Algorithm Library

CReatiQ

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常用文件

DEBUG 头

```
#include <bits/stdc++.h>
    using namespace std;
    using i64=long long;
    using i128=__int128;
    namespace DBG
        template <class T>
        void _dbg(const char *f,T t) { cerr<<f<<'='<<t<'\n'; }</pre>
10
        template <class A,class... B>
11
        void _dbg(const char *f,A a,B... b)
12
13
            while (*f!=',') cerr<<*f++;</pre>
14
            cerr<<'='<<a<<",";
15
            _dbg(f+1,b...);
16
17
        }
18
        template <class T>
19
20
        ostream& operator << (ostream& os,const vector<T> &v)
21
            os<<"[ ";
            for (const auto &x:v) os<<x<<", ";</pre>
23
            os<<"]";
24
            return os;
25
        }
26
27
        #define dbg(...) _dbg(#__VA_ARGS__, __VA_ARGS__)
28
29
30
    using namespace DBG;
    __int128 输出流
    ostream &operator << (ostream &os,i128 n)
2
        string s;
        bool neg=n<0;</pre>
        if (neg) n=-n;
        while (n)
            s+='0'+n\%10;
            n/=10;
10
        if (neg) s+='-';
11
        reverse(s.begin(),s.end());
12
13
        if (s.empty()) s+='0';
        return os<<s;</pre>
14
    }
    常用数学函数
    i64 ceilDiv(i64 n,i64 m)
    {
2
        if (n>=0) return (n+m-1)/m;
        else return n/m;
    }
    i64 floorDiv(i64 n,i64 m)
    {
        if (n>=0) return n/m;
        else return (n-m+1)/m;
    }
11
    i128 gcd(i128 a,i128 b)
13
    {
14
```

```
return b?gcd(b,a%b):a;
15
16
    纳秒级随机种子
   mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
   Linux 对拍
    记得先 chmod 777 check.sh.
1
   for ((i=0;i<100;i++))</pre>
   do
2
        ./A__Generator > A.in
        ./A < A.in > A.out
        ./A__Good < A.in > A.ans
5
        if diff A.out A.ans;
            echo "AC"
        else
10
            echo "WA"
11
            exit 1
12
        fi
13
14
   done
    数学
   欧拉筛
   vector<int> minp,primes;
   void sieve(int n)
    {
        minp.assign(n+1,0);
        primes.clear();
        for (int i=2;i<=n;i++)</pre>
            if (!minp[i])
            {
10
11
                minp[i]=i;
                primes.push_back(i);
12
13
            for (auto p:primes)
14
15
            {
16
                if (i*p>n) break;
                minp[i*p]=p;
17
18
                if (p==minp[i]) break;
            }
19
20
   }
21
   取模类 (MInt)
   template <class T>
1
2
    constexpr T power(T a,i64 b)
3
    {
        T res=1;
        for (;b;b>>=1,a*=a)
            if (b&1) res∗=a;
        return res;
   }
   template <int P>
10
   struct MInt
11
12
13
        int x;
        constexpr MInt():x{} {}
14
```

```
constexpr MInt(i64 x):x{norm(x%getMod())} {}
15
16
        static int Mod;
17
        constexpr static int getMod()
18
19
             if (P>0) return P;
20
21
             else return Mod;
        }
22
23
        constexpr static void setMod(int Mod_) { Mod=Mod_; }
24
25
26
        constexpr int norm(int x) const
27
             if (x<0) x+=getMod();
28
            if (x>=getMod()) x-=getMod();
29
            return x;
30
31
32
33
        constexpr int val() const { return x; }
34
        explicit constexpr operator int () const { return x; }
35
36
37
        constexpr MInt operator - () const
38
             MInt res;
39
40
             res.x=norm(getMod()-x);
41
             return res;
        }
42
43
        constexpr MInt inv() const
44
45
             assert(x!=0);
46
47
             return power(*this,getMod()-2);
48
49
50
        constexpr MInt &operator *= (MInt rhs) &
51
            x=1ll*x*rhs.x%getMod();
52
53
            return *this;
        }
54
55
        constexpr MInt &operator += (MInt rhs) &
56
57
58
             x=norm(x+rhs.x);
            return *this;
59
60
61
62
        constexpr MInt &operator -= (MInt rhs) &
63
64
             x=norm(x-rhs.x);
65
            return *this;
        }
66
        constexpr MInt &operator /= (MInt rhs) &
68
69
            return *this*=rhs.inv();
70
        }
71
72
        friend constexpr MInt operator * (MInt lhs, MInt rhs)
73
74
             MInt res=lhs;
75
76
             res*=rhs;
77
            return res;
        }
78
        friend constexpr MInt operator + (MInt lhs,MInt rhs)
80
81
            MInt res=lhs;
82
             res+=rhs;
83
84
             return res;
        }
85
```

```
86
87
         friend constexpr MInt operator - (MInt lhs, MInt rhs)
88
              MInt res=lhs;
89
              res-=rhs;
              return res;
91
92
93
         friend constexpr MInt operator / (MInt lhs,MInt rhs)
94
95
             MInt res=lhs;
96
97
              res/=rhs;
98
             return res;
         }
99
100
         friend constexpr istream &operator >> (istream &is,MInt &a)
101
102
             i64 v;
103
104
              is>>v;
             a=MInt(v);
105
             return is;
106
107
108
         friend constexpr ostream &operator << (ostream &os,const MInt &a) { return os<<a.val(); }</pre>
110
         friend constexpr bool operator == (MInt lhs,MInt rhs) { return lhs.val()==rhs.val(); }
111
112
         friend constexpr bool operator != (MInt lhs,MInt rhs) { return lhs.val()!=rhs.val(); }
113
114
    };
115
     template<>
116
     int MInt<0>::Mod=1;
117
118
119
     template<int V,int P>
     constexpr MInt<P> CInv=MInt<P>(V).inv();
120
     组合数
 1
     struct Comb
 2
     {
 3
         int n;
         vector<Z> _fac,_inv,_finv;
 4
         Comb():n\{0\},\_fac\{1\},\_inv\{0\},\_finv\{1\}\{\}
         Comb(int n):Comb() { init(n); }
 8
         void init(int m)
10
11
             m=min(m,Z::getMod()-1);
              if (m<=n) return;</pre>
12
              _fac.resize(m+1);
13
14
              _inv.resize(m+1);
              _finv.resize(m+1);
15
16
              for (int i=n+1;i<=m;i++)</pre>
17
18
                  _fac[i]=_fac[i-1]*i;
              _finv[m]=_fac[m].inv();
19
              for (int i=m;i>n;i--)
20
21
              {
                  _finv[i-1]=_finv[i]*i;
22
23
                  _inv[i]=_finv[i]*_fac[i-1];
              }
24
              n=m;
         }
26
27
28
         Z fac(int m)
29
              if (m>n) init(m<<1);</pre>
30
              return _fac[m];
31
         }
32
33
```

```
Z finv(int m)
34
35
             if (m>n) init(m<<1);</pre>
36
             return _finv[m];
37
38
         }
39
40
         Z inv(int m)
41
             if (m>n) init(m<<1);
42
43
             return _inv[m];
         }
44
45
         Z binom(int n,int m)
46
47
             if (n \le m \mid m \le 0) return 0;
48
             return fac(n)*finv(m)*finv(n-m);
49
    } comb;
51
    多项式
    vector<int> rev;
    vector<Z> roots{0,1};
2
    void dft(vector<Z> &a)
5
    {
         int n=a.size();
         if (int(rev.size())!=n)
8
             int k=__builtin_ctz(n)-1;
             rev.resize(n);
10
11
             for (int i=0;i<n;i++)</pre>
                  rev[i]=rev[i>>1]>>1|(i&1)<<k;
12
         for (int i=0;i<n;i++)</pre>
14
               if (rev[i]<i)</pre>
15
16
                  swap(a[i],a[rev[i]]);
         if (int(roots.size())<n)</pre>
17
18
             int k=__builtin_ctz(roots.size());
19
20
             roots.resize(n);
             while ((1<<k)<n)
21
             {
22
23
                  Z = power(Z(3), (P-1) >> (k+1));
                  for (int i=1<<(k-1);i<(1<<k);i++)</pre>
24
25
                  {
                       roots[i<<1]=roots[i];</pre>
26
                       roots[i<<1|1]=roots[i]*e;</pre>
27
28
                  }
                  k++;
29
30
31
         for (int k=1;k<n;k<<=1)</pre>
32
             for (int i=0;i<n;i+=k*2)</pre>
33
                  for (int j=0;j<k;j++)</pre>
34
35
                  {
                       Z u=a[i+j],v=a[i+j+k]*roots[j+k];
36
                       a[i+j]=u+v;
37
                       a[i+j+k]=u-v;
38
                  }
39
    }
41
42
    void idft(vector<Z> &a)
43
    {
         int n=a.size();
44
45
         reverse(a.begin()+1,a.end());
         dft(a);
46
47
         Z inv=(1-P)/n;
         for (int i=0;i<n;i++) a[i]*=inv;</pre>
48
    }
49
```

```
struct Poly
51
52
     {
         vector<Z> a;
53
54
55
         Poly(){}
         explicit Poly(int size, function<Z(int)>f=[](int) { return 0; }):a(size)
56
57
         { for (int i=0;i<size;i++) a[i]=f(i); }
         Poly(const vector<Z> &a):a(a){}
58
         Poly(const initializer_list<Z> &a):a(a){}
59
60
         int size() const { return a.size(); }
61
62
         void resize(int n) { a.resize(n); }
63
64
         Z operator [] (int idx) const
65
66
67
              if (idx<size()) return a[idx];</pre>
             else return 0;
68
         }
70
         Z & operator [] (int idx) { return a[idx]; }
71
72
73
         Poly mulxk(int k) const
74
             auto b=a;
75
76
             b.insert(b.begin(),k,0);
77
             return Poly(b);
         }
78
79
         Poly modxk(int k) const
80
81
             k=min(k,size());
82
             return Poly(vector<Z>(a.begin(),a.begin()+k));
83
84
         }
85
86
         Poly divxk(int k) const
87
             if (size()<=k) return Poly();</pre>
88
             return Poly(vector<Z>(a.begin()+k,a.end()));
89
         }
90
91
         friend Poly operator + (const Poly &a,const Poly &b)
92
93
94
             vector<Z> res(max(a.size(),b.size()));
              for (int i=0;i<int(res.size());i++)</pre>
95
96
                  res[i]=a[i]+b[i];
             return Poly(res);
97
98
         }
99
         friend Poly operator - (const Poly &a,const Poly &b)
100
101
             vector<Z> res(max(a.size(),b.size()));
102
             for (int i=0;i<int(res.size());i++)</pre>
                  res[i]=a[i]-b[i];
104
             return Poly(res);
105
106
107
         friend Poly operator - (const Poly &a)
108
109
              vector<Z> res(a.size());
110
             for (int i=0;i<int(res.size());i++)</pre>
111
                 res[i]=-a[i];
112
113
             return Poly(res);
         }
114
115
         friend Poly operator * (Poly a,Poly b)
116
117
             if (!a.size()||!b.size()) return Poly();
118
             if (a.size() < b.size()) swap(a,b);</pre>
119
             if (b.size()<128)
             {
121
```

```
Poly c(a.size()+b.size()-1);
122
123
                  for (int i=0;i<a.size();i++)</pre>
                       for (int j=0;j<b.size();j++)</pre>
124
                           c[i+j]+=a[i]*b[j];
125
126
                  return c;
127
              int sz=1,tot=a.size()+b.size()-1;
128
              while (sz<tot) sz<<=1;</pre>
129
              a.a.resize(sz);
130
131
              b.a.resize(sz);
              dft(a.a);
132
133
              dft(b.a);
              for (int i=0;i<sz;i++)</pre>
134
                  a.a[i]=a[i]*b[i];
135
136
              idft(a.a);
              a.resize(tot);
137
138
              return a;
139
140
         friend Poly operator * (Z a,Poly b)
141
142
143
              for (int i=0;i<int(b.size());i++) b[i]*=a;</pre>
              return b;
144
         }
145
146
147
         friend Poly operator * (Poly a,Z b)
148
              for (int i=0;i<int(a.size());i++) a[i]*=b;</pre>
149
150
              return a;
         }
151
152
         Poly &operator += (Poly b) { return (*this)=(*this)+b; }
153
         Poly &operator -= (Poly b) { return (*this)=(*this)-b; }
154
155
         Poly &operator *= (Poly b) { return (*this)=(*this)*b; }
         Poly &operator *= (Z b) { return (*this)=(*this)*b; }
156
157
         Poly deriv() const
158
159
160
              if (a.empty()) return Poly();
              vector<Z> res(size()-1);
161
162
              for (int i=0;i<size()-1;i++)</pre>
                  res[i]=(i+1)*a[i+1];
163
              return Poly(res);
164
165
         }
166
167
         Poly integr() const
168
              vector<Z> res(size()+1);
              for (int i=0;i<size();i++)</pre>
170
                  res[i+1]=a[i]/(i+1);
171
172
              return Poly(res);
         }
173
         Poly inv(int m) const
175
176
177
              Poly x\{a[0].inv()\};
              int k=1;
178
179
              while (k<m)
180
              {
                   k<<=1;
181
182
                  x=(x*(Poly{2}-modxk(k)*x)).modxk(k);
183
184
              return x.modxk(m);
         }
185
186
         Poly ln(int m) const { return (deriv()*inv(m)).integr().modxk(m); }
187
188
189
         Poly exp(int m) const
190
              Poly x\{1\};
              int k=1;
192
```

```
while (k<m)
193
194
              {
                   k<<=1;
195
                   x=(x*(Poly{1}-x.ln(k)+modxk(k))).modxk(k);
196
197
              }
              return x.modxk(m);
198
199
200
         Poly pow(int k,int m) const
201
202
              int i=0:
203
204
              while (i<size()&&a[i].val()==0) i++;</pre>
205
              if (i==size()||1ll*i*k>=m) return Poly(vector<Z>(m));
              Z v=a[i];
206
              auto f=divxk(i)*v.inv();
207
              return (f.ln(m-i*k)*k).exp(m-i*k).mulxk(i*k)*power(v,k);
208
210
211
         Poly sqrt(int m) const
212
              Poly x\{1\};
213
214
              int k=1;
              while (k<m)
215
216
                   k < < = 1:
217
                   x=(x+(modxk(k)*x.inv(k)).modxk(k))*((P+1)/2);
218
219
              return x.modxk(m);
220
221
         Poly mulT(Poly b) const
222
223
              if (b.size()==0) return Poly();
224
              int n=b.size();
225
226
              reverse(b.a.begin(),b.a.end());
              return ((*this)*b).divxk(n-1);
227
228
229
         vector<Z> eval(vector<Z> x) const
230
231
              if (size()==0) return vector<Z>(x.size(),0);
232
233
              const int n=max(int(x.size()),size());
              vector<Poly> q(n<<2);</pre>
234
              vector<Z> ans(x.size());
235
236
              x.resize(n);
              function<void(int,int,int)> build=[&](int p,int l,int r)
237
238
                   if (r-l==1) q[p]=Poly{1,-x[l]};
239
240
                   else
                   {
241
                       int m=(l+r)>>1;
242
243
                       build(p<<1,1,m);</pre>
                       build(p<<1|1,m,r);
244
                       q[p]=q[p<<1]*q[p<<1|1];
245
246
              };
247
              function<void(int,int,int,const Poly&)> work=[&](int p,int l,int r,const Poly &num)
248
              {
249
                   if (r-l==1)
250
251
                   {
                       if (l<int(ans.size())) ans[l]=num[0];</pre>
252
                   }
253
                   else
254
255
                       int m=(l+r)>>1;
256
257
                       work(p \le 1, l, m, num.mulT(q[p \le 1|1]).modxk(m-l));
258
                       work(p << 1 | 1, m, r, num.mulT(q[p << 1]).modxk(r-m));
259
                   }
260
              build(1,0,n);
261
              work(1,0,n,mulT(q[1].inv(n)));
              return ans;
263
```

```
264 }
265 };
```

