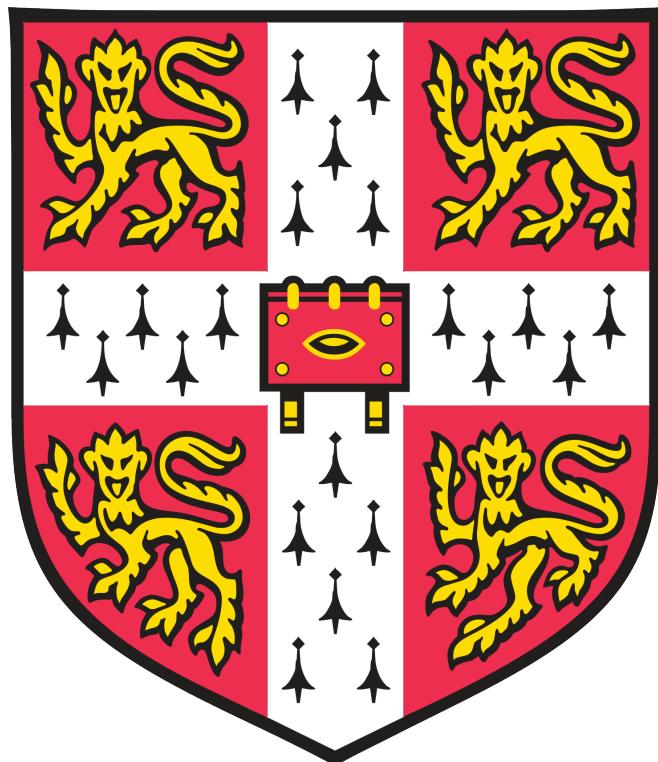


Joshua Bird

Distributed Visual Simultaneous Localization and Mapping



Computer Science Tripos – Part II
Queens' College

April 24, 2024

Declaration

I, Joshua Bird of Queens' College, being a candidate for Part II of the Computer Science Tripos, hereby declare that this dissertation and the work described in it are my own work, unaided except as may be specified below, and that the dissertation does not contain material that has already been used to any substantial extent for a comparable purpose. In preparation of this dissertation I did not use text from AI-assisted platforms generating natural language answers to user queries, including but not limited to ChatGPT. I am content for my dissertation to be made available to the students and staff of the University.

Signed: Joshua Bird

Date: April 24, 2024

Proforma

Candidate number: <CANDIDATE NUMBER>
Project Title: **Distributed Visual Simultaneous Localization
and Mapping**
Examination: **Computer Science Tripos – Part II, 2024**
Word Count: <WORD COUNT>¹
Code Line Count: <LINE COUNT>²
Project Originator: Joshua Bird, Jan Blumenkamp
Project Supervisor: Jan Blumenkamp

Original Aims of the Project

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Special Difficulties

None.

¹This word count was computed using `texcount`.

²This code line count was computed using `cloc` (excluding autogenerated test output).

Contents

Chapter 1

Introduction

Visual Simultaneous Localization and Mapping (visual SLAM) serves as the foundation of countless modern technologies, with self-driving cars, augmented reality devices and autonomous drones just being a few examples. By using purely visual inputs, visual SLAM is able to create a 3D map of the surroundings while also localizing the camera's position within this map in real time.

Unlike other SLAM systems which may use expensive and heavy sensor such as LIDAR, RGB-Depth cameras or Radar, visual SLAM only requires the ubiquitous camera sensor, allowing the technology to be used in many commercial applications such as Google's ARCore¹, Boston Dynamic's GraphNav system used on their robot Spot², and several models of DJI quadcopters³ making this a particularly practical field of research.

1.1 Motivation

Multi-robot systems are only becoming more common as automation in numerous fields continues to grow, such as self-driving cars, drone swarms and warehouse robots. These systems require the agents to understand the world around them, as know each other's locations within that world for collision avoidance. This task is often achieved with technologies such as GPS or motion capture setups, however we can not assume that all environments will have access to these systems. A few emerging examples include:

- Search and rescue operations in large indoor systems, assisted by drone swarms.
- Self-driving cars in underground road networks.
- Multi-agent cave/subsea exploration.

These are scenarios where multi-agent SLAM is able to assist, as it enables us to build a map of an unknown environment and keep agents aware of their relative poses. However, the majority of existing multi-agent visual SLAM implementations are centralized systems, requiring the agents to maintain reliable communications with the central server in order to operate. This is somewhat counterintuitive, as environments which don't have access to GPS or motion capture systems are more than likely to also have very poor communication channels – greatly limiting the use cases of these centralized multi-agent SLAM systems.

Naturally, this leaves us with distributed multi-agent visual SLAM systems which do not rely on a centralized management server, allowing the agents to be used in environments where network

¹<https://developers.google.com/ar/develop/fundamentals>

²<https://support.bostondynamics.com/s/article/GraphNav-Technical-Summary>

³DOI: 10.1016/j.vrih.2019.09.002

infrastructure may be lacking. Instead of a central node, the agents are able to communicate peer-to-peer when they come within close proximity with one another.

It is easy to see the broad reaching uses cases this opens up. Agents will be able to explore sections of the world independently or in small teams, sharing new world locations with their peers as they come into communication range using an ad-hoc network. Agents will only know their peer's locations when they are within communication range, but this is sufficient if we only need the relative position for collision avoidance (as is common in multi-robot systems).

1.2 Project Overview

In this project, I:

1. Design and implement a distributed multi-agent visual SLAM system that is capable of localization, relative pose estimation and collaborative mapping, all while being tolerant to degraded network conditions and not reliant on any single leader agent.
2. Create a simulation environment for testing and evaluating my system locally.
3. Deploy my system on physical robots, demonstrating the practical use cases of this system and benchmarking real world performance.
4. Develop *Multi-Agent EVO* – the first open source evaluation library for multi-agent SLAM systems.
5. Develop the *Raspberry Pi Video Publisher* – a generic platform for SLAM data collection or augmented reality visualizations.
6. Evaluate the performance of my system on standardized datasets, **demonstrating that its performance is superior to comparable state-of-the-art systems.**

Chapter 2

Preparation

2.1 Starting Point

As noted in the *Relevant Work* section, visual SLAM systems are a mature and well-researched subfield of Computer Science with many advanced implementations. To avoid spending the majority of my effort re-implementing a visual SLAM system from scratch, I instead used a **single-agent** visual SLAM implementation as the starting point for my project. The thinking behind this decision was that it would allow me to focus my efforts on the distributed multi-agent aspect of this project, which I believe is a novel and under-researched aspect of the field.

I chose ORB-SLAM3 as the single agent SLAM system to base my system on top of, as it ranks at the top of benchmarks in a variety of environments [1] and its researchers released code alongside their paper. I primarily utilized the system's visual odometry (VO) front end and helper functions from the backend to perform operations such as bundle adjustment.

While ORB-SLAM3 is an excellent SLAM system, it is fundamentally a single-agent system with no considerations in place for use in a multi-agent context. As I will expand on in the *ORB-SLAM 3* section, a significant amount of time and effort was required to understand its extremely large undocumented codebase, especially since an almost complete understanding of its inner workings were needed to both extract and inject map information from the system. In retrospect, using an existing single-agent SLAM system as a foundation may not have saved as much time as I had initially hoped. I spent all of Michaelmas term wrangling with ORB-SLAM's codebase and was not able to begin making proper progress on the distributed aspect of my project until after Christmas break.

Nevertheless, using a cutting-edge single-agent SLAM system as a foundation for my project has allowed me to create a distributed SLAM system that performs better than comparable state-of-the-art systems, making it suitable for real-world applications.

At the time of submitting my project proposal, I had forked the ORB-SLAM3 [2] git repository¹ and explored the codebase. ORB-SLAM3 is licensed under GPL-3.0, and as such, I have open-sourced my code under the same license.

I had no prior experience working with SLAM systems, but I had researched the current state of multi-agent visual SLAM systems to evaluate the feasibility of my project and to prevent it from being a duplication of prior work.

¹https://github.com/UZ-SLAMLab/ORB_SLAM3

2.2 Relevant Work

While single-agent SLAM systems are a relatively mature field of research, multi-agent systems are still very much in active development.

TODO: even include?

Centralized multi-agent systems such as CCM-SLAM(2019) [3] and COVINS(2021) [4] require a centralized server to perform map merges and PGO. While simpler to implement, this comes with the obvious limitations that come with centralized systems such as scalability issues and requiring existing networking infrastructure.

In recent years we have seen the emergence of a handful of decentralized multi-agent systems, however they have various limitations. Various systems such as [5] [6] [7] require the agents to be initialized with their ground truth poses, which limits their real-world usability. In contrast, my system is able to provide accurate relative localization even when agents are initialized in arbitrary and unknown locations by identifying common landmarks in the world.

?? lays out the sensor configurations used by other various state-of-the-art distributed SLAM systems, showing that my system stands out as the only distributed system capable of operating with purely monocular visual data. This is advantageous, as LiDAR, & RGBD sensors have considerable weight, and stereo cameras may require a minimum camera separation to operate, both of which limit their usage on small aerial robots.

System	Collaboration Type	Monocular	Stereo	Monocular +IMU	Stereo +IMU	LiDAR +IMU	RGBD +IMU
My System	Decentralized	X					
D²SLAM	Decentralized				X		
CCM-SLAM	Centralized	X					
COVINS	Centralized			X			
Kimera-multi	Decentralized				X		X
Swarm-SLAM	Decentralized				X	X	X
DOOR-SLAM	Decentralized				X		

Figure 2.1: Comparison of modern multi-agent SLAM systems. My SLAM system is the only decentralized monocular system available.

TODO: fact check below lol Additionally, my system provides a novel approach to the Distributed Pose Graph Optimization (DPGO) problem. There are various methods to approaching DPGO. SWARM-SLAM(2024) [8] elects a single agent to perform the PGO for the entire swarm, which is simple but has a high communication overhead since all agents have to send their pose estimations before each optimization. Other systems perform DPGO by spreading computation across agents by using algorithms such as ARock [9] or Distributed Gauss-Seidel [10], however these methods still present a communication overhead and may stall under unreliable communication.

Instead of performing discrete optimization runs, my method of DPGO is performed incrementally. Each agent optimizes its pose graph as external data streams in, with a separate map alignment step. This method has no additional communication overhead, apart from the infrequent map alignment step, and we show its very competitive performance in the ?? Section. The details of this are presented in the ?? Section.

2.3 Visual SLAM Background

Before developing a distributed multi-agent SLAM system, we must first understand the basics of a visual SLAM. This is a topic on which numerous books [11] and research papers [12] have discussed in depth, which I will attempt to summarize here.

2.3.1 Problem Statement

2.3.2 Visual Odometry

2.3.3 Feature Descriptors

2.3.4 Loop Closure

2.4 Development Tools & Frameworks

From the start, I knew that a well-structured development plan would be essential to the successful implementation of this project. An entire suite of infrastructure had to be implemented to aid the development of my distributed SLAM system.

2.4.1 Webots Simulation Software

Robotics projects work in the physical domain, however testing in the real world requires a large amount of setup and infrastructure. To ensure fast iteration, I decided to use simulations for the majority of my development, allowing me to easily test my system in various environments and scenarios before committing to deploying it on physical robots.

The details of integrating Webots into my project are explored in the ?? Section, including the ROS interfaces developed and agent controllers.

2.4.2 Testing Infrastructure

Along with being very useful for real-time testing, the simulation software also allowed me to record numerous test cases which I used as regression tests and benchmarks for my system throughout development.

I have built a central management interface that allows me to record and replay datasets from the simulation software, among many other functions. There are datasets for testing all core functionality of my SLAM system, which I would run at regular intervals during development to ensure that no features had regressed and to ensure performance was improving.

2.4.3 Robot Operating System 2 Communication Middleware

Robot Operating System (ROS) 2 is the glue holding everything together, allowing independent software processes and hardware to communicate through an abstracted messaging interface.

ROS has long been the industry standard, being almost ubiquitous in both robotics research and the commercial sector. Confusingly, ROS is not an operating system at all, but instead a cross-platform development framework that provides a middleware to facilitate reliable communication between independent processes called *nodes*. These nodes can be on the same device or a device within the local area network and may be written in C++ or Python. Nodes communicate by *publishing* and *subscribing* to different *topics*, allowing both peer-to-peer communication and broadcasting.

Since every node is abstracted away behind the interface provided by the various topics, we can easily swap out nodes in this system. For example, we can substitute the real camera for a simulated camera to test our system in a virtual environment without having to change any other part of our system – as shown in ???. This makes transitioning between the real and simulated world almost seamless, which I knew would be essential for this project as I planned to test my system in simulations before running it on physical robots.

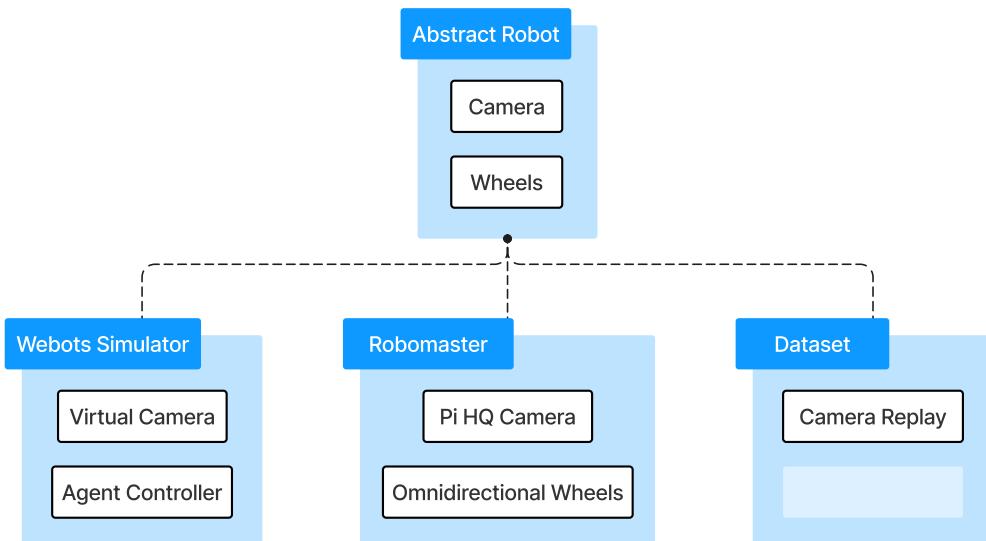


Figure 2.2: All robot types inherit the abstract robot interface, allowing my SLAM system and its supporting infrastructure to be completely agnostic to the actual type of robot used.

