



# Balanced Patch Antenna for 6 GHz

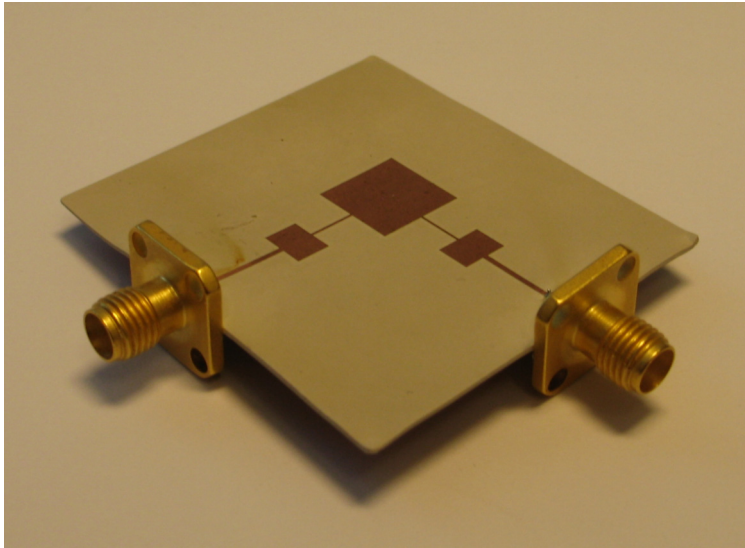
## *Introduction*

---

Patch antennas are becoming more common in wireless equipment, like wireless LAN access points, cellular phones, and GPS handheld devices. The antennas are small in size and can be manufactured with simple and cost-effective techniques. Due to the complicated relationship between the geometry of the antenna and the electromagnetic fields, it is difficult to estimate the properties of a certain antenna shape. At the early stages of antenna design, engineers can benefit a lot from using computer simulations. The changes in the shape of the patch are directly related to the changes in radiation pattern, antenna efficiency, and antenna impedance.

Balanced antennas are fed using two inputs, resulting in less disturbances on the total system through the ground. Balanced systems also provide a degree of freedom to alter antenna properties, by adjusting the phase and magnitude of the two input signals.

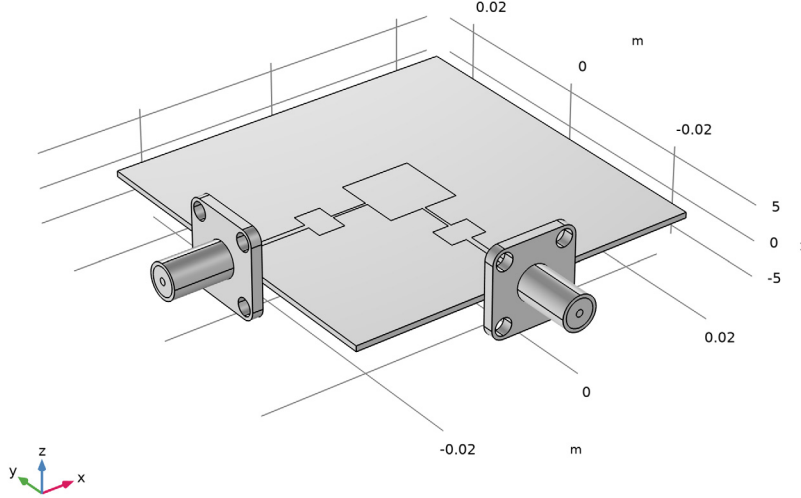
[Figure 1](#) shows the antenna that this example simulates.



*Figure 1: A photo of the real antenna that the model extracts the properties for.*

## Model Definition

The patch antenna is fabricated on a printed circuit board (PCB) with a relative dielectric constant of 5.23 (Ref. 1). The entire backside is covered with copper, and the front side has a pattern as shown in Figure 2 below.



*Figure 2: The patch antenna geometry is composed of a PCB board, two connectors, and a printed antenna pattern on top of the circuit board.*

The coaxial connectors have an outer conductor with an inner diameter of 4 mm and a center conductor with a diameter of 1 mm. The gap between the conductors is filled with a material with a dielectric constant of 2.07, giving a characteristic impedance close to 58  $\Omega$ . The signals into the connectors have the same magnitude but are shifted 180 degrees in phase. This results in a balanced feed.