原根表

```
prime
                           k
                       r
   3
                       1
                           1
                               2
2
   5
                           2
                       1
                               2
   17
                       1
                           4
                               3
   97
   193
                           6
                       3
                               5
   257
                       1
                       15
                           9
                               17
   7681
   12289
                       3
                           12 11
   40961
                       5
                           13
                               3
11
   65537
                       1
                           16
                              3
   786433
                       3
                           18
12
13
   5767169
                       11
                           19
                              3
   7340033
                           20 3
14
15
   23068673
                       11 21 3
                       25
   104857601
                          22
16
17
   167772161
                       5
                           25
   469762049
                       7
                           26
18
   1004535809
                       479 21
19
                       15 27 31
20
   2013265921
   2281701377
                       17 27
                               3
21
22
   3221225473
                       3
                           30
                               5
   75161927681
                       35 31 3
23
   77309411329
                       9
24
                       3
25
   206158430209
                           36 22
                           37
   2061584302081
                       15
                               7
26
27
   2748779069441
                       5
                           39
                               3
   6597069766657
                       3
                           41
                              5
28
   39582418599937
                       9
                           42 5
                       9
30
   79164837199873
                           43 5
   263882790666241
                       15
                           44
31
                       35 45 3
32
   1231453023109121
   1337006139375617
                      19 46 3
33
34
   3799912185593857
                       27 47 5
                       15 48 19
   4222124650659841
35
36
   7881299347898369
                       7
                           50
   31525197391593473
                      7
                           52 3
37
   180143985094819841 5
38
   1945555039024054273 27 56 5
   4179340454199820289 29 57 3
40
```

