



Drug Delivery System

Introduction

This example describes the operation of a drug delivery system that supplies a variable concentration of a water soluble drug. A droplet with a fixed volume of water travels down a capillary tube at a constant velocity. Part of the capillary wall consists of a permeable membrane separating the interior of the capillary from a concentrated solution of the drug. As the drop passes by the membrane, the drug dissolves into the water. To model this process, a constant flux of the drug is assumed on the capillary wall for the duration of its contact with the membrane. By altering the droplet velocity, the final concentration of the drug in the drop can be adjusted. The principle of the device is illustrated in [Figure 1](#).

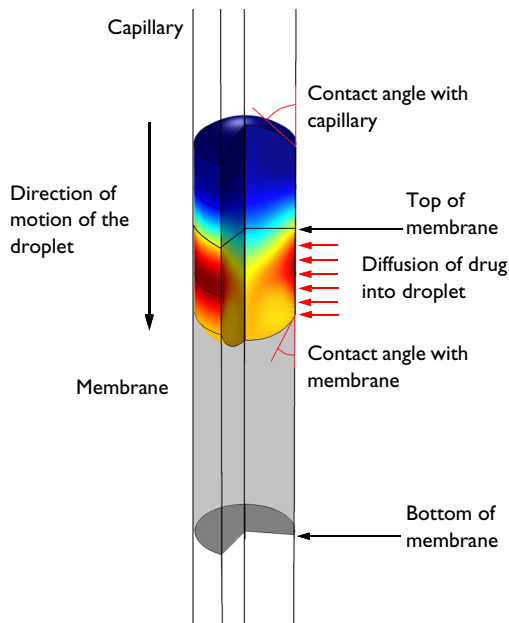


Figure 1: Diagram showing the operating principle of the drug delivery device. The color in the droplet represents drug concentration, with red indicating a higher concentration and blue indicating zero concentration. Note that the membrane length is not shown to scale.

Model Definition

The axisymmetric model geometry is shown in [Figure 2](#). The droplet is visible near the top of the geometry. The horizontal lines across the capillary are included to assist with meshing. The drop is initially stationary at the top of the domain, but accelerates rapidly

to a constant velocity before it reaches the permeable membrane. The permeable part of the capillary is not visible as part of the geometry as it is represented by a function applied to the boundary condition. It is located between $z = 0.6$ mm and $z = 0.8$ mm.

The droplet consists of liquid water of density 1000 kg/m^3 and viscosity $10^{-3} \text{ Pa}\cdot\text{s}$. The remainder of the capillary is filled with air, with a density of 1.25 kg/m^3 and a viscosity of $2 \times 10^{-5} \text{ Pa}\cdot\text{s}$. The water air surface tension coefficient is 70 mN/m . The contact angle of the droplet with the capillary wall is 135° , whilst that with the membrane is 157.5° . As the droplet passes the membrane the flux of the drug entering it is $1 \times 10^{-3} \text{ mol/(m}^2\cdot\text{s)}$. The diffusion coefficient of the drug in the water is $5 \times 10^{-9} \text{ m}^2/\text{s}$.

The droplet velocity past the membrane is varied between 0.1 and 1 mm/s to adjust the final concentration of the drug in the droplet.

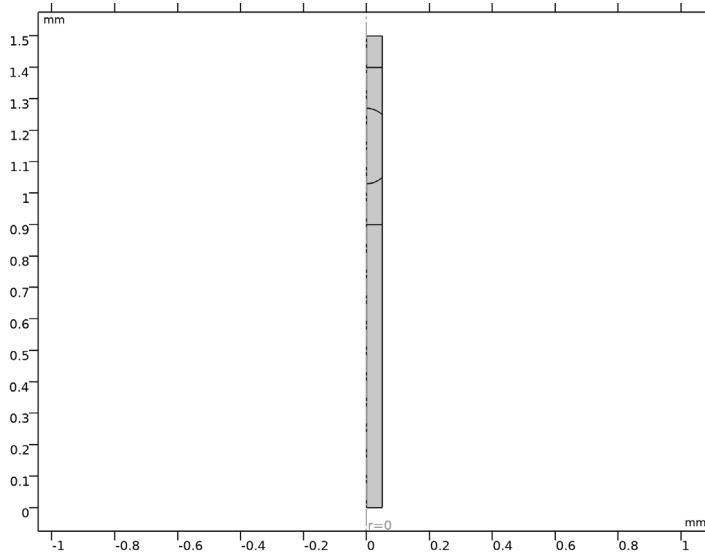


Figure 2: Axisymmetric model geometry.

