

Double Gauss Lens Image Simulation

If a lens has designed for an imaging application, it is useful to simulate the image that a user would expect see. In this tutorial we demonstrate how to load a bitmap that can be used as the object in a finite conjugate ray trace.

Model Definition

The model used in this simulation is the Double Gauss Lens found in the Ray Optics Module Application Library. The lens shown in Figure 1 is a 100 mm focal length lens by Lautenbacher & Brendel (see Ref. 1). Full details of this model (including instructions for creating the lens geometry) can be found in the Double Gauss Lens tutorial.

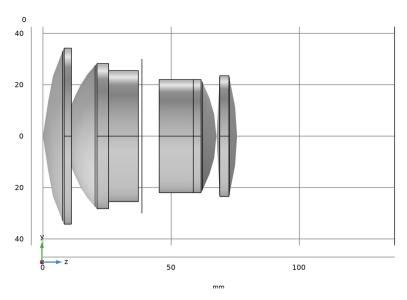


Figure 1: The Double Gauss Lens geometry sequence. Details of this lens are from Ref. 1.

STUDY I

The lens, which has an f/1.7 focal ratio and a 19° field of view, has a focal plane that is positioned for imaging an object at infinity. In this model we will place the bitmap at a distance of 1 meter in front of the lens. **Study I** is therefore used to determine the new finite conjugate focal plane.

We do this by releasing a cone of rays from the point on the optical axis intersecting the object plane. The rays can be made to ignore the image surface because, as can be seen in the Ray Diagram shown in Figure 2, the focus is now somewhere behind this plane.

The Spot Diagram feature can be used to automatically find the location of the best RMS focus (see Figure 3). The on-axis aberrations can also be seen in Figure 4. For more details see the Modeling Instructions at the end of this document.

Time=4.0028E-9 s Ray trajectories Surface: (1) Line: (1)

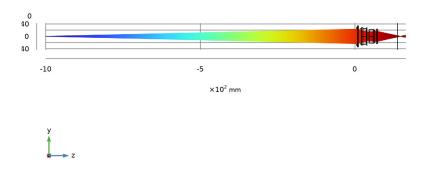


Figure 2: A ray diagram showing the finite conjugate ray trace. The rays now pas through the nominal focal plane.

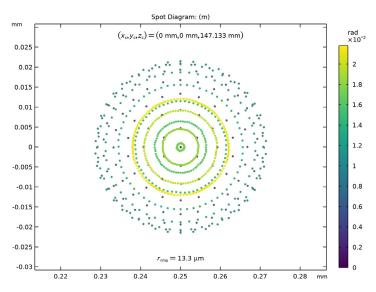


Figure 3: A spot diagram showing the global coordinates of the finite conjugate focal plane.

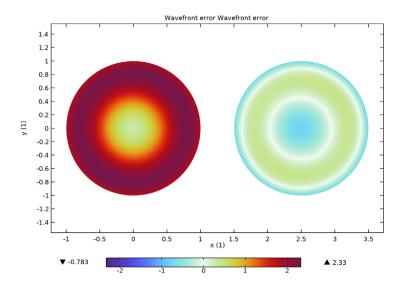


Figure 4: The aberration plot showing the wavefront error at the new focus. The left diagram includes all Zernike terms, whereas the right diagram does not include piston and defocus.

STUDY 2

The image simulation is performed using **Study 2**. First, the geometry is updated to locate the image plane at the new focus. In this simulation only a small section of the object surface will be sampled. Therefore, the geometry now includes rectangular surfaces on both the object and image planes (see Figure 5). These are approximately scaled so that an object (the bitmap) placed on the object surface will be imaged onto the section of the image plane defined by the image surface.

The **Mesh** is used to define the spatial sampling of the rays that are released from the object surface, and the spatial binning of rays on the image surface. A **Mapped** mesh with a **Distribution** set to have a fixed number of elements is applied to each of the object and image surfaces. The number of elements is npix on the image surface and 2*npix on the object surface.

The rays used in this simulation are defined using a **Release from Boundary** feature. The spatial density of these rays as they are released from the object surface is proportional to the value of the imported bitmap. Each ray is released into a solid angle approximately centered on the entrance pupil of the lens. A random sampling from within this cone gives a uniform distribution of rays across the entrance pupil.

Detailed step-by-step instructions can be found in the Modeling Instructions.