线性基

```
struct LB
1
2
    {
        static constexpr int L=60;
3
        array<i64,L+1> a{};
5
        LB(){}
        LB(const vector<i64> &v) { init(v); }
8
        bool insert(i64 t)
10
11
             for (int i=L;i>=0;i--)
12
13
                 if (t&(1ll<<i))</pre>
14
                 {
                      if (!a[i])
15
                      {
                          a[i]=t;
17
18
                          return 1;
                      }
19
                      else t^=a[i];
20
                 }
             return 0;
22
```

```
}
23
24
         void init(const vector<i64> &v) { for (auto x:v) insert(x); }
25
26
         bool check(i64 t)
27
28
29
             for (int i=L;i>=0;i--)
                  if (t&(1ll<<i))</pre>
30
                      if (!a[i]) return 0;
31
32
                      else t^=a[i];
             return 1;
33
34
35
         i64 QueryMax()
36
37
             i64 res=0;
38
39
             for (int i=L;i>=0;i--)
                 res=max(res,res^a[i]);
40
41
             return res;
         }
42
43
         i64 QueryMin()
44
45
             for (int i=0;i<=L;i++)</pre>
                  if (a[i]) return a[i];
47
48
             return 0;
         }
49
50
51
         i64 QueryKth(int k)
52
             i64 res=0;
53
             int cnt=0;
54
55
             array<i64,L+1> tmp{};
56
             for (int i=0;i<=L;i++)</pre>
57
             {
58
                  for (int j=i-1;j>=0;j--)
                      if (a[i]&(1ll<<j)) a[i]^=a[j];</pre>
59
                  if (a[i]) tmp[cnt++]=a[i];
60
61
             if (k>=(1ll<<cnt)) return -1;</pre>
62
63
             for (int i=0;i<cnt;i++)</pre>
                 if (k&(1ll<<i)) res^=tmp[i];
64
             return res;
65
66
         }
    };
67
    min-plus 卷积
    \mathcal{O}(n \log n), 但要求 b 是凸的。
    template <class T>
    vector<T> min_plus_convolution(const vector<T> &a,const vector<T> &b)
2
    {
         int n=a.size(),m=b.size();
4
         vector<T> c(n+m-1);
         function<void(int,int,int,int)> solve=[&](int l,int r,int ql,int qr)
             if (l>r) return;
             int mid=(l+r)>>1;
             while (ql+m<=l) ++ql;</pre>
11
             while (qr>r) --qr;
12
             int qmid=-1;
13
             c[mid]=inf;
14
15
             for (int i=ql;i<=qr;i++)</pre>
16
                  if (a[i]+b[mid-i]-i<c[mid])</pre>
17
18
                      c[mid] = a[i] + b[mid-i];
19
20
                      qmid=i;
                  }
21
```

```
else if (mid-i>=0&&mid-i<m) qmid=i;</pre>
22
23
            }
            solve(l,mid-1,ql,mid);
24
            solve(mid+1,r,qmid,qr);
25
27
28
        solve(0,n+m-2,0,n-1);
        return c;
29
   }
30
    模意义分数还原
    分别是求:分子不大于 A 时分子最大的分数;分子分母最大值最小的分数。
   pair<int,int> restore(int q,int A)
2
    {
        int x=q,y=P,a=1,b=0;
        while (x>A)
            swap(x,y);
            swap(a,b);
            a^{-=}x/y*b;
            x%=y;
10
        return make_pair(x,a);
11
12
   }
13
   pair<int,int> restore(int x)
14
15
16
        vector<int> a;
17
        int p=P;
        Z inv=Z(x).inv();
18
19
        while (x)
20
        {
            a.push_back(x);
21
22
            swap(x,p);
            x%=p;
23
24
        pair<int, int> res{P,P};
25
26
        for (auto ca:a)
27
            int cb=(Z(ca)*inv).x;
28
29
            ca=min(ca,P-ca);
            cb=min(cb,P-cb);
30
31
            if (max(res.first,res.second)>max(ca,cb))
32
                res={ca,cb};
        }
33
34
        return res;
   }
35
    Exgcd
    void exgcd(i64 a,i64 b,i64 &x,i64 &y)
    {
2
        if (!b)
3
        {
            x=1; y=0;
            return;
        exgcd(b,a%b,x,y);
        swap(x,y);
        y=a/b*x;
10
        return;
   }
12
```

二元一次不定方程

给定不定方程

若该方程无整数解,输出 -1。

若该方程有整数解,且有正整数解,则输出其**正整数**解的数量,所有**正整数**解中x的最小值,所有**正整数**解中y的最小值,所有**正整数**解中y的最小值,所有**正整数**解中y的最大值。

若方程有整数解,但没有正整数解,你需要输出所有整数解中x的最小正整数值,y的最小正整数值。

```
void exgcd(i64 a,i64 b,i64 &x,i64 &y)
    {
2
        if (!b)
        {
             x=1; y=0;
             return;
        exgcd(b,a%b,x,y);
        swap(x,y);
10
        y-=a/b*x;
        return;
11
12
13
    i64 ceilDiv(i64 n,i64 m)
14
15
         if (n>=0) return (n+m-1)/m;
16
17
         else return n/m;
    }
18
19
    i64 floorDiv(i64 n,i64 m)
20
    {
21
        if (n>=0) return n/m;
22
         else return (n-m+1)/m;
23
    }
24
25
    void R()
26
27
        i64 a,b,c,x,y,t;
28
29
        cin>>a>>b>>c;
        t=__gcd(a,b);
30
        if (c%t)
31
32
        {
             cout<<"-1\n";
33
34
             return;
        }
35
36
        exgcd(a,b,x,y);
37
        x*=c/t,y*=c/t;
38
        i64 l=ceilDiv(1ll-x,b/t),r=floorDiv(y-1ll,a/t);
        if (l>r) cout<<x+l*b/t<<' '<<y-r*a/t<<'\n';</pre>
39
        else cout<<r-l+1ll<<' '<x+l*b/t<<' '<<y-r*a/t<<' '<x+r*b/t<<' '<<y-l*a/t<<'\n';</pre>
40
        return;
    }
42
```