Furthermore, using the ROS framework allows my code to be far more portable, as anyone can download my nodes, link the camera topics up to their robot's camera, and run my SLAM system with minimal effort. This turns my project from being something that only runs on my hardware to something that anyone can take and run on their own robot.

There are two versions of ROS: ROS 1 and ROS 2. I chose to use ROS 2 due to its improved decentralized properties, which align with the goals of this project. ROS 2 conforms to the Data Distribution Service (DDS)¹ specification, which guarantees a reliable broadcast and, unlike ROS 1, it does not require a leader node when used in a multi-agent setup.

¹https://en.wikipedia.org/wiki/Data_Distribution_Service

2.4.4 Docker Containers

Docker containers are used on all physical deployments of my software, including the Cambridge RoboMasters used for real-world testing of my SLAM system and my Raspberry Pi Video Publisher platform which is used for custom dataset collection and augmented reality visualizations.

Docker allows the software to be isolated in self-sufficient environments, making it easy to deploy on many computing environments. Additionally, using Docker allows my code to be built once and then deployed on multiple robots, preventing the need to rebuild the system on every robot which saves a significant amount of time. These aspects of Docker are expanded upon in the section below.

2.4.5 Continuous Integration / Continuous Deployment

My GitHub repositories are set up to perform continuous integration via GitHub Action. Every time code is pushed to the repository, all 5 core packages (`controller`, `interfaces`, `motion_controller`, `orb_slam3_ros`, `webots_sim`) are built to ensure there are no compile time errors.

Additionally, a Docker container is cross-compiled to `arm64` and uploaded to Docker Hub. These Docker images can then be downloaded to the Cambridge RoboMasters (the platform used for real-world testing) and immediately run. This greatly speeds up development, as compiling the codebase locally on the Cambridge RoboMasters takes over 20 minutes for each robot.

Aside from the core packages, we also perform continuous integration as well as continuous deployment for the Raspberry Pi video publisher package. This pipeline is displayed in ???. A Docker container is similarly cross-compiled to `arm64` and uploaded to Docker Hub, and it is automatically deployed to the Raspberry Pis so they will run the latest version of the package.

Continuous deployment makes sense for this use case as the Raspberry Pis are designed to be plug-and-play, starting video streaming as soon as they are turned on. Unlike the Cambridge RoboMasters which are frequently ssh'ed into to pull specific Docker images and start experiments, we want the Raspberry Pis to use the latest software as soon as it is pushed to the GitHub repository.

The ease of use of the Raspberry Pi ROS video publisher platform that I have developed has made them an invaluable tool in the Prorok Lab, even being used by other researchers. TODO: get other people to use them lol

2.5 Datasets

A variety of industry-standard datasets were utilized to benchmark the performance of my SLAM system, including the EuRoC Machine Hall [13] and TUM-VI [14] datasets. While these datasets provide a variety of sensors, we only utilize a monocular video as input when evaluating performance. Further information about each dataset is provided in the ?? Section.

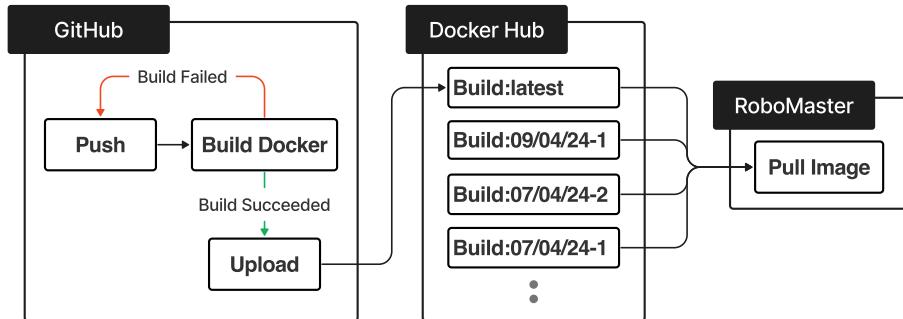


Figure 2.3: Automated continuous integration pipeline for the Cambridge RoboMasters. Continuous deployment is implemented for the Raspberry Pi video publishers by pulling from Docker Hub and running the container on startup.

In addition to standard datasets, I also generated custom datasets within the simulated environment to use as regression tests during development. These datasets test individual capabilities of the system such as multi-agent map merging, losing localization, etc. I then ran these tests on my system to ensure that the system performed as expected and that metrics such as time-to-merge and average trajectory error were decreasing as I iterated on my system.

2.6 Algorithms

This section will briefly cover some of the existing algorithms utilized within my SLAM system, and can be used as a reference when reading the ?? Section.

2.6.1 Kabsch-Umeyama Algorithm

2.6.2 Visual Bag of Words

2.6.3 RANSAC

2.7 Requirements Analysis

2.7.1 Development Model

Chapter 3

Implementation

3.1 Agent Architectural Overview

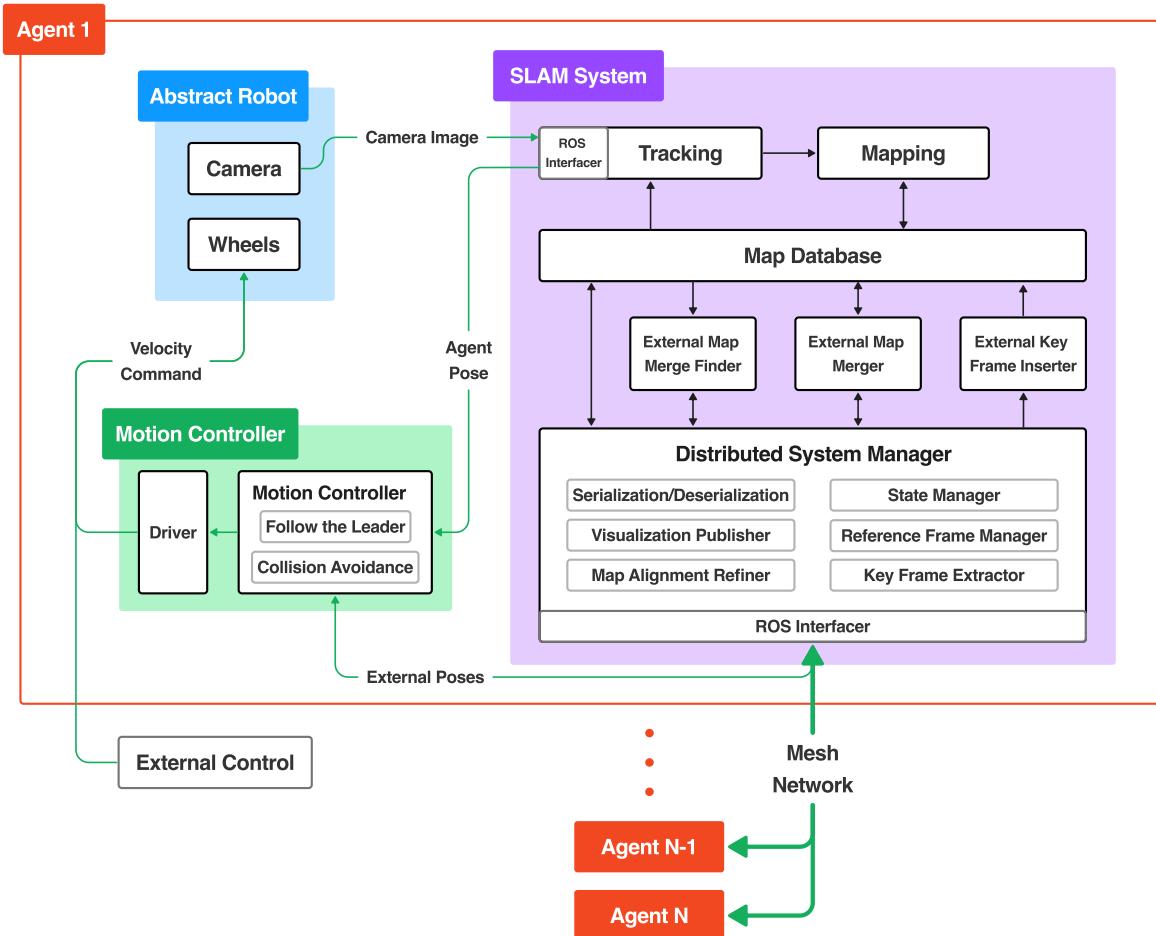


Figure 3.1: Agent diagram. Green arrows represent messages sent over ROS topics, while black arrows represent internal communications within a node.

?? gives an architectural overview of an agent, showing how the **Abstract Robot**, **SLAM System** and **Motion Controller** ROS nodes interconnect.

From a high level, we have an **Abstract Robot** node that provides an interface to the robot's hardware, as explained in ?? . This sends camera images to the **SLAM System** node, which builds a map of the world in collaboration with its peers. The **Motion Controller** node receives agent pose information from both the local **SLAM System** and the external peers to perform tasks such as collision avoidance by sending velocity commands back to the **Abstract Robot** node, closing the control loop.

In the following sections, we will explore these nodes in detail.

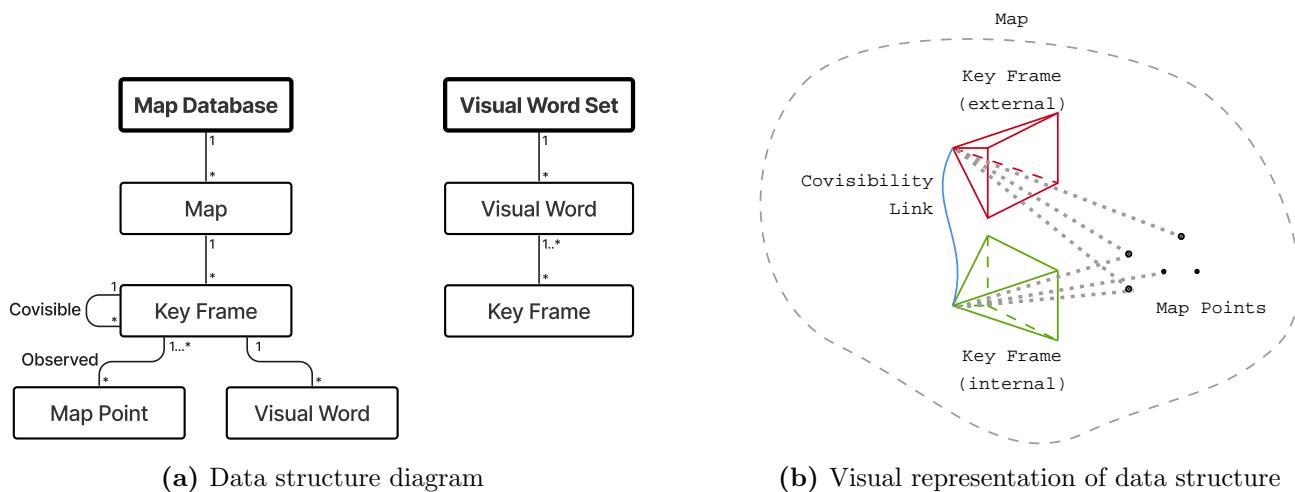
3.2 SLAM System

The SLAM System node is the majority of this project's implementation. It processes monocular images from the camera to localize the agent while also collaboratively building up a map of the world with its peers. As discussed in ??, my system is based on an existing single-agent SLAM system that performs the **Tracking** and **Mapping** tasks. While substantial modifications were made to the base single-agent system, I will generally focus on the decentralized layer I have built on top in the interest of space.

3.2.1 Datastructures

A brief discussion of my SLAM system's internal data structures is required to understand the following sections. ?? shows the two key data structures: the map database and the visual word set. The map database contains multiple maps, which primarily consist of keyframes and map points. Keyframes are "snapshots" of the world, containing the predicted pose of the agent at that time along with the observed world features which we call "map points". These map points can be observed by multiple keyframes, as shown in ??, and when this happens we connect the keyframes with a "co-visible" link.

Keyframes also have multiple "visual words", which are vectors describing the visual contents of the keyframe. These are essential for detecting potential map merges, so we also build a "visual word set" that allows us to find all keyframes that contain a particular visual word.



3.2.2 Decentralized System Manager

Decentralized collaborative SLAM systems have significantly more complexity than a single-agent or even centralized collaborative system, due to the complex interactions between agents as they merge maps, lose localization, or lose connection with the network. Therefore, a robust framework must be put in place to ensure the robustness and correctness of the system, which I have implemented in the **Decentralized System Manager** component.

For the sake of simplicity, the following explanations will explore the interactions between just two agents: a *local* and *external* agent. In the ?? Section, we will show how this easily generalizes to a system with an arbitrary number of agents when augmented by some simple rules.

