

DS → Linear DS → continuous and non continuous  
Non linear DS → Trees, Memory

Stack

Evaluation → Infix

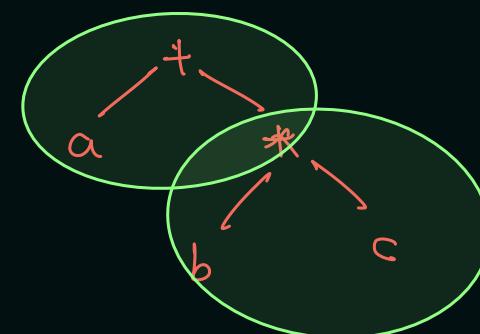
BDMAS

# Mathematical Expression → ]  
# Heap (Binary Tree)

Importance of left & Right node.



a + b \* c



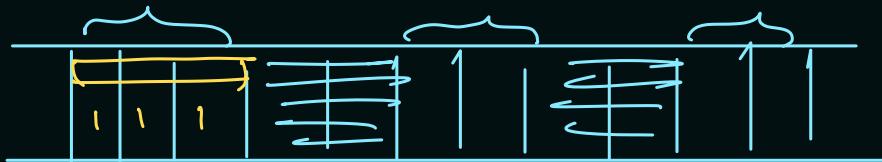
\* Why Recursion considered good in trees but in LL.

Linear DS

Recursion

→ level of Recursion (no. of nodes)

Max. no. nodes → Amount of memory free Heap.



Max. size of array = 3

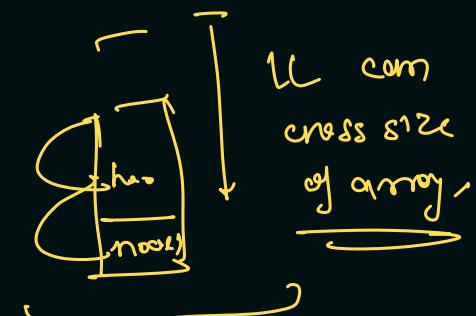
Max. size of LL = 7

Height of Tree =  $\log_2 n$

put value of n

$$\log_2^{32} = \underline{\underline{82}} \rightarrow \text{max level}$$

Stack → overflow → fix sized



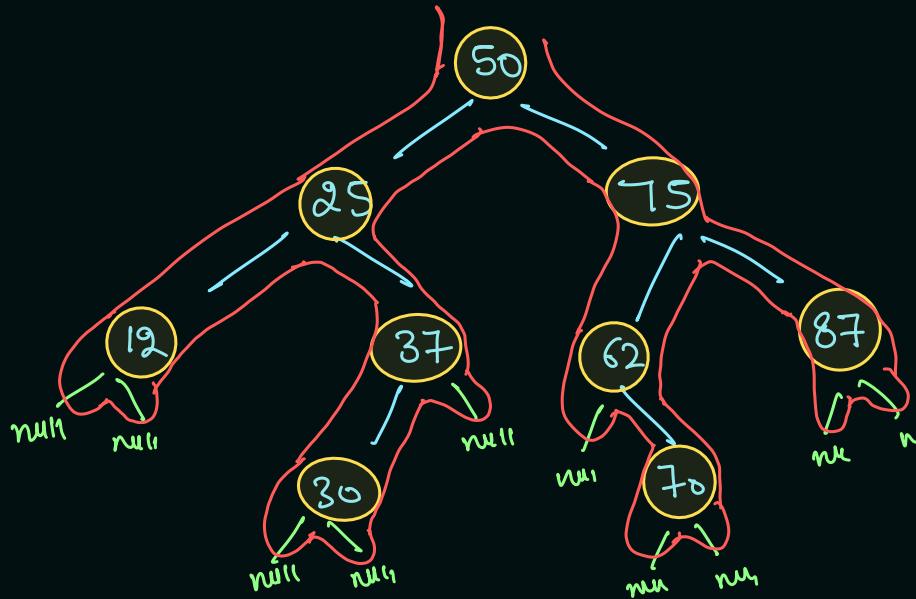
→ Reverse pointer recursively.

