

Three Sum - Notes

Problem Statement:

Given an integer array `nums`, return all the unique triplets `[nums[i], nums[j], nums[k]]` such that:

- $i \neq j, i \neq k, \text{ and } j \neq k$
- $\text{nums}[i] + \text{nums}[j] + \text{nums}[k] == 0$

Approach 1: Brute Force

- Explanation:

Iterate through each triplet using three nested loops to find the sum of three elements that equal zero.

- Time Complexity: $O(n^3)$
- Space Complexity: $O(1)$

Approach 2: Sorting + Two Pointers

- Explanation:

Sort the array, then for each element `nums[i]`, use two pointers to find the other two elements that sum to zero.

- Fix one element, and use two pointers to find the other two elements.
- Time Complexity: $O(n^2)$
- Space Complexity: $O(1)$ (excluding the space used by the input array)

Approach 3: HashMap

- Explanation:

For each number in the array, calculate the complement ($0 - \text{nums}[i]$), and check if the complement exists using a HashMap.

- Time Complexity: $O(n^2)$
- Space Complexity: $O(n)$

Corner / Edge Cases Handled:

- Duplicate values (ensure unique triplets by skipping over duplicates after sorting).
- Array with fewer than three elements (no valid triplet).
- Handling negative numbers.
- Target sum of zero (all solutions should sum to zero).