

lecture 2 Grammar

Eg. 1

$\Sigma = \{a, b\}$, then $\Sigma^* = \{\epsilon, a, b, aa, ba, ab, bb, aaaa, \dots\}$

pay attention to the differences ϵ , $\{\}$, and $\{\epsilon\}$

Eg. 2. $E \rightarrow i$ Derivations of $(i+i)$

$$E \rightarrow E+E \quad E \Rightarrow (E) \Rightarrow (E+E) \Rightarrow (i+E) \Rightarrow (i+i)$$

$$E \rightarrow E * E$$

$$E \rightarrow (E)$$

Eg. 3 $G_1: S \rightarrow bA$

$$A \rightarrow aA \mid a$$

From the start symbol S , we have

$$S \Rightarrow bA \Rightarrow ba$$

$$S \Rightarrow bA \Rightarrow baA \Rightarrow baa$$

$$S \Rightarrow bA \Rightarrow baA \Rightarrow baaA \Rightarrow \dots \Rightarrow ba \dots a$$

$$L(G_1) = \{b a^n \mid n \geq 1\} \quad \text{start with } b, \text{ followed by } n \cdot a, n \geq 1$$

Eg. 4 $G_2: S \rightarrow AB$

$$A \rightarrow aA \mid a$$

$$B \rightarrow bB \mid b$$

$$L(G_2) = \{a^m b^n \mid m, n \geq 1\}$$

Eg. 5 Construct a grammar G_3 and let

$$L(G_3) = \{a^n b^n \mid n \geq 1\}$$

$$S \rightarrow a s b \mid a b$$

Eg. 6. rightmost derivation

$$E \Rightarrow (E) \Rightarrow (E+E) \Rightarrow (E+i) \Rightarrow (E * E + i) \Rightarrow (E * i + i) \Rightarrow (i * i + i)$$

leftmost derivation

$$E \Rightarrow (E) \Rightarrow (E+E) \Rightarrow (E * E + E) \Rightarrow (i * E + E) \Rightarrow (i * i + E) \Rightarrow (i * i + i)$$

Eg. 7.

using context-free grammar we can obtain

$$L = \{a^n b^n c^i \mid i \geq 1, n \geq 1\}$$

$$S \rightarrow AB$$

$$A \rightarrow aAb \mid ab$$

$$B \rightarrow cB \mid c$$

but we cannot use context-free grammar to obtain

$$L = \{a^n b^n c^n \mid n \geq 1\}$$

$$S \rightarrow aSBA \quad AA' \rightarrow AB$$

$$S \rightarrow abB \quad bA \rightarrow bb \quad \text{Context-sensitive grammar}$$

$$BA \rightarrow BA' \quad bB \rightarrow bc$$

$$BA' \rightarrow AA' \quad cB \rightarrow cc$$

$$L = \{\alpha c \alpha \mid \alpha \in (a|b)^*\} \text{ only can be described using}$$

Type-0 grammar.

Context-free grammar has the ability to describe most syntax structure of modern program language.