数据结构

并查集(启发式合并+带撤销)

```
struct DSU
1
2
    {
        int n=0;
        vector<int> fa,siz;
        stack<int> s;
        DSU(int n) { init(n); }
        void init(int n)
10
11
            fa.resize(n);
            iota(fa.begin(),fa.end(),0);
12
            siz.assign(n,1);
13
```

```
while (!s.empty()) s.pop();
14
15
16
         int get(int x) { return fa[x] == x?x:get(fa[x]); }
17
        void merge(int x,int y)
19
20
             x=get(x),y=get(y);
21
             if (x==y) return;
22
             if (siz[x]<siz[y]) swap(x,y);</pre>
             s.push(y),fa[y]=x,siz[x]+=siz[y];
24
25
26
        void undo()
27
28
             if (s.empty()) return;
29
             int y=s.top();
             s.pop();
31
32
             siz[fa[y]]-=siz[y];
33
             fa[y]=y;
34
35
         void back(int t=0) { while (s.size()>t) undo(); }
36
    状压 RMQ
    template <class T,class Cmp=less<T>>
    struct RMQ
2
3
4
        const Cmp cmp=Cmp();
         static constexpr unsigned B=64;
        using u64=unsigned long long;
        vector<vector<T>> a;
        vector<T> pre,suf,ini;
        vector<u64> stk;
11
12
        RMQ() {}
        RMQ(const vector<T> &v) { init(v); }
13
14
        void init(const vector<T> &v)
15
        {
16
             n=v.size();
17
18
             pre=suf=ini=v;
             stk.resize(n);
19
20
             if (!n) return;
             const int M=(n-1)/B+1;
21
             const int lg=__lg(M);
             a.assign(lg+1,vector<T>(M));
23
             for (int i=0;i<M;i++)</pre>
24
25
             {
                  a[0][i]=v[i*B];
26
                   \label{eq:formula}  \mbox{for } (\mbox{int} \ j=1; j < B\&\&i * B+j < n; j++) 
27
                      a[0][i]=min(a[0][i],v[i*B+j],cmp);\\
28
29
             for (int i=1;i<n;i++)</pre>
30
                  if (i%B) pre[i]=min(pre[i],pre[i-1],cmp);
31
32
             for (int i=n-2;i>=0;i--)
                  if (i%B!=B-1) suf[i]=min(suf[i],suf[i+1],cmp);
33
             for (int j=0;j<lg;j++)</pre>
                  for (int i=0;i+(2<<j)<=M;i++)</pre>
35
                      a[j+1][i]=min(a[j][i],a[j][i+(1<<j)],cmp);
             for (int i=0;i<M;i++)</pre>
37
             {
38
                  const int l=i*B;
                  const int r=min(1U*n,l+B);
40
                  u64 s=0;
41
                  for (int j=l;j<r;j++)</pre>
42
43
                  {
                      while (s&&cmp(v[j],v[__lg(s)+l])) s^=1ULL<<__lg(s);</pre>
44
```

```
s = 1ULL << (j-1);
45
46
                     stk[j]=s;
                 }
47
            }
48
49
50
        //查询区间 [l,r) 的 RMQ
51
        T operator()(int l,int r)
52
53
             if (1/B!=(r-1)/B)
54
55
             {
                 T ans=min(suf[l],pre[r-1],cmp);
56
                 l=l/B+1,r=r/B;
57
                 if (l<r)
58
59
                 {
                     int k=__lg(r-l);
60
                     ans=min({ans,a[k][l],a[k][r-(1<<k)]},cmp);
61
                 }
62
                 return ans;
            }
64
             else
65
             {
67
                 int x=B*(1/B);
                 return ini[__builtin_ctzll(stk[r-1]>>(l-x))+l];
69
             }
70
    };
    ST 表
    template <class T>
1
2
    struct ST
3
    {
        int n;
        vector<vector<T>> a;
        ST() {}
        ST(const vector<T> &v) { init(v); }
        void init(const vector<T> &v)
10
11
        {
            n=v.size();
12
             if (!n) return;
13
             const int lg=__lg(n);
            a.assign(lg+1,vector<T>(n));
15
16
             for (int j=0;j<lg;j++)</pre>
17
                 for (int i=0;i+(2<<j)<=n;i++)</pre>
18
                     a[j+1][i]=__gcd(a[j][i],a[j][i+(1<<j)]);
19
        }
20
21
        T operator()(int l,int r)
22
23
             int k=__lg(r-l);
24
            return __gcd(a[k][l],a[k][r-(1<<k)]);</pre>
25
    };
27
    树状数组
    template <class T>
1
    struct BIT
2
3
        int n;
        vector<T> a;
5
        BIT(int n_=0) { init(n_); }
        void init(int n_)
10
        {
```

```
n=n_;
11
12
             a.assign(n,T{});
         }
13
14
         void add(int x,const T &v)
15
16
17
              for (int i=x+1;i<=n;i+=i&-i)</pre>
                  a[i-1]=a[i-1]+v;
18
         }
19
20
         //查询区间 [0,x)
21
22
         T sum(int x)
23
             T ans{};
24
             for (int i=x;i>0;i-=i&-i)
25
                  ans=ans+a[i-1];
26
27
             return ans;
         }
28
29
         //查询区间 [1,r)
30
         T rangeSum(int l,int r) { return sum(r)-sum(l); }
31
32
33
         int select(const T &k)
35
             int x=0;
36
             T cur{};
             for (int i=1<<__lg(n);i;i>>=1)
37
38
             {
                  if (x+i<=n&&cur+a[x+i-1]<=k)</pre>
                  {
40
41
                      x+=i;
                      cur=cur+a[x-1];
42
43
44
             }
             return x;
45
46
    };
47
    线段树
1
    template <class Info,class Tag>
    struct SGT
2
    {
3
         int n;
         vector<Info> info;
5
         vector<Tag> tag;
         SGT():n(0) {}
         SGT(int n_,Info v_=Info()) { init(n_,v_); }
10
         template <class T>
11
         SGT(vector<T> init_) { init(init_); }
12
13
         void init(int n_,Info v_=Info()) { init(vector(n_,v_)); }
14
15
16
         template <class T>
         void init(vector<T> init_)
17
18
19
             n=init_.size();
             info.assign(4<<__lg(n),Info());
tag.assign(4<<__lg(n),Tag());</pre>
20
21
             function<void(int,int,int)> build=[&](int p,int l,int r)
22
             {
                  if (r-l==1)
24
                  {
25
26
                      info[p]=init_[l];
                      return;
27
28
                  int m=(l+r)>>1;
29
                  build(p<<1,1,m);
30
                  build(p<<1|1,m,r);
31
```

```
pushup(p);
32
33
               };
               build(1,0,n);
34
          }
35
          void pushup(int p) { info[p]=info[p<<1]+info[p<<1|1]; }</pre>
37
38
          void apply(int p,const Tag &v)
39
40
41
               info[p].apply(v);
42
               tag[p].apply(v);
43
44
          void pushdown(int p)
45
46
               apply(p<<1,tag[p]);</pre>
47
48
               apply(p<<1|1,tag[p]);
               tag[p]=Tag();
49
          }
51
          void modify(int p,int l,int r,int x,const Info &v)
52
53
               if (r-l==1)
54
               {
                    info[p]=v;
56
57
                    return;
58
               int m=(l+r)>>1;
59
               pushdown(p);
               if (x<m) modify(p<<1,l,m,x,v);</pre>
61
               else modify(p <<1 | 1, m, r, x, v);
62
63
               pushup(p);
          }
64
65
          //O(log n) 单点修改
66
67
          void modify(int p,const Info &v) { modify(1,0,n,p,v); }
68
          Info rangeQuery(int p,int l,int r,int x,int y)
69
70
               if (l>=y||r<=x) return Info();</pre>
71
72
               if (l>=x&&r<=y) return info[p];</pre>
               int m=(l+r)>>1;
73
74
               pushdown(p);
75
               \textbf{return} \ \ \text{rangeQuery}(\texttt{p}\texttt{<<1},\texttt{l},\texttt{m},\texttt{x},\texttt{y}) + \\ \text{rangeQuery}(\texttt{p}\texttt{<<1} \,|\, \texttt{1},\texttt{m},\texttt{r},\texttt{x},\texttt{y});
76
77
          //O(log n) 区间查询 [l,r)
78
79
          Info rangeQuery(int l,int r) { rangeQuery(1,0,n,l,r); }
80
81
          void rangeApply(int p,int l,int r,int x,int y,const Tag &v)
82
               if (l>=y||r<=x) return;
83
               if (l>=x&&r<=y)
               {
85
86
                    apply(p,v);
87
                    return;
88
               int m=(l+r)>>1;
90
               pushdown(p);
               rangeApply(p<<1,l,m,x,y,v);</pre>
91
               rangeApply(p<<1|1,m,r,x,y,v);</pre>
92
               pushup(p);
93
94
95
96
          //O(log n) 区间操作 [l,r)
          void rangeApply(int l,int r,const Tag &v) { rangeApply(1,0,n,l,r,v); }
97
          //O(log\ n) 区间 [l,r) 内查找第一个合法位置
99
          template <class F>
100
101
          int findFirst(int p,int l,int r,int x,int y,F pred)
102
```

```
if (l>=y||r<=x||!pred(info[p])) return -1;</pre>
103
104
                if (r-l==1) return l;
                int m=(l+r)>>1;
105
                pushdown(p);
106
107
                int res=findFirst(p<<1,l,m,x,y,pred);</pre>
               \textbf{if} \ (\texttt{res} \texttt{==-1}) \ \texttt{res} \texttt{=} \texttt{findFirst}(\texttt{p} \texttt{<<1} | \texttt{1}, \texttt{m}, \texttt{r}, \texttt{x}, \texttt{y}, \texttt{pred}) \texttt{;}
108
                return res;
109
           }
110
111
           template <class F>
112
           int findFirst(int l,int r,F pred) { return findFirst(1,0,n,l,r,pred); }
113
114
           template <class F>
115
           int findLast(int p,int l,int r,int x,int y,F pred)
116
117
                if (l>=y||r<=x||!pred(info[p])) return -1;</pre>
118
119
                if (r-l==1) return l;
                int m=(l+r)>>1;
120
121
                pushdown(p);
                int res=findFirst(p<<1|1,m,r,x,y,pred);</pre>
122
                if (res==-1) res=findFirst(p<<1,l,m,x,y,pred);</pre>
123
124
                return res;
125
126
           template <class F>
127
           int findLast(int l,int r,F pred) { return findLast(1,0,n,l,r,pred); }
128
129
     };
130
131
      //这里默认乘法优先 (x*a+b)*c+d=x*(a*c)+(b*c+d)
     struct Tag
132
133
      {
           i64 a=1,b=0;
134
           void apply(Tag t)
135
136
               a*=t.a;
137
                b=b*t.a+t.b;
138
139
     };
140
141
     struct Info
142
143
           i64 x=0,l=0,r=0;
144
           void apply(Tag t)
145
146
                int len=r-l+1;
147
148
                x=x*t.a+len*t.b;
           }
149
150
     };
151
     Info operator + (Info a,Info b)
152
153
           return {a.x+b.x,min(a.l,b.l),max(a.r,b.r)};
154
```