3.2.2.1 State Manager

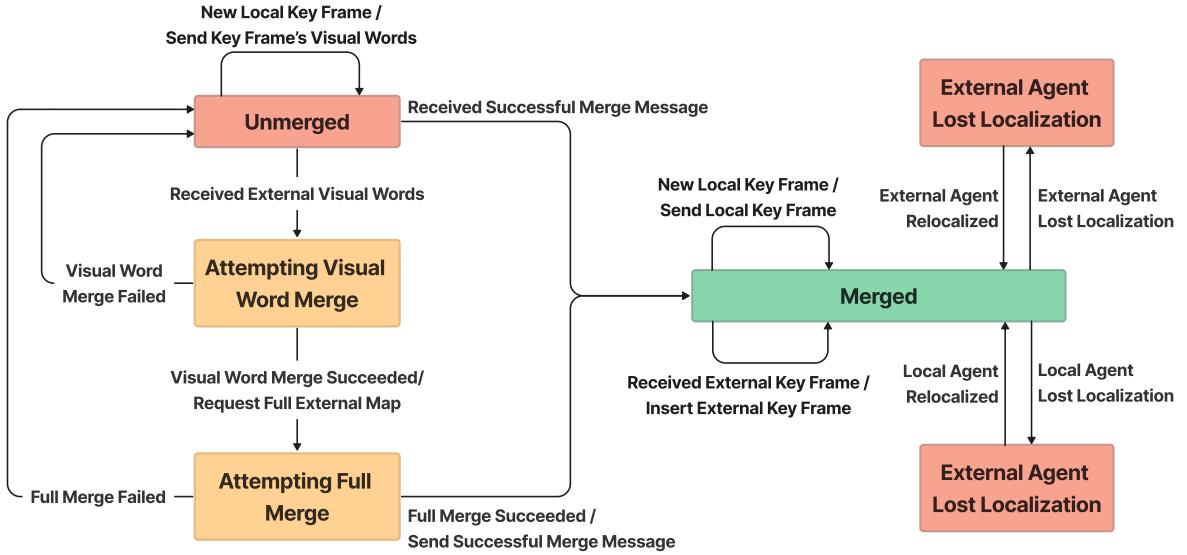


Figure 3.3: SLAM system state machine for a single peer. Mealy machine notation is used, where each transition is defined as: `input/output`.

Each agent's Decentralized System Manager maintains a state machine for every peer in the system, shown in ???. All peers are initially in the **unmerged** state, meaning that they are in different coordinate frames and can not collaboratively build a map together. As the local agent starts to explore the same places as its peers, we are able to recognize the visual overlaps and merge their maps, bringing us to the **merged** state where the agents share the same coordinate frame and map, enabling relative positioning and collaborative map building.

3.2.2.2 External Map Merge Finder

A naive approach to merging maps with an external agent is to constantly exchange our full maps, each time trying to identify if a map merge is possible. While simple, this approach clearly does not scale well from both a networking and computational perspective, as maps are often 1MB in size and computing a full map merge is extremely computationally expensive.

Instead, we first identify if a map merge is even feasible by using visual words before attempting a full map merge. This eliminates superfluous map merge attempts that have no chance of succeeding because the agents' maps have no visual overlap.

As the agents generate new keyframes, we use DBoW2 [15] to calculate the visual bag of words seen by that keyframe and send them to our peers over the `/new_key_frame_bows` ROS topic. These visual words are significantly smaller than sending over the complete map (as shown in ??) and enable agents to detect if there is a significant amount of visual overlap between its local map and the external agent's map. This is computed by ??.

This method gives a recall of almost 100%, at the cost of potentially lower precision. This is a worthwhile tradeoff however, as it is essential to have very few false negatives so we can merge maps as soon as possible so the agents can begin collaborating and determine relative positioning.

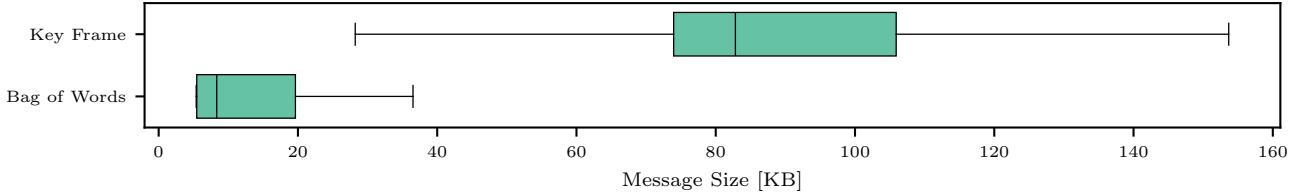


Figure 3.4: Comparison of the message size difference between a raw keyframe and a bag of words representation of a keyframe.

Algorithm 1 Map merge finder using visual words. TODO: improve

Input: $VisualWords_{ext}$: Set containing external keyframe's visual words

Output: $Success$: Boolean value signaling if a merge is possible based on visual words

- 1: $(MergeScore_{ext}, BestMatchKeyFrame) \leftarrow CalculateMergeScore(VisualWords_{ext})$
 - 2: $(MergeScore_{baseline}, _) \leftarrow CalculateMergeScore(BestMatchKeyFrame's \text{ visual words})$
 - 3: $Success \leftarrow MergeScore_{ext} \geq MergeScore_{baseline}$
-

3.2.2.3 External Map Merger

Performing full map merges is perhaps the most important component of the decentralized SLAM system, as a bad map merge will make it impossible for agents to collaborate. Additionally, it is one of the most computationally intensive parts of this system, therefore, it has gone through numerous iterations to optimize performance and reduce map merge errors.

The external map merger leverages components of the ORB-SLAM3 loop closure module, as it is a fundamentally similar problem. The final version of the map merger works as follows:

1. **Request external agent's full map.**

Once a potential map merge with the external agent is identified by the external map merge finder, we can begin a full merge attempt. We first request the full map from the external agent through the `/get_current_map` ROS topic. Once the map is received, we deserialize it and place it into our *map database* data structure as a separate map.

2. **Confirm that a map merge is possible using the full map data, and find the translation $T_{loc \rightarrow ext}$ that aligns the local map to the external map.**

The visual word map merge finder works well considering its very low communication overhead, however we need to confirm that a map merge is possible using the full map data from both agents. This is performed using the ORB-SLAM3 loop closure detector.

If we determine the merge to not be possible, we delete the external map from our map database and exit this process.

3. **Apply translation $T_{loc \rightarrow ext}$ to our local map.**

4. **Move a subset of the external map's keyframes and map points into our local map**

Given the external keyframe k_0 whose visual words triggered this map merge attempt, we extract a *local window* K of keyframes connected to k_0 in the co-visibility graph and move them to our local map. Moving only a small number of keyframes at first allows the merge and bundle adjustment process to be completed faster, which is important as they block local mapping from being performed.

5. **Merge local and external map points, connecting the maps**

6. Run bundle adjustment to optimize map point and keyframe positions.
7. Repeat steps 5-7 with the entirety of the external map.
8. Broadcast successful merge message.

If the full map merge is ultimately successful, we broadcast a `/successfully_merged` message to tell the external agent that we have successfully merged their map. The external agent will then move to the `merged` state and both agents will begin sharing keyframes with each other.

By the end of the merge process, the local agent will change its coordinate frame to that of the external agent.

It is important to note that this system requires only one agent to identify and calculate the map merge, significantly reducing the computational overhead of map merging, especially in systems with many agents (further explained in the ?? Section).

3.2.2.4 External KeyFrame Inserter

Once the local and external agents have merged their maps and share the same coordinate frame, they can begin sharing keyframes with each other.

Each agent maintains a set of sent keyframes K_{sent} and map points M_{sent} . The set of unsent keyframes and map points are therefore represented as $K_{unsent} = K / K_{sent}$ and $M_{unsent} = M / M_{sent}$ respectively. Once $\#K_{unsent}$ exceeds a certain threshold, we serialize K_{unsent} and M_{unsent} and send them to the external agent. Finally, we add K_{unsent} to K_{sent} and M_{unsent} to M_{sent}

Upon receiving the serialized keyframes and map points, the external agent deserializes them and adds them to a queue to await insertion into their local copy of the shared map by the *external keyframe inserter*.

The external keyframe inserter is run whenever we have spare cycles on the CPU, to prevent impacting the local tracking and mapping performance. The insertion process involves the following operations:

1. Pop external keyframe k_{ext} from front of queue.
2. Move k_{ext} and its new external observed map points M_{ext} to the local map.
Since the local and external agents are merged and in the same coordinate frame, we can simply move k_{ext} and M_{ext} to our local map without any transformations.¹

¹I had previously used a *keyframe anchor* method, where instead of k_{ext} having an absolute pose we would send its pose relative to the previous k_{ext} . The thought process behind this was to prevent minor misalignments between the local and external maps from preventing external keyframes from properly integrating with the local map. However, experimental testing showed that this method instead caused the local and external maps to frequently diverge.

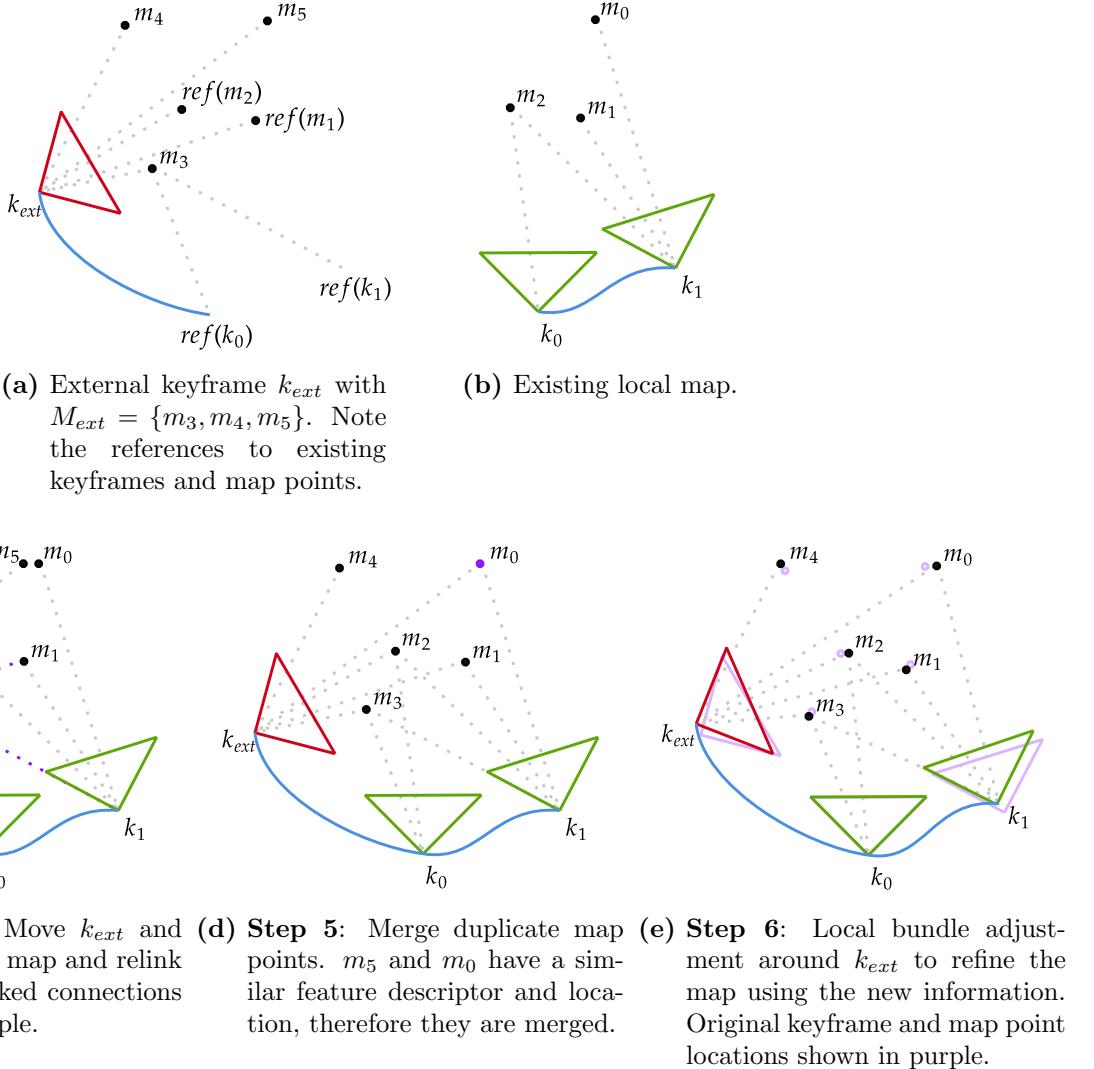


Figure 3.5: Visual overview of inserting external keyframes and map points into the local map. External keyframe (a) and initial local map (b) are combined to create our final local map (e).

3. Relink k_{ext} with co-visible keyframes and observed map points in the local map.

k_{ext} contains references to its co-visible keyframes and child map points that have already been sent or were generated by another agent. We search our local map for objects that match these references, reconnecting them. More details of the deserialization process are given in ??.

4. Relink M_{ext} with keyframes in the local map which observe it.

M_{ext} contains references to keyframes that observe it which have already been sent or were generated by another agent. We search our local map for keyframes that match these references, reconnecting them. More details of the deserialization process are given in ??.

5. Merge M_{ext} with map points in the local map.

M_{ext} will already be correctly linked to observing keyframes in the local map, however, due to communication latency some map points in M_{ext} may be duplicates of existing map points in the local map. Therefore, we exploit spatial locality to combine duplicate map points that describe the same physical feature. A key observation was that this step

is essential to ensuring the local and external keyframes stay well connected, ensuring the local and external maps do not diverge.

6. Perform a local bundle adjustment around k_{ext} .

Since we have merged map points in the previous step, we need to perform bundle adjustment to tweak the keyframe and map point locations to minimize reprojection error. This helps create a more accurate map, minimizing tracking error. We also only need to perform this bundle adjustment locally, greatly reducing the computational cost.

3.2.2.5 Local KeyFrame Inserter

As mentioned in the ?? section, it is essential that the local and external maps stay well connected, sharing the majority of their map points. In other words, we must ensure that the external map data is integrated throughout the whole SLAM pipeline.

The *Tracking* and *Mapping* modules, which are responsible for localizing the robot and generating new keyframes, only interact with the *Map Database*. Our external keyframe inserter does all the work of properly reconnecting external map points and merging duplicate map points, leaving the *Map Database* data structure looking as if all the map points and keyframes were generated locally. This abstracts the *Tracking* and *Mapping* modules away from the distributed aspects of the system, allowing them to fully utilize the external map points when localizing the agent and generating new keyframes.

