

Production and Operations Management

INFT 3611

Dr. J. Burns

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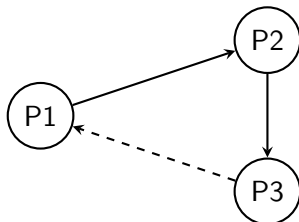
Section 2: Architectures

This content is based on the following public resources: <https://www.distributed-systems.net/index.php/books/ds4/>

Distributed Computation is Hard

Problem

Distributed systems consist of independently executing processes that communicate over unreliable networks. Each process has only a partial, delayed, and inconsistent view of global state.

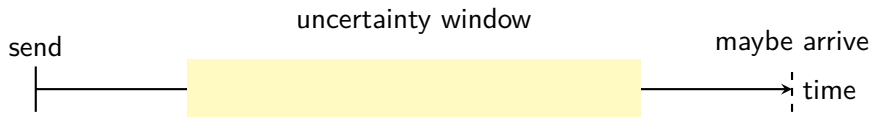


Different and delayed knowledge

- **Logical clocks** for ordering without synchronized time.
- **Quorum-based decisions** instead of global agreement.
- **Replicated state machines** for deterministic consistency.
- **Retry and reconciliation** to overcome uncertainty.
- **Failure detectors** to approximate liveness information.

Problem

Message delays are unbounded. A node cannot distinguish a slow peer from a failed or partitioned one. Silence has no meaning.

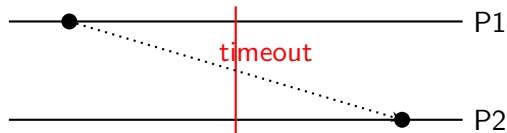


- **Partial synchrony assumptions** for eventual timing bounds.
- **Randomized timeouts** to avoid synchronized failure.
- **Quorum reads/writes** to avoid waiting for all nodes.
- **Eventual failure detectors** that improve over time.
- **Logical ordering** instead of timing-based decisions.

Timeout Ambiguity

Problem

A timeout indicates missing messages, not a crash. Reacting prematurely can cause split-brain or two leaders if delayed messages later arrive.



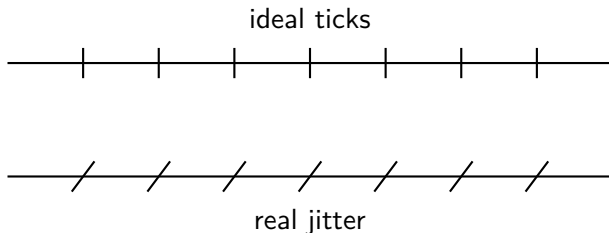
Timeout Ambiguity — Solutions

- **Terms/epochs** invalidate outdated leaders (Raft).
- **Leases** provide time-bounded authority.
- **Commit rules** require quorum confirmation.
- **Redundant communication** to detect restored nodes.
- **Delayed leadership transition** to avoid flapping.

Synchronous Model

Problem

The synchronous model assumes predictable message and processing times. Real systems rarely meet these assumptions, causing synchronous algorithms to fail under modest delay.



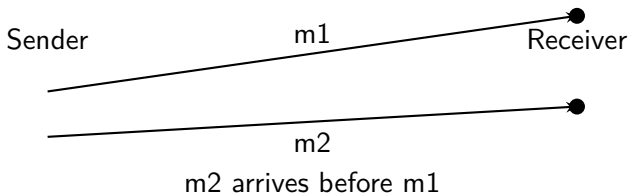
Synchronous Model — Solutions

- **Treat synchrony as conceptual only.**
- **Design protocols for weaker models** (e.g., Raft, Paxos).
- **Avoid timing-based correctness assumptions.**
- **Use timeouts as hints, not proofs of failure.**
- **Use logical clocks** when real time is unreliable.

Message Reordering

Problem

Messages may traverse different network paths or face variable queueing delays. As a result, they can arrive in an order different from the one in which they were sent.