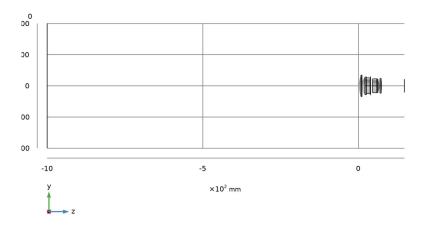


Figure 5: The Double Gauss Lens Image Simulation geometry. The object surface is on the left.

A simulation using 100,000 rays is shown in Figure 6 and Figure 7. Figure 8 shows the 2D image side by side with the original bitmap object.

Time=4.1696E-9 s Ray trajectories Surface: Refractive index, d-line (1) Surface: Image 1 Surface: Accumulated variable Inum (1)

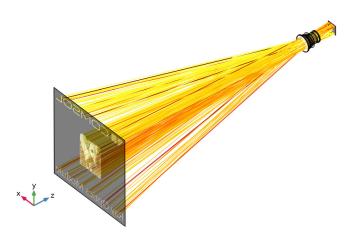


Figure 6: Ray diagram showing the object and image surfaces together with a fraction of the rays used in this simulation.

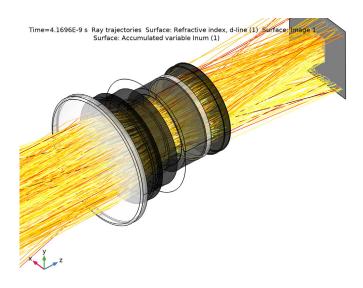


Figure 7: A closeup of the image simulation ray diagram.

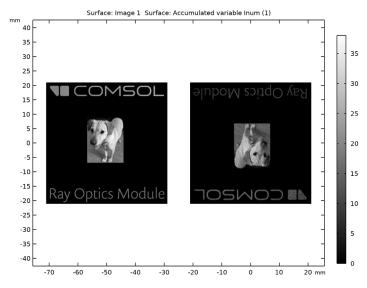


Figure 8: The object (left) and the resulting ray-traced image (right).

1. W.J. Smith, Modern lens design, vol. 2. New York, NY, USA: McGraw Hill, 2005.

Application Library path: Ray Optics Module/Lenses Cameras and Telescopes/ double gauss lens image simulation

Modeling Instructions

APPLICATION LIBRARIES

- I From the File menu, choose Application Libraries.
- 2 In the Application Libraries window, select Ray Optics Module> Lenses Cameras and Telescopes>double_gauss_lens in the tree.
- 3 Click Open.

COMPONENT I (COMPI)

For this simulation the diameter of the aperture stop is slightly reduced. This will slightly improve the image quality at the finite conjugate focus.

In the Model Builder window, expand the Component I (compl) node.

DOUBLE GAUSS LENS

Stop (pi4)

- I In the Model Builder window, expand the Component I (compl)>Double Gauss Lens node, then click Stop (pi4).
- 2 In the Settings window for Part Instance, locate the Input Parameters section.
- **3** In the table, enter the following settings:

Name	Expression	Value	Description
dl	0.80*d1_S	29.76 mm	Diameter, inner

GEOMETRICAL OPTICS (GOP)

Use the following steps to determine the distance to the finite conjugate focal plane.

Release from Grid 2

- I In the Model Builder window, under Component I (compl) right-click Geometrical Optics (gop) and choose Release from Grid. This will be used to release rays from the object plane.
- 2 In the Settings window for Release from Grid, locate the Initial Coordinates section.
- **3** In the $q_{z,0}$ text field, type -1[m].
- 4 Locate the Ray Direction Vector section. From the Ray direction vector list, choose Conical.
- 5 From the Conical distribution list, choose Hexapolar.
- **6** In the N_{θ} text field, type N_ring.
- **7** Specify the **r** vector as

nix	x
niy	у
niz	z

This is the direction of the optical axis.

8 In the α text field, type 0.70*atan(0.5*d1_clear_1/1[m]). This is the approximate angular size of the Double Gauss Lens entrance pupil as seen from the object plane.

STUDY I

Next, adjust the study to allow for the finite conjugate ray trace.

Step 1: Ray Tracing

- I In the Model Builder window, expand the Study I node, then click Step I: Ray Tracing.
- 2 In the Settings window for Ray Tracing, locate the Study Settings section.
- 3 In the Lengths text field, type 0 1200. The maximum optical path length now accounts for the distance to the object plane.
- 4 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 5 In the tree, select Component I (compl)>Geometrical Optics (gop)>Release from Grid I and Component I (compl)>Geometrical Optics (gop)>Image.
- **6** Right-click and choose **Disable**. This disables the original (infinite conjugate) release. It also allows the rays to pass through the image plane which needs to be repositioned.
- 7 In the Home toolbar, click **Compute**.

