Time-dependent adiabatic GW

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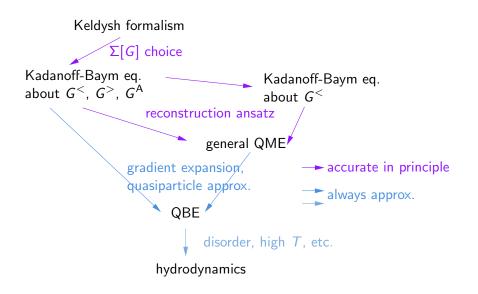
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Relation between formalisms



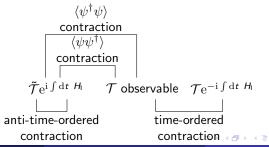
Non-equilibrium Green function

Motivation

$$\langle A \rangle = \langle S^{-1} \mathcal{T}_t(SA_I(t)) \rangle, \quad S = U(\infty, -\infty)$$
 (1)

Non-equilibrium state: not pure; contains excited state components; $|\Psi_n\rangle$ is excited state $\Rightarrow S |\Psi_n\rangle \neq \mathrm{e}^{\mathrm{i}\,\alpha} |\Psi_n\rangle \Rightarrow$ we can't peel the S^{-1} off!!

Solution Four (instead of one) types of propagators: (note S^{-1} is *anti*-time ordered)

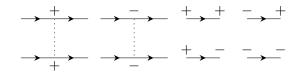


Keldysh formalism

Four types of (fermionic) propagators

$$\begin{split} &\mathrm{i}\,G^{--}=\mathrm{i}\,G^{\mathrm{c}}=\,\langle\mathcal{T}\,\psi_{1}\psi_{2}^{\dagger}\rangle\,,\quad\mathrm{i}\,G^{++}=\mathrm{i}\,G^{\mathrm{a}}=\,\langle\tilde{\mathcal{T}}\psi_{1}\psi_{2}^{\dagger}\rangle\,,\\ &\mathrm{i}\,G^{+-}=\mathrm{i}\,G^{>}=\,\langle\psi_{1}\psi_{2}^{\dagger}\rangle\,,\quad\mathrm{i}\,G^{-+}=\mathrm{i}\,G^{<}=-\,\langle\psi_{2}^{\dagger}\psi_{1}\rangle\,. \end{split} \tag{2}$$

Diagrams

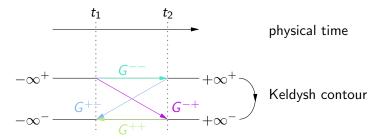


Self-energy

$$G = \begin{pmatrix} G^{--} & G^{-+} \\ G^{+-} & G^{++} \end{pmatrix}, \quad \Sigma = \begin{pmatrix} \Sigma^{--} & \Sigma^{-+} \\ \Sigma^{+-} & \Sigma^{++} \end{pmatrix}, \quad G = G_0 + G_0 \Sigma G. \quad (3)$$

Alternative formulation: Keldysh contour

Keldysh contour The information in the G matrix can be alternatively stored in a time-ordered Green function on *Keldysh contour*



Green function EOM

From Keldysh contour to physical contour Lengreth theorem:

$$(AB)^{<} = A^{R}B^{<} + A^{<}B^{A}, \quad (AB)^{>} = A^{R}B^{>} + A^{>}B^{A},$$

 $(AB)^{R} = A^{R}B^{R}, \quad (AB)^{A} = A^{A}B^{A},$
(4)

where

$$A^{>}(t_{1}, t_{2}) = A(t_{1}^{+}, t_{2}^{-}), \quad A^{<}(t_{1}, t_{2}) = A(t_{1}^{-}, t_{2}^{+}),$$

$$A^{R}(t_{1}, t_{2}) = \theta(t_{1} - t_{2})(A^{>} - A^{<}),$$

$$A^{A}(t_{1}, t_{2}) = -\theta(t_{1} - t_{2})(A^{>} - A^{<}).$$
(5)

Mapping an equation on Keldysh contour to its counterpart on the physical time axis!

