

Lab 08

Jyosna Philip

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Aim:

To find the difference between the theoretical and practical rendition of goodness of fit test.

Qs. Suppose you are analysing the distribution of the preferred programming languages among a group of 500 data science students. You have collected data and observed the following distribution: Python: 300 R: 120 Java: 40 Other: 40 Now the theoretical distribution based on your expectation is as follows(in proportions): Python: 0.56(56%) R: 0.2(20%) Java: 0.1(10%) Other: 0.14(14%)

1. Evaluate whether the observed values of preferred programming languages align with the expectation?
2. Find the expected values and the residuals?

```
observed=c(300,120,40,40)
prob=c(0.56,0.2,0.1,0.14)
m=chisq.test(observed,p=prob)
m

##
##  Chi-squared test for given probabilities
##
## data:  observed
## X-squared = 20.286, df = 3, p-value = 0.0001481
```

We get chi-squared value as 20.286 and p-value 0.00014. Since pvalue is less than 0.05 we reject H0 and conclude that the observation doesn't align with the expected values.

```
m$expected
## [1] 280 100  50  70
```

280,100,50 and 70 are the expected values of Python,R,Java and other languages respectively.

```
m$residuals
## [1]  1.195229  2.000000 -1.414214 -3.585686
```

1.19, 2,-1.4,-3.58 are the residuals associated with Python,R,Java and other languages respectively.

Conclusion: $p\text{-value} < 0.05$, Hence we conclude that the preference doesn't align with the expectations.

Theoretical test:

• Lab qs : Goodness of fit:

Language	Observed	Expected	$(O-E)^2$	$(O-E)^2/E$
Python	300	280	400	1.43
R	120	100	400	4
Java	40	50	100	2
Other	40	70	900	12.86

$$\sum \frac{(O-E)^2}{E} = 20.29$$

$$\chi^2_{\text{tab}} < \chi^2_{\text{calculated}}$$

The chi-square value aligns with that obtained practically.

#Notebook Questions Q1. test the hypothesis that the no of parts in demand doesn't depend on the type of day H_0 : no of parts in demand doesn't depend on the type of day H_1 : no of parts in demand depend on the type of day

```

observed=c(1124,1125,1110,1120,1126,1115)
prob=c(1/6,1/6,1/6,1/6,1/6,1/6)
chisq.test(observed,p=prob)

##
## Chi-squared test for given probabilities
##
## data: observed
## X-squared = 0.18036, df = 5, p-value = 0.9993

```

We get chi-squared value is 0.18 and p-value as 0.99. Conclusion: since $p\text{-value} > 0.05$ we conclude that there is no dependency of parts on demand and type of day.

Q.3. In a sampling study the following info was obtained.

Days	Mon	Tue	Wed	Thue	Fri	Sat
No. of parts demanded	1124	1125	1110	1120	1126	1115

$$\chi^2_{(5)} (0.05) = 11.07$$

Test the hypothesis that no. of parts demanded doesn't depend on day

$$\chi^2_{(6)} = 12.59$$

$$\chi^2_{(7)} = 14.07$$

Ans. Here, we don't know the distribution. \therefore We take mean as expected frequency of each of them.

$$E = 1120$$

O	E	$(O-E)^2$	$(O-E)/E$
1124	1120	16	0.014
1125	1120	25	0.02
1110	1120	100	0.089
1120	1120	0	0
1126	1120	36	0.032
1115	1120	25	0.022

$$= 0.177$$

$$\chi^2_{cal} < \chi^2_{tab} = 11.07$$

H_0 is accepted. Demand is independent of day of week

The chi-square value aligns with that obtained practically.

CONCLUSION

Goodness of fit test was carried out for the given questions both practically and theoretically and the results were compared.