Estimating General Election Support for President Using Multilevel Regression & Poststratification (MRP)

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Comments and Critiques Welcome

Morning Consult asked more than 44,000 registered voters nationally over the past three months who they would support in a series of hypothetical general election match ups. We used a statistical technique called multilevel regression and poststratification (MRP) to construct state-level estimates from the national survey data. The results suggest that Democrat Hillary Clinton currently has an advantage over Republicans Donald Trump and Ted Cruz. On the other hand, the estimates suggest that Ohio Governor John Kasich edges out Clinton, likely due to much higher favorability levels among registered voters than Trump or Cruz and advantages in his home state of Ohio. Many caveats are in store due to the length of time between now and November, the high proportion of adults who are undecided and close margins in key states such as Florida, but the results suggest the 2016 presidential election map will look similar to the 2012 map if Hillary Clinton and Donald Trump are their parties' respective nominees.

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Republican Donald Trump and Democrat Hillary Clinton hold large leads in delegate counts in their parties' respective presidential primary campaigns. In this white paper, we use about 45,000 interviews conducted nationally since January 2016, combined with a statistical methodology called multilevel regression and post-stratification (MRP), to provide state-level estimates of outcomes for the November 2016 presidential election.

We find that Hillary Clinton would win the presidency with 328 electoral votes to Donald Trump's 210 if the election were held today. In a prospective match up with Ted Cruz, Clinton would receive 332 electoral votes and the Texas Senator would receive 206 electoral votes. On the other hand, if the election were held today, John Kasich would receive 304 electoral votes to Hillary Clinton's 234, largely due to strong performances in the Midwest and Mid Atlantic. Many caveats in this analysis are in store due to the length of time between now and November, the high proportion of adults who are undecided and close margins in key states such as Florida, but the results suggest the 2016 presidential election map will look similar to the 2012 map if Hillary Clinton and Donald Trump are their parties' respective nominees.

The paper is organized as follows. First, we describe our research design and why we utilize multilevel regression and post-stratification. Next, we describe the unique data sources, both from national Morning Consult polling and Census data, that we use to construct these estimates. Third, we present and describe our main findings in prospective general election match-ups between Hillary Clinton and Donald Trump, along with potential match ups including Texas Senator Ted Cruz and Ohio Governor John Kasich. Subsequent sections describe alternative modeling specifications and how those approaches influence the overall results and conclusions. We conclude with implications and further caveats to this analysis.

¹Both Clinton and Trump, respectively, are leading their respective fields in betting markets such as PredictIt. As of April 8, 2016, Clinton has an 84% chance of winning the nomination and Trump has a 46% chance of winning the nomination.

Research Design and Data Sources

Since January 1, 2016, Morning Consult has interviewed more than 44,000 registered voters across the country using large online survey vendors and has asked each respondent who they would support in a series of hypothetical 2016 general election match ups.² The interviews were distributed relatively evenly across the three month period, with about 10,000 registered voters contacted in January, about 10,000 registered voters in February, about 20,000 registered voters in March and about 4,000 registered voters in the first week of April. Morning Consult will interview hundreds of thousands of additional voters between now and November 2016. The surveys included about 30 demographic questions, along with a series of questions on the presidential primary and general elections.³

We develop state-level estimates from our national survey data by utilizing a statistical technique known as multilevel regression and poststratification (MRP) (Gelman and Hill, 2006; Gelman, 2009; Ghitza and Gelman, 2013; Howe et al., 2015; Kastellec, Lax, and Phillips, 2010; Lax and Phillips, 2009; Leemann and Wasserfallen, 2014,?; Park, Gelman, and Bafumi, 2004; Warshaw and Rodden, 2012). MRP has been widely used in industry and in academia, and MRP estimates of state and Congressional District level public opinion have generally been shown to outperform national polling, especially when there are few respondents in smaller geographic areas (Warshaw and Rodden, 2012).

Responses to the general election vote choice question are modeled via multilevel regression as a function of both individual level and state-level variables. Our models

²When respondents enter the polls, we obtain location information that allows us to allocate them to their respective state, Congressional district or city.

