cmcR: Congruent Matching Cells Method in R for Cartridge Case Identification

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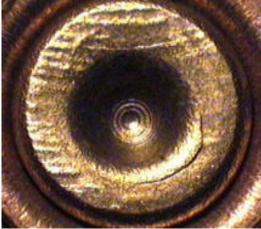
Abstract Firearm evidence identification is the process of analyzing bullets or cartridge cases left at a crime scene to determine if they originated from a particular firearm. Statistical methods have long been developed and used to aid in such analyses. The Congruent Matching Cells (CMC) method is one such method developed at the National Institute of Standards and Technology (NIST) to quantify the similarity between two spent cartridge cases based on the markings left by the firearm barrel during the firing process. We introduce the first open-source implementation of the CMC method in the R package **cmcR**. The package will bolster forensic researchers' abilities to investigate, validate, and improve upon current statistical methodology in the field of forensic science.

Introduction

A cartridge case is a type of firearm ammunition that contains a projectile (e.g., bullet, shots, or slug). When a firearm is discharged, the projectile stored in the cartridge case is propelled down the barrel of the firearm. In response, the rest of the cartridge case that remains inside of the firearm is forced towards the back of the barrel. The force with which the cartridge case is propelled backwards causes it to strike the back wall, known as the *breech face*, of the barrel. Markings due to, e.g., manufacturing imperfections are ingrained on the breech face. When the cartridge case slams against the breech face, these markings can be "stamped" into either the primer of the cartridge case or the cartridge case itself. The markings left on a cartridge case from the firearm's breech face are called *breech face impressions*.

An example of the breech face from a 12 GAUGE, single-shot shotgun is shown in Figure 1a. The hole in the center of the breech face houses the firing pin that shoots out to strike a region on the base of the cartridge case known as the *primer*. This in turn ignites the propellant within the cartridge case causing a deflagration of gases that propels the bullet forward down the barrel. Figure 1b shows a cartridge case fired from the shotgun shown in Figure 1a. This cartridge case displays both a circular impression left by the firing pin in the middle of the primer as well as breech face impressions left on the outer region of the primer not impressed into by the firing pin.





(a) Breech face of a shotgun barrel

(b) Breech face impressions on a cartridge case primer

Figure 1: Breech face of a barrel and breech face impression on a cartridge case (Doyle, 2019)

These breech face impressions are considered to be analogous to a firearm's "fingerprint" left on a cartridge case. Matching an expended cartridge case of unknown source to one of known source based on breech face impressions has been performed for over 100 years by forensic practitioners (Thompson, 2017). The development of computational and statistical methods to perform such identification has recently grown in interest (National Research Council, 2009).

One such method is the Congruent Matching Cells (CMC) method developed at NIST that involves partitioning a cartridge case image or scan into a grid of "correlation cells" to isolate areas containing identifying breech face impression markings (Song, 2013). Since its invention in 2012, researchers at NIST have developed a number of extensions and improvements of the CMC method. However, to

date there does not exist an openly available implementation of any of these techniques. Rather, many methods described in the CMC literature include a qualitative description of a proposed technique followed by results from the authors' implementation. The description of these methods do not delve into the intricacies of the implementation, which makes it especially difficult to validate or assess. Additionally, some procedures related to pre-processing the cartridge case data are seemingly done by-hand at NIST rather than with an automated method. This compounds the difficulty to accurately reproduce results. The **cmcR** package provides an open-source, fully-automatic implementation of the CMC method as originally described as well an extension known as the "High CMC" method proposed by Tong et al. (2015).

Cartridge case data

Cartridge case data commonly come in two forms: 2D grayscale images and 3D topographical scans. It is common in the CMC literature to use the 3D topographical scans to demonstrate the efficacy of a proposed method [(Tong et al., 2015), (Chen et al., 2017)]. A variety of scans are openly available for download through the NIST Ballistics Toolmark Research Database (Zheng et al., 2016). The cmcR package was designed specifically for use with the 3D topographies.

