# Q# 0.15 Language Quick Reference

<b>Primitive Types</b>				
64-bit integers	Int			
Double-precision floats	Double			
Booleans	Bool			
	e.g.: true or false			
Qubits	Qubit			
Pauli basis	Pauli			
	e.g.: PauliI, PauliX, PauliY, or PauliZ			
Measurement	Result			
results e.g.: Zero or One				
Sequences of	Range			
integers	e.g.: 110 or 510			
Strings	String			
	e.g.: "Hello Quantum!"			
"Return no	Unit			
information" type	e.g.: ()			

Derived Types	
Arrays	elementType[]
Tuples	(type0, type1,) e.g.:(Int, Qubit)
Functions	<pre>input -&gt; output e.g.: ArcCos : (Double) -&gt; Double</pre>
Operations	<pre>input =&gt; output is variants e.g.: H : (Qubit =&gt; Unit is Adj)</pre>

<b>User-Defined Ty</b>	pes					
Declare UDT with	newtype <i>Name</i> = (Type, Type);					
anonymous items	e.g.: newtype <i>Pair</i> = (Int, Int);					
Define UDT literal	Name(baseTupleLiteral)					
	e.g.: let origin = Pair(0, 0);					
Unwrap operator!	VarName!					
(convert UDT to	<pre>e.g.: let originTuple = origin!;</pre>					
underlying type)	(now originTuple = (0, 0))					
Declare UDT with	newtype <i>Name</i> =					
named items	(Name1: Type, Name2: Type);					
	e.g.: newtype Complex =					
	(Re : Double, Im : Double);					
Accessing named	VarName::ItemName					
items of UDTs	e.g.: complexVariable::Re					
Update-and-	set VarName w/= ItemName <- val;					
reassign for named e.g.: mutable $p = Complex(0., 0.)$ UDT items set $p = Re < -1.0$ ;						

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Symbols and Variables

Declare immutable symbol

Declare mutable symbol (variable)

Update mutable symbol (variable)

Apply-and-reassign

Symbol symbol (variable)

