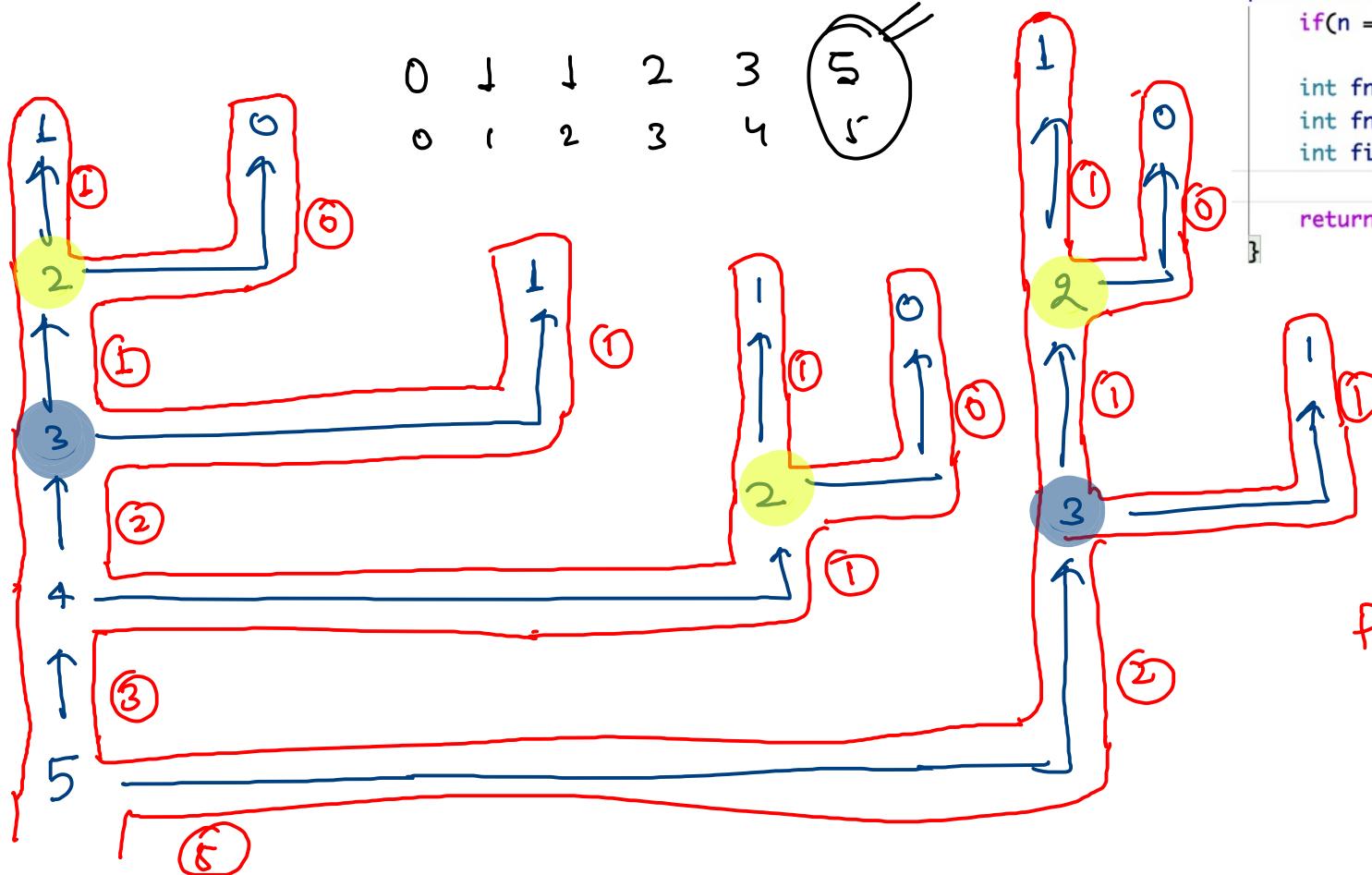


Dynamic Programming

↳ Repitated problems

Sacrifice with space
and
Save time } massive time



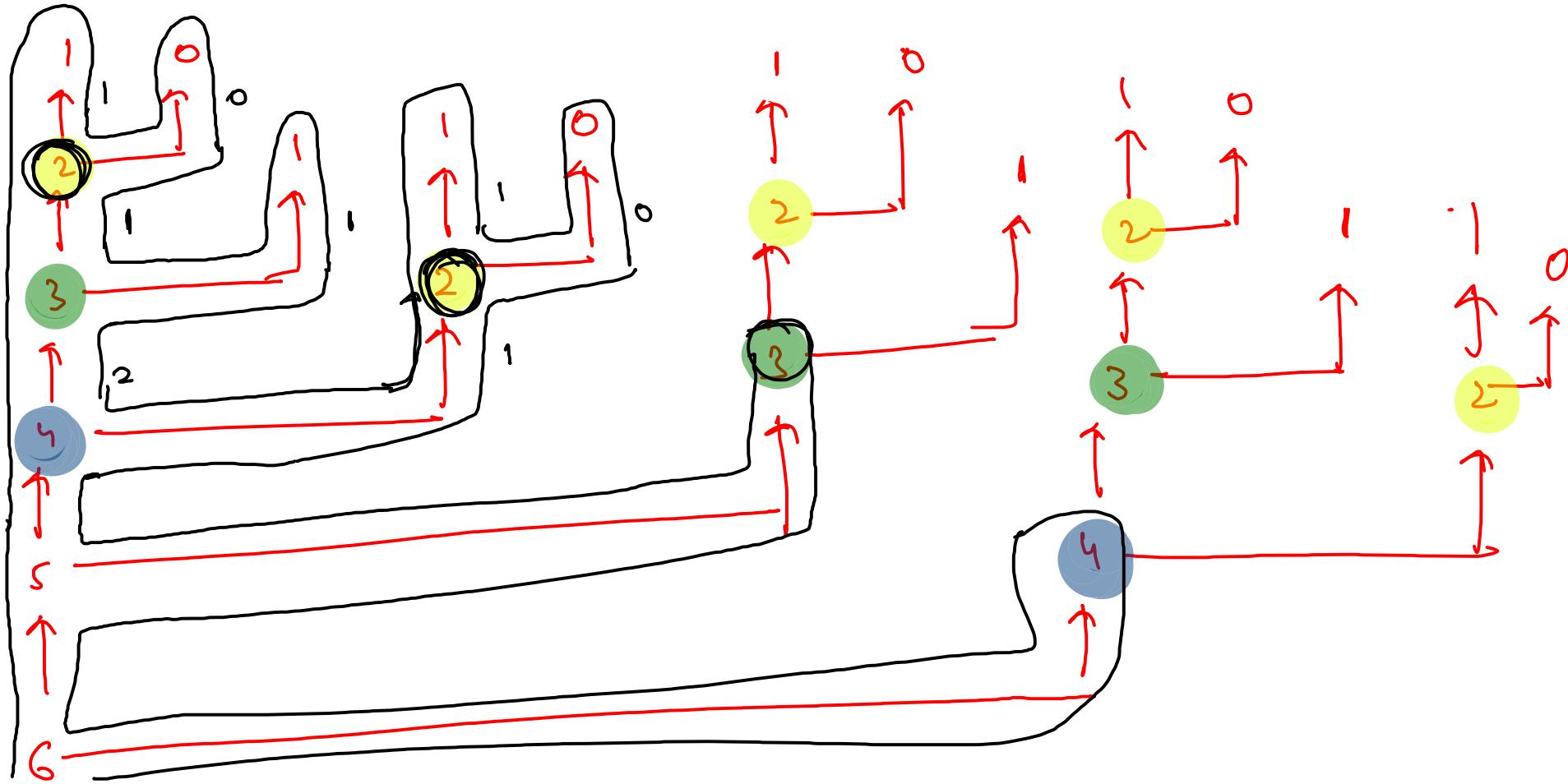
```
public static int fib_rec(int n) {
    if(n == 0 || n == 1) return n;

    int fnm1 = fib_rec(n - 1);
    int fnm2 = fib_rec(n - 2);
    int fibn = fnm1 + fnm2;

    return fibn;
}
```