字符串

字符串哈希 (随机模数)

```
bool isPrime(int n)
1
2
         if (n<=1) return 0;</pre>
3
         for (int i=2;i*i<=n;i++)</pre>
             if (n%i==0) return 0;
        return 1;
    }
    int findPrime(int n)
10
    {
        while (!isPrime(n)) n++;
11
12
        return n;
```

```
}
13
14
    mt19937 rng(time(0));
15
    const int P=findPrime(rng()%900000000+1000000000);
16
    struct StrHash
18
    {
19
        int n;
        vector<int> h,p;
20
21
        StrHash(const string &s){ init(s); }
22
23
24
        void init(const string &s)
25
             n=s.size();
26
27
            h.resize(n+1);
             p.resize(n+1);
28
29
             p[0]=1;
             for (int i=0;i<n;i++) h[i+1]=(10ll*h[i]+s[i]-'a')%P;</pre>
30
31
             for (int i=0;i<n;i++) p[i+1]=10ll*p[i]%P;</pre>
32
33
        //查询 [l,r) 的区间哈希
34
        int get(int l,int r) { return (h[r]+1ll*(P-h[l])*p[r-l])%P; }
35
    };
    KMP
    vector<int> KMP(const string &s)
2
    {
3
        int now=0;
        vector<int> pre(s.size(),0);
4
        for (int i=1;i<s.size();i++)</pre>
             while (now&&s[i]!=s[now]) now=pre[now-1];
             if (s[i]==s[now]) now++;
             pre[i]=now;
10
        return pre;
11
12
    }
    Z函数
    vector<int> zFunction(string s)
    {
2
3
        int n=s.size();
        vector<int> z(n);
4
        z[0]=n;
        for (int i=1,j=1;i<n;i++)</pre>
            z[i]=max(0,min(j+z[j]-i,z[i-j]));
            while (i+z[i]<n&&s[z[i]]==s[i+z[i]]) z[i]++;</pre>
             if (i+z[i]>j+z[j]) j=i;
        }
11
        return z;
12
    }
13
    AC 自动机
    struct ACAM
1
2
    {
        static constexpr int ALPHABET=26;
3
        struct Node
             int len;
             int link;
             array<int,ALPHABET> next;
            Node():len{0},link{0},next{}{}
        };
10
```

```
vector<Node> t;
12
13
        ACAM() { init(); }
14
15
        void init()
16
17
        {
18
             t.assign(2,Node());
             t[0].next.fill(1);
19
             t[0].len=-1;
20
        }
21
22
        int newNode()
23
24
             t.emplace_back();
25
             return t.size()-1;
26
27
        }
28
        int add(const string &a)
29
30
        {
             int p=1;
31
32
             for (auto c:a)
33
34
                 int x=c-'a';
35
                 if (t[p].next[x]==0)
                 {
36
37
                      t[p].next[x]=newNode();
                      t[t[p].next[x]].len=t[p].len+1;
38
39
40
                 p=t[p].next[x];
41
42
             return p;
        }
43
44
45
        void work()
46
        {
47
             queue<int> q;
             q.push(1);
48
             while (!q.empty())
49
50
             {
                 int x=q.front();
51
52
                 q.pop();
                 for (int i=0;i<ALPHABET;i++)</pre>
53
54
                      if (t[x].next[i]==0) t[x].next[i]=t[t[x].link].next[i];
55
                      else
56
57
                      {
                          t[t[x].next[i]].link=t[t[x].link].next[i];
58
                          q.push(t[x].next[i]);
                      }
60
61
                 }
             }
62
63
        int next(int p,int x) { return t[p].next[x]; }
65
66
        int link(int p) { return t[p].link; }
67
68
        int size() { return t.size(); }
69
70
    };
    后缀数组
    struct SA
2
    {
        int n;
3
        vector<int> sa,rk,lc;
        SA(const string &s)
             n=s.length();
             sa.resize(n);
             rk.resize(n);
```

```
lc.resize(n-1);
10
11
           iota(sa.begin(),sa.end(),0);
           sort(sa.begin(),sa.end(),[&](int a,int b){ return s[a]<s[b]; });</pre>
12
           rk[sa[0]]=0;
13
           for (int i=1;i<n;i++) rk[sa[i]]=rk[sa[i-1]]+(s[sa[i]]!=s[sa[i-1]]);</pre>
           int k=1:
15
           vector<int> tmp,cnt(n);
16
           tmp.reserve(n);
17
           while (rk[sa[n-1]] < n-1)
18
19
           {
               tmp.clear();
20
21
               for (int i=0;i<k;i++) tmp.push_back(n-k+i);</pre>
22
               for (auto i:sa)
                   if (i>=k) tmp.push_back(i-k);
23
               fill(cnt.begin(),cnt.end(),0);
24
               for (int i=0;i<n;i++) cnt[rk[i]]++;</pre>
25
26
               for (int i=1;i<n;i++) cnt[i]+=cnt[i-1];</pre>
               for (int i=n-1;i>=0;i--) sa[--cnt[rk[tmp[i]]]]=tmp[i];
27
28
               swap(rk,tmp);
               rk[sa[0]]=0;
29
               for (int i=1;i<n;i++)</pre>
30
                   31
               k <<=1;
32
           for (int i=0,j=0;i<n;i++)</pre>
34
35
           {
               if (rk[i]==0) j=0;
36
               else
37
38
                   for (j-=j>0;i+j<n&&sa[rk[i]-1]+j<n&&s[i+j]==s[sa[rk[i]-1]+j];) j++;</pre>
39
40
                   lc[rk[i]-1]=j;
               41
           }
42
43
   };
44
     (广义) 后缀自动机
1
   struct SAM
2
   {
3
       static constexpr int ALPHABET=26;
4
       struct Node
           int len;
           int link;
           array<int,ALPHABET> next;
8
           Node():len{},link{},next{} {}
       };
10
11
       vector<Node> t;
12
13
       SAM() { init(); }
14
15
       void init()
16
17
18
           t.assign(2,Node());
           t[0].next.fill(1);
19
           t[0].len=-1;
20
21
       }
22
23
       int newNode()
24
           t.emplace_back();
26
           return t.size()-1;
       }
27
28
       int extend(int lst,int c)
29
30
           if (t[lst].next[c]&&t[t[lst].next[c]].len==t[lst].len+1)
31
               return t[lst].next[c];
32
           int p=lst,np=newNode(),flag=0;
33
```

```
t[np].len=t[p].len+1;
34
35
            while (!t[p].next[c])
36
             {
                 t[p].next[c]=np;
37
                 p=t[p].link;
39
40
            if (!p)
41
             {
                 t[np].link=1;
42
43
                 return np;
44
45
            int q=t[p].next[c];
            if (t[q].len==t[p].len+1)
46
47
            {
                 t[np].link=q;
48
49
                 return np;
            if (p==lst) flag=1,np=0,t.pop_back();
51
            int nq=newNode();
            t[nq].link=t[q].link;
53
54
            t[nq].next=t[q].next;
55
            t[nq].len=t[p].len+1;
56
            t[q].link=t[np].link=nq;
            while (p&&t[p].next[c]==q)
58
            {
59
                 t[p].next[c]=nq;
60
                 p=t[p].link;
61
62
            return flag?nq:np;
        }
63
64
        int add(const string &a)
65
66
67
            int p=1;
            for (auto c:a) p=extend(p,c-'a');
68
69
            return p;
        }
70
71
        int next(int p,int x) { return t[p].next[x]; }
72
73
        int link(int p) { return t[p].link; }
74
75
        int len(int p) { return t[p].len; }
76
77
        int size() { return t.size(); }
78
79
    };
    Manacher
    vector<int> manacher(vector<int> s)
1
2
    {
3
        vector<int> t{0};
        for (auto c:s)
4
        {
            t.push_back(c);
            t.push_back(0);
        }
        int n=t.size();
10
        vector<int> r(n);
        for (int i=0,j=0;i<n;i++)</pre>
11
12
            if (j*2-i>=0&&j+r[j]>i) r[i]=min(r[j*2-i],j+r[j]-i);
13
            while (i-r[i]>=0&&i+r[i]<n&&t[i-r[i]]==t[i+r[i]]) r[i]++;</pre>
            if (i+r[i]>j+r[j]) j=i;
15
16
17
        return r;
    }
18
```

回文自动机

```
struct PAM
2
    {
        static constexpr int ALPHABET_SIZE=28;
        struct Node
             int len,link,cnt;
             array<int,ALPHABET_SIZE> next;
             Node():len\{\},link\{\},cnt\{\},next\{\}\{\}
        };
        vector<Node> t;
10
        int suff;
11
12
        string s;
13
        PAM() { init(); }
14
15
        void init()
16
17
             t.assign(2,Node());
18
             t[0].len=-1;
             suff=1;
20
21
             s.clear();
        }
22
23
24
        int newNode()
25
        {
             t.emplace_back();
26
             return t.size()-1;
27
        }
28
29
        bool add(char c,char offset='a')
30
31
32
             int pos=s.size();
             s+=c;
33
34
             int let=c-offset;
             int cur=suff,curlen=0;
35
36
             while (1)
37
             {
                 curlen=t[cur].len;
38
                 if (pos-curlen-1>=0&&s[pos-curlen-1]==s[pos]) break;
39
40
                 cur=t[cur].link;
41
             if (t[cur].next[let])
42
43
                 suff=t[cur].next[let];
44
                 return 0;
45
46
             int num=newNode();
47
             suff=num;
49
             t[num].len=t[cur].len+2;
             t[cur].next[let]=num;
50
51
             if (t[num].len==1)
52
             {
53
                  t[num].link=t[num].cnt=1;
                 return 1;
54
55
             while (1)
56
57
             {
58
                 cur=t[cur].link;
                 curlen=t[cur].len;
59
60
                 if (pos-curlen-1>=0&&s[pos-curlen-1]==s[pos])
61
                      t[num].link=t[cur].next[let];
62
63
                      break;
64
65
             t[num].cnt=t[t[num].link].cnt+1;
66
             return 1;
67
    };
69
```