The 3D topographies are commonly stored in an .x3p (XML 3D Surface Profile) file format that includes metainformation such as who took the scan and the parameters under which the scan was taken (e.g., the lateral resolution in microns). The x3ptools package in R provides an interface to manipulate and visualize these .x3p files (Hofmann et al., 2019). The physical surface is represented using a surface matrix: a matrix of spatially-ordered elements or "pixels" whose values correspond to the height of the cartridge case surface at a particular location. Figure 2 shows the surface matrices of a known match (KM) pair of cartridge cases, meaning there were fired from the same firearm. Note that white regions in the images below represent unobserved or missing values. When read into R using the x3ptools package, these elements are encoded as NA. The size of a surface matrix depends on the lateral resolution with which the scans were taken. For example, a popular set of scans in the CMC literature were taken by Fadul et al. (2011); two of which are shown is the scan shown in Figure 2. These scans were taken with a lateral resolution of 6.25 microns per pixel. The actual surface matrices from this study vary around 1200 \times 1200 pixels in size.

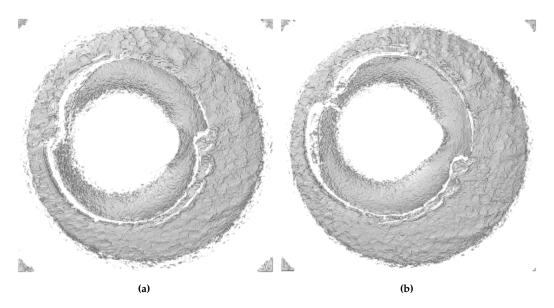


Figure 2: Two known match cartridge case scans from Fadul et al. (2011)

Only certain regions of a cartridge case contain identifying breech face impression markings. Song (2013) refers to these as "valid correlation regions" that are to be used to determine whether two cartridge cases match. The cell-based comparison procedure described in section 3.1 is designed to emphasize such regions. However, prior to applying this procedure cartridge scans must undergo some pre-processing to remove sections of the cartridge case surface that do not come into contact with the breech face of the barrel. These include a circular plateaued region in the center of the scan that is pushed aside by the firing pin during the firing process and clusters of observed values in the corners of the scan that are artifacts of the staging area in which the scan was captured. The task in pre-processing is to automatically remove these unwanted regions from the scan to accentuate unique markings left by the breech face. This is discussed in greater detail in section (LINK).

Cell-based surface matrix comparisons

Cell-based comparison procedure

The Congruent Matching Cells method was developed at the National Institute of Standards and Technology to quantify the similarity between two spent cartridge cases based on their breech face impressions. The CMC method involves dividing a breech face impression scan into a grid of cells and comparing each cell in one scan to a corresponding region in the other scan. This method is motivated by the fact that breech face markings are not uniformly impressed upon the cartridge case during the firing process. As such, only certain sections of the cartridge case have identifiable markings that make it possible to match to a firearm. Calculating a similarity score between the entirety of two cartridge case surfaces might not highlight these identifying regions. Instead, the number of highly similar cell pairs between the two scans can be used as a more granular similarity metric.

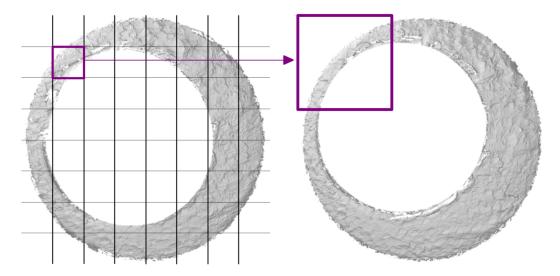


Figure 3: Illustration of comparing a "cell" in one cartridge case scan to a region in another

Figure 3 illustrates the cell-based comparison procedure between two cartridge case scans. The scan on the left is divided into a grid of 8×8 cells. Each cell is paired with an associated larger region in the other scan. The absolute location of each cell and region in their respective surface matrices remain constant. However, the scan on the right is rotated to determine the rotation at which the two scans are the most "similar," which is quantified using the *cross-correlation function* (CCF). For two real-valued, $M \times N$ matrices A and B, the cross-correlation function, denoted $(A \star B)$ can be defined as

$$(A \star B)[m,n] = \sum_{i=0}^{M} \sum_{j=0}^{N} A[i,j]B[(i+m)_{\text{mod } M}, (j+n)_{\text{mod } N}].$$