## Example (BST)X

point zig-zag

↓  
Areas - in Recursion

- Pre Area
- In Area
- Post Area



Traversal → pre Order Traversal

In Order Traversal

Post order Traversal

\* Level order Traversal

fun - function

- Pre Area [Area Before call]
- Call ① → In Area [Area After first call & Before last call]
- Call ② → Post Area [Area after all calls]

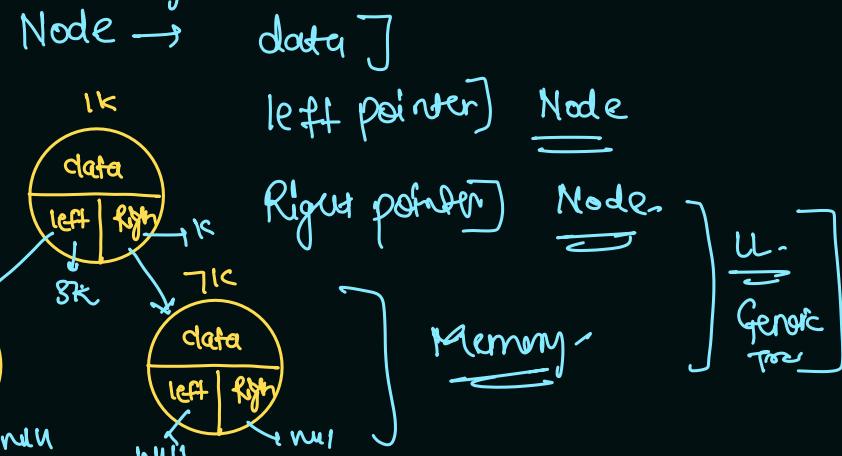
Construction using pre order

Pre Order → 50 25 12 37 30 75 62 70 87

In Order → 12 25 30 37 50 62 70 75 87

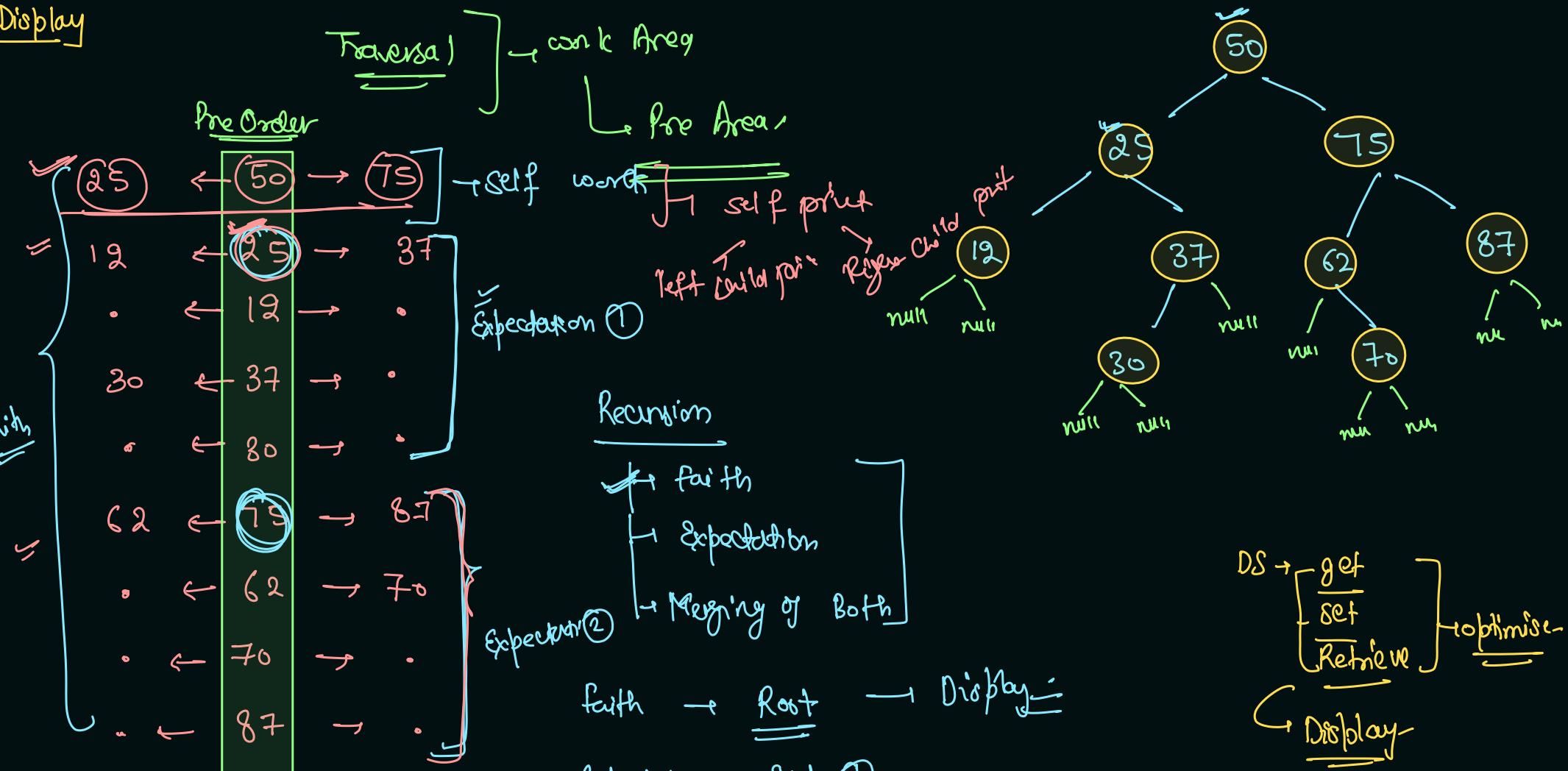
Post order → 12 30 37 25 70 62 87 75 50

Binary Tree





## Display



Merging → self work

Exp. ①

Exp. ②

DS → [ get  
 set  
 Retrieve ] → optimise  
 ↗ Display

```

int indx = 0;
while(indx < data.length && st.size() > 0) {
    Pair top = st.peek();
    if(top.state == 1) {
        indx++;
        if(data[indx] != null) {
            Node nn = new Node(nn = btree.co
            top.node.left = nn;
            st.push(new Pair(nn, 1));
        }
        top.state++;
    } else if(top.state == 2) {
        indx++;
        if(data[indx] != null) {
            Node nn = new Node(data[indx]);
            top.node.right = nn;
            st.push(new Pair(nn, 1));
        }
        top.state++;
    } else {
        st.pop();
    }
}

```

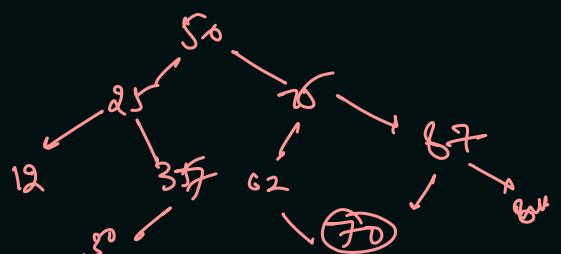
Input [preorder]

