DigiPen Institute of Technology Singapore

IBF- Day 6 Exericise Vector Calculus

Instructor: Yilin Wu

Jan 26 2020

This exercise contains 7 pages (including this cover page) and 10 questions. Total of points is 100. Good luck and Happy reading work!

Distribution of Marks

| Question: | 1 | 2 | 3 | 4 | 5 | 6 |
|-----------|----|----|----|----|----|-------|
| Points: | 10 | 10 | 10 | 10 | 10 | 10 |
| Score: | | | | | | |
| Question: | 7 | 8 | 9 | 10 | | Total |
| Points: | 10 | 10 | 10 | 10 | | 100 |
| Score: | | | | | | |

1. (10 points) Find the Taylor polynomials of degree **Two** for

$$f(x) = 1 + x + x^2$$
 at $a = 1$

2. (10 points) Find the Taylor polynomial of degree Four for

$$f(x) = \cos(2x)$$
 at $a = \pi$

3. (10 points) Determine the 1st and 2nd degree Taylor polynomial approximations for the following function of x and y near the given point

$$f(x,y) = x\sqrt{y}$$
 near $(1,4)$

4. (10 points) Find all the 1st order partial derivatives

$$f(x, y, z) = 4x^{3}y^{2} - e^{z}y^{4} + \frac{z^{3}}{x^{2}} + 4y - x^{16}$$

5. (10 points) Find the Jacobian Matrix and the Hessian Matrix of

$$f(u,v) = u^2 \sin(u+v^3) - \sec(4u)\arctan(2v)$$

6. (10 points) Find the linearization of $f(x) = \sqrt{x+10}$ and at a=1, use it to approximate the value $\sqrt{10.04}$ and $\sqrt{9.97}$

7. (10 points) Find the linearization of $f(x,y) = x^2y$ at the point (3,8).

8. (10 points) Find the derivative of

$$\begin{bmatrix} x_1 x_2 & x_3 & x_2 + x_3 \\ x_1 & x_2 & x_3 \\ x_1 + x_3 & x_1 & x_1^2 x_2 \end{bmatrix}$$

Respect to \mathbf{x}

9. (10 points) Find the partial derivative

$$R(x,y) = \frac{x^2}{y^2 + 1} - \frac{y^2}{x^2 + y}$$

10. (10 points) A company is selling cell phones and the monthly demand x is the following function of the price \$p:

$$x = f(p) := 300000 - 400p + 0.2p^2$$

The current price is \$300. How much will demand drop if the price is increased by 10 cents?

This page is intentionally left blank to accommodate work that wouldn't fit elsewhere and/or scratch work.