3.2.3 Generalizing to $N \geq 3$ Agent Systems

Now that we have explained how a pair of agents interact, we can explore how this can be generalized to a system with an arbitrary number of agents.

We assume a system with N agents $A = \{agent_1, agent_2, \dots, agent_N\}$, where $agent_i$ is the agent with ID = i. Within this system we maintain a state $S_i = state_{n-m}$ for every agent pair ($agent_n, agent_m$), giving us a total of $N(N-1)/2$ states. Conceptually, this is a fully connected graph with agents as the nodes and states between agents as the edges. We also have a set G which contains all the groups of merged agents. The *group leader* is defined as the agent in a group with the lowest agentId.

In the case where agents can lose communication with one another, we also assume that if any given $agent_n$ is able to communicate with an $agent_m$, $agent_n$ can also communicate with all of $agent_m$'s connected peers. This is held if the agents are using a mesh network to communicate, for example.

Initially, every agent pair is unmerged so every state in S is set as *unmerged* and $G = \{\{agent_1\}, \{agent_2\}, \dots, \{agent_N\}\}$

A key insight of my distributed SLAM system is to delegate all merge operations to group leaders. This means that instead of all agents attempting merges with every other agent, only group agents have to attempt merges amongst themselves. This is significant, as the computational load of these merge operations scale proportional to the square of the number of agents involved, and in most use cases the number of group leaders quickly drops to be much lower than the total number of agents.

Additionally, having all merge operations performed by the group leader prevents potential race conditions introduced by communication latency within a group, for example two agents within a group both merging with different agents at the same time.

As discussed in the External Map Merge Finder and External Map Merger Sections, the two major operations needed to merge are (1) exchanging visual words to identify visual overlap and therefore merge opportunities and (2) sending over the map and attempting a full map merge.

Tackling (1) first, instead of the group leader only sending the visual words of its own keyframes, it will send the visual words of all keyframes generated by agents within its group. Keep in mind that it will only be sending these visual words to other group leaders. This introduces no additional intra-group communication, as all agents within a group already send each other all new keyframes.

Moving on to (2), once a pair of group leaders ($agent_n, agent_m$) (with $n < m$) have successfully merged their maps, the agent with the larger ID ($agent_m$) will change its coordinate frame to the agent with the smaller ID ($agent_n$). $agent_m$ will then send the transform from $agent_m$ to $agent_n$'s coordinate frame to the other agents in its group, allowing them to also change to $agent_n$'s coordinate frame. After this has been completed, $agent_m$'s group merges into $agent_n$'s group by updating S according to ??, and agents begin exchanging keyframes to update each other's maps. Eventually, once all agents are merged together, they will all be in $agent_0$'s coordinate frame.

Agents are able to keep track of the current groups and group leaders within the decentralized system since all successful merge messages are broadcast on the shared /`successfully_merged` ROS topic.

$$\forall i \in g_n. \forall j \in g_m. state_{i-j} \in S \text{ and } state_{i-j} = \text{"merged"} \quad (3.1)$$

where $g_n, g_m \in G$ are the groups that $agent_n$ and $agent_m$ respectively lead.

This is perhaps best represented in visual form by the simple 3-agent merge example given in ?? which shows the messages sent between the agents. This example is slightly simplified as all potential merges result in successful full merges. In reality, multiple potential merges may be identified before two agents successfully merge.

3.2.3.1 Map Alignment Refiner

As our shared map grows, the maps stored locally by the agents may "fall out of alignment". By this, we mean that the maps are slightly translated, rotated, or scaled with respect to the lead agent's map. This is largely a side effect of our aggressive early merge strategy which may merge two agents' maps before there is significant overlap, causing the estimated map alignment (ie. transformation between the two agents' origins) to have some error.

These small alignment errors are completely acceptable when maps are small, but may cause the maps to diverge as they grow.

To remedy this problem, we continuously refine our map alignment using ?? and the Kabsch-Umeyama point alignment algorithm. Map alignment is performed as follows:

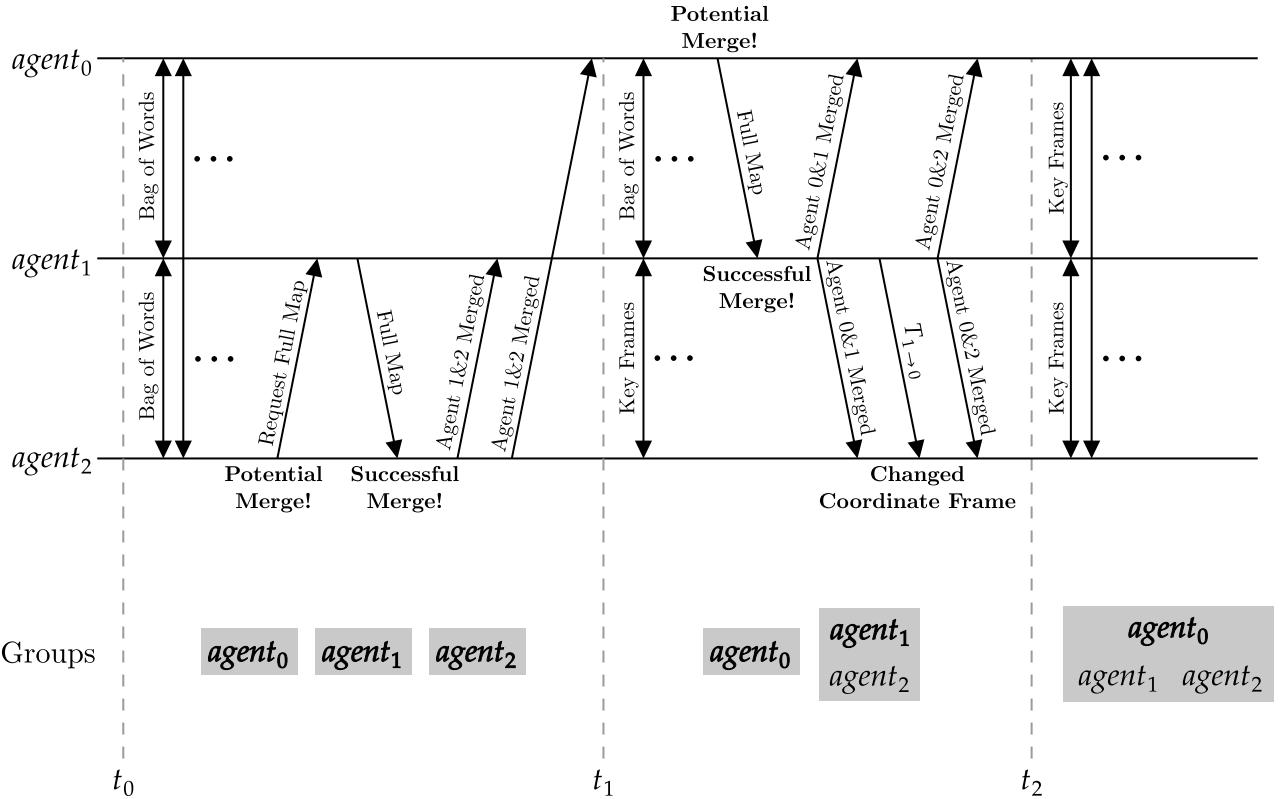


Figure 3.6: This is a simple 3 agent merge example where $agent_1$ and $agent_2$ merge first, and then $agent_0$ and $agent_1$. Agents in the same group are shown in the same rectangle, and the group leader is bolded.

Initially at t_0 , all agents are unmerged and therefore share the bag of words representations of new keyframes with the other agents. A potential merge with $agent_1$ is then detected by $agent_2$. Since $2 > 1$, $agent_2$ needs to perform the merge so it request $agent_1$'s full map. It successfully merges with $agent_1$'s full map and broadcasts this information to all other agents.

At t_1 , $agent_1$ and $agent_2$ are merged therefore they begin exchanging keyframes. $agent_0$ and $agent_1$ are the two remaining group leaders, so they continue to exchange their new keyframe's bag of words. $agent_0$ detects a potential merge, and since $0 < 1$ it sends its full map to $agent_1$. $agent_1$ is able to successfully merge with $agent_0$'s full map, so it broadcasts that $agent_0$ and $agent_1$ have implicitly merged. Additionally, it sends the transform $T_{1 \rightarrow 0}$ ($agent_1$'s coordinate frame to $agent_0$'s coordinate frame) to $agent_2$ allowing it to change to $agent_0$'s coordinate frame. $agent_1$ then broadcasts that $agent_0$ and $agent_2$ have implicitly merged.

At t_2 , all three agents are merged and in $agent_0$'s coordinate frame, and therefore they all exchange keyframes with one another.

1. **Request map point locations from the lead agent.**

This is defined as the set $TaggedMP_{ext}$ where $TaggedMP_{exti} = (uuid, (x, y, z))$

2. **Extract local map point locations.**

This is defined as the set $TaggedMP_{local}$ where $TaggedMP_{locali} = (uuid, (x, y, z))$

3. **Use the Kabsch-Umeyama and RANSAC algorithms to find transform T which best aligns $TaggedMP_{ext}$ to $TaggedMP_{local}$.** The Kabsch-Umeyama algorithm finds the

$SIM(3)$ transformation T from $TaggedMP_{ext}$ to $TaggedMP_{local}$, minimizing the RMSE. However, our input data has a large number of outliers so we use RANSAC on top to find a good fit while ignoring outliers.

The RANSAC and Kabsch-Umeyama algorithms are described in detail in ?? and ?? respectively.

4. Apply transformation T to our local map.

We use an *additive increase multiplicative decrease* methodology to control how often map alignment is performed. Given t_i is the time between the i -th and $(i + 1)$ -th map alignments, we set $t_{i+1} = t_i + 1$ if the maps were well aligned, and $t_{i+1} = t_i/2$ if the maps were not well aligned. This prevents agents from continuously performing map alignments when their maps are already well aligned.

3.2.3.2 Losing Localization / Connection

An agent can lose localization within the map, for example, if the camera is blocked for a short period of time. When this happens, the agent signals to the other agents that it has lost localization and they temporarily stop sharing new keyframes. When the agent relocates itself, keyframe sharing resumes and the agents send all the stored-up unsent keyframes.

Losing connection is very similar, where keyframe exchanging is stopped until the connection is regained, at which point the agents update each other with the stored-up unsent keyframes.

3.2.3.3 Visualization Publisher

All 3D visualizations are created by publishing ROS markers, a standardized ROS message type that represents some object in 3D space such as lines, points, or meshes. These ROS markers can then be displayed by a variety of third-party visualization tools such as RViz [16] and Foxglove Studio [17].

Using ROS markers allows me to leverage these mature visualization tools instead of creating one from scratch, and also allows visualizations to be easily saved and replayed for later analysis.

3.2.4 Map Serialization and Deserialization

Map serialization and deserialization are essential and non-trivial components of this SLAM system, allowing agents to share their maps across the network. For this task, I used the Boost [18] Serialization C++ library since it supports standard library collections and other common classes.

As discussed in ??, maps contain keyframes and map points. Individually, these objects are relatively easy to serialize with boost – in fact, the single agent SLAM program my system is based on already supported saving and loading maps allowing me to leverage some of their serialization helper functions. To serialize these objects we simply need to define a serialization scheme for each custom class, describing which class variables should be serialized and which

shouldn't. Strategically selecting only the parameters that need to be serialized allows us to cut back on communication overhead. For example, there is no need for us to serialize a keyframe's raw image, as it is not used in the rest of our SLAM pipeline.

Complexities arise when we try to serialize/deserialize the connections between these objects, especially when we are only sending map fragments. For example, if we send a new keyframe k and its map points M_k to an external agent, due to the many-to-many relationship between keyframes and map points, some of the map points in M_k may have already been sent before. We can define $M_k = M_{k_sent} \cup M_{k_unsent}$, where M_{k_sent} are the map points that have already been sent to the external agent and M_{k_unsent} are the ones that have not. Map points in M_{k_sent} will need to be connected to k when it is deserialized by the external agent, and map points in M_{k_unsent} will need to be sent to the external agent and connected to any existing keyframes in the external map that observe the map points.

We manage these connections by giving every keyframe and map point a universal unique identifier (UUID), allowing us to use these UUIDs as references to a specific object in our multi-agent system. The beauty of UUIDs is that they do not require a centralized server to assign a unique ID to every object. Instead, we can generate the unique IDs without any communication with our peers¹.

This method of using UUIDs as references is used to rebuild all connections after deserialization, including the keyframe-to-keyframe connections that build the co-visibility graph and many others that I have not had the space to discuss in this dissertation.

3.3 Motion Controller

While not a part of the core SLAM system, the motion controller node closes the control loop and demonstrates the real-world usability of my system. From a high level, the motion controller node consumes the local and external agents' poses and outputs a command velocity to the robot's movement system – all via ROS topics. For this project, I have implemented two different motion control systems which can be switched out seamlessly.

3.3.1 Follow The Leader

The "follow the leader" motion controller consists of two agents: one leader and one follower. The follower is given a position and rotation offset to the leader which it attempts to maintain as the leader is moved around.

For example, you could set the follower to be 1 meter behind the leader and with a 180° rotational offset. This ensures that the leader and follower have no visual overlap, demonstrating that my SLAM system is truly building a shared map.

Spinning the agents around in a circle demonstrates that the two agents' maps are properly merged and that the agents are using map points generated by an external agent to localize themselves, giving accurate relative positioning even when there is no visual overlap at any given moment.

TODO: add figure of the map built

¹While not *verifiably* unique, UUIDs are unique within practical limits. A commonly cited anecdote is that it is far more likely for a cosmic ray to cause a bug than a UUID collision.