RESULTS

Ray Diagram 1

First, update the ray diagram to show the finite conjugate ray trace.

- I In the Settings window for 3D Plot Group, locate the Color Legend section.
- 2 Clear the Show legends check box.
- 3 Click → Plot Last.
- 4 In the Ray Diagram I toolbar, click Plot.
- 5 Click the 12 Zoom Extents button in the Graphics toolbar. Compare the result to Figure 2.

Spot Diagram

We now use the Spot Diagram feature to compute the new focus position.

- I In the Model Builder window, click Spot Diagram.
- 2 In the Settings window for 2D Plot Group, locate the Color Legend section.
- 3 From the Position list, choose Right.
- 4 Click → Plot Last.

Spot Diagram 1

- I In the Model Builder window, expand the Spot Diagram node.
- 2 Right-click Spot Diagram I and choose Disable. This spot diagram is no longer used in this modified study.

Spot Diagram 2

This spot diagram uses an Intersection Point Dataset.

- I In the Model Builder window, click Spot Diagram 2.
- 2 In the Settings window for Spot Diagram, click to expand the Inherit Style section.
- 3 From the Plot list, choose None.
- 4 Click to expand the Focal Plane Orientation section. Click Recompute Focal Plane Dataset. The Intersection Point Dataset will be repositioned to minimize the RMS spot size.

Color Expression 1

- I In the Model Builder window, click Color Expression I.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type at (0, gop.phic).

4 In the **Spot Diagram** toolbar, click Plot. The global coordinates this location can be now be seen in this plot. Compare the result to Figure 3.

Optical Aberration Diagram

Update the Optical Aberration Diagram to show the aberrations with the adjusted focus.

- I In the Model Builder window, under Results click Optical Aberration Diagram.
- 2 In the Settings window for 2D Plot Group, click Plot Last.

Optical Aberration 1

- I In the Model Builder window, click Optical Aberration I.
- 2 In the Settings window for Optical Aberration, locate the Focal Plane Orientation section.
- **3** Click **Recompute Reference Hemisphere Dataset**. This will also reposition this dataset at the location that minimizes the RMS spot size. Compare the result to Figure 4.

GLOBAL DEFINITIONS

Add a new parameters node containing details of the image simulation. A parameter defining the distance to the finite conjugate focal plane location is entered here. The total number of rays to use in the image simulation (Nrays) is also defined here.

Parameters 3: Image Simulation

- I In the Home toolbar, click Pi Parameters and choose Add>Parameters.
- 2 In the Settings window for Parameters, type Parameters 3: Image Simulation in the Label text field.
- **3** Locate the **Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
h_object	400.0[mm]	0.4 m	Object height
mag	9.5	9.5	Approximate magnification
h_image	h_object/mag	0.042105 m	Image height
Z_focus	147.124[mm]	0.14712 m	Finite conjugate focus
Nrays	250e3	2.5E5	Total number of rays
npix	300	300	Number of image pixels

In the following steps we add the object plane and update the location and size of the image plane.

4 In the Model Builder window, under Global Definitions right-click Geometry Parts and choose Part Libraries

PART LIBRARIES

- I In the Part Libraries window, select Ray Optics Module>3D>Apertures and Obstructions> rectangular_planar_annulus in the tree.
- 2 Click Add to Model.

DOUBLE GAUSS LENS

Image (þi8)

- I In the Model Builder window, under Component I (compl)>Double Gauss Lens click Image (pi8).
- 2 In the Settings window for Part Instance, locate the Part section.
- 3 From the Part list, choose Rectangular Planar Annulus. This will convert the image plane from circular to rectangular.
- **4** Locate the **Input Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
w0	h_image	42.105 mm	Width, outer
h0	h_image	42.105 mm	Height, outer
wl	0	0 m	Width, inner
hl	0	0 m	Height, inner

- 5 Locate the Position and Orientation of Output section. Find the Coordinate system to match subsection. From the Take work plane from list, choose Lens I (pil).
- 6 From the Work plane list, choose Surface I vertex intersection (wpl).
- 7 Find the Displacement subsection. In the zw text field, type Z_focus. This is the zcomponent of the best focus position.

