Longest Zig-Zag Subsequence

Filename: zigzag

A sequence of numbers is called a zig-zag sequence if the differences between successive numbers strictly alternate between positive and negative. The first difference (if one exists) may be either positive or negative. A sequence with fewer than two elements is trivially a zig-zag sequence. For example, 1,7,4,9,2,5 is a zig-zag sequence because the differences (6,-3,5,-7,3) are alternately positive and negative. In contrast, 1,4,7,2,5 and 1,7,4,5,5 are not zig-zag sequences, the first because its first two differences are positive and the second because its last difference is zero. Given a sequence of integers, sequence, calculate the length of the longest subsequence of sequence that is a zig-zag sequence. A subsequence is obtained by deleting some number of elements (possibly zero) from the original sequence, leaving the remaining elements in their original order.

The Input:

First line of the input contains T the number of test cases. First line of each test case contains N the number of integers in the sequence. Second line contains N integers separated by a single space. N is between 1 and 50 inclusive. Each of the integers in the sequence will fit into signed 32 bit integers.

The Output:

For each test case output the length of the longest subsequence of the input sequence that is a zig-zag sequence.

Sample Input	Sample Output
8	6
6	7
1 7 4 9 2 5	2
10	2
1 17 5 10 13 15 10 5 16 8	1
2	1
10 20	2
2	3
20 10	
2	
20 20	
1	
44	
9	
1 2 3 4 5 6 7 8 9	
9	
10 9 8 7 6 7 8 9 10	