3.3.2 Multi-Agent Collision Avoidance

The "multi-agent collision avoidance" example is more complex, employing a non-linear model predictive controller (NMPC) to avoid collisions with both static and dynamic obstacles. My NMPC system is derived from [19] and is defined as follows:

3.3.2.1 Non-Linear Model Predictive Controller Formulation

We assume an agent with current pose $\mathbf{p} \in \mathbb{R}^2$ and radius r . Firstly, we define our agent's control input \mathbf{v}_{cmd} as a function describing its velocity over time. We can then define our agent's state \mathbf{x} as the control input \mathbf{v}_{cmd} applied to its current pose \mathbf{p} :

$$\mathbf{x}(t) = \mathbf{p} + \int_0^t \mathbf{v}_{cmd} dt \quad (3.2)$$

We can then solve the following minimization problem to find an optimal \mathbf{v}_{cmd} :

$$\begin{aligned} \min_{\mathbf{v}_{cmd}} & \int_{t=0}^T J_x(\mathbf{x}(t), \mathbf{x}_{ref}(t)) + J_s(\mathbf{x}(t)) + J_d(\mathbf{x}(t)) dt \\ \text{subject to } & \mathbf{v}_{min} \leq \mathbf{v}_{cmd} \leq \mathbf{v}_{max} \end{aligned} \quad (3.3)$$

where T is our horizon length, \mathbf{x}_{ref} is our target trajectory, and J_x , J_s , J_d are the cost functions for this system.

Cost function J_x rewards following the target trajectory \mathbf{x}_{ref} and is shown below:

$$J_x(\mathbf{x}, \mathbf{x}_{ref}) = \|\mathbf{x} - \mathbf{x}_{ref}\|^2 \quad (3.4)$$

J_s and J_d penalize collisions with static objects and dynamic objects respectively. They are defined as:

$$J_s(\mathbf{x}) = \sum_{i=1}^{N_{static}} \frac{s_s * Q_s}{1 + \exp(d_i^{static}/s_s)} \quad (3.5)$$

$$J_d(\mathbf{x}) = \sum_{i=1}^{N_{dynamic}} \frac{s_d * Q_d}{1 + \exp(d_i^{dynamic}/s_d)} \quad (3.6)$$

where d_i^{static} is the distance between the agent and the i -th static obstacle, and $d_i^{dynamic}$ is the distance between the agent and the i -th dynamic obstacle. For example, if the i -th dynamic obstacle is another agent with radius r then $d_i^{dynamic} = \|\mathbf{x}(t) - \mathbf{x}_i(t)\|^2 - r$. $Q_s > 0$ and $Q_d > 0$ are weights that define how far the agent stays away from static obstacles compared to dynamic ones.

Additionally, we define s_s and s_d as a scale normalizing parameter that ensures the minima of $J_x + J_s$ and $J_x + J_d$ are greater than agent radius r in the single obstacle case. Essentially, this ensures that the optimized trajectory of the agent never comes within radius r of an obstacle unless it is being "squished" by two obstacles.

To calculate s_s , we first find the positive minima x_{min} of $J_x + J_s$ in the worst case where $d_i^{static} = J_x$ (ie. the static obstacle and x_{ref} are in the same place), with $s = 1$. This gives us x_{min} as defined in ???. Our scaling factor can then be defined as $s_s = \frac{r}{x_{min}}$, which sets the positive minima of $J_x + J_s$ to be r in the above situation. The calculation of s_d is symmetric, simply using Q_d instead of Q_s .

$$x_{min} = \ln \left(\frac{\sqrt{Q_s^2 - 4Q_s} + Q_s}{2} - 1 \right) \quad (3.7)$$

The key benefit of these cost functions is that the optimal distance to obstacles of r is invariant to parameters Q_s and Q_d . This is in contrast to [19] which requires you to retune the parameters κ and Q upon changing agent radius r . This is because their cost functions do not have their minima at the collision point, but instead at some point before the collision that varies with κ , Q , and r , making tuning very difficult. This is visualized in ???

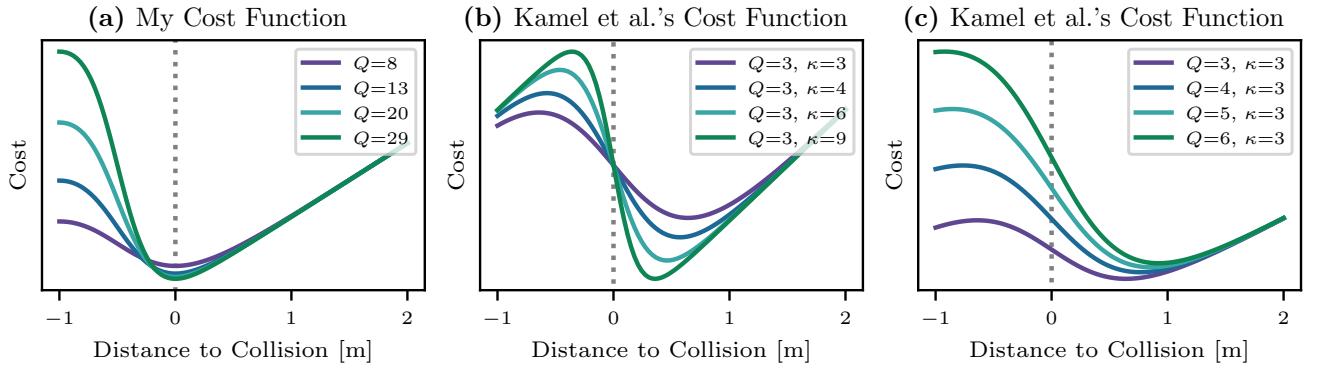


Figure 3.7: Comparison of my cost function (a) and Kamel et al.’s cost function (b), (c) when the obstacle and goal pose are at the same location. This demonstrates that my cost function’s minima is always at the collision point and does not vary as the parameters are changed, as opposed to Kamel et al.’s function.

3.3.2.2 Implementation Details

Solving the integral in ?? is computationally inefficient, therefore we split our calculations into discrete time steps. Specifically, the time horizon is set as $T = 500ms$ with $100ms$ timesteps.

The Sequential Least Squares Programming minimization method is used due to its robustness and ability to constrain the optimization space. We set parameters $Q_s = 8$ and $Q_d = 12$ to make the agent more adverse to approaching dynamic obstacles compared to static ones, as there is more uncertainty in the dynamic obstacle’s location. To calculate the future locations of dynamic obstacles $x_i^{dynamic}$ we employ a simple constant velocity model.

Our SLAM system does not use a depth camera or LiDAR, and therefore only produces a sparse map. Therefore, we need to define the location of static obstacles manually. Both static obstacles and the goal pose are set using interactive ROS markers, allowing them to be changed “on the fly” using software such as RViz.

3.4 Central Management Interface

While my multi-agent system is fully decentralized, a significant amount of work was put into developing the supporting infrastructure needed to control, test, and evaluate this system.

This was part of a broader aim of this project to create more than just a research project that only runs on my machine. I have strived to develop a system that can be deployed in real-world use cases, and the significant infrastructure released alongside my SLAM system hopes to help achieve that goal.

The primary method of managing the distributed system is through the *Central Management Interface*, which can be used to:

1. **Manually control the agent's poses.**

Users can click and drag on an image in area 1 to rotate the agent's camera and use the keyboard to move the agent around.

2. **Record camera data from the simulation software.**

3. **Play datasets back for testing and benchmarking purposes.**

Additionally, there are settings to remap topics and control the speed of playback.

4. **Record trajectories generated by the SLAM system as well as ground truth data for later evaluation.**

The recorded trajectory data can later be ingested by my custom evaluation library Multi-Agent Evo for analysis.

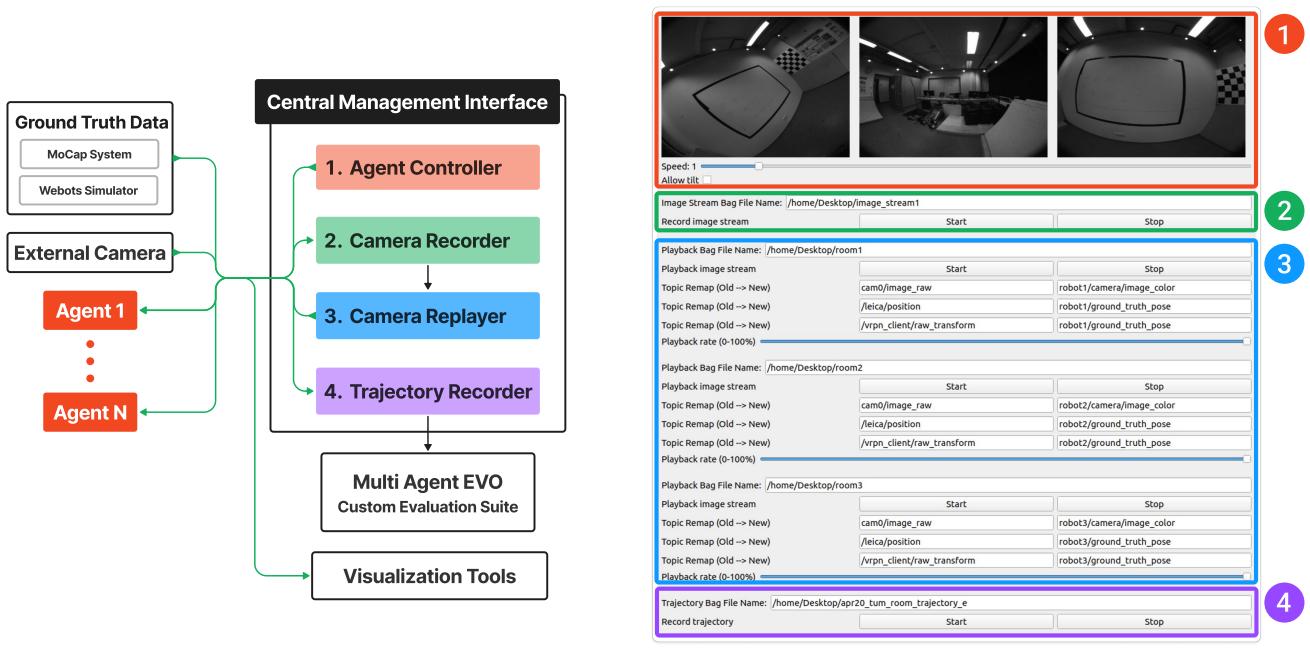


Figure 3.8: The central management interface, used for controlling agents, recording datasets, playing back datasets, and recording trajectories for later analysis.

The central management interface was built using the PyQt cross-platform user interface framework.

As a result of abstracting implementation details behind ROS topics, this central management interface is able to work seamlessly with both agents running in a simulator and agents running on real-world robots. This is true of every component of this project.

3.5 Custom Evaluation Suite – Multi-Agent EVO

While there are several mature single-agent SLAM evaluation tools, I found there to be a complete lack of evaluation tools for multi-agent SLAM systems – to the best of my knowledge no papers have published their evaluation code. Continuing with my goal to develop and publish transferrable infrastructure alongside this project, I have created an open-source multi-agent SLAM evaluation tool: *Multi Agent EVO*, based on the popular single agent SLAM evaluation tool *EVO* [20].

Besides the simple data structure and data ingestion modifications needed to allow EVO to process multi-agent SLAM data, there is some additional nuance to evaluating data from multiple agents.

Initially, all agents will be in separate reference frames until they explore an area previously seen by another agent, allowing them to merge their maps and share the same coordinate frame. We may also have cases where two independent groups of agents meet and merge maps, which requires multiple agents to simultaneously change coordinate frames. We also must note that these coordinate frames are part of the SIM(3) transformation group, which is composed of rotation, translation, and uniform scale in 3-dimensional space (scale being necessitated by the scale ambiguity of monocular visual SLAM).

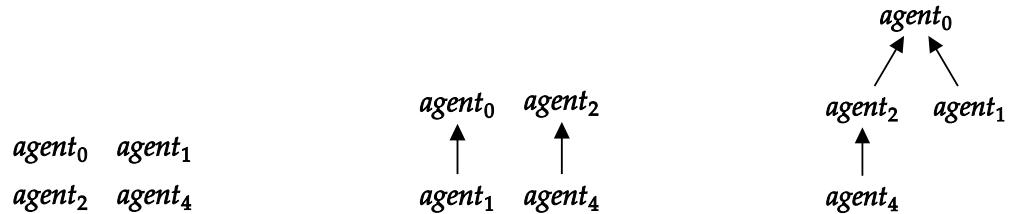
Therefore, I have created a new data format to capture these changes in coordinate frames over time within our trajectory data, which Multi-Agent EVO is able to ingest. This allows us to properly compare the multi-agent SLAM trajectories to the ground truth data, giving us insights into how long it takes for agents to successfully merge maps, the accuracy of relative pose estimation, and much more.

Once agents m and n merge, they publish the translation $T_{m \rightarrow n}$ to the `sim_transform` ROS topic. When we go to evaluate the trajectory error, Multi-Agent EVO ingests the `sim_transform` data to build a directed acyclic graph (DAG) of all merged agents, as shown in ???. This DAG can then be used to find if agents are merged with each other, and the transform between their coordinate frames. We then transform all the trajectories to be in $agent_0$'s coordinate frame for us to perform error analysis on the joint trajectory.

This method allows us to retroactively transform trajectories into $agent_0$'s coordinate from before the agents merged, allowing us to also analyze the quality of the pre-merge estimated relative trajectories.

3.6 Simulation Environment

The Webots Simulation Software Section in the Preparation Chapter explains the motivation behind using a simulator. Essentially, leveraging simulations enabled much faster iteration



- (a) All agents are initially unmerged.
- (b) $agent_0$ and $agent_1$ merge, $agent_2$ and $agent_3$ merge.
- (c) $agent_0$ and $agent_2$ merge.

Figure 3.9: Example of how coordinate frames are managed in Multi-Agent EVO. A path from $agent_m$ to $agent_n$ signifies that the agents are merged and there is an available translation from $agent_m$'s coordinate frame to $agent_n$'s.

cycles and the ability to test in a variety of environments. This section will focus on the details of integrating the simulation software into my system.