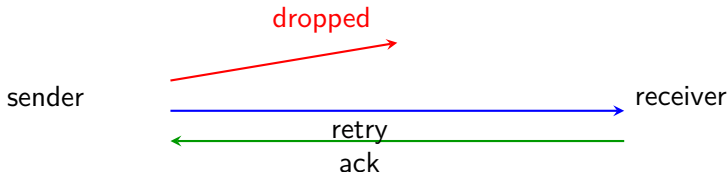
Message Reordering — Solutions

- **Sequence numbers** to restore intended order.
- **Version vectors** to track causality across replicas.
- **Idempotent operations** to tolerate duplicates.
- **Deterministic replay** in replicated state machines.
- **Ordering layers** such as TCP or application-level queues.

Message Loss

Problem

Networks drop messages due to congestion, queue overflow, or transient link faults. Loss prevents updates from propagating and may leave replicas inconsistent.



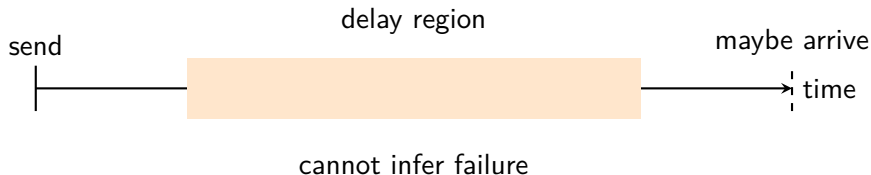
Message Loss — Solutions

- **Retransmissions** until confirmation is received.
- **Acknowledgments** to confirm delivery.
- **Checksums** to detect corruption.
- **Backoff algorithms** to reduce congestion.
- **Periodic anti-entropy** to reconcile state.

Arbitrary Delay

Problem

Messages may be delayed indefinitely. Such delays look identical to failures, making timing unreliable for determining remote state or coordinating decisions.

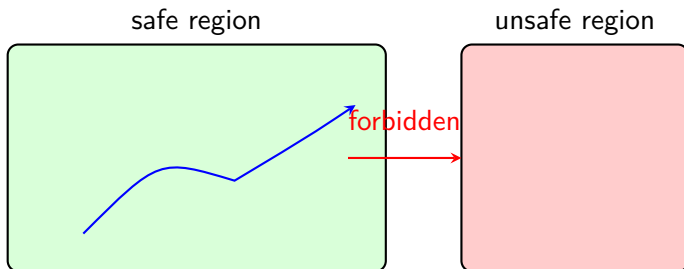


Arbitrary Delay — Solutions

- **Quorum-based operations** to tolerate missing responses.
- **Randomized timeouts** to reduce coordination conflicts.
- **Eventually perfect failure detectors** improving over time.
- **Epoch-based leadership** to avoid split-brain.
- **Delay-independent safety rules** in consensus protocols.

Problem

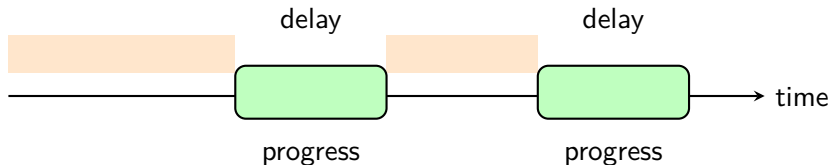
A system violates safety if it reaches an invalid state—such as electing two leaders or committing conflicting operations. Safety violations cannot be undone once they occur.



- **Single-writer leadership** to serialize decisions.
- **State machine replication** for deterministic behavior.
- **Quorum-based commits** to avoid conflicting decisions.
- **Monotonic state transitions** (legal state space).
- **Invariant-preserving protocols** such as Raft/Paxos.

Problem

Even if safety holds, a system may stall indefinitely under heavy delay or unstable leadership. Liveness requires eventual forward progress.



- **Randomized leader election** to break symmetry.
- **Eventually stable timeouts** after network recovery.
- **Retry loops** to ensure completion under partial failure.
- **Failure detectors** that improve accuracy over time.
- **Progress conditions** built into consensus protocols.

