

$$Q24) 2) \rightarrow \neg [\exists x, \exists y, \forall z, ((x \neq y) \wedge (C(x, z) \leftrightarrow C(y, z)))]$$

$$\neg \exists y C(x, z) \rightarrow C(y, z) = \neg \exists y (C(y, z) \wedge \neg C(x, z)) = \neg \exists y (C(y, z) \wedge \neg C(x, z))$$

$$C(y, z) \rightarrow C(x, z) = \neg C(x, z) \vee C(y, z) = P_2(z)$$

~~LP: P(z)~~

$$\neg [\exists x, \exists y, \forall z, (x \neq y) \wedge P_1(z) \wedge P_2(z)]$$

$$= \forall x, \neg (\exists y, \forall z, (x \neq y) \wedge P_1(z) \wedge P_2(z))$$

$$= \forall x, \forall y, \exists z, \neg ((x \neq y) \wedge P_1(z) \wedge P_2(z))$$

$$= \forall x, \forall y, \exists z, (x = y) \vee \neg P_1(z) \vee \neg P_2(z)$$

$$= \forall x, \forall y, \exists z, (x = y) \vee (C(y, z) \wedge \neg C(x, z)) \vee (C(x, z) \wedge \neg C(y, z))$$

don't forget this!

LP: Can make $[C(x, z) \wedge \neg C(y, z)] \vee [C(y, z) \wedge \neg C(x, z)]$

$$= [C(x, z) \vee C(y, z) \wedge (\neg C(x, z) \vee \neg C(y, z))]$$

$$Q25) \forall x \in D, P(x) \rightarrow Q(x) = \forall x \in D, \neg Q(x) \vee P(x)$$

$$LP: = \forall x \in D, \neg (\neg \neg Q(x) \wedge \neg P(x)) = \forall x \in D, \neg (Q(x) \wedge \neg P(x)) \quad \times$$

TA: Trick is to use $Q(x) = \neg \neg Q(x)$, then convert back to implication.

$$TA: \forall x \in D, \neg Q(x) \vee P(x) \quad \times$$

LP: $A \rightarrow B = \neg A \vee B$ NOT $\neg B \vee A$ because $\neg B \rightarrow \neg A$!

$$CTA: \forall x \in D, P(x) \rightarrow Q(x) = \forall x \in D, \neg P(x) \vee Q(x)$$

$$= \forall x \in D, Q(x) \vee \neg P(x) = \forall x \in D, \neg \neg Q(x) \vee \neg P(x)$$

$$= \forall x \in D, \neg Q(x) \rightarrow \neg P(x) \quad \checkmark$$

$$Q26) \neg (\forall x, P(x) \rightarrow Q(x)) = \exists x, \neg (P(x) \rightarrow Q(x)) = \exists x, \neg (\neg P(x) \vee Q(x))$$

$$= \exists x, \neg \neg P(x) \wedge \neg Q(x) = \exists x, P(x) \wedge \neg Q(x) \quad \checkmark$$

Q27) False. \times TA: 2 is a prime and $2 = 2 \times 1$.

$$Q28) S = \{ \text{students} \} \quad C = \{ \text{courses} \}$$

$$\forall s \in S \quad \times$$

TA: $D = \{ \text{SCE students} \}$. $P(x) = "x \text{ studies DM}"$.

$$\forall x \in D, P(x)$$

$$\forall x \in D, P(x); \text{Jackson} \in D; \therefore P(\text{Jackson}) \quad \checkmark$$