Webots is an open-source 3D robotics simulator with realistic rendering, which is essential for testing a visual SLAM system. Webots can not be built for the ARM Ubuntu VM I used for development, therefore it had to be run on MacOS, and the data was streamed to the Ubuntu VM through a websocket bridge developed by Webots.

I then developed a ROS node that exposes the Webots cameras and agent controls as ROS topics, following the abstract robot interface specifications. This allowed my SLAM system to process the camera streams and the motion controller / central management interface to control the agent's movements.

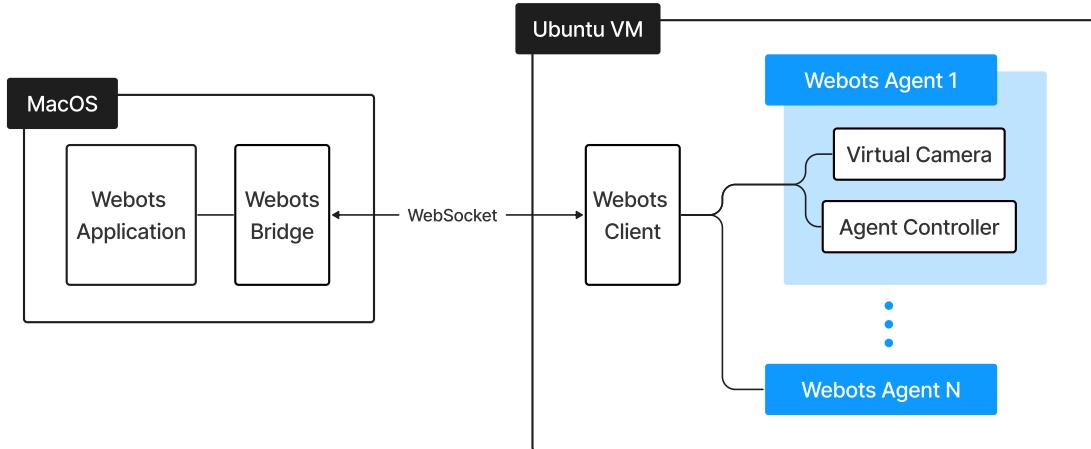


Figure 3.10: Simulation system architecture. The Webots application runs on MacOS and is exposed to the Ubuntu VM as ROS topics by the custom `Webots Client` ROS node.

3.7 Real World Implementation

After months of development within a simulator, my distributed SLAM system was able to seamlessly be deployed in a real-world multi-agent system. This was largely due to the decisions made during the preparation phase. For example, the choice to use ROS 2 as a communication middleware allows the agents to easily communicate even when deployed on different physical devices. Another key choice was to abstract the implementation of nodes away behind the communication layer, as it allowed my system to run on the physical robots without making any changes to the SLAM system or motion controller nodes.

3.7.1 Cambridge RoboMaster Platform

I chose to deploy my system on the Cambridge RoboMaster, which is an omnidirectional robot platform controlled by a NVidia Jetson Orin. The only sensor used on the RoboMaster was the integrated Raspberry Pi HQ Camera, which provides a 1920x1080 image at 15hz.

This was an obvious platform to use, as ROS drivers for the camera and wheels had already been developed and a ground-based platform allows for easier testing.

As an aside, I was an author for the paper *The Cambridge RoboMaster: An Agile Multi-Robot Research Platform*, which has been submitted to the 17th International Symposium on Distributed Autonomous Robotic Systems. My distributed SLAM system running the multi-agent collision avoidance motion controller was included as one of the experiments analyzed in the paper.

3.7.2 Deploying with Docker

My SLAM system is deployed on the RoboMasters in Docker containers. This allows my code to be compartmentalized from other projects being developed on the RoboMasters, as they are actively used by numerous researchers in the Prorok Lab. Additionally, I have set up a continuous integration process on GitHub to build a Docker container for the RoboMasters on every code push, which can then be pulled to the RoboMasters. This is a very useful feature, as building my full codebase can take upwards of 20 minutes on the NVidia Jetson Orins.

3.7.3 OptiTrack Motion Capture System

The ground truth for my real-world experiments are provided by the Prorok Lab's OptiTrack Motion Capture System, which advertises accuracies of $\leq 0.3\text{mm}$ at rates of 180hz [21]. These motion capture system publishes the real-time poses of the tracked objects to a ROS topic which can be recorded for later analysis.

3.7.4 Raspberry Pi Video Publisher

This dissertation also presents the Raspberry Pi Video Publisher, an independent piece of infrastructure which I have developed both the hardware and software for. This platform publishes real-time camera data to a ROS topic and can be tracked by the lab's motion capture system. The two primary use cases I have used this platform for are (1) dataset generation and (2) real-time AR visualization of 3D data (??).

As explained in the ?? Section, the software for this platform is entirely dockerized and a CI/CD pipeline has been implemented to automatically build and deploy the software to all Raspberry Pi video publishers when new code is pushed to the GitHub repository. This is particularly useful, as it is designed as a plug-and-play system that starts streaming video data as soon as it is turned on.

The hardware for this platform consists of a Raspberry Pi 4b, Raspberry Pi Camera v2, 3D printed frame, and motion capture markers. The 3D-printed frame securely mounts the components together, allowing them to be carried around or mounted to a tripod.

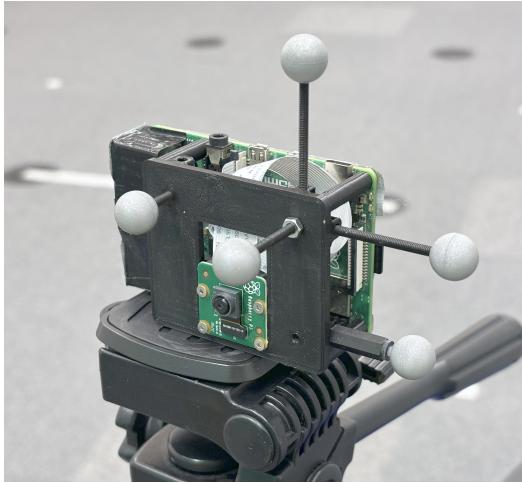


Figure 3.11: Custom-built Raspberry Pi Video Publisher mounted on a tripod.



Figure 3.12: Cambridge RoboMaster platform with NVidia Jetson Orin and Raspberry Pi HQ Camera.

3.7.5 Augmented Reality Visualization

The Raspberry Pi Video Publisher platform is tracked by the motion capture system, allowing us to project 3D visualization data onto the captured video. This can be used to visualize the SLAM system's keyframe and map point locations in the real world and to view how the SLAM system's predicted trajectory aligns with reality.

To overlay our SLAM system's data on the video, we must first align the SLAM system and motion capture systems' coordinate frames. This needs to be done on every run, as monocular SLAM systems have an arbitrary scale. Therefore, we use the Kabsch-Umeyama algorithm to align the trajectories captured by the motion capture system and SLAM system after enough data has been collected to create a successful alignment. We can then use Foxglove Studio to draw our 3D markers and project them on top of the tracked camera's video stream, a snapshot of which is displayed in ??.

To my knowledge, this system is the first of its kind to be used in such a project. Not only is it visually impressive, but it also can be used for further analysis and understanding. For example, the camera can be used to understand which features the SLAM system is tracking and how well their predicted location aligns with reality. Additionally, it can be used to analyze the SLAM system's predicted trajectory – this visualization helped me identify that my collision avoidance demo was being severely impacted by latency spikes which I proceeded to fix.

3.8 Repository Overview

The repository is split into 5 ROS packages. =====

orb_slam3_ros/.....	Core SLAM system
configs/.....	Configuration files for different cameras
include/.....	C++ headers for my SLAM system
src/.....	Source code for my SLAM system
orb_slam3_wrapper.cpp	
peer.cpp	



Figure 3.13: Features tracked by the RoboMaster on the floor overlayed over an “external perspective” handheld video from my Raspberry Pi Video Publisher. Note that the features are not being generated by the Raspberry Pi video itself, but instead the features generated by the RoboMaster are reprojected onto the Raspberry Pi video as it moves through space. This is made more obvious in the video demonstration of this feature: TODO add video.

This visualization makes it clear that my SLAM system is tracking the corners of boxes, letters on the Prorok Lab banner, and the floor vents.

```

publish_ros_viz_topics.cpp
ros_mono.cpp.....Entrypoint for the SLAM system
orb_slam3/.....Heavily modified ORB-SLAM3 codebase
include/.....C++ headers
src/
src
  orb_slam3_ros/.....Core SLAM system
    configs/.....Configuration files for different cameras
    include/.....C++ headers for my SLAM system
    src/.....Source code for my SLAM system
      orb_slam3_wrapper.cpp
      peer.cpp
      publish_ros_viz_topics.cpp
      ros_mono.cpp.....Entrypoint for the SLAM system
  orb_slam3/.....Heavily modified ORB-SLAM3 codebase
    include/.....C++ headers
    src/
controller/.....Central management interface package
  controller/
    my_node.py .....Source code for central management interface
evaluation/.....Evaluation Jupyter Notebooks
  evaluation.ipynb.....Primary evaluation notebook
  mocap_calibrations.json.....Coordinate frame offsets from an objects motion
    capture to camera coordinate frame
  motion_capture_post_processing.ipynb .... Notebook to process and evaluate
    motion capture data from real-world experiments
interfaces/.....Definitions for custom ROS message types

```

```
└── msg/ ..... Custom message definitions
    └── srv/ ..... Custom service definitions
    └── CMakeLists.txt ..... Build configuration for the package
└── motion_controller/ ..... Motion controller
└── webots_sim/ ..... Simulation package
    └── launch/
        └── robot_launch.py/ ..... Simulation bridge configuration
    └── webots_sim/
        └── robot_driver/ ..... Webots to ROS bridge
    └── worlds/ ..... Simulation environments
        └── city.wbt
        └── complete_apartment.wbt
    └── local_simulation_server.py ..... Server-side Webots bridge script
    └── tools/ ..... Misc. scripts
└── .github/workflows/config.yml ..... CI/CD configuration
└── Dockerfile ..... Main dockerfile for the project
└── nvidia_jetson.Dockerfile ..... Dockerfile for the NVidia Jetson
```

Chapter 4

Evaluation

4.1 Review of Success Criteria

My project has met all success criteria as outlined below:

- 1a. **Multiple agents will be able to localize themselves within a world using purely visual data.**
My system is the first decentralized SLAM system capable of operating using only monocular camera data. This removes the need for large and expensive stereo camera, LiDAR or RGBD sensors.
 - 1b. **Agents will be capable of communicating with each other to build a shared understanding of the world.**
Agents use ROS to perform decentralized and reliable communication with eachother, and are able to merge maps and share key frames to build a shared world.
 - 1c. **Agents will be able to act independently, failing gracefully if it loses communication with its peers.**
Agents fall back to performing single-agent visual SLAM when communication with their peers is degraded or lost. Once communication is regained, the agents share their unsent map data.
2. **Evaluate the capabilities of the system compared to a comparable single-agent system.**
This is done in the ?? Section. I go beyond the original success criteria by also comparing my system to comparable multi-agent systems, demonstrating my system's superior performance.

After discussions with my supervisor, we decided to not pursue my original project extensions of optimizing data transfer rates and adding additional sensors inputs to the system. We instead chose to focus on deploying the SLAM system on physical robots and building infrastructure around the system to improve usability and benefit the wider open source community. Deploying my system on real robots was a considerable amount of work, however I believe it was important as it provides

4.2 Benchmarking

This section will benchmark the performance of my system when run on industry standard visual SLAM datasets. All evaluations are run using only monocular camera data.

The Central Management Interface is used to stream the dataset to the agents and my library *Multi Agent EVO* is used to provide the Absolute Trajectory Error (ATE).

4.2.1 EuRoC Machine Hall

The EuRoC Machine Hall dataset [13] is one of the most widely used visual SLAM datasets, providing a 752x480 20fps video feed and millimeter level ground truth data at 20hz. The camera rig is attached to a Micro Aerial Vehicle (MAV) which flies through a machine room approximately 15x15 meters in size. To simulate a multi-agent dataset, we run the Machine Hall 01-03 scenarios in parallel on three agents.

?? presents the RMS absolute trajectory error and total system data transfer of my distributed system running this dataset. The median RMS ATE is 5.9cm over the 279 meter total trajectory

length, demonstrating my system's very impressive accuracy. There ATEs and data transfer rates have a 1.4cm and 0.11 MB/s spread around the median respectively across 5 trials, demonstrating the repeatability and robustness of my system.

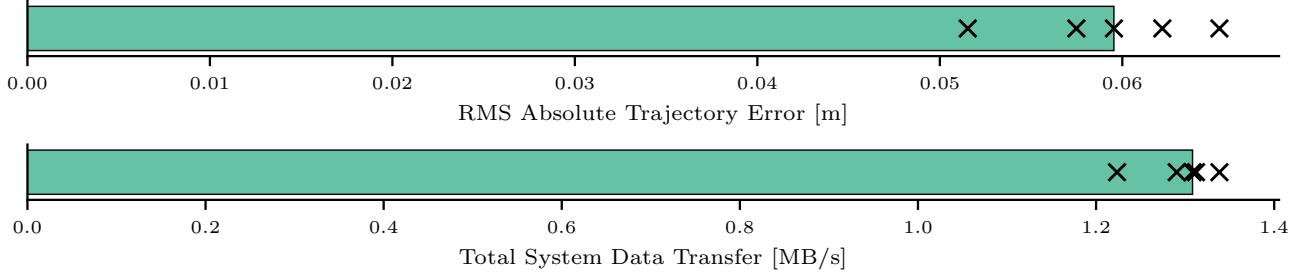


Figure 4.1: Plot the RMS ATE and Total Data Transfer rate of running the EuRoC Machine Hall 01-03 dataset 5 times on my system.