Results and Discussion

The flow velocity is shown for the drop moving at 0.25 mm/s in [Figure 3](#). The flow pattern around the interface is complex as the flow must redistribute itself from a Poiseuille flow profile away from the droplet surface to a constant velocity flow at the surface of the droplet. Notice that the change in contact angle as the droplet passes the edge of the membrane at $z = 8 \text{ mm}$ is apparent.

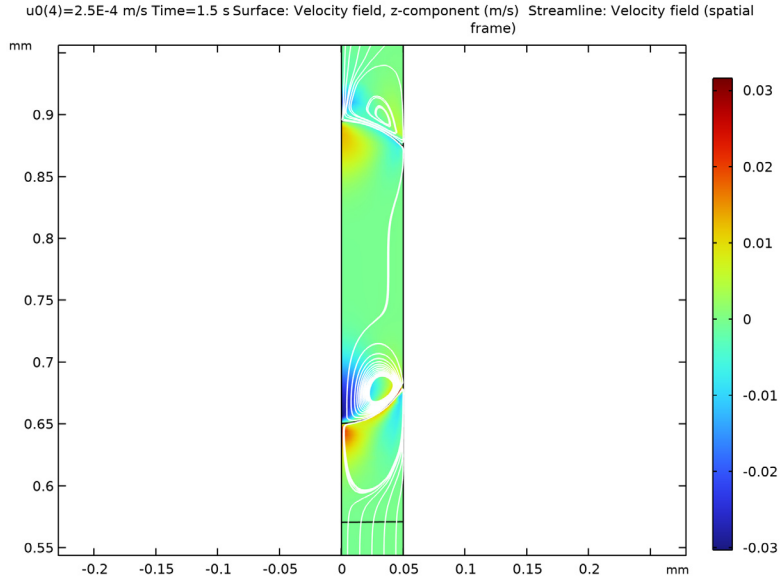


Figure 3: Flow velocity around the droplet as it travels past the edge of the permeable membrane. The droplet velocity is 0.25 mm/s.

Figure 4 shows the concentration profile for the 0.25 mm/s at the same point in time. The drug is diffusing into the droplet and is also convected by the fluid flow. A marked change in concentration is apparent between the top and the bottom of the droplet.

The total amount of drug in the droplet as a function of time is shown in Figure 5, for the drop traveling at 0.1 mm/s. The dissolved drug quantity increases with an ‘S’ shaped profile as the drug travels down the capillary.

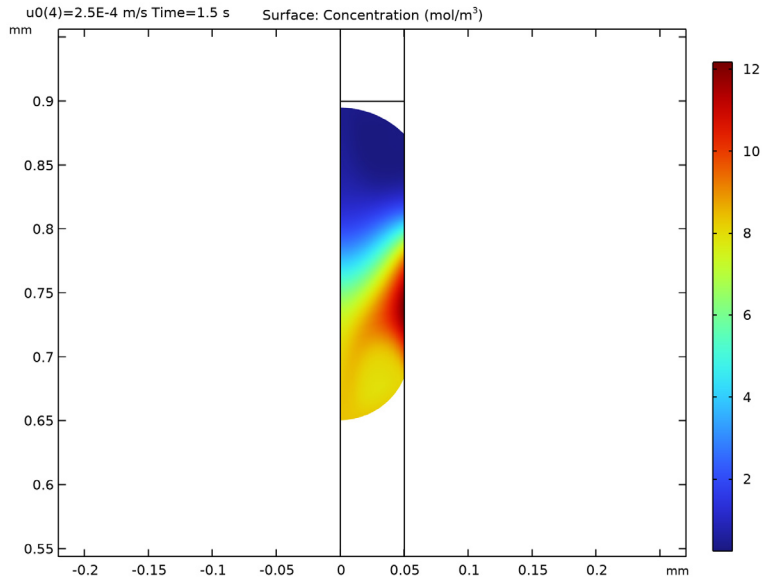


Figure 4: Drug concentration in the droplet as it travels past the edge of the permeable membrane. The droplet velocity is 0.25 mm/s.