Derivation of EOM of $G^{<,>}$ and G^A I

Recommended references The following series:

- Václav Špička, Bedřich Velický, and Anděla Kalvová. "Long and short time quantum dynamics: I. Between Green's functions and transport equations". In: *Physica E: Low-dimensional Systems and Nanostructures* 29.1-2 (2005), pp. 154–174
- Jørgen Rammer and H Smith. "Quantum field-theoretical methods in transport theory of metals". In: Reviews of modern physics 58.2 (1986), p. 323

Derivation of EOM of $G^{<,>}$ and G^A II

From self-energy correction to EOM From Lengreth theorem:

$$G = G_0 + G_0 \Sigma G \Rightarrow G^{<} = G_0^{<} + G_0^{<} \Sigma^{A} G^{A} + G_0^{R} \Sigma^{R} G^{<} + G_0^{R} \Sigma^{<} G^{A},$$
 (6)

$$G = G_0 + G\Sigma G_0 \Rightarrow G^{<} = G_0^{<} + G_0^R \Sigma^R G_0^{<} + G^R \Sigma^{<} G_0^A + G^{<} \Sigma^A G^A,$$
 (7)

$$G^{A} = G_{0}^{A} + G_{0}^{A} \Sigma^{A} G^{A}, \quad G^{R} = G_{0}^{R} + G_{0}^{R} \Sigma^{R} G^{R}.$$
 (8)

Getting rid of G_0 We define

$$G_0^{-1} := i \, \partial_t - H_0, \tag{9}$$

and

$$G_0^{-1}G_0^{A,R} = I, \quad G_0^{-1}G_0^{<,>} = 0.$$
 (10)

Taking complex conjugate of the def. of $G_0^{<,>}$ we find (left arrow = apply ∂_t and H_0 to the second index of $G_0^{<,>}$)

$$G_0^{<,>}(-i\overleftarrow{\partial_{t_2}} - H_0) = 0.$$
 (11)

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Derivation of EOM of $G^{<,>}$ and G^A III

The Schrödinger-like Kadanoff-Baym eq. Applying G_0^{-1} to the left of (6) and to the right of (7):

$$(i \partial_{t_1} - H_0)G^{<}(1,2) = \Sigma^{\mathsf{R}}G^{<} + \Sigma^{<}G^{\mathsf{A}},$$
 (12)

$$-i \partial_{t_2} G^{<}(1,2) - G^{<} H_0 = G^{\mathsf{R}} \Sigma^{<} + G^{<} \Sigma^{\mathsf{A}}, \tag{13}$$

$$\Rightarrow i(\partial_{t_1} + \partial_{t_2})G^{<} - [H_0, G^{<}] = \Sigma^{R}G^{<} + \Sigma^{<}G^{A} - G^{R}\Sigma^{<} - G^{<}\Sigma^{A}.$$
 (14)

Mixed coordinates We define "average time" and "relative time":

$$T = \frac{t_1 + t_2}{2}, \quad t = t_1 - t_2,$$
 (15)

$$\Rightarrow \frac{\partial}{\partial T} = \frac{\partial}{\partial t_1} + \frac{\partial}{\partial t_2}.$$
 (16)

We then do Fourier transform over t: similar to the equilibrium case. ($T \simeq \text{driving}$, $t \simeq \text{internal time evolution}$)

Towards a single-time formalism

Summary up to now

• Accurate EOMs about $G^{A,R}$, and EOM of $G^{<}$:

$$i \partial_{\mathcal{T}} G^{<} - [H_0, G^{<}] = \Sigma^{R} G^{<} + \Sigma^{<} G^{A} - G^{R} \Sigma^{<} - G^{<} \Sigma^{A}.$$
 (17)

The RHS contains t (or ω) and $G^{<}$.

• Note: we can actually put the t=0 part of Σ into $H_0! \Rightarrow$ Example: COHSEX TD-aGW

Goal Obtaining quantum kinetics:

- Quantum master equation (QME), i.e. EOM of $\rho(\mathbf{r}_1, \mathbf{r}_2, t)$,
- and its downfolded version (in long wave length, well-defined quasiparticle limit), the quantum Boltzmann equation (QBE)

Problem Both LHS and RHS contain ω : problem too large. What we want Obtaining a close form EOM about $G^{<}(T, t=0)$

Quantum master equation

Reduced density matrix Single-electron density matrix:

$$i \rho(T) = G^{<}(T, t = 0) = \int \frac{d\omega}{2\pi} G^{<}(T, \omega)$$
 (18)

What we want Two types of reduction:

- Reducing Σ to an easy function of G, ideally $G^{<}$
- Reducing $G^{<}$ to $\rho(T)$

Reducing Σ

- Always possible: we can formally eliminate χ, ϵ , etc. from Hedin eq. and get a Σ about G i.e. about $G^{<}, G^{A,R}$
- But then $G^{A,B}$ can be eliminated with (8) as well
- In reality: a truncation is needed . . .

