Plane Modes/ Parametric Solutions 2 (sol7).

Global Evaluation 1

- I In the Model Builder window, expand the Terminal Plane: Mode Solution Index node, then click Global Evaluation I.
- 2 In the Settings window for Global Evaluation, locate the Expressions section.
- **3** In the table, enter the following settings:

Expression	Unit	Description
lpfbm2.kn		kn

4 In the Terminal Plane: Mode Solution Index toolbar, click **=** Evaluate.