Spec FAQ Project Submit

Write a program to estimate the value of the *percolation threshold* via Monte Carlo simulation.

Install our Java programming environment (optional). Install our custom IntelliJ programming environment by following these step-by-step instructions for your operating system [Mac OS X · Windows · Linux].

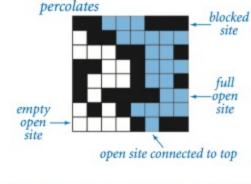
After following these instructions, the commands javac-algs4 and java-algs4 will classpath in algs4.jar , which contains Java classes for I/O and all of the algorithms in the textbook. To access a class in algs4. jar, you need an import statement, such as the ones below:

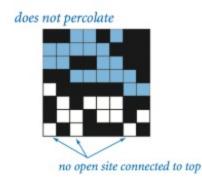
```
import edu.princeton.cs.algs4.StdRandom;
import edu.princeton.cs.algs4.StdStats;
import edu.princeton.cs.algs4.WeightedQuickUnionUF;
```

Note that your code must be in the default package, if you use a package statement, the autograder will reject your submission.

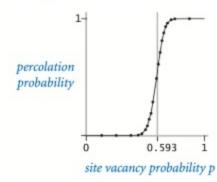
Percolation. Given a composite systems comprised of randomly distributed insulating and metallic materials: what fraction of the materials need to be metallic so that the composite system is an electrical conductor? Given a porous landscape with water on the surface (or oil below), under what conditions will the water be able to drain through to the bottom (or the oil to gush through to the surface)? Scientists have defined an abstract process known as *percolation* to model such situations.

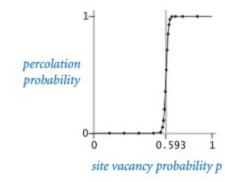
The model. We model a percolation system using an *n*-by-*n* grid of *sites*. Each site is either *open* or *blocked*. A *full* site is an open site that can be connected to an open site in the top row via a chain of neighboring (left, right, up, down) open sites. We say the system percolates if there is a full site in the bottom row. In other words, a system percolates if we fill all open sites connected to the top row and that process fills some open site on the bottom row. (For the insulating/metallic materials example, the open sites correspond to metallic materials, so that a system that percolates has a metallic path from top to bottom, with full sites conducting. For the porous substance example, the open sites correspond to empty space through which water might flow, so that a system that percolates lets water fill open sites, flowing from top to bottom.)





The problem. In a famous scientific problem, researchers are interested in the following question: if sites are independently set to be open with probability p (and therefore blocked with probability 1 - p), what is the probability that the system percolates? When p equals 0, the system does not percolate; when p equals 1, the system percolates. The plots below show the site vacancy probability p versus the percolation probability for 20-by-20 random grid (left) and 100-by-100 random grid (right).





When n is sufficiently large, there is a threshold value p^* such that when $p < p^*$ a random n-by-n grid almost never percolates, and when $p > p^*$, a random n-by-n grid almost always percolates. No mathematical solution for determining the percolation threshold p^* has yet been derived. Your task is to write a computer program to estimate p^* .

Percolation data type. To model a percolation system, create a data type Percolation with the following API:

```
public class Percolation {
    // creates n-by-n grid, with all sites initially blocked
    public Percolation(int n)
    // opens the site (row, col) if it is not open already
    public void open(int row, int col)
    // is the site (row, col) open?
    public boolean isOpen(int row, int col)
    // is the site (row, col) full?
    public boolean isFull(int row, int col)
    // returns the number of open sites
    public int numberOfOpenSites()
    // does the system percolate?
    public boolean percolates()
    // test client (optional)
    public static void main(String[] args)
}
```

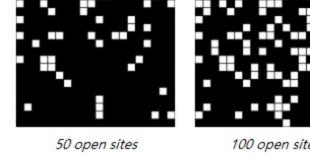
Corner cases. By convention, the row and column indices are integers between 1 and n, where (1, 1) is the upper-left site: Throw an IllegalArgumentException if any argument to open(), isOpen(), Or isFull() is outside its prescribed range. Throw an IllegalArgumentException in the constructor if $n \leq 0$.

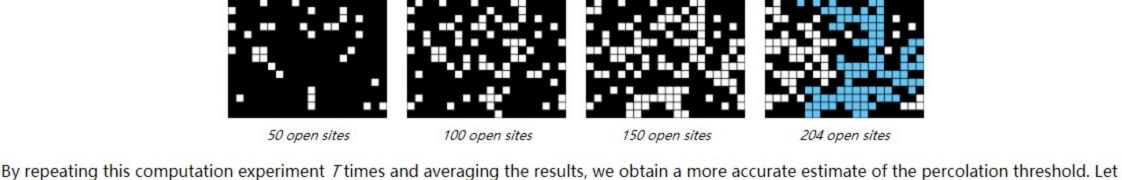
Performance requirements. The constructor should take time proportional to n^2 ; all methods should take constant time plus a constant number of calls to the union-find methods union(), find(), connected(), and count().