Object

- I In the Geometry toolbar, click A Part Instance and choose Rectangular Planar Annulus. This plane will to position the object (an imported bitmap) in this simulation.
- 2 In the Settings window for Part Instance, type Object in the Label text field.
- 3 Locate the **Input Parameters** section. In the table, enter the following settings:

Name	Expression	Value	Description
w0	h_object	400 mm	Width, outer
h0	h_object	400 mm	Height, outer

Name	Expression	Value	Description
wl	0	0 m	Width, inner
hl	0	0 m	Height, inner

- 4 Locate the Position and Orientation of Output section. Find the Coordinate system to match subsection. From the Take work plane from list, choose Lens I (pil).
- 5 From the Work plane list, choose Surface I vertex intersection (wpl).
- 6 Find the **Displacement** subsection. In the **zw** text field, type -1[m].
- 7 Click to expand the **Boundary Selections** section. Click to select row number 1 in the table.
- 8 Click New Cumulative Selection.
- 9 In the New Cumulative Selection dialog box, type Object Plane in the Name text field.
- IO Click OK.
- II In the Settings window for Part Instance, click **Build All Objects**. The new geometry for this model can be seen in Figure 5.

MESH I

Details of the mesh need to be defined to support the image simulation.

- I In the Model Builder window, under Component I (compl) right-click Mesh I and choose Size.
- 2 In the Settings window for Size, locate the Geometric Entity Selection section.
- 3 From the Geometric entity level list, choose Boundary.
- 4 From the Selection list, choose Clear Apertures.
- **5** Locate the **Element Size** section. Click the **Custom** button.
- 6 Locate the Element Size Parameters section.
- 7 Select the Maximum element size check box. In the associated text field, type 1.0.

Size

- I In the Model Builder window, click Size.
- 2 In the Settings window for Size, locate the Element Size section.
- 3 From the Predefined list, choose Extra fine. It is necessary to increase the level of the Physics-based mesh refinement to account for the increase in size of the model geometry.

Mapped I

- I In the Mesh toolbar, click A Boundary and choose Mapped. A mapped mesh will be used to define the spatial bins for releasing rays from the object, and for accumulating the image.
- 2 In the Settings window for Mapped, locate the Boundary Selection section.
- 3 From the Selection list, choose Object Plane.

Distribution I

- I Right-click Mapped I and choose Distribution.
- 2 Select Edges 1–3 and 160 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type 2*npix. This ensures that there are approximately two mesh elements (in each direction) on the object plane for each image mesh element.

Mapped 2

- I In the Mesh toolbar, click A Boundary and choose Mapped.
- 2 In the Settings window for Mapped, locate the Boundary Selection section.
- 3 From the Selection list, choose Image Plane.

Distribution 1

- I Right-click Mapped 2 and choose Distribution.
- 2 Select Edges 54–56 and 150 only.
- 3 In the Settings window for Distribution, locate the Distribution section.
- 4 In the Number of elements text field, type npix.

Free Tetrahedral I

- I In the Mesh toolbar, click A Free Tetrahedral.
- 2 In the Settings window for Free Tetrahedral, click **Build All**.

DEFINITIONS

In this section we load a bitmap to use as the object in this simulation.

Image I (im I)

- I In the Home toolbar, click f(x) Functions and choose Local>Image.
- 2 In the Settings window for Image, locate the File section.
- 3 Click **Browse**.

- **4** Browse to the model's Application Libraries folder and double-click the file double gauss lens image simulation example.png.
- 5 Locate the Coordinates section. In the x minimum text field, type -h_object/2.
- 6 In the x maximum text field, type h_object/2.
- 7 In the y minimum text field, type -h_object/2.
- 8 In the y maximum text field, type h_object/2.
- 9 Locate the File section. Click | Import.

GEOMETRICAL OPTICS (GOP)

Here we add a release to launch rays based on the imported bitmap.

Release from Boundary I

- In the Physics toolbar, click **Boundaries** and choose Release from Boundary.
- 2 In the Settings window for Release from Boundary, locate the Boundary Selection section.
- **3** From the **Selection** list, choose **Object Plane**. This is the Boundary Selection referenced in the geometry Part Instance that defines the object plane.
- 4 Locate the Initial Position section. From the Initial position list, choose Density.
- **5** In the N text field, type Nrays.
- **6** In the ρ text field, type comp1.im1(x,y). The number density of the rays launched from the object plane will be proportional to the value of the image at each launch location.
- 7 Locate the Ray Direction Vector section. From the Ray direction vector list, choose Conical.
- **8** In the $N_{\rm w}$ text field, type 1.
- **9** Specify the **r** vector as

x/z	x
y/z	у
1	z

This direction vector points to the center of the first plane of the first lens.