50	75
25	62
12	null
null	70
null	11
37	null
30	87
null	null
null	null

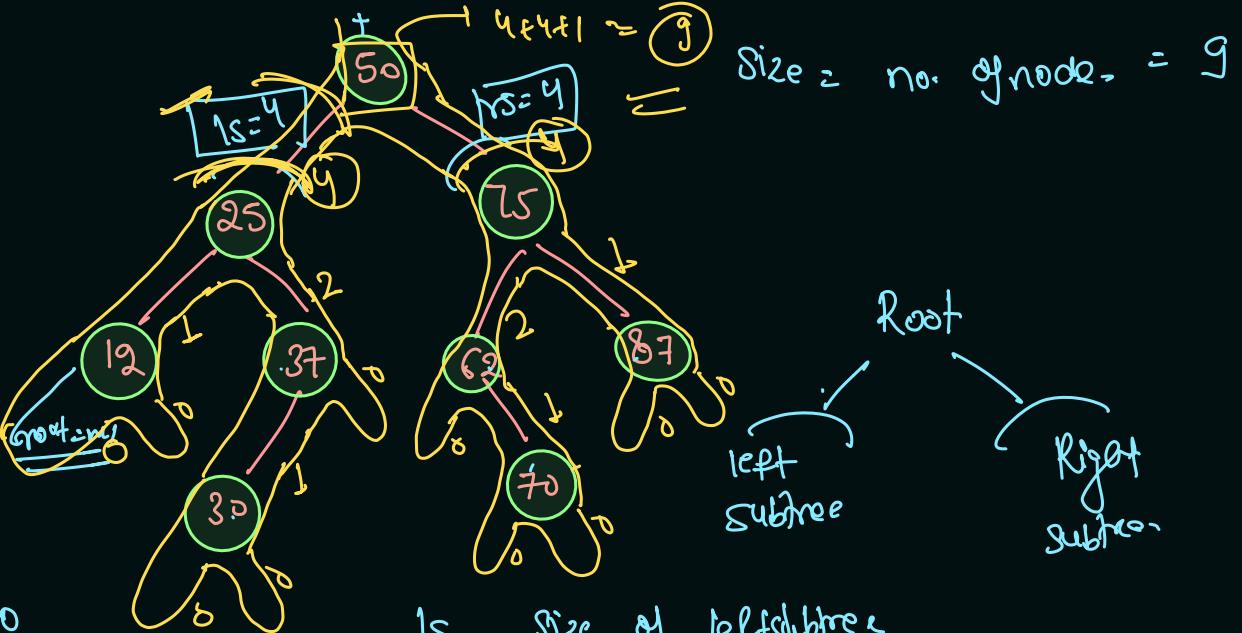
gray →      top →



~~87 123~~  
~~75 62 3~~  
~~50 - 123~~



- ① Size
  - ② Sum
  - ③ Max
  - ④ Height
- } of Binary Tree



base case:  
return 0

```
public static int size(Node node) {
    if(node == null) return 0;
    int lsize = size(node.left);
    int rsize = size(node.right);
    int msize = lsize + rsize + 1;
    return msize;
}
```

$$\text{complete size} = \underline{\underline{lsize + rsize + 1}}$$

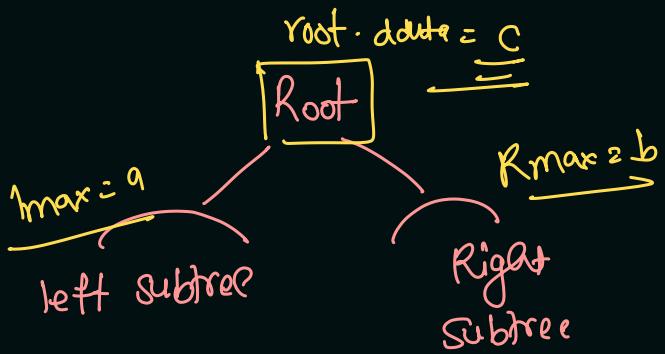
sum & max is similar to size

sum =  $\frac{lsum}{rsum}$  = from left subtree  
 $\frac{rsum}{lsum}$  = from Right subtree

Total sum =  $\underline{\underline{lsum + rsum + root}}$

Base case  $\Rightarrow \text{root} = \text{null}$   
 ↳ return 0

Max →



max. of left Subtree

max. of Right Subtree,

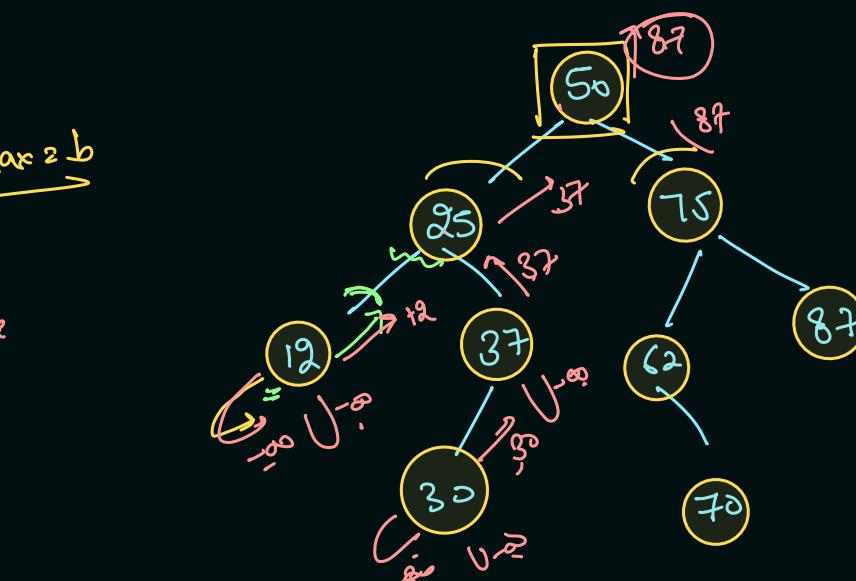
$$\text{Final Result} = \underline{\underline{\max(a, b, c)}}$$

