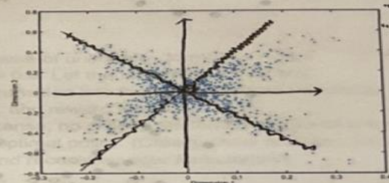
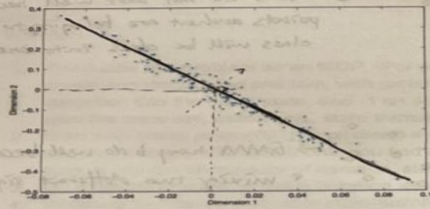


1. You have a language with three symbols A, B and C. The probability of observing A is 50% while that of observing B and C is 25% each. Design an appropriate encoding for this language. What is the entropy of this signal in bits?

2. Show that the K-means procedure can be viewed as a special case of the EM algorithm applied to an appropriate mixture of Gaussian densities model.

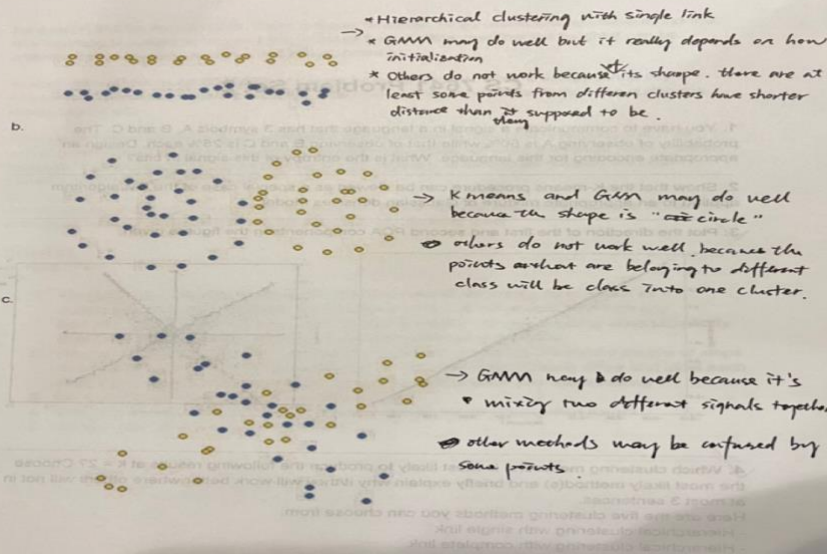
3. Plot the direction of the first and second PCA components in the figures given.



4. Which clustering method(s) is most likely to produce the following results at $k=2$? Choose the most likely method(s) and briefly explain why it/they will work better where others will not in at most 3 sentences.

Here are the five clustering methods you can choose from:

- Hierarchical clustering with single link
- Hierarchical clustering with complete link
- Hierarchical clustering with average link
- K-means
- EM



Total exploration: $Q(s, a_1) = 2.5$
 $Q(s, a_2) = 2.75$

Greedy exploration: $Q(s, a_1) = 2.5$
 $Q(s, a_2) = 3$

6. Use the Bellman equation to calculate $Q(s, a_1)$ and $Q(s, a_2)$ the scenario shown in the figure. Consider two different policies:

- Total exploration: All actions are chosen with equal probability.
- Greedy exploitation: The agent always chooses the best action.

Note that the rewards/next states are stochastic for the actions a_1' , a_2' and a_3' . Assume that the probabilities for the outcome of these actions are all equal. Assume that reward gathering / decision making stops at the empty circles at the bottom.

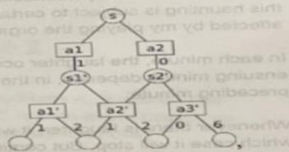


Figure 1.

7. Consider the following simple grid-world problem. (Actions are N, S, E, W and are deterministic.) Our goal is to maximize the following reward: