

Electric Fields

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1. Calculate the magnitude and direction of the electric force if a charge of $-3.5 \times 10^{-7} \text{ C}$ is placed in a field of 12 N/C [right]. (5 marks)

- $q_1 = -3.5 \times 10^{-7} \text{ C}$
- $\vec{E} = 12 \text{ N/C}$ [right]
- $\text{Force} = q_1 \vec{E} = (-3.5 \times 10^{-7}) \times 12 = -4.2 \times 10^{-6} \text{ N}$

Thus, the answer would be $4.2 \times 10^{-6} \text{ N}$ that moves to the left.

2. An electron at rest of mass $9.11 \times 10^{-31} \text{ kg}$ is accelerated through a potential difference of 350 V . It then enters some deflecting plates of 50 V with dimensions as shown. Calculate the distance, x , or of the deflection of the electron. The charge on an electron is $1.6 \times 10^{-19} \text{ C}$.

- Electron is accelerated from rest ($u = 0 \text{ m/s}$) to a particular velocity v in a potential difference of 350 V .

$$\Delta v \cdot q = \frac{1}{2}mv^2 (\text{Final kinetic energy}) - \frac{1}{2}mu^2 (\text{Initial kinetic energy})$$

$$1.6 \times 10^{-19} \times 350 = \frac{1}{2} \times 9.11 \times 10^{-31} \times v^2 - \frac{1}{2}m(0)^2$$

$$v^2 = \frac{2 \times 1.6 \times 10^{-19} \times 350}{9.11 \times 10^{-31}} \rightarrow v = \sqrt{\frac{2 \times 1.6 \times 10^{-19} \times 350}{9.11 \times 10^{-31}}} = 1.11 \times 10^7 \text{ m/s}$$

- Now when electrons with velocity v enter in the 50 V region. Initially, when it enters the electron, it only has horizontal velocity v_h . But, due to some electric force in the vertical fashion, it gains some velocity in the direction

- Force in vertical direction

$$E = \frac{V}{r} = \frac{50}{5 \times 10^{-2}}$$

$$F = q_1 E = \frac{1.6 \times 10^{-19} \times 50}{5 \times 10^{-2}}$$

$$F = ma \rightarrow a = \frac{F}{m} = \frac{1.6 \times 10^{-19} \times 50}{9.11 \times 10^{-31} \times 5 \times 10^{-2}} \frac{\text{m}}{\text{s}^2}$$

- Thus, the time required to cover a distance 25 cm in horizontal direction is the following.

$$\text{distance} = \text{velocity} \times \text{time}$$

$$\text{time} = \frac{\text{distance}}{\text{velocity}} = \frac{25 \times 10^{-2}}{11.1 \times 10^6} = 2.25 \times 10^{-8} \text{ s}$$

- Now, use the equation in horizontal direction.

$$s = ut + \frac{1}{2}at^2$$

$$x = 0 \times t + \frac{1}{2} \frac{1.6 \times 10^{-19} \times 50 \times 2.25 \times 2.25 \times 10^{-16}}{9.11 \times 10^{-31} \times 5 \times 10^{-2}}$$

$$x = 4.445 \times 10^{-2} m$$

Thus, the answer would be 4.4cm.