Reconstruction of $G^{<}$ from ρ

Reconstruction theorem From ρ , $G^{A,R}$ (which can be calculated using (8) from ρ), $G^{<}$ can be completely restored¹

Constructive proof See (71) in the reference; note that

$$(G^{R})^{-1}\theta(t_{1}-t_{2})G^{<} = (\partial_{t_{1}}-H_{0}-\Sigma^{R})\theta(t_{1}-t_{2})G^{<}$$

$$= \delta(t_{1}-t_{2})G^{<} + \theta(t_{1}-t_{2})(\partial_{t_{1}}-H_{0}-\Sigma^{R})G^{<}$$

$$= \rho(t_{1}) + \cdots$$
(19)

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¹Václav Špička, Bedřich Velickỳ, and Anděla Kalvová. "Long and short time quantum dynamics: I. Between Green's functions and transport equations". In: *Physica E: Low-dimensional Systems and Nanostructures* 29.1-2 (2005), pp. 154–174.

Quantum master equation as an accurate formalism

Existence of accurate quantum master equation In conclusion, in principle we can always write down something accurate like this:

$$\frac{\partial \rho}{\partial t} + i [H_0, \rho] = \int_{-\infty}^{t} F[\rho(t')] dt', \qquad (20)$$

where F is obtained from $\Sigma^{\mathsf{R}} G^< + \Sigma^< G^{\mathsf{A}} - G^{\mathsf{R}} \Sigma^< - G^< \Sigma^{\mathsf{A}}$, and $G^{\mathsf{R},\mathsf{A}}$ is reconstructed from ρ by doing a complete self-energy run, and $G^<$ is reconstructed from G^{A} and G^{R} and ρ .

... but of course simplification is needed

Gradient expansion: first step from QME to QBE

Mixed coordinates

$$\tilde{\rho}(\boldsymbol{p}, \boldsymbol{X}, t) = \int dx e^{-i\boldsymbol{p}\cdot\boldsymbol{x}} \rho\left(\boldsymbol{X} + \frac{\boldsymbol{x}}{2}, \boldsymbol{X} - \frac{\boldsymbol{x}}{2}, t\right), \tag{21}$$

$$\frac{1}{\mathsf{i}}\widetilde{[H_0,\rho]} = \frac{\partial \epsilon}{\partial \mathbf{p}} \cdot \frac{\partial \widetilde{\rho}}{\partial \mathbf{X}} - \frac{\partial \epsilon}{\partial \mathbf{X}} \cdot \frac{\partial \widetilde{\rho}}{\partial \mathbf{p}} + \cdots$$
 (22)

Gradient expansion Only take the first two terms: assuming no higher dependence

Issue: the definitions of G_0 and Σ

Ambiguity in the meaning of Σ

- In ordinary usage: G_0 directly from H_0
- But some prefer to move a part of Σ that looks like "effective potential" into H_0 ...
- G_0 contains "interactively corrected band structure"; Σ contains "scattering" what is the distinction?

Comparison with similar issue in QBE

- When impurities are rare: they appear in collision integral
- When impurities are abundant: they lead to an impurity band ... and appear in the diffusion term?
- In QBE: it depends on the shape of the spectral function . . .

Lacking proof of equivalence

• Do different division of labor between Σ and G_0 lead to consistent results?

A radical move towards quantum Boltzmann equation I

Approximations leading to QBE

• Smooth $U_{\text{ext}} \Rightarrow \text{Gradient expansion}$:

$$[H_0, \rho] \longrightarrow i \left(\frac{\partial \epsilon}{\partial \boldsymbol{p}} \cdot \frac{\partial \tilde{\rho}}{\partial \boldsymbol{X}} - \frac{\partial \epsilon}{\partial \boldsymbol{X}} \cdot \frac{\partial \tilde{\rho}}{\partial \boldsymbol{p}} + \cdots \right). \tag{23}$$

Weakly correlated states ⇒ Quasiparticle approx.:

$$G^{<}(\boldsymbol{X},\boldsymbol{p},T,\omega) = i\underbrace{2\pi\delta(\omega - \xi_{\boldsymbol{p}} + \mu - U(\boldsymbol{X},T))}_{A(\boldsymbol{X},\boldsymbol{p},T,\omega)} f(\boldsymbol{p},\boldsymbol{X},T), \quad (24)$$

$$G^{>}(\boldsymbol{X},\boldsymbol{p},T,\omega) = -i A(\boldsymbol{X},\boldsymbol{p},T,\omega)(1-f(\boldsymbol{p},\boldsymbol{X},T)).$$
 (25)

