

Data matrix

$$X \in \mathbb{R}^{N \times d}$$

N # observations

d # features

$$X = \begin{bmatrix} x_1 & x_2 & \dots & x_{1d} & \dots & x_{Nd} \\ \left[\begin{array}{c} x_{11} \\ x_{21} \\ \vdots \\ x_{N1} \end{array} \right] & \left[\begin{array}{c} x_{12} \\ x_{22} \\ \vdots \\ x_{N2} \end{array} \right] & \dots & \vdots & \dots & \left[\begin{array}{c} x_{1d} \\ \vdots \\ x_{Nd} \end{array} \right] \end{bmatrix}$$

Features

$$\underline{x}_1 = \lambda x_2 + \mu$$

$$y = \beta_0 + \beta_1 x_1 + \dots + \beta_d x_d + \epsilon$$

$$\boxed{\beta^* = \left[\begin{array}{c|c} x^T & 1 \end{array} \right]^{-1} x^T y}$$

$(d \times n) \quad (n \times 1)$

$d \times 1$

Colinearity

$$\frac{2}{0} \rightarrow \frac{2}{0.001} = 2000$$

Original - raw

	A	B	C
0	NaN	11	NaN
1	1	5	5
2	2	NaN	10
3	3	NaN	11
4	NaN	NaN	NaN
5	NaN	8	8

$$\frac{4}{0.0001} = 4000$$

row - bfill

Original - raw

	A	B	C
0	1 NaN	11 ✓	NaN 5
1	1 ✓	5 ✓	5 ✓
2	2 ✓	NaN 8	10
3	3	NaN 8	11
4	NaN	NaN 8	NaN 8
5	NaN	8	8

col - bfill

Original - raw

	A	B	C
0	11 NaN	11	NaN ✓
1	1	5	5
2	2	10	10
3	3	11	11
4	NaN ✓	NaN ✓	NaN ✓
5	8	8	8

row - fill

col - Pfill

Original - raw

	A	B	C
0	Non ✓	11	Non ✓
1	1	5	5
2	2	Non 5	10
3	3	Non 5	11
4	3 Non	Non 5	Non 11
5	3 Non	8	8

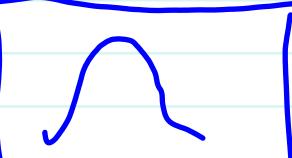
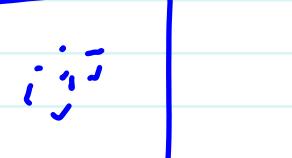
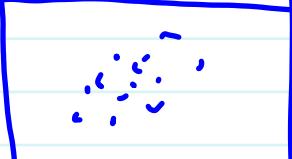
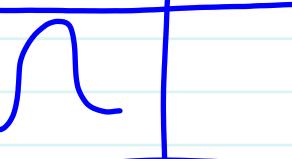
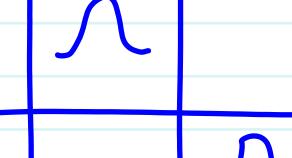
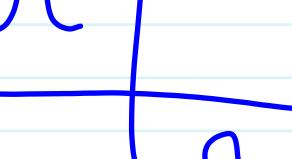
Fracture 2

Feature 1

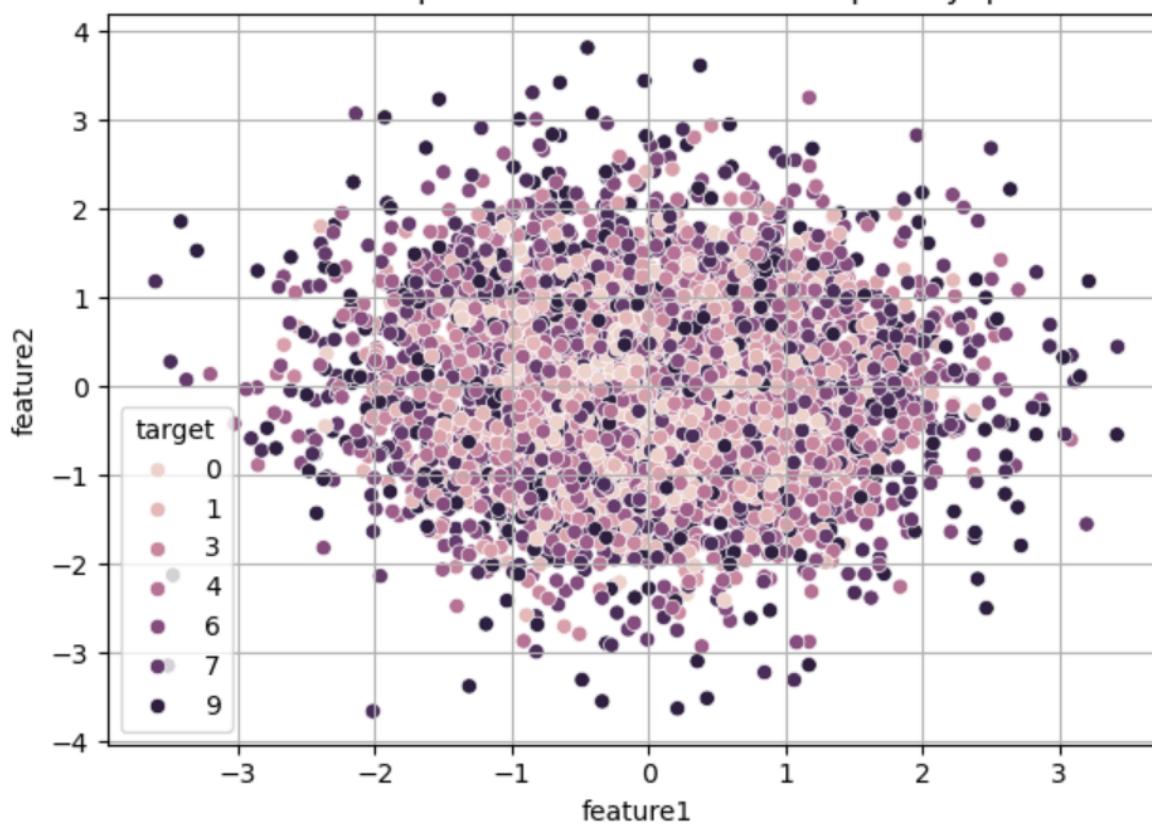
original_raw

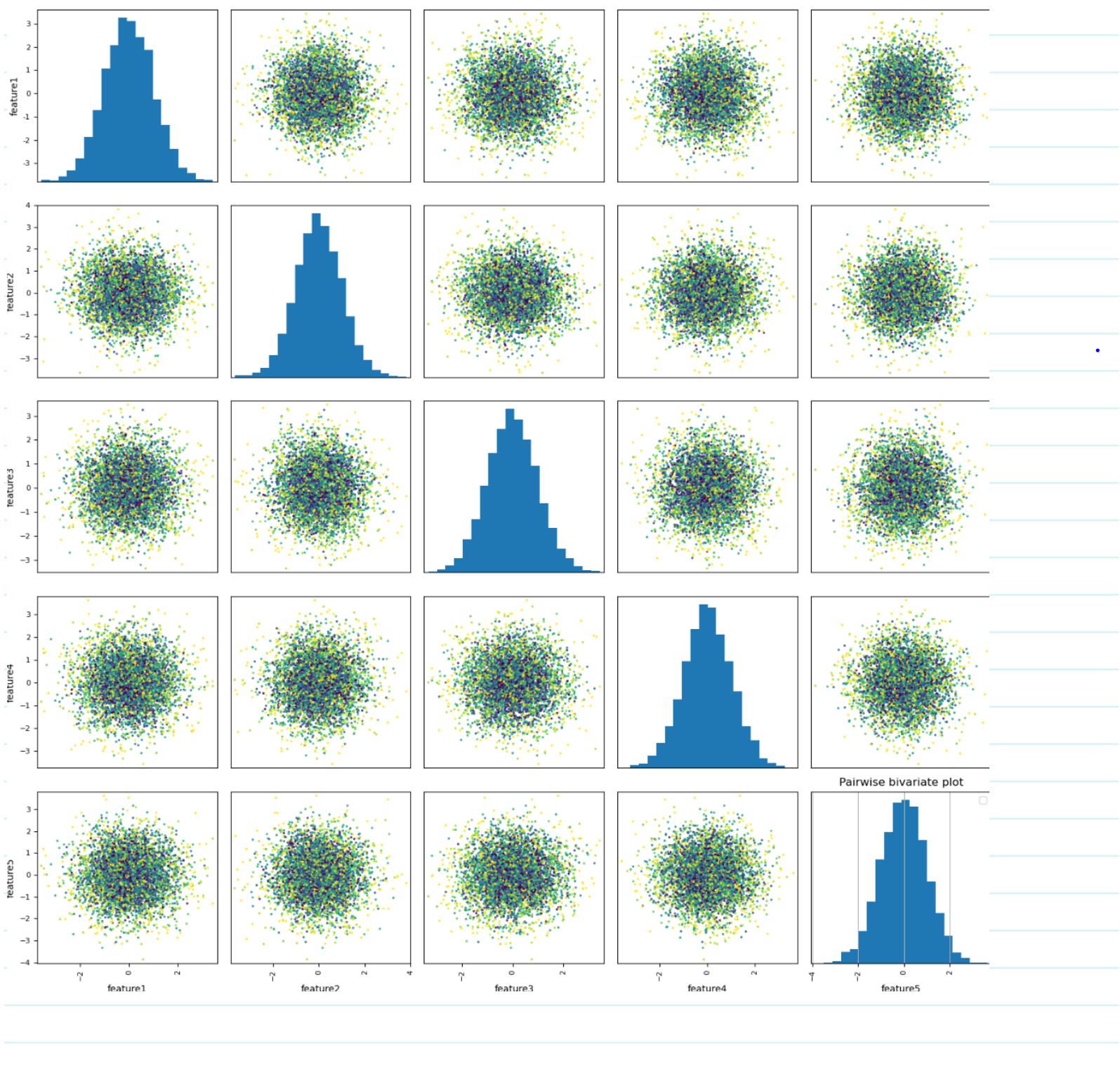
	A	B	C
0	Non ✓	11	Non 11
1	1 ✓	5 ✓	5 ✓
2	2	Non 2	10
3	3	Non 3	11
4	Non ✓	Non ✓	Non ✓
5	✓ Non	8	8

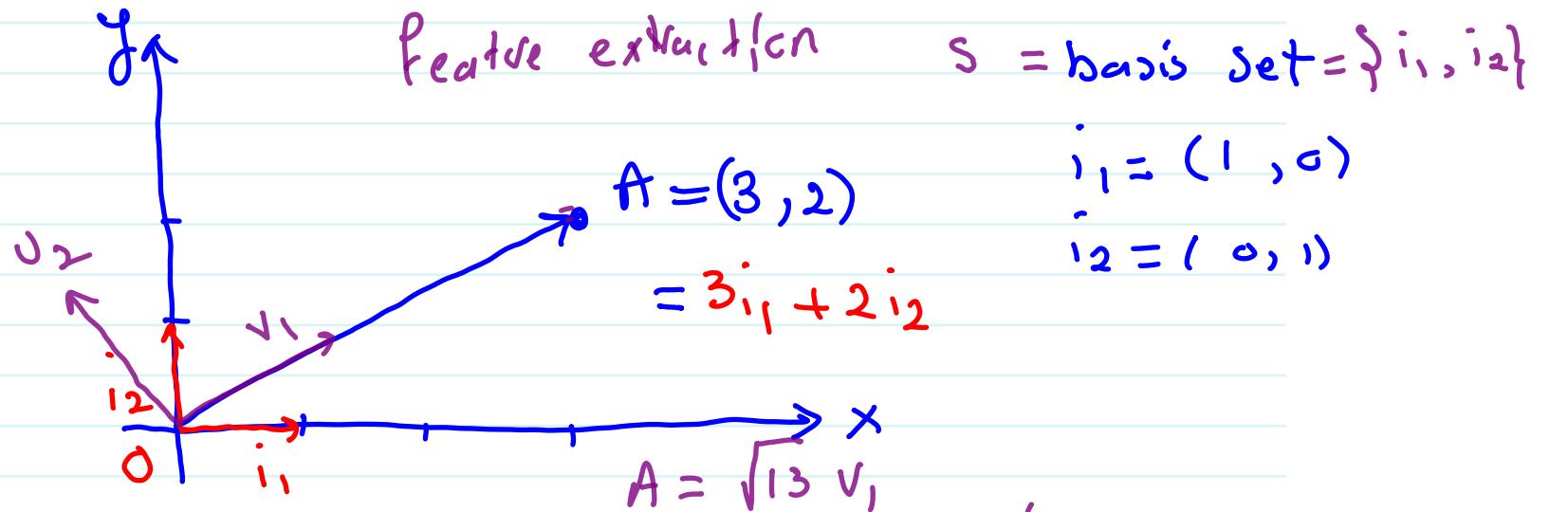
- ; |
- : 2
- ; ?
- ; ?

	1	2	3	4	5
1					
2					
3					
4					
5					

Generate isotropic Gaussian and label samples by quantile







S' : new basis $= \{v_1, v_2\}$