The time-harmonic nature of the signals makes it possible to solve the vector-Helmholtz equation for the electric field everywhere in the geometry,

$$\nabla \times (\mu^{-1} \nabla \times \mathbf{E}) - k_0^2 \epsilon_r \mathbf{E} = 0$$

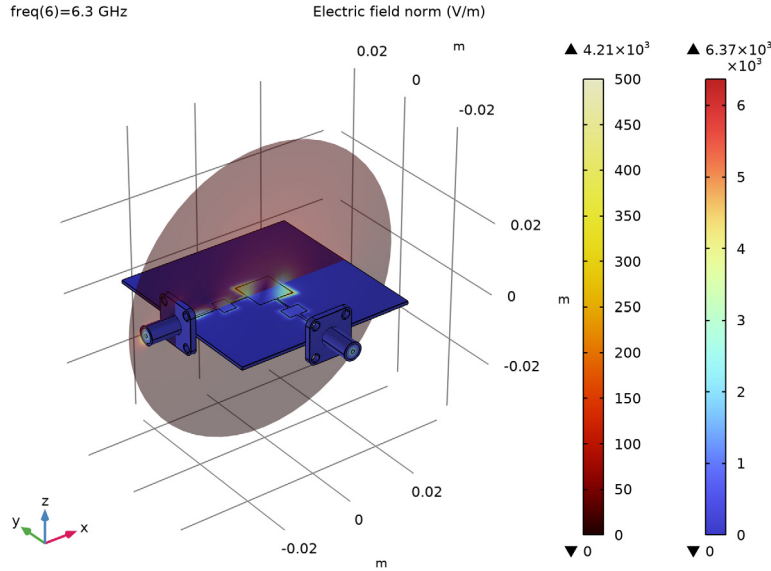
where  $k_0$  is the wave number for free space and is defined as

$$k_0 = \omega \sqrt{\epsilon_0 \mu_0}$$

All metallic objects are defined as perfect electric conductors. The antenna is placed in a spherical air domain surrounded by a Perfectly Matched Layer (PML) serving to absorb the radiation from the antenna with a minimum of reflection.

The model is run through a range of frequencies surrounding the operational frequency of 6.28 GHz.

## Results and Discussion



*Figure 3: The patch antenna with the electric field plotted both on its surface and on a slice through the air domain. The surrounding PML is hidden from view.*

Figure 3 shows the distribution of the electric field norm on the surface of the antenna and in the air, at 6.26 GHz. Most of the energy radiates out from the central patch.

The Lumped Port boundary condition, which is applied to the coaxial cables, is mimicking a connection to a transmission line feed with a characteristic impedance,  $Z_{\text{ref}}$ . The incident voltage wave from the transmission line has an amplitude equal to  $V_0$ , part of which is reflected directly at the port depending on how well  $Z_{\text{ref}}$  matches the characteristic impedance of the coaxial cable.

Under these circumstances and from each coaxial cable, the theoretical maximum power that can be produced in the antenna is achieved when the antenna impedance matches that of the coaxial cable. This power evaluates to

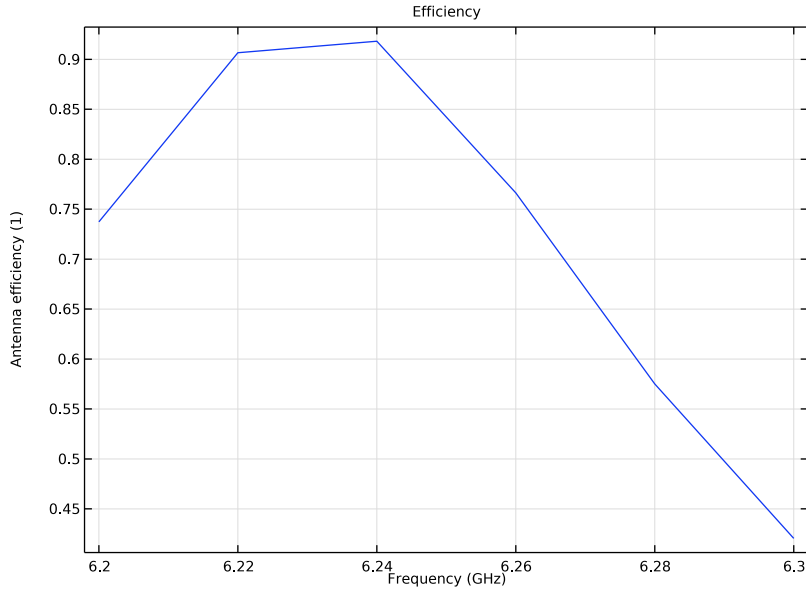
$$P_{\max} = \frac{V_0^2}{2Z_{\text{ref}}}$$

where  $V_0$  is the peak value of the time-harmonic applied voltage.