$$\text{fib}(5) = 5$$

$$n=5$$



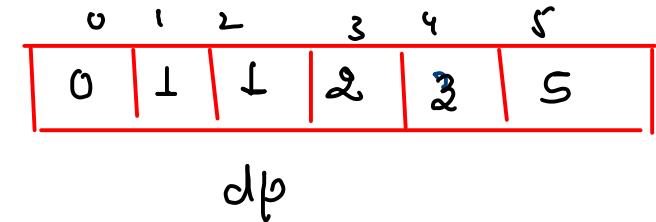
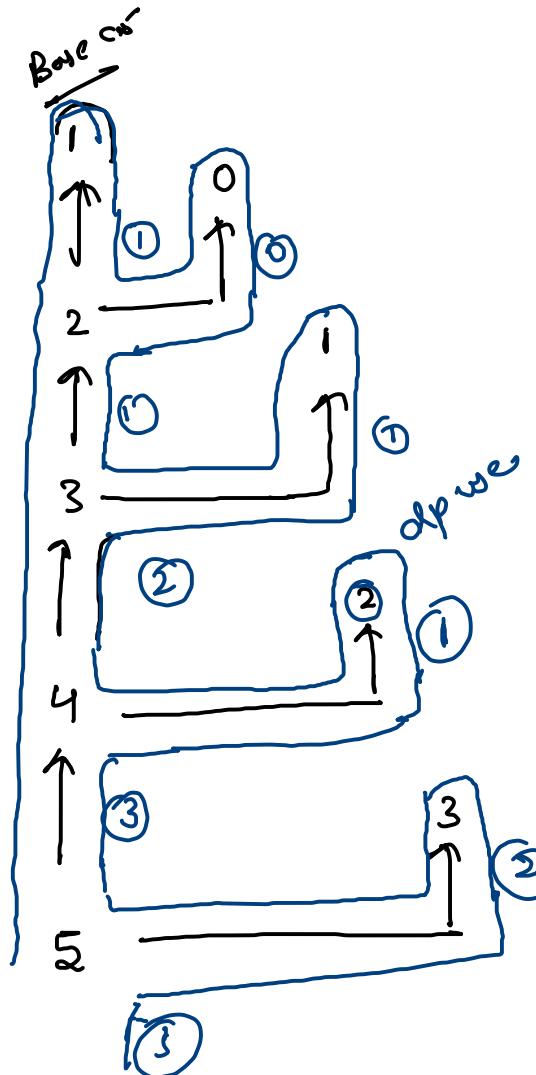
```

public static int fib_memo(int n, int[] dp) {
    if(n == 0 || n == 1) {
        dp[n] = n;
        return dp[n];
    }
    // if problem is already solved, then return the solution
    if(dp[n] != 0) {
        return dp[n];
    }
    int fnm1 = fib_memo(n - 1, dp);
    int fnm2 = fib_memo(n - 2, dp);
    int fibn = fnm1 + fnm2;
    // solve and store the problem in dp
    dp[n] = fibn;
    return fibn;
}

```

$n=5$

$dp\ size = \underline{n+1}$



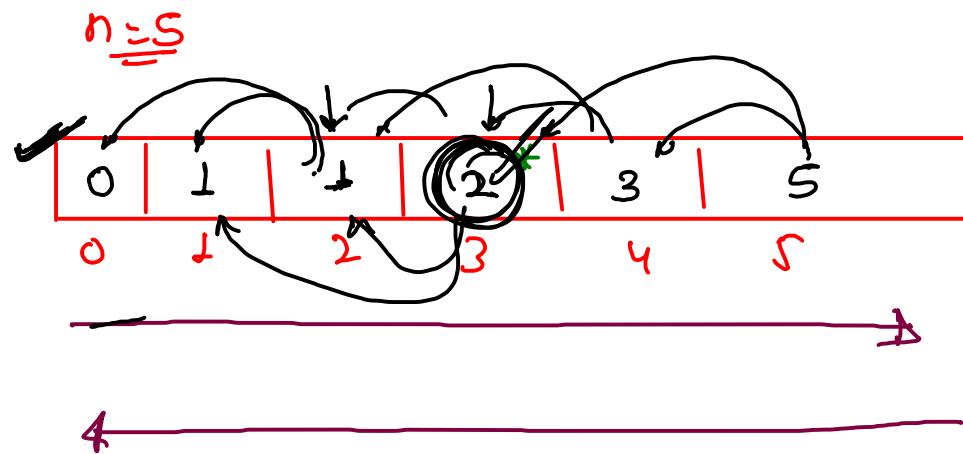
Tabulation-

- ✓ 1. Make storage
- ✓ 2. Assign meaning to cell
- ✓ 3. Identify traversal of problem.
- ✓ 4. Set pre requisite in 'dp' \rightarrow smallest to largest problem