 $^{^3}$ Voters were asked: If the 2016 presidential election were held today and the candidates were Democrat Hillary Clinton and Republican Donald Trump, for whom would you vote? The response options were Hillary Clinton, Donald Trump and Don't Know / No Opinion. The order of the first two response options was randomized, and similar questions were asked to test hypothetical match ups between Hillary Clinton and Ted Cruz, along with a hypothetical match up between Hillary Clinton and John Kasich

use age, gender, and education as individual level predictor variables.

Presidential election models typically utilize a combination of state-level economic data, current voter sentiment, and historical elections to make predictions (Fair, 1978). For our state-level variables, therefore, we chose variables that may influence state-level vote choice such as the percent change in state gross domestic product (GDP),⁴ state unemployment rates, state median household income, and state-level outcomes from 2012 Presidential election.⁵

Then, in the next step, we calculate a weighted sum of the individual demographic-geographic type for each state. Namely, we poststratify the predictions from our regression models on age, education and gender obtained from the 5-year estimates of the adult citizen population from the 2013 American Community Survey (ACS). These variables were chosen because we needed true values of the individual level variables and their interactions (e.g., males 50+ with a college degree, etc.), which are available in the ACS. Please see the appendix for more information on model specification.

Many MRP models convert survey questions into binary response choices such as 1s (e.g. support) and 0s (e.g., both oppose and don't know). Our main outcome variable has three response options (i.e., 1 - Vote for Clinton, 2 - Vote for Trump and 3 - Don't Know). For each response option, we create a binary variable and then fit a multi-level logistic regression. We obtain estimates for each response option and then normalize the estimates to sum to 1.

Standard errors for our estimates were calculated by taking 100 bootstrap samples with replacement from our full national dataset (n = 44,000+) for each hypothetical match up and then assessing this empirical distribution at the state level. The distribution of these predictions at the state level allows us to construct a predictive interval, which gives us a sense of the spread of MRP estimates. The 95% predictive intervals range

⁴This is calculated as the percent state-GDP growth from the first quarter of 2012 to the third quarter of 2015

 $^{^5}$ This is calculated as the percent of the overall vote Barack Obama received at the state level in November 2012

from two percentage points in larger states such as California, Florida, New York, Pennsylvania and Texas, to around four percentage points in smaller states such as Hawaii, Rhode Island or Wyoming. The size of the 95% predictive interval increases as the state sample size decreases, but is not completely determined by the size of the state sample in the draw for a number of reasons. First, the state-level grouping variables (e.g., median household income, 2012 Presidential election outcomes) have a strong influence on the overall size of the predictive interval and states with more homogeneous demographic characteristics may tend to have less variation than more heterogeneous states. If, all things equal, smaller states like Wyoming are more homogeneous than larger states such as California, then we would expect smaller predictive intervals in these smaller samples than their sample size alone would suggest.

General Election Results

Figure 1 shows that if the election were held today, we estimate that Hillary Clinton would win the presidency with 328 electoral votes to Donald Trump's 210. States where Clinton receives more support than Trump are shaded blue, whereas states where Trump receives more support than Clinton are shaded red.

Figure 2 shows that the estimated margins between the two candidates are less than four percentage points in Florida, Indiana, Maine, Michigan, Nevada, Ohio, and Pennsylvania. States such as Missouri and North Carolina appear to be safely in the Republican column, wheras states in the upper Midwest such as Iowa, Minnesota and Wisconsin appear to be leaning strongly toward the Democrats.

In the 2012 election, President Barack Obama received 332 electoral votes and former Massachusetts Governor Mitt Romney received 206 electoral votes. Figure 3 compares the Clinton vs. Trump estimates with results from the 2012 Presidential Election between Barack Obama and Mitt Romney. The two maps look remarkably similar.

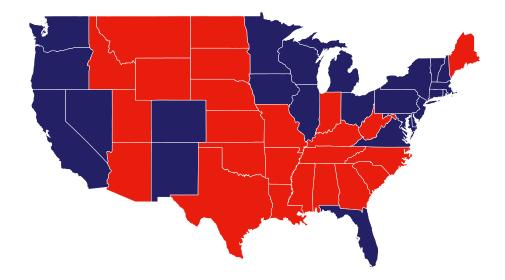


Figure 1: "If the 2016 presidential election were held today and the candidates were Democrat Hillary Clinton and Republican Donald Trump, for whom would you vote?" States where Clinton receives more support than Trump are shaded blue, whereas states where Trump receives more support than Clinton are shaded red.