This makes sense: we then have

$$A = i(G^{R} - G^{A}) = i(G^{>} - G^{<}).$$
 (26)

ullet Gradient expansion in time domain \Rightarrow Markovian collision integral

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A radical move towards quantum Boltzmann equation II

Note

- The conditions are sufficient, but not necessary: in the formalism above, field renormalization (as in electron-phonon interaction) is not included, but by correcting the collision term (essentially, a mild breakdown of Fermi golden rule), a Boltzmann equation can still be established (with necessary corrections).
- The first condition and the rest two conditions are orthogonal: the first condition can also be used in QME: it gives the diffusion part of QBE
- The second and third conditions are used to simply the interactive RHS into the collision integral

A radical move towards quantum Boltzmann equation III

Convolution in Green function EOM

$$AB := \int d2 A(1,2)B(2,3).$$
 (27)

Gradient expansion, in r **and** t Taking Taylor expansion in (r, t)

$$AB|_{\mathbf{X},\mathbf{p},T,\omega} = A_{\mathbf{X},\mathbf{p},T,\omega}B_{\mathbf{X},\mathbf{p},T,\omega} + \frac{i}{2}\left(\frac{\partial A}{\partial \mathbf{X}} \cdot \frac{\partial B}{\partial \mathbf{p}} - \frac{\partial A}{\partial \mathbf{p}} \cdot \frac{\partial B}{\partial \mathbf{X}} - \frac{\partial A}{\partial T} \frac{\partial B}{\partial \omega} + \frac{\partial A}{\partial \omega} \frac{\partial B}{\partial T}\right) + \cdots$$
(28)

We only keep the terms shown above.

 \Rightarrow [G $^{<}$, H_0] reduces to the diffusion term seen in QBE

Multi-band, spin index, etc. When we have discrete labels in A, B, \ldots , quantities in (28) are matrices with these discrete indices

A radical move towards quantum Boltzmann equation IV

Prototype of the collision integral Keeping only the first term in gradient expansion (28):

$$\Sigma^{R}G^{<} + \Sigma^{<}G^{A} - G^{R}\Sigma^{<} - G^{<}\Sigma^{A}$$

$$\stackrel{\text{gradient exp.}}{\approx} G^{<}(\Sigma^{R} - \Sigma^{A}) - (G^{R} - G^{A})\Sigma^{<}$$

$$= G^{<}\Sigma^{>} - G^{>}\Sigma^{<}$$

$$\stackrel{\text{QP approx.}}{\approx} i Af(\mathbf{p}) \operatorname{Im} \Sigma - \operatorname{incoming terms}$$
(29)

- Second line: the commutator terms assume the same form as that of (28), but are an order of magnitude smaller than it.
- Third line: from $A^R A^A = A^> A^<$
- The quasiparticle approximation (24) \Rightarrow introduction of $f(\mathbf{p})$; the "out" part $\propto \operatorname{Im} \Sigma$ (Im Σ generally is even not well-defined)

A radical move towards quantum Boltzmann equation V

Obtaining the collision integral

LHS =
$$i \partial_{T} G^{<} - i \left(\frac{\partial H_{0}}{\partial \mathbf{X}} \cdot \frac{\partial G^{<}}{\partial \mathbf{p}} - \frac{\partial H_{0}}{\partial \mathbf{p}} \cdot \frac{\partial G^{<}}{\partial \mathbf{X}} \right),$$
 (30)

where the $-\frac{\partial H_0}{\partial T}\frac{\partial G^<}{\partial \omega}+\frac{\partial H}{\partial \omega}\frac{\partial G^<}{\partial T}$ terms vanish when H_0 contains no strong time dependence.

$$RHS = G^{\langle}\Sigma[i G^{\rangle}] - G^{\rangle}\Sigma[i G^{\langle}].$$
 (31)

 $G^<$ appears in the LHS once, so there is a $2\pi\,\mathrm{i}\,\delta(\omega-H)$ factor in the LHS; in the RHS suppose $\Sigma\sim G^n$, then the normalization factor coming with G is $(2\pi\,\mathrm{i}\,\delta(\omega-H))^{n+1}$; but since there are n propagators in Σ , we have n-1 frequency integrals connecting them to the "skeleton" of Σ , each with a factor of $1/2\pi$, so finally there is a $2\pi\delta(\omega-H)$ factor in the

A radical move towards quantum Boltzmann equation VI

RHS, which exactly is the factor seen in Fermi golden rule. The imaginary units always cancel each other finally.