To further analyze the characteristics of my SLAM system, we focus on an individual trial. ?? displays the full trajectory of the three agents compared to the ground truth, demonstrating my systems high global accuracy and relative positioning. ?? plots the ATE as the trial progresses. It is clear that my system is performing SLAM as opposed to simple visual odometry as the ATE returns back to the baseline at the end of the trial when the agents return back to their starting position.

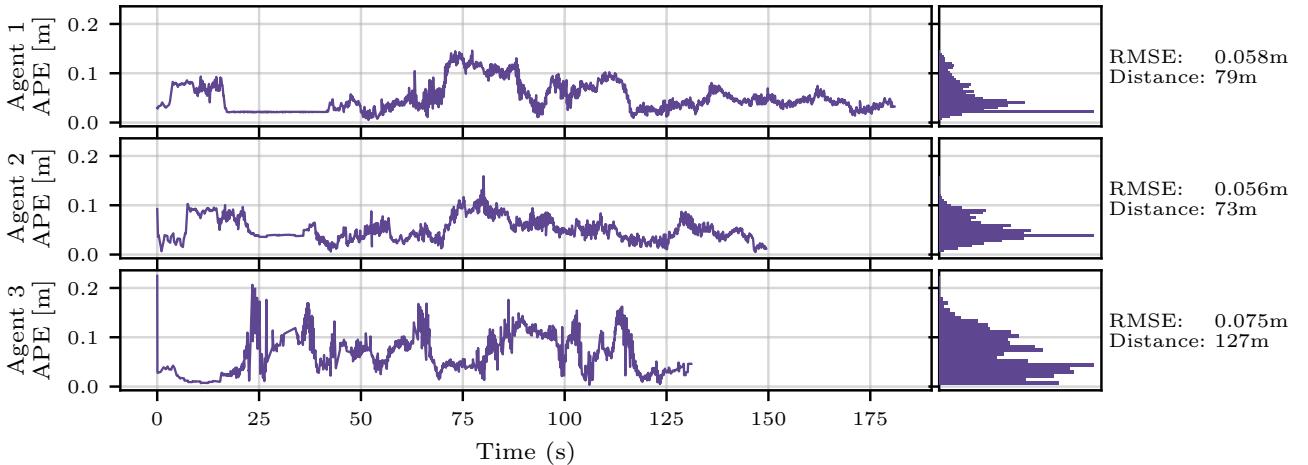


Figure 4.2: Plot of my system's absolute trajectory error (ATE) with respect to the ground truth when running the EuRoC Machine Hall 01-03 scenarios in parallel on three agents.

RMSE represents the root mean square of the ATE.

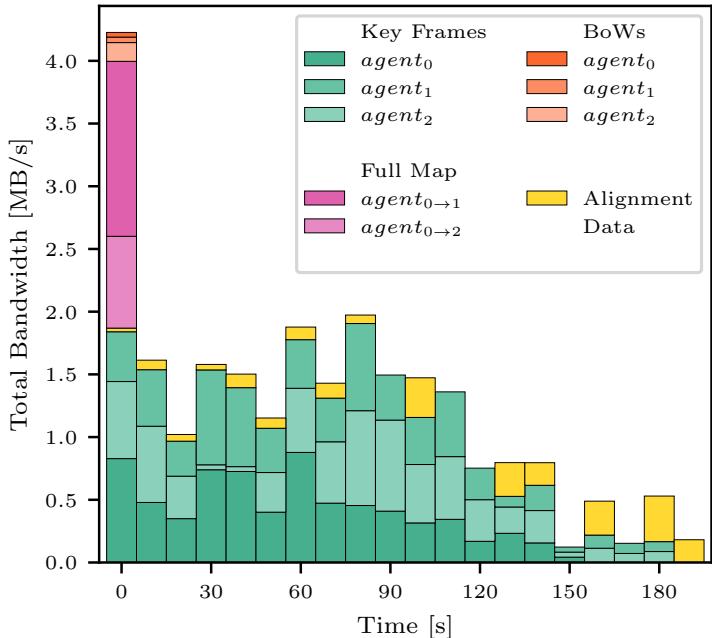
We now analyze the network usage presented in ???. Initially, the agents send bag of word information before quickly detecting a merge opportunity. Agent 1 proceeds to send its full map to agent 2, which can be seen in the large initial spike in network bandwidth. The agents successfully merge, and begin exchanging key frames. The rate of key frame data being sent rises and falls depending on how much new area the agent is exploring.

Along with sending key frames, the agents sporadically send map points to refine their map alignment. This occurs less frequently the longer system runs due to the additive increase multiplicative decrease method used to schedule map alignments, described in the ?? Section. However, the size of the messages also grows over time due to the larger number of tracked map points.

The data exchanged between agents largely consists of new key frames, and further work should be dedicated to optimizing the serialized representation of key frames.

4.2.2 TUM-VI Rooms

The TUM visual-intertial dataset [14] consists of handheld fisheye 512x512 video with ground truth data. As before, we use only monocular visual data and combine the room1-3 sessions to



(a) Total system data over time

	KB	Avg. KB/s
Key Frames	$agent_0$	69,971
	$agent_1$	63,908
	$agent_2$	65,164
BoWs	$agent_0$	371
	$agent_1$	437
	$agent_2$	1,496
Full Map	$agent_{0\rightarrow 1}$	13,953
	$agent_{0\rightarrow 2}$	7,319
Alignment Data		22,560
Total Data		245,218
		1,233.1

(b) Total system data by message type

	Sent		Received	
	KB	Avg. KB/s	KB	Avg. KB/s
$agent_0$	114,585	576.2	131,005	658.8
$agent_1$	64,345	323.6	173,554	872.8
$agent_2$	66,660	335.2	164,606	827.7

(c) Data by agent

Figure 4.3: Bandwidth used by the EuRoC Machine Hall 01-03 scenarios running on my SLAM system.

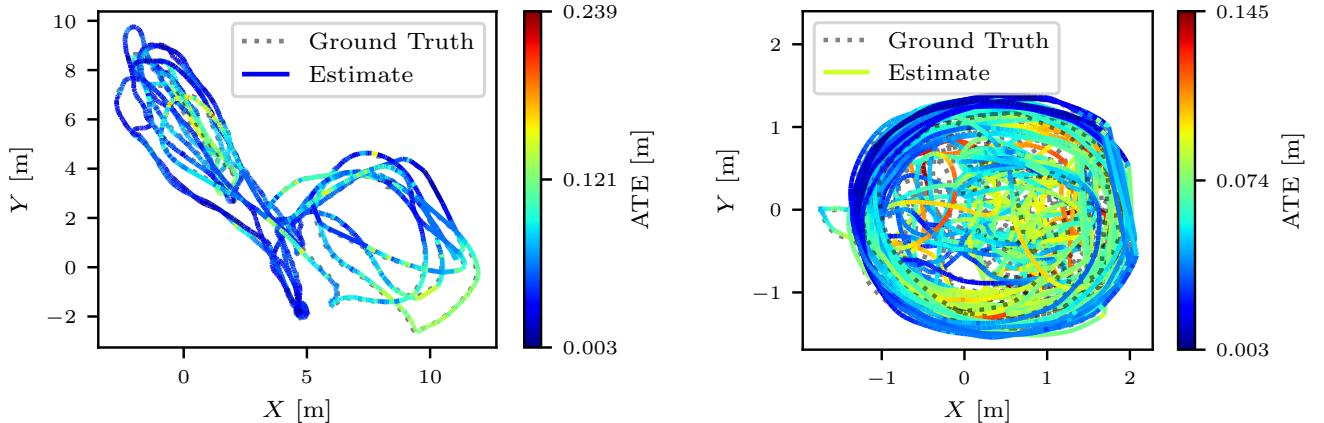


Figure 4.4: EuRoC Machine Hall 01-03 estimated trajectory and ground truth.

Figure 4.5: TUM-VI Rooms 01-03 estimated trajectory and ground truth.

simulate a multi-agent dataset. The "room" environment is used for this evaluation, which is a 3x3 meter motion capture lab with plain flat walls with some posters hung up. There is less texture in this environment than the machine hall, making visual-only SLAM more difficult. As seen in the full trajectory estimate given in ??, parts of the room are revisited dozens of times by different agents, allowing us to evaluate our system's ability to relocalize agents within previously mapped environments.

?? shows that the RMS ATE is very tightly clustered around the median of 6.95cm, with one outlier caused by an agent in that trial having a slightly unoptimal map merge. The tight clustering is most likely due to the small environment with areas being revisited many times, allowing the shared map to converge on a very similar solution each time. The lower median data transfer rate of 0.84 MB/s is also due to the small environment, resulting in the agents having to share less information.

Once again, we focus on an individual trial to further evaluate my system. ?? shows that there is no long term error build up, demonstrating that my system is successfully localizing agents within the shared map and performing long-term map point association.

?? presents the data transfer breakdown of a single trial, and yields similar conclusions to that of the EuRoC Machine Hall dataset. The only difference to note is the smaller key frame and

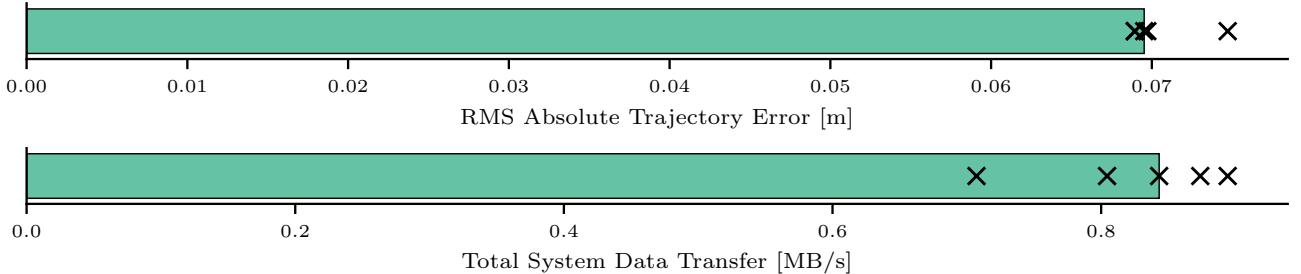


Figure 4.6: Plot the RMS ATE and Total Data Transfer rate of running the EuRoC Machine Hall 01-03 dataset 5 times on my system.

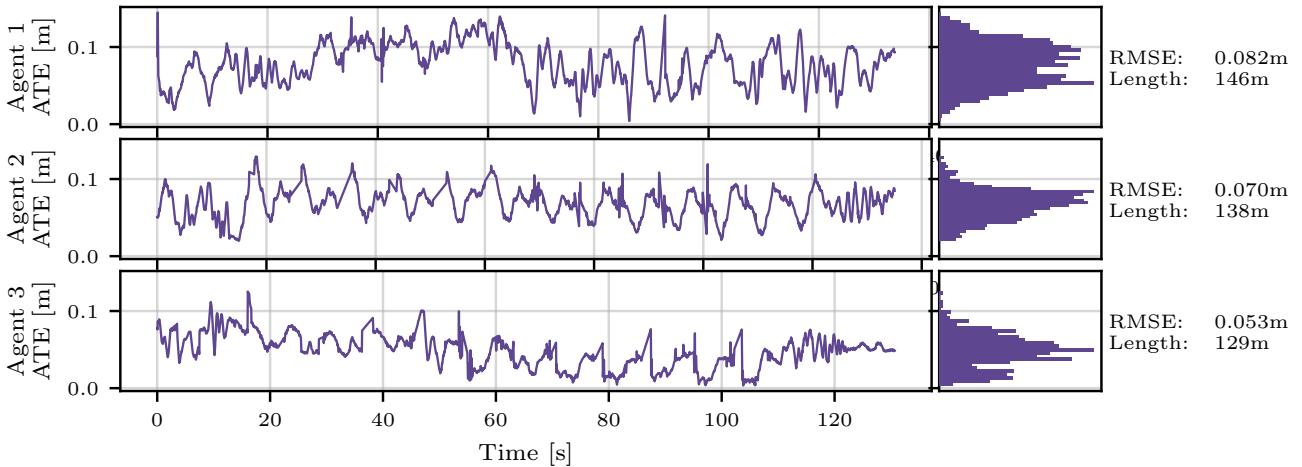


Figure 4.7: Plot of my system’s average trajectory error (ATE) with respect to the ground truth when running the EuRoC Machine Hall 01-03 scenarios in parallel on three agents. The average RMSE of the multi-agent system is 0.062m over the 279m total trajectory length. RMSE represents the root mean square of the ATE.

alignemnt data transfer rate due to the smaller environment.

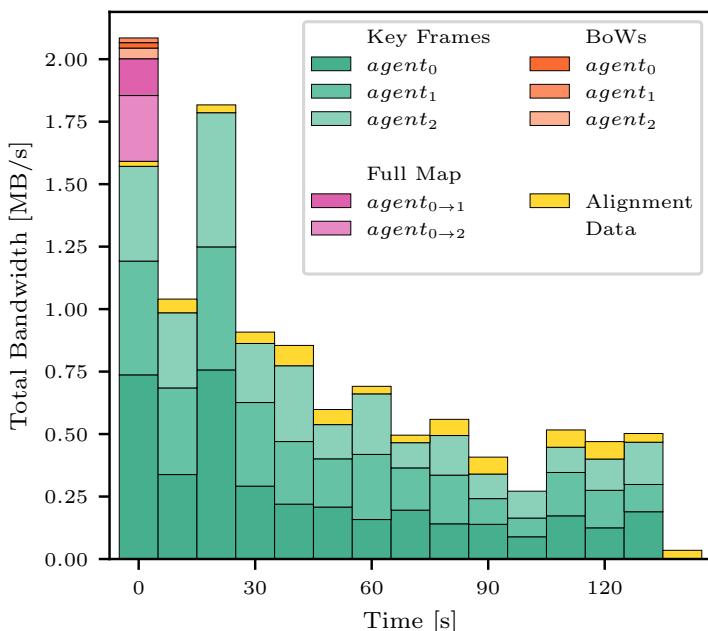
4.3 Comparison to Related Work

As discussed in the ?? Section, my system is the first decentralized monocular vision SLAM system available. This makes direct comparisons with other multi-agent SLAM systems difficult, as they rely on more accurate but bulky sensors such as stereo cameras and LiDAR. However, this section still attempts to compare my system to the latest research in the field to give context to its performance relative to other state of the art systems.

