STAT 471: Homework 1

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Due: September 15, 2021 at 11:59pm

Contents

In	structions	2
	Setup	2
	Collaboration	2
	Writeup	
	Programming	
	Grading	
	Submission	
C	se study: Major League Baseball	3
1	Wrangle (30 points for correctness; 5 points for presentation)	3
	1.1 Import (5 points)	:
	1.2 Tidy (15 points)	
	1.3 Quality control (10 points)	ŀ
2	Explore (40 points for correctness; 7 points for presentation)	6
	2.1 Payroll across years (15 points)	6
	2.2 Win percentage across years (10 points)	
	2.3 Win percentage versus payroll (10 points)	
	2.4 Team efficiency (5 points)	
2	Model (15 points for correctness; 3 points for presentation)	14
_	3.1 Running a linear regression (5 points)	
	3.2 Comparing Oakland Athletics to the linear trend (10 points)	

Instructions

Setup

Pull the latest version of this assignment from Github and set your working directory to stat-471-fall-2021/homework-1. Consult the getting started guide if you need to brush up on R or Git.

Collaboration

The collaboration policy is as stated on the Syllabus:

"Students are permitted to work together on homework assignments, but solutions must be written up and submitted individually. Students must disclose any sources of assistance they received; furthermore, they are prohibited from verbatim copying from any source and from consulting solutions to problems that may be available online and/or from past iterations of the course."

In accordance with this policy,

Please list anyone you discussed this homework with: Alex Chen

Please list what external references you consulted (e.g. articles, books, or websites): Stack Overflow, Tidyverse documentation

Writeup

Use this document as a starting point for your writeup, adding your solutions after "Solution". Add your R code using code chunks and add your text answers using **bold text**. Consult the preparing reports guide for guidance on compilation, creation of figures and tables, and presentation quality.

Programming

The tidyverse paradigm for data wrangling, manipulation, and visualization is strongly encouraged, but points will not be deducted for using base R.

Grading

The point value for each problem sub-part is indicated. Additionally, the presentation quality of the solution for each problem (as exemplified by the guidelines in Section 3 of the preparing reports guide will be evaluated on a per-problem basis (e.g. in this homework, there are three problems). There are 100 points possible on this homework, 85 of which are for correctness and 15 of which are for presentation.

Submission

Compile your writeup to PDF and submit to Gradescope.

Case study: Major League Baseball

What is the relationship between payroll and wins among Major League Baseball (MLB) teams? In this homework, we'll find out by wrangling, exploring, and modeling the dataset in data/MLPayData_Total.csv, which contains the winning records and the payroll data of all 30 MLB teams from 1998 to 2014.

The dataset has the following variables:

- payroll: total team payroll (in billions of dollars) over the 17-year period
- avgwin: the aggregated win percentage over the 17-year period
- Team.name.2014: the name of the team
- p1998, ..., p2014: payroll for each year (in millions of dollars)
- X1998, ..., X2014: number of wins for each year
- X1998.pct, ..., X2014.pct: win percentage for each year

We'll need to use the following R packages:

```
library(tidyverse)  # tidyverse
library(ggrepel)  # for scatter plot point labels

## Warning: package 'ggrepel' was built under R version 4.1.1

library(kableExtra) # for printing tables

## Warning: package 'kableExtra' was built under R version 4.1.1

library(cowplot) # for side by side plots

## Warning: package 'cowplot' was built under R version 4.1.1
```

1 Wrangle (30 points for correctness; 5 points for presentation)

1.1 Import (5 points)

- Import the data into a tibble called mlb_raw and print it.
- How many rows and columns does the data have?
- Does this match up with the data description given above?

