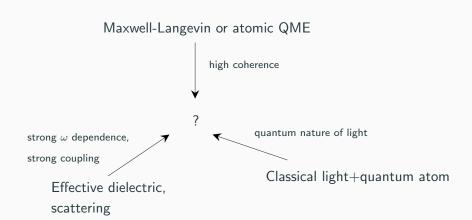
Cavity QED

Quantum light-matter interaction to the extreme

Jinyuan Wu

April 13, 2024

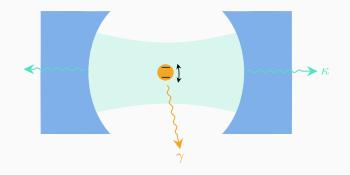
When do all effective theories of light or matter fail?



One scenario: in a cavity.

Cavity and one atom

Cavity quantum electrodynamics (cavity QED)



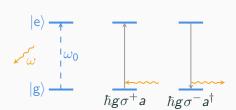
Coupling with the environment

- ullet Cavity leaking κ
- \bullet Atomic spontaneous emission rate (outside the cavity) γ
- (Possible non-radiative decay: phonon, etc.)

Small $\kappa, \gamma, \ldots \Rightarrow$ closed-system cavity QED

Jaynes-Cummings model

- No atom-atom interaction
- Rotating-wave approx.
- Single active photon mode
- No damping at all



$$H^{\mathsf{Jaynes\text{-}Cummings}} = \hbar\omega\left(a^\dagger a + \frac{1}{2}\right) + \frac{\hbar\omega_0}{2}\sigma^z + \hbar g(a\sigma^+ + a^\dagger\sigma^-)$$

Possible coherent state driving $\omega_0 \to \Delta = \omega_0 - \omega_{\mathsf{drive}}$

Quantum Rabi oscillation

Quantum nature of the model

 $\bullet \;\; |e\rangle \stackrel{\mathsf{Spontaneous}\;\mathsf{emission}}{\to} \; |g\rangle \; \mathsf{(but\;not\;irreversible)}$

Dressed state $H^{\text{Jaynes-Cummings}}$ in $\{|g, n+1\rangle, |e, n\rangle\} =$

$$\hbar\omega\left(n+\frac{1}{2}\right)-\frac{\hbar\omega_0}{2}+\begin{pmatrix}\hbar\omega&\hbar g\sqrt{n+1}\\\hbar g\sqrt{n+1}&\hbar\omega_0\end{pmatrix}$$

- Starting with |e>
- Markovian approx. fails

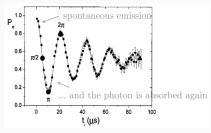


Fig. from S Haroche et al., RMP 73 565 (2001)

Collapse and revival

What happens when we start with $|e, \alpha\rangle$?

$$\begin{aligned} |\psi(t=0)\rangle &= |e\rangle \otimes e^{-\frac{|\alpha|^2}{2}} \sum_{n=0}^{\infty} \frac{\alpha^n}{\sqrt{n!}} \\ \Rightarrow P_{e}(t) &= \frac{1}{2} \left[1 + e^{-|\alpha|^2} \sum_{n=0}^{\infty} \frac{|\alpha|^{2n}}{n!} \cos(\Omega_n t) \right]. \end{aligned}$$

Generalizations

Medium

Medium within cavity?