ITIS 6200/8200 Principles of Information Security and Privacy

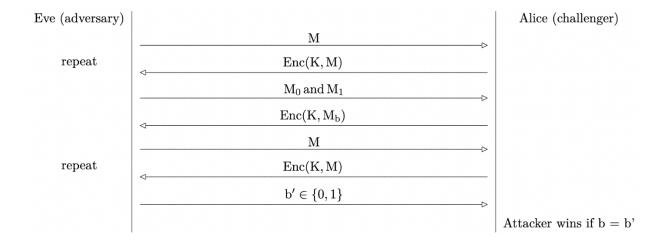
Homework 2

Question 1. Break block cipher DES (10 points)

The DES (Data Encryption Standard) was a symmetric encryption algorithm designed in 1976. It was the government standard until 2001. It has a block size of 64 bits, and key size of 56 bits. If Eve wants to brute-force attack DES, i.e., try all possible keys, how much time does Eve need? Assume that she can try 10^{10} keys per second with her personal computer. And one year is approximately 3×10^{7} seconds.

Question 2. IND-CPA (20 points)

When formalizing the notion of confidentiality, as provided by a proposed encryption scheme, we introduce the concept of indistinguishability under a chosen plaintext attack, or IND-CPA security. A scheme is considered IND-CPA secure if an attacker cannot gain additional information about a message given its ciphertext. This definition can be defined as an experiment between a challenger and adversary, detailed in the diagram below. Note that the same key K is used for encrypting different messages here.



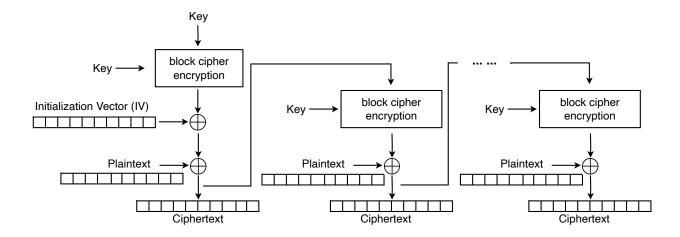
Q 2.1: Eve sends two messages M_0 and M_1 to Alice. Alice will flip a random bit $b \in \{0,1\}$, encrypt M_b , and send back $C = \text{Enc}(k, M_b) = M_b \oplus k$ to Eve. How does Eve determine b with probability > 1/2?

Q 2.2: Explain how an adversary can always win the IND-CPA game with probability 1 against a deterministic encryption algorithm. Note: Given an identical plaintext, a deterministic encryption algorithm will produce identical ciphertext.

Q 2.3: Explain why reusing keys in one-time pads is dangerous.

Question 3. Block Cipher Design (25 points)

Alice has developed a new block cipher as below:



The message M is split into j plaintext blocks $M_1 ... M_j$ each of size n. The encryption mode outputs (IV, $C_1, ..., C_j$) as the overall ciphertext. Assume that IV is randomly generated per encryption.

Q 3.1: Write down the encryption formula. That is, what is the formula for C_1 and C_i (0 < i <= j) given (1) plaintext $M_1 ... M_j$ (2) encryption algorithm Enc(K, M) which takes a key K and message M as inputs, and (3) a randomly generated IV.

Q 3.2: Write the decryption formula for M_i ($0 \le i \le j$) using this mode. That is, how to get M_1 and M_i ($0 \le i \le j$) given (1) ciphertext (IV, C_1 , ..., C_j) and (2) encryption algorithm Enc(K, M).

Q 3.3: Is this mode IND-CPA secure? If yes, explain why; if not, describe how an attacker can break IND-CPA.

Question 4. Hash (20 points)

Alice is sending message M to Bob in the following way:

Ciphertext
$$c = c_1 \parallel c_2$$
 where $c_1 = \text{Enc}(K, m)$ and $c_2 = \text{Hash}(c_1)$

Here, Enc(K,m) is the secure encryption scheme AES-CBC, and Hash(m) is the cryptographic hash function SHA-256.

- Q 3.1: Does this scheme provide confidentiality? E.g., can an eavesdropper Eve learn about the contents of the message?
- Q 3.2: Does this scheme provide integrity? E.g., can Mallory tamper with message without being detected?
- Q 3.3: Can you design an approach for sending the message so it provides both integrity and confidentiality?

Question 5. PRNGs and Diffie-Hellman Key Exchange (25 points)

Eve is an eavesdropper between Alice and Bob.

- 1. Alice and Bob each seed a PRNG with different random inputs.
- 2. Alice uses her PRNG from the previous step to generate a, and Bob uses his PRNG from the previous step to generate b.
- 3. Alice and Bob perform a Diffie-Hellman key exchange using their generated secrets (a and b). Recall that, in Diffie-Hellman, neither a nor b are directly sent over the channel.
- 4. Alice and Bob, without reseeding, each use their PRNG to generate some pseudorandom output.
- 5. Eve learns both Alice's and Bob's pseudorandom outputs.

Assume that Eve can learn the internal state of a PRNG at step 5. And Eve wants to learn the Diffie-Hellman shared secret g^{ab} mod p.

- Q 4.1: If Alice and Bob both use a PRNG that are not rollback-resistant. Can Eve learn about the shared secret g^{ab} mod p? If yes, how? If no, why?
- Q 4.2: If Alice uses a PRNG that is not rollback-resistant. Bob uses a PRNG that is rollback-resistant. Can Eve learn about the shared secret g^{ab} mod p? If yes, how? If no, why?
- Q 4.3: Assume that at step 2, Alice generates a secret value a = 3, and Bob generates a secret value b = 2. For step 3, the values of g and p are 5 and 7 respectively. Then, the shared secret should be $g^{ab} \mod p = 5^6 \mod 7 = 1$. However, Diffie-Hellman Key Exchange is vulnerable to Man-in-the Middle attack. Assume that Mallory is successfully launching Man-in-the Middle attack against the key exchange between Alice and Bob. Can you find a positive value m from Mallory, such that the shared secret Alice computes is the same as the shared secret Bob computes? (Hint: consider writing a short loop program in whatever programming languages you prefer to try different m)