Figure 6 shows the total amount of drug delivered against the droplet velocity. The number of moles delivered is approximately inversely proportional to the droplet velocity, which is expected as the amount of drug that diffuses into the drop depends on the time the drop takes to traverse the permeable part of the capillary.

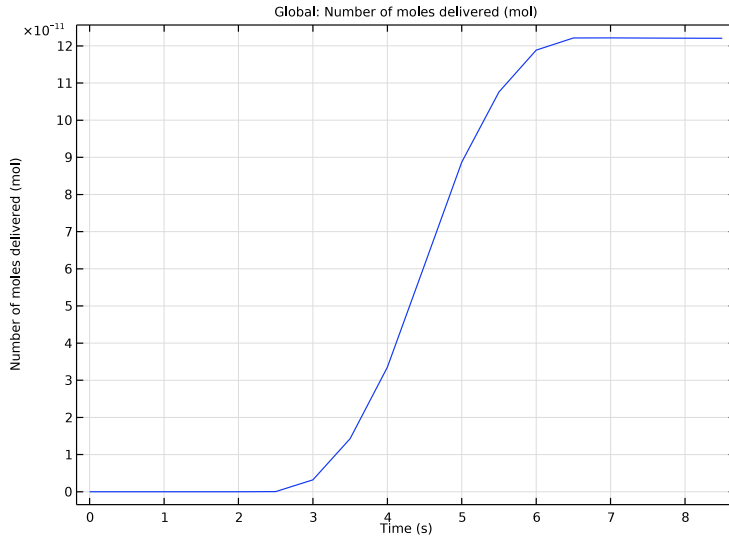


Figure 5: Total drug dose contained in the droplet as a function of time for the droplet traveling at 0.1 mm/s.

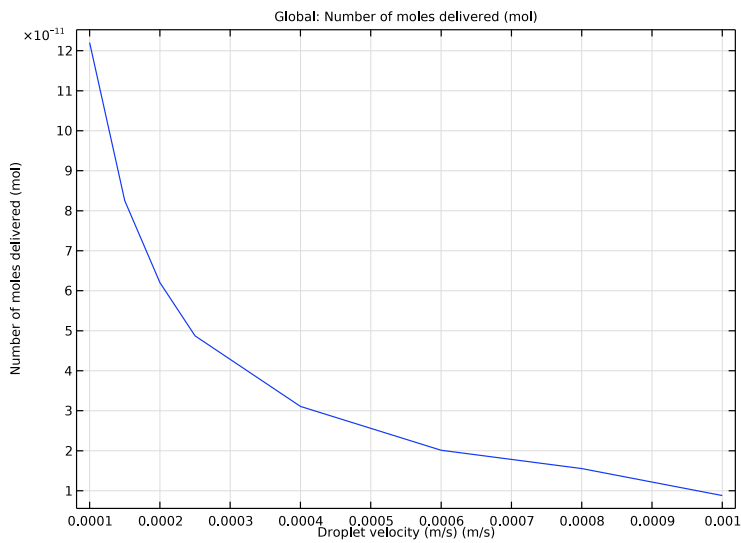



Figure 6: Total drug dose delivered shown against the droplet velocity.

Application Library path: Microfluidics_Module/Two-Phase_Flow/
drug_delivery_mm




Modeling Instructions

From the **File** menu, choose **New**.

NEW


In the **New** window, click  **Model Wizard**.

MODEL WIZARD

- 1 In the **Model Wizard** window, click  **2D Axisymmetric**.
- 2 In the **Select Physics** tree, select **Fluid Flow>Multiphase Flow>Two-Phase Flow, Moving Mesh>Laminar Two-Phase Flow, Moving Mesh**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Time Dependent**.
- 6 Click  **Done**.

GEOMETRY I

For convenience, the device geometry is inserted from an existing file. You can read the instructions for creating the geometry in the [Appendix — Geometry Instructions](#).