The antenna efficiency  $\eta$  is defined as the fraction of the theoretical max power that actually radiates out of the antenna:

$$\eta = \frac{P_1 + P_2}{2P_{\max}}$$

where  $P_1$  and  $P_2$  are the net power flow through ports 1 and 2 respectively. In [Figure 4](#) this efficiency is plotted against the frequency, showing that the optimum operating frequency is located at 6.24 GHz.



*Figure 4: The antenna efficiency as a function of the frequency.*

### *Notes About the COMSOL Implementation*

---

Possible model extensions include the addition of an external circuit or a far-field computation.

### *Reference*

---


1. E. Recht and S. Shiran, “A Simple Model for Characteristic Impedance of Wide Microstrip Lines for Flexible PCB,” *Proceedings of IEEE EMC Symposium 2000*, pp. 1010–1014, 2000.

### *Modeling Instructions*




---

From the **File** menu, choose **New**.

#### **NEW**

In the **New** window, click  **Model Wizard**.

#### **MODEL WIZARD**

- 1 In the **Model Wizard** window, click  **3D**.
- 2 In the **Select Physics** tree, select **Radio Frequency>Electromagnetic Waves, Frequency Domain (emw)**.
- 3 Click **Add**.
- 4 Click  **Study**.
- 5 In the **Select Study** tree, select **General Studies>Frequency Domain**.
- 6 Click  **Done**.

#### **STUDY I**

##### *Step 1: Frequency Domain*

Define the study frequency ahead of performing any frequency-dependent operation such as building mesh. The physics-controlled mesh uses the highest frequency value in the specified range.

- 1 In the **Model Builder** window, under **Study 1** click **Step 1: Frequency Domain**.
- 2 In the **Settings** window for **Frequency Domain**, locate the **Study Settings** section.
- 3 In the **Frequencies** text field, type range(6.2[GHz], 0.02[GHz], 6.3[GHz]).

## GLOBAL DEFINITIONS


### Parameters 1

- 1 In the **Model Builder** window, under **Global Definitions** click **Parameters 1**.
- 2 In the **Settings** window for **Parameters**, locate the **Parameters** section.
- 3 In the table, enter the following settings:

Name	Expression	Value	Description
V0	1[V]	1 V	Applied voltage
epsilon <sub>r</sub> _coax	2.07	2.07	Relative permittivity, coaxial cable
epsilon <sub>r</sub> _pcb	5.23	5.23	Relative permittivity, circuit board
a <sub>coax</sub>	0.5[mm]	5E-4 m	Inner coax conductor radius
b <sub>coax</sub>	2[mm]	0.002 m	Inner radius of outer coax conductor
Z <sub>coax</sub>	$\sqrt{\mu_0 \text{const} / (\epsilon_{\text{r\_coax}} \cdot \epsilon_0 \text{const})} / (2 \cdot \pi) \cdot \log(b_{\text{coax}} / a_{\text{coax}})$	57.772 Ω	Cable impedance
P <sub>max</sub>	$V_0^2 / (2 \cdot Z_{\text{coax}})$	0.0086546 W	Theoretical max power

## GEOMETRY 1


### Import 1 (impl)

- 1 In the **Home** toolbar, click  **Import**.
- 2 In the **Settings** window for **Import**, locate the **Import** section.
- 3 Click  **Browse**.
- 4 Browse to the model's Application Libraries folder and double-click the file patch\_antenna.mphbin.




- 5 Click  **Import**.

The imported geometry consists of the patch antenna and its connectors. Add two concentric spheres, one for the air surrounding the antenna and one for the PML.

#### *Sphere 1 (sph1)*


- 1 In the **Geometry** toolbar, click  **Sphere**.
- 2 In the **Settings** window for **Sphere**, locate the **Size** section.
- 3 In the **Radius** text field, type 0.06.
- 4 Click to expand the **Layers** section. In the table, enter the following settings:

Layer name	Thickness (m)
Layer 1	0.02



- 5 Click  **Build All Objects**.
- 6 Click the  **Wireframe Rendering** button in the **Graphics** toolbar.
- 7 Click the  **Zoom Extents** button in the **Graphics** toolbar.