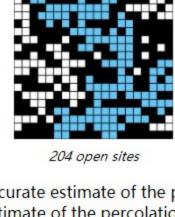
Monte Carlo simulation. To estimate the percolation threshold, consider the following computational experiment:

- Initialize all sites to be blocked.
- Repeat the following until the system percolates:
 - Choose a site uniformly at random among all blocked sites.
 - Open the site.
- The fraction of sites that are opened when the system percolates provides an estimate of the percolation threshold.

For example, if sites are opened in a 20-by-20 lattice according to the snapshots below, then our estimate of the percolation threshold is 204/400 = 0.51 because the system percolates when the 204th site is opened.







 x_t be the fraction of open sites in computational experiment t. The sample mean \overline{x} provides an estimate of the percolation threshold; the sample standard deviation s, measures the sharpness of the threshold. $\overline{x} = rac{x_1 + x_2 + \dots + x_T}{T}, \quad s^2 = rac{(x_1 - \overline{x})^2 + (x_2 - \overline{x})^2 + \dots + (x_T - \overline{x})^2}{T}$

Assuming
$$T$$
 is sufficiently large (say, at least 30), the following provides a 95% confidence interval for the percolation threshold:

 $\left[\overline{x} - \frac{1.96s}{\sqrt{T}}, \ \overline{x} + \frac{1.96s}{\sqrt{T}} \right]$

L
$$\sqrt{T}$$
 \sqrt{T}]

To perform a series of computational experiments, create a data type PercolationStats with the following API.

public class PercolationStats {

```
public PercolationStats(int n, int trials)
           // sample mean of percolation threshold
           public double mean()
           // sample standard deviation of percolation threshold
           public double stddev()
           // low endpoint of 95% confidence interval
           public double confidenceLo()
           // high endpoint of 95% confidence interval
           public double confidenceHi()
          // test client (see below)
          public static void main(String[] args)
       }
Throw an Illegal Argument Exception in the constructor if either n \leq 0 or trials \leq 0.
Also, include a main() method that takes two command-line arguments n and T, performs T independent computational experiments (discussed
```

// perform independent trials on an n-by-n grid

above) on an n-by-n grid, and prints the sample mean, sample standard deviation, and the 95% confidence interval for the percolation threshold. Use StdRandom to generate random numbers; use StdStats to compute the sample mean and sample standard deviation.

~/Desktop/percolation> java-algs4 PercolationStats 200 100 = 0.5929934999999997 mean

```
= 0.00876990421552567
       95% confidence interval = [0.5912745987737567, 0.5947124012262428]
       ~/Desktop/percolation> java-algs4 PercolationStats 200 100
                            = 0.592877
       stddev
                              = 0.009990523717073799
        95% confidence interval = [0.5909188573514536, 0.5948351426485464]
       ~/Desktop/percolation> java-algs4 PercolationStats 2 10000
                             = 0.666925
                             = 0.11776536521033558
       95% confidence interval = [0.6646167988418774, 0.6692332011581226]
        ~/Desktop/percolation> java-algs4 PercolationStats 2 100000
                              = 0.6669475
       stddev
                              = 0.11775205263262094
        95% confidence interval = [0.666217665216461, 0.6676773347835391]
Analysis of running time and memory usage (optional and not graded). Implement the Percolation data type using the quick find algorithm in
QuickFindUF .
```

- Use Stopwatch to measure the total running time of PercolationStats for various values of n and T. How does doubling n affect the total running time? How does doubling Taffect the total running time? Give a formula (using tilde notation) of the total running time on your computer (in seconds) as a single function of both n and T.
- Using the 64-bit memory-cost model from lecture, give the total memory usage in bytes (using tilde notation) that a Percolation object uses to model an *n*-by-*n* percolation system. Count all memory that is used, including memory for the union–find data structure.

Now, implement the Percolation data type using the weighted quick union algorithm in WeightedQuickUnionUF . Answer the questions in the previous paragraph.

Web submission. Submit a .zip file containing only Submit only Percolation. java (using the weighted quick-union algorithm from WeightedQuickUnionUF) and PercolationStats. java. We will supply algs4. jar. Your submission may not call library functions except those in StdIn , StdOut , StdRandom , StdStats , WeightedQuickUnionUF , and java.lang.

For fun. Create your own percolation input file and share it in the discussion forums. For some inspiration, do an image search for "nonogram" puzzles solved."