- 1 In the **Geometry** toolbar, click **Insert Sequence** and choose **Insert Sequence**.
- 2 Browse to the model's Application Libraries folder and double-click the file `drug_delivery_mm_geom_sequence.mph`.
- 3 In the **Geometry** toolbar, click  **Build All**.

GLOBAL DEFINITIONS

Set up a parameter for the droplet velocity.

Parameters I

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters I**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.


3 In the table, enter the following settings:

| Name | Expression | Value | Description |
|------|------------|-----------|------------------------|
| u0 | 0.001[m/s] | 0.001 m/s | Droplet velocity (m/s) |


Set up integration coupling variables to compute volume and point integrals.

DEFINITIONS

Integration 1 (intop1)


- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Integration**.
- 2 Select Domain 3 only.
- 3 In the **Settings** window for **Integration**, locate the **Advanced** section.
- 4 Clear the **Compute integral in revolved geometry** check box.

Integration 2 (intop2)

- 1 In the **Definitions** toolbar, click  **Nonlocal Couplings** and choose **Integration**.
- 2 In the **Settings** window for **Integration**, locate the **Source Selection** section.
- 3 From the **Geometric entity level** list, choose **Point**.
- 4 Select Point 4 only.
- 5 Locate the **Advanced** section. Clear the **Compute integral in revolved geometry** check box.

Set up model variables to track drug dose and drop location. Define a function to represent the permeable part of the capillary wall.



Variables 1

- 1 In the **Definitions** toolbar, click  **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 In the table, enter the following settings:

| Name | Expression | Unit | Description |
|-------|------------------|------|----------------------------|
| n_abs | intop1(2*pi*r*c) | | Number of moles delivered |
| z_pnt | intop2(z) | m | Position of top of droplet |



Create a rectangle function that is zero everywhere except at heights corresponding to the permeable membrane.

Rectangle 1 (rect1)

- 1 In the **Definitions** toolbar, click  **More Functions** and choose **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Parameters** section.
- 3 In the **Lower limit** text field, type $6e-4$.
- 4 In the **Upper limit** text field, type $8e-4$.
- 5 Click to expand the **Smoothing** section. In the **Size of transition zone** text field, type $5e-5$.
- 6 Click  **Plot**.

Create a step function to ramp up the velocity from zero in the **Inlet** boundary condition.


Step 1 (step1)

- 1 In the **Definitions** toolbar, click  **More Functions** and choose **Step**.
- 2 In the **Settings** window for **Step**, locate the **Parameters** section.
- 3 In the **Location** text field, type $1e-4$.
- 4 Click to expand the **Smoothing** section. In the **Size of transition zone** text field, type $1e-4$.
- 5 Click  **Plot**.

Set constraints on the mesh displacement.

MOVING MESH

Symmetry/Roller 1

- 1 In the **Moving Mesh** toolbar, click  **Symmetry/Roller**.
- 2 Select Boundaries 1, 3, 5–7, and 10–14 only (lateral boundaries).

The **Navier Slip** boundary condition must be used on the walls along which the contact line moves.

LAMINAR FLOW (SPF)


Wall 2

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Laminar Flow (spf)** and choose **Wall**.
- 2 Select Boundaries 10–14 only.
- 3 In the **Settings** window for **Wall**, locate the **Boundary Condition** section.


- 4 From the **Wall condition** list, choose **Navier slip**.

Set the inlet boundary condition to accelerate the droplet rapidly to a constant velocity.


Inlet 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Inlet**.
- 2 Select Boundary 9 only.
- 3 In the **Settings** window for **Inlet**, locate the **Boundary Condition** section.
- 4 From the list, choose **Fully developed flow**.
- 5 Locate the **Fully Developed Flow** section. In the U_{av} text field, type $u0*step1(t/1[s])$.
Apply a **Pressure** constraint at the **Outlet**.

Outlet 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Outlet**.
- 2 Select Boundary 2 only.
Set up the boundary conditions for the droplet surface and the contact point.

Fluid-Fluid Interface 1


- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Fluid-Fluid Interface**.
- 2 Select Boundaries 15 and 16 only.
- 3 In the **Settings** window for **Fluid-Fluid Interface**, locate the **Surface Tension** section.
- 4 From the **Surface tension coefficient** list, choose **User defined**. Locate the **Normal Direction** section. Select the **Reverse normal direction** check box.