Apply-and-reassign

Set varName operator= expression e.g.: set counter += 1;
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Functions and Operations
Define function
                    function Name(in0 : type0, ...)
(classical routine)
                    : returnType {
                         // function body
Call function
                    Name(parameters)
                    e.g.: let two = Sqrt(4.0);
                    operation Name(in0 : type0, ...)
Define operation
(quantum routine)
                    : returnType {
with explicitly
                         body { ... }
specified body,
                         adjoint { ... }
                         controlled { ... }
controlled and
adjoint variants
                         adjoint controlled { ... }
                    operation Name(in0 : type0, ...)
Define operation
with automatically
                    : returnType is Adj + Ctl {
generated adjoint
and controlled
variants
Call operation
                    Name(parameters)
                    e.g.: Ry(0.5 * PI(), q);
Call adjoint
                    Adjoint Name(parameters)
operation
                    e.g.: Adjoint Ry(0.5 * PI(), q);
Call controlled
                    Controlled Name(controlQubits,
                         parameters)
operation
                    e.g.: Controlled Ry(controls,
                         (0.5 * PI(), target));
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Control Flow
Iterate over
                     for index in range {
a range of numbers
                         // Use integer index
                     e.g.: for i in 0..N-1 { ... }
While loop
                     while (condition) {
(within functions)
Iterate over
                     for val in array {
an array
                         // Use value val
                     e.g.: for q in register { ... }
Repeat-until-
                     repeat { ... }
success loop
                    until condition
                    fixup { ... }
Conditional
                     if cond1 { ... }
statement
                     elif cond2 { ... }
                     else { ... }
Ternary operator
                     condition ? caseTrue | caseFalse
Return a value
                     return value
Stop with an error
                     fail "Error message"
Conjugations
                     within { ... }
(ABA^{\dagger} \text{ pattern})
                     apply { ... }
```

Arrays						
Allocate array	rray mutable <i>name</i> = new <i>Type</i> [ <i>Length</i> ] e.g.: mutable b = new Bool[2];					
Get array length Length(name)						
Access k-th element	th element name[k] NB: indices are 0-based					
Assign k-th element (copy-and-update)	set name w/= k <- value e.g.: set b w/= 0 <- true;					
Array literal	[value0, value1,] e.g.: let b = [true, false, true];					
Array concatenation	<pre>array1 + array2 e.g.: let t = [1, 2, 3] + [4, 5];</pre>					
Slicing (subarray)	name[sliceRange] e.g.: if t = [1, 2, 3, 4, 5], then t[1 3]					

Debugging (classical)			
Print a string	Message("Hello Quantum!")		
Print an interpolated string	Message(\$"Value = {val}")		

## **Resources**

Documentation	
Quantum	https://docs.microsoft.com/
Development Kit	azure/quantum
QDK user guides	<pre>https://docs.microsoft.com/ azure/quantum/user-guide</pre>
Q# Libraries	https://docs.microsoft.com/