### DEFINITIONS

#### *Perfectly Matched Layer 1 (pml1)*

- 1 In the **Definitions** toolbar, click  **Perfectly Matched Layer**.  
Activate the PML in the volume covered by the outer but not the inner sphere:
- 2 Select Domains 1–4 and 13–16 only.
- 3 In the **Settings** window for **Perfectly Matched Layer**, locate the **Geometry** section.
- 4 From the **Type** list, choose **Spherical**.


### ADD MATERIAL

- 1 In the **Home** toolbar, click  **Add Material** to open the **Add Material** window.
- 2 Go to the **Add Material** window.
- 3 In the tree, select **Built-in>Air**.
- 4 Click **Add to Component** in the window toolbar.
- 5 In the **Home** toolbar, click  **Add Material** to close the **Add Material** window.



MATERIALS

Coax Dielectric

- 1 In the **Model Builder** window, under **Component 1 (comp1)** right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type Coax Dielectric in the **Label** text field.
- 3 Locate the **Geometric Entity Selection** section. Click  **Clear Selection**.  
Select the cylinders between the inner and outer conductors of the coaxial cables:
- 4 Select Domains 7 and 11 only.
- 5 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilon_nr_iso ; epsilon_nr_ii = epsilon_nr_iso, epsilon_nr_ij = 0	epsilon_nr_coax	l	Basic
Relative permeability	mu_r_iso ; mu_r_ii = mu_r_iso, mu_r_ij = 0	1	l	Basic
Electrical conductivity	sigma_iso ; sigma_ii = sigma_iso, sigma_ij = 0	0	S/m	Basic

PCB



- 1 Right-click **Materials** and choose **Blank Material**.
- 2 In the **Settings** window for **Material**, type PCB in the **Label** text field.  
Select the PCB board:
- 3 Select Domain 9 only.

4 Locate the **Material Contents** section. In the table, enter the following settings:

Property	Variable	Value	Unit	Property group
Relative permittivity	epsilon <sub>nr_iso</sub> ; epsilon <sub>nr<sub>ii</sub></sub> = epsilon <sub>nr_iso</sub> , epsilon <sub>nr<sub>ij</sub></sub> = 0	epsilon <sub>nr_pcb</sub>	l	Basic
Relative permeability	mu <sub>r_iso</sub> ; mu <sub>r<sub>ii</sub></sub> = mu <sub>r_iso</sub> , mu <sub>r<sub>ij</sub></sub> = 0	1	l	Basic
Electrical conductivity	sigma <sub>iso</sub> ; sigma <sub>ii</sub> = sigma <sub>iso</sub> , sigma <sub>ij</sub> = 0	0	S/m	Basic

### ELECTROMAGNETIC WAVES, FREQUENCY DOMAIN (EMW)

By default, the Electromagnetic Waves equation is active in all domains. However, because you represent the metal in this model as perfectly conductive boundaries, there is no need to model the interior of the contacts. Therefore, remove the metal domains from the domains selection.

- 1 In the **Model Builder** window, under **Component 1 (comp1)** click **Electromagnetic Waves, Frequency Domain (emw)**.
- 2 In the **Settings** window for **Electromagnetic Waves, Frequency Domain**, locate the **Domain Selection** section.
- 3 Click  **Clear Selection**.
- 4 Click  **Paste Selection**.
- 5 In the **Paste Selection** dialog box, type 1-5, 7, 9, 11, 13-16 in the **Selection** text field.
- 6 Click **OK**.

#### Lumped Port 1

- 1 In the **Physics** toolbar, click  **Boundaries** and choose **Lumped Port**.

To define the first port, select the outer air/dielectric boundary on the cable facing the  $x$  direction:

- 2 Select Boundary 16 only.
- 3 In the **Settings** window for **Lumped Port**, locate the **Lumped Port Properties** section.

4 From the **Type of lumped port** list, choose **Coaxial**.

For the first port, wave excitation is **on** by default.

5 Locate the **Settings** section. In the  $V_0$  text field, type  $V_0$ .

6 In the  $Z_{ref}$  text field, type  $Z_{coax}$ .

#### *Lumped Port 2*

1 In the **Physics** toolbar, click  **Boundaries** and choose **Lumped Port**.

The second port is the outer air/dielectric boundary on the contact facing the  $y$  direction:

2 Select Boundary 96 only.

3 In the **Settings** window for **Lumped Port**, locate the **Lumped Port Properties** section.

4 From the **Type of lumped port** list, choose **Coaxial**.

5 From the **Wave excitation at this port** list, choose **On**.

6 Locate the **Settings** section. In the  $V_0$  text field, type  $V_0$ .

7 In the  $\theta_{in}$  text field, type  $\pi$ .

8 In the  $Z_{ref}$  text field, type  $Z_{coax}$ .

Although you have not yet specified any conducting boundaries, there is already a Perfect Electric Conductor condition in the model. By default, it applies to all boundaries that are exterior to the active domains. It then gets overridden by any other conditions that you are applying. If you click its node in the Model Builder, you can see that it still applies to the conductors.