We are only able to compare results using the EuRoC dataset as it is the only public dataset evaluated by CCM-SLAM. Ideally, I would run more datasets on CCM-SLAM system, however I encountered many issues when trying to build the codebase published alongside their paper. This reinforces the well known reproducibility issues within the field of visual SLAM [1]. **My SLAM system is not specifically tweaked to perform well in the EuRoC dataset and we get similarly low RMS ATE values in both the TUM Rooms dataset and real world evaluations.**

4.3.1 CCM-SLAM

Centralized Collaborative Monocular SLAM (CCM-SLAM) (2019) from the ETH Zurich Vision for Robotics Lab [3] is the most comparable multi-agent SLAM system in recent literature, and is well cited in the field. Their approach also uses purely monocular vision with ORB-SLAM to the front-end tracking and local mapping stages of the SLAM pipeline, with a custom backend



(a) Total system data over time

		KB	Avg. KB/s
Key Frames	agent ₀	37,599	264.9
	agent ₁	33,066	233.0
	agent ₂	29,963	211.1
BoWs	agent ₀	217	1.5
	agent ₁	188	1.3
	agent ₂	426	3.0
Full Map	agent ₀ -> ₁	1,472	10.4
	agent ₀ -> ₂	2,631	18.5
Alignment Data		6,947	49.0
Total Data		112,511	792.8

(b) Total system data by message type

	Sent		Received	
	KB	Avg. KB/s	KB	Avg. KB/s
agent ₀	49,083	345.9	63,644	448.5
agent ₁	33,254	234.3	76,624	539.9
agent ₂	30,389	214.1	80,649	568.3

(c) Data by agent

Figure 4.8: Bandwidth used by the TUM-VI Rooms 01-03 scenarios running on my SLAM system.

to integrate data from multiple agents into the shared map. To my knowledge, it is the most recent monocular vision capable multi-agent SLAM system.

The results of CCM-SLAM and my system running the EuRoC Machine Hall 01-03 dataset are presented in ???. It is important to note that CCM-SLAM is a centralized system, significantly simplifying their multi-agent SLAM problem compared to my distributed system. Nevertheless, my system is able to outperform CCM-SLAM in terms of RMS ATE, demonstrating its competitiveness. My system's total data transferred is 32% higher than CCM-SLAM, however this could easily be reduced as I have made no attempt to optimize the data transfer efficiency of my system.

4.3.2 VINS-Mono Multisession SLAM

VINS-Mono (2018) [22] is a popular open source single-agent monocular vision SLAM system. While it is a multi-agent system, it has multisession capabilities. This allows multiple datasets to be played consecutively, with each session building upon the map built by the previous sessions (eg. session 2 is initialized in the map generated after running session 1). This is an easier problem than multi-agent SLAM, where the sessions are run in parallel and the agents have to share their maps in real time. As presented in ??, my system still outperforms VINS-Mono multisession.

	My system	CCM-SLAM ¹	VINS-Mono ²
RMS ATE [m] ³	0.059	0.077	0.074

Figure 4.9: Comparison of my SLAM system to comparable state of the art multi-agent systems running the EuRoC Machine Hall 01-03 dataset with only monocular images.

¹CCM-SLAM is a centralized system, as opposed to my decentralized system.

²VINS-Mono is a single-agent SLAM system run in multisession mode.

³RMS ATE is taken as the median of 5 trials. Results of external systems are taken from [3].

4.3.3 Comparison to Single-Agent SLAM Systems

Along with providing relative positioning, we would hypothesise a multi-agent SLAM system to have higher accuracy than a comparable single-agent system. However, the reality is far more complex than this simple assumption. ?? presents my multi-agent system's errors compared to ORB-SLAM3 running the datasets individually. ORB-SLAM3 is used to perform the tracking and local mapping in my multi-agent system, and is widely regarded as the most accurate single-agent SLAM system currently available so there is no surprise that it performs very well. An observation is that some dataset sessions have only a marginal improvement in error over the single-agent system, which I hypothesize is the result of the varying ability among agents to utilize the shared map. For example, the TUM-VI Room dataset has very similar performance in both the single-agent and multi-agent systems since the environment is very small and areas of the map are revisited dozens of times in one session. This reduces the benefit of a multi-agent system's as a single-agent system already observes more than enough data to build an accurate map of the world, making the extra data provided by the additional agents in a multi-agent system redundant.

TODO talk about euroc dataset

	My system ¹	ORB-SLAM3 ²
EuRoC MH 01	0.051	0.049
EuRoC MH 02	0.048	0.099
EuRoC MH 03	0.058	0.062
TUM-VI Room 1	0.072	0.071
TUM-VI Room 2	0.048	0.050
TUM-VI Room 3	0.041	0.042

Figure 4.10: Comparison of individual agent errors from my multi-agent SLAM system and the single-agent ORB-SLAM system. All results are the median of 5 runs.

¹Trajectories are aligned with the ground truth on a per-agent basis so we can compare each individual agent's performance in isolation.

²Results are generated by running ORB-SLAM3 on my device with its default settings for the EuRoC dataset.

On a broader note, many researchers believe single-agent SLAM to be a solved problem. This is reflected by the results seen here, where single-agent systems are able to give incredibly low trajectory errors that even multi-agent systems with far more data struggle to improve upon. This is not something specific to my system – many other multi-agent systems do not have significantly higher accuracies than single-agent systems.

Therefore, I believe that the primary benefits of a multi-agent system are its ability to provide relative positioning for path planning and collision avoidance capabilities, and to build a shared map of the environment which is useful in applications such as search and rescue or cave mapping.

?? visualizes the collaborative shared map built by my system compared to the individual maps from the single-agent ORB-SLAM3. There is clear deep integration between the different agents' map data in my collaborative map, demonstrating that the agents are truly collaborating and welding their maps together. The multi-agent system is also able to build a full map of the environment, showing the advantage of collaborative SLAM systems.

4.4 Real World Experiments

Deploying my system on physical robots demonstrates its ability to be run in real time within the computational, bandwidth and latency constraints of real world systems. Furthermore, it demonstrates the robustness of my development framework which allowed seamless migration from local testing using simulations to a real distributed system using live camera feeds with no changes to my code base.

The details of the real world setup are given in the ?? Section. In summary, the Cambridge RoboMasters platform was used

4.4.1 Multi-Agent Collision Avoidance

In this experiment, we showcase the NMPC collision avoidance motion controller working in conjunction with the SLAM system to avoid collisions with both static and dynamic obstacles. Real time relative position data from the SLAM system is fed to the NMPC collision avoidance motion controller which controls the robot's velocity accordingly. The SLAM system is running locally on each Cambridge RoboMaster, with communication facilitated by a router in the lab. ?? tests the system in an intersection environment, where two robots (traveling along the horizontal and vertical axis) would normally collide. The shared map generated by the two agents allows them to localize each other even when their views do not overlap and they can not see the other agent, showcasing the versatility and wide ranging use cases of my distributed SLAM system. Additionally, this demonstrate the real time capabilities of my SLAM system, allowing the robots to react fast enough to avoid collisions in dynamic environments.

Out of the four consecutive trials run in this environment, there were zero collisions between the two agents, and ?? shows that the distance between agents never went below the collision threshold of 0.55 meters.

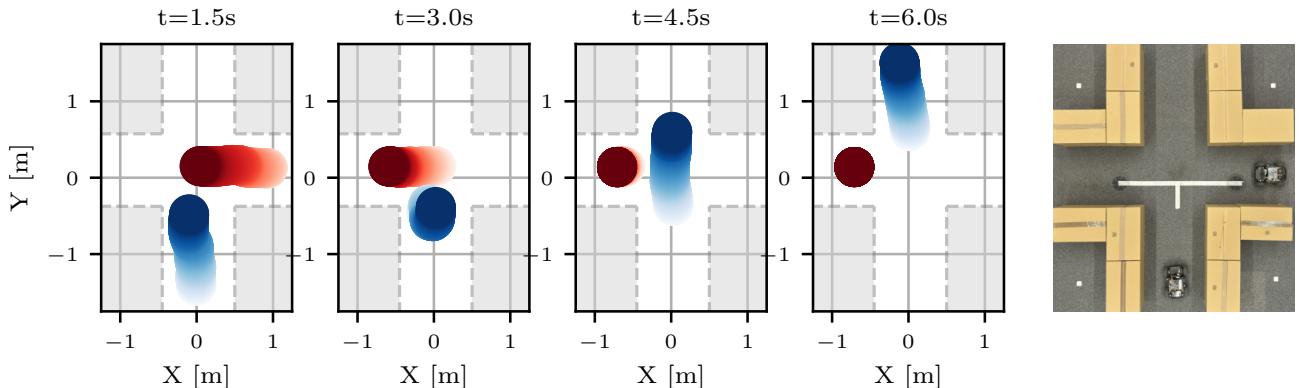


Figure 4.11: Demonstration of multi-agent collision avoidance, facilitated by my distributed SLAM system running locally on the Cambridge RoboMasters. Two robots are set 90° to each other in an intersection environment, with no direct view of the other robot and little visual overlap (right). The agent travelling along the Y axis is given a goal pose on the other side of the intersection, and successfully avoids a collision when the agent travelling along the X axis is pushed through the intersection. The trajectories generated by the SLAM system are presented on the left charts.

My projected included the development of an augmented reality visualization system to view my SLAM system's data overlayed on top of a video captured by an external camera. ?? shows a snapshot of this visualization, with the agents' map points and predicted locations overlayed on top of a video.

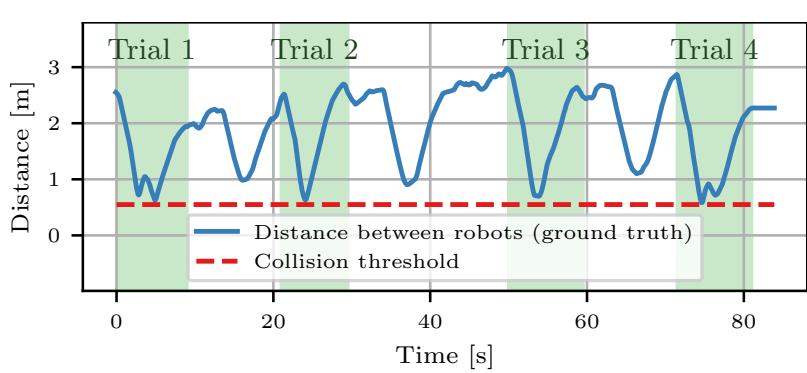


Figure 4.12: Plot of ground truth distance between the two robots throughout all four collision avoidance trials conducted in the intersection environment. The dips between trials are the robots' positions being reset. ?? visualizes Trial 4 in more detail.

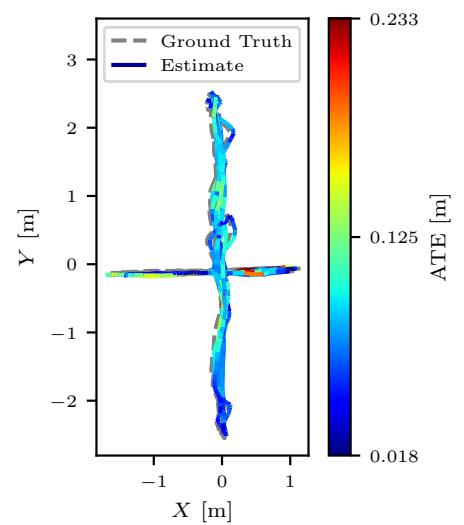


Figure 4.13: Collision avoidance estimated trajectory and ground truth. The RMS ATE is 0.074 meters.

Chapter 5

Conclusions

5.1 Future Work

Visual SLAM is a mature field, with improvements being incremental as opposed to ground breaking.

5.2 Lessons Learned

The most important lesson learnt from this project is that cutting edge research does not equate to well written or documented code. I committed to using the single agent ORB-SLAM3 system as the foundation for my project, however I quickly discovered that it was extremely hard to build upon their codebase. Large chunks of code were commented out without explanation, everything was defined as an instance variable making dataflow hard to decypher, and many function were named `localMapping()`, `localMapping2()`, `localMapping3()`, with different parts of the code arbitrarily choosing any one of the functions to use. In addition, there was simply a large amount of inherit complexity within the codebase as it is the most advanced single-agent SLAM system and is multithreaded.

ORB-SLAM also did not compile out-of-the-box, requiring me to make modifications to both the makefiles and codebase. Due to the above complexities as well as being my first time using C++, it took almost month to get ORB-SLAM running and many more before I began making good progress on the distributed aspect of the project – far longer than I had expected. In summary, I should not have assumed that research code would be easy to compile and build upon, even if it was one of the most well cited and performant systems in the field.

5.3 Reflection

Four years ago when I was applying to Cambridge, I wrote in my personal statement that I was fascinated by computer vision – specifically visual SLAM. At the time I didn’t understand the topic at all, I just thought it looked cool! I find it rather fitting that I now conclude my degree by developing a distributed visual SLAM system that performs better than comparable state of the art systems – something I could have only dreamt of when writing my personal statement all those years ago.

Overall, I am very satisfied with the results achieved by my system. I knew from the beginning that I did not want to spend a year creating something worse than what was already out there, however that is not an easy task in such a well researched field within computer science. Importantly, I chose to tackle a moderately niche yet well motivated area within the field, in this case a monocular video multi-agent system.

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Appendix A

⟨APPENDIX A NAME⟩

Appendix A...

Appendix B

⟨APPENDIX B NAME⟩

Appendix B...

Appendix C

Proposal

Proposal...