Every operator have an Identity.

$$a * e = a$$

$\xrightarrow{\text{operator}}$

e → Identity of that operation.



what if (root == null)

op →	<u>Identity.</u>
+	0
-	0
*	1

$$\max() \rightarrow \underline{-\infty}$$

$$\min() \rightarrow \underline{+\infty}$$

Identity of  
operator

$$a + 0 = a$$

0 is identity of +

$$a * 1 = a$$

$$a / 1 = a$$

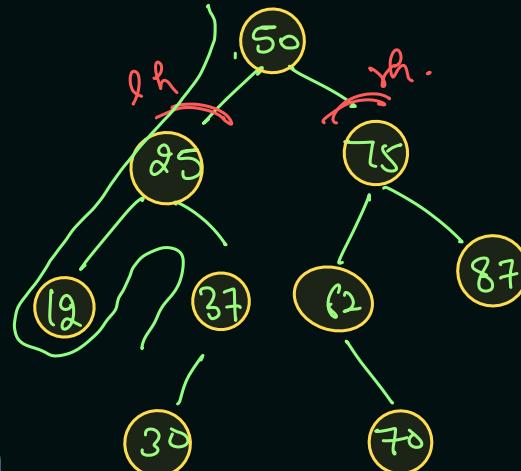
$$\max(a, e) = a$$

$$\underline{e = -\infty}$$

Height → Structure based problem

what is Height?

Max distance between Root to leaf  
is Height of the tree.



Height = 4

OR

Height = 3

distance



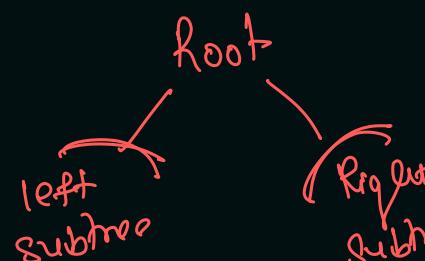
distance = 2[Node] OR L[Edge]

Height → on the basis of Edge  
on the basis of node.

left subtree Height = lh

Right subtree height = rh

Max distance, my Height =  $\max(lh, rh) + 1$



Node base | Edge base



height=? = 1

$$\max(lh, rh) + 1$$

≡ Node base  
↳ if (root == null)  
↳ return 0

Height=? = 0

$$\max(lh, rh) + 1$$

Edge base

if (root == null)  
return -1;

## level Order of a Binary Tree

Algo = BFS from Graph

level order →

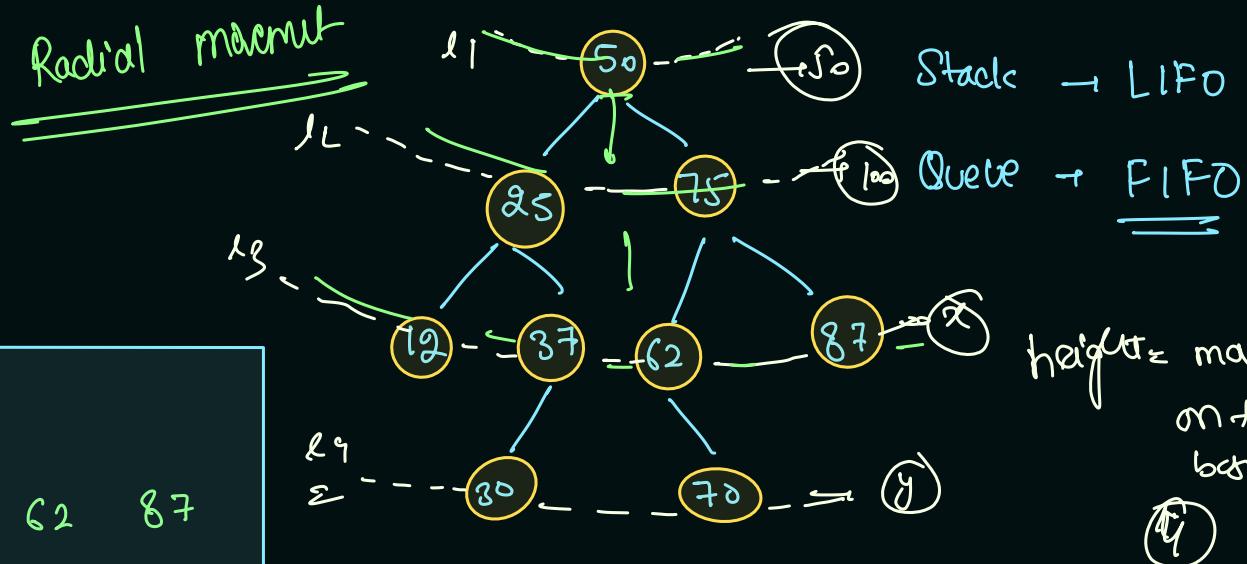
level order

sym

level 3 →

level 4 →

50
25    75
12    87    62    87
30    70

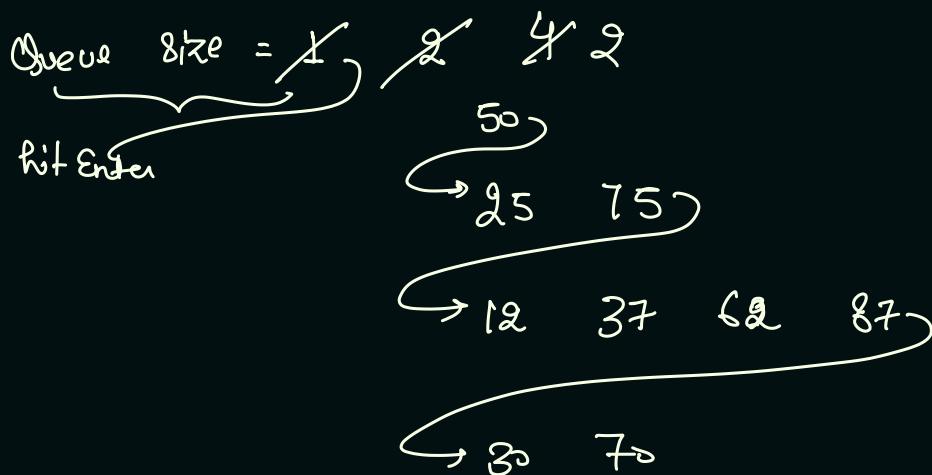
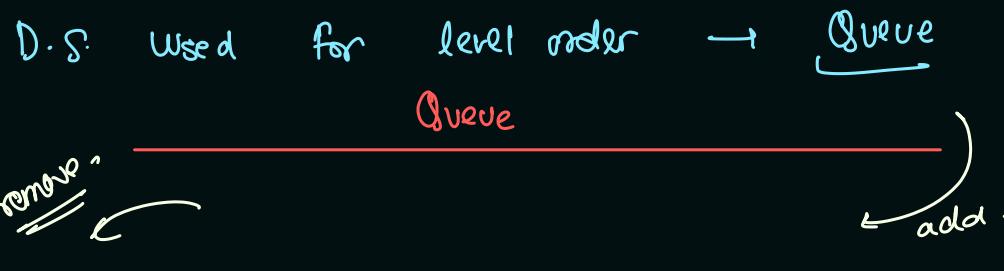


height = max. level  
on the basis of no.  
of levels

(4)

steps of Algo.