Trump leads in one state, Maine, that Obama won in 2012. Importantly, Clinton is able to hold on to key swings states such as Colorado, Florida, and Ohio.

Results: Clinton vs. all GOP candidates

There is a chance that Trump will not become the Republican presidential nominee in the general election. Therefore, we also ran statistical models to assess Texas U.S. Senator Ted Cruz's and Ohio Governor John Kasich's viability against Hillary Clinton. Figure 4 shows how the potential match-ups would play out across the country if we vary the GOP nominee.

The strongest GOP nominee with the potential to beat Hillary Clinton come November is John Kasich, who wins 304 electoral votes to Clinton's 234. Kasich, a northern Republican, has the ability hold the Republican Party's Southern coalition, as well as make deep inroads into the Midwest by potentially winning Michigan, Minnesota, and

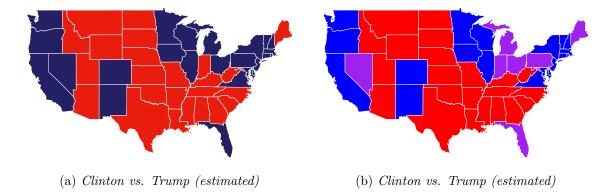


Figure 2: Electoral Maps of Clinton v. Trump and Clinton v. Trump battleground states. In the left frame, states are shaded blue if Clinton is leading and red if Trump is leading. In the right frame, states are shaded blue if Clinton is leading by at least four percentage points, states are shaded red if Trump is leading by at least four percentage points and states are shaded purple if the difference is less than four percentage points.

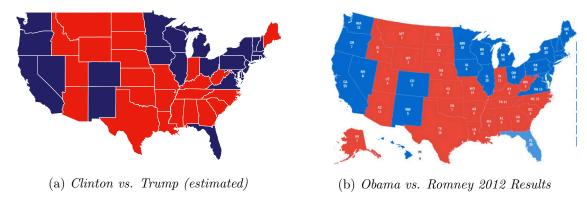


Figure 3: Electoral Maps of Clinton v. Trump compared with Obama v. Romney 2012 Results

Wisconsin. Kasich is almost guaranteed to win his home state of Ohio and has the strong potential pick up additional swing states such as Colorado, New Hampshire, and Pennsylvania.⁶

⁶The head-to-head match ups with Hillary Clinton and Donald Trump, along with Hillary Clinton and Ted Cruz, include data collected from early January 2016 through early April 2016, with a total of more than 44,000 responses. We did not start including a head-to-head match up with Hillary Clinton and John Kasich until polls starting February 15, 2016, so there are about 28,000 completed cases in this match up. If we estimate MRP models for Clinton vs. Trump or Clinton vs. Cruz using only data collected after February 15, the map does not change considerably. Clinton would receive 324 electoral votes instead of 326 in a Clinton vs Trump match up, and Clinton would receive 314 electoral votes instead of 332 in a Clinton vs Cruz match up.

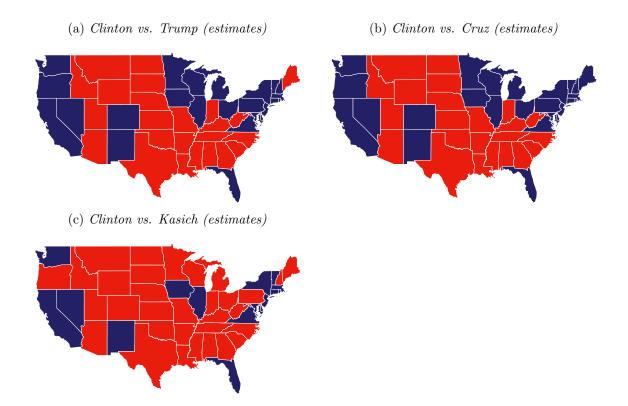


Figure 4: Electoral Maps of Hypothetical Match ups with Clinton vs. Trump, Clinton vs. Cruz, and Clinton vs. Kasich

In terms of electoral votes, Ted Cruz fares slightly worse than Donald Trump. Overall, Cruz garners 206 electoral votes to Clinton's 332.