Contact Angle 1

- 1 In the **Model Builder** window, expand the **Fluid-Fluid Interface 1** node, then click **Contact Angle 1**.
- 2 In the **Settings** window for **Contact Angle**, locate the **Contact Angle** section.
- 3 In the θ_w text field, type $3*pi*(1-rect1(z/1[m]))/4+7*pi*rect1(z/1[m])/8$.
Note: using the rectangle function in this manner makes the contact angle vary on the permeable part of the wall.
- 4 Locate the **Normal Wall Velocity** section. Select the **Constrain wall-normal velocity** check box.
Add the **Diluted Species** interface to model the solute transport in the droplet.


ADD PHYSICS

- 1 In the **Physics** toolbar, click  **Add Physics** to open the **Add Physics** window.

- 2 Go to the **Add Physics** window.
- 3 In the tree, select **Chemical Species Transport>Transport of Diluted Species (tds)**.
- 4 Click **Add to Component 1** in the window toolbar.
- 5 In the **Physics** toolbar, click  **Add Physics** to close the **Add Physics** window.

TRANSPORT OF DILUTED SPECIES (TDS)


Ensure the drug transport occurs only in the liquid domain.

- 1 In the **Settings** window for **Transport of Diluted Species**, locate the **Domain Selection** section.
- 2 Click  **Clear Selection**.
- 3 Select Domain 3 only.
Set up convection and diffusion for the drug.

Transport Properties 1

- 1 In the **Model Builder** window, under **Component 1 (comp1)>Transport of Diluted Species (tds)** click **Transport Properties 1**.
- 2 In the **Settings** window for **Transport Properties**, locate the **Convection** section.
- 3 From the **u** list, choose **Velocity field (spf)**.
- 4 Locate the **Diffusion** section. In the D_c text field, type 5E-9.
Add a boundary condition for the drug flux into droplet.

Flux 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Flux**.
- 2 Select Boundary 12 only.
- 3 In the **Settings** window for **Flux**, locate the **Inward Flux** section.
- 4 Select the **Species c** check box.
- 5 In the $J_{0,c}$ text field, type $\text{rect1}(z/1[\text{m}]) * 0.001[\text{mol}/(\text{m}^2 * \text{s})]$.

Note: this expression ensures flux only enters the droplet as it passes the permeable membrane.

Add the water and air material properties to the model.

MATERIALS

Material 1 (mat1)

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.

- 2 In the **Settings** window for **Material**, locate the **Material Contents** section.
- 3 In the table, enter the following settings:

| Property | Variable | Value | Unit | Property group |
|-------------------|----------|--------|-------------------|----------------|
| Density | rho | 1 . 25 | kg/m ³ | Basic |
| Dynamic viscosity | mu | 2e - 5 | Pa·s | Basic |

- 4 Select Domains 1, 2, 4, and 5 only.

Material 2 (mat2)


- 1 Right-click **Materials** and choose **Blank Material**.
- 2 Select Domain 3 only.
- 3 In the **Settings** window for **Material**, locate the **Material Contents** section.
- 4 In the table, enter the following settings:

| Property | Variable | Value | Unit | Property group |
|-------------------|----------|--------|-------------------|----------------|
| Density | rho | 1000 | kg/m ³ | Basic |
| Dynamic viscosity | mu | 1e - 3 | Pa·s | Basic |


Mesh the geometry. The mesh is refined around the edges of the droplet.

MESH 1

Scale 1


- 1 In the **Mesh** toolbar, click  **More Attributes** and choose **Scale**.
- 2 In the **Settings** window for **Scale**, locate the **Geometric Entity Selection** section.
- 3 From the **Geometric entity level** list, choose **Boundary**.
- 4 Select Boundaries 12, 15, and 16 only.
- 5 Locate the **Scale** section. In the **Element size scale** text field, type 0.5.

Free Quad 1

- In the **Mesh** toolbar, click  **Free Quad**.



Size

- 1 In the **Model Builder** window, click **Size**.
- 2 In the **Settings** window for **Size**, locate the **Element Size** section.
- 3 Click the **Custom** button.