- **10** In the α text field, type 0.70*atan(0.5*d1_clear_1/abs(z)). The release angle is defined so that the entrance pupil is slightly overfilled.
- **II** From the **Sampling from distribution** list, choose **Random**. A random distribution ensures the entrance pupil is well sampled.

Image

In the Model Builder window, click Image.

Accumulator I

- I In the Physics toolbar, click 🧲 Attributes and choose Accumulator. This will be used to create the image in the focal plane.
- 2 In the Settings window for Accumulator, locate the Accumulator Settings section.
- 3 From the Accumulator type list, choose Count.
- 4 From the Accumulate over list, choose Rays in boundary elements.
- 5 In the Accumulated variable name text field, type Inum.
- 6 In the R text field, type 1. In this monochromatic simulation, each time a ray hits the image plane it is summed to create the final image.

Before adding a new study (Study 2), first update Study 1.

STUDY I

Steb 1: Ray Tracing

- I In the Model Builder window, under Study I click Step I: Ray Tracing.
- 2 In the Settings window for Ray Tracing, locate the Physics and Variables Selection section.
- 3 In the tree, select Component I (compl)>Geometrical Optics (gop)> Release from Boundary 1. This release is not used in the existing study.
- 4 Right-click and choose Disable.

ADD STUDY

- I In the Home toolbar, click Add Study to open the Add Study window.
- 2 Go to the Add Study window.
- 3 Find the Studies subsection. In the Select Study tree, select Preset Studies for Selected Physics Interfaces>Ray Tracing.
- 4 Click Add Study in the window toolbar.
- 5 In the Home toolbar, click Add Study to close the Add Study window.

STUDY 2

- I In the Model Builder window, click Study 2.
- 2 In the Settings window for Study, locate the Study Settings section.
- 3 Clear the Generate default plots check box. Because an image simulation may involve a large number of rays, some plots may need to adjusted manually.

Step 1: Ray Tracing

- I In the Model Builder window, under Study 2 click Step I: Ray Tracing.
- 2 In the Settings window for Ray Tracing, locate the Study Settings section.
- 3 From the Time-step specification list, choose Specify maximum path length.
- 4 From the Length unit list, choose mm.
- 5 In the Lengths text field, type 0 1250.
- 6 Locate the Physics and Variables Selection section. Select the Modify model configuration for study step check box.
- 7 In the tree, select Component I (compl)>Geometrical Optics (gop)>Release from Grid I and Component I (compl)>Geometrical Optics (gop)>Release from Grid 2.
- **8** Right-click and choose **Disable**. These features are only used in Study 1.

RESULTS

- I In the Model Builder window, click Results.
- 2 In the Settings window for Results, locate the Update of Results section.
- **3** Select the **Only plot when requested** check box. This is to avoid rendering an unnecessarily large number of rays used in an image simulation.
- 4 In the Home toolbar, click **Compute**.

Rav 2

- I In the Model Builder window, expand the Results>Datasets node.
- 2 Right-click Results>Datasets and choose More Datasets>Ray.
- 3 In the Settings window for Ray, locate the Ray Solution section.
- **4** From the **Solution** list, choose **Solution 2 (sol2)**. This creates a second Ray dataset based on the solution to the new study.

Object Surface

- I In the Results toolbar, click More Datasets and choose Surface.
- 2 In the Settings window for Surface, type Object Surface in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).
- 4 Locate the Selection section. From the Selection list, choose Object Plane.

Image Surface

- I In the Results toolbar, click More Datasets and choose Surface.
- 2 In the Settings window for Surface, type Image Surface in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Study 2/Solution 2 (sol2).

4 Locate the Selection section. From the Selection list, choose Image Plane.

Use the following steps to create a 3D Ray Diagram together with the imported object and the accumulated image.

Ray Diagram 2

- I In the Model Builder window, under Results click Ray Diagram 2.
- 2 In the Settings window for 3D Plot Group, click > Plot Last.
- 3 Click the **Zoom Extents** button in the **Graphics** toolbar.

Ray Diagram 3

- I Right-click Ray Diagram 2 and choose Duplicate.
- 2 In the Settings window for 3D Plot Group, type Ray Diagram 3 in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Ray 2.
- 4 Click to expand the Window Settings section. Locate the Plot Settings section. From the View list, choose New view.
- **5** Locate the **Color Legend** section. Clear the **Show legends** check box.
- 6 In the Model Builder window, expand the Ray Diagram 3 node.