Reference	qsharp/api

Q# Code Repositories				
QDK Samples	https://github.com/microsoft/			
	quantum			
QDK Libraries	https://github.com/microsoft/			
	QuantumLibraries			
Quantum Katas	https://github.com/microsoft/			
(tutorials)	QuantumKatas			
Q# compiler and	https://github.com/microsoft/			
extensions	qsharp-compiler			
Simulation	https://github.com/microsoft/			
framework	qsharp-runtime			
Jupyter kernel and	https://github.com/microsoft/			
Python host	iqsharp			
Source code for	https://github.com/			
the documentation	MicrosoftDocs/quantum-docs			

# Qubit Allocation Allocate a register of N qubits use reg = Qubit[N]; // Qubits in reg start in $|0\rangle$ . ... // Qubits must be returned to $|0\rangle$ . Allocate one qubit use one = Qubit(); ... Allocate a mix of qubit registers and individual qubits use $(x, y, \dots) = (Qubit[N], Qubit(), \dots)$ ; ...

### 

Measurements	
Measure qubit in	M(oneQubit)
Pauli $Z$ basis	yields a Result (Zero or One)
Reset qubit to $ 0\rangle$	Reset( <i>oneQubit</i> )
Reset an array of	ResetAll( <i>register</i> )
qubits to $ 00\rangle$	

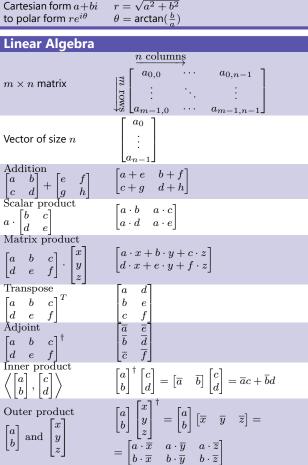
# Working with Q# from command line

Command Line Basics				
Change directory	cd dirname			
Go to home	cd ~			
Go up one directory	cd			
Make new directory	mkdir <i>dirname</i>			
Open current	code .			
directory in VS Code				

Working with Q# Projects				
Create new project	<pre>dotnet new console -lang Q#output project-dir</pre>			
Change directory to project directory	cd project-dir			
Build project	dotnet build			
Run all unit tests	dotnet test			

# **Math reference**

Complex Arithmetic				
-1				
(a+c) + (b+d)i				
$a \cdot c + a \cdot di + b \cdot ci + (b \cdot d)i^2 =$				
$= (a \cdot c - b \cdot d) + (a \cdot d + b \cdot c)i$				
$\overline{a+bi} = a - bi$				
$\frac{a+bi}{c+di} \cdot 1 = \frac{a+bi}{c+di} \cdot \frac{c-di}{c-di} = \frac{(a+bi)(c-di)}{c^2+d^2}$				
$\sqrt{a^2+b^2}$				
$\cos \theta + i \sin \theta$				
$e^a \cdot e^{bi} = e^a \cos b + ie^a \sin b$				
$r^a \cdot r^{bi} = r^a \cdot e^{bi \ln r} =$				
$= r^a \cos(b \ln r) + i \cdot r^a \sin(b \ln r)$				
$a = r \cos \theta$				
$b = r \sin \theta$				
$r = \sqrt{a^2 + b^2}$				
$\theta = \arctan(\frac{b}{a})$				



Gates i	Gates reference						
	Qubit gates						
Gate	Matrix representation	Ket-bra representation	Applying to $ \psi angle=lpha 0 angle+eta 1 angle$	Applying to basis states:	$\ket{0}, \ket{1}, \ket{+}, \ket{-}$ and	$ \pm i\rangle = \frac{1}{\sqrt{2}}( 0\rangle \pm i 1\rangle)$	
Χ	$\begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}$	$ 0\rangle \langle 1  +  1\rangle \langle 0 $	$ \psi\rangle = \alpha  1\rangle + \beta  0\rangle$	$X  0\rangle =  1\rangle X  1\rangle =  0\rangle$	$X \mid + \rangle = \mid + \rangle$ $X \mid - \rangle = - \mid - \rangle$	$egin{aligned} X \left  i  ight angle &= i \left  -i  ight angle \ X \left  -i  ight angle &= -i \left  i  ight angle \end{aligned}$	
Υ	$\begin{bmatrix} 0 & -i \\ i & 0 \end{bmatrix}$	$i(\ket{1}\bra{0}-\ket{0}\bra{1})$	$Y  \psi\rangle = i(\alpha  1\rangle - \beta  0\rangle)$	$Y  0\rangle = i  1\rangle$ $Y  1\rangle = -i  0\rangle$	$Y \mid + \rangle = -i \mid - \rangle$ $Y \mid - \rangle = i \mid + \rangle$	$egin{aligned} Y\ket{i} &= \ket{i} \ Y\ket{-i} &= -\ket{-i} \end{aligned}$	