Note that this finite, discretized CCF is a matrix of elements representing the similarity between matrices *A* and *B* for various translations of matrix *B*. The index at which the CCF attains a maximum represents the translations needed to align *B* with *A*. In practice, calculating the CCF from the definition is often computationally intractable. The *Cross-Correlation Theorem* provides a feasible alternative to calculating the CCF. For two matrices *A* and *B*, the Cross-Correlation Theorem implies that

$$(A \star B)[m, n] = \mathcal{F}^{-1}\left(\overline{\mathcal{F}(A)} \cdot \mathcal{F}(B)\right)[m, n]$$

where \mathcal{F} and \mathcal{F}^{-1} denote the discrete Fourier and inverse discrete Fourier transforms, respectively (Brigham, 1988). Note that the multiplication on the right-hand side is pointwise (Hadamard) multiplication. This result allows us to trade the moving sum computations from the definition of the CCF for two forward Fourier transformation, a pointwise product, and an inverse Fourier transformation. The Fast Fourier Transform (FFT) algorithm is used to reduce the computational load considerably. However, a practical consideration for applying this method with cartridge case data is the large number of non-random missing values in a surface matrix. Recall that missing values are represented in Figures 2 and 3 as white pixels. The discrete Fourier transform is not defined for matrices containing missing values, so these need to be replaced. The convention adopted in the **cmcR** package is to replace missing values with 0 after standardizing a matrix by subtracting away its average height value and dividing by its standard deviation. Such standardization is commonly performed by authors at NIST [for example, (Ott et al., 2017)]. While replacing missing values is essential for using the

FFT-based method of calculating the CCF, doing so causes the CCF values to be "deflated" relative to the pairwise-complete cross-correlation in which only pairs of pixels in which neither element is missing are considered. However, the translation estimates obtained from this method are often good estimates for true translation values by which the two matrices align.

Figure 4 provides an example of the output from the FFT-based CCF calculation method. In the top-left we see a 72×72 pixel cell from one surface matrix. In the top-right we see this cell's associated region in the other surface matrix of dimension 216×216 (triple the cell's side lengths). The bottom-left shows the CCF "map" calculated using this FFT-based method. Although the CCF need not be bounded between -1 and 1 based on the definition, it is common to normalize the CCF for interpetability purposes and is done so in the **cmcR** package. A summary of the alignment parameters at which the CCF_{max} occurs is shown in the bottom-right. We can see that the two matrices are best-aligned when the cell is shifted "east" 20 pixels and "north" 9 pixels starting from the center of the region. The $\theta = -18$ indicates that the overall cartridge case scan from which the region (shown in the top-right) was extracted was rotated by -18 degrees for this comparion. The orange square in the top-right plot shows where the cell would be located if the translation were performed.

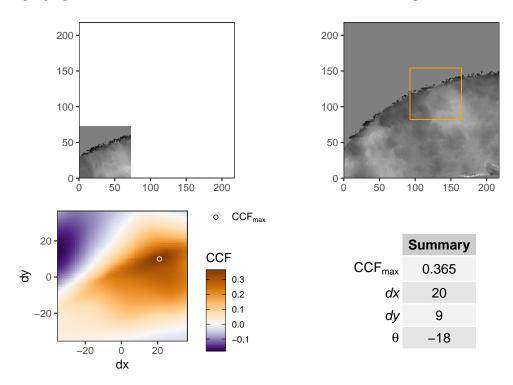


Figure 4: Example of a cross-correlation function "map" for a particular cell/region comparison

Using the estimated translation values at which the CCF $_{max}$ occurs, we can calculate the pairwise-complete cross-correlation between the cell and a cell-sized matrix extracted from the larger region where missing values are not replaced. Think of this as punching-out the matrix enclosed in the orange square shown in the top-right plot of Figure 4. This will be used as the high CCF $_{max}$ estimate. This cell-based comparison procedure is performed for each cell/region pair for various rotation values.