[Hint: If your working directory is stat-471-fall-2021/homework/homework-1, then you can use a *relative* path to access the data at ../../data/MLPayData_Total.csv.]

```
mlb_raw <- read_csv(file = "../../data/MLPayData_Total.csv") # Importing the csv
mlb_raw</pre>
```

```
## # A tibble: 30 x 54
##
      payroll avgwin Team.name.2014 p1998 p1999 p2000 p2001 p2002 p2003 p2004 p2005
##
        <dbl>
               <dbl> <chr>
                                     <dbl> <
##
        1.12
                                           70.5
                                                  81.0 81.2 103.
                                                                      80.6
                                                                          70.2
   1
               0.490 Arizona Diamo~
                                      31.6
##
    2
        1.38
               0.553 Atlanta Braves
                                      61.7
                                            74.9
                                                   84.5
                                                         91.9
                                                               93.5 106.
                                                                            88.5
##
    3
        1.16
               0.454 Baltimore Ori~
                                      71.9
                                            72.2
                                                   81.4
                                                        72.4
                                                               60.5
                                                                     73.9
                                                                            51.2
##
    4
        1.97
               0.549 Boston Red Sox
                                      59.5
                                            71.7
                                                   77.9 110.
                                                              108.
                                                                      99.9 125.
##
    5
        1.46
               0.474 Chicago Cubs
                                      49.8
                                            42.1
                                                   60.5
                                                         64.0
                                                               75.7
                                                                     79.9
##
        1.32
               0.511 Chicago White~
                                      35.2
                                            24.5
                                                   31.1
                                                         62.4
                                                               57.1
    6
                                                                     51.0
                                                                            65.2
##
    7
        1.02
               0.486 Cincinnati Re~
                                      20.7
                                            73.3
                                                   46.9
                                                         45.2
                                                               45.1
                                                                     59.4
                                                                            43.1
##
                                                               78.9
    8
        0.999
               0.496 Cleveland Ind~
                                      59.5
                                            54.4
                                                  75.9
                                                         92.0
                                                                     48.6
                                                                            34.6
##
    9
        1.03
               0.463 Colorado Rock~
                                      47.7
                                            55.4
                                                  61.1
                                                         71.1
                                                               56.9
                                                                     67.2
               0.482 Detroit Tigers 19.2 35.0 58.3 49.8 55.0 49.2 46.4
        1.43
## # ... with 20 more rows, and 43 more variables: p2006 <dbl>, p2007 <dbl>,
       p2008 <dbl>, p2009 <dbl>, p2010 <dbl>, p2011 <dbl>, p2012 <dbl>,
```

```
## # p2013 <dbl>, p2014 <dbl>, X2014 <dbl>, X2013 <dbl>, X2012 <dbl>,
## # X2011 <dbl>, X2010 <dbl>, X2009 <dbl>, X2008 <dbl>, X2007 <dbl>,
## # X2006 <dbl>, X2005 <dbl>, X2004 <dbl>, X2003 <dbl>, X2002 <dbl>,
## # X2001 <dbl>, X2000 <dbl>, X1999 <dbl>, X1998 <dbl>, X2014.pct <dbl>,
## # X2013.pct <dbl>, X2012.pct <dbl>, X2011.pct <dbl>, X2010.pct <dbl>, ...
```

The data has 30 rows for 54 columns, which does match up with the data description. There are 30 teams and 54 columns described $(3 + 3 \times 17)$.

1.2 Tidy (15 points)

The raw data are in a messy format: Some of the column names are hard to interpret, we have data from different years in the same row, and both year-by-year and aggregate data are present.

- Tidy the data into two separate tibbles: one called mlb_aggregate containing the aggregate data and another called mlb_yearly containing the year-by-year data. mlb_aggregate should contain columns named team, payroll_aggregate, pct_wins_aggregate and mlb_yearly should contain columns named team, year, payroll, pct_wins, num_wins. Comment your code to explain each step.
- Print these two tibbles. How many rows do mlb_aggregate and mlb_yearly contain, and why?