Example: disorder self-energy The self-energy is

$$-i\Sigma(\boldsymbol{p},\omega) = \sum_{\boldsymbol{q}} -\frac{1}{V}c|v(\boldsymbol{q}-\boldsymbol{p})|^{2} \cdot iG(\boldsymbol{q},\omega), \quad (32)$$

where each dotted line corresponds to $-i gv(\boldsymbol{q} - \boldsymbol{p})/\sqrt{V}$, and c comes from averaging over the distribution of disorders.

The equation becomes

$$i \partial_{\mathcal{T}} G^{<} - i \left(\frac{\partial H_{0}}{\partial \mathbf{X}} \cdot \frac{\partial G^{<}}{\partial \mathbf{p}} - \frac{\partial H_{0}}{\partial \mathbf{p}} \cdot \frac{\partial G^{<}}{\partial \mathbf{X}} \right)$$

$$= \frac{1}{V} \sum_{\mathbf{q}} c |v(\mathbf{p} - \mathbf{q})|^{2} (G^{<}(\mathbf{p}) \cdot G^{>}(\mathbf{q}) - G^{>}(\mathbf{p}) \cdot G^{<}(\mathbf{q})),$$
(33)

A radical move towards quantum Boltzmann equation VII

and thus from quasiparticle approximation (f and A also depend on X, T)

$$\frac{\mathrm{d}}{\mathrm{d}T}A(\boldsymbol{p})f(\boldsymbol{p}) = \int \frac{\mathrm{d}^{d}\boldsymbol{q}}{(2\pi)^{d}}c|v(\boldsymbol{p}-\boldsymbol{q})|^{2}A(\boldsymbol{p})f(\boldsymbol{p})\cdot(-A(\boldsymbol{q}))(1-f(\boldsymbol{q}))+\boldsymbol{p}\leftrightarrow\boldsymbol{q},$$
(34)

and integrating over ω we get

$$\frac{\mathrm{d}}{\mathrm{d}T}f(\mathbf{p}) = \int \frac{\mathrm{d}^{d}\mathbf{q}}{(2\pi)^{d}}c|\nu(\mathbf{p}-\mathbf{q})|^{2}(-2\pi)\delta(\epsilon_{\mathbf{p}}-\epsilon_{\mathbf{q}})f(\mathbf{p})(1-f(\mathbf{q})) + \mathbf{p} \leftrightarrow \mathbf{q},$$
(35)

which is exactly what is obtained by intuitively inserting Fermi golden rule to the RHS of QBE.

Comments on derivation of QBE

The role of the assumptions

- Gradient expansion does most of the heavy lifting job
- Quasiparticle approximation is used to write down an explicit collision integral
- The locality of the collision integral comes from gradient expansion on the temporal domain as well

Phenomenon covered

- Exciton is multi-band phenomenon, but multi-band QBE can be established; see Lifshitz's Statistical Physics: Theory of the Condensed State, §5 for a magnetic field-induced exciton
- Plasmon comes from long-range divergence of Hartree term (in BerkeleyGW the $\mathbf{q}=0, \mathbf{G}=0$ part is omitted)

A little beyond the quasiparticle approximation

 ω dependence in Σ , no damping \Rightarrow QBE with field renormalization.²

Example: electron-phonon interaction Renormalized QBE:

$$(\partial_{T} + \nabla_{\boldsymbol{p}} E_{\boldsymbol{p}} \cdot \nabla_{\boldsymbol{R}} - \nabla_{\boldsymbol{R}} (E_{\boldsymbol{p}} + e\varphi) \cdot \nabla_{\boldsymbol{p}}) n_{\boldsymbol{p}}$$

$$= -2\pi \int \frac{\mathrm{d}^{3} \boldsymbol{p}'}{(2\pi)^{3}} Z_{\boldsymbol{p}} Z_{\boldsymbol{p}'} |g_{\boldsymbol{p}-\boldsymbol{p}'}|^{2}$$

$$\times (n_{\boldsymbol{p}} (1 - n_{\boldsymbol{p}'}) (1 + N(E_{\boldsymbol{p}} - E_{\boldsymbol{p}'})) - n_{\boldsymbol{p}'} (1 - n_{\boldsymbol{p}}) N(E_{\boldsymbol{p}} - E_{\boldsymbol{p}'}))$$

$$\times (\delta(E_{\boldsymbol{p}} - E_{\boldsymbol{p}'} - \omega_{\boldsymbol{p}-\boldsymbol{p}'}) - \delta(E_{\boldsymbol{p}} - E_{\boldsymbol{p}'} + \omega_{\boldsymbol{p}-\boldsymbol{p}'}))$$
(36)