- 4 Locate the **Element Size Parameters** section. In the **Maximum element size** text field, type 0.01.
- 5 In the **Minimum element size** text field, type 3E-5.
- 6 In the **Maximum element growth rate** text field, type 1.1.
- 7 In the **Curvature factor** text field, type 0.2.
- 8 Click  **Build All**.
Set up the parametric sweep.

STUDY I

Parametric Sweep

- 1 In the **Study** toolbar, click  **Parametric Sweep**.
- 2 In the **Settings** window for **Parametric Sweep**, locate the **Study Settings** section.
- 3 Click  **Add**.
- 4 In the table, enter the following settings:


| Parameter name | Parameter value list | Parameter unit |
|-----------------------------|--|----------------|
| u0 (Droplet velocity (m/s)) | 0.0001 0.00015 0.0002 0.00025 0.0004 0.0006 0.0008 0.001 | m/s |

Step 1: Time Dependent

- 1 In the **Model Builder** window, click **Step 1: Time Dependent**.
- 2 In the **Settings** window for **Time Dependent**, locate the **Study Settings** section.
- 3 In the **Output times** text field, type range(0,0.5,10).

Use a strict time step to avoid interpolation of the concentration field at output times, and add a stop condition to prevent the droplet from leaving the geometry.


Solution I (sol1)

- 1 In the **Study** toolbar, click  **Show Default Solver**.
- 2 In the **Model Builder** window, expand the **Solution I (sol1)** node, then click **Time-Dependent Solver I**.
- 3 In the **Settings** window for **Time-Dependent Solver**, click to expand the **Time Stepping** section.
- 4 From the **Steps taken by solver** list, choose **Strict**.
- 5 Right-click **Study I>Solver Configurations>Solution I (sol1)>Time-Dependent Solver I** and choose **Stop Condition**.

6 In the **Settings** window for **Stop Condition**, locate the **Stop Expressions** section.

7 Click  **Add**.

8 In the table, enter the following settings:

| Stop expression | Stop if | Active | Description |
|--------------------|------------|---|-------------------|
| comp1.z_pnt<0.0004 | True (>=1) |  | Stop expression 1 |

Note that the solver will stop when the real part of the stop expression is negative.

Adjust solver settings for optimum performance.

9 In the **Model Builder** window, under **Study 1>Solver Configurations>Solution 1 (sol1)** click **Time-Dependent Solver 1**.

10 In the **Settings** window for **Time-Dependent Solver**, click to expand the **Absolute Tolerance** section.

11 From the **Global method** list, choose **Unscaled**.

12 Click to expand the **Output** section. Clear the **Store time derivatives** check box.

13 In the **Study** toolbar, click  **Compute**.

RESULTS

Velocity (spf)

1 In the **Model Builder** window, expand the **Results>Velocity (spf)** node, then click **Velocity (spf)**.

2 In the **Settings** window for **2D Plot Group**, locate the **Data** section.

3 From the **Parameter value (u0 (m/s))** list, choose **2.5E-4**.

4 From the **Time (s)** list, choose **1.5**.

Streamline 1

1 Right-click **Velocity (spf)** and choose **Streamline**.

2 In the **Settings** window for **Streamline**, locate the **Streamline Positioning** section.

3 In the **Number** text field, type 10.





4 Select Boundaries 2 and 9 only.

5 Locate the **Coloring and Style** section. Find the **Point style** subsection. From the **Color** list, choose **White**.

Surface

1 In the **Model Builder** window, click **Surface**.

2 In the **Settings** window for **Surface**, locate the **Expression** section.


- 3 In the **Expression** text field, type **w**.
- 4 Click the  **Zoom Extents** button in the **Graphics** toolbar.
- 5 Click the  **Zoom In** button in the **Graphics** toolbar.
- 6 Click the  **Zoom In** button in the **Graphics** toolbar.
- 7 In the **Velocity (spf)** toolbar, click  **Plot**.

Compare the resulting plot with that in [Figure 2](#).

Streamline 1


- 1 In the **Model Builder** window, expand the **Results>Concentration (tds)** node.
- 2 Right-click **Streamline 1** and choose **Disable**.