图论

Dijkstra

注意设定合适的 inf。

```
vector<i64> dijk(const vector<vector<pair<int,i64>>> &adj,int s)
2
    {
3
        int n=adj.size();
        using pa=pair<i64,int>;
        vector<i64> d(n,inf);
        vector<int> ed(n);
        priority_queue<pa,vector<pa>,greater<pa>> q;
        q.push({0,s}); d[s]=0;
        while (!q.empty())
10
            int u=q.top().second;
11
12
            q.pop();
            ed[u]=1;
13
            for (auto [v,w]:adj[u])
                if (d[u]+w< d[v])
15
                {
16
17
                    d[v]=d[u]+w;
                    q.push({d[v],v});
18
19
            while (!q.empty()&&ed[q.top().second]) q.pop();
20
21
22
        return d;
   }
23
   SPFA
    注意设定合适的 inf。
   vector<i64> spfa(const vector<vector<pair<int,i64>>> &adj,int s)
   {
2
3
        int n=adj.size();
        assert(n);
        queue<int> q;
        vector<int> len(n),ed(n);
        vector<i64> d(n,inf);
        q.push(s); d[s]=0;
        while (!q.empty())
            int u=q.front();
11
12
            q.pop();
13
            ed[u]=0;
            for (auto [v,w]:adj[u])
14
15
                if (d[u]+w<d[v])
16
                {
                    d[v]=d[u]+w;
17
                    len[v]=len[u]+1;
18
                    if (len[v]>n) return {};
19
                    if (!ed[v]) ed[v]=1,q.push(v);
                }
21
22
        return d;
23
   }
24
   Johnson
    vector<vector<i64>> dijk(const vector<vector<pair<int,i64>>> &adj)
    {
2
        vector<vector<i64>> res;
        for (int i=0;i<adj.size();i++)</pre>
            res.push_back(dijk(adj,i));
        return res;
   }
   vector<i64> spfa(const vector<vector<pair<int,i64>>> &adj)
```

```
{
10
        int n=adj.size();
11
        assert(n);
12
        queue<int> q;
13
14
        vector<int> len(n),ed(n,1);
        vector<i64> d(n);
15
        for (int i=0;i<n;i++) q.push(i);</pre>
16
        while (!q.empty())
17
18
             int u=q.front();
19
20
             q.pop();
21
             ed[u]=0;
             for (auto [v,w]:adj[u])
22
                 if (d[u]+w<d[v])
23
24
                 {
                      d[v]=d[u]+w;
25
26
                      len[v]=len[u]+1;
                      if (len[v]>n) return {};
27
                      if (!ed[v]) ed[v]=1,q.push(v);
28
                 }
29
30
31
        return d;
    }
32
33
    vector<vector<i64>> john(vector<vector<pair<int,i64>>> adj)
34
35
    {
        int n=adj.size();
36
        assert(n);
37
38
        auto h=spfa(adj);
        if (!h.size()) return {};
39
        for (int u=0;u<n;u++)</pre>
40
             for (auto &[v,w]:adj[u])
41
42
                 w+=h[u]-h[v];
43
        auto res=dijk(adj);
        for (int u=0;u<n;u++)</pre>
44
45
             for (int v=0;v<n;v++)</pre>
                 if (res[u][v]!=inf)
46
                      res[u][v]-=h[u]-h[v];
47
48
        return res;
    }
49
    强连通分量
    struct SCC
1
2
    {
        int n,cur,cnt;
3
        vector<vector<int>> adj;
        vector<int> stk,dfn,low,bel;
        SCC() {}
        SCC(int n) { init(n); }
        void init(int n)
10
11
        {
             this->n=n;
12
13
             adj.assign(n,{});
             stk.clear();
14
             dfn.assign(n,-1);
15
16
             low.resize(n);
17
             bel.assign(n,-1);
18
             cur=cnt=0;
19
        void add(int u,int v) { adj[u].push_back(v); }
21
22
23
        void dfs(int x)
24
             dfn[x]=low[x]=cur++;
25
             stk.push_back(x);
26
             for (auto y:adj[x])
27
28
             {
```

```
if (dfn[y]==-1)
29
30
                 {
                      dfs(y);
31
                      low[x]=min(low[x],low[y]);
32
                 else if (bel[y]==-1) low[x]=min(low[x],dfn[y]);
34
35
             if (dfn[x]==low[x])
36
37
             {
                 int y;
38
                 do
39
40
                 {
41
                      y=stk.back();
                      bel[y]=cnt;
42
                      stk.pop_back();
43
                 } while (y!=x);
44
45
                 cnt++;
             }
46
47
        }
48
        vector<int> work()
49
50
51
             for (int i=0;i<n;i++)</pre>
                 if (dfn[i]==-1) dfs(i);
             return bel;
53
54
        }
55
        struct Graph
56
57
             int n;
58
59
             vector<pair<int,int>> edges;
             vector<int> siz,cnte;
60
61
        };
62
        Graph compress()
63
64
             Graph G;
65
             G.n=cnt;
66
             G.siz.resize(cnt);
67
             G.cnte.resize(cnt);
68
             for (int i=0;i<n;i++)</pre>
69
70
                 G.siz[bel[i]]++;
71
72
                 for (auto j:adj[i])
                      if (bel[i]!=bel[j])
73
74
                          G.edges.emplace_back(bel[j],bel[i]);
             }
75
             return G;
        };
77
78
    };
    边双连通分量
    struct EBCC
    {
2
3
        vector<vector<int>> adj;
        vector<int> stk,dfn,low,bel;
        int cur,cnt;
        EBCC() {}
        EBCC(int n) { init(n); }
        void init(int n)
11
12
        {
13
             this->n=n;
             adj.assign(n,{});
14
15
             dfn.assign(n,-1);
             low.resize(n);
16
17
             bel.assign(n,-1);
             stk.clear();
18
```

```
cur=cnt=0;
19
20
         }
21
         void add(int u,int v)
22
23
             adj[u].push_back(v);
24
25
             adj[v].push_back(u);
         }
26
27
         void dfs(int x,int p)
28
29
30
             dfn[x]=low[x]=cur++;
31
             stk.push_back(x);
             for (auto y:adj[x])
32
33
             {
                  if (y==p) continue;
34
35
                  if (dfn[y]==-1)
                  {
36
37
                       dfs(y,x);
                       low[x]=min(low[x],low[y]);
38
39
                  else if (bel[y]=-1\&\&dfn[y]<dfn[x]) low[x]=min(low[x],dfn[y]);
40
41
             if (dfn[x]==low[x])
42
43
             {
                  int y;
44
45
                  do
                  {
46
47
                       y=stk.back();
48
                      bel[y]=cnt;
49
                      stk.pop_back();
                  } while (y!=x);
50
51
                  cnt++;
             }
52
         }
53
54
         vector<int> work()
55
56
         {
             dfs(0,-1);
57
             return bel;
58
         }
59
60
         struct Graph
61
62
         {
63
              int n;
64
             vector<pair<int,int>> edges;
             vector<int> siz,cnte;
65
         };
67
68
         Graph compress()
69
             Graph G;
70
             G.n=cnt;
             G.siz.resize(cnt);
72
73
             G.cnte.resize(cnt);
             for (int i=0;i<n;i++)</pre>
74
75
             {
                  G.siz[bel[i]]++;
                  for (auto j:adj[i])
77
78
                       if (bel[i] < bel[j]) G.edges.emplace_back(bel[i],bel[j]);</pre>
79
80
                       else if (i<j) G.cnte[bel[i]]++;</pre>
81
                  }
82
83
             return G;
84
         };
    };
```

