

Trion ARPES signature

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1 ARPES theory

When the probe is much weaker than the pump and does not itself influence the electronic structure, the most generic theory of driven ARPES is based on the pumped single-electron lesser Green function, to which the pump adds a self-energy correction, [1, 2]; the theory reduced to the usual Fermi golden rule when the pump itself is weak [3, 4]. When the pump pulse is strong at its peak but has faded away at the probing time, the main effect of pumping is preparing an initial state, and the ARPES intensity can be evaluated from pure-state first-order time dependent perturbation theory, which gives a Fermi golden rule-like final result [5]. Here we generalize the methodology in [5] to all possible exciton states caused by the pump and not just excitons.

2 Two-band model for trion

In this work, we generalize the two-band model approach to trions [6] to the indirect band gap case. We start with the following example.

$$H = \frac{(\mathbf{k}_e - \mathbf{w})^2}{2m_e} + E_g + \frac{\mathbf{k}_{h1}^2}{2m_h} + \frac{\mathbf{k}_{h2}^2}{2m_h} + V(\mathbf{r}_{h1} - \mathbf{r}_{h2}) - V(\mathbf{r}_e - \mathbf{r}_{h1}) - V(\mathbf{r}_e - \mathbf{r}_{h2}). \quad (1)$$

Here \mathbf{k}_{hi} is the crystal momentum of the quantum state containing hole i only, which is the opposite of the momentum of the corresponding electron state of the hole; similarly, $\mathbf{k}^2/2m_h$ is the opposite of the dispersion relation of the valence band top, and therefore $m_h > 0$.

It can be easily seen that the total momentum of the trion

$$\mathbf{P} = \mathbf{k}_e + \mathbf{k}_{h1} + \mathbf{k}_{h2} \quad (2)$$

is conserved, and we are to rewrite the Hamiltonian in terms of the total momentum, which should only appear in the total kinetic energy term, and two internal degrees of freedom. Following the procedure in [6], we define

$$\mathbf{r}_1 = \mathbf{r}_{h1} - \mathbf{r}_e, \quad \mathbf{r}_2 = \mathbf{r}_{h2} - \mathbf{r}_e \quad (3)$$

as the internal degrees of freedom. To separate the Hamiltonian into terms about \mathbf{P} and terms about the internal degrees of freedom, we need to find the canonical coordinate corresponding to \mathbf{P} and the canonical momenta corresponding to $\mathbf{r}_{1,2}$.

Regarding the canonical coordinate corresponding to \mathbf{P} , intuitively we may choose the center of mass

$$\mathbf{R} = \frac{m_e \mathbf{r}_e + m_h \mathbf{r}_{h1} + m_h \mathbf{r}_{h2}}{M}, \quad M = m_e + 2m_h \quad (4)$$

as the canonical coordinate corresponding to \mathbf{P} ; this correctness of this choice can be directly verified by writing $\mathbf{R}, \mathbf{r}_1, \mathbf{r}_2$ as functions of $\mathbf{r}_e, \mathbf{r}_{h1}, \mathbf{r}_{h2}$ and verifying that $\partial_{\mathbf{R}}$ is the sum of $\partial_{\mathbf{r}_e}$, $\partial_{\mathbf{r}_{h1}}$ and $\partial_{\mathbf{r}_{h2}}$, and hence $\mathbf{P} = -i\hbar\partial_{\mathbf{R}}$ is indeed the total momentum.

We can define the canonical momenta of $\mathbf{r}_{1,2}$, hereafter referred to as $\mathbf{k}_{1,2}$, as $-i\hbar\partial_{\mathbf{r}_{1,2}}$; in this way

$$\mathbf{k}_e = \frac{m_e}{M} \mathbf{P} - \mathbf{k}_1 - \mathbf{k}_2, \quad \mathbf{k}_{h1,2} = \mathbf{k}_{1,2} + \frac{m_h}{M} \mathbf{P}, \quad (5)$$

and the kinetic energy part of the (1) now reads

$$H_{\text{kin}} = \frac{(\mathbf{P} - \mathbf{w})^2}{2M} + E_g + \frac{\mathbf{k}_1^2}{2m_h} + \frac{\mathbf{k}_2^2}{2m_h} - \frac{\mathbf{w}^2}{2M} + \frac{(\mathbf{k}_1 + \mathbf{k}_2 + \mathbf{w})^2}{2m_e}. \quad (6)$$

We however want to shift the definitions of \mathbf{k} so that the kinetic part resembles the kinetic energy in a direct band gap system. By redefining

$$\mathbf{k}_{1,2} = -i\hbar\mathbf{r}_{1,2} + \frac{\mathbf{w}}{1 + m_e/\mu}, \quad \mu = \frac{m_e m_h}{m_e + m_h}, \quad (7)$$

and therefore

$$\mathbf{k}_e = \frac{m_e}{M}\mathbf{P} + \frac{2m_h\mathbf{w}}{M} - \mathbf{k}_1 - \mathbf{k}_2, \quad \mathbf{k}_{h1,2} = \mathbf{k}_{1,2} - \frac{m_h\mathbf{w}}{M} + \frac{m_h}{M}\mathbf{P}, \quad (8)$$

the total Hamiltonian now reads

$$H = \frac{(\mathbf{P} - \mathbf{w})^2}{2M} + E_g + \frac{\mathbf{k}_1^2}{2m_h} + \frac{\mathbf{k}_2^2}{2m_h} + \frac{\mathbf{k}_1 \cdot \mathbf{k}_2}{2m_e} + V(\mathbf{r}_1 - \mathbf{r}_2) - V(\mathbf{r}_1) - V(\mathbf{r}_2). \quad (9)$$

The redefinition of $\mathbf{k}_{1,2}$ does not change the commutation relation between $\mathbf{r}_{1,2}$ and $\mathbf{k}_{1,2}$. We find that the internal part of the Hamiltonian has the same form as the Hamiltonian in [6].

3 Variational wave function

The spin part is in a singlet state, and therefore the orbital part of the wave function is symmetric.

An immediate consequence of this fact is that since at the ground state

$$\mathbf{k}_e = \frac{m_e}{M}\mathbf{P} + \frac{2m_h}{M}\mathbf{w}. \quad (10)$$

The same procedure can be applied to other configurations of peaks and valleys.

4 ARPES signatures

References

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