The Congruent Matching Cells method

A particular cell/region pair is deemed "highly similar" if it passes a collection of user-defined similarity criteria. The criteria are based on the fact that a pair of matching cartridge case scans are not necessarily aligned properly in their raw format. In particular, one cartridge case scan needs to be rotated and translated to align correctly the other. Let CCF_{max} , dx, dy, θ denote the "true" but unknown CCF, translation, and rotation values by which a particular pair aligns the best. These unknown alignment parameters can be estimated for each cell/region pair using the cell-based comparison procedure discussed in section 3.1. Let $CCF_{max,i}$, dx_i , dy_i , θ_i denote the estimated alignment parameter values for cell/region pair i, i = 1, ..., n. For a truly matching pair of cartridge cases, we would expect these alignment parameter estimates to agree with each other across cell/region pairs; at least up to some threshold. Conversely, we would expect the estimates to vary randomly for a truly *non*-matching pair. As such, the CMC method details how to determine whether a consensus exists among the

estimated alignment parameter values across the cell/region pairs. The initially proposed method by Song (2013) as well as an extension by Tong et al. (2015) known as the High CMC method are implemented in the **cmcR** package.

The initially proposed method

The method as originally proposed by Song (2013) considers only the alignment parameter estimates by which each cell/region pair attains its $CCF_{max,i}$. Intuitively, this can be thought of as only allowing each cell/region pair to "vote" for a single set of alignment parameter values. It's reasonable to assume that a consensus would exist amongst these values for a truly matching pair of cartridge cases. Song proposes using the median of the dx_i , dy_i , θ_i values as a consensus, although others are certainly plausible. Let \overline{dx} , \overline{dy} , $\overline{\theta}$ denote the consensual alignment parameter values. To declare a particular cell/region pair as "conruent matching," Song requires that (1) the pair's estimated alignment parameter values be within some threshold distance of the consensual values and (2) the CCF_{max} value is greater than some threshold. That is, for thresholds T_{dx} , T_{dy} , T_{θ} , T_{CCF} , cell/region pair i is declared a match if all of the following conditions hold:

- 1. $|dx_i \overline{dx}| \le T_{dx}$
- 2. $|dy_i \overline{dy}| \le T_{dy}$
- 3. $|\theta_i \bar{\theta}| \leq T_{\theta}$
- 4. $CCF_{max,i} \geq T_{CCF}$.

Song proposes using a minimum of 6 congruent matching cells to declare a cartridge case pair a match, although this threshold is based on a common threshold used in matching bullets via the striae left by a firearm barrel. This has been shown in subsequent extensions to not always be an effective threshold (Chen et al., 2017).

The High CMC method

Experimentation demonstrated that the assumption underlying the initially proposed method, that the CCF_{max,i} estimated alignment parameter values would reach a consensus across all cell/region pairs, does not always hold in general. In particular, if we only consider the "top" vote for each cell/region pair, then many pairs may vote far away from the consensual value and thus would not be declared congruent matching. However, Tong et al. (2015) observe that such pairs are often highly similar at the consensual rotation value, $\bar{\theta}$. The extension they propose utilizes the behavior of the estimated alignment parameter values more advantageously across various rotation values than the initially proposed method. Additionally, comparisons are performed in both "directions" so that each cartridge case scan takes on the role of the scan that is partitioned into a grid of cells.

Tong et al. (2015) propose applying the translation and CCF_{max} CMC criteria discussed in section 3.2.1 to the comparison results for each rotation value. In doing so, a CMC count for each rotation can be obtained. They identify a common behavior among known match cartridge case pairs that the CMC counts often attain a mode around the rotation value by which they align best. For known non-match pairs, the CMC counts often vary randomly across rotation values. These phenomena are illustrated in Figures 5 and 6. Figure 5 shows the CMC counts per rotation value in both directions for a known match pair of cartridge case scans from Fadul et al. (2011). We can clearly see a CMC mode around $\theta = -21$ in one direction and 21 or 24 in the other, which is to be expected for a known match pair. Figure 6, on the other hand, shows the CMC counts for a known non-match pair. We can see that no such CMC count mode is achieved.

Tong et al. (2015) introduce an additional criterion to identify a mode in the CMC per θ counts. Namely, they introduce a "high" CMC threshold defined to be CMC_{high} = CMC_{max} – τ for some constant τ (they choose τ = 1) where CMC_{max} is the maximum CMC count attained across all rotation values considered. In the example shown in Figure 5, CMC_{max} = 17 in one direction and 15 in the other. They propose finding the range of rotation values with associated CMC count greater than or equal to CMC_{high}. If this range is greater than the threshold T_{θ} , then there is evidence to suggest that a CMC count mode does not exist and the cartridge case pair is not a match. The CMC_{high} thresholds are shown as horizontal dashed lines in Figures 5 and 6. We can see in Figure 5 that the only θ values with associated CMC counts greater than or equal to CMC_{high} are adjacent. This particular cartridge case pair would "pass" the high CMC criterion. The pair shown in Figure 6 elicit considerably more