[Hint: For mlb_yearly, the main challenge is to extract the information from the column names. To do so, you can pivot_longer all these column names into one column called column_name, separate this column into three called prefix, year, suffix, mutate prefix and suffix into a a new column called tidy_col_name that takes values payroll, num_wins, or pct_wins, and then pivot_wider to make the entries of tidy_col_name into column names.]

```
mlb_aggregate <- mlb_raw %>% # Creating the mlb_aggregate
  select("Team.name.2014", "payroll", "avgwin") %>% #Selecting the relevant columns
  rename("team" = "Team.name.2014", "payroll_aggregate" = "payroll",
         "pct wins aggregate" = "avgwin") #Renaming the columns
mlb yearly <- mlb raw %>% # Creating mlb yearly
  select(!c("payroll", "avgwin")) %>% # Selecting the columns in the new tibble
  rename("team" = "Team.name.2014") %>% # Renaming the columns
  pivot_longer(!"team", names_to = "col_name", # Pivoting longer the non-team columns
               values to = "values") %>%
  separate("col_name", c("prefix", "year", "suffix"), c(1, 5)) %% #Separating the name
  mutate("tidy_col_name" = # Recoding the prefix/suffix combinations to be meaningful
          recode(paste0(prefix,suffix), p = "payroll", X = "num_wins",
                 X.pct = "pct_wins"),
         .keep = "unused") %>% #Keep only the unused columns
  pivot wider(names from = "tidy col name", # Pivoting wider with the new column names
              values_from = "values")
```

mlb_aggregate

```
## # A tibble: 30 x 3
##
      team
                           payroll_aggregate pct_wins_aggregate
##
      <chr>
                                        <dbl>
                                                           <dbl>
##
   1 Arizona Diamondbacks
                                        1.12
                                                           0.490
## 2 Atlanta Braves
                                        1.38
                                                           0.553
## 3 Baltimore Orioles
                                        1.16
                                                           0.454
## 4 Boston Red Sox
                                        1.97
                                                           0.549
## 5 Chicago Cubs
                                        1.46
                                                           0.474
## 6 Chicago White Sox
                                        1.32
                                                           0.511
## 7 Cincinnati Reds
                                        1.02
                                                           0.486
## 8 Cleveland Indians
                                        0.999
                                                           0.496
```

```
## 9 Colorado Rockies 1.03 0.463
## 10 Detroit Tigers 1.43 0.482
## # ... with 20 more rows
```

mlb_yearly

```
## # A tibble: 510 x 5
##
      team
                           year
                                 payroll num wins pct wins
##
      <chr>>
                                    <dbl>
                                             <dbl>
                                                      <dbl>
                           <chr>
##
  1 Arizona Diamondbacks 1998
                                     31.6
                                                65
                                                      0.401
## 2 Arizona Diamondbacks 1999
                                               100
                                                      0.617
                                    70.5
## 3 Arizona Diamondbacks 2000
                                    81.0
                                                85
                                                      0.525
## 4 Arizona Diamondbacks 2001
                                    81.2
                                                92
                                                      0.568
## 5 Arizona Diamondbacks 2002
                                    103.
                                                98
                                                      0.605
## 6 Arizona Diamondbacks 2003
                                    80.6
                                                84
                                                      0.519
   7 Arizona Diamondbacks 2004
                                    70.2
                                                51
                                                      0.315
## 8 Arizona Diamondbacks 2005
                                                77
                                                      0.475
                                    63.0
## 9 Arizona Diamondbacks 2006
                                     59.7
                                                76
                                                      0.469
## 10 Arizona Diamondbacks 2007
                                     52.1
                                                90
                                                      0.556
## # ... with 500 more rows
```

mlb_aggregate contains 30 rows, because it is aggregating for each team over the entire seventeen year period. However, mlb_yearly has 510 rows because it is providing information for all 30 teams over each of the 17 years.

1.3 Quality control (10 points)

geom_point() +

theme_bw() + # Setting a nice theme

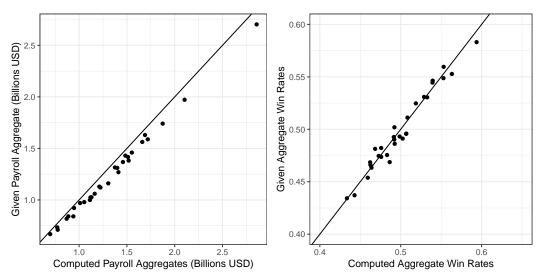
It's always a good idea to check whether a dataset is internally consistent. In this case, we are given both aggregated and yearly data, so we can check whether these match. To this end, carry out the following steps:

- Create a new tibble called mlb_aggregate_computed based on aggregating the data in mlb_yearly, containing columns named team, payroll_aggregate_computed, and pct_wins_aggregate_computed.
- Ideally, mlb_aggregate_computed would match mlb_aggregate. To check whether this is the case, join these two tibbles into mlb_aggregate_joined (which should have five columns: team, payroll_aggregate, pct_wins_aggregate, payroll_aggregate_computed, and pct_wins_aggregate_computed.)
- Create scatter plots of payroll_aggregate_computed versus payroll_aggregate and pct_wins_aggregate_computed versus pct_wins_aggregate, including a 45° line in each. Display these scatter plots side by side, and comment on the relationship between the computed and provided aggregate statistics.

labs(x = "Computed Payroll Aggregates (Billions USD)", # Adding informative axis labels

geom_abline(slope=1, intercept= 0) + #Adding the 45 degree line

```
y = "Given Payroll Aggregate (Billions USD)")
# Plotting the computed vs actual pct_win values
pct_wins_comparison <- ggplot(mlb_aggregate_joined,</pre>
                             aes(x= pct_wins_aggregate_computed,
                                 y = pct_wins_aggregate)) +
  geom_point() +
  geom_abline(slope=1, intercept= 0) + #Adding the 45 degree line
  theme bw() + # Setting a nice theme
  labs(x = "Computed Aggregate Win Rates", # Adding informative axis labels
       y = "Given Aggregate Win Rates") +
  scale_x_continuous(breaks = c(0.4, 0.5, 0.6), # Setting my own custom scales
                     limits = c(0.4, 0.65)) +
  scale_y_continuous(breaks = c(0.4, 0.45, 0.5, 0.55, 0.6),
                     limits = c(0.4, 0.6))
plot_grid(payroll_comparison, pct_wins_comparison, # Plotting the two graphs side by side
          align = "h")
```



These values tend to generally line up with one another. However, the computed payroll values slightly dip below those of the given values, which is likely due to rounding differnces.

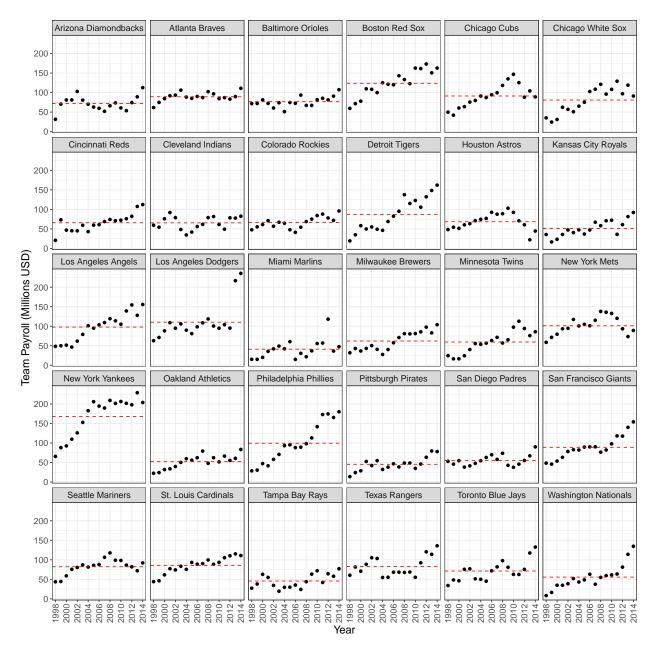
2 Explore (40 points for correctness; 7 points for presentation)

Now that the data are in tidy format, we can explore them by producing visualizations and summary statistics.