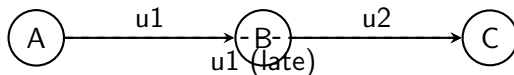
Algorithm 1 Retry-with-Ack Protocol

```
1: send(msg)
2: while no ack received do
3:   wait(timeout)
4:   resend(msg)
5: end while
```

Eventual Consistency

Problem

Replicas receive updates in different orders and at different times. Without coordination, their states may temporarily diverge, producing inconsistent reads across the system.



temporary divergence

Eventual Consistency — Solutions

- **Anti-entropy protocols** to exchange and reconcile state.
- **Version vectors** for detecting missing causal updates.
- **Idempotent updates** to tolerate replay and duplicates.
- **Convergent conflict-resolution rules** (e.g., LWW).
- **Periodic gossip** for reliable dissemination.

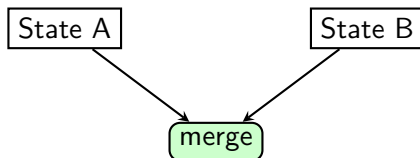
Eventual Consistency — Anti-Entropy Algorithm

Algorithm 2 Periodic Anti-Entropy

```
1: while true do  
2:   wait(random_interval())  
3:   peer  $\leftarrow$  pickRandomReplica()  
4:   send(localState, peer)  
5:   remoteState  $\leftarrow$  receive(peer)  
6:   localState  $\leftarrow$  merge(localState, remoteState)  
7: end while
```

Problem

Conflict-free Replicated Data Types require carefully designed merge rules. Incorrect merge semantics or non-commutative operations can cause replicas to diverge permanently.



deterministic, convergent result

CRDT Convergence — Solutions

- **Commutative updates** so order does not matter.
- **Associative merge operations** for consistent folding.
- **Idempotent merges** to handle duplicate state.
- **State-based CRDTs** for robust reconciliation.
- **Grow-only or monotonic structures** to avoid conflicts.

CRDT — Version Vector Update Algorithm

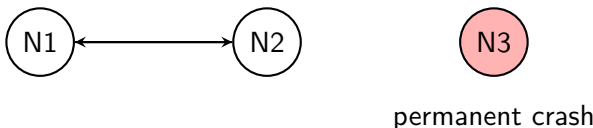
Algorithm 3 Version Vector Update

```
1:  $vv[node] \leftarrow vv[node] + 1$ 
2:  $attach(operation, vv)$ 
3:  $broadcast(operation)$ 
4:  $onReceive(op)$ :
5:    $vv[op.src] \leftarrow \max(vv[op.src], op.vv[op.src])$ 
6:    $apply(op)$ 
```

Crash-Stop Failures

Problem

Nodes may halt permanently due to hardware faults or power loss. They never recover or rejoin, reducing available replicas and risking loss of majority quorums.



- **Majority quorums** to tolerate permanent minority loss.
- **Replicated logs** to keep state despite node loss.
- **Leader re-election** to maintain progress.
- **Durable writes** that survive local crashes.
- **Static membership** for predictable fault tolerance.

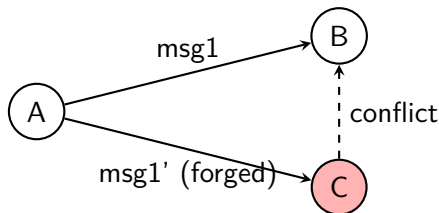
Algorithm 4 Crash-Recovery Log Rebuild

```
1: onStartup():
2:   log  $\leftarrow$  loadFromDisk()
3:   lastIndex  $\leftarrow$  log.tail
4:   send(hello, peers)
5:   missing  $\leftarrow$  fetchEntries(lastIndex, peers)
6:   append(log, missing)
7:   restoreState(log)
```

Byzantine Failures

Problem

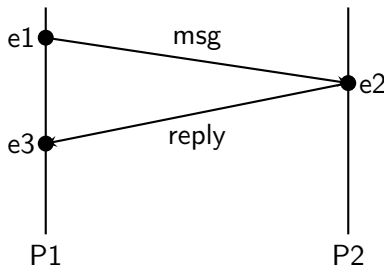
Nodes may behave arbitrarily: forging messages, equivocating, or selectively dropping updates. This breaks assumptions in non-Byzantine protocols and can mislead peers.



Lamport Clocks

Problem

Without synchronized clocks, processes cannot agree on the order of events using physical time. Concurrent events make real-time ordering ambiguous.



