

1 Number Representation

1.1 What is the range of integers represented by a n -bit binary number? Your answers should include expressions that use 2^n .

(a) Unsigned:

(b) Two's Complement:

(c) Bias (with bias b):

1.2 How many unique integers can be represented in each case?

(a) Unsigned:

(b) Two's Complement:

(c) Bias (with bias b):

2 Memory Addresses

2.1 Consider the following C program:

```
int a = 5;
int main()
{
    int b = 0;
    char* s1 = "cs61c";
    char s2[] = "cs61c";
    char* c = malloc(sizeof(char) * 100);
    return 0;
};
```

For each of the following values, state the location in the memory layout where they are stored. Answer with code, static, heap, or stack.

(a) s1

(b) s2

(c) s1[0]

(d) s2[0]

(e) c[0]

(f) a

- 2.2 Consider the C code here, and assume the malloc call succeeds. Rank the value of each variable (which may be an address!) from 1 to 5 (with 1 being the least) right before bar returns. Use the memory layout from class; Treat all addresses as unsigned numbers.

```
#include <stdlib.h>

int FIVE = 5;

int bar(int x) {
    return x * x;
}

int main(int argc, char *argv[]) {
    int *foo = malloc(sizeof(int));
    if (foo) free(foo);
    bar(10); // snapshot just before it returns
    return 0;
}

foo:   _____
&foo:  _____
FIVE:  _____
&FIVE: _____
&x:    _____
```

3 Linked Lists Revisited

- 3.1 Fill out the declaration of a singly linked linked-list node below.

```
typedef struct node {
    int value;
    _____ next; // pointer to the next element
} sll_node;
```

3.2 Let's convert the linked list to an array. Fill in the missing code.

```
int* to_array(sll_node *sll, int size) {
    int i = 0;
    int *arr = _____;
    while (sll) {
        arr[i] = _____;
        sll = _____;
        _____;
    }
    return arr;
}
```

3.3 Finally, complete the function `delete_even()` that will delete every second element of the list. For example, given the lists below:

Before: Node 1 → Node 2 → Node 3 → Node 4

After: Node 1 → Node 3

Calling `delete_even()` on the list labeled "Before" will change it into the list labeled "After". All list nodes were created via dynamic memory allocation.

```
void delete_even(sll_node *sll) {
    sll_node *temp;
    if (!sll || !sll->next) {
        return;
    }
    temp = _____;
    sll->next = _____;
    free(_____);
    delete_even(_____);
}
```

4 Floating Point Intro

The IEEE standard defines a binary representation for floating point using **sign**, **exponent**, and **mantissa**.

Sign	Exponent	Significand
1 bit	8 bits	23 bits

For normalized floats:

$$\text{Value} = (-1)^{\text{Sign}} \times 2^{(\text{Exponent} - \text{Bias})} \times 1.\text{significand}_2$$

For denormalized floats:

$$\text{Value} = (-1)^{\text{Sign}} \times 2^{(\text{Exponent} - \text{Bias} + 1)} \times 0.\text{significand}_2$$

Exponent	Significand	Meaning
0	Anything	Denorm
1-254	Anything	Normal
255	0	Infinity
255	Nonzero	NaN

- 4.1 (a) How would 10.625 be represented in floating point format?
- (b) What decimal number is encoded as 0xC0A80000?
- (c) How many non-negative floats are strictly less than 2?
- (d) What is the smallest positive value that can be stored using a single precision float?

5 More Floating Point (Sp18 Final)

- 5.1 IEEE 754-2008 introduces half precision, which is a binary floating-point representation that uses 16 bits: 1 sign bit, 5 exponent bits (with a bias of 15) and 10 significand bits. This format uses the same rules for special numbers that IEEE754 uses. Considering this half-precision floating point format, answer the following questions:
- (a) For 16-bit half-precision floating point, how many different valid representations are there for NaN?
 - (b) What is the smallest positive non-infinite number it can represent? You can leave your answer as an expression.
 - (c) What is the largest non-infinite number it can represent? You can leave your answer as an expression.
 - (d) How many floating point numbers are in the interval $[1, 2)$ (including 1 but excluding 2)?