Color Expression 1

- I In the Model Builder window, expand the Results>Ray Diagram 3>Ray Trajectories I node, then click Color Expression I.
- 2 In the Settings window for Color Expression, locate the Expression section.
- 3 In the Expression text field, type at (0, im1 (qx, qy)). This will color each ray according to the value of the imported bitmap at location it was released.
- 4 Locate the Coloring and Style section. Click Change Color Table.
- 5 In the Color Table dialog box, select Thermal>Thermal in the tree.
- 6 Click OK.

Filter 1

- I In the Model Builder window, right-click Ray Trajectories I and choose Filter.
- 2 In the Settings window for Filter, locate the Ray Selection section.
- 3 From the Rays to render list, choose Number.
- 4 In the Number of rays text field, type 500. This will limit the number of rays that are rendered.

Selection 1

- I In the Model Builder window, expand the Results>Ray Diagram 3>Surface I node, then click Selection 1.
- 2 In the Settings window for Selection, locate the Selection section.
- **3** From the **Selection** list, choose **Lens Exteriors**.

Object

- I In the Model Builder window, right-click Ray Diagram 3 and choose Surface.
- 2 In the Settings window for Surface, type Object in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Object Surface.
- 4 Locate the Expression section. In the Expression text field, type im1(x,y). This will show the imported bitmap on the object plane.
- 5 Locate the Coloring and Style section. Click | Change Color Table.
- 6 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, click to expand the Quality section.
- **9** From the **Resolution** list, choose **No refinement**.
- **10** From the **Smoothing** list, choose **None**.

Transparency I

Right-click **Object** and choose **Transparency**.

Image

- I In the Model Builder window, right-click Ray Diagram 3 and choose Surface.
- 2 In the Settings window for Surface, type Image in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Image Surface.
- **4** Locate the **Expression** section. In the **Expression** text field, type gop.wall3.bacc1.Inum. This is the value of the accumulated image.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Quality section.
- **9** From the Resolution list, choose No refinement.
- **10** From the **Smoothing** list, choose **None**.

Transparency I

- I Right-click Image and choose Transparency.
- 2 In the Ray Diagram 3 toolbar, click Plot.
- 3 Click the Show Grid button in the Graphics toolbar.
- 4 Click the Orthographic Projection button in the Graphics toolbar. Compare the result to Figure 7.

Next, create a 2D Plot showing the accumulated image together with the imported bitmap.

Object and Image

- I In the Home toolbar, click Add Plot Group and choose 2D Plot Group.
- 2 In the Settings window for 2D Plot Group, type Object and Image in the Label text field.
- **3** Locate the **Plot Settings** section. Clear the **Plot dataset edges** check box.

Object

- I Right-click Object and Image and choose Surface.
- 2 In the Settings window for Surface, type Object in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Image Surface. Note that this is actually the Image surface dataset.
- 4 Locate the Expression section. In the Expression text field, type im1 (mag*x, mag*y). This scales and flips the object to match the image.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Coloring and Style section.
- **9** Clear the **Color legend** check box.
- 10 Click to expand the Quality section. From the Resolution list, choose No refinement.
- II From the **Smoothing** list, choose **None**.

Deformation I

- I Right-click **Object** and choose **Deformation**.
- 2 In the Settings window for Deformation, locate the Expression section.
- 3 In the x-component text field, type -50[mm].
- **4** Locate the **Scale** section. Select the **Scale factor** check box.

Image

- I In the Model Builder window, right-click Object and Image and choose Surface.
- 2 In the Settings window for Surface, type Image in the Label text field.
- 3 Locate the Data section. From the Dataset list, choose Image Surface.
- **4** Locate the **Expression** section. In the **Expression** text field, type gop.wall3.bacc1.Inum.
- 5 Locate the Coloring and Style section. Click Change Color Table.
- 6 In the Color Table dialog box, select Linear>GrayScale in the tree.
- 7 Click OK.
- 8 In the Settings window for Surface, locate the Quality section.
- **9** From the **Resolution** list, choose **No refinement**.
- **10** From the **Smoothing** list, choose **None**.
- II In the Object and Image toolbar, click **Plot**.
- 12 Click the Zoom Extents button in the Graphics toolbar. Compare to Figure 8.