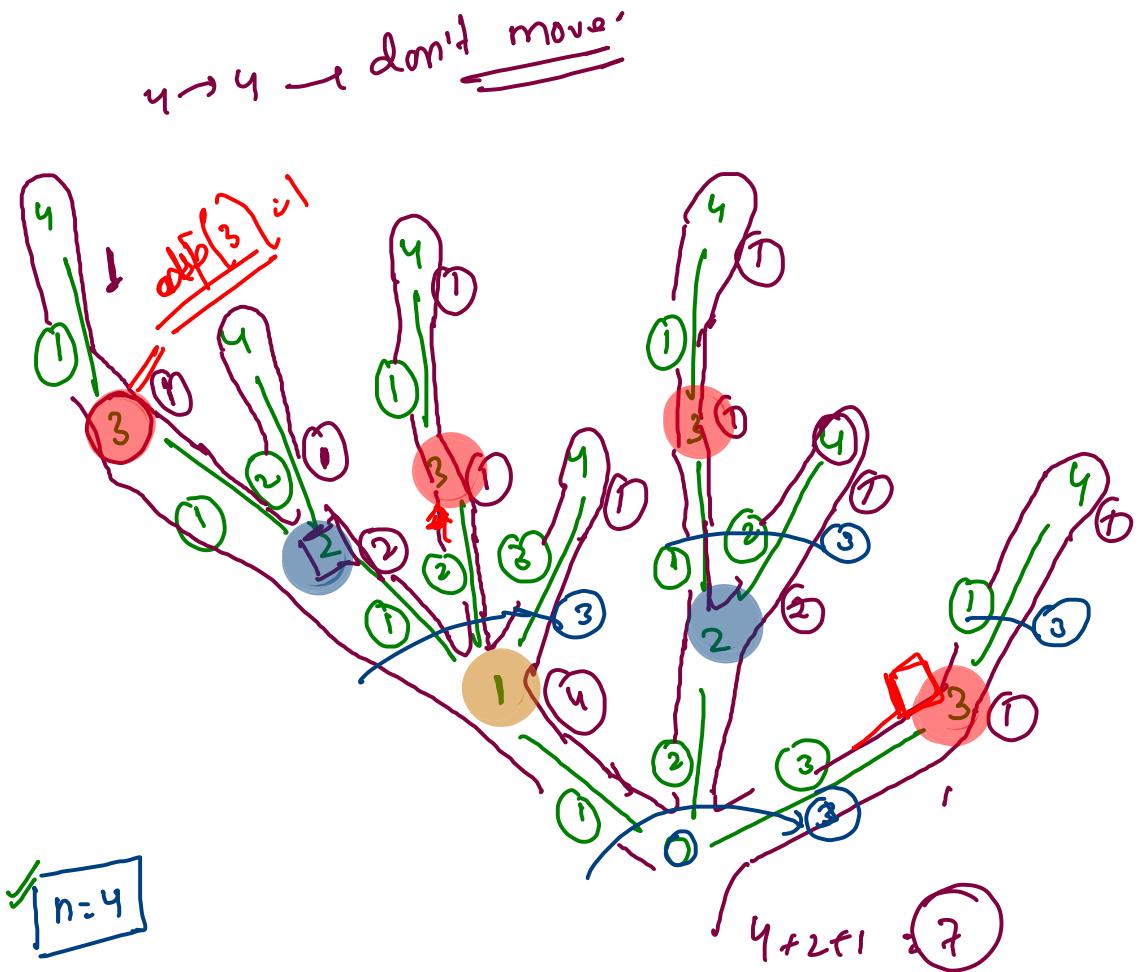
$dp[3] = \text{answer of fib}(n)$.

