

Problem 2

- (a) The sentence generated by this language would start with one or more 'a's, followed by some number of 'b's and 'c's. It is important to note that every 'b' will have a corresponding 'c' because everytime the bBc case is invoked, it results in a 'b' and 'c' pair. Moreover, the sentence will also end with one or more 'a's.
- (b) The following sentences are generated by the grammar:

1. baab

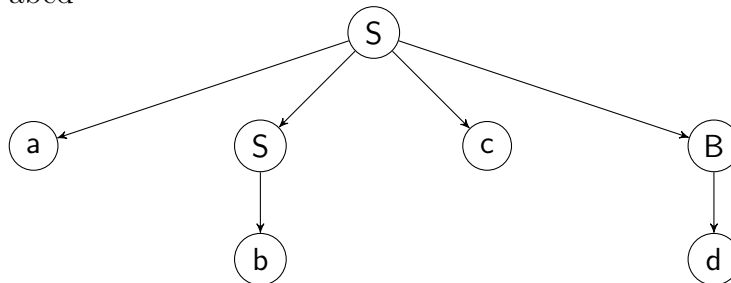
$S \Rightarrow AaBb$
 $\Rightarrow baBb$
 $\Rightarrow baab$

4. bbaab

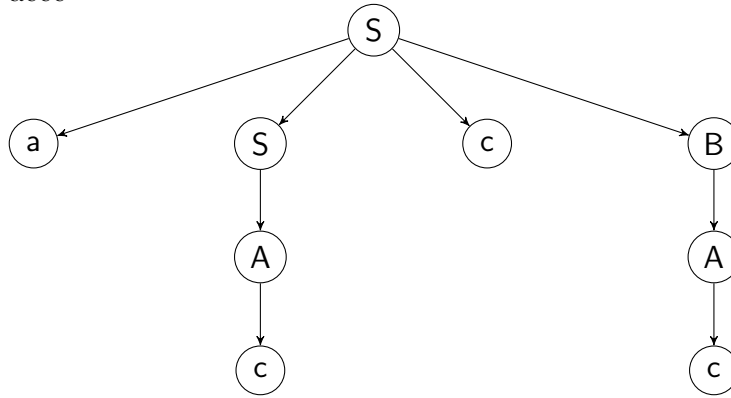
$S \Rightarrow AaBb$
 $\Rightarrow AbaBb$
 $\Rightarrow bbaBb$
 $\Rightarrow bbaab$

- (c) The following sentences are generated by the grammar:

1. abcd



5. accc



- (d) The following trees show that the grammar is ambiguous, because they are different trees, yet they generate the same sentence:



- (d) The inference rules that inductively define the judgement form are as follows:

$$\frac{x \Downarrow n \quad y \Downarrow m}{x \oplus y \Downarrow n + m} \quad \overline{a \Downarrow 1} \quad \overline{b \Downarrow 0}$$

Problem 3

- (a) (i) The expressions generated by the grammars consist of a combination of operands and operators, where the operands are separated by operators.
 (ii) Yes, the grammars generate the same expressions, but they do so with different parse trees.
- (b) Our Scala expression for testing '-' or '<<' precedence is as follows:

```

if( 1 << 3 - 2 ) == ( (1 << 3) - 2 )
  print "left shift has higher precedence"
else if ( 1 << 3 - 2 ) == ( 1 << (3 - 2) )
  print "minus has higher precedence"

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The order in which the values are evaluated determines the precedence of the operators. Since scala evaluates its parse trees in a bottom-up fashion, the return from our expression shows the relative precedence of '-' and '<<'.

(c) The BNF grammar for floating points made up of fractions is as follows:

$$\begin{aligned} \textit{floating point} &::= (\textit{non zero integer})\text{'.'}(\textit{fraction}) \\ \textit{fraction} &::= (\textit{middle sequence})|(\textit{fraction with exponent}) \\ \textit{fraction with exponent} &::= (\textit{non zero fraction})\text{'E'}(\textit{non zero integer}) \\ \textit{non zero fraction} &::= (\textit{middle sequence})(\textit{non zero digit}) \\ \textit{non zero integer} &::= \text{'-'}(\textit{non zero number})|\textit{non zero number} \\ \textit{non zero number} &::= (\textit{non zero digit})(\textit{middle sequence}) \\ \textit{middle sequence} &::= (\textit{any digit})(\textit{middle sequence})|\epsilon \\ \textit{any digit} &::= \text{'0'}|\textit{non zero digit} \\ \textit{non zero digit} &::= \text{'1'}|\text{'2'}|\text{'3'}|\text{'4'}|\text{'5'}|\text{'6'}|\text{'7'}|\text{'8'}|\text{'9'} \end{aligned}$$