



## COMPUTER SCIENCE 12B (SPRING TERM, 2017) ADVANCED PROGRAMMING TECHNIQUES

### PROGRAMMING ASSIGNMENT 5

**Due: March 27<sup>th</sup> at 11:55pm**

#### Stable marriage

This program will give you practice with a complex data structure. You are going to write a program that solves a classic computer science problem known as the stable marriage problem. The input file is divided into men and women and the program tries to pair them up so as to generate as many marriages as possible that are all stable. A set of marriages is unstable if you can find a man and a woman who would rather be married to each other than to their spouses (in which case, the two would be inclined to divorce their spouses and marry each other).

The input file for the program will list all of the men, one per line, followed by an input line with just the word “END” on it, followed by all of the women, one per line, followed by another input line with just the word “END” on it. The men and women are numbered by their position in the input file. To make this easier, we have numbered starting at 0 (the first man is #0, the second man is #1, and so on; the first woman is #0, the second woman is #1, and so on). Each input line (except the two lines with “END”) has a name followed by a colon followed by a list of integers. The integers are the preferences for this particular person. For example, the following input line in the men's section:

```
Joe: 9 7 34 8 19 21 32 5 28 6 31 15 17 24
```

indicates that the person is named “Joe” and that his first choice for marriage is woman #9, his second choice is woman #7, and so on. Any women not listed are considered unacceptable to Joe. The data file has been purged of any impossible pairings where one person is interested in the other, but the other considers that person unacceptable. Thus, if a woman appears on Joe’s list, then Joe is acceptable to that woman.

There are many ways to approach the stable marriage problem. You are to implement a specific algorithm described below. This is the basic outline:

```
set each person to be free
while (some man m with a nonempty preference list is free) {
    w = first woman on m's list;
    if (some man p is engaged to w) {
        set p to be free
    }
    set m and w to be engaged to each other
    for (each successor q of m on w's list) {
        delete w from q's preference list
    }
}
```

```

    delete q from w's preference list
  }
}

```

Consider, for example, the following short input:

Man 0: 3 0 1 2	Woman 0: 3 0 2 1
Man 1: 1 2 0 3	Woman 1: 0 2 1 3
Man 2: 1 3 2 3	Woman 2: 0 1 2 3
Man 3: 2 0 3 1	Woman 3: 3 0 2 1

It doesn't matter where we start, so suppose we start with man 0. We engage him to woman 3 (the first choice on his list). Men 2 and 1 appear after man 0 in woman 3's list. Thus, we delete those connections.

Man 0: 3 0 1 2	Woman 0: 3 0 2 1	Man 0 and Woman 3 engaged
Man 1: 1 2 0	Woman 1: 0 2 1 3	
Man 2: 1 2 0	Woman 2: 0 1 2 3	
Man 3: 2 0 3 1	Woman 3: 3 0	

Notice that three things have changed: the list for man 1, the list for man 2 and the list for woman 3.

Suppose we next go to man 1. We engage him to woman 1. Man 3 appears after man 1 on woman 1's list, so we have to delete that connection, obtaining:

Man 0: 3 0 1 2	Woman 0: 3 0 2 1	Man 0 and Woman 3 engaged
Man 1: 1 2 0	Woman 1: 0 2 1	Man 1 and Woman 1 engaged
Man 2: 1 2 0	Woman 2: 0 1 2 3	
Man 3: 2 0 3	Woman 3: 3 0	

Notice that two things have changed: the list for man 3 and the list for woman 1.

Suppose we next go to man 2. We engage him to woman 1, which requires breaking woman 1's engagement to man 1 (making man 1 again available). Man 1 appears after man 2 on woman 1's list, so we break that connection, obtaining:

Man 0: 3 0 1 2	Woman 0: 3 0 2 1	Man 0 and Woman 3 engaged
Man 1: 2 0	Woman 1: 0 2	
Man 2: 1 2 0	Woman 2: 0 1 2 3	Man 2 and Woman 1 engaged
Man 3: 2 0 3	Woman 3: 3 0	

Suppose we next go to man 3. We engage him to woman 2. Nobody appears on woman 2's list after man 3, so we don't have to remove any connections:

Man 0: 3 0 1 2	Woman 0: 3 0 2 1	Man 0 and Woman 3 engaged
Man 1: 2 0	Woman 1: 0 2	
Man 2: 1 2 0	Woman 2: 0 1 2 3	Man 2 and Woman 1 engaged
Man 3: 2 0 3	Woman 3: 3 0	Man 3 and Woman 2 engaged

Now we go back to man 1 (because he's still free). We engage him to woman 2, which requires breaking woman 2's engagement to man 3 (making man 3 again available). Men 2 and 3 appear after man 1 on woman 2's list, so we break those connections, obtaining:

Man 0: 3 0 1 2	Woman 0: 3 0 2 1	Man 0 and Woman 3 engaged
Man 1: 2 0	Woman 1: 0 2	Man 1 and Woman 2 engaged
Man 2: 1 0	Woman 2: 0 1	Man 2 and Woman 1 engaged
Man 3: 0 3	Woman 3: 3 0	

Finally, the last man is man 3. We engage him to woman 0. We could actually stop at this point, but according to the algorithm, we should notice that men, 0, 2, and 1 all appear after man 3 on woman 0's list, so we break those connections:

Man 0: 3 1 2	Woman 0: 3	Man 0 and Woman 3 engaged
Man 1: 2	Woman 1: 0 2	Man 1 and Woman 2 engaged
Man 2: 1	Woman 2: 0 1	Man 2 and Woman 1 engaged
Man 3: 0 3	Woman 3: 3 0	Man 3 and Woman 0 engaged

This, then, is our stable marriage solution.

