

Question 1

III-A

Quick Sort

66	77	11	88	99	22	33	44	55
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taking 66 as pivot.

pivot = 66

0	1	2	3	4	5	6	7	8
66	77	11	88	99	22	33	44	55

\uparrow pivot i

 $i = 1, j = 8$

Here i is greater than pivot, so checking $j < \text{pivot}$
 and since $j < \text{pivot}$ we swap i and j

66	55	11	88	99	22	33	44	77
----	----	----	----	----	----	----	----	----

p i j

 $i = i + 1$, incrementing i

$$j = j - 1$$

→ so, $i = 2$, $j = 7$

$$\text{array}[i] = 11$$

Here $i < \text{pivot}$,

$$11 < 66$$

so incrementing i to $i+1$

$$i = 3, j = 7$$

$$\text{array}[3] = 88$$

$i > \text{pivot}$ so checking j value.

$$\text{array}[j] = 44$$

$44 < \text{pivot}$ so swapping j and i

0	1	2	3	4	5	6	7	8
66	55	11	44	99	22	33	88	77

incrementing ~~both~~ i value and j

decrementing j

→ $i = 4$ $j = 6$

Here $\text{array}[i] > \text{pivot}$ so checking with j

① $\text{array}[j] < \text{pivot} \longrightarrow \text{True}$

So swapping j and i

0	1	2	3	4	5	6	7	8
66	55	11	44	33	22	99	88	77

incrementing i and decrementing j

→ Here i and j are at same index so we check is ϕ .

$i > \text{pivot} \longrightarrow \text{False}$

So we swap i with pivot

0	1	2	3	4	5	6	7	8
22	55	11	44	33	66	99	88	77

Now we get left of ~~66~~ pivot is less than 66 and right is greater than 66

we are doing the same procedure for both left and right

Left sub array =

22	55	11	44	33
----	----	----	----	----

Right sub array =

99	88	77
----	----	----

11	22	33	44	55	66	77	88	99
----	----	----	----	----	----	----	----	----

Final Sorted array =

0	1	2	3	4	5	6	7	8
11	22	33	44	55	66	77	88	99

Time complexity - worst case

$$T(n) = [(n+1) + (n) + (n-1) + \dots + 3 + 2] + T(0)$$

$$= 1 + 2 + 3 + \dots + n + n+1$$

$$= (n+1)(n+2)/2$$

$$= (n^2 + 12n + 2) / 2 < n^2 / 2$$

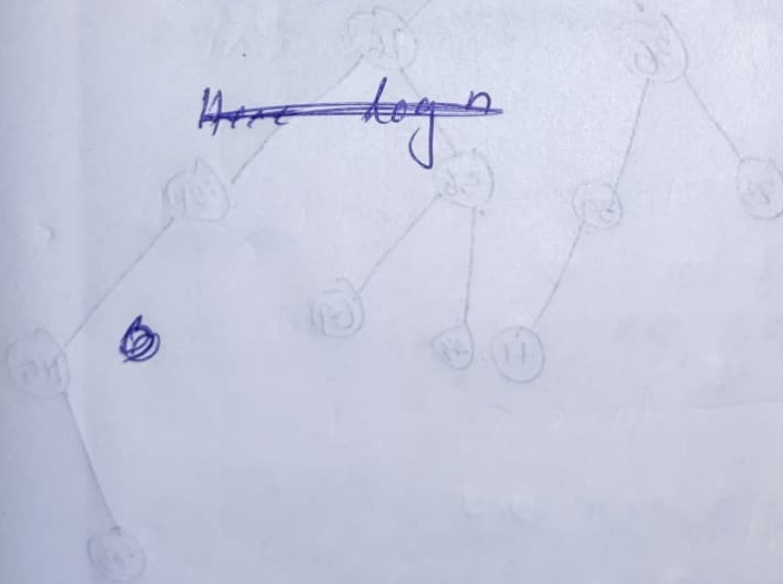
$$= O(n^2)$$

Time complexity of Best case

$$T(n) = O(n \log n)$$

Because it works n times $\log n$.

~~Here $\log n$~~



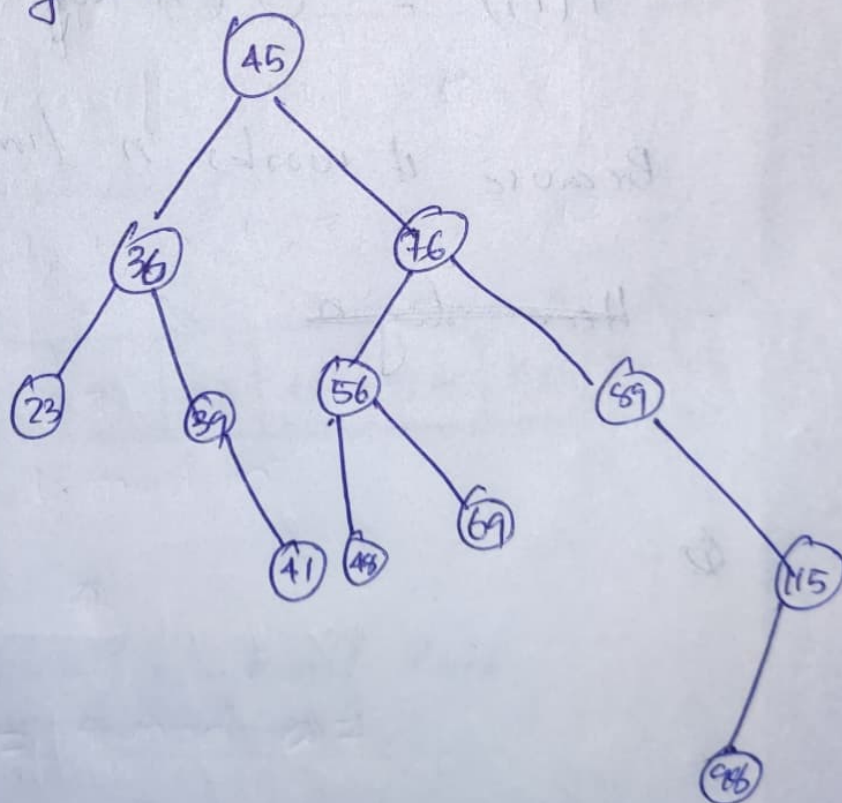
(log, left, right)

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Question 2

1A.

BST → Binary Search Tree



Inorder (Left, Root, Right)

23, 36, 39, 41, 45, 48, 56, 69, 76, 98, 115

89, 98, 115

preorder (Root, left, right)

45, 36, 23, ~~41~~, 39, 41, 76, 56, 48,

69, 89, 115, 98, ~~41~~

postorder (^{Left} ~~Right~~, ^{Right} ~~Left~~, Root)

~~41, 39,~~

23, 41, 39, 36, 48, 69, 56, 98, 115, 89,

76, 45

Question 3~~11.A~~

11.B

Division Method. $k = \text{key}$ $m = \text{Size of array, } 7$

8, 20, 9, 4, 15, 10, 7, 22, 3, 12

$$h(k) = k \bmod m$$

$$= 1$$

$$h(8) = 8 \bmod 7$$

$$= 1$$

$$h(20) = 6$$

$$h(9) = 2$$

~~11.C~~

$$h(4) = \underline{4}$$

$$h(15) = \underline{1}$$

$$h(10) = \underline{0}$$

here 0 is already exists so
 $\underline{3}$ we have to do other operation
 to avoid collision

$$h(7) = \underline{0}$$

$$h(22) = \underline{1}$$

$$h(3) = \underline{3}$$

$$h(12) = \underline{5}$$

here also collision, so we have
 to do other operation, like
 other hash functions.

Flooding Method

Flooding method.

key	8	20	9	4	15	10	7	22	3	12
parts	8	2,0	9	4	15	10	7	2,2	3	12
sum	8	2	9	4	6	1	7	4	3	3
Hash Value	8	2	9	4	6	1	7	4	3	3