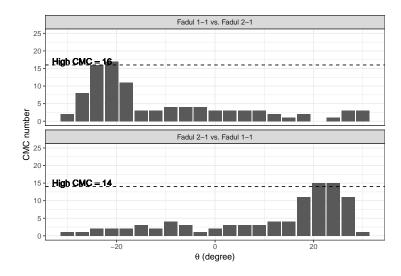


Figure 5: CMC count per rotation (θ) values in both directions for a KM cartridge case pair

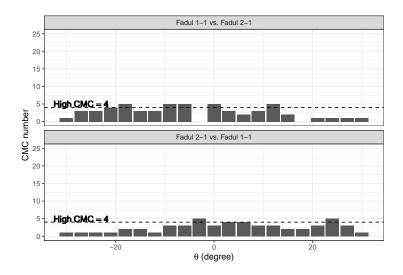


Figure 6: CMC count per rotation (θ) values in both directions for a KNM cartridge case pair

diffuse θ values with associated CMC count great than or equal to CMC_{high} and thus would not pass the high CMC criterion.

Cartridge case pairs that do not pass the high CMC criterion are assigned the CMC count under the initially proposed method. Pairs that do pass the criterion are assigned all CMCs in and within T_{θ} of the identified CMC count mode in both directions (excluding replicates). Among other considerations, Tong et al. (2015) do not indicate how to deal with adjacent CMC count ties (as is the case in the Fadul 1-2 vs. Fadul 1-1 direction in Figure 5) nor situations in which a CMC count mode is identified in one direction but not the other. This, again, illustates how a qualitative description of a method often fails to cover critical details. While individually small in scope, leaving such details ambiguous can quickly compound how difficult it is to effectively reproduce results.

The cmcR package

This section will highlight the **cmcR** package's functionality by walking through a possible use case. Many of the functions in this package provide the user with a variety of processing options with which they can experiment. This is due to the fact that processing techniques differ considerably among authors or are not discussed in great detail.

Pre-processing procedures

Studies in which cartridge cases are matched by forensic examiners often involve giving examiners a set of known matches and asking them to classify additional matches from a collection of unknown source scans. For brevity, we will consider a comparison between two cartridge cases. This particular pair of scans, as well as many other cartridge case scans, are openly available from the NIST Ballistics and Toolmarks Research Database. Figure 7 shows the pair of scans after performing the necessary preprocessing procedures. Note that the color scheme has been scaled by quantiles to visually highlight regions of the cartridge case scan containing strong breech face impression "signal."

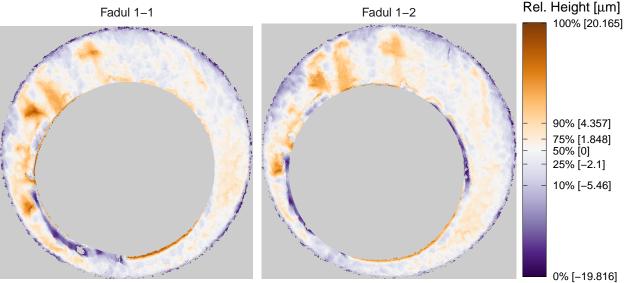


Figure 7: A known match pair of processed cartridge case scans

The family of functions in the **cmcR** package beginning with preProcess_ can be used to perform the necessary pre-processing steps for a pair of cartridge case scans to be comparable using the cell-based comparison procedure outlined in section 3.1. The implementation of many of these pre-processing procedures is inspired largely by Tai and Eddy (2018) who detail a fully-automatic procedure for processing cartridge case 2D images as opposed to 3D scans. The functions available include:

- 1. preProcess_ransac: estimates the height value of the breech face impressions in a scan using the Random Sample Consensus (RANSAC) robust, iterative plane-fitting algorithm (Fischler and Bolles, 1981).
- 2. preProcess_levelBF: extracts the observations containing breech face impressions from the scan using the estimated height value obtained from preProcess_levelBF.
- 3. preProcess_cropWS: removes rows/columns containing mostly if not all NA values from the surface matrix on the exterior of breech face impressions.
- 4. preProcess_removeFPCircle: detects and removes observations within the firing pin impression circle using the Hough Transform circle detection algorithm (Hough, 1962).
- preProcess_gaussFilter: applies a low-pass, high-pass, or band-pass Gaussian filter to the breech face impressions to reduce the effects of high frequency noise, low frequency global structure, or both, respectively.