Z	$\begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix}$	$ 0\rangle \left<0 - 1\rangle \left<1 \right $	$Z \left  \psi \right\rangle = \alpha \left  0 \right\rangle - \beta \left  1 \right\rangle$	$Z  0\rangle =  0\rangle$ $Z  1\rangle = - 1\rangle$	$Z \mid + \rangle = \mid - \rangle$ $Z \mid - \rangle = \mid + \rangle$	$egin{aligned} Z\ket{i} &= \ket{-i} \ Z\ket{-i} &= \ket{i} \end{aligned}$	
1	$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	$ 0\rangle \langle 0  +  1\rangle \langle 1 $	$I\ket{\psi}=\ket{\psi}$				
Н	$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}$	$ 0 angle\left\langle + + 1 angle\left\langle -  ight.$	$H  \psi\rangle = \alpha  +\rangle + \beta  -\rangle = \frac{\alpha + \beta}{\sqrt{2}}  0\rangle + \frac{\alpha - \beta}{\sqrt{2}}  1\rangle$	$H  0\rangle =  +\rangle H  1\rangle =  -\rangle$	$H \mid + \rangle = \mid 0 \rangle$ $H \mid - \rangle = \mid 1 \rangle$	$H \left  i \right\rangle = e^{i\pi/4} \left  -i \right\rangle$ $H \left  -i \right\rangle = e^{-i\pi/4} \left  i \right\rangle$	
S	$egin{bmatrix} 1 & 0 \ 0 & i \end{bmatrix}$	$\left 0\right\rangle \left\langle 0\right +i\left 1\right\rangle \left\langle 1\right $	$S\left \psi\right\rangle = \alpha\left 0\right\rangle + i\beta\left 1\right\rangle$	$S  0\rangle =  0\rangle$ $S  1\rangle = i  1\rangle$	$S \mid + \rangle = \mid i \rangle$ $S \mid - \rangle = \mid -i \rangle$	$S  i\rangle =  -\rangle$ $S  -i\rangle =  +\rangle$	
Т	$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\pi/4} \end{bmatrix}$	$\left 0\right\rangle \left\langle 0\right +e^{i\pi/4}\left 1\right\rangle \left\langle 1\right $	$T\left \psi\right\rangle = \alpha\left 0\right\rangle + e^{i\pi/4}\beta\left 1\right\rangle$	$T\ket{0}=\ket{0}$	$T\ket{1}=e^{i\pi/4}\ket{1}$		
$R_x(\theta)$	$\begin{bmatrix} \cos\frac{\theta}{2} & -i\sin\frac{\theta}{2} \\ -i\sin\frac{\theta}{2} & \cos\frac{\theta}{2} \end{bmatrix}$	$\begin{array}{l} \cos\frac{\theta}{2}\left 0\right\rangle\left\langle 0\right -i\sin\frac{\theta}{2}\left 1\right\rangle\left\langle 0\right -\\ -i\sin\frac{\theta}{2}\left 0\right\rangle\left\langle 1\right +\cos\frac{\theta}{2}\left 1\right\rangle\left\langle 1\right  \end{array}$	$\begin{array}{l} R_x(\theta) \left  \psi \right> = \ (\alpha \cos \frac{\theta}{2} - i\beta \sin \frac{\theta}{2}) \left  0 \right> + \\ + \left(\beta \cos \frac{\theta}{2} - i\alpha \sin \frac{\theta}{2}\right) \left  1 \right> \end{array}$	$R_x(\theta)  0\rangle = \\ = \cos \frac{\theta}{2}  0\rangle - i \sin \frac{\theta}{2}  1\rangle$	$egin{aligned} R_x( heta) \ket{1} &= \ &= \cos rac{ heta}{2} \ket{1} - i \sin rac{ heta}{2} \ket{0} \end{aligned}$		
$R_y(\theta)$	$\begin{bmatrix} \cos\frac{\theta}{2} & -\sin\frac{\theta}{2} \\ \sin\frac{\theta}{2} & \cos\frac{\theta}{2} \end{bmatrix}$	$\cos\frac{\theta}{2}\ket{0}\bra{0} + \sin\frac{\theta}{2}\ket{1}\bra{0} - \\ -\sin\frac{\theta}{2}\ket{0}\bra{1} + \cos\frac{\theta}{2}\ket{1}\bra{1}$	$\begin{split} R_y(\theta) \left  \psi \right\rangle &= \left( \alpha \cos \frac{\theta}{2} - \beta \sin \frac{\theta}{2} \right) \left  0 \right\rangle + \\ &+ \left( \beta \cos \frac{\theta}{2} + \alpha \sin \frac{\theta}{2} \right) \left  1 \right\rangle \end{split}$	$\begin{array}{l} R_y(\theta) \left  0 \right\rangle = \\ = \cos \frac{\theta}{2} \left  0 \right\rangle + \sin \frac{\theta}{2} \left  1 \right\rangle \end{array}$	$\begin{array}{l} R_y(\theta) \left  1 \right\rangle = \\ = \cos \frac{\theta}{2} \left  1 \right\rangle - \sin \frac{\theta}{2} \left  0 \right\rangle \end{array}$		
