## **COS 226 Programming Assignment**

## 8 Puzzle

Write a program to solve the 8-puzzle problem (and its natural generalizations) using

**The problem.** The 8-puzzle problem is a puzzle invented and popularized by Noyes square blocks labeled 1 through 8 and a blank square. Your goal is to rearrange the b permitted to slide blocks horizontally or vertically into the blank square. The followir goal board (right).

**Best-first search.** Now, we describe a solution to the problem that illustrates a gener

algorithm. We define a search node of the game to be a board, the number of moves

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initial search node (the initial board, 0 moves, and a null previous search node) into a with the minimum priority, and insert onto the priority queue all neighboring search modes (mose man can be reached in one move from the dequeued search node). Repeat this procedure until the search node dequeued corresponds to a goal board. The success of this approach hinges on the choice of priority *function* for a search node. We consider two priority functions:

- *Hamming priority function*. The number of blocks in the wrong position, plus the number of moves made so far to get to the search node. Intutively, a search node with a small number of blocks in the wrong position is close to the goal, and we prefer a search node that have been reached using a small number of moves.
- Manhattan priority function. The sum of the Manhattan distances (sum of the vertical and horizontal distance) from the blocks to their goal positions, plus the number of moves made so far to get to the search node.

For example, the Hamming and Manhattan priorities of the initial search node below are 5 and 10, respectively.

```
8
  1
      3
                   5
   6
      5
                   8
initial
                                Hamming = 5 + 0
                                                           Manhattan = 10 + 0
                  goal
```

We make a key oberservation: To solve the puzzle from a given search node on the priority queue, the total number of moves we need to make (including those already made) is at least its priority, using either the Hamming or Manhattan priority function. (For Hamming priority, this is true because each block that is out of place must move at least once to reach its goal position. For Manhattan priority, this is true because each block must move its Manhattan distance from its goal position. Note that we do not count the blank square when computing the Hamming or Manhattan priorities.) Consequently, when the goal board is dequeued, we have discovered not only a sequence of moves from the initial board to the goal board, but one that makes the fewest number of moves. (Challenge for the mathematically inclined: prove this fact.)

A critical optimization. Best-first search has one annoying feature: search nodes corresponding to the same board are enqueued on the priority queue many times. To reduce unnecessary exploration of useless search nodes, when considering the neighbors of a search node, don't enqueue a neighbor if its board is the same as the board of the previous search node.

```
1
      3
                                     3
                                                            2
                                  2
                                                        4
previous
             search node
                              neighbor
                                          neighbor
                                                       neighbor
                                         (disallow)
```

Detecting infeasible puzzles. Not all initial boards can lead to the goal board such as the one below.

infeasible

To detect such situations, use the fact that boards are divided into two equivalence classes with respect to reachability: (i) those that lead to the goal board and (ii) those that lead to the goal board if we modify the initial board by swapping any pair of adjacent (non-blank) blocks in the same row. (Difficult challenge for the mathematically inclined: prove this fact.) To apply the fact, run the A\* algorithm simultaneously on two puzzle instances—one with the initial board and one with the initial board modified by swapping a pair of adjacent blocks in the same row. Exactly one of the two will lead to the goal board.

**Board and Solver data types.** Organize your program by creating an immutable data type Board with the following API:

```
public class Board {
         public Board(int[][] blocks)
                                                 // construct a board from an N-by-N array of blocks
                                                 // (where blocks[i][j] = block in row i, column j)
                                                 // board dimension N
         public int dimension()
         public int hamming()
                                                 // number of blocks out of place
         public int manhattan()
                                                 // sum of Manhattan distances between blocks and goal
         public boolean isGoal()
                                                 // is this board the goal board?
         public Board twin()
                                                 // a board obtained by exchanging two adjacent blocks in the same row
         public boolean equals(Object y)
                                                 // does this board equal y?
                                                 // all neighboring boards
         public Iterable<Board> neighbors()
                                                 // string representation of the board (in the output format specified below)
         public String toString()
and an immutable data type Solver with the following API:
     public class Solver {
         public Solver(Board initial)
                                                  // find a solution to the initial board (using the A* algorithm)
                                                  // is the initial board solvable?
         public boolean isSolvable()
         public int moves()
                                                  // min number of moves to solve initial board; -1 if no solution
         public Iterable<Board> solution()
                                                  \ensuremath{//} sequence of boards in a shortest solution; null if no solution
         public static void main(String[] args) // solve a slider puzzle (given below)
```

To implement the A\* algorithm, you must use the MinPQ data type from algs4.jar for the priority queues.

**Solver test client.** Use the following test client to read a puzzle from a file (specified as a command-line argument) and print the solution to standard output.

```
public static void main(String[] args) {
    // create initial board from file
    In in = new In(args[0]);
    int N = in.readInt();
    int[][] blocks = new int[N][N];
    for (int i = 0; i < N; i++)
        for (int j = 0; j < N; j++)
blocks[i][j] = in.readInt();
    Board initial = new Board(blocks);
    // solve the puzzle
    Solver solver = new Solver(initial);
    // print solution to standard output
    if (!solver.isSolvable())
        StdOut.println("No solution possible");
    else {
        StdOut.println("Minimum number of moves = " + solver.moves());
        for (Board board : solver.solution())
            StdOut.println(board);
}
```

**Input and output formats.** The input and output format for a board is the board dimension *N* followed by the *N*-by-*N* initial board, using 0 to represent the blank square. As an example,

```
% more puzzle04.txt
0 1
      3
   2
      5
 4
   8 6
% java Solver puzzle04.txt
Minimum number of moves = 4
3
0
   1
      3
 4
   2
      5
 7
    8
       6
   0
      3
   2
      5
    8
       6
   2
      3
 4
   0
       5
   8
      6
 1
   2
      3
 4
   5
      0
```

```
7 8 6
3
1 2 3
4 5 6
7 8 0
% more puzzle-unsolvable3x3.txt
3
1 2 3
4 5 6
8 7 0
% java Solver puzzle3x3-unsolvable.txt
No solution possible
```

Your program should work correctly for arbitrary N-by-N boards (for any  $1 \le N \le 128$ ), even if it is too slow to solve some of them in a reasonable amount of time.

**Deliverables.** Submit the files Board.java and Solver.java (with the Manhattan priority). We will supply stdlib.jar and algs4.jar. Your may not call any library functions other than those in java.lang, java.util, stdlib.jar, and algs4.jar. You must use the MinPQ data type from algs4.jar for the priority queues.