See the **cmcR** package documentation for more information about these functions.

For computational purposes it is common the CMC literature to down-sample a surface matrix prior to performing the cell-based comparison procedure. The sample_x3p function from the x3ptools package can be used used to sample every *m*th row/column of a surface matrix. The selectBFImpression_sample_x3p performs all of these pre-processing procedures in a single call. The code to produce the first surface matrix shown in Figure 7 is given by the following example. Note that the RANSAC method relies on randomly selecting points within the surface matrix, so a seed needs to be set for reproducibility.

library(cmcR)
library(x3ptools)
library(magrittr)

Implementation of cell-based comparison procedure

The cell-based comparison procedure outlined in section 3.1 is implemented in the cellCCF_bothDirections function. In particular, the procedure is performed twice so that both cartridge case scans take on the role of the scan that is partitioned into a grid of cells. This is necessary to apply the High CMC logic discussed in section 3.2.2. Continuing with the current use case example, the code to perform this procedure on fadul1.1 and fadul1.2 is given by the following example.

The first few rows of results from the comparison between fadul1.1 and fadul1.2 in which fadul1.1 was divided into a grid of cells and fadul1.2 was rotated by 3 degrees is given below. Although a grid of 8×8 cells were used, there were only 43 cell/region pairs that contained a sufficient proportion of non-missing values (10% in this example). Recall that the features used in the CMC method are the CCF_{max} values (ccf column) and estimated alignment parameter values (dx, dy, and theta columns).

kmComparison\$comparison_1to2\$ccfResults\$`3` %>%
head()

cellNum	cellID	ccf	fft.ccf	dx	dy	theta
2	y = 1 - 73, x = 74 - 145	0.7762319	0.2108462	34	-30	3
3	y = 1 - 73, x = 146 - 217	0.1006877	0.1145874	29	22	3
4	y = 1 - 73, x = 218 - 289	0.1863672	0.1030728	-32	-16	3
5	y = 1 - 73, $x = 290 - 362$	0.8004083	0.3658809	5	4	3
6	y = 1 - 73, $x = 363 - 434$	0.7036884	0.2353348	22	10	3
7	y = 1 - 73, $x = 435 - 506$	0.7965972	0.1407746	-25	-18	3

Table 1: Example of output from cellCCF function

Congruent Matching Cells logic

cmcPlots\$initialCMC

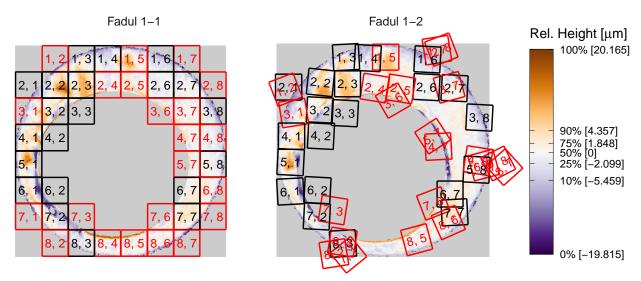


Figure 8: CMC results from a known match comparison under the initially proposed method

The CMCs determined under the High CMC method (i.e., the "high" CMCs) are show below. We can see that 40 out of the

cmcPlots\$highCMC

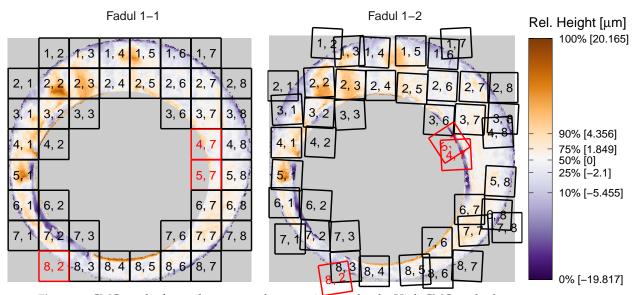


Figure 9: CMC results from a known match comparison under the High CMC method

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