2.1 Payroll across years (15 points)

- Plot payroll as a function of year for each of the 30 teams, faceting the plot by team and adding a red dashed horizontal line for the mean payroll across years of each team.
- Using dplyr, identify the three teams with the greatest payroll_aggregate_computed, and print a table of these teams and their payroll_aggregate_computed.
- Using dplyr, identify the three teams with the greatest percentage increase in payroll from 1998 to 2014 (call it pct_increase), and print a table of these teams along with pct_increase as well as their payroll figures from 1998 and 2014.
- How are the metrics payroll_aggregate_computed and pct_increase reflected in the plot above, and how can we see that the two sets of teams identified above are the top three in terms of these metrics?

[Hint: To compute payroll increase, it's useful to pivot_wider the data back to a format where different years are in different columns. Use names_prefix = "payroll_ inside pivot_wider to deal with the fact column names cannot be numbers. To add different horizontal lines to different facets, see this webpage.]



The three teams with the greatest payroll:

Table 1: Teams with the highest aggregate payroll

Team	Computed Aggregate Payroll
New York Yankees Boston Red Sox	2.86 2.10
Los Angeles Dodgers	1.87

The three teams with the greatest percentage increases in payroll:

```
mlb yearly %>%
  # Get only the columns needed to find the greatest increase
  select(c(team, year, payroll)) %>%
  # Pivoting it wider to make it easier to calculate the increase
  pivot_wider(names_from = year, values_from = c(payroll), names_prefix = "payroll_") %>%
  mutate(pct_increase = #Calculating the increase
           (payroll_2004 - payroll_1998)/payroll_1998 * 100) %>%
  # Arranging the data from highest to lowest payroll increase
  arrange(desc(pct_increase)) %>%
  select(team, payroll_1998, payroll_2014, pct_increase) %>%
  rename(Team = team, "% Increase in Payroll" = pct_increase,
         "Payroll 1998 (Millions $)" = payroll_1998,
         "Payroll 2014 (Millions $)" = payroll_2014) %>%
  slice(1:3) %>% # Getting the top 3
  kable(format = "latex", row.names = NA,
       booktabs = TRUE, digits = 2,
        caption = "Teams and their payroll increase") %>%
  kable_styling( position = "center", latex_options = "HOLD_position")
```

Table 2: Teams and their payroll increase

Team	Payroll 1998 (Millions \$)	Payroll 2014 (Millions \$)	% Increase in Payroll
Washington Nationals	8.32	135	419
Philadelphia Phillies	28.62	180	226
New York Yankees	65.66	204	178

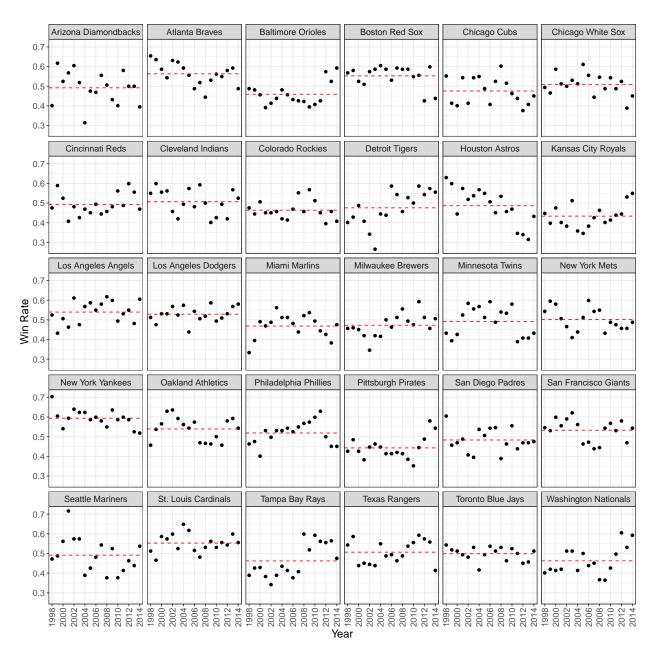
The payroll_aggregate_computed and pct_increase are reflected in the above plot by the red line (i.e mean payroll) and the trend of the dots, respectively. Mean payroll is just the aggregate payroll divided by seventeen. The trend of the dots is the literal increase in payroll value. We can see that the top three teams in payroll_aggregate_computed have the highest red line and the top three teams in pct_increase have the dots that increase the most.

