

Mon

Name

M#

Solve the following ODEs

■  $y' = (1+y)e^t$   $y(0) = 1$

$$\ln(1+y) = e^t + C$$

$$C = \ln(2) - 1$$

sep  $dy/dt = (1+y)e^t$

$$\int \frac{dy}{1+y} = \int e^t dt + C$$

$$\ln(1+y) = e^t + C$$

1.  $y' = \frac{\sin(y)}{\cos(y)} (t^2 + 1)$

■  $t^2 y' + t y = t^3$  with  $y(1) = 2$

$$t y' + y = t^2$$

$$(t y)' = t^2$$

$$t y = \frac{t^3}{3} + C$$

$$y = \frac{t^2}{3} + \frac{C}{t}$$

2.  $e^t y' + 2 e^t y = e^t$  with  $y(0) = 1$

lin  $y' + \frac{1}{t} y = t$   
 $y' + p(t) y = s(t)$   
 $V(t) = e^{\int \frac{1}{t} dt}$   
 $v(t) = e^{\ln(t)} = t$

$$C = 2 - \frac{1}{3}$$

$$2 = \frac{1}{3} + \frac{C}{1}$$