Concentration (tds)

- 1 In the **Model Builder** window, click **Concentration (tds)**.
- 2 In the **Settings** window for **2D Plot Group**, locate the **Data** section.
- 3 From the **Parameter value (u0 (m/s))** list, choose **2.5E-4**.
- 4 From the **Time (s)** list, choose **1.5**.
- 5 In the **Concentration (tds)** toolbar, click  **Plot**.

Compare the resulting plot with that in [Figure 3](#).

ID Plot Group 7


- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.
- 2 In the **Settings** window for **ID Plot Group**, locate the **Data** section.
- 3 From the **Dataset** list, choose **Study 1/Parametric Solutions 1 (sol2)**.
- 4 From the **Parameter selection (u0)** list, choose **First**.

Global 1


- 1 Right-click **ID Plot Group 7** and choose **Global**.
- 2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
- 3 In the table, enter the following settings:

| Expression | Unit | Description |
|------------|------|---------------------------|
| n_abs | mol | Number of moles delivered |

- 4 Locate the **x-Axis Data** section. From the **Axis source data** list, choose **Inner solutions**.
- 5 Click to expand the **Legends** section. Clear the **Show legends** check box.

- 6 In the **ID Plot Group 7** toolbar, click  **Plot**.
Compare the resulting plot with that in [Figure 4](#).


ID Plot Group 8

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **ID Plot Group**.
2 In the **Settings** window for **ID Plot Group**, locate the **Data** section.
3 From the **Dataset** list, choose **Study 1/Parametric Solutions 1 (sol2)**.
4 From the **Time selection** list, choose **Last**.

Global 1

- 1 Right-click **ID Plot Group 8** and choose **Global**.
2 In the **Settings** window for **Global**, locate the **y-Axis Data** section.
3 In the table, enter the following settings:


| Expression | Unit | Description |
|------------|------|---------------------------|
| n_abs | mol | Number of moles delivered |

- 4 Locate the **x-Axis Data** section. From the **Axis source data** list, choose **Outer solutions**.
5 From the **Parameter** list, choose **Expression**.
6 In the **Expression** text field, type **u0**.
7 Locate the **Legends** section. Clear the **Show legends** check box.
8 In the **ID Plot Group 8** toolbar, click  **Plot**.
Compare the resulting plot with that in [Figure 5](#).

Appendix — Geometry Instructions

From the **File** menu, choose **New**.

NEW

In the **New** window, click  **Blank Model**.


ADD COMPONENT

In the **Home** toolbar, click  **Add Component** and choose **2D**.

GEOMETRY 1


- 1 In the **Settings** window for **Geometry**, locate the **Units** section.
2 From the **Length unit** list, choose **mm**.

Rectangle 1 (r1)



- 1 In the **Geometry** toolbar, click  **Rectangle**.
- 2 In the **Settings** window for **Rectangle**, locate the **Size and Shape** section.
- 3 In the **Width** text field, type 0.05.
- 4 In the **Height** text field, type 1.5.
- 5 Click to expand the **Layers** section. In the table, enter the following settings:

| Layer name | Thickness (mm) |
|------------|----------------|
| Layer 1 | 0.9 |
| Layer 2 | 0.5 |

Ellipse 1 (e1)

- 1 In the **Geometry** toolbar, click  **Ellipse**.
- 2 In the **Settings** window for **Ellipse**, locate the **Size and Shape** section.
- 3 In the **a-semiaxis** text field, type 0.09.
- 4 In the **b-semiaxis** text field, type 0.12.
- 5 Locate the **Position** section. In the **y** text field, type 1.15.
- 6 Locate the **Object Type** section. From the **Type** list, choose **Curve**.

Partition Objects 1 (par1)

- 1 In the **Geometry** toolbar, click  **Booleans and Partitions** and choose **Partition Objects**.
- 2 Select the object **r1** only.
- 3 In the **Settings** window for **Partition Objects**, locate the **Partition Objects** section.
- 4 Click to select the  **Activate Selection** toggle button for **Tool objects**.
- 5 Select the object **e1** only.

Form Union (fin)

- In the **Geometry** toolbar, click  **Build All**.