Kasich may outperform Cruz and Trump because he has much higher favorability levels than the other Republican contenders. In a Morning Consult poll conducted among 2,004 registered voters nationally from April 1-3, 2016, 38% have a favorable view of Kasich, 34% have an unfavorable view of Kasich and 29% do not have a view either way. By contrast, more than 50% of registered voters have negative views of Ted Cruz and Donald Trump. Overall, 37% have a favorable opinion of Ted Cruz and 52% have an unfavorable opinion. Similarly, 37% have an unfavorable opinion of Donald Trump and 60% have an unfavorable opinion of Trump.

Importantly, Kasich's net favorability among Independents is +7 (37% favorable, 30% unfavorable), whereas Cruz's net favorability among Independents is -27% (29% fa-

vorable, 56% unfavorable) and Trump's net favorability is -24% (36% favorable, 60% unfavorable).

Clinton's advantage over Cruz and Trump, along with Kasich's edge over Clinton, is consistent with national results from Morning Consult in recent months. Figure 5 displays national head-to-head match ups in each Morning Consult poll conducted since mid-February 2016. In general, Hillary Clinton holds a small advantage over Donald Trump and at least as large of an advantage over Ted Cruz. However, the hypothetical match up between John Kasich and Hillary Clinton is considerably closer in polls conducted since early March.

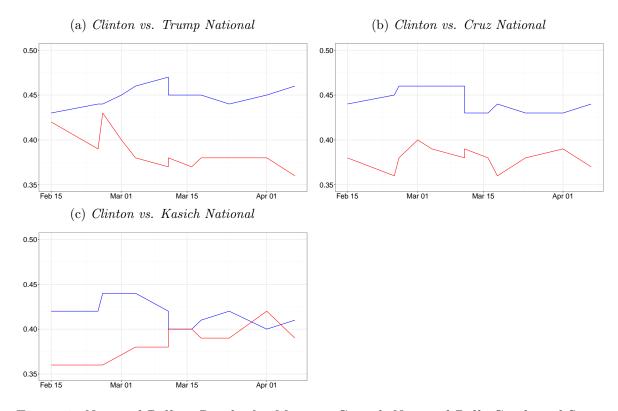


Figure 5: National Polling Results for Morning Consult National Polls Conducted Since Mid-February 2016

Alternative Specifications

In addition to creating state-by-state estimates using MRP, we used an alternative approach where we first allocated respondents to their respective state and then we post-stratified by applying state-based weights using population parameters from the 2012 Current Population Survey (CPS). This approach does not utilize the state-level grouping variables, and the estimates in this approach are more variable in states with smaller samples.

Figure 6 displays the comparison of MRP estimates (left side) with the state-based weights approach (right side. The results are highly similar, but the state-by-state approach suggests Indiana may lean toward Clinton in a Clinton vs Trump match up, that Pennsylvania may lean toward Trump in a Clinton vs Trump match up, and the results in Maine differ across the two sets of models.

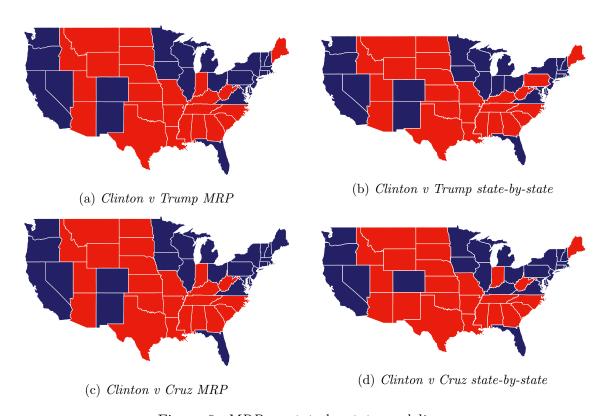
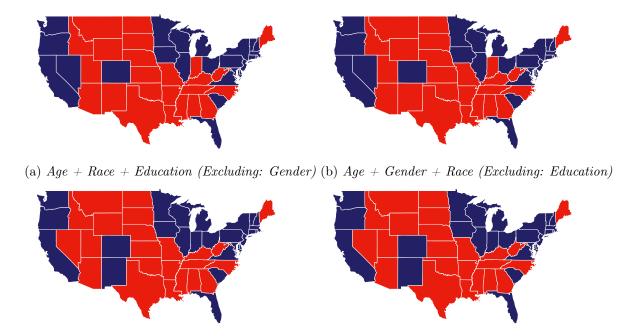