Lamport Clocks — Solutions

- **Monotonic counters** incremented on each event.
- **Piggyback timestamps** on every message.
- **Max-merge rule** to update local clocks.
- **Defines happens-before** without physical time.
- **Total order** via tie-breaking with process ID.

Lamport Clock Update Algorithm

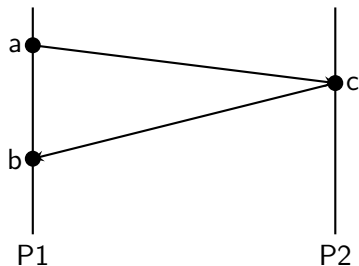
Algorithm 5 Lamport Timestamp Update

```
1: onLocalEvent():
2:   clock  $\leftarrow$  clock + 1
3: onSend(msg):
4:   clock  $\leftarrow$  clock + 1
5:   msg.ts  $\leftarrow$  clock
6:   send(msg)
7: onReceive(msg):
8:   clock  $\leftarrow$  max(clock, msg.ts) + 1
```

Happens-Before Relation

Problem

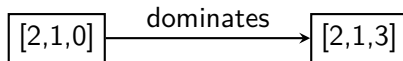
Determining causality between events is difficult without a global timeline. Concurrent events appear unordered in real time.



- **Lamport timestamps** encode causal precedence.
- **HB defines concurrency** when neither event dominates.
- **Prevents reordering errors** in replicated logs.
- **Supports deterministic replay.**
- **Enables causal consistency** across replicas.

Problem

Lamport clocks cannot distinguish true concurrency from causality. Systems require richer metadata to track causality accurately.



componentwise comparison

Vector Clocks — Solutions

- **Track causality** per process dimension.
- **Detect concurrency** using vector comparison rules.
- **Support multi-writer replication.**
- **Drive conflict resolution** in CRDTs.
- **Minimal metadata** for consistent ordering.

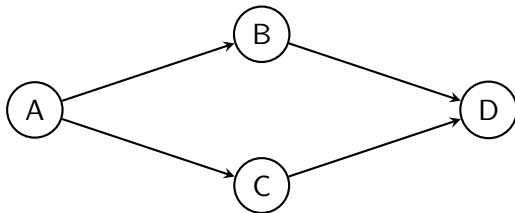
Vector Clock Update Algorithm

Algorithm 6 Vector Clock Update

```
1: onLocalEvent():
2:    $VC[i] \leftarrow VC[i] + 1$ 
3: onSend(op):
4:    $VC[i] \leftarrow VC[i] + 1$ 
5:    $op.VC \leftarrow VC$ 
6: onReceive(op):
7:
8:   for each process  $j$  do
9:      $VC[j] \leftarrow \max(VC[j], op.VC[j])$ 
10:  end for
11:    $VC[i] \leftarrow VC[i] + 1$ 
```

Problem

Broadcasting updates reliably in large clusters is expensive. Loss or delays slow convergence if updates aren't propagated probabilistically.



multi-step, probabilistic spreading

- **Random peer selection** to avoid bottlenecks.
- **Push-pull exchange** to accelerate convergence.
- **Periodic rounds** for steady dissemination.
- **Rumor-mongering** to limit message load.
- **Epidemic-style propagation** for scalability.

Gossip Round Algorithm

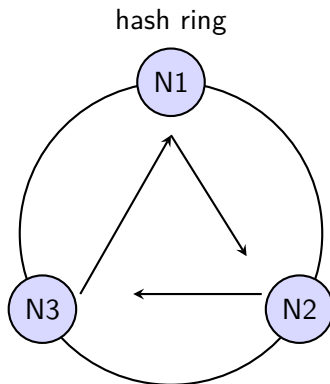
Algorithm 7 Push-Pull Gossip

```
1: while true do  
2:   wait(roundInterval)  
3:   peer  $\leftarrow$  pickRandom()  
4:   send(localState, peer)  
5:   remote  $\leftarrow$  receive(peer)  
6:   localState  $\leftarrow$  merge(localState, remote)  
7: end while
```

Consistent Hashing

Problem

When nodes join or leave, naive sharding causes large-scale data movement. Systems need key distribution that minimizes redistribution.





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