轻重链剖分

```
struct HLD
1
2
    {
        int n;
        vector<int> siz,top,dep,pa,in,out,seq;
        vector<vector<int>> adj;
        int cur;
        HLD(){}
        HLD(int n) { init(n); }
10
        void init(int n)
11
12
             this->n=n;
13
             siz.resize(n);
14
15
             top.resize(n);
             dep.resize(n);
16
17
             pa.resize(n);
             in.resize(n);
18
19
             out.resize(n);
             seq.resize(n);
20
21
             cur=0;
             adj.assign(n,{});
22
        }
23
24
        void addEdge(int u,int v)
25
26
             adj[u].push_back(v);
27
             adj[v].push_back(u);
28
29
        }
30
31
        void work(int rt=0)
32
             top[rt]=rt;
33
34
             dep[rt]=0;
             pa[rt]=-1;
35
36
             dfs1(rt);
37
             dfs2(rt);
38
        }
39
40
        void dfs1(int u)
41
             if (pa[u]!=-1) adj[u].erase(find(adj[u].begin(),adj[u].end(),pa[u]));
42
             siz[u]=1;
43
             for (auto &v:adj[u])
44
45
             {
46
                 pa[v]=u;
                 dep[v]=dep[u]+1;
47
48
                 dfs1(v);
49
                 siz[u]+=siz[v];
                 if (siz[v]>siz[adj[u][0]])
50
51
                      swap(v,adj[u][0]);
             }
52
53
        }
54
55
        void dfs2(int u)
56
             in[u]=cur++;
57
58
             seq[in[u]]=u;
             for (auto v:adj[u])
59
60
                 top[v]=(v==adj[u][0])?top[u]:v;
61
                 dfs2(v);
62
63
             out[u]=cur;
64
65
        }
66
        int lca(int u,int v)
67
68
             while (top[u]!=top[v])
69
```

```
70
             {
71
                  if (dep[top[u]]>dep[top[v]]) u=pa[top[u]];
72
                  else v=pa[top[v]];
73
             }
74
             return dep[u] < dep[v] ?u:v;</pre>
         }
75
76
         int dist(int u,int v) { return dep[u]+dep[v]-(dep[lca(u,v)]<<1); }</pre>
77
78
79
         int jump(int u,int k)
80
81
             if (dep[u] < k) return -1;</pre>
82
             int d=dep[u]-k;
             while (dep[top[u]]>d) u=pa[top[u]];
83
84
             return seq[in[u]-dep[u]+d];
85
         bool isAncester(int u,int v) { return in[u]<=in[v]&&in[v]<out[u]; }</pre>
87
88
         int rootedParent(int u,int v)//u->root,v->point
89
90
91
             if (u==v) return u;
             if (!isAncester(v,u)) return pa[v];
92
             auto it=upper_bound(adj[v].begin(),adj[v].end(),u,[&](int x,int y){ return in[x]<in[y]; })-1;
             return *it;
94
95
         }
96
         int rootedSize(int u,int v)//same as rootedParent
97
98
             if (u==v) return n;
99
             if (!isAncester(v,u)) return siz[v];
100
             return n-siz[rootedParent(u,v)];
101
         }
102
103
         int rootedLca(int a,int b,int c) { return lca(a,b)^lca(b,c)^lca(c,a); }
104
    };
105
    2-SAT
    struct TwoSat
1
2
    {
         int n;
         vector<vector<int>> e:
         vector<bool> ans;
         TwoSat(int n):n(n),e(n<<1),ans(n){}</pre>
         void addClause(int u,bool f,int v,bool g)
             e[u*2+!f].push_back(v*2+g);
11
             e[v*2+!g].push_back(u*2+f);
12
13
         }
14
         bool satisfiable()
15
16
17
             vector<int> id(n*2,-1),dfn(n*2,-1),low(n*2,-1),stk;
             int now=0,cnt=0;
18
             function<void(int)> tarjan=[&](int u)
19
20
             {
                  stk.push_back(u);
21
                  dfn[u]=low[u]=now++;
22
                  for (auto v:e[u])
23
                      if (dfn[v]==-1)
25
                      {
26
27
                           tarjan(v);
                           low[u]=min(low[u],low[v]);
28
29
                      else if (id[v]==-1)
30
                           low[u]=min(low[u],dfn[v]);
31
                  }
32
```

```
if (dfn[u] == low[u])
33
34
                      int v;
35
                      do
36
37
                      {
                           v=stk.back();
38
39
                           stk.pop_back();
                          id[v]=cnt;
40
                      } while (v!=u);
41
42
                      cnt++;
                 }
43
44
             };
             for (int i=0;i<n*2;i++)</pre>
45
                  if (dfn[i]==-1)
46
47
                      tarjan(i);
             for (int i=0;i<n;i++)</pre>
48
49
             {
                  if (id[i*2]==id[i*2+1]) return 0;
50
                  ans[i]=id[i*2]>id[i*2+1];
51
             }
52
             return 1;
53
54
55
         vector<bool> answer() { return ans; }
    最大流
    template <class T>
    struct MaxFlow
2
3
         struct _Edge
4
         {
             int to;
             _Edge(int to,T cap):to(to),cap(cap){}
         };
10
         int n;
11
12
         vector<_Edge> e;
         vector<vector<int>> g;
13
14
         vector<int> cur,h;
15
         MaxFlow(){}
16
         MaxFlow(int n) { init(n); }
17
18
19
         void init(int n)
20
             this->n=n;
21
22
             e.clear();
             g.assign(n,{});
23
24
             cur.resize(n);
25
             h.resize(n);
         }
26
27
         bool bfs(int s,int t)
28
29
             h.assign(n,-1);
30
             queue<int> que;
31
32
             h[s]=0;
33
             que.push(s);
34
             while (!que.empty())
35
                  const int u=que.front();
                  que.pop();
37
                  for (int i:g[u])
38
39
                      auto [v,c]=e[i];
40
41
                      if (c>0&&h[v]==-1)
42
                      {
                           h[v]=h[u]+1;
43
                           if (v==t) return 1;
44
```

```
que.push(v);
45
46
                       }
                  }
47
              }
48
              return 0;
         }
50
51
         T dfs(int u,int t,T f)
52
53
              if (u==t) return f;
54
              auto r=f;
55
              for (int &i=cur[u];i<int(g[u].size());i++)</pre>
56
57
                  const int j=g[u][i];
58
                  auto [v,c]=e[j];
59
                  if (c>0\&\&h[v]==h[u]+1)
60
61
                  {
                       auto a=dfs(v,t,min(r,c));
62
63
                       e[j].cap-=a;
64
                       e[j^1].cap+=a;
65
                       r-=a;
                       if (r==0) return f;
66
67
                  }
              }
              return f-r;
69
70
         }
71
         void addEdge(int u,int v,T c)
72
              g[u].push_back(e.size());
74
75
              e.emplace_back(v,c);
              g[v].push_back(e.size());
76
77
              e.emplace_back(u,0);
78
79
80
         T flow(int s,int t)
81
         {
              T ans=0;
82
83
              while (bfs(s,t))
84
85
                  cur.assign(n,0);
                  ans+=dfs(s,t,numeric_limits<T>::max());
86
87
88
              return ans;
89
         }
90
         vector<bool> minCut()
91
92
         {
              vector<bool> c(n);
93
94
              for (int i=0;i<n;i++) c[i]=(h[i]!=-1);</pre>
95
              return c;
         }
96
97
         struct Edge
98
99
         {
              int from;
100
              int to;
101
102
              T cap;
              T flow;
103
         };
104
105
         vector<Edge> edges()
106
107
              vector<Edge> a;
108
109
              for (int i=0;i<e.size();i+=2)</pre>
110
              {
111
                  Edge x;
                  x.from=e[i+1].to;
112
                  x.to=e[i].to;
113
114
                  x.cap=e[i].cap+e[i+1].cap;
                  x.flow=e[i+1].cap;
115
```

```
a.push_back(x);
116
117
              }
118
              return a;
         }
119
    };
     最小费用最大流
     template <class T>
     struct MinCostFlow
 2
 3
     {
 4
         struct _Edge
              int to;
              T cap;
              T cost:
              _Edge(int to,T cap,T cost):to(to),cap(cap),cost(cost){}
10
         };
11
12
         int n;
13
14
         vector<_Edge> e;
         vector<vector<int>> g;
15
         vector<T> h,dis;
16
17
         vector<int> pre;
18
19
         bool john(int s,int t)
20
              dis.assign(n,numeric_limits<T>::max());
21
22
              pre.assign(n,-1);
              priority_queue<pair<T,int>>,vector<pair<T,int>>>,greater<pair<T,int>>>> q;
23
24
              dis[s]=0;
              q.emplace(0,s);
25
              while (!q.empty())
27
                  T d=q.top().first;
28
29
                  int u=q.top().second;
                  q.pop();
30
31
                  if (dis[u]!=d) continue;
                  for (int i:g[u])
32
33
                  {
                       int v=e[i].to;
34
                       T cap=e[i].cap;
35
                       T cost=e[i].cost;
                       if (cap>0&&dis[v]>d+h[u]-h[v]+cost)
37
38
                       {
                            \label{eq:discontinuity} \mbox{dis}[v] = \mbox{d+h}[u] - \mbox{h}[v] + \mbox{cost};
39
                           pre[v]=i;
40
41
                            q.emplace(dis[v],v);
                       }
42
43
44
              return dis[t]!=numeric_limits<T>::max();
45
         }
46
47
48
         MinCostFlow(){}
         MinCostFlow(int n) { init(n); }
49
50
         void init(int n_)
51
52
         {
53
              n=n_;
54
              e.clear();
              g.assign(n,{});
         }
56
57
58
         void addEdge(int u,int v,T cap,T cost)
59
              g[u].push_back(e.size());
              e.emplace_back(v,cap,cost);
61
              g[v].push_back(e.size());
62
              e.emplace_back(u,0,-cost);
63
```

```
}
64
65
         pair<T,T> flow(int s,int t)
66
67
             T flow=0;
68
              T cost=0;
69
70
             h.assign(n,0);
             while (john(s,t))
71
72
                  for (int i=0;i<n;i++) h[i]+=dis[i];</pre>
73
                  T aug=numeric_limits<int>::max();
74
                  for (int i=t;i!=s;i=e[pre[i]^1].to)
75
                      aug=min(aug,e[pre[i]].cap);
76
                  for (int i=t;i!=s;i=e[pre[i]^1].to)
77
78
                  {
                       e[pre[i]].cap-=aug;
79
80
                       e[pre[i]^1].cap+=aug;
81
82
                  flow+=aug;
                  cost+=aug*h[t];
83
84
              return make_pair(flow,cost);
85
86
         }
87
         struct Edge
88
89
         {
             int from;
90
              int to;
91
92
             T cap;
93
             T cost:
94
              T flow;
         };
95
96
         vector<Edge> edges()
97
98
99
              vector<Edge> a;
              for (int i=0;i<e.size();i+=2)</pre>
100
              {
101
102
                  Edge x;
                  x.from=e[i+1].to;
103
104
                  x.to=e[i].to;
                  x.cap=e[i].cap+e[i+1].cap;
105
                  x.cost=e[i].cost;
106
107
                  x.flow=e[i+1].cap;
                  a.push_back(x);
108
109
             return a;
110
111
    };
112
     计算几何
     EPS
 1
     const double eps=1e-8;
     int sgn(double x)
 2
     {
 3
         if (fabs(x)<eps) return 0;</pre>
         if (x>0) return 1;
         return -1;
    }
     Point
```