Figure 6: MRP vs state-by-state modeling

As with any statistical model, the decision to include or exclude certain variables will ultimately result in different predictive outcomes. Understanding this, in the hypothetical Clinton vs. Trump match up, we also developed separate models that looked at varying combinations of individual-level predictors to see how the electoral landscape is affected. Figure 7 is a set of four different predictive models with varying independent variables.



 $\hbox{(c) Gender} + Race + Education \ (\textit{Excluding: Age}) \ \hbox{(d) Gender} + Education + Age \ (\textit{Excluding: Race})$

Figure 7: Hypothetical Electoral Outcomes by Varying Individual-level Covariates

Simulations

We ran 100 bootstrap simulations with replacement of the full sample size. These simulations allow us to generate estimates of the percent of times each state leans Democratic (or Republican) and to construct levels of uncertainty using predictive intervals. Figure 8 below displays the results of each of these simulations. States are shaded dark red if close to 100% of the simulations showed the Republican candidate

winning the state, states are shaded dark blue if close to 100% of the simulations showed the Democratic candidate winning the state and they are shaded purple if each candidate has a 50-50 chance in the state.

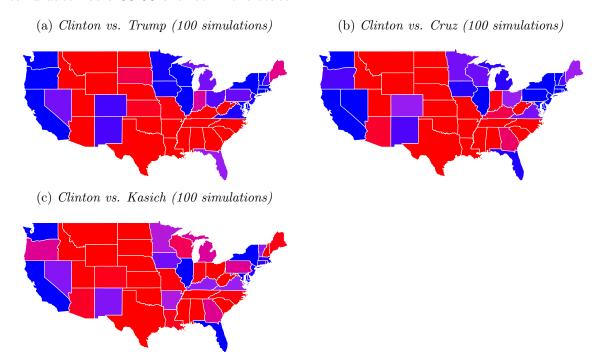


Figure 8: Electoral Maps of Hypothetical Match ups. Dark red means that 100% of the simulations yielded a Republican winner, dark blue means that 100% of the simulations yielded a Democratic winner and purple means that 50% of the simulations yielded a Republican winner.

Focusing first on the match up between Democrat Hillary Clinton and Republican Donald Trump (the top left pane), the simulations suggest that states like Florida are pure tossups and there is considerable uncertainty in states like Indiana, Michigan, and Nevada. The Clinton vs. Cruz simulation map (top right pane) looks quite similar, though states such as Colorado, Minnesota, Virginia, and Wisconsin have moved from the strong Democratic side to toss ups. The third map (bottom left pane), which displays Clinton vs. Kasich, is much more varied than the previous two maps. Kasich would perform strongly in the upper Midwest and has an advantage in states such as Colorado and Pennsylvania.

Some caveats in this work

In this section, we describe a few caveats concerning MRP in particular and in constructing state-level estimates more broadly.

First, we interviewed registered voters nationally rather than likely voters. Only about eight in 10 registered voters actually voted in the 2012 Presidential election, according to the 2012 Current Population Survey.⁷ If the composition of registered voters and likely voters differs considerably, then our results may change.

Second, respondents on these national surveys were asked about their vote if the election were held today. The November election is more than six months away and much can change throughout the Spring, Summer and Fall.

Third, we include all interviews conducted since January 1, 2016 for our estimates of Clinton vs. Trump and Clinton vs. Cruz. However, more than 30 primaries and caucuses have been held this cycle and a significant number of Americans may have changed their minds over the course of the past three months. It is worth noting that the estimates look similar if we construct them based only on interviews from late Mid-February 2016 through the present rather than starting in early January 2016.

Fourth, our poststratification utilizes 5-year estimates from the American Community Survey (ACS) among a sample of adult citizens. Using this set of data allows us to include variables such as education and race in our modeling that might not be available in statewide voter files, but it contains a broader universe of adults than registered voter samples from voter files might include. If likely voters differ considerably from likely voters based on characteristics such as age, gender and education, then our estimates may be biased.