2.2 Win percentage across years (10 points)

- Plot pct_wins as a function of year for each of the 30 teams, faceting the plot by team and adding a red dashed horizontal line for the average pct_wins across years of each team.
- Using dplyr, identify the three teams with the greatest pct_wins_aggregate and print a table of these teams along with pct_wins_aggregate.
- Using dplyr, identify the three teams with the most erratic pct_wins across years (as measured by the standard deviation, call it pct_wins_sd) and print a table of these teams along with pct_wins_sd.

• How are the metrics payroll_aggregate_computed and pct_wins_sd reflected in the plot above, and how can we see that the two sets of teams identified above are the top three in terms of these metrics?

```
mlb_average_winrate <- mlb_yearly %>% # Calculating the average win rate for each team
  group_by(team) %>%
  summarise(avg_winrate = mean(pct_wins), # The average win rate
            pct_wins_sd = sd(pct_wins)) # The sd of the win rates
ggplot(mlb_yearly, aes(x = year, y = pct_wins)) + # Plot the win rate by year
  geom_point() +
  scale_x_discrete(breaks=seq(1998, 2014, 2)) +
  facet_wrap(team ~ .) + # Facet this graph by teams
  # Add the dashed, red lines of the mean win rate to each graph
  geom_hline(mlb_average_winrate,
             mapping = aes(yintercept = avg_winrate), linetype='dashed', col = 'red') +
  theme_bw() +
  theme(axis.text.x = # A little theme working to make it better
    element_text(angle = 90, vjust = 0.5, hjust=.9),
    text = element_text(size = 14)) +
  labs(y = "Win Rate", x = "Year")
```



The three teams with the greatest win rate:

Table 3: Teams and their win rate

Team	Win Rate
New York Yankees St. Louis Cardinals Atlanta Brayes	0.58 0.56 0.55

The three teams with the most erratic win rate:

Table 4: Teams and the SD of their win rate

Team	SD of Win Rate
Houston Astros	0.09
Detroit Tigers	0.09
Seattle Mariners	0.09

The pct_wins_aggregate and pct_wins_sd are reflected in the plot above by the red line (i.e. mean win rate) and the movement of the dots, respectively. Mean win rate is just the aggregate payroll divided by seventeen. The movement of the dots is the literal variation in win rate We can see that the top three teams in pct_wins_aggregate have the highest red line and the top three teams in pct_wins_sd have the dots that vary the most.

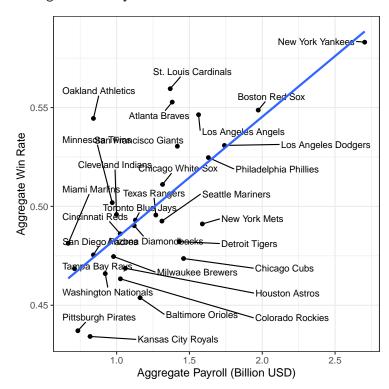
2.3 Win percentage versus payroll (10 points)

The analysis goal is to study the relationship between win percentage and payroll.

- Create a scatter plot of pct_wins versus payroll based on the aggregated data, labeling each point
 with the team name using geom_text_repel from the ggrepel package and adding the least squares
 line.
- Is the relationship between payroll and pct_wins positive or negative? Is this what you would expect, and why?

```
geom_smooth(method='lm', se= FALSE) + # Adding the least squares line
theme_bw() +
labs(x = "Aggregate Payroll (Billion USD)", y = "Aggregate Win Rate")
```

`geom_smooth()` using formula 'y ~ x'



The relationship between payroll and win_rate is positive, which makes sense as more money means better players and therefore more wins.

2.4 Team efficiency (5 points)

Define a team's *efficiency* as the ratio of the aggregate win percentage to the aggregate payroll—more efficient teams are those that win more with less money.

- Using dplyr, identify the three teams with the greatest efficiency, and print a table of these teams along with their efficiency, as well as their pct_wins_aggregate and payroll_aggregate.
- In what sense do these three teams appear efficient in the previous plot?