$R_z(\theta)$	$\begin{bmatrix} e^{-i\theta/2} & 0 \\ 0 & e^{i\theta/2} \end{bmatrix}$	$e^{-i\theta/2}\left 0\right\rangle \left\langle 0\right +e^{i\theta/2}\left 1\right\rangle \left\langle 1\right $	$R_z(\theta)  \psi\rangle = \alpha e^{-i\theta/2}  0\rangle + \beta e^{i\theta/2}  1\rangle$	$R_z(\theta)  0\rangle = e^{-i\theta/2}  0\rangle$	$R_z(\theta)  1\rangle = e^{i\theta/2}  1\rangle$		
$R_1(\theta)$	$\begin{bmatrix} 1 & 0 \\ 0 & e^{i\theta} \end{bmatrix}$	$ 0\rangle \langle 0  + e^{i\theta}  1\rangle \langle 1 $	$R_1(\theta)  \psi\rangle = \alpha  0\rangle + \beta e^{i\theta}  1\rangle$	$R_1(\theta) 0\rangle =  0\rangle$	$R_1(\theta)  1\rangle = e^{i\theta}  1\rangle$		
Two-a	ubit gates						
Gate	Matrix Representation	Ket-Bra Representation	Applying to $ \psi\rangle=lpha 00 angle+eta$	$ 01\rangle + \gamma  10\rangle + \delta  11\rangle$ Ap	oplying to basis states		
CNOT	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix}$	$\begin{array}{l}  00\rangle\langle00  +  01\rangle\langle01  +  11\rangle\langle\\ \text{or}\\  0\rangle\langle0  \otimes I +  1\rangle\langle1  \otimes X \end{array}$	$ 10 + 10 angle\langle11 $ CNOT $ \psi angle=lpha 00 angle+eta 01 angle$			$NOT\ket{10} = \ket{11}$ $NOT\ket{11} = \ket{10}$	
SWAP	$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$	$ 00\rangle \langle 00  +  01\rangle \langle 10  +  10\rangle$	$\langle 01 + 11 angle \langle 11 $ SWAP $ \psi angle = lpha  00 angle + oldsymbol{\gamma}  oldsymbol{01} angle$			$WAP\ket{10} = \ket{01}$ $WAP\ket{11} = \ket{11}$	
Controlle	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	$ 0\rangle\langle 0 \otimes I +  1\rangle\langle 1 \otimes U$	$CU\ket{\psi} = lpha\ket{00} + eta\ket{01} + (\gamma a_{0,0} + \delta a_{0,1})\ket{10} + (\gamma a_{0,0} + \delta a_{0,1})\ket{10} + (\gamma a_{0,0} + \delta a_{0,1})$			$\begin{array}{l} U \left  10 \right\rangle = a_{0,0} \left  10 \right\rangle + a_{1,0} \left  11 \right\rangle \\ U \left  11 \right\rangle = a_{0,1} \left  10 \right\rangle + a_{1,1} \left  11 \right\rangle \end{array}$	
Toffoli	(CCNOT) gate						

Gate	Matrix Representation Ket-Bra Representation	Applying to $ \psi\rangle = \alpha  000\rangle + \beta  001\rangle + \gamma  010\rangle + \delta  011\rangle + \epsilon  100\rangle + \lambda  101\rangle + \eta  110\rangle + \kappa  111\rangle$	Applying to basis states	
CCNOT	$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \end{bmatrix} (I_2 -  11\rangle \langle 11 ) \otimes I_1 +  11\rangle \langle 11  \otimes X$	$\begin{array}{l} CCNOT \left  \psi \right\rangle \ = \ \alpha \left  000 \right\rangle \ + \ \beta \left  001 \right\rangle \ + \ \gamma \left  010 \right\rangle \ + \\ \delta \left  011 \right\rangle + \epsilon \left  100 \right\rangle + \lambda \left  101 \right\rangle + \kappa \left  110 \right\rangle + \boldsymbol{\eta} \left  111 \right\rangle \end{array}$	$CCNOT  001\rangle =  001\rangle$ $CCNOT  010\rangle =  010\rangle$	$\begin{array}{l} {\sf CCNOT} 100\rangle =  100\\ {\sf CCNOT} 101\rangle =  101\\ {\sf CCNOT} 110\rangle =  111\\ {\sf CCNOT} 111\rangle =  110 \end{array}$