#### *Perfect Electric Conductor 1*

The patch and the PCB ground plane are interior to the model domain (meaning they neighbor only to domains where the equation is active) and hence need to be explicitly assigned this same condition.

#### *Perfect Electric Conductor 2*

1 In the **Physics** toolbar, click  **Boundaries** and choose **Perfect Electric Conductor**.


Select the patch and the ground plane (bottom surface) of the PCB:

2 Select Boundaries 59 and 69 only.

The settings that you have made until now completely define the physics of your model. To enable postprocessing of the antenna efficiency, you need to add integral operators on the port boundaries.

## DEFINITIONS

### Variables 1

- 1 In the **Home** toolbar, click  **Variables** and choose **Local Variables**.
- 2 In the **Settings** window for **Variables**, locate the **Variables** section.
- 3 In the table, enter the following settings:


Name	Expression	Unit	Description
P1	$0.5 * \text{real}(\text{emw.Vport\_1} * \text{conj}(\text{emw.Iport\_1}))$	W	Power into Port 1
P2	$0.5 * \text{real}(\text{emw.Vport\_2} * \text{conj}(\text{emw.Iport\_2}))$	W	Power into Port 2
eff	$(P1 + P2) / (2 * P_{\text{max}})$		Antenna efficiency

The power that goes through each of the ports is computed from port voltage and current. The last variable defines the efficiency as the ratio of the input power and the theoretical maximum for each port.

## MESH 1

In the **Model Builder** window, under **Component 1 (comp1)** right-click **Mesh 1** and choose **Build All**.

## STUDY 1


In the **Home** toolbar, click  **Compute**.

## RESULTS

### Electric Field (emw)


The default plot shows a slice plot of the electric field norm at 6.3 GHz. It is dominated by the result near the antenna. Most of the remaining part of these model instructions will guide you toward an informative and nice-looking plot of the local electric field on and around the antenna. But first, take the following steps in order to plot the antenna efficiency versus the frequency.

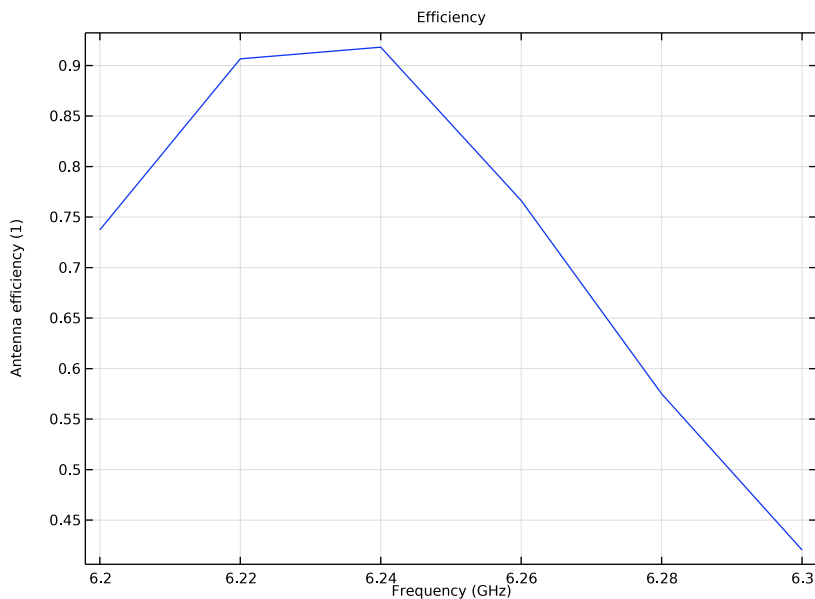
### 1D Plot Group 2

- 1 In the **Home** toolbar, click  **Add Plot Group** and choose **1D Plot Group**.
- 2 In the **Settings** window for **1D Plot Group**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Efficiency.

- 5 Locate the **Plot Settings** section.
- 6 Select the **x-axis label** check box. In the associated text field, type **Frequency (GHz)**.