$dp[3] = \text{it have sum of } \underline{dp[2]} + \underline{dp[1]}$

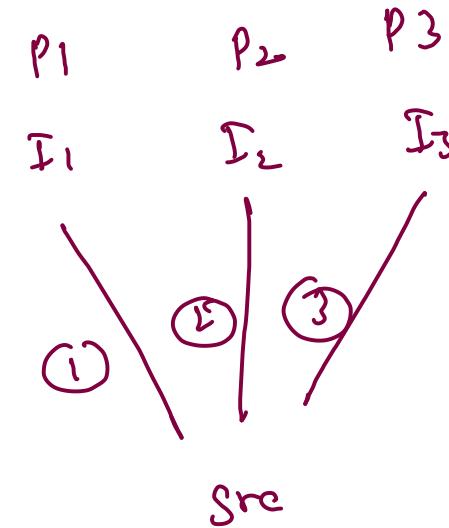
fib tabulation-



Climb Stair path



$\alpha s \cdot$



$$\text{src} \rightarrow \text{dst} = p_1 + p_2 + p_3$$

```

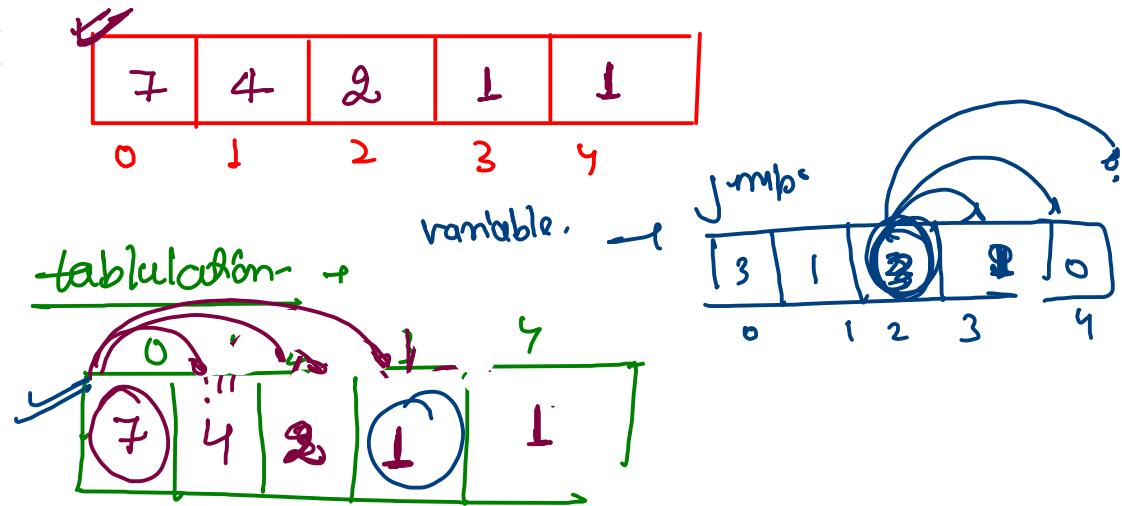
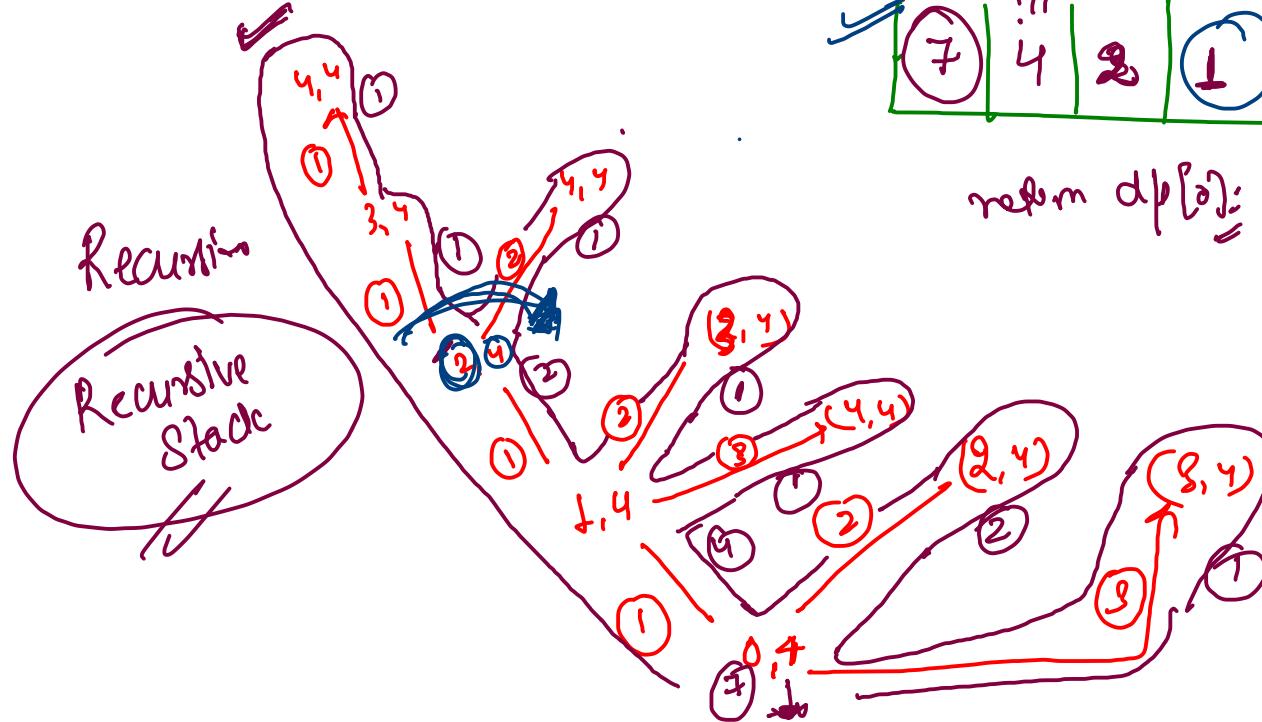
public static int climbStair_memo(int i, int n, int[] dp) {
    if(i == n) return dp[i] = 1;

    if(dp[i] != 0) return dp[i];

    int count = 0;
    for(int jump = 1; jump <= 3 && i + jump <= n; jump++) {
        count += climbStair_memo(i + jump, n, dp);
    }

    return dp[i] = count;
}