Side note: The movie "Moneyball" portrays "Oakland A's general manager Billy Beane's successful attempt to assemble a baseball team on a lean budget by employing computer-generated analysis to acquire new players."

```
mlb_aggregate <- mlb_aggregate %>%
  mutate(efficiency = pct_wins_aggregate/payroll_aggregate)
#Getting the three highest efficiency teams
mlb_aggregate %>%
  # Arrange them from highest to lowest aggregate payroll
  arrange(desc(efficiency)) %>%
  select(c("team", "efficiency")) %>%
  rename(Team = team, Efficiency = efficiency) %>%
  slice(1:3) %>% # Get the top 3
```

Table 5: Highest efficiency teams

Team	Efficiency
Miami Marlins	0.72
Tampa Bay Rays	0.66
Oakland Athletics	0.65

These are the teams with the highest win rate given their payrolls, so they will be in the top left of the scatter plot.

3 Model (15 points for correctness; 3 points for presentation)

Finally, we build a predictive model for pct_wins_aggregate in terms of payroll_aggregate using the aggregate data mlb_aggregate.

3.1 Running a linear regression (5 points)

- Run a linear regression of pct_wins_aggregate on payroll_aggregate and print the regression summary.
- What is the coefficient of payroll aggregate, and what is its interpretation?
- What fraction of the variation in pct_wins_aggregate is explained by payroll_aggregate?

```
lm_pctwins <- lm(mlb_aggregate, formula = pct_wins_aggregate~payroll_aggregate) #
summary(lm_pctwins)</pre>
```

```
##
## lm(formula = pct_wins_aggregate ~ payroll_aggregate, data = mlb_aggregate)
##
## Residuals:
       Min
                 1Q
                     Median
                                   30
                                           Max
## -0.04003 -0.01749 0.00094 0.01095 0.07030
##
## Coefficients:
                    Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                      0.4226
                                 0.0153
                                          27.56 < 2e-16 ***
                      0.0614
## payroll_aggregate
                                           5.23 1.5e-05 ***
                                 0.0117
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.027 on 28 degrees of freedom
## Multiple R-squared: 0.494, Adjusted R-squared: 0.476
## F-statistic: 27.4 on 1 and 28 DF, p-value: 1.47e-05
```

The coefficient is 0.0614. This means that for every billion dollars spent on the team, the winrate increased by 0.0614. Only 0.494 of the variation is explained.

3.2 Comparing Oakland Athletics to the linear trend (10 points)

- Given their payroll, what is the linear regression prediction for the winning percentage of the Oakland Athletics? What was their actual winning percentage?
- Now run a linear regression of payroll_aggregate on pct_wins_aggregate. What is the linear regression prediction for the payroll_aggregate of the Oakland Athletics? What was their actual payroll?

```
oakland_athletics <- mlb_aggregate %>%
  filter(team == "Oakland Athletics")
predict(lm_pctwins, oakland_athletics)
##
       1
## 0.474
The predicted win rate is 0.474, while their actual win rate was 0.545.
lm_payroll <- lm(formula = payroll_aggregate~pct_wins_aggregate, data =mlb_aggregate)</pre>
summary(lm_payroll)
##
## Call:
## lm(formula = payroll_aggregate ~ pct_wins_aggregate, data = mlb_aggregate)
##
## Residuals:
      Min
##
                1Q Median
                                30
                                       Max
## -0.7674 -0.1871 -0.0371 0.1663
                                   0.7843
##
## Coefficients:
                      Estimate Std. Error t value Pr(>|t|)
##
## (Intercept)
                         -2.78
                                     0.77
                                            -3.61
                                                    0.0012 **
                          8.06
## pct_wins_aggregate
                                     1.54
                                             5.23 1.5e-05 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.309 on 28 degrees of freedom
## Multiple R-squared: 0.494, Adjusted R-squared: 0.476
## F-statistic: 27.4 on 1 and 28 DF, p-value: 1.47e-05
```

```
## 1
## 1.61
```

predict(lm_payroll, oakland_athletics)

The predicted payroll of the Oakland A's is \$1.61 billion, while the actual is \$0.841 million.