#### *Global 1*

- 1 Right-click **ID Plot Group 2** and choose **Global**.
- 2 In the **Settings** window for **Global**, click **Replace Expression** in the upper-right corner of the **y-Axis Data** section. From the menu, choose **Component 1 (comp1)>Definitions>Variables>eff - Antenna efficiency - 1**.
- 3 Click to expand the **Legends** section. Clear the **Show legends** check box.
- 4 In the **ID Plot Group 2** toolbar, click  **Plot**.



The plot has sharp edges because you solved only for 6 frequencies. See [Figure 4](#) for a smoother version over a wider frequency range.

#### *Electric Field (emw)*


The plot group you just selected already contains a slice plot of the electric field norm.

#### *Multislice*

Delete the multislice plot and add a single slice.

- 1 In the **Model Builder** window, expand the **Electric Field (emw)** node.
- 2 Right-click **Multislice** and choose **Delete**.



### *Slice I*

- 1 In the **Model Builder** window, right-click **Electric Field (emw)** and choose **Slice**.
- 2 In the **Settings** window for **Slice**, locate the **Plane Data** section.
- 3 From the **Plane** list, choose **ZX-planes**.
- 4 In the **Planes** text field, type 1.
- 5 Click to expand the **Range** section. Select the **Manual color range** check box.
- 6 In the **Maximum** text field, type 500.
- 7 Locate the **Coloring and Style** section. Click  **Change Color Table**.
- 8 In the **Color Table** dialog box, select **Thermal>ThermalDark** in the tree.
- 9 Click **OK**.

### *Transparency I*

Right-click **Slice I** and choose **Transparency**.

### *Selection I*


- 1 In the **Model Builder** window, right-click **Slice I** and choose **Selection**.
- 2 In the **Settings** window for **Selection**, locate the **Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 5-12 in the **Selection** text field.
- 5 Click **OK**.
- 6 In the **Electric Field (emw)** toolbar, click  **Plot**.

You are now looking at a nicely scaled plot of the electric field norm on a slice of your geometry, excluding the PML where it does not have any physical relevance.

### *Surface I*

In the **Model Builder** window, right-click **Electric Field (emw)** and choose **Surface**.


### *Selection I*

- 1 In the **Model Builder** window, right-click **Surface I** and choose **Selection**.
- 2 In the **Settings** window for **Selection**, locate the **Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 13-106, 114-121, 131-144 in the **Selection** text field.
- 5 Click **OK**.

- 6 In the **Electric Field (emw)** toolbar, click  **Plot**.

The electric field norm now also shows up on the surface of the antenna. All exterior surfaces are hidden from view, but the edges defining the contour of the PML are still visible.

#### *Electric Field (emw)*



- 1 In the **Model Builder** window, under **Results** click **Electric Field (emw)**.
- 2 In the **Settings** window for **3D Plot Group**, locate the **Plot Settings** section.
- 3 Clear the **Plot dataset edges** check box.
- 4 In the **Electric Field (emw)** toolbar, click  **Plot**.

Now all edges are gone. This makes the contours of the PCB and the contacts less prominent. To retain a sharper-looking geometry, draw your selected edges in black with the help of a line plot.


#### *Line 1*


- 1 Right-click **Electric Field (emw)** and choose **Line**.
- 2 In the **Settings** window for **Line**, locate the **Expression** section.
- 3 In the **Expression** text field, type 1.
- 4 Locate the **Coloring and Style** section. From the **Coloring** list, choose **Uniform**.
- 5 From the **Color** list, choose **Black**.

#### *Selection 1*

- 1 Right-click **Line 1** and choose **Selection**.
- 2 In the **Settings** window for **Selection**, locate the **Selection** section.
- 3 Click  **Paste Selection**.
- 4 In the **Paste Selection** dialog box, type 10-235, 243-264, 278-335 in the **Selection** text field.
- 5 Click **OK**.
- 6 In the **Electric Field (emw)** toolbar, click  **Plot**.

#### *Electric Field (emw)*

- 1 In the **Model Builder** window, under **Results** click **Electric Field (emw)**.
- 2 In the **Settings** window for **3D Plot Group**, click to expand the **Title** section.
- 3 From the **Title type** list, choose **Manual**.
- 4 In the **Title** text area, type Electric field norm (V/m).
- 5 In the **Electric Field (emw)** toolbar, click  **Plot**.

- 6 Click the  **Go to Default View** button in the **Graphics** toolbar.  
Your plot should now look like that in [Figure 3](#).