Fifth, about one in six registered voters are undecided, or say they do not have an

⁷Link to the voting supplement of the November 2012 Current Population Survey https://www.census.gov/hhes/www/socdemo/voting/publications/p20/2012/tables.html

opinion either way, across the three hypothetical match ups. In this draft, we do not model how these undecided voters might act if they had to take a position.

Sixth, as shown above, the MRP models can be sensitive to the inclusion or exclusion of additional individual level and state-level variables, especially in smaller states or in battleground states.

Conclusions

Morning Consult asked more than 44,000 registered voters nationally over the past three months who they would support in a series of hypothetical general election match ups. We used a statistical technique called multilevel regression and poststratification (MRP) to construct state-level estimates from the national survey data. The results suggest that Democrat Hillary Clinton currently has an advantage over Republicans Donald Trump and Ted Cruz. On the other hand, the estimates suggest that Ohio Governor John Kasich edges out Clinton, likely due to much higher favorability levels among registered voters than Trump or Cruz and advantages in his home state of Ohio. Many caveats are in store due to the length of time between now and November, the high proportion of adults who are undecided and close margins in key states such as Florida, but the results suggest the 2016 presidential election map will look similar to the 2012 map if Democrat Hillary Clinton and Republican Donald Trump are their parties' respective nominees.

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Appendices

Model Specifications

Below we describe the specific parameters in our MRP model.

Let $\hat{\mathcal{Y}}$ be defined as the predicted probability that any one individual will support Hillary Clinton

$$Pr(y_i = 1) = \hat{\mathcal{Y}} = logit^{-1}(B^0 + \alpha_{k[i]}^{age} + \alpha_{l[i]}^{education} + \alpha_{m[i]}^{gender} + \alpha_{s[i]}^{state} + Bx_i)$$

Where:

$$logit^{-1}(\alpha) = \frac{exp(\alpha)}{exp(\alpha) + 1}$$

Where the modeled effects of individual level groups are drawn from a normal distributions with a mean of zero and variance that's unique to each covariate.

$$\begin{split} &\alpha_k^{age} \sim N(0,\sigma_{age}^2), for \ k=1,...,4 \\ &\alpha_l^{education} \sim N(0,\sigma_{education}^2), for \ l=1,...,4 \\ &\alpha_m^{gender} \sim N(0,\sigma_{gender}^2), for \ m=1,...,3 \\ &\alpha_s^{state} \sim N(0,\sigma_{state}^2), for \ s=1,...,51 \end{split}$$

Once we have $\hat{\mathcal{Y}}$ for each individual strata based on age, gender, education and state, we then compute the poststratified averages of $\hat{\mathcal{Y}}$ to develop state estimates of electoral support for each candidate. These mixed effects models allow both the state-level intercepts and slopes to vary. Specifically, the mixed-effects model develops estimates for each "type" of person and those estimates (support for Trump/Hillary) are then weighted in proportion to the frequencies of those types of people in each state.

$$\widehat{MRP_{state_i}} = \frac{\sum_{c \in s} N_c \theta_c}{\sum_{c \in s} N_c}$$

MRP Model Validation

We attempted to validate our MRP estimates by predicting well known demographic variables. In particular, we created a model to predict each state's population distribu-

tion by gender. The same variables that were used to predict election outcomes were used in the validation model (minus gender).

We then compared the MRP-gender-model to the standard approach of allocating respondents by state and applying state-based weights to see which method produced less error in predicting known census quantities of gender distributions by state.

To compare each method (MRP vs state-aggregation) we calculated the root-mean-squared-error (RMSE) for each method. RMSE is used to measure of the total differences between values predicted by the MRP model and the true observed values (Census estimates of gender by state). A lower RMSE score indicates a more accurate predictive model.

MRP-RMSE	State-Weights-RMSE
0.066	0.075

Table 1: Validation: RMSE scores for MRP and State-Weighting

When comparing MRP to the state-weights approach, we find that the RMSE for MRP is lower, which indicates that MRP performs better at predicting gender distributions at the state level.