- ① Get + Remove
- ② work → print
- ③ Add children



if que.size() > 0

- size = que.size()
- while size -- > 0
- get + remove
- works
- Add children
- hit Enter.

level order  
BFS  
Height

linked list as a queue →

<u>add</u>	→	<u>add Last</u>
<u>remove</u>	→	<u>remove first</u>
		<u>get first</u>
size is common in Both.		

level order

<u>Delimiter</u>	→ <u>null</u>
<u>Using two queue</u>	
<u>while → in while</u>	

linked

get + Remove ] → C++

get ]  
remove ] } remove doesn't return anything in C++  
while JAVA return removal element

work → point

add children

till Right ]      height  
height      n+1

~~level~~  
function task  
root

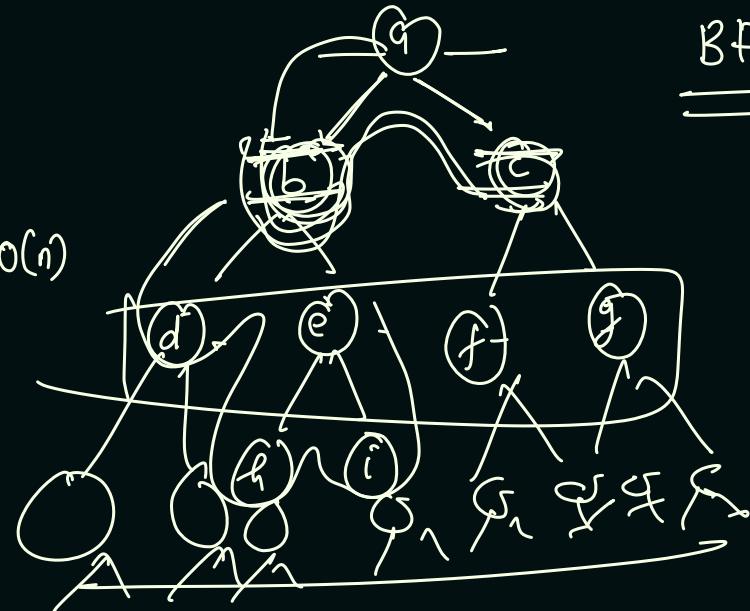
① → ①

② (b) ③

③

④

single level -  $O(n)$   
Recursion  
 $\downarrow$   
 $O(n^2)$



# Iterative Pre, Post and In order:

Base problem → construction of tree

First Encounter → Pre Area ] → Pre order ] →

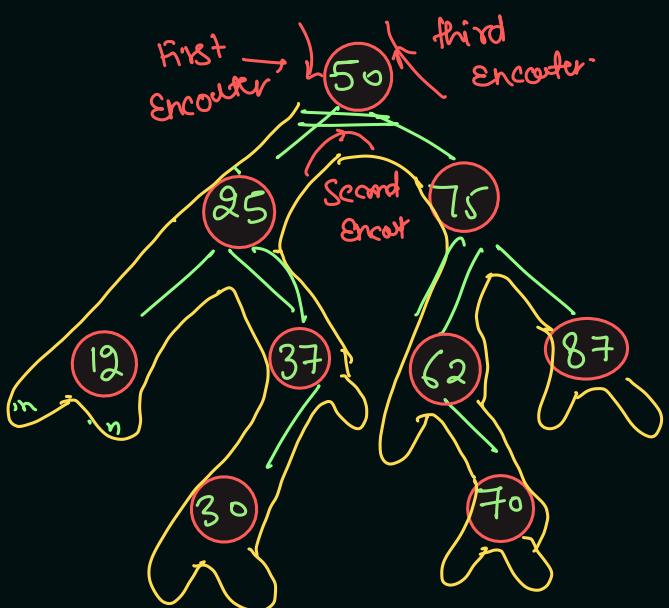
State -



Second Encounter → In Area ] → In order ] →



Third Encounter → Post Area ] → Post order ] →



~~Pre Order →~~ 50 25 12 37 30 75 62 70 87

Inorder → 12 25 30 37 50 62 70 75 87

Post order → 12 30 37 25 70 62 87 75 50

~~75 - 123~~

~~50 - 123~~

$\Leftarrow$  root = 50

get  $\top$  =

top-state = 1 ] → pre Add  
 ↳ left child add in stack  
 $\top\text{-state}++$   
 $= 2 \rightarrow$  in Add  
 ↳ right child add in stack  
 $\top\text{-state}--$   
 $= 3 \rightarrow$  post add pop from stack