An interesting property of this simple stable marriage algorithm is that it favors one group over the other. The approach above favors the men at the expense of the women. In fact, the final result will give each man his best possible match for stable marriage situations, and will give each woman her worst possible match. But there is no reason that the algorithm can't be reversed with the women being favored over the men (just reversing the roles in the algorithm above).

In your program you should run the above algorithm twice, once favoring the men and once favoring the women.

Apart from implementing the above algorithm, your program will also report in a column called "Choice" the relative position of the chosen partner in the original preference list and you must report the average of the choice column at the end of each sublist. For example, you should have the following line of output for the result that favors the men:

Name	Choice	Partner
-----		
William	6	Rachana
Ted	5	Rob
Mean choice = 5.5		

This indicates that William is paired with Rachana, and that Rachana was 6th on William's original list. The result that favors the women should have this line of output:

Name	Choice	Partner
-----		
Caroline	19	William

This indicates that William is paired with Caroline, and that William was 19th on Caroline's original list.

The stable marriage algorithm always converges on an answer, but it is possible that some people will end up without being paired (this is inevitable in the large sample input file where there are 40 men and 35 women). Remember that the original algorithm terminates when there are no men left who are free and have a nonempty preference list. People are unpaired in the final result if they run out of choices on their preference lists. Your program should detect this case and report it like that:

Name	Choice	Partner
-----		
William	--	nobody

Be careful not to report a "choice" value for these people and don't include them in the calculation of the overall choice value.

### General Guidelines:

Two test files are available on LATTE. File `short.dat` has a small set of men/women and you can use it to test your program. When the algorithm runs on this file it gives a mean choice of 1.5 when men are favored and 1.75 when women are favor. Use these numbers to test the correctness of your code. You should also make sure your program runs with the larger file `stable.dat` (that's the one the TAs will use for testing your program).

You should create a class the represents a person (man or woman). Among other things, a person has a name, marriage preferences and eventually a partner.

Also your implementation of the stable marriage algorithm should be part of your client program. That program should ask the user for the input file, read the data, execute the algorithm and print the results in the format specified above. You should break your client program into methods (at least 3: read input/execute algo/print output results).

You will be graded on correctness and programming style including the use of good variable names, comments on each class and each method, using local variables when possible, correct use of generics and the other standard style guidelines (constants, encapsulation, etc).

**Big-O problems (please write your answer in a text file to submit with your code)**

Give a big-O characterization, in terms of  $n$ , of the running time of the following algorithms:

**Algorithm A**

Input: An array A storing  $n \geq 1$  integers

Output: The sum of the elements in A

```
s = A[0]
for i = 1 to n - 1{
    s = s + A[i]
}
return s
```

**Algorithm B**

Input: An array A storing  $n \geq 1$  integers

Output: The sum of the elements at even cells in A

```
s = A[0]
for i = 2 to n - 1 by increments of 2{
    s = s + A[i]
}
return s
```

**Algorithm C**

Input: An array A storing  $n \geq 1$  integers

Output: The sum of the prefix sums in A

```
s = 0
for i = 0 to n - 1{
    s = s + A[0]
    for j = 1 to i{
        s = s + A[j]
    }
}
return s
```

**Algorithm D**

Input: An array A storing  $n \geq 1$  integers

Output: The sum of the prefix sums in A

```
s = A[0]
t = s
```

```

for i = 1 to n - 1{
    s = s + A[i]
    t = t + s
}
return t

```

### Algorithm E

Input: Arrays A and B each storing  $n \geq 1$  integers

Output: The number of elements in B equal to the sum of prefix sums in A

```

c = 0
for i = 0 to n-1{
    s = 0
    for j = 0 to n-1{
        s = s+A[0]
        for k = 1 to j{
            s = s+A[k]
        }
        if B[i] = s then
            c = c+1
    }
}
return c

```

### Submission:

Your Java source code should be submitted via Latte the day it is due. For late policy check the syllabus.

### Grading:

You will be graded on

- **External Correctness:** The output of your program should match exactly what is expected. Programs that do not compile will not receive points for external correctness.
- **Internal Correctness:** Your source code should follow the stylistic guidelines shown in class. Also, remember to include the comment header at the beginning of your program.
- **One-on-one interactive grading:** By the end of the day that the assignment is due, please make an appointment with your TA for an interactive 10-15 minute grading session. You will receive an email notifying you of the name of the TA who has been assigned to you for this assignment with further instructions on setting up the appointment. (You will be meeting with a different TA for each assignment). One-on-one interactive grading will help you improve your programming skills and avoid repeating mistakes from one assignment to the next.