```



$$dp[n] = 1;$$

$n=7$

$$\text{dp-size} = n+1 = 8$$

Meaning $\text{dp}[i] = \text{No. of paths from } i \text{ to } n$

49	24	13	7	4	2	1	1
0	1	2	3	4	5	6	7

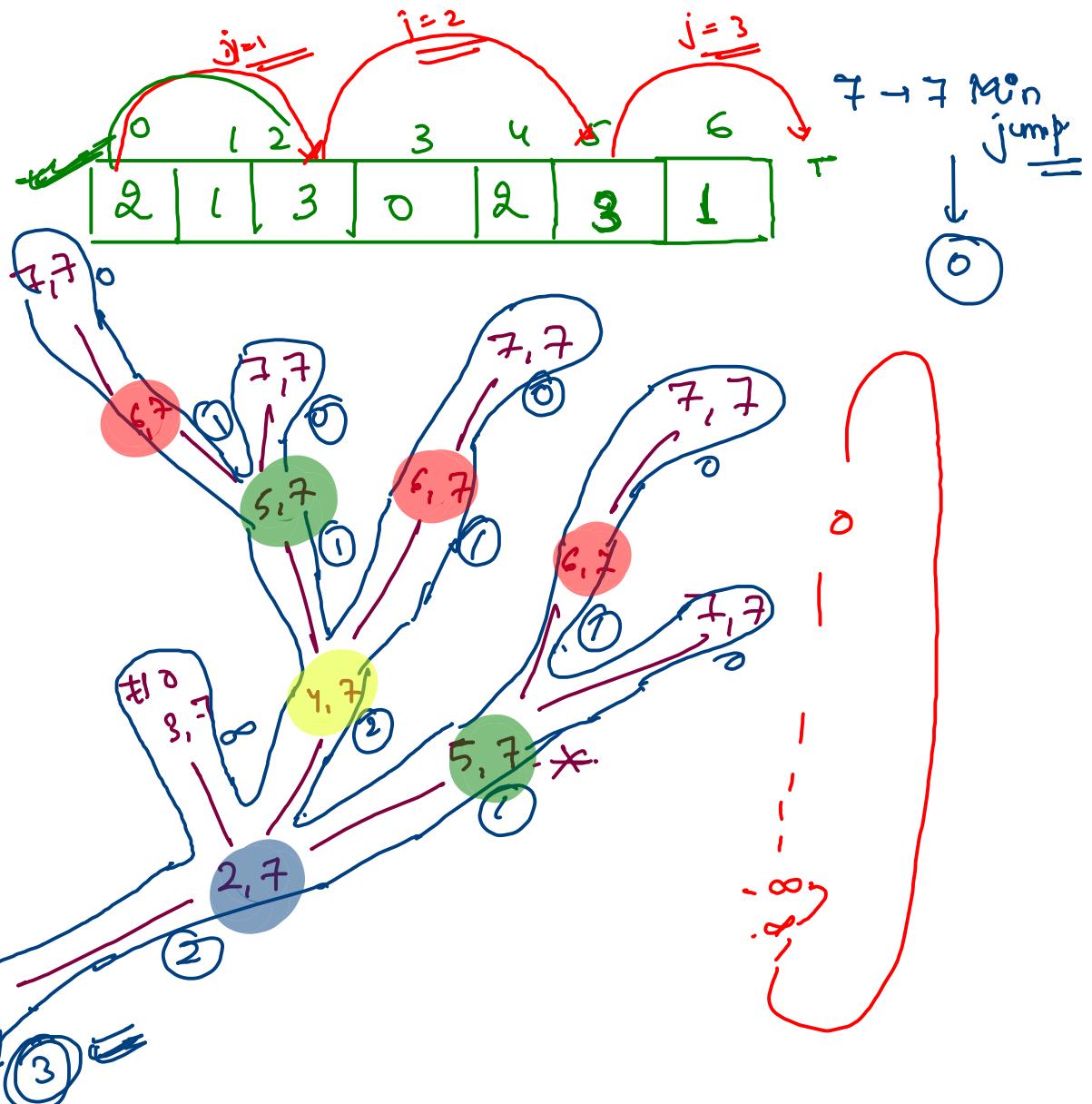
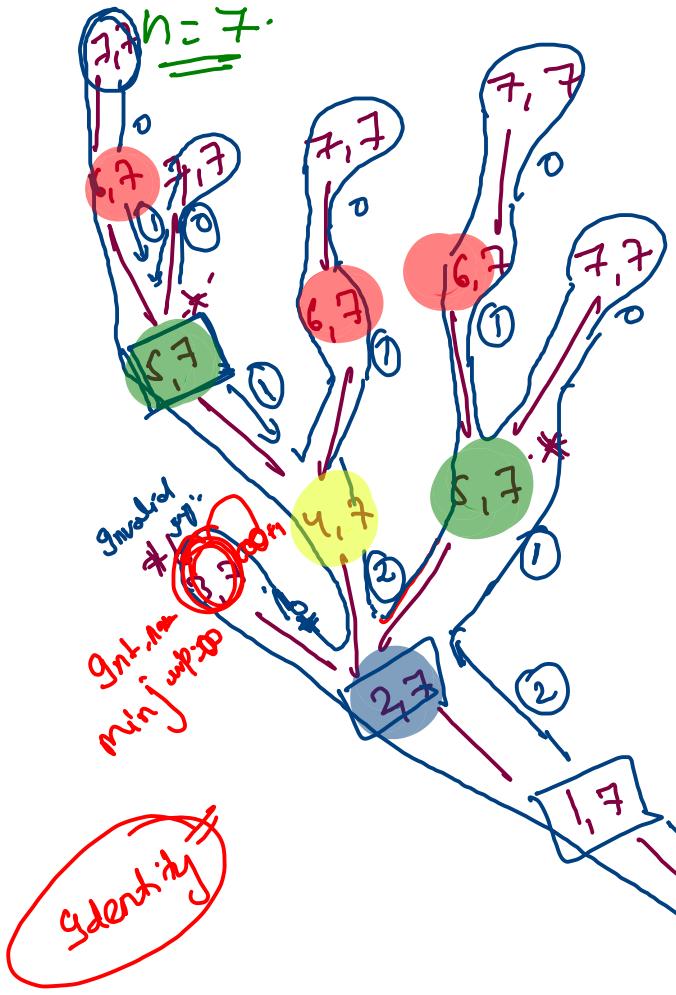
smallest problem $\text{dp}[n]$