⇒ Fermi golden rule is not accurate when field renormalization is strong Another example: DMFT QBE³

² Jørgen Rammer and H Smith. "Quantum field-theoretical methods in transport theory of metals". In: *Reviews of modern physics* 58.2 (1986), p. 323.

³Michael Wais et al. "Quantum Boltzmann equation for strongly correlated systems: Comparison to dynamical mean field theory". In: *Physical Review B* 98.13 (2018), p. 134312.

QBE in crystal

In crystal:

- If we work in r representation, u_{nk} means the relation between r and k is not simply Fourier transform; we can't define f(X, p) directly from Wigner transform.
- ullet If we work in ${m k}$ representation, no well-defined ${m r}$ is initially given.

Solution

- Working in k representation; expanding $\varepsilon_{nk} + er \cdot E$ in this basis;
- TODO: prove that i $\partial_{\pmb{k}}$ is indeed the \pmb{r} appearing in electric field; after Wigner transform in \pmb{k} space, recover $\epsilon_{n\pmb{k}} + e(\pmb{r} + \pmb{A}) \cdot \pmb{E}$
- From semi-conservation law of ${\bf k}$ we get localized collision integral in RHS; the matrix elements of the screened Coulomb interaction are evaluated in $\psi_{n{\bf k}}$ basis as well.

BSE and single-electron kinetic theory

BSE for second-order correlation

Bethe-Salpeter equation (BSE)

$$= + | \mathcal{K} |$$
 (37)

What we need Linear response of single-electron under external field = BSE (simplest single-electron theory: QBE)

Next step: relation between K and Σ

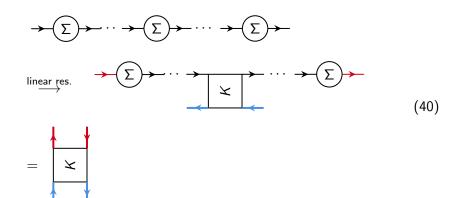
Linking Σ with K

Linear response of a single self-energy diagram



Linking Σ with K

Whole picture



Linking Σ with K

Example: linear response from time-dependent GW = BSE

$$\Sigma = \begin{array}{c} & & & & & \\ & & & & \\ & & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & & \\ & & \\ & & & \\$$

- First term = Electron Hartree term = Electron direct term = Exciton exchange term; +1 prefactor;
- Second term = Electron Fock term = Electron exchange term = Exciton direct term; (-1) prefactor.

Summary of formalisms

- Keldysh formalism (TODO: subtleties in initial correlation)
 - In principle we can get a closed equation system (with retardation) about G and hence G[<];
 - in practice $\Sigma[G]$ has to be truncated; n corrected propagator in $\Sigma=n$ -order non-trivial correlation
- ullet \Rightarrow ...and hence a (highly complicated) accurate quantum master equation
 - G needs to be reconstructed from ρ : reconstruction formalism
 - Issue: how to decide the division of labor between H_0 and Σ , when no physical pictures like "distinction between diffusion and collision" are available?
- Boltzmann formalism
 - Approximation 1: gradient expansion
 - Approximation 2: well-defined quasiparticle
 - Slight violation of approx. 2 (e.g. Z renormalization factor): Fermi golden rule no longer 100 % correct
- QBE ⇒ hydrodynamics with random fluctuation

Time-dependent adiabatic GW

Overview

- ("Adiabatic") approximation for Σ : static limit of GW (i.e. t=0) =: static COHSEX
- In linear limit: W doesn't change \Rightarrow only high-order correlation taken into account is the ladder approximation using static screening = static screening BSE
- Σ has no $t \neq t'$ components $\Rightarrow \Sigma$ can be placed into $H_0 \Rightarrow \mathsf{TD}\text{-aGW}$ usually carried out in QME framework

Introduction to COHSEX

Example:

