Unit 3 Lecture 3: Ridge regression

October 12, 2021

NOTE: This R demo has been updated since it was presented in class on October 12. Through the use of the glmnetUtils package, it is no longer necessary to separately construct X and Y to pass into cv.glmnet, or to scale the X matrix manually, or to remove the intercept manually. You can use cv.glmnet in much the same way you have been using lm and glm: by specifying a formula and supplying a data frame.

In this R demo, we will learn about the glmnet and glmnetUtils packages and how to run a cross-validated ridge regression using the cv.glmnet() function.

First, let's install the glmnet and glmnetUtils packages:

```
# install.packages("glmnet")
# install.packages("glmnetUtils")
```

Next, we load the glmnetUtils package:

```
library(glmnetUtils)
```

Let's also source a function called plot_glmnet to help us plot our results:

```
source("../../functions/plot_glmnet.R")
```

We will be applying ridge regression to study the effect of 97 socioeconomic factors on violent crimes per capita based on data from 90 communities in Florida:

```
crime_data = read_csv("../../data/CrimeData_FL.csv")
crime_data
```

```
## # A tibble: 90 x 98
##
      population household.size race.pctblack race.pctwhite race.pctasian
##
           <dbl>
                           <dbl>
                                          <dbl>
                                                         <dbl>
                                                                        <dbl>
                                                          83.9
##
    1
           16023
                            2.63
                                          13.8
                                                                         1.42
##
    2
           29721
                            2.34
                                           3.52
                                                          95.1
                                                                         1.03
##
   3
           10205
                            2.46
                                           1.06
                                                          97.4
                                                                         1.04
##
          124773
                            2.47
                                                          68.2
                                                                         1.75
   4
                                          29.1
##
   5
           13024
                            2.25
                                          31.3
                                                          67.2
                                                                         0.5
##
   6
          280015
                                          25.0
                                                          70.9
                                                                         1.35
                            2.44
##
   7
           79443
                            2.94
                                                          93.1
                                                                         2.12
                                           3.48
           16444
##
   8
                            2.57
                                           5.38
                                                          91.2
                                                                         1.96
##
   9
           46194
                            2.28
                                          20.1
                                                          77.7
                                                                         0.63
                            2.17
                                                                         0.58
## 10
           14044
                                           0.48
                                                          98.3
## # ... with 80 more rows, and 93 more variables: race.pcthisp <dbl>,
       age.pct12to21 <dbl>, age.pct12to29 <dbl>, age.pct16to24 <dbl>,
## #
```

```
## # age.pct65up <dbl>, pct.urban <dbl>, med.income <dbl>, pct.wage.inc <dbl>,
## # pct.farmself.inc <dbl>, pct.inv.inc <dbl>, pct.socsec.inc <dbl>,
## # pct.pubasst.inc <dbl>, pct.retire <dbl>, med.family.inc <dbl>,
## # percap.inc <dbl>, white.percap <dbl>, black.percap <dbl>,
## # indian.percap <dbl>, asian.percap <dbl>, hisp.percap <dbl>, ...
```

Let's split the data into training and testing, as usual:

```
set.seed(471)
train_samples = sample(1:nrow(crime_data), 0.8*nrow(crime_data))
crime_data_train = crime_data %>% filter(row_number() %in% train_samples)
crime_data_test = crime_data %>% filter(!(row_number() %in% train_samples))
```

Running a cross-validated ridge regression

We call cv.glmnet on crime_data_train:

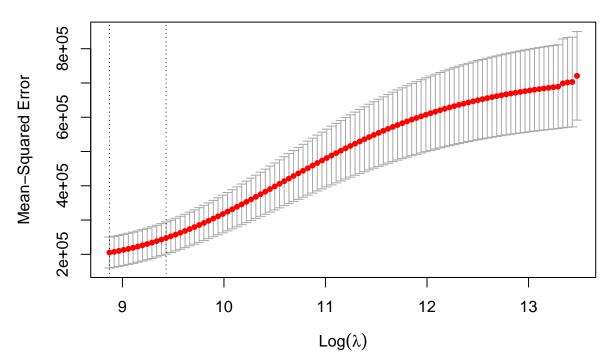
A few things to note:

- the sequence of penalty parameters is automatically chosen for you
- alpha = 0 means "ridge regression" (we'll discuss other values of alpha next lecture)
- nfolds specifies the number of folds for cross-validation
- ullet the columns of the matrix X are being standardized for you behind the scenes; there is no need to standardize yourself

Inspecting the results

The glmnet package has a very nice plot function to produce the CV plot:

plot(ridge_fit)



The ridge_fit object has several fields with information about the fit:

lambda sequence head(ridge_fit\$lambda)

[1] 713062.9 680653.1 649716.3 620185.7 591997.3 565090.1

CV estimates head(ridge_fit\$cvm)

[1] 720856.9 702831.8 701779.3 698965.2 689312.4 687654.4

CV standard errors head(ridge_fit\$cvsd)

[1] 129230.7 130921.2 131034.4 129625.3 122211.3 121927.5

lambda achieving minimum CV error ridge_fit\$lambda.min

[1] 7130.629

lambda based on one-standard-error rule ridge_fit\$lambda.1se

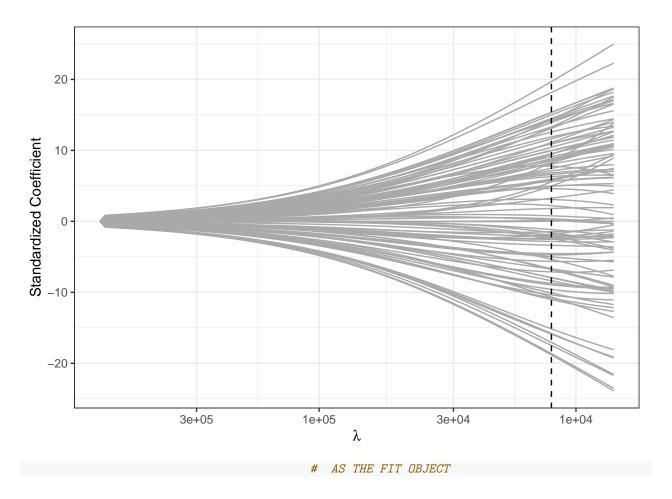
[1] 12460.98

To get the fitted coefficients at the selected value of lambda:

```
coef(ridge_fit, s = "lambda.1se") %>% head()
## 6 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                  4.335514e+03
## population
                  1.020056e-04
## household.size 2.871272e+00
## race.pctblack
                 1.172688e+00
## race.pctwhite -1.201426e+00
## race.pctasian -7.830098e+00
coef(ridge_fit, s = "lambda.min") %>% head()
## 6 x 1 sparse Matrix of class "dgCMatrix"
##
## (Intercept)
                  5.226134e+03
## population
                  1.367863e-04
## household.size 1.337954e+00
## race.pctblack
                 1.424616e+00
## race.pctwhite -1.464308e+00
## race.pctasian -1.131950e+01
```

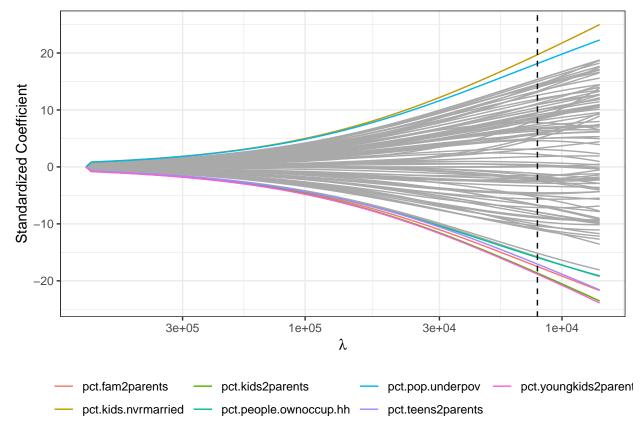
To visualize the fitted coefficients as a function of lambda, we can make a plot of the coefficients like we saw in class. To do this, we can use the plot_glmnet function, which by default shows a dashed line at the lambda value chosen using the one-standard-error rule:

```
plot_glmnet(ridge_fit, crime_data_train) # NOTE: MUST PASS IN THE DATA AS WELL
```



If we want to annotate the features with the top few coefficients, we can use the **features_to_plot** argument:

plot_glmnet(ridge_fit, crime_data_train, features_to_plot = 7)



To interpret these coefficient estimates, recall that they are for the *standardized* features.

Making predictions

To make predictions on the test data, we can use the predict function (which we've seen before):

Ridge logistic regression

[1] 397.7994

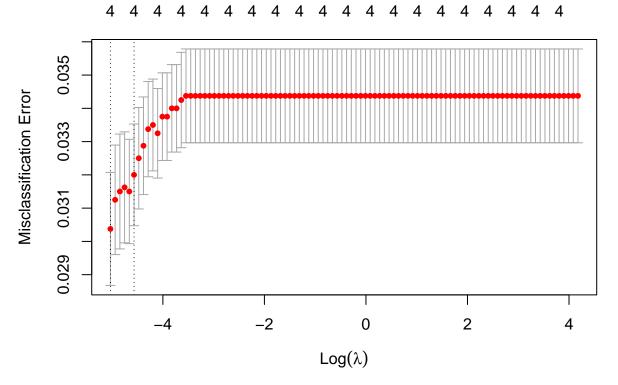
We can also run a ridge-penalized logistic regression. Let's try it out on default_data.

```
# load data, convert default to binary
default_data = ISLR2::Default %>%
    as_tibble() %>%
    mutate(default = as.numeric(default == "Yes"))
# split into train and test
set.seed(471)
train_samples = sample(1:nrow(default_data), 0.8*nrow(default_data))
default_train = default_data %>% filter(row_number() %in% train_samples)
default_test = default_data %>% filter(!(row_number() %in% train_samples))
```

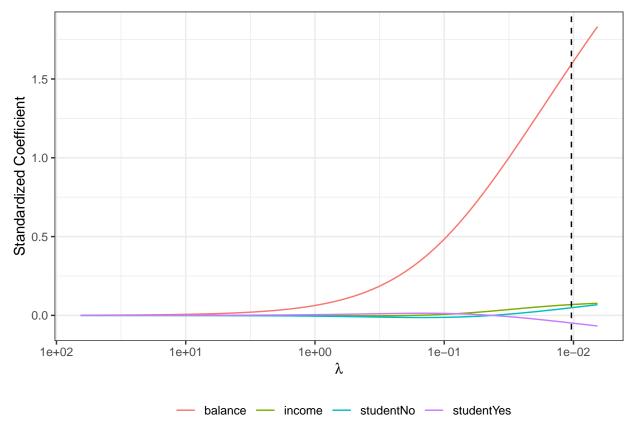
To run the logistic ridge regression, we call cv.glmnet as before, adding the argument family = binomial to specify that we want to do a logistic regression and the argument type.measure = "class: to specify that we want to use the misclassification error during cross-validation.

We can then take a look at the CV plot and the trace plot as before:

```
plot(ridge_fit)
```



```
plot_glmnet(ridge_fit, default_train, features_to_plot = 4)
```



To predict using the fitted model, we can use the predict function again, this time specifying type = "response" to get the predictions on the probability scale (as opposed to the log-odds scale).

```
## [1] 0.0006226396 0.0289927850 0.0022106111 0.0034241229 0.0018848093 ## [6] 0.0065551004
```

We can threshold the probabilities to get binary predictions as we did with regular logistic regression.