Chapter 8. Optimization (Part 4)

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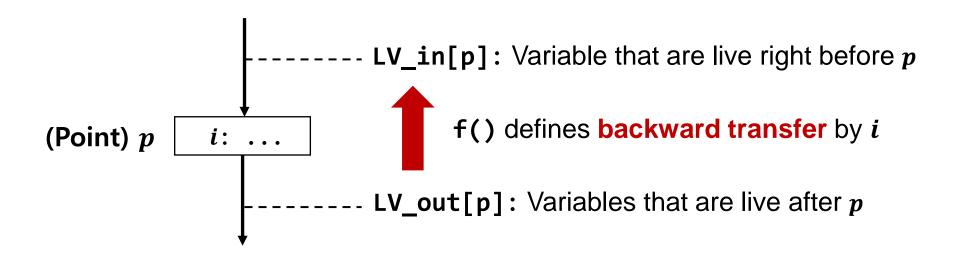
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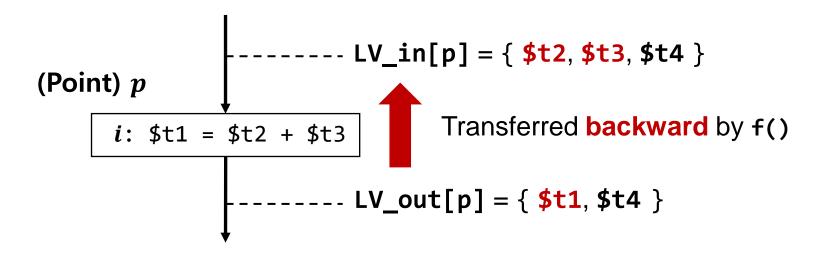
Liveness Analysis: Transfer Function

- Note that liveness analysis must be performed backward
 - Start from the exit node and goes backward
- Therefore, the transfer function must define the input live variables in terms of the output live variables
 - For point p with instruction i: LV_in[p] = f(LV_out[p], i)



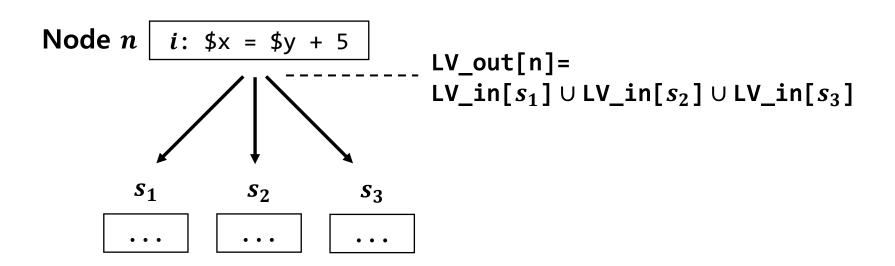
Liveness Analysis: Transfer Function

- For instruction i, let's introduce the following two sets:
 - def(i) denotes the set of registers defined by i
 - use(i) denotes the set of registers used by i
 - Ex) def("\$t1 = \$t2 + \$t3") = { \$t1 }
 - Ex) use("\$t1 = \$t2 + \$t3") = { \$t2, \$t3 }
- Now we can define: $f(LV, i) = LV def(i) \cup use(i)$



Liveness Analysis: Propagation

- If a variable is *live before* a certain node, then it is also *live after* its predecessors
- Therefore, live variables after node n can be obtained by joining the live variables before the successors of n
 - These live variables must be joined with union (U)



Liveness Analysis: Iterative Algorithm

- Now we can put things together and run the following iterative algorithm (a.k.a. fixpoint algorithm)
 - There can be variations of algorithm, but the basic idea is same

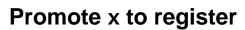
```
for each node n { LV_in[n] = Ø; }
while (there is any change to LV_in[]) {
  for each node n and its instruction i {
    LV_out[n] = U_{s \in succ(n)} LV_in[s];
    LV_in[n] = f(LV_out[n],i);
  }
}
```

Optimization with Memory?

- Recall that compilers focus on optimizing register computations, and usually ignore variables in memory
- For example, let's consider *dead-store elimination:*
 - Why don't we remove a store instruction if it is dead?
 - Unfortunately, it is not trivial to decide whether a store updates a variable that is not going to be used anymore
 - It requires the compiler to analyze which memory addresses can be accessed by each load and store
- As a result, real-world compilers usually perform only limited form of dead-store elimination
 - By targeting trivial and obvious patterns

Mem2Reg Optimization

- Mem2Reg optimization moves some variables from the memory to register (a.k.a., *promotion* to register)
 - Once it is promoted, various optimizations can be applied
 - Ex) Consider C code "int x = 100; x = x + 1;"





$$%x = 100$$

 $$t1 = %x + 1$

$$%x = $t1$$

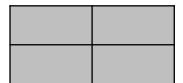
Memory

2000	101

Registers

\$t1	2000
•••	• • •

Memory

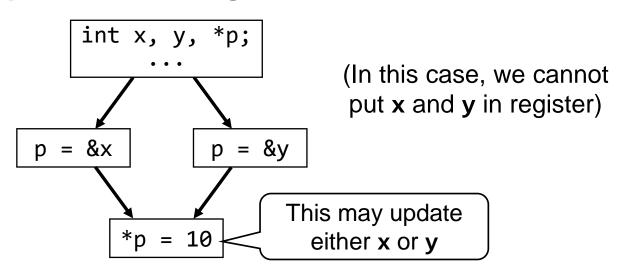


Registers

%x	101
• • •	• • •

Mem2Reg Optimization

- Of course, not all variables can be promoted to register
 - Compiler must carefully decide which variables can be promoted
- Array type variables cannot be promoted to register
 - Ex) int arr[16]; // We cannot put this in register
- Pointer operations also disqualify some variables from the promotion to register



Appendix

Constant Folding + Propagation

- Part 1 slide mentioned advanced form of optimization for "constant folding + constant propagation" at once
 - Unfortunately, we don't have time to discuss it in this course
 - If you are interested, read Chapter 9.4 of our textbook*
 - Sometimes, we can reduce the number of repetition by making each optimization pass smarter
 - For example, we may perform constant folding and constant propagation at once (we will see such optimization later)