$$\text{dp}[n] = 1;$$

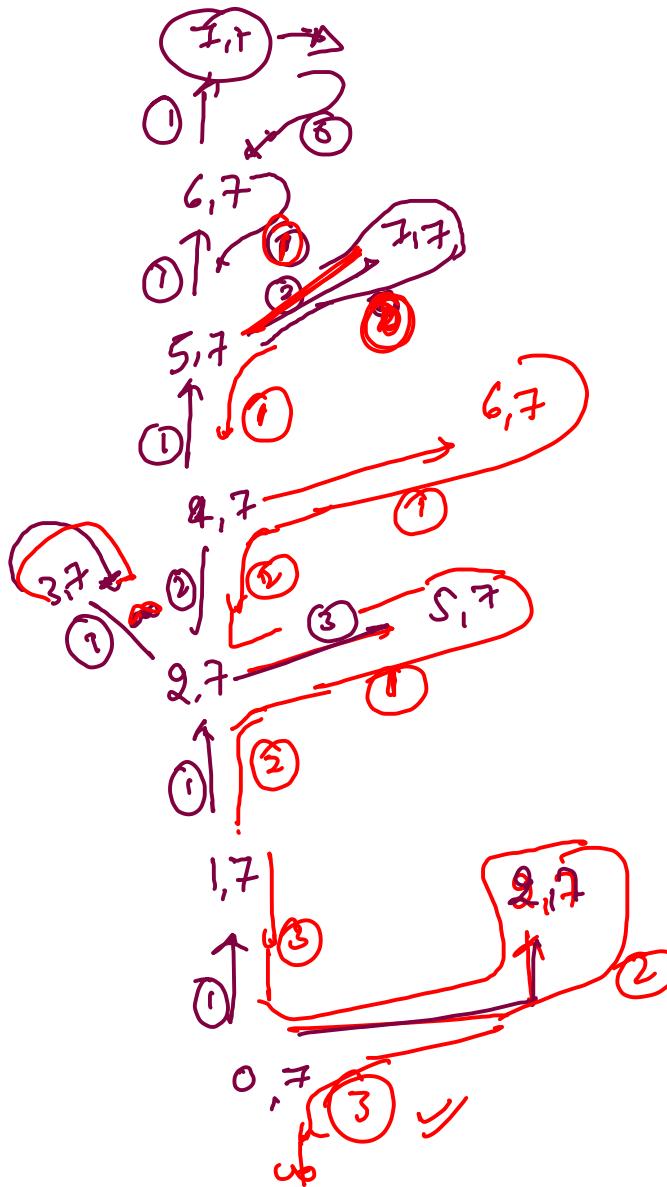
2	4	2	0	0
0	1	2	3	7

3	2	1	0	1
0	1	2	3	7

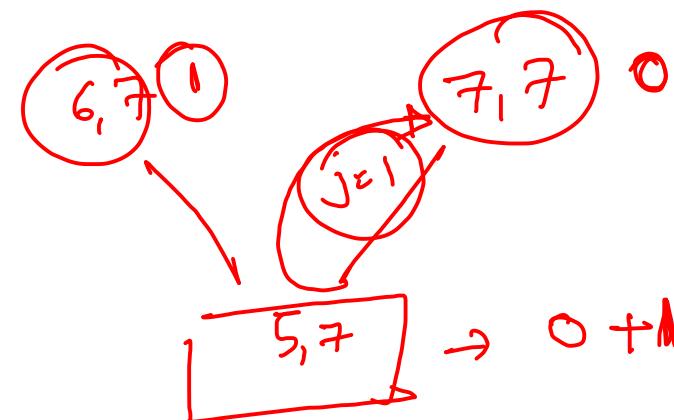
Climb Stair Min Jump δ .



$$\boxed{n=7}$$



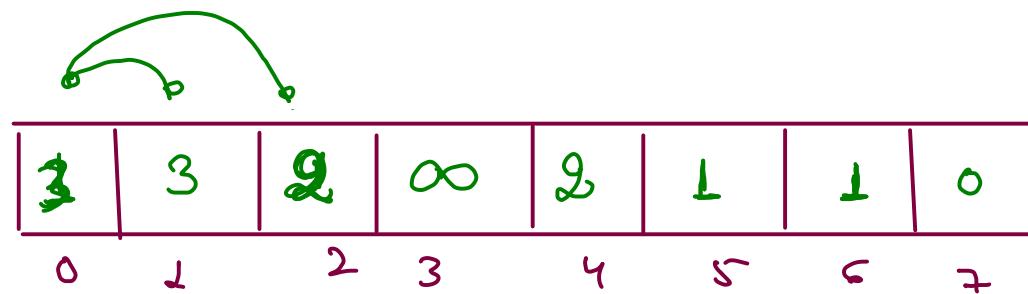
2 0	1 1	3 2	0 3	2 4	3 5	1 6
3 0	3 1	2 2	∞ 3	2 4	1 5	1 6



$$0 + 1$$

Tabulation-

2	1	3	0	2	3	1
0	1	2	3	4	5	6
↑	↑			↑		



$$dp[0] = 3$$

* Meaning $dp[i]$ - $dp[i]$ have min jumps, in which we can reach at destination for i .