template <class T>

Point(T $x_{=0}$,T $y_{=0}$): $x(x_{-})$, $y(y_{-})$ {}

struct Point

1 2

3 {

```
7
        Point & operator += (Point p) &
8
            x+=p.x;
            y+=p.y;
10
            return *this;
11
12
13
        Point & operator -= (Point p) &
14
15
16
            x-=p.x;
17
            y-=p.y;
            return *this;
18
19
20
        Point &operator *= (T v) &
21
22
            x*=v:
23
24
            y*=v;
            return *this;
25
        }
26
27
        Point operator - () const { return Point(-x,-y); }
28
        friend Point operator + (Point a,Point b) { return a+=b; }
30
        friend Point operator - (Point a,Point b) { return a-=b; }
31
        friend Point operator * (Point a,T b) { return a*=b; }
32
        friend Point operator * (T a,Point b) { return b*=a; }
33
        friend bool operator == (Point a,Point b) { return a.x==b.x&&a.y==b.y; }
35
36
        friend istream &operator >> (istream &is,Point &p) { return is>>p.x>>p.y; }
37
38
39
        friend ostream &operator << (ostream &os,Point p) { return os<<'('<<p.x<<','<<p.y<<')'; }</pre>
    };
40
41
    template <class T>
42
    int sgn(const Point<T> &a) { return a.y>0||(a.y==0&&a.x>0)?1:-1; }
43
44
    template <class T>
45
    T dot(Point<T> a,Point<T> b) { return a.x*b.x+a.y*b.y; }
47
    template <class T>
48
49
    T cross(Point<T> a,Point<T> b) { return a.x*b.y-a.y*b.x; }
50
51
    template <class T>
    T square(Point<T> p) { return dot(p,p); }
52
    template <class T>
54
    double length(Point<T> p) { return sqrt(double(square(p))); }
55
56
    long double length(Point<long double> p) { return sqrt(square(p)); }
57
    Line
1
    template <class T>
    struct Line
2
3
4
        Point<T> a,b;
        Line(Point<T> a_=Point<T>(),Point<T> b_=Point<T>()):a(a_),b(b_) {}
5
    };
    距离
    template <class T>
    double dis_PP(Point<T> a,Point<T> b) { return length(a-b); }
    template <class T>
    \label{eq:double_dis_PL(Point<T> a, Line<T> l) { return } fabs(cross(a-l.a,a-l.b))/dis_PP(l.a,l.b); } \\
```

```
template <class T>
    double dis_PS(Point<T> a,Line<T> l)
8
        if (dot(a-l.a,l.b-l.a)<0) return dis_PP(a,l.a);</pre>
10
11
        if (dot(a-l.b,l.a-l.b)<0) return dis_PP(a,l.b);</pre>
        return dis_PL(a,l);
12
    }
13
    点绕中心旋转
   template <class T>
    Point<T> rotate(Point<T> a,double alpha)
    { return Point<T>(a.x*cos(alpha)-a.y*sin(alpha),a.x*sin(alpha)+a.y*cos(alpha)); }
    关于线的对称点
    template <class T>
1
    Point<T> lineRoot(Point<T> a,Line<T> l)
2
3
        Point<T> v=l.b-l.a;
        return l.a+v*(dot(a-l.a,v)/dot(v,v));
   }
    template <class T>
    Point<T> symmetry_PL(Point<T> a,Line<T> l) { return a+(lineRoot(a,l)-a)*2; }
    位置关系判断
    template <class T>
    bool pointOnSegment(Point<T> a,Line<T> l)
2
    { return (sgn(cross(a-l.a,a-l.b))==0)&&(sgn(dot(a-l.a,a-l.b))<=0); }
    template <class T>
   bool lineCrossLine(Line<T> a, Line<T> b)
    {
        double f1=cross(b.a-a.a,a.b-a.a),f2=cross(b.b-a.a,a.b-a.a);
        double g1=cross(a.a-b.a,b.b-b.a),g2=cross(a.b-b.a,b.b-b.a);
10
        return ((f1<0)^(f2<0))&&((g1<0)^(g2<0));
   }
11
12
13
    template <class T>
    bool pointOnLineLeft(Point<T> a,Line<T> l) { return cross(l.b-l.a,a-l.a)>0; }
14
15
    //适用任意多边形,O(n)
16
17
    template <class T>
18
    bool pointInPolygon(Point<T> a,const vector<Point<T>> &p)
19
20
        int n=p.size();
        for (int i=0;i<n;i++)</pre>
21
22
             if (pointOnSegment(a,Line<T>(p[i],p[(i+1)%n])))
                 return 1;
23
24
        bool t=0;
        for (int i=0;i<n;i++)</pre>
25
26
            Point<T> u=p[i],v=p[(i+1)%n];
27
            if (u.x<a.x\&\&v.x>=a.x\&\&pointOnLineLeft(a,Line<T>(v,u))) t^=1;
28
             if (u.x>=a.x&&v.x<a.x&&pointOnLineLeft(a,Line<T>(u,v))) t^=1;
29
        }
30
        return t;
31
32
   }
33
    //适用凸多边形,0(log n)
34
    template <class T>
35
    bool pointInPolygon_(Point<T> a,const vector<Point<T>> &p)
36
37
        int n=p.size():
38
        if (cross(a-p[0],p[1]-p[0])<0||cross(a-p[0],p[n-1]-p[0])>0) return 0;
39
        \textbf{if} \ (\texttt{pointOnSegment(a,Line} < T > (\texttt{p[0],p[1]})) \mid | \texttt{pointOnSegment(a,Line} < T > (\texttt{p[n-1],p[0]}))) \ \textbf{return} \ 1;
40
41
        int l=1,r=n-1;
```

```
while (l+1<r)
42
43
            int mid=(l+r)>>1;
44
            if (cross(a-p[1],p[mid]-p[1])<0) l=mid;</pre>
45
            else r=mid;
47
48
        if (cross(a-p[l],p[r]-p[l])>0) return 0;
        if (pointOnSegment(a,Line<T>(p[l],p[r]))) return 1;
49
50
51
   线段交点
   //小 心 平 行
   template <class T>
   Point<T> lineIntersection(Line<T> a,Line<T> b)
        Point<T> u=a.a-b.a,v=a.b-a.a,w=b.b-b.a;
        double t=cross(u,w)/cross(w,v);
        return a.a+t*v;
   }
   过定点做圆的切线
   template <class T>
   vector<Line<T>> tan_PC(Point<T> a,Point<T> c,T r)
2
3
    {
        Point<T> v=c-a;
        vector<Line<T>> res;
        int dis=dis_PP(a,c);
        if (sgn(dis-r)==0) res.push_back(rotate(v,acos(-1)/2));
        else if (dis>r)
            double alpha=asin(r/dis);
10
            res.push_back(rotate(v,alpha));
            res.push_back(rotate(v,-alpha));
12
13
14
        return res;
   }
15
    两圆交点
    template <class T>
   vector<Point<T>> circleIntersection(Point<T> c1,T r1,Point<T> c2,T r2)
2
3
    {
        auto get=[&](Point<T> c,T r,double alpha)->Point<T>
        { return Point<T>(c.x+cos(alpha)*r,c.y+sin(alpha)*r); };
5
        auto angle=[&](Point<T> a)->double { return atan2(a.x,a.y); };
        vector<Point<T>> res;
10
        double d=dis_PP(c1,c2);
        if (sgn(d)==0) return res;
11
        if (sgn(r1+r2-d)<0) return res;</pre>
12
13
        if (sgn(fabs(r1-r2)-d)>0) return res;
        double alpha=angle(c2-c1);
14
        double beta=acos((r1*r1-r2*r2+d*d)/(r1*d*2));
15
        Point<T> p1=get(c1,r1,alpha-beta),p2=get(c1,r1,alpha-beta);
16
17
        res.push_back(p1);
        if (p1!=p2) res.push_back(p2);
18
        return res;
19
   }
    多边形面积
   template <class T>
    double polygonArea(const vector<Point<T>> &p)
2
3
    {
        int n=p.size();
```

```
double res=0;
        for (int i=1;i<n-1;i++) res+=cross(p[i]-p[0],p[i+1]-p[0]);</pre>
        return fabs(res/2);
    自适应辛普森法
    //注意边界函数值不能小于 eps
    double f(double x) { return pow(x,0.5); }
    double calc(double l,double r)
5
        double mid=(l+r)/2.0;
        return (r-l)*(f(l)+f(r)+f(mid)*4.0)/6.0;
    double simpson(double l,double r,double lst)
    {
        double mid=(l+r)/2.0;
10
11
        double fl=calc(l,mid),fr=calc(mid,r);
        if (sgn(fl+fr-lst)==0) return fl+fr;
12
13
        else return simpson(l,mid,fl)+simpson(mid,r,fr);
   }
14
    静态凸包
    template <class T>
    vector<Point<T>> getHull(vector<Point<T>> p)
2
3
    {
        vector<Point<T>> h,l;
        sort(p.begin(),p.end(),[&](auto a,auto b)
5
            if (a.x!=b.x) return a.x<b.x;</pre>
            else return a.y<b.y;</pre>
8
        });
10
        p.erase(unique(p.begin(),p.end()),p.end());
        if (p.size()<=1) return p;</pre>
        for (auto a:p)
12
13
14
            while (h.size()>1&&sgn(cross(a-h.back(),a-h[h.size()-2]))<=0) h.pop_back();</pre>
            while (l.size()>1&&sgn(cross(a-l.back(),a-l[l.size()-2]))>=0) l.pop_back();
15
            l.push_back(a);
            h.push_back(a);
17
18
        l.pop_back();
19
        reverse(h.begin(),h.end());
20
21
        h.pop_back();
        l.insert(l.end(),h.begin(),h.end());
22
23
        return l;
   }
24
    旋转卡壳求直径
1
    template <class T>
    double getDiameter(vector<Point<T>> p)
2
    {
3
        double res=0;
5
        if (p.size()==2) return dis_PP(p[0],p[1]);
        int n=p.size();
        p.push_back(p.front());
        int j=2;
        for (int i=0;i<n;i++)</pre>
10
            while (sgn(cross(p[i+1]-p[i],p[j]-p[i])-cross(p[i+1]-p[i],p[j+1]-p[i]))<0)
11
                i = (i+1)%n:
12
            res=max({res,dis_PP(p[i],p[j]),dis_PP(p[i+1],p[j])});
13
14
        return res:
15
   }
```

半平面交

```
template <class T>
    vector<Point<T>> hp(vector<Line<T>> lines)
2
    {
        sort(lines.begin(),lines.end(),[&](auto l1,auto l2)
             auto d1=l1.b-l1.a;
             auto d2=l2.b-l2.a;
             if (sgn(d1)!=sgn(d2)) return sgn(d1)==1;
10
             return cross(d1,d2)>0;
        });
11
12
        deque<Line<T>> ls;
13
        deque<Point<T>> ps;
14
15
        for (auto l:lines)
16
17
             if (ls.empty())
18
             {
                 ls.push_back(l);
                 continue;
20
21
             while (!ps.empty()&&!pointOnLineLeft(ps.back(),l))
22
23
                 ps.pop_back();
24
                 ls.pop_back();
25
26
            while (!ps.empty()&&!pointOnLineLeft(ps[0],l))
27
28
             {
                 ps.pop_front();
30
                 ls.pop_front();
31
32
             if (cross(l.b-l.a,ls.back().b-ls.back().a) ==0)
33
34
                 if (dot(l.b-l.a,ls.back().b-ls.back().a)>0)
35
36
                     if (!pointOnLineLeft(ls.back().a,l))
37
                          assert(ls.size()==1);
38
39
                          ls[0]=l;
40
41
                     continue;
                 }
42
                 return {};
43
44
             ps.push_back(lineIntersection(ls.back(),l));
45
46
             ls.push_back(l);
        }
47
        while (!ps.empty()&&!pointOnLineLeft(ps.back(),ls[0]))
49
50
             ps.pop_back();
51
             ls.pop_back();
52
53
        if (ls.size()<=2) return {};</pre>
        ps.push_back(lineIntersection(ls[0],ls.back()));
54
55
        